Global Distribution of CO₂ in the Upper Troposphere and Stratosphere

M. Diallo¹,²,⁷, B. Legras¹, E. Ray³,⁴, A. Engel⁵, and J. A. Añel²,⁶

¹Laboratoire de Météorologie Dynamique, UMR8539, IPSL, CNRS/ENS/UPMC/Ecole Polytechnique, Paris, France
²EPhysLab, Facultade de ciencias, Universidade de Vigo, Ourense, Spain
³Chemical Sciences Division, Earth Systems Research Laboratory, NOAA, Boulder, Colorado, USA
⁴Cooperative Institute for Research in Environmental Sciences, University of Colorado, Boulder, Colorado, USA
⁵Institute for Atmospheric and Environmental Sciences, Goethe University Frankfurt, Frankfurt am Main, Germany
⁶Smith School of Enterprise and the Environment, University of Oxford, Oxford, UK
⁷Institute for Energy and Climate Research - Stratosphere (IEK-7), Forschungszentrum Jülich, Jülich, Germany

Correspondence to: M. Diallo (m.diallo@fz-juelich.de)
Abstract

In this study, we construct a new monthly zonal mean carbon dioxide (CO$_2$) distribution from the upper troposphere to the stratosphere and over the 2000–2010 time period. This reconstructed CO$_2$ product is based on a Lagrangian backward trajectory model driven by ERA-Interim reanalysis meteorology and tropospheric CO$_2$ measurements. Comparisons of our CO$_2$ product to extra-tropical in situ measurements from aircraft transects and balloon profiles show remarkably good agreement. The main features of the CO$_2$ distribution include (1) relatively large mixing ratios in the tropical stratosphere, (2) seasonal variability in the extra-tropics with relatively high mixing ratios in the summer and autumn hemisphere in the 15–20 km altitude layer, and (3) decreasing mixing ratios with increasing altitude from the upper troposphere to the middle stratosphere (∼35 km) and nearly constant mixing ratios in the upper stratosphere. These features are consistent with expected variability due to the transport of long-lived trace gases by the stratospheric Brewer-Dobson circulation. The method used here to construct this CO$_2$ product is unique from other modeling efforts and should be useful for model and satellite validation in the upper troposphere and stratosphere, as a prior for inversion modeling and to analyze features of stratosphere-troposphere exchange as well as the stratospheric circulation and its variability.

1 Introduction

The global stratospheric meridional circulation, also called the Brewer-Dobson circulation (BDC), was recognized as a major component of the climate system, which affects radiative forcing (Lacis et al., 1990; Forster and Shine, 1997; Forster et al., 2007) and atmospheric circulation (Andrews et al., 1987; Holton et al., 1995; Salby and Callaghan, 2005, 2006). The increase of greenhouse gases, in particular the carbon dioxide (CO$_2$) concentration, affects the atmospheric temperature and wave propagation, which increases the tropical upwelling mass flux (Butchart et al., 2010; Garny et al., 2011; Abalos et al., 2015) and therefore changes the BDC. Within the context of climate change, the stratospheric circulation variability can also be
diagnosed using the trace gas CO$_2$.

CO$_2$ is a useful tracer of the atmospheric dynamics and transport because of its long lifetime in the troposphere and stratosphere where it has essentially no sources or sinks as it is basically chemically inert in the free troposphere. The only stratospheric source of CO$_2$ is a small contribution from methane oxidation that can reach up to 1 ppmv (i.e. parts per million per volume) (Boucher et al., 2009). CO$_2$ is regularly exchanged between four reservoirs: the biosphere (photosynthesis and respiration), the lithosphere (soil and fossil pool), the hydrosphere (surface and deep ocean), and the atmosphere with a much longer residence time in the oceans and soil than in the atmosphere. These exchanges are described as the carbon cycle. Anthropogenic emissions due primarily to deforestation and biomass and fossil fuel burning have systematically increased the mean CO$_2$ and modified its seasonal cycle during these last two decades (Tans and Keeling, 2015). With the influences of steady growth and seasonal variation, CO$_2$ concentrations in the atmosphere contain both monotonically increasing and periodic signals that represent stringent tests of stratospheric transport and stratosphere-troposphere exchange (STE) in models (Waugh and Hall, 2002; Bönisch et al., 2008, 2009).

Despite its potential to increase global change by cooling the stratosphere and warming the troposphere via the greenhouse effect, information on stratospheric CO$_2$ and its variability was sparse until recently. In recent years, in situ aircraft and balloon campaigns were implemented in order to measure a number of chemical tracers including CO$_2$. The in situ campaigns included SPURT aircraft measurements in the upper troposphere and lower stratosphere (UTLS) (Engel et al., 2006; Gurk et al., 2008), CONTRAIL (Sawa et al., 2008) and CARIBIC (Schuck et al., 2009; Sprung and Zahn, 2010). Although sporadic in time and space coverage, these in situ measurements were used to analyse the BDC changes (Andrews et al., 2001a; Engel et al., 2009; Ray et al., 2014), to validate chemistry-transport models (CTMs) (Strahan et al., 2007; Waugh, 2009) and to diagnose STE (Strahan et al., 1998; Hegglin et al., 2005; Hoor et al., 2005; Bönisch et al., 2009; Hoor et al., 2010; Bönisch et al., 2011).

The stratospheric overworld circulation changes that affect the extratropical UTLS were recently assessed by Engel et al. (2009) from balloon-based measurements of SF$_6$ and CO$_2$. The stratospheric mean age of the air, that is defined as the residence time of air parcels in
the stratosphere (Li and Waugh, 1999; Waugh and Hall, 2002; Butchart et al., 2010), was calculated by Ray et al. (2014) from the in situ balloon measurements of trace gases with an idealized model to identify the natural variability in the BDC and its significant linear trends. This study demonstrated the importance of reconstructed in situ measurements to validate the stratospheric representation in global CTMs and chemistry climate models (CCMs).

In addition to the very localized in situ observations, which have high spatial resolution, a large spatial and temporal coverage of CO₂ is obtained from space instruments such as the vertical nadir sounders TOVS (Chedin et al., 2002, 2003b), AIRS (Chedin et al., 2003a), SCIAMACHY (Bowman et al., 2000), IASI (Chedin et al., 2003a), GOSAT (Hammerling et al., 2012; Liu et al., 2014) and recently OCO-2 (Frankenberg et al., 2015). These spaceborne instruments essentially measure total column CO₂, weighted more by the lower and mid troposphere, hence they provide limited information on the upper troposphere and the stratosphere. Foucher et al. (2009, 2011) obtained five years of monthly mean CO₂ vertical profiles by analysing the ACE-FTS data (Bernath et al., 2005). The ACE-retrieved CO₂ shows qualitatively good agreement with in situ observations for the 2004–2008 time period and at the 50°N–60°N latitude bins. However, the retrieval sensitivity is limited and averages need to be performed on a large number of profiles.

Because of the limited observations, CTMs and Lagrangian transport models are a complementary and useful framework to widely diagnose the BDC and to represent the global transport and distribution of long-lived species, such as CO₂.

Previous studies using the two-dimensional CTM Caltech/JPL (Shia et al., 2006) and the three-dimensional CTM TM5 (Transport Model 5) (Bönisch et al., 2008) were unable to accurately represent the BDC. Bönisch et al. (2008) investigated the UTLS exchanges in a three-dimensional transport model using the observed CO₂ and SF₆ distributions and concluded that major disagreements between the model and observations occur in winter, where a too strong BDC leads to some overestimates of the CO₂, and in boreal summer, where the vertical transport is too slow in the upper troposphere. During autumn, the models showed an unrealistic persistent reverse gradient in the lower stratosphere, and during spring, the transport processes through the tropical tropopause are overestimated, inducing too high CO₂ values in the lower
stratosphere. Furthermore, many three-dimensional models are too diffusive and/or have too strong mixing when crossing the tropopause, which leads to an underestimation of the amplitude of the seasonal cycle in the column of CO$_2$ (Olsen and Randerson, 2004). Shia et al. (2006) suggested that the lack of a reliable representation of stratospheric influence on CO$_2$, e.g. intrusion and recirculation, could explain part of the discrepancy between a CTM and observations. The persistence of the inverted CO$_2$ gradient noted in these models can result in an underestimation of the exchange of air masses from the stratosphere to the troposphere in mid-latitudes during autumn. Due to the short time period of simulations, models also fail to calculate a reliable CO$_2$ seasonal cycle as well as STE. Shia et al. (2006) concluded that at least three years are required for the surface CO$_2$ to be transported into the upper troposphere and LMS then moved to the temperate and polar latitudes. In order to eliminate the spurious diffusivity effect, Lagrangian or quasi-Lagrangian models, such as TRACZILLA (Legras et al., 2005) and CLaMS (Chemical Lagrangian Model of the Stratosphere) (Pommrich et al., 2014), were widely used to investigate transport properties. The combination of these Lagrangian models with in situ observations to reconstruct chemical trace gas distributions has significantly contributed to our understanding of the mixing effects across the extratropical tropopause (Hoor et al., 2004; Pan et al., 2006; James and Legras, 2009), the filamentary structure in long-lived and short-lived species near the edge of the polar vortex (Konopka et al., 2003), the transport of long-lived species and CO from the tropical troposphere to the stratosphere (Pommrich et al., 2014) and on the processes that control UTLS composition (Riese et al., 2012).

The small-scale variability of CO$_2$, its strong gradients across the tropopause and the scarcity of suitable observations for validation purposes lead to a challenging task for CTMs and CCMs in reconstructing its distribution in the UTLS (Hegglin et al., 2008).

In this paper, our goal is to build a database of the monthly zonal mean distribution of CO$_2$ on a global scale extending from the upper troposphere to the stratosphere using backward Lagrangian trajectories. This product can be used to validate CTMs, CCMs, as a prior for inversion modelling and to analyse features of the STE as well as the stratospheric circulation and its variability.

The trajectory data set, on which this work is based, was used by Diallo et al. (2012) to study
the age of air and its variability in the stratosphere. We refer to this previous work for all related questions. The present study can also be seen as a further validation of Diallo et al. (2012).

We reconstruct a global distribution of CO$_2$ calculated over the time period 2000–2010 from a Lagrangian transport model driven by horizontal winds and diabatic heating rates representing the vertical velocity in the isentropic coordinate, from the ERA-Interim reanalysis provided by the European Centre for Medium Range Weather Forecast (ECMWF) (Dee et al., 2011). We describe the data and method used in this study in Sect. 2 and Sect. 3, respectively. The reconstructed CO$_2$ is compared with observations in Sect. 4. The global monthly distribution of the zonal mean CO$_2$ and its variability are discussed in Sect. 5. Finally, Sect. 6 provides further discussions and conclusions.

2 Data

The reconstruction of the global distribution of CO$_2$ from the upper troposphere to the stratosphere through the use of back trajectories requires the value of the CO$_2$ mixing ratio to be assigned at the lower tropospheric boundary. This is achieved by using two different types of CO$_2$ data: ground stations (Worden et al., 2015) and CarbonTracker (Peters et al., 2007). In addition, in situ measurements of CO$_2$ from balloons and aircraft were used to validate the reliability of the model reconstructions (Daube et al., 2002; Engel et al., 2009; Sawa et al., 2008).

2.1 Lower boundary condition of the backward trajectories

Two different observation-based data sets are used to assign CO$_2$ to air parcels transported along the backward trajectories. During the 1989–1999 time period, data from ground stations of the World Data Centre for Greenhouse Gases (WDCGG, http://ds.data.jma.go.jp/gmd/wdcgg/) are applied. The WDCGG is an international data centre participating in the WMO Global Atmosphere Watch. It provides extensive data from ground stations and aircraft measurements across the Earth that are non-homogeneously distributed. The monthly CO$_2$ data from ground stations
(e.g. Mauna Loa, South Pole and others) located at different latitudes were used to overcome the daily fluctuations of CO$_2$ in the atmospheric boundary layer. The criterion for selecting the ground stations is that they are remotely located with respect to localized anthropogenic sources. In highly industrialized regions, this criteria is performed by retaining only high altitude stations to neglect the variability from localized sources at ground level. The CO$_2$ data are averaged from pole to pole in latitude increments of 30° and over all longitudes to represent the global, free tropospheric CO$_2$ field. To better model the latitude dependence of the seasonal cycle and to overcome discontinuities, the averaged CO$_2$ data obtained are then interpolated linearly in latitude. Since the ground station locations are inadequate to define longitudinal variability, we use a constant CO$_2$ value at all longitudes for each latitude bin. According to CarbonTracker residuals against the NOAA North American aircraft network data at altitudes above the PBL (http://www.esrl.noaa.gov/gmd/ccgg/carbontracker/profiles.php), the mean error of CarbonTracker is less than 1.25 ppmv at 500 hPa. This error should be added, in mean square, to the error determined in this study as a result of model dispersion (Sect. 5.3).

For the 2000–2010 time period, we use CO$_2$ output from the coupled data assimilation system CarbonTracker with the TM5 transport model for the lower boundary condition (Huijnen et al., 2010). CarbonTracker produces full 3D dimensional output so the backward trajectories are assigned to daily CO$_2$ mole fractions based on the latitude and longitude (3° × 2° resolution) of the trajectory at the 5 km (500 hPa) level. The 5 km level was chosen to represent the well-mixed free troposphere. The CarbonTracker system assimilates CO$_2$ observations from atmospheric stations and optimizes underlying from the fluxes of the ocean, biosphere, biomass burning and fossil fuel usage. These data are meant to achieve a complete and realistic diagnostic of the lower atmospheric CO$_2$ and fluxes (CarbonTracker-2013B, www.esrl.noaa.gov/gmd/ccgg/carbontracker/). The version used in this study corrects an error in vertical mixing in the previous versions.

Admittedly, the reduced sampling of the pre-2000 period and the lack of zonal variability induces an increased uncertainty in our calculation. However, the zonal variability is largely filtered out in the upper troposphere and lower stratosphere, especially during winter. Moreover, we only provide CO$_2$ reconstructions for 2000–2010. During this period, the tropospheric
conditions are mostly determined by CarbonTracker output due to the fast transport time in the troposphere, and the zonal fluctuations are mostly washed out in the stratosphere. The influence of pre-2000 data then decays exponentially and almost vanishes after 2005.

2.2 In situ aircraft and balloon measurements

In the UTLS, there are strong horizontal and vertical gradients. These gradients may occur on a small scale and exhibit high temporal and spatial variability. In this study, we are interested in airborne measurements in order to validate our model as well as to characterize the stratospheric variability and mixing process. Aircraft observations have a vertical resolution of a few metres (during ascents and descents) and a horizontal resolution of a few hundred metres resulting from the high sampling frequency of these instruments (0.5–2 Hz). Therefore, the aircraft observations are able to sample the small-scale variability of the tracers.

The SAGE III Ozone Loss and Validation Experiment (SOLVE) sought to establish a comprehensive data set of UTLS trace gases and meteorological data in the northern polar regions, including latitudinal gradients across the polar vortex. Measurements were made in the Arctic high-latitude region during winter 1999–2000 using the NASA DC-8 and ER-2 aircraft, as well as balloon platforms and ground-based instruments. CO₂, CH₄ and N₂O were measured by several instruments and used to calculate a composite mean age (as in Andrews et al. (2001b), using earlier measurements).

In situ balloon-based CO₂ profile measurements are also used as a basis for comparisons with the reconstructed CO₂ from the Lagrangian transport model. The data sets used in this study are high-quality observations with sufficient altitude coverage. They are measurements of whole air samples collected cryogenically from balloons or in situ measurements on-board a balloon gondola (Engel et al., 2009; Ray et al., 2014). Four balloon flights were selected for which a full CO₂ profile is available: (1) at Ft. Sumner, New Mexico, USA (34.5°N) on 17 September 2004, (2) at Sanriku, Japan (39.33°N) on 30 May 2001, (3 and 4) at Aire sur L’Adour, France (43.75°N) on 24 September 2002 and on 9 October 2001, respectively. Note that most profile observations are from the May to October period, when stratospheric variability in the northern hemisphere is expected to be lower than during the winter period. The combined measurements
of CO$_2$ and SF$_6$ was used by Engel et al. (2009) to derive the mean age of the air, but here we focus on CO$_2$.

A further data set, based on the CONTRAIL experiment (Machida et al., 2008) was used in the validation process of the reconstructed CO$_2$ in the whole troposphere (6–13 km) from 20°S to 60°N during November 2005–2009. CO$_2$ mixing ratios were measured during regular flights by Japan Airlines from Japan to Australia, Europe, North America, and Asia with Continuous Measuring Equipment (CME) for in situ CO$_2$ observations, as well as improved automatic Air Sampling Equipment (ASE) for flask sampling [for more details about the instrument see Machida et al. (2002)]. This data set provides significant spatial coverage particularly in the northern hemisphere (Sawa et al., 2008).

3 Method of global CO$_2$ reconstruction

To calculate the global CO$_2$ distribution, air parcels are distributed from the upper troposphere to the stratosphere and integrated backward in time.

3.1 Global backward trajectory

Backward deterministic trajectories were calculated using the Lagrangian transport model, TRACZILLA (Legras et al., 2005), which is a modified version of FLEXPART (Stohl et al., 2005). TRACZILLA uses analysed winds to move air parcels in the horizontal direction and performs direct interpolation from data on hybrid levels. In the vertical direction, we used potential temperature coordinates and total heating rates. We denote the trajectories as diabatic following a convention established by Eluszkiewicz et al. (2000). At each level in the vertical, trajectories are initially distributed over a longitude-latitude grid with 2° resolution in latitude and an almost uniform spacing in longitude of 2°/$\cos(\phi)$, where $\phi$ is the latitude, generating 10,255 air parcels on each level from pole to pole. For the sake of simplicity, the vertical levels of the initial grid are chosen to be the hybrid levels of the ECMWF model. In order to encompass the whole stratosphere at any latitude and longitude, 30 levels from about 400 hPa
(varying according to the surface pressure) to 2 hPa were selected. Above 56 hPa, the hybrid levels are reduced to pure pressure levels. Trajectories ending below the tropospheric boundary condition at 500 hPa, at which we assign the free tropospheric CO2 to each trajectory, were discarded during the initialization. Trajectories ending above this boundary are integrated backward in time up to 10 years or until they cross the boundary condition. In practice, stratospheric trajectories reach this boundary shortly (less than two months) after crossing the tropopause. Ensembles of trajectories were launched at the end of every month over the period 2000–2010 (Diallo et al., 2012).

3.2 Calculation of global CO2

Once a parcel has reached the tropospheric boundary condition at 500 hPa at a given time and a given location, its CO2 mixing ratio is assigned according to the mixing ratio at that time and that location calculated from CarbonTracker and WDCGG. CarbonTracker was chosen when a back trajectory reached the tropospheric boundary after 1 January 2000 and WDCGG was chosen when it was impacted before this date. Since WDCGG provides surface data only, it was assumed that the vertical transport was fast in the lower troposphere and induces only a negligible bias at 500 hPa in the CO2 mixing ratio, which was well verified (not shown) in the inner tropical region where most parcels reach the boundary. The assigned value was then used to reconstruct the CO2 mixing ratio at the location and time of the trajectory initialization.

The monthly zonal mean CO2 for a given bin in latitude and altitude was calculated as the average over all longitudes of the trajectories initialized within this bin (Fig. 1). The latitudinal resolution of the bins is centred 2° equatorward of 68° and decreases near the poles (69°–73°, 73°–77°, 77°–81°, 81°–90°). For each date, the average is made over 180 air parcels at the equator and 67 air parcels at 68° N or S. Near the poles, towards which the number of trajectories launched per degree of latitude decreased to zero, larger intervals were chosen to maintain a sufficiently large number of trajectories in the bins. This calculation uses the same approach as Sect. 2.3 of Diallo et al. (2012). Further averaging over time is performed to improve statistics and to reduce noise. These averaging procedures are a simple way to account for mixing in the stratosphere and gather within each bin a distribution of air parcels with different histories.
As observed by Scheele et al. (2005), the number of backward trajectories launched at a given date and remaining within the stratosphere after some residence time, $\tau$, decreases exponentially with $\tau$. Diallo et al. (2012) showed that this relationship held for $\tau > 3$ yr with an exponential decay parameter ($b$) equal to $0.2038$ yr$^{-1}$ using ERA-Interim winds and heating rates. The standard deviation of the mean (where each month was considered separately) decayed at the same rate. After 10 years, 88% of the particles initialised in the stratosphere reached the troposphere. We followed Scheele et al. (2005) in using this property to correct the estimated CO$_2$ for the truncation of trajectory lengths at 10 years. If we define $G(J|t,\tau)$ as the probability density of the residence time $\tau$ at time $t$ for parcels launched in the bin $J$, the monthly mean stratospheric CO$_2$ mixing ratio is

$$\overline{\text{CO}_2(J,t)} = \int_0^{\infty} \text{CO}_2^T(t-\tau)G(J|t,\tau)d\tau.$$  

(1)

where $\text{CO}_2^T$ is the tropospheric mixing ratio of CO$_2$, which is assumed here to be uniform for simplicity. The truncated version of this integral, up to $t_f = 10$ yr, can be calculated explicitly from the backward trajectories as a mean for all parcels from bin $J$, which have hit the 500 hPa surface weighted by their proportion among all launched parcels in bin J. Assuming that $G(J|t,\tau) = G(J|t,t_f)\exp(-b(\tau-t_f))$ for $t > t_f$ with $\text{CO}_2^T$ governed by an annual modulation added to a linear growth, $\text{CO}_2^T(\tau) = p_0 + p_1 \cdot \tau + a_0 \cdot \cos(2\pi(\tau-\varphi))$, the monthly mean CO$_2$ mixing ratio can be estimated as

$$\overline{\text{CO}_2(J,t)} = \int_0^{t_f} \text{CO}_2^T(t-\tau)G(J|t,\tau)d\tau + \frac{G(J|t,t_f)}{b} \left\{ \left( p_0 + p_1 (t-t_f - \frac{1}{b}) \right) + \frac{ba_0}{b^2 + 4\pi^2} [b\cos(2\pi(t-t_f-\varphi)) + 2\pi \sin(2\pi(t-t_f-\varphi))] \right\}.$$  

(2)

where all times are in years. The contribution of the remaining air parcels after 10 years of backward motion was thus accounted for by the integrated term in Eq. (2) where $G(J|t,t_f)/b$ is the proportion of parcels in the bin that have not hit the 500 hPa surface at time $t_f$. The coefficients $\{p_0,p_1,a_0,\varphi\}$ are estimated by fitting the Mauna Loa CO$_2$ data. The correction can also
be applied below the tropopause as the only tropospheric parcels which live for 10 yr without hitting the 500 hPa surface are among those which have been entrained in the stratosphere.

### 3.3 Validations of the global reconstruction method

The reconstruction during SOLVE and in situ balloon campaigns are used to validate of the global reconstruction of CO₂ and the ability of TRACZILLA to reproduce the small-scale CO₂ variations along the flight tracks.

#### 3.3.1 Reconstruction of CO₂ along aircraft flight track and balloon profiles

The procedure used here differs from that of the global reconstruction described above in three main respects. First, the parcels were initialized at locations distributed along the flight track or the balloon profile. In the case of the ER-2 flights, parcels were released with the frequency of the measurement, that is at 0.25 Hz (Daube et al., 2002), amounting to 900 locations per flight hour. In the case of the balloon flight (Engel et al., 2009), the air parcels were distributed along the balloon profile with a frequency higher than the tracer measurements. Namely, they were released at 200 locations in the vertical, regularly distributed in log-pressure between 500 hPa and 1 hPa at the same latitude-longitude position as the balloon.

Second, we take into account that a single sample can be understood as a mixture of sub-parcels arising from a large number of origins. The simplest representation of this mixing is by a constant diffusion, which mainly acts in the vertical direction, and it is well known that such a process can be represented by a Wiener process. Therefore, following Legras et al. (2005), we released a large number of air parcels (200 for the ER-2 flights, 5000 for the balloon profiles) from each measurement location. The Lagrangian advection was modified such that on a time step \( \delta t \) the motion of a given parcel located in \( X \) is

\[
\delta X = u(X,t) \delta t + \delta \eta k
\]

where \( u \) is the wind fields, \( k \) is the vertical unit vector and \( \delta \eta = w(t) \delta t \) is the product of the time step \( \delta t \) and a Wiener process \( w \) approximated by 50 iterations of the white noise during
a time step. In the small $\delta t$ limit, this is equivalent to a diffusion $D = \frac{1}{2} < w^2 > \delta t$. The well-posedness in the backward time direction arises from the adjoint equation of the Green function of advection-diffusion [for more details see Legras et al. (2005)]. The value $D$ in the lower stratosphere was estimated (Legras et al., 2005; Pisso and Legras, 2008) by comparing the observed small-scale tracer fluctuations and their reconstructions. The resulting value is $D \approx 0.1 \text{m}^2\text{s}^{-1}$, which is applied to the whole atmosphere in the present study. Physically, this turbulent diffusion, which is about four orders of magnitude larger than the molecular diffusion of CO$_2$ in the air (Haynes and Lide, 2012, $1.6 \times 10^{-5}$ m$^2$ s$^{-1}$), accounts for the small-scale motion missing in the ERA-Interim reanalysis winds. It is noticeable that the diffusion is effective at dispersing the clouds of parcels emitted from a single location only for a few days, after which dispersion by the resolved wind strain dominates.

Third, the trajectories were integrated backward for six months, after which the CO$_2$ mixing ratio was assigned according to the zonal mean CO$_2$ value calculated from the global reconstruction at that time and at the locations of the parcels. The mean value and confidence interval were calculated over all the initialized particles. The air parcels that reached the 500 hPa level were assigned the CO$_2$ mixing ratio on that surface.

4 Comparison of observations and model reconstructions

In this section, we test the realism of CO$_2$ reconstructions against several observation data sets that span a large range of scales, geographical locations and altitudes.

4.1 SOLVE campaign

Figure 2 shows observed and reconstructed CO$_2$ mixing ratio time series from 16 flights during the SOLVE campaign. Figure 3 compares the observed versus reconstructed CO$_2$ mixing ratios for each flight along with correlation coefficients and mean distances ($\Delta$ in ppmv), defined as the sum of the absolute difference between the observed and the reconstructed values divided by the number of recorded values. The flight patterns include test flights at subtropical (11 De-
cember 1999, 16 December 1999, 06 January 2000) and mid latitudes (11 January 2000), transit flights between mid and high latitudes (14 January 2000, 16 March 2000), and flights inside the polar vortex or across its edge (all other dates). In nearly all of the flights the observed CO₂ falls within the 95% confidence interval of the reconstruction. It can be seen from Fig. 3 that the correlation is not a good indicator of the similarity between the observed and the reconstructed curves as it can be high due to trends even for cases that exhibit large differences such as 3 February 2000. The ∆ value is a much better metric of the agreement between the observed and reconstructed CO₂. In 6 cases out of 16, the agreement is excellent with ∆ ≤ 0.36 ppmv and the two curves agree fairly well even for the magnitude of small-scale fluctuations. In four other cases with 0.49 ≤ ∆ ≤ 0.61 ppmv, the two curves stay very close with only a few features missed by the reconstruction. In two other cases with 0.66 ≤ ∆ ≤ 0.67 ppmv the reconstruction shows some larger deviations from the observations. On 11 December 1999, the reconstruction missed the decrease in CO₂ as the plane ascended at the beginning of the flight and then stayed slightly too high for the subsequent horizontal lag. The 27 January 2000 case is a flight from the inside of the polar vortex to the outside, which was poorly reconstructed for the outside part between 10:30UTC and 13UTC. Using similar methods, Legras et al. (2005) showed that the stratospheric tracers O₃ and N₂O could be reconstructed for this flight, but also found a large standard deviation for the outside section where filaments of polar and extratropical air were interleaved. The flights with the largest discrepancies (∆ > 0.74 ppmv) on 14 January, 3 February, 7 and 16 March 2000 can be explained by flight tracks that followed the edge of the polar vortex. In these flights, the reconstruction is very sensitive to any misplacement of the vortex edge in the reanalysis and thus not useful as an evaluation of the reconstructed CO₂. In addition, it is important to emphasize that the value of the applied diffusion (D ≈ 0.1 m²s⁻¹) allows the reconstruction to fit the observed small-scale variability (∼ 1 km). See Legras et al. (2005) for a complete discussion on this matter.


4.2 Balloon vertical profiles

In order to test the reconstruction over a larger vertical range of altitude, Figure 4 shows a comparison of the vertical profiles of the reconstructed mean CO$_2$ by TRACZILLA with the observations of four mid latitude stratospheric balloon flights (Engel et al., 2009; Ray et al., 2014). For three of the cases, most of the measurements fall within the 95% confidence interval of the reconstructed profiles and the local maxima at 23 and 18 km on Fig. 4(c, d), respectively, are well reproduced. These three profiles have relatively large CO$_2$ mixing ratios in the troposphere in common, which decrease with altitude. However, the reconstructed profile on Fig. 4b is 1 ppmv smaller on average than the observed profile and misses the large fluctuations above 20 km. This flight was performed from Aire sur l’Adour (France) when a cold front crossed the region with strong local tracer gradients in the lower stratosphere as seen in the potential vorticity map shown in the panel. In order to test the spread induced by this meteorological structure, we have reconstructed 8 vertical profiles at 1° distance around the initial profile. However, the observed spread among this ensemble of profiles is too small to explain the discrepancy in Fig. 4b. Notice that SF$_6$ derived mean ages, are in good agreement with the reconstructed mean age of Diallo et al. (2012). Therefore, we are left without any satisfactory explanation for this case but to assume some undocumented instrument malfunction.

4.3 Temporal series

To obtain additional details about the upward propagation of the tropospheric CO$_2$ seasonal cycle into the LMS and to evaluate the model near the lower boundary condition and the tropical tropopause, we compare the time series of the reconstructed monthly mean CO$_2$ (Sect. 3.2) with the observations.

Figure 5a compares the time series of modelled monthly mean CO$_2$ with the measurements from CONTRAIL (Sawa et al., 2008, 2012) in the tropical region 10°S–20°N and in the vertical range 7–9 km between November 2006 and January 2010. The comparison shows the ability of the model to capture the tropospheric CO$_2$ seasonal variation and validates the tropospheric boundary condition.

15
Figure 5b compares the modelled monthly mean CO$_2$ time series in the altitude bin 16–17 km and between 10°S and 20°N just below the tropical tropopause, where the tropospheric air enters the stratosphere, with the average of ground-based CO$_2$ data from Mauna Loa (19°N) and American Samoa (14°S) delayed by 15 days. We find, consistent with Boering et al. (1996) and Andrews et al. (1999, 2001a,b), that the amplitude of the two signals is the same and we diagnose a delay of 2 months at a higher altitude in the layer 18–19 km (not shown) in agreement with Boering et al. (1996). The shorter time scale below the tropopause is in agreement with other studies (Bergman et al., 2012; Tissier and Legras, 2016).

Figure 5c shows the modelled monthly mean CO$_2$ in the latitude bin 50–60°N at different altitudes in the range 7–13 km between November 2005 and January 2010. These curves are compared with CONTRAIL measurements in the same latitude band (Sawa et al., 2008). The modelled and measured CO$_2$ differ by less than 1 ppmv except for a few isolated months such as March 2006 and March 2009 and outliers such as April at 12–13 km. There is a shift in the order of 4–6 months in the mean CO$_2$ seasonal cycle above 11–12 km, in the lowermost extratropical stratosphere, with respect to the tropospheric signal. This is due to the delay induced by the shallow branch of the BDC also found by Bönisch et al. (2009) and Sawa et al. (2008). The discrepancies are concentrated during the spring season, during which large gradients of CO$_2$ span the region, as discussed in Sect. 5.

5 Global distribution of zonal mean CO$_2$

The zonal mean distribution of CO$_2$ illustrates the main features of the BDC, such as mixing and transport variabilities through temporal and spatial evolution. Figure 6 illustrates the typical seasonal variation of the monthly mean CO$_2$ derived from the Lagrangian reconstruction for 2010 as an example among the 11 years.
5.1 Upper troposphere and lowermost stratosphere

The zonal mean distribution of CO$_2$ in the free atmosphere, especially above 5 km, is driven by the large-scale transport processes. Fast quasi-isentropic mixing is combined with upwelling in the tropics and downwelling in the extratropical lowermost stratosphere. Figure 6a shows the meridional and vertical CO$_2$ distribution during six different months in 2010. In the northern hemisphere, the tropospheric monthly mean CO$_2$ is dominated by a strong seasonal cycle reflecting the biospheric activity. The terrestrial vegetation removes CO$_2$ by photosynthesis during its growth phase and returns CO$_2$ to the atmosphere when it dies and decomposes. CO$_2$ concentration increases during autumn and winter to reach a maximum in April-May followed by a rapid decay due to the spring biospheric bloom and reaches a minimum in July-August. The cycle is much weaker in the southern hemisphere and is influenced by transport from the northern hemisphere. The combined effect of fast isentropic mixing (Haynes and Shuckburgh, 2000a,b) and convection (Sawa et al., 2008) propagates the cycle towards the tropics creating both a horizontal and a vertical gradient (Nakamura et al., 1991; Bönisch et al., 2009; Sawa et al., 2012). From Fig. 6a, it is clear that during the northern hemisphere winter the concentration tends to follow the isentropes in the extratropics for potential temperatures up to about 330 K. The barrier effect of the subtropical jet (Miyazaki et al., 2009) generates a strong meridional gradient near 30°N, which reaches a maximum near 350 K. Once it has reached the tropics, CO$_2$ is then transported upward by tropical convection and propagates into the stratosphere through the BDC. Throughout the summer (June, July and August), while the tropospheric CO$_2$ is removed from the atmosphere due to the biosphere activity, a layer of high CO$_2$ extends from the tropics to the northern mid-latitudes into the lower stratosphere driven by the lower branch of the BDC (Bönisch et al., 2008). This transport is promoted by the Asian monsoon anticyclone, which traps young continental air lifted from the surface and induces a flux to the extratropical stratosphere on its west side as it is eroded across the jet (Dethof et al., 2000; Bannister et al., 2004; Park et al., 2007b, 2008, 2009, 2010; Randel et al., 2010; Pan et al., 2016). Due to the turnover time of this transport, the maximum concentration of CO$_2$ in the northern lower stratosphere lags behind that at the surface by 4 to 6 months and this con-
concentration is reached basically when the surface concentration is at its minimum. The result is an inverted vertical profile, which is at its maximum in July and persists over the summer. A qualitative comparison between the reconstructed CO\(_2\) in Fig. 6a and observations from Sawa et al. (2008) (see their Figure 7) exhibits good agreement in the cycle of the tropospheric and lower stratospheric CO\(_2\) and in particular in the cycle of the inversion. There are, however, differences in the location and intensity of the meridional gradient, which might be due to the specific sampling by Sawa et al. (2008) and which gives a strong weight to the most intense region of the Pacific jet stream.

### 5.2 Middle and upper stratosphere

Figure 6b shows the CO\(_2\) global distribution in the middle and upper stratosphere up to 42 km for even months in 2010. As the tropospheric seasonal cycle is transported into the middle and upper stratosphere through the tropical pipe, its amplitude decreases upward because of the combined effect of the upwelling branch of the BDC and mixing processes. The deep branch of the BDC is much slower than the shallow branch and old air with low CO\(_2\) concentrations in the middle and upper stratosphere. Younger air with high CO\(_2\) is isolated in the tropical area, an effect which is at a maximum during northern hemisphere winter in agreement with the age of the air calculations (Li et al., 2012; Diallo et al., 2012). The horizontal mixing homogenizes CO\(_2\) in the mid and high latitudes during summer. Because of this prior mixing, the winter containment within the polar vortex generates only a weak polar minimum (and no localized horizontal gradient averaged over the latitude circle and do not follow the CO\(_2\) or potential vorticity contours).

### 5.3 Uncertainty about CO\(_2\) global distribution

Figure 6c shows the monthly averaged uncertainties about the reconstructed monthly zonal mean CO\(_2\) over the 2000–2010 period calculated from the trajectories. The uncertainty is estimated as the standard error of the mean by assuming that the contributing trajectories are independent samples. The standard error is performed for each month over 2000–2010. As an
illustration, the standard error is then averaged over 11 years (Figure 6c). The estimated CO₂ uncertainties reveal smaller values for the trajectories starting in the troposphere than the trajectories starting in the stratosphere, which have a longer transit time of several years to reach the lower boundary condition where the CO₂ value is assigned. As expected, the uncertainty roughly scales with the transit time of the trajectories from the upper troposphere to the stratosphere. The maximum uncertainty reaches 1 ppbv in the stratospheric polar regions where the mean age of the air reaches a maximum during winter and sampling is lowest. Note that the mean error of CarbonTracker on the initialization values should be added to this uncertainty from the spread of the trajectories.

5.4 Spring-summer vertical profiles

In this section, monthly averaged CO₂ profiles are investigated to better describe the changes in the CO₂ vertical structure within the upper troposphere and stratosphere. The spring-summer reconstructed vertical profiles of CO₂ are compared with those from the CONTRAIL aircraft measurements for the year 2007 in the 50–60°N latitude range (Fig. 7a). Good agreement is obtained, including for the inversion of the CO₂ vertical profile during August in the lower stratosphere. The monthly mean CO₂ vertical profiles, calculated by backward trajectories, exhibit a complex vertical structure with gradient layers interspersed with no gradient layers.

The annual structure of the profile is made apparent in Figure 7b where we show averaged monthly profiles over the period 2000–2010 after removing the mean CO₂ trend at each level. Starting from January, the increase of CO₂ in the troposphere penetrates upward in the stratosphere over the limited vertical range of the Extratropical Transition Layer (Hegglin et al., 2010; Gettelman et al., 2011), which is over 2 to 3 km above the tropopause as is visible in the March profile. Between March and May, another process occurs, which injects young air rich in CO₂ above 13 km. This can only be due to a tropical intrusion promoted by the weakening of the tropical barrier at the end of the winter. The profile suggests (i) that the intrusion is deep from 13 to about 23 km, (ii) that the well-mixed layer between 13 and 16 km is influenced by the well-mixed tropical tropospheric profile at such altitudes and (iii) that the mixing layer between
16 and 23 km is also induced by the tropical lower stratosphere vertical gradient. The mixing layer persists with the same slope during the whole summer and the bottom of the intrusion corresponds to the maximum of CO$_2$ when the inversion is at its maximum. During fall, when the subtropical barrier is re-established, the gradient weakens, the residual well-mixed layer disappears and the profile returns to the fairly uniform slope of January.

6 Conclusions

Our study provides a monthly zonal mean distribution of CO$_2$ spanning the upper troposphere and the stratosphere over the time period 2000–2010, established from observations and the state-of-the-art reanalysis ERA-Interim. The zonal mean distribution of CO$_2$ is a unique data set of a critical trace gas that has a variety of uses for validating the representation of upper tropospheric and stratospheric tracer distributions in chemical transport models and chemical climate models, in particular regarding the summer inversion of the CO$_2$ profile in the northern hemisphere. This CO$_2$ product is also intended for satellite validation in the upper troposphere and the stratosphere, used as a preliminary process before (a prior) for inversion modelling and to analyse features of the stratospheric-tropospheric exchange as well as the stratospheric circulation and its variability. The reconstructed CO$_2$ product contains zonal mean, monthly mean mixing ratios in 77 latitude bins from 90°S to 90°N and 36 vertical levels from 5 to 42 km. This reconstructed monthly zonal mean CO$_2$ exhibits a remarkable agreement with CONTRAIL data as well as with SOLVE and in situ balloon measurements.

The comparison with SOLVE shows that a Lagrangian-diffusive model is able to reproduce the mean value and the amount of small-scale fluctuations that are recorded by in situ measurements along flight tracks in the lower stratosphere. This reconstruction suggests that the distribution of long-lived tracers, such as CO$_2$, can be fully explained by the properties of transport as resolved by meteorological analysis or reanalysis and a simple representation of sub-grid scale effects as a diffusion.

In the northern hemisphere troposphere, the monthly mean CO$_2$ is dominated by biospheric activity and displays a strong seasonal cycle, which is vertically and horizontally propagated.
to the tropopause and above in the lowermost extratropical stratosphere, on the one hand, and to the tropics, on the other hand, where it reaches the tropopause and enters the stratospheric Brewer-Dobson circulation. In regions of high horizontal mixing such as the mid-latitudes, \( \text{CO}_2 \) tends to be uniformly mixed at isentropic surfaces and its meridional gradients are meridional gradients are enhanced near transport barriers such as the subtropical jet during winter.

Transport of \( \text{CO}_2 \) into the northern extratropical stratosphere above the lowermost stratosphere is due to the export of tropical air. The long circuit of \( \text{CO}_2 \) from the extratropics to the tropics in the troposphere and then back to the extratropics in the stratosphere induces a time lag of 4–6 months such that the tropospheric and stratospheric variability are almost opposite at mid latitudes. The result is the production of an inverted vertical \( \text{CO}_2 \) profile during summer. In the mid and upper stratosphere, we found that as the tropospheric seasonal cycle is transported into the stratosphere through the tropical pipe, its amplitude is smoothed out because of the combined effect of the upwelling branch of the BDC and quasi-horizontal mixing. A more confined tropical pipe is found in the tropical band during the winter and spring than during summer and autumn.

Acknowledgements. We particularly thank Y. Sawa, H. Matsueda and T. Machida for providing \( \text{CO}_2 \) measurements from CONTRAIL, the ECWMF for providing reanalysis data, WDCGG (http://ds.data.jma.go.jp/gmd/wdcgg/) and its contributors for providing the ground station \( \text{CO}_2 \) data from 1989–1999, nd the CarbonTracker team for providing the \( \text{CO}_2 \) data from 2000–2010. We thank Harald Bonisch and Alain Chédin for comments and helpful discussions. We acknowledge support from the EU 7th Framework Program under grant 603557 (StratoClim). M. Diallo was mainly supported by a postdoctoral grant from the ExCirEs Project (CGL2011-24826) funded by the Government of Spain. Further thanks are due to the CICLAD cluster at the Institut Pierre Simon Laplace in Paris, on which most parts of this work were carried out. The TRACZILLA model \( \text{CO}_2 \) data set may be requested from the corresponding author (mdiallo@lmd.ens.fr/m.diallo@fz-juelich.de) before may publically available to the scientific community on Earth System Science Data (ESSD).
References


Chedin, A., Serrar, S., Scott, N. A., Crevoisier, C., and Armante, R.: First global measurement of


James, R. and Legras, B.: Mixing processes and exchanges in the tropical and the subtropical UT/LS,


Fig. 1. A schematic representation of the backward Lagrangian trajectories of air parcels starting in a (latitude \(\times\) longitude \(\times\) altitude) grid box. Here the longitudinal extend of the box should be seen as the whole latitudinal circle.
Fig. 2. Comparison of the reconstructed monthly mean CO$_2$ from backward trajectories with aircraft measurements from SOLVE campaign (Daube et al., 2002). (Black): reconstructed mean CO$_2$ along the ER-2 flight track using the TRACZILLA Lagrangian transport model. (Red): observed mean CO$_2$. (Green): potential temperature of the ER-2 flight track. The gray shading area indicates the 95% confidence interval calculated from the reconstruction.
**Fig. 3.** Comparison of the reconstructed monthly mean CO$_2$ from the backward trajectories with aircraft measurements from SOLVE campaign (Daube et al., 2002). Colors indicate different flights in Fig. 2. R-squared and the $\Delta$ (in ppmv) defined as the mean of the absolute value of model–observations differences are shown in the legend. The dashed line is the 1:1.
Fig. 4. Reconstructed vertical profiles of the monthly mean CO₂ compared with each in situ stratospheric balloon observations of CO₂ (Engel et al., 2009). (Black curves): reconstructed vertical profiles of mean CO₂. (Green squares): in situ balloon measurements of mean CO₂. (Gray shading): 95% confidence interval from the reconstruction. The measurements were taken from Sanriku, Japan (39.33°N) on 30 May 2001 (a), Aire sur l’Adour, France (43.75°N) on 9 October 2001 (b) and on 24 September 2002 (c) and Ft. Sumner, New Mexico, USA (34.5°N) on 1 September 2005 (d), respectively. The different dashed lines show the 8 reconstructed other profiles surrounding the measurement on 9 October 2001. The insert on the upper right panel shows the potential vorticity (in PVU) on the 70 hPa surface for 9 October 2001 at 12UTC over France from ERA-Interim. The location of Aire sur l’Adour is indicated by a diamond.
Fig. 5. Temporal evolution of the monthly mean CO$_2$ seasonal cycle from TRACZILLA calculations (line) compared with CONTRAIL and ground measurements (circle). (a): Comparison model with CONTRAIL in the tropospheric region above the tropospheric boundary in the latitude range 10°S–20°N. (b): In the upper tropospheric region close to the tropical tropopause and the latitude range 10°S–20°N, comparison with the average of surface station data at Mauna Loa, Hawaii (19°N) and American Samoa (14°S) delayed by 15 days. (c): Comparison model with CONTRAIL in the upper troposphere near the extratropical tropopause at 50°N–60°N and at several heights from 7 to 15 km. The error estimated from the reconstruction is indicated as vertical gray bars.
Fig. 6. (a) Global distribution of the seasonal cycle of the reconstructed monthly mean CO₂ (in ppmv) in the upper troposphere and the lower stratosphere from 5 to 25 km for the odd months of 2010. (b) Same as (a) but for the even months of 2010 and the altitude range from 5 to 45 km. CO₂ calculated on model levels is first interpolated to altitude levels using the latitude dependency of the zonally and monthly averaged geopotential. (c) The standard error of the mean CO₂ over the 2000–2010 period. The white contours show the isentropic surfaces.