

1    Supplement:

2    **Detailed Methodology**

3       The buoyancy flux parameter ( $F_B$ ) **Equation A1** is a function of the temperature difference between the air  
 4       ( $T_A$ ) and the fire ( $T_F$ ), the vertical motion of air ( $v$ ) and the size of the fire,  $d$  (here always measured at  $1\text{km}^2$  in  
 5       this work).

6       
$$F_B = gv \frac{d^2}{4} \left( \frac{T_F - T_A}{T_A} \right) \quad (\text{A1})$$

7       The buoyancy flux parameter has been found empirically to demonstrate whether the plume rise is buoyancy or  
 8       momentum dominated. Under stable atmospheric conditions [Stone and Carlson, 1979], where the atmospheric  
 9       lapse rate is ( $L_A = \frac{\Delta T}{\Delta Z} < -5$ ), for a buoyancy dominated plume, (defined as where the difference between  $T_A$  and  
 10       $T_F$  is given in **Equation A2b1**), the plume rise height ( $\Delta h$ ) is given by **Equation A2b2**, where ( $U$ ) is the  
 11      horizontal wind magnitude.

12      
$$(T_F - T_A) > 0.01958T_F\sqrt{v} \quad (\text{A2b1})$$

13      
$$\Delta h = 2.4 \left( \frac{F_B}{0.02U} \right)^{1/3} \quad (\text{A2b2})$$

14       Whereas, for a momentum dominated plume (where the difference between  $T_A$  and  $T_F$  is less than the right hand  
 15      side of **Equation A2b1**), the height rise is given by **Equation A2b3**.

16      
$$\Delta h = 1.5 \left( \frac{v^2 d^2 T_A}{\frac{4}{\sqrt{0.02}} T_F} \right)^{1/3} \quad (\text{A2b3})$$

17       On the other hand, under unstable atmospheric conditions (where  $L_A > -5$ ), and where the plume rise is  
 18       buoyancy dominated, the plume rise height is given by either **Equation A2b4** when  $F_B > 55$  or **Equations**  
 19       **A2b5, A2b6** when  $F_B < 55$  [Woodward, 2010].

20      
$$X^* = 14F_B^{\frac{5}{8}} \quad (\text{A2b4})$$

21      
$$X^* = 34F_B^{\frac{2}{5}} \quad (\text{A2b5})$$

22      
$$\Delta h = 1.6 \frac{F_B^{\frac{1}{3}} (3.5X^*)^{\frac{2}{3}}}{U} \quad (\text{A2b6})$$