

1 **Retrieval of aerosol optical depth from surface solar radiation measurements using machine**
2 **learning algorithms, nonlinear regression and a radiative transfer based look-up table**

3 **J. Huttunen^{1,2}, H. Kokkola¹, T. Mielonen¹, M. E. J. Mononen³, A. Lipponen^{1,2}, J. Reunanen⁴, A. V.**
4 **Lindfors¹, S. Mikkonen², K. E. J. Lehtinen^{1,2}, N. Kouremeti^{5,6}, A. Bais⁶, H. Niska⁷ and A. Arola¹**

5 [1]{Finnish Meteorological Institute (FMI), Atmospheric Research Centre of Eastern Finland, Kuopio,
6 Finland.}

7 [2]{Department of Applied Physics, University of Eastern Finland, Kuopio, Finland.}

8 [3]{Kuopio, Finland.}

9 [4]{Tomaattinen Oy, Helsinki, Finland.}

10 [5] {Physikalisch-Meteorologisches Observatorium Davos, Dorfstrasse 33, CH-7260 Davos Dorf,
11 Switzerland.}

12 [6] {Aristotle University of Thessaloniki, Laboratory of Atmospheric Physics, Thessaloniki, 54124,
13 Greece.}

14 [7]{Department of Environmental and Biological Sciences, University of Eastern Finland, Kuopio,
15 Finland.}

16 Corresponding author: J. Huttunen, Finnish Meteorological Institute (FMI), Kuopio Unit, P.O.
17 Box 1627, FI-70211 Kuopio, Finland. (jani.huttunen@fmi.fi)

18 Key points:

19 -Machine learning methods can produce very good aerosol optical depth estimates from surface solar
20 radiation data

21 -These tools have the potential to be used to retrieve long aerosol optical depth time series from surface
22 solar radiation measurements

23

24 **Abstract**

25 In order to have a good estimate of the current forcing by anthropogenic aerosols knowledge on past
26 aerosol levels is needed. Aerosol optical depth (AOD) is a good measure for aerosol loading. However,
27 dedicated measurements of AOD are only available from 1990's onward. One option to lengthen the
28 AOD time series beyond 1990's is to retrieve AOD from surface solar radiation (SSR) measurements
29 done with pyranometers. In this work, we have evaluated several inversion methods designed for this
30 task. We compared a look-up table method based on radiative transfer modelling, a nonlinear
31 regression method and four machine learning methods (Gaussian Process, Neural Network, Random
32 Forest and Support Vector Machine) with AOD observations done with a sun photometer at an Aerosol
33 Robotic Network (AERONET) site in Thessaloniki, Greece. Our results show that most of the machine
34 learning methods produce AOD estimates comparable to the look-up table and nonlinear regression
35 methods. All of the applied methods produced AOD values that corresponded well to the AERONET
36 observations with the lowest correlation coefficient value being 0.87 for the Random Forest method.
37 While many of the methods tended to slightly overestimate low AODs and underestimate high AODs,
38 Neural network and support vector machine showed overall better correspondence for the whole AOD
39 range. The differences in producing both ends of the AOD range seem to be caused by differences in
40 the aerosol composition. High AODs were in most cases those with high water vapour content which
41 might affect the aerosol single scattering albedo (SSA) through uptake of water into aerosols. Our study
42 indicates that machine learning methods benefit from the fact that they do not constrain the aerosol
43 SSA in the retrieval where as the LUT method assumes a constant value for it. This would also mean
44 that machine learning methods could have potential in reproducing AOD from SSR even though SSA
45 would have changed during the observation period.

46

47 **1.Introduction**

48 The Fifth Assessment Report of the Intergovernmental Panel on Climate Change states that the most
49 significant source of uncertainty in the projections of climate is related to aerosols (IPCC, 2013). One
50 significant contribution to this uncertainty comes from the fact that without the knowledge of the
51 aerosol burden in the past, we are not able to estimate the current forcing of anthropogenic aerosol. For
52 example, the effect of changes in the current aerosol emissions on climate depends on the background
53 aerosol load during the pre-industrial era (e.g. Andreae, 2008; Carslaw et al., 2013). In addition, the
54 current estimates of past aerosol emissions are highly uncertain (Granier et al., 2011) thus increased
55 knowledge on historical aerosol levels would increase our ability to estimate the present day aerosol
56 radiative forcing.

57 One limiting factor in determining the properties of global aerosol in the past has been that
58 observations of aerosol radiative effects have been limited to fairly recent periods. For example, the
59 aerosol optical depth has mainly been measured using sun photometers and the most widely known
60 ground-based network of sun photometers is Aerosol Robotic Network (AERONET; Holben et al.,
61 1998). Although, AERONET contains globally already over 700 stations, with a fairly good spatial
62 coverage compared to many other observation networks, it still lacks in temporal coverage, providing
63 aerosol optical properties and AOD only since 1990s, and reaching the current status until the recent
64 years. The earliest records of satellite-based AOD are provided by TOMS (Total Ozone Mapping
65 Spectrometer, e.g. Torres et al., 2002) and AVHRR (Advanced Very High Resolution Radiometer,
66 Geogdzhayev et al., 2005), from 1979 and 1983 onwards, respectively. However, neither one of these
67 instruments were specifically designed to retrieve aerosol properties. The more recent dedicated aerosol
68 sounders, such as ATSR (The Along Track Scanning Radiometer 2, Llewellyn-Jones and Remedios,
69 2012), MODIS (Moderate Resolution Imaging Spectroradiometer, Levy et al., 2010), VIIRS (Visible

70 Infrared Imaging Radiometer Suite, Jackson et al., 2013), and MISR (Multi-angle Imaging
71 SpectroRadiometer, Kahn and Gaitley, 2015) offer data from 1995, 2000 and 2002 onwards,
72 respectively. It is therefore apparent that neither sun-photometer nor satellite records of AOD are
73 available for all the decades where industrialization has had a significant effect on the aerosol load.

74 There have been, however, recent studies where aerosol load has been indirectly retrieved from global
75 surface solar radiation (SSR) or separately from direct and diffuse radiation measurements, which
76 cover much longer time periods than sun photometer and satellite observations of AOD. Recently,
77 Kudo et al., 2011 and Lindfors et al., 2013 used radiation measurements done with pyranometers and
78 pyrhemometers to estimate AOD. Lindfors et al., 2013 demonstrated that AOD can be estimated by
79 using SSR and water vapor information and a look-up table (LUT) generated with a radiative transfer
80 code. Their method produces AOD estimates that have 2/3 of the results within $\pm 20\%$ or ± 0.05 of
81 collocated AERONET AODs. Because pyranometer SSR measurements have been done since 1950's
82 over the globe, the usage of AOD estimates based on SSR measurements would enable us to construct
83 AOD time series that go several decades back in time.

84 Since the 1990's machine learning methods have made their way to atmospheric sciences and have
85 been used in e.g. satellite data processing, climate modeling, and weather prediction (Hsieh, 2009).
86 Because of their ability to retrieve parameters from data that have strongly non-linear relationships,
87 they have potential of retrieving AOD from a combination of solar radiation measurements and
88 auxiliary data such as water vapour content (WVC) and solar zenith angle (SZA), similarly to what was
89 done by Lindfors et al. (2013) using a radiative transfer based approach. The aim the present work is to
90 investigate how well machine learning methods are able to estimate AOD from pyranometer
91 observations, by evaluating their performance in comparison with a radiative transfer based look-up-
92 table approach. We chose four different methods: Neural Network (NN, McCulloch and Pitts, 1943),

93 Random Forest (RF, Breiman, 2001), Gaussian Process (GP, Santner et al., 2013) and Support Vector
94 Machine (SVM, Smola and Schölkopf, 2004) and compared them against a look-up table and a
95 nonlinear regression method (NR, Bates and Watts, 1988). The performance of these methods was
96 evaluated with AERONET AOD observations done in Thessaloniki, Greece, after the AOD estimates
97 were derived with SSR observations. Nonlinear regression has been successfully used in multiple
98 studies within aerosol and atmospheric sciences (e.g. Huttunen et al., 2014; Ahmad et al., 2013). Out of
99 these machine learning methods, Neural network (NN) has been actively used in different types of
100 applications in atmospheric sciences. For example, it has been applied to retrieve aerosol properties
101 from remote sensing instruments (Olcese et al. 2015; Taylor et al., 2014; Foyo-Moreno et al, 2014).
102 There have been, however, recent studies where aerosol load has been indirectly retrieved from global
103 surface solar radiation (SSR) or separately from direct and diffuse radiation measurements, which
104 cover much longer time periods than sun photometer and satellite observations of AOD. Recently,
105 Kudo et al., 2011 and Lindfors et al., 2013 used radiation measurements done with pyranometers and
106 pyrhemeters to estimate AOD. The study by Olcese et al. 2015 is similar to ours in the sense that
107 they use alternative data together with Neural Network approach in an attempt to retrieve AOD at an
108 AERONET site. In their study, they fill in missing AOD values (due to e.g. cloud cover) at one
109 AERONET station based on trajectories and AOD observed on another site. To our knowledge, the rest
110 of the analyzed methods have not been used to retrieve aerosol properties directly from observations.

111 **2. Data and Methods**

112 We compared the ability of several methods to estimate AOD, based on SSR and water vapor
113 measurements (and SZA that can be readily determined for any given time and location), against
114 AERONET AOD measurements at 500 nm (henceforth AOD) done at Thessalonki, Greece. This site
115 was chosen for this study, because it has all the necessary measurements with high quality from a 10

116 year time period, and because it is the same site to which Lindfors et al. (2013) applied their LUT-
117 approach. Furthermore, the location has varying aerosol concentrations and relatively high AOD values
118 throughout the year.

119 **2.1 Pyranometer measurements of surface solar radiation**

120
121 SSR has been measured at Thessaloniki since January 1993 with a CM21 pyranometer manufactured
122 by Kipp and Zonen. The instrument is located on the roof of the Physics Department at the Aristotle
123 University of Thessaloniki (40.63 N, 22.96 E), ca. 60 m above sea level. The data are sampled every 1–
124 2 s and every minute the average and standard deviation of the samples are recorded (see more details
125 from Lindfors et al., 2013). The calibration of the pyranometer has been confirmed to stay within the
126 quoted by the manufacturer accuracy (Bais et al., 2013).

127 **2.2 AERONET measurements**

128 AERONET is a network of sun and sky scanning radiometers that measure direct sun and sky radiance
129 at several wavelengths, typically centered at 340, 380, 440, 500, 670, 870, 940, and 1020 nm, providing
130 measurements of various aerosol related properties (Holben et al., 1998). From direct sun
131 measurements we exploited AOD and WVC data. When also sky radiance measurements are included,
132 more detailed aerosol properties such as single scattering albedo (SSA) and asymmetry parameter (gg)
133 can be retrieved (Dubovik et al., 2000). In the evaluation of the machine learning methods we used
134 Level 2.0 (cloud-screened and quality assured) AERONET direct sun measurements of AOD and WVC
135 for Thessaloniki. The Cimel sun photometer is located at the roof of the Physics Department in the
136 close vicinity of the pyranometer discussed above. From the inversion products, to interpret some of
137 our results in more detail, we used level 1.5 (cloud-screened) retrievals. However, when we selected the
138 data from the Level 1.5 inversion product, we applied all the other level 2.0 AERONET criteria except

139 for the AOD threshold. In other words, we applied otherwise the same rigorous quality control that is
140 required for Level 2 data, but we only relaxed the requirement for AOD at 440nm to range from 0.4 to
141 0.1, in order to have more reliable measurements for our data analysis.

142 **2.3 Cloud-screening of the pyranometer measurements and collocation with the AERONET** 143 **measurements**

144 Cloud-screening is a crucial factor in the analysis, thus only contribution of aerosols are considered, not
145 clouds. The SSR data was at first cloud-screened in order to ensure that only clear-sky measurements
146 were included in the analysis (see Lindfors et al., 2013 for more details). However, during the analysis
147 of the data it became evident that even after the initial cloud-screening, the SSR data still included
148 observations that deviated significantly from the main body of the observations. Since there is a high
149 probability that these outliers in the data were caused by e.g. cloud-contamination, we applied
150 additional screening to the data. Thus, we removed the clear outliers of possibly undetected clouds, in
151 our case those observations that deviated by more than $\pm 20 \text{ Wm}^{-2}$ from the exponential regression fit
152 ($\text{SSR} = a \times \exp(-b \times \text{AOD}) + c$, where a, b and c are regression constants). This additional screening was
153 applied through regression of SSR against AOD for a given range of SZA (within $\pm 0.5^\circ$). It has to be
154 noted that this data was only a small fraction of all the data that remained after the cloud screening and
155 it is very unlikely that the additional cloud-screening would affect the main results and the conclusions
156 of our study.

157 The SSR values were collocated for each AOD with the ± 1 minutes difference, averaged and finally
158 normalized for the Sun-Earth distance corresponding to January 1st. The training dataset for the
159 machine learning methods contained years 2009-2014 and the validation (verification) dataset years
160 2005-2008. These periods were selected because we wanted to verify if the methods could provide

161 reasonable AOD estimates for a period different than the training. The training dataset covered
162 approximately 2/3 and the validation dataset 1/3 of the whole data. For all the methods the input
163 parameters are SSR, WVC and SZA, and they produce AOD estimates (Table A1 summarises the
164 statistics of maximum, minimum, average, STD and median for the input and the output parameters.
165 Table A1 shows that e.g. AOD is larger for the validation dataset, although the maximum value is larger
166 for the training).

167

168 **2.4 LUT and NR methods for AOD retrievals**

169

170 **2.4.1 Radiative transfer model based look-up table (LUT)**

171 To retrieve AOD from SSR observations Lindfors et al., (2013) produced a LUT based on radiative
172 transfer simulations. They simulated SSR in different atmospheric conditions by varying AOD, WVC
173 and SZA systematically. They used a single aerosol model for all the simulations, and therefore called
174 their AOD estimate as an effective AOD, which is only a function of SSR, SZA, WVC. Other
175 parameters were assumed as constants e.g. Ångström Exponent of 1.1, SSA at 500 nm of 0.92 (the
176 SSA's spectral pattern follows the rural background aerosol model by Shettle, 1989, where SSA
177 changes from roughly 0.92 at 400 nm to 0.89 at 1000 nm), the asymmetry parameter was assumed
178 wavelength independent with a value of 0.68 while the albedo was varying with wavelength and SZA.
179 For a more detailed description of the LUT method see Lindfors et al., (2013).

180 **2.4.2 Nonlinear regression method (NR)**

181 The nonlinear regression (NR) is a multivariate analysis method which is used when the dependencies
182 between the study variables are not linear (Bates and Watts, 1988). NR is useful especially when there

183 are physical reasons for believing that the relationship between the response and the predictors follows
184 a particular functional form. Benefits of NR are that it needs only moderate sized sample of the studied
185 phenomena to give adequately precise results and as an output it gives a simple, but not predefined,
186 function for prediction. Additional advantage of NR against the other methods presented in this paper is
187 that once the parameters are estimated, they can be used in similar cases without additional training
188 data. In this study we assume that AOD can be estimated as a function of SSR, WVC and SZA.
189 Multiple different formulations for the NR function was tested and the function with the best prediction
190 ability found for this data is given by

$$191 \text{AOD} = b_0 + b_1 \exp\left(\frac{1}{\text{SZA}}\right) + b_2 \exp\left(\frac{1}{\text{SSR}}\right) + b_3 \exp\left(\frac{1}{\text{WVC}}\right) \\ + b_4 \exp\left(\frac{1}{\text{SZA}} + \frac{1}{\text{SSR}}\right) + b_5 \exp\left(\frac{1}{\text{SZA}} + \frac{1}{\text{WVC}}\right) + b_6 \exp\left(\frac{1}{\text{SSR}} + \frac{1}{\text{WVC}}\right). \quad (1)$$

192 The coefficients b_0 - b_6 were determined using R-software (R Core Team, 2014) and are shown in Table
193 A2.

194 **2.5 Machine learning methods for AOD retrievals**

195

196 **2.5.1 Neural Network (NN)**

197 Artificial neural networks belong to the family of machine learning methods (McCulloch and Pitts,
198 1943). As usual in machine learning methods, the aim of an artificial NN is to generate a mathematical
199 model to represent the phenomenon that is examined. The mathematical model of NN structure
200 specifically consists of interconnected neurons with numeric weights. A typical NN model is multilayer
201 perceptron (MLP) (Rosenblatt, 1958), which is used in this study. A MLP network consists of several
202 neuron layers: an input layer, hidden layers and an output layer. The weights and other parameters of
203 the model are tuned or trained with a specific training data set containing input-output pairs of the
204 phenomenon. In this case the model inputs are SSR, WVC, SZA and the output is AOD. The training is

205 executed with a training algorithm and in this paper the Levenberg-Marquardt algorithm is used (Hagan
206 and Menhaj, 1994). A total of 20 NNs were trained in this case. The NNs differed from each other by
207 the number of neurons in a hidden layer. Five networks with the smallest prediction error within the
208 training data set were selected to the final committee of networks. The final prediction of the NN model
209 was computed as a median of the outputs of all networks in the committee. For more information on
210 NNs see, for example, Bishop, (1995).

211 **2.5.2 Random Forest (RF)**

212 Random Forest is a machine learning technique that may be used for classification and nonlinear
213 regression (Breiman, 2001). RF for nonlinear regression consists of an ensemble of binary regression
214 trees. Each of these trees is constructed using a randomized training scheme and is essentially a
215 piecewise constant fit to the training data set. The prediction of a RF model is obtained by averaging
216 the regression tree predictions over the whole model ensemble. In this study, the RF implementation
217 from the Scikit-Learn machine learning library (Pedregosa et al. 2011) was used. We used (SSR, WVC,
218 SZA, SSRxWVC, SSWxSZA, WVCxSZA) as the RF model inputs and AOD as the output. A
219 randomized cross-validation scheme was used to find the optimal training parameters for the RF. For
220 more information on RFs see, for example, Friedman et al., (2001).

221 **2.5.3 Support vector machine (SVM)**

222 Support vector machine (SVM) is a machine learning technique (Vapnik, 1995; Burges, 1998). In this
223 study, we use the standard SVM regression (SVR), the formulation based on the commonly used ϵ -
224 SVR with radial basis kernel function. For implementing the SVM the libsvm package was used
225 (Chang and Lin, 2011). The objective of ϵ -SVR is to find a function that has at most ϵ deviation from
226 the training data set outputs. The training of an ϵ -SVR model is formulated as a quadratic (convex)

227 optimization problem in which the Vapnik's ϵ -insensitive loss function is minimized (e.g. Vapnik 1995).
228 The ϵ -SVR model has two training parameters that were used to control the training: the regularization
229 parameter, which controls the smoothness of the approximation function (sensitivity to noise), and the
230 parameter ϵ , which dominates the number of support vectors by governing the accuracy of the
231 approximation function. The determination of SVM control parameters was solved by the means of a
232 grid search. For a more detailed description of the method, the reader is referred, for example, to Smola
233 and Schölkopf (2004).

234 **2.5.4 Gaussian process (GP)**

235 Gaussian process (GP) for machine learning is a generic supervised learning method that may be used,
236 for example, for nonlinear regression. In GP learning, the function inputs and outputs are treated as
237 Gaussian random variables and the correlations between these variables are modelled. The predictions
238 given by a GP model are computed as conditional probability distributions given the training data and
239 function inputs. As the prediction given by a GP model is a probability distribution, the error estimates
240 for the predicted point estimates are obtained automatically. In this study, the GP implementation from
241 the Scikit-Learn machine learning library was used. The same inputs and output variables as with the
242 RF models were used in the GP training. The best performing correlation function training parameters
243 were sought for using maximum likelihood estimation. A total of 25 GP models were trained. The
244 training of each model was carried out using 2500 training data samples that were randomly sampled
245 from the full training data set. The five best performing GP models were selected into the final GP
246 model committee. The final prediction was computed as the median of the predictions given by the GP
247 models in the committee. For more information on GPs for machine learning see, for example, Welch
248 et al., (1992), Rasmussen and Williams (2006), and Santner et al., (2013).

249 **3. Results**

250 **3.1 Comparison of the methods**

251 Table 1 shows the statistics of the AOD observed by AERONET together with the statistical
252 characteristics of the predicted AOD for the years 2005-2008. From the table, we can see that predicted
253 values show good correlation against the observations for all the methods. Predictions by RF had the
254 lowest correlation coefficient with a value of 0.87 while the correlation coefficient for NR was only
255 slightly larger, 0.88. For the best performing methods, LUT, GP, NN, and SVM, the correlation
256 coefficients were approximately 0.92. Their predicted AODs in comparison to AERONET AOD are
257 shown in Figure 1. To visualize the distribution of the data, the colorbar in Figure 1 represents the
258 number of observations for each AOD interval of 0.005. Based on the different statistics in Table 1,
259 machine learning methods (NN, SVM, GP) produce a good match with AERONET data and they
260 perform equally good or better than the LUT method according to all the metrics. Due to the fact that
261 RF and NR are not able to produce as good estimates as the LUT method, they were left out from the
262 more detailed analysis.

263 Although these methods are able to predict the average AOD with a good accuracy, they differ when
264 we compare their ability to predict different AOD levels. In Figure 1, the color scales indicate the
265 absolute amount of results in the areas with the interval of 0.01x0.01 (vertically and horizontally) for
266 AOD, in addition 1:1-lines and linear fits are included. Based on the linear fits, NN appears to have the
267 best agreement with AERONET data for the whole AOD range. As the average and median values of
268 AERONET AOD are 0.240 and 0.207 respectively (Table 1), the main population of the measurements
269 is in the range of moderate AODs. The machine learning methods are obviously weighted to perform
270 best in this range of AODs. However, from Figure 2, which shows the absolute difference between

271 AERONET and predicted AOD, we can see that LUT and GP tend to significantly underestimate AOD
272 for AODs larger than 0.5, while NN and SVM are able to reach smaller differences with AERONET on
273 average, although with larger overall variabilities than LUT and GP. Although NN and SVM also start
274 to deviate from the observations at higher AODs, these deviations are more modest in relative sense as
275 can be seen from Figure 3 which shows the relative difference between the observations and
276 predictions. All the methods overestimate AOD in relative terms, when AOD approaches zero (Figure
277 3). However, as Figure 2 demonstrates, the absolute error is systematically very low in the small AOD
278 region ($\text{AOD} < 0.2$). NN and SVM are generalized better for large AODs than the other methods,
279 where the amount of data are small.

280 As an additional test, we tested combining different the colorbar in Figure 1 represents the number of
281 observations for each AOD interval of 0.005. methods. In Table 1, the four last rows represent the
282 values for cases where the results of machine learning methods are combined by averaging them. As
283 can be seen from the table, these combinations do not improve the estimates compared to the statistical
284 values of individual methods.

285 **3.2 The effect of water vapour on AOD predictions**

286 Huttunen et al. (2014) showed that WVC and AOD have typically a positive correlation. Therefore, we
287 investigated how the AOD estimates from different methods are affected by WVC. Figure 4 shows the
288 relative difference between the predictions and measured AOD with respect to WVC. From this figure,
289 we can see that the LUT-based AODs are overestimated at the smallest and underestimated at the
290 largest WVC contents. The reason for this behaviour is that the LUT method has been set to assume
291 prescribed and constant properties for many relevant parameters that affect SSR (other than AOD and
292 WVC); e.g. aerosol single scattering albedo, asymmetry parameter and surface albedo (Lindfors et al.,

293 2013). Consequently, the assumption of constant SSA in particular leads to WVC-dependent systematic
294 bias of the LUT-based AOD, as we will show next. The other methods are closer to the ratio of 1
295 without such a systematic bias, excluding the SVM's underestimation for the smallest WVC.

296 Figure 5 shows measured SSR and LUT-based SSR for a narrow set of SZAs (48.50° - 51.50°). AOD is
297 on the horizontal axis, SSR on the vertical axis and WVC is shown with the colorbar. From Figure 5a it
298 is evident that LUT incorporates a strong WVC-dependent structure: for a given SSR level, AOD
299 decreases with increasing water vapor content. This pattern follows from the assumption that the
300 aerosol composition remains the same, i.e. it has a fixed SSA value. Thus in the LUT method, increases
301 in SSR absorption by water vapour are compensated by decreases in aerosol extinction. In the real
302 atmosphere, water vapour content has also implications on aerosol composition and size. If all
303 conditions apart from water vapour remained constant, increase of water vapour would also increase
304 the uptake of water into aerosol particles thus affecting the aerosol SSA. The effect of fixed SSA is also
305 visible in the way the LUT-based AOD estimates are distributed (Figure 5a). In Figure 5c we can see
306 that for a given AOD in the LUT, the highest WVC values always correspond to the lowest SSR values.
307 However, the same pattern is not clearly visible either in the plot with the measured values (Figure 5b)
308 or in the plot with AOD from NN (Figure 5d). This indicates that although the machine learning
309 methods do not get explicitly any information about the possible systematic co-variability of WVC and
310 SSA, they seem to be able to detect it indirectly, at least to some extent.

311 To further illustrate this, Figure 6a shows the AERONET measurements of AOD and single scattering
312 co-albedo, 1 -SSA at 500 nm as a function of WVC. Here, together with the absorption strength by the
313 water vapour, we considered more illustrative to show the single scattering co-albedo rather than SSA.
314 In this plot, SZA, SSR and season were limited respectively to: $58^\circ < \text{SZA} < 62^\circ$, $420 \text{ Wm}^{-2} < \text{SSR} <$
315 460 Wm^{-2} , June-August, allowing enough data with the limited parameters. Thus, the plot illustrates the

316 co-variability of WVC and SSA for a limited range of surface solar radiation and SZA, for conditions
317 when the LUT method produces lower AOD values for higher WVC (Figure 5a). However, Figure 6a
318 clearly shows that an opposite relationship between AOD and WVC is obtained by the measurements.
319 Moreover, this pattern is compensated by aerosol absorption (remember that in this sub-set we
320 constrained SSR), which decreases with increasing WVC; this is likely related to the aerosol swelling
321 by hygroscopic growth that increases the scattering of the aerosol. Therefore, we can conclude from the
322 measurements that because of the co-variability of WVC and SSA in Thessaloniki, the assumption of a
323 fixed SSA in the LUT causes limitations for predicting AOD, while the machine learning methods can
324 take into account, at least to some extent, this relationship indirectly. Using radiative transfer modeling
325 we demonstrated that the magnitude of these changes in water vapor and aerosol absorption, as
326 indicated in Figure 6. Indeed, they induced opposite effects of similar magnitude in surface solar
327 irradiance. For the base case, we simulated SSR with WVC of 2.8 cm and 1-SSA of 0.06 (with SZA of
328 60° and AOD of 0.3) as inputs, resulting in 439.9 Wm^{-2} . When we increased the water vapour column
329 to 3.6 cm, the corresponding decrease in SSR was about 6.8 Wm^{-2} . However, when we additionally
330 decreased the aerosol absorption (1-SSA) to 0.04, the difference to the base case shrank to 1.8 Wm^{-2}
331 and this remaining amount can mostly be explained by the asymmetry parameter, which also exhibits a
332 systematic dependence with WVC (stronger forward scattering by particles grown in humid
333 conditions).

334 The lower panel of Figure 6 further illustrates the role of fixed SSA in the observed WVC-dependent
335 bias in the LUT results, which can be avoided with the machine learning methods. It shows the mean
336 ratio of LUT-estimated and AERONET-measured AOD on the right-hand side y-axis as a function of
337 water vapour content (so essentially the same results shown by a box-plot in Figure 4). Additionally, on
338 the left-hand side y-axis, the single scattering albedo (estimated for 500 nm) from AERONET

339 measurements is shown as a function of water vapour amount as well. This also demonstrates that the
340 over- and underestimations of the LUT method coincide with SSA range that is under and over the
341 assumed fixed value of 0.92 (shown with red dashed line), respectively. Visibly, the ratio in the right-
342 hand axis of Fig. 6b, reaches one not until SSA is roughly 0.93 instead of 0.92. Presumably, SSA has
343 actually a different wavelength pattern than the one assumed in LUT.

344 **4. Conclusions**

345 We have used several inverse methods to retrieve aerosol optical depth (AOD) from surface solar
346 radiation (SSR) and water vapour content (WVC) measurements (with corresponding solar zenith angle
347 data) done in Thessaloniki, Greece. Two traditional (look-up table (LUT) and nonlinear regression
348 (NR)) and four machine learning methods (Gaussian Process (GP), Neural Network (NN), Random
349 Forest (RF) and Support Vector Machine (SVM)) were used to retrieve AOD estimates for the years
350 2005-2008. Then we compared the AOD estimates with collocated AOD measurements done by
351 Aerosol Robotic Network (AERONET). Our comparisons showed that:

352 -AOD estimates based on the LUT method agreed better with AERONET than the NR estimates but
353 apart from RF, the machine learning methods produced AOD estimates that were comparable or better
354 than LUT.

355 -NN and SVM methods reproduced good correspondence to AERONET observations for both low and
356 high AODs while rest of the methods tended to overestimate low AODs and underestimate high AODs.
357 The main reason for the better performance of these machine learning methods was that there were no
358 constrains of the aerosol single scattering albedo (SSA) in the retrieval. In other words, the methods do
359 not need to explicitly make assumptions on the optical aerosol properties of the atmosphere and
360 because seem to be able to indirectly account for the covariation of WVC and SSA.

361 -When compared with AERONET measurements, the best AOD estimates were retrieved with the
362 machine learning algorithms, but only NN and SVM were able to generalize accurate estimates also for
363 large AODs.

364 -The machine learning methods are sensitive to the selection of the training data set and other
365 constraints, and are generally valid only for the range of the variables used for their training; thus care
366 needs to be taken when these methods are employed.

367 -These tools have the potential to be used in the retrieval of AOD from SSR measurements to lengthen
368 the time series of AOD. Historical AOD is essential in the estimation of anthropogenic aerosol effects
369 and in the evaluation of AOD retrievals from space borne instruments before the 1990s.

370 -The intention of comparing different methods was to test their ability in an "out-of-the-box"
371 configuration. With this in mind, methods were not particularly tuned to reach the best possible results.
372 It is very likely that e.g. optimizing the free parameters used in each of the nonlinear modeling
373 approaches, their ability to reproduce observed AOD could be further improved.

374 **Acknowledgements.**

375 We thank the AERONET team, principal investigators and other participants for their effort in
376 establishing and maintaining the network. This study is supported by Graduate school in Physics,
377 Chemistry, Biology and Meteorology of Atmospheric Composition and Climate Change: From
378 Molecular Processes to Global Observations and Models. The Academy of Finland Center of
379 Excellence program (project number 272041) is also acknowledged. The financial support by the
380 strategic funding of the University of Eastern Finland is gratefully acknowledged. The author thank
381 Juha Tonttila and Mikko Pitkänen from Finnish Meteorological Institute, Kuopio, for their help with
382 the python (python.org) and in the production of the MatLab (mathworks.com) boxplot-figures. Also
383 JH thank the Finnish Cultural Foundation, North Savo Regional fund.

384 **References**

- 385 Ahmad, I., Mielonen, T., Grosvenor, D., Portin, H., Arola, A., Mikkonen, S., Kühn, T., Leskinen, A.,
386 Joutsensaari, J., Komppula, M., Lehtinen, K., Laaksonen, A. and Romakkaniemi, S. (2013). Long-term
387 measurements of cloud droplet concentrations and aerosol-cloud interactions in continental boundary
388 layer clouds. *Tellus B*, 65. doi:<http://dx.doi.org/10.3402/tellusb.v65i0.20138>.
- 389 Andreae, M. O. and Rosenfeld, D. Aerosol–cloud–precipitation interactions. Part 1. The nature and
390 sources of cloud-active aerosols, *Earth Sci. Rev.* 89, 13–41, 2008.
- 391 Bais, A. F., Drosoglou, Th., Meleti, C., Tourpali, K. and Kouremeti, N., Changes in surface shortwave
392 solar irradiance from 1993 to 2011 at Thessaloniki (Greece). *Int. J. Climatol.*, 33: 2871–2876. doi:
393 10.1002/joc.3636, 2013.
- 394 Bates D.M. and Watts D. G., *Nonlinear Regression Analysis and Its Applications*, Wiley, New York,
395 1988.
- 396 Bishop C. M., *Neural Networks for Pattern Recognition*, Oxford University Press, Inc. New York, NY,
397 USA, ISBN:0198538642, 1995.
- 398 Breiman, L., Random forests, *Machine learning*, vol 45, 1, 5-32, 2001.
- 399 Burges C. J. C., A tutorial on support vector machines for pattern recognition, *Data Mining and*
400 *Knowledge Discovery*, 2, 121–167, 1998.
- 401 Carslaw K. S., Lee L. A., Reddington C. L., Pringle K. J., Rap A., Forster P. M., Mann G. W.,
402 Spracklen D. V., Woodhouse M. T., Regayre L. A. and Pierce J. R., Large contribution of natural
403 aerosols to uncertainty in indirect forcing, *Nature*, 2013.
- 404 Dubovik, O., A. Smirnov, B. N. Holben, M. D. King, Y.J. Kaufman, T. F. Eck, and I. Slutsker, 2000:
405 Accuracy assessments of aerosol optical properties retrieved from AERONET sun and sky-radiance
406 measurements, *J. Geophys. Res.*, 105, 9791-9806.
- 407 Foyo-Moreno I., Alados I., Anton M., Fernandez-Galvez J., Cazorla A. and Alados-Arbodelas L.,
408 Estimating aerosol characteristics from solar irradiance measurements at an urban location in
409 southeastern Spain, *J. of Geophys. Res. Atmos*, 119, 1845-1859, doi:10.1002/2013JD020599, 2014.
- 410 Friedman J., Hastie T., and Tibshirani R., *The elements of statistical learning*, Springer, vol 1, 2001.
- 411 Geogdzhayev, I. V., M. I. Mishchenko, E. I. Terez, G. A. Terez, and G. K. Gushchin, Regional
412 advanced very high resolution radiometer–derived climatology of aerosol optical thickness and size, *J.*
413 *Geophys. Res.*, 110, D23205, doi:10.1029/2005JD006170, 2005.
- 414 Chang C.-C. and Lin C.-J. LIBSVM: a library for support vector machines. *ACM Transactions on*
415 *Intelligent Systems and Technology*, 2:27:1-27:27, 2011.
- 416 Claire Granier, Bertrand Bessagnet, Tami Bond, Ariela D’Angiola, Hugo Denier van der Gon, Gregory
417 J. Frost, Angelika Heil, Johannes W. Kaiser, Stefan Kinne, Zbigniew Klimont, Silvia Kloster, Jean-
418 François Lamarque, Catherine Lioussé, Toshihiko Masui, Frederik Meleux, Aude Mieville, Toshimasa
419 Ohara, Jean-Christophe Raut, Keywan Riahi, Martin G. Schultz, Steven J. Smith, Allison Thompson,
420 John van Aardenne, Guido R. van der Werf, and Detlef P. van Vuuren, Evolution of anthropogenic and
421 biomass burning emissions of air pollutants at global and regional scales during the 1980–2010 period,
422 *Climatic Change*, 109, 1, 163-190, 2011.
- 423 Hagan M.T. and Menhaj M.B., Training feedforward networks with the Marquardt algorithm, *IEEE*

424 Trans. Neural Networks, 5, 6, 989-993, 1994.

425 Holben B.N., T.F. Eck, I. Slutsker, D. Tanre, J.P. Buis, A. Setzer, E. Vermote, J.A. Reagan, Y. Kaufman,
426 T. Nakajima, F. Lavenu, I. Jankowiak, and A. Smirnov, 1998: AERONET - A federated instrument
427 network and data archive for aerosol characterization, Rem. Sens. Environ., 66, 1-16.

428 Hsieh, Machine Learning Methods in the Environmental Sciences Neural Networks and Kernels,
429 Cambridge Univ Press, 2009.

430 Huttunen, J., Arola, A., Myhre, G., Lindfors, A. V., Mielonen, T., Mikkonen, S., Schafer, J. S., Tripathi,
431 S. N., Wild, M., Komppula, M., and Lehtinen, K. E. J.: Effect of water vapor on the determination of
432 aerosol direct radiative effect based on the AERONET fluxes, Atmos. Chem. Phys., 14, 6103-6110,
433 doi:10.5194/acp-14-6103-2014, 2014.

434 IPCC, Climate Change 2013: The Physical Science Basis. Contribution of Working Group I to the Fifth
435 Assessment Report of Intergovernmental Panel on Climate Change, Cambridge University Press,
436 Cambridge, United Kingdom and New York, NY, USA, ISBN 978-1-107-66182-0,
437 doi:10.1017/CBO9781107415324, 2013.

438 Jackson, J. M., H. Liu, I. Laszlo, S. Kondragunta, L. A. Remer, J. Huang, and H.-C. Huang, Suomi-
439 NPP VIIRS aerosol algorithms and data products, J. Geophys. Res. Atmos., 118, 12, 673–12, 689,
440 doi:[10.1002/2013JD020449](https://doi.org/10.1002/2013JD020449), 2013.

441 Kahn, R. A., and B. J. Gaitley, An analysis of global aerosol type as retrieved by MISR. J. Geophys.
442 Res. Atmos., 120, 4248–4281. doi: [10.1002/2015JD023322](https://doi.org/10.1002/2015JD023322), 2015.

443 Kudo, R., Uchiyama, A., Yamazaki, A., Sakami, T., and Ijima, O., Decadal changes in aerosol optical
444 thickness and single scattering albedo estimated from ground-based broadband radiometers: A case
445 study in Japan, J. Geophys. Res., 116, D03207, doi:10.1029/2010JD014911, 2011.

446 Levy, R. C., Remer, L. A., Kleidman, R. G., Mattoo, S., Ichoku, C., Kahn, R., and Eck, T.F., Global
447 evaluation of the Collection 5 MODIS dark-target aerosol products over land, Atmos. Chem. Phys., 10,
448 10399-10420, doi:10.5194/acp-10-10399-2010, 2010.

449 Llewellyn-Jones D. and Remedios J., The Advanced Along Track Scanning Radiometer (AATSR) and
450 its predecessors ATSR-1 and ATSR-2: An introduction to the special issue, Remote Sensing of
451 Environment, Vol 116, 15, Pages 1–3, doi:10.1016/j.rse.2011.06.002, 2012.

452 Lindfors, A. V., Kouremeti, N., Arola, A., Kazadzis, S., Bais, A. F., and Laaksonen, A., Effective
453 aerosol optical depth from pyranometer measurements of surface solar radiation (global radiation) at
454 Thessaloniki, Greece, Atmos. Chem. Phys., 13, 3733-3741, doi:10.5194/acp-13-3733-2013, 2013.

455 McCulloch, W. and Pitts W., A Logical Calculus of Ideas Immanent in Nervous Activity, Bulletin of
456 Mathematical Biophysics 5, 4, 115–133. doi:10.1007/BF02478259, 1943.

457 Olcese L. E., Palancar G. G. and Toselli B. M., A method to estimate missing AERONET AOD values
458 based on artificial neural networks, Atmospheric Environment, 113, 140–150,
459 doi:10.1016/j.atmosenv.2015.05.009, 2015.

460 Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V., Thirion, B., Grisel, O., Blondel, M.,
461 Prettenhofer, P., Weiss, R., Dubourg, V., Vanderplas, J., Passos, A., Cournapeau, D., Brucher, M.,
462 Perrot, M., and Duchesnay, E., Scikit-learn: Machine Learning in Python, Journal of Machine Learning
463 Research, 12, 2825-2830, 2011.

464 R Core Team (2014). R: A language and environment for statistical computing. R Foundation for

465 Statistical Computing, Vienna, Austria. URL <http://www.R-project.org/>.

466 Rasmussen, C.E. and Williams, C.K.I., Gaussian processes for machine learning, MIT Press, 2006.

467 Santner, T. J., Williams, B. J., and Notz, W. I., The design and analysis of computer experiments,
 468 Springer Science & Business Media, 2013.

469 Rosenblatt, F. A, probabilistic model for information storage and organization in the brain, Psychol.
 470 Rev., 65, 6, 368-408, 1958.

471 Shettle, E. P., Models of aerosols, clouds and precipitation for atmospheric propagation studies, in:
 472 Atmospheric Propagation in the UV, Visible, IR and mm-region and Related System Aspects, no. 454
 473 in AGARD Conf. Proc., 15-1-15-13, 1989.

474 Smola A. J. and Schölkopf B., A tutorial on support vector regression, Stat. Comput., 14, 199-222,
 475 2004.

476 Taylor, M., Kazadzis, S., Tsekeri, A., Gkikas, A., and Amiridis, V., Satellite retrieval of aerosol
 477 microphysical and optical parameters using neural networks: a new methodology applied to the Sahara
 478 desert dust peak, Atmos. Meas. Tech., 7, 3151-3175, doi:10.5194/amt-7-3151-2014, 2014.

479 Torres, O., Bhartia P. K., Herman J. R., Sinyuk A., Ginoux P., and Holben B., A long-term record of
 480 aerosol optical depth from TOMS observations and comparison to AERONET measurements, Journal
 481 of the Atmospheric Sciences, 59, 3, 398-413, 2002.

482 Vapnik, V., The Nature of Statistical Learning Theory. New York: Springer, 1995.

483 Welch, W. J., Buck, R. J., Sacks, J., Wynn, H. P., Mitchell, T. J., and Morris, M. D., Screening,
 484 predicting, and computer experiments, Technometrics, vol 34, 1, 15-25, 1992.

485

487

488 Table 1: Statistical characteristics of observed (AERONET) and predicted AOD by the methods of NR
 489 (nonlinear regression), LUT (look-up table), NN (neural network), RF (random forest), GP (gaussian
 490 process), SVM (support vector machine) and some of their combinations (averages without weights,
 491 e.g. NN, SVM combination is their average result). Correlation coefficient (R^2), mean absolute
 492 deviation (MAD), median and their $\pm 20\%$ percentiles between the observed and predicted. Also time
 493 consumptions with a recent average computer power of the methods for training / estimation in the
 494 magnitude of seconds, minutes and hours. The number of observations is 10684.

Method	Average(std)	R^2	MAD	Median	Fraction in +/-20%	Time consumption
AERONET	0.240(0.147)			0.207		
NR	0.228(0.123)	0.880	0.053	0.210	48.4 %	seconds / < second

LUT	0.254(0.136)	0.920	0.046	0.236	52.6 %	hours / minutes
NN	0.251(0.156)	0.920	0.044	0.212	59.1 %	hours / < second
RF	0.225(0.116)	0.870	0.052	0.204	52.9 %	tens of seconds / < second
GP	0.240(0.130)	0.927	0.041	0.213	60.8 %	minutes / tens of seconds
SVM	0.242(0.150)	0.918	0.044	0.201	58.4 %	tens of seconds / < second
NN, SVM	0.247(0.152)	0.924	0.043	0.207	59.7 %	
NN, SVM, RF	0.240(0.138)	0.922	0.042	0.205	59.9 %	
SVM, RF	0.234(0.131)	0.913	0.044	0.202	58.0 %	
NN, RF	0.238(0.134)	0.916	0.043	0.207	59.0 %	

495

496

497

498

499

500

501

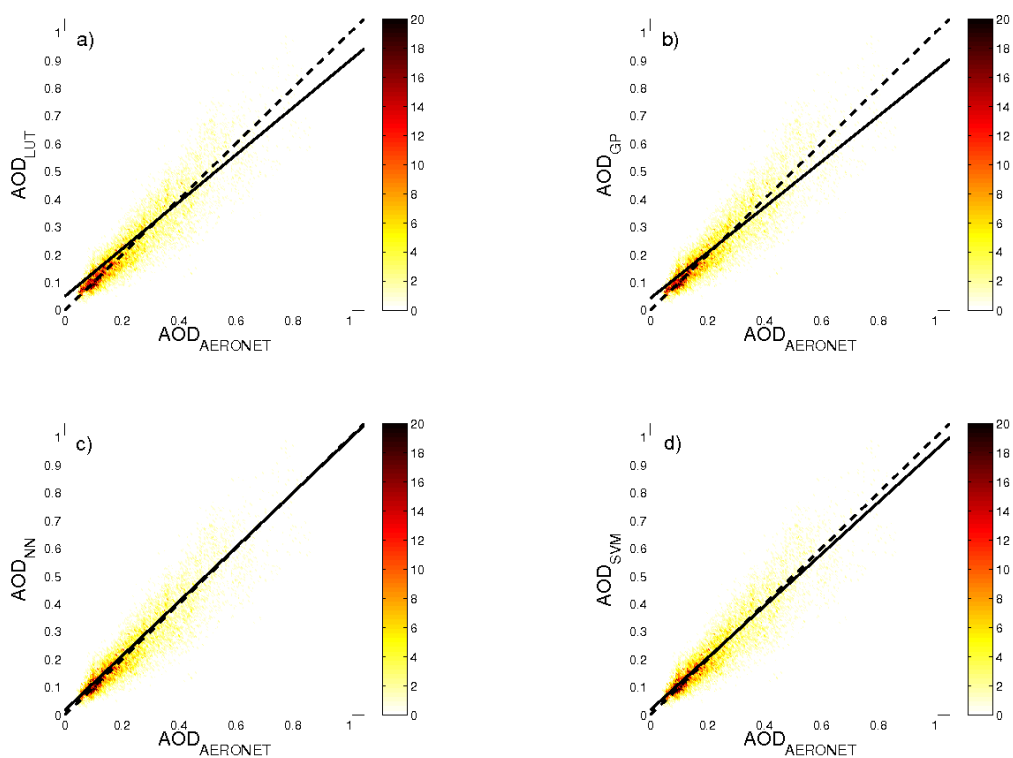
502

503

504

505

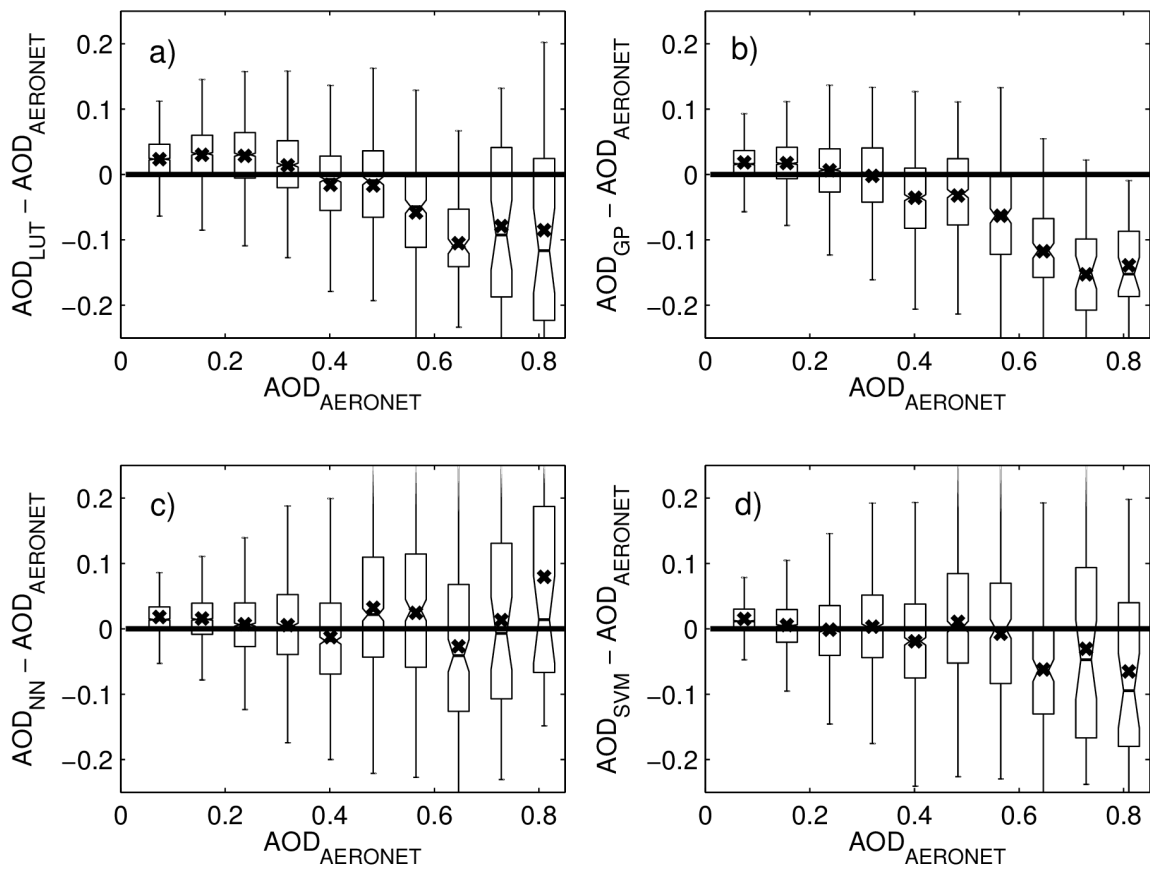
506



509 Figure 1: Observed (AERONET) and predicted AOD by the methods of a) LUT (look-up table), b) GP
 510 (Gaussian Process), c) NN (Neural Network) and d) SVM (Support Vector Machine). The colorbar
 511 indicates the absolute amount of results in the areas with the interval of 0.01×0.01 . The 1:1-lines and
 512 linear fits included. The number of observations is 10684. The relation for the linear fits is, estimated
 513 $AOD = a_1 + a_2 \times AERONET \text{ AOD}$, and the coefficients of the fits are (a_1, a_2) : 0.0503, 0.8492; 0.0429,
 514 0.8204; 0.0164, 0.9791 and 0.0178, 0.9355, for LUT; GP; NN and SVM, respectively.

515

516



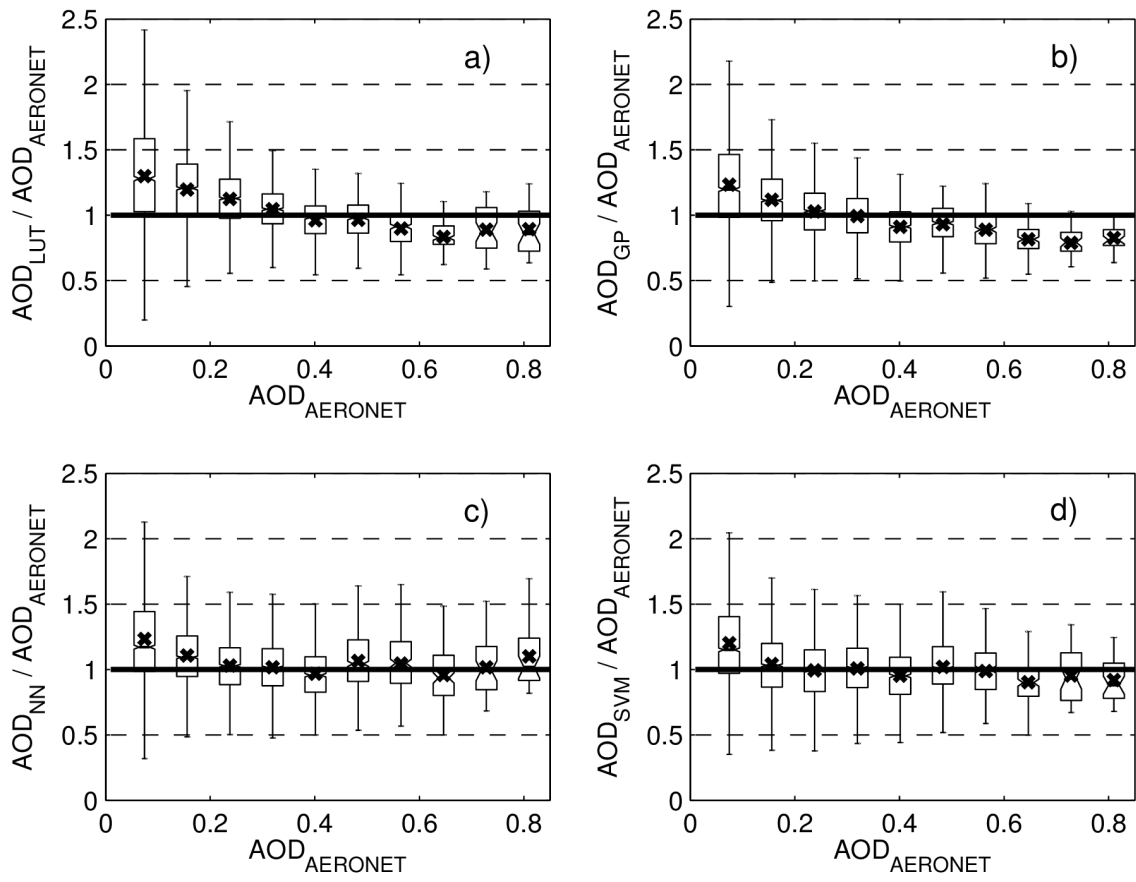
518 Figure 2: Differences between predicted and observed (AERONET) AOD for the methods: a) LUT
 519 (look-up table), b) GP (Gaussian Process), c) NN (Neural Network) and d) SVM (Support Vector
 520 Machine) with respect of the observed AOD. The crosses indicate the means of each sub-group, the
 521 limits of the boxes are 25 %, 50 % and 75 % of the data, and the lines are plotted with 1.5 times the
 522 inter-quartile ranges.

523

524

525

526



528

529 Figure 3: The same as Fig. 2, but in the vertical axis is the ratio of the predicted to the observed

530 (AERONET) AOD.

531

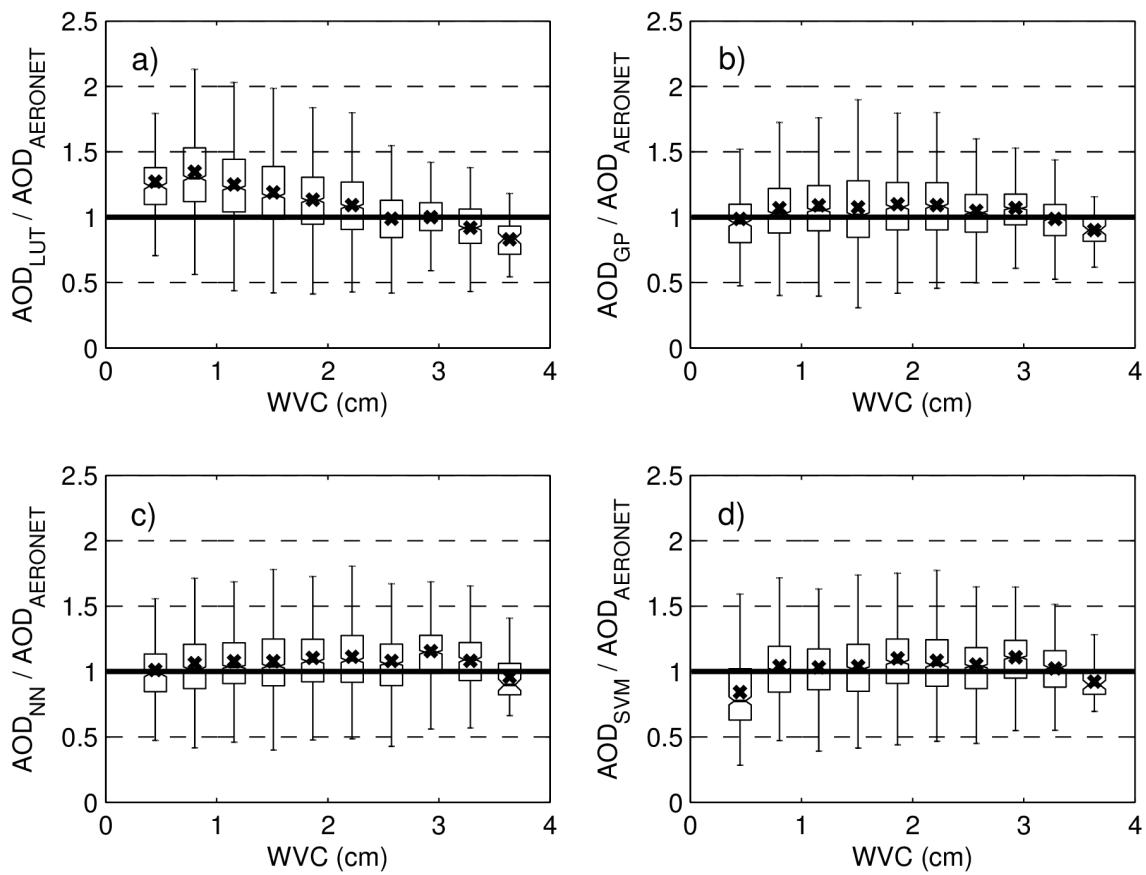
532

533

534

535

536



538

539 Figure 4: The same as Fig. 3, but the ratio of predicted to measured AOD is given as a function of the
 540 water vapor column (WVC).

541

542

543

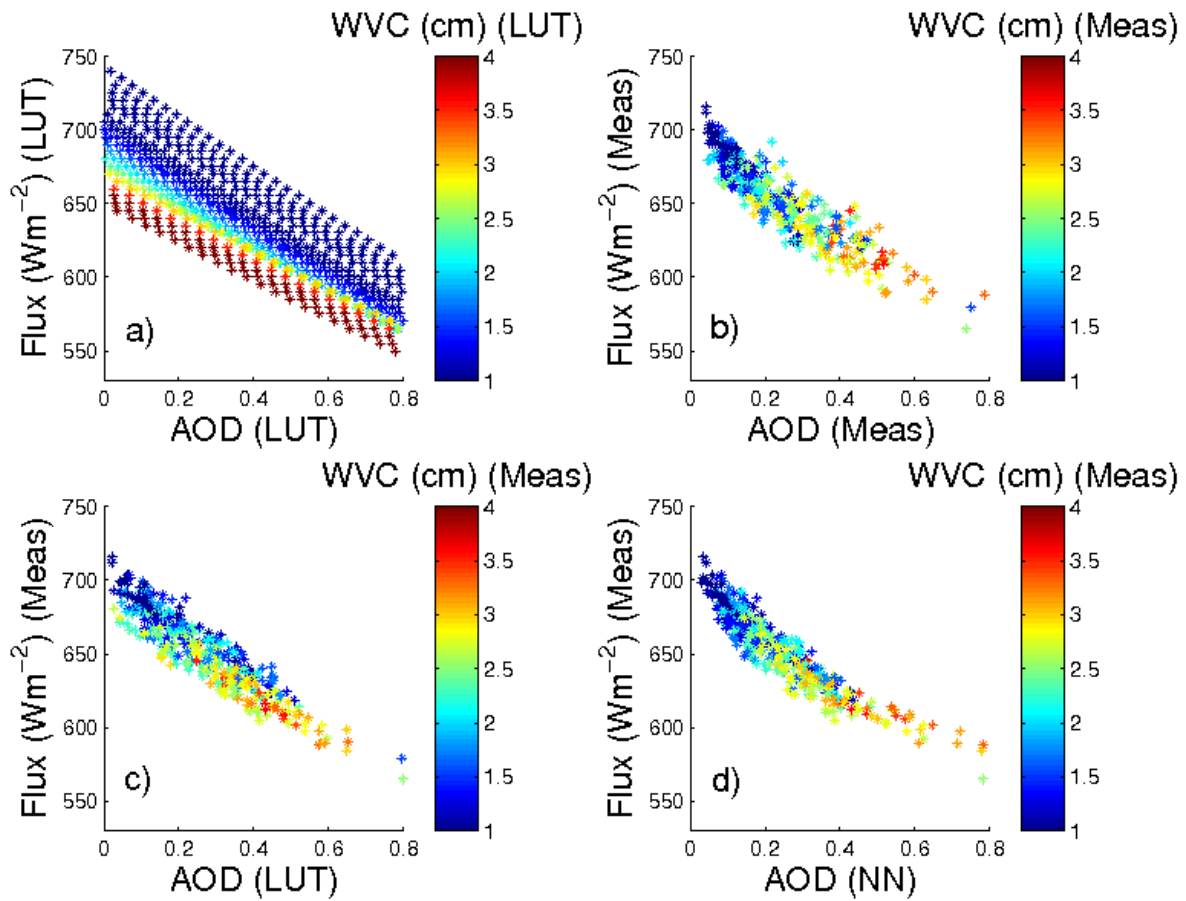
544

545

546

547

548



550

551 Figure 5: Solar surface radiation (SSR), aerosol optical depth (AOD) and water vapor column (WVC)
 552 for a fixed solar zenith angle (48.50° - 51.50°) for a) look-up table (LUT) and b) measurements (Meas).
 553 The predicted AODs for c) LUT and d) neural network (NN) corresponding the same SSR, WVC and
 554 SZA.

555

556

557

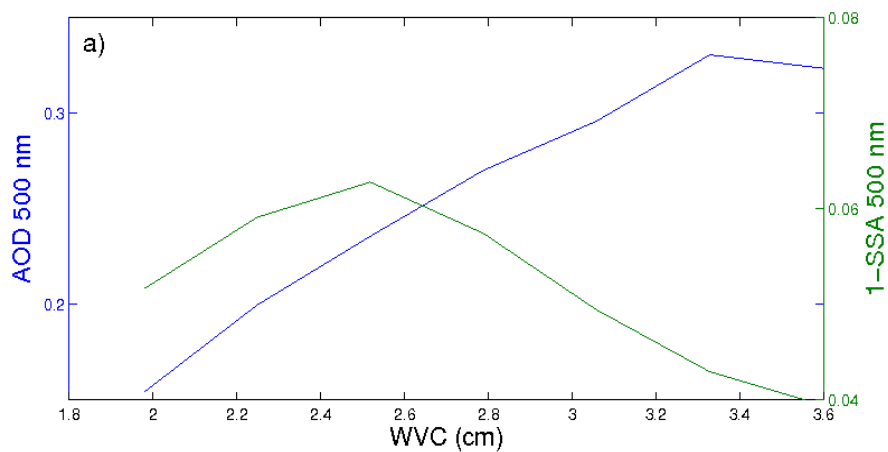
558

559

560

561

562



563

564

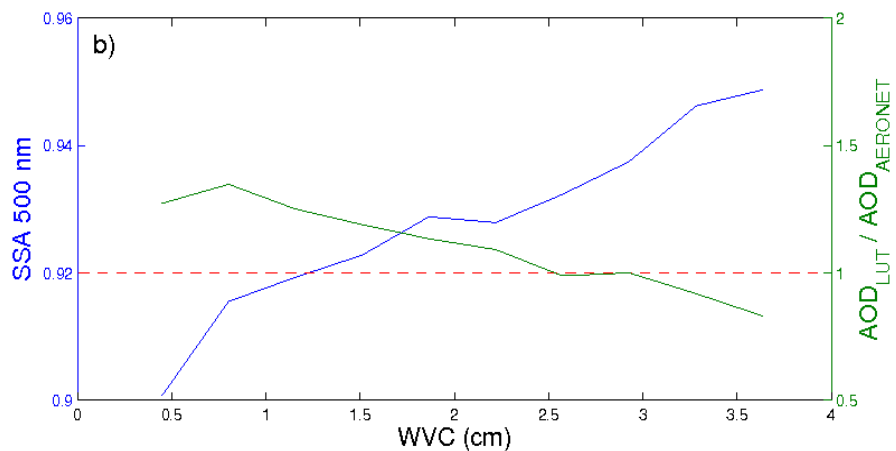
565

566

567

568

569



570

571

572

573 Figure 6: a) Aerosol optical depth (AOD), water vapor column (WVC) and 1-SSA at 500 nm from the

574 AERONET inversion sky data. b) SSA at 500 nm, WVC and the LUT's predicted AOD divided with

575 the observational AOD (AERONET), with the red line fixed to SSA (500 nm) = 0.92 (as in LUT).

576

577

578

579

580 **Appendix A**

581

582 Table A1. The statistics between the training and the validation data for the input and the output

583 parameters. The units for SZA, SSR and WVC are degrees, Wm^{-2} and cm, respectively.

Training:					
Parameter	Max	Min	Average	STD	Median
SZA	78.6	17.5	56.2	15.7	60.0
SSR	1071.9	120.5	522.7	247.1	479.6
WVC	4.12	0.23	2.23	0.73	2.29
AOD	1.06	0.01	0.22	0.12	0.20
Validation:					
Parameter	Max	Min	Average	STD	Median
SZA	78.7	17.5	60.6	14.7	65.3
SSR	1060.0	113.2	450.2	235.9	384.5
WVC	3.81	0.27	1.87	0.82	1.79
AOD	0.85	0.03	0.24	0.15	0.21

584

585 Table A2. The coefficient values of eq.(1) and errors (STD) for the NR method.

Coefficients	Estimate	STD error
b_0	1.716×10^5	8.372×10^2
b_1	-1.696×10^5	8.272×10^2
b_2	-1.715×10^5	8.363×10^2
b_3	-1.206×10^1	5.727×10^{-1}
b_4	1.694×10^5	8.264×10^2
b_5	5.145×10^0	2.465×10^{-1}
b_6	6.819×10^0	3.728×10^{-1}

586