A new downscaling method for sub-grid turbulence modeling

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Abstract.

In this study we explore a new way to model sub-grid turbulence using particle systems. The ability of particle systems to model small scale turbulence is evaluated using high resolution numerical simulations. These high-resolution simulations have been performed with the research atmospheric model Meso-NH and averaged at larger scale from which a complete downscaling experience, via a particle system, have been performed. The particle simulations are compared to the high-resolution simulation for the representation of the wind fluctuations and the turbulent kinetic energy. Despite the simplicity of the physical model used to drive the particles, the results show that particle system is able to represent the average field. It is shown that this system is able to reproduce much finer turbulent structures than the numerical high-resolution simulations. In addition, this study provides an estimate of the effective spatial and temporal resolution of the numerical models. This highlights the need for higher resolution simulations to be able to evaluate the very fine turbulent structures predicted by the particle systems. Eventually a study of the influence of the forcing scale on the particle system is presented.

1 Introduction

Following the increase in computing power, the resolutions of meteorological model have increased steadily over the past years. The refinement of the temporal and spatial resolution of atmospheric model requires a finer and finer representation of physical phenomena. The current weather forecast models have a kilometric resolution. However, the small processes, which have local effects, are still sub-grid processes in such models. Thus they are subject to physical parametrization.

The sub-grid modeling issue concerns many meteorological research fields, from snow pack modeling to cloud cover modeling. A particularly delicate matter is to model the turbulence in the Atmospheric Boundary Layer (ABL). In the ABL there is a transfer of energy from kilometric scales to metric scales. This transfer is called the energy cascade. Thus whatever the model resolution, some turbulent processes are sub-grid processes. For numerical weather forecast models, the processes associated to kilometric scales are not resolved yet. For instance, a recent study shows that these processes are not resolved by AROME Airport which has a horizontal resolution of 500 meters (Hagelin et al., 2014). As the local turbulence is a pilot of the local atmosphere evolution, for high resolution modeling a key point is to use a good turbulence parametrization. For instance, recent studies have shown the influence of the turbulence parametrization on the cloud modeling in tropical regions (Machado and Chaboureau, 2014). Several field experiments have helped to understand the influence of small scale turbulence on local weather conditions – the erosion of the nocturnal valley inversion for instance (Rotach et al., 2004; Drobinski et al., 2007; Rotach et al., 2008). The Passy field experiment which took place during the winter 2014-2015 in the Northern Alps aims at improving the understanding of the atmospheric dynamics during wintertime anticyclonic condition (Paci, 2015). In such meteorological conditions, the small scale turbulence influences the dissipation of cold air masses and has a major role in the air pollution dispersion.

Because of their variability and their sensitivity to local conditions, these turbulent phenomena are especially difficult to model. Instead of a larger decrease of the grid size, we suggest here another way to model sub-grid turbulence. In this paper, we present a stochastic downscaling approach. Our method is based on particle systems that are driven by a local turbulence model. Those particles are embedded in grid cells (illustration 1). From the mathematical point of view, the particles sample the probability density function (pdf) of the sub-grid wind. The description of sub-grid processes based on their pdf has been introduced by Sommeria and Deardorff since 1977 (Sommeria and Deardorff, 1977).
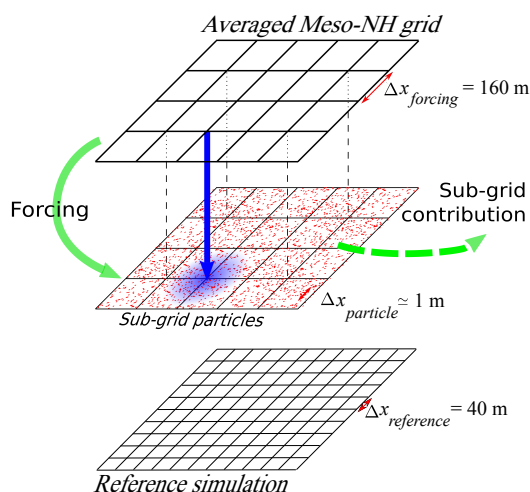
Figure 1. The downscaling experience. Averaged fields are used to force a sub-grid particle system. The sub-grid fields are compared to a reference Meso-NH simulation.

The Gaussian approximation they made to describe the liquid water content has then been extended to other variables. Nowadays, this kind of approximation is still widely used for sub-grid modeling (Larson et al., 2002; Perraud et al., 2011; Larson et al., 2012; Jam et al., 2013; Bogenschutz and Krueger, 2013). The method we suggest differs from these previous works : no assumption is made on the pdf shape. The particles give access to a discrete representation of the pdf. The pdf time evolution is thus given by the particle evolution.

In order to keep the average particles behavior consistent with the grid-point model, some grid-point fields are used as an external forcing on the particle system. The grid-point fields provide the values of the control parameters of the particle evolution model. This forcing is constant during the grid-point model time step and is applied every time new values are available. However, the particle evolution is performed at a shorter time step. Thus, the suggested downscaling method enables to refine both time and space scales.

In this work, the French research model Meso-NH is used to obtain high resolution grid-point fields. The chosen simulations have been performed for the BLLAST experiment (Lothon et al., 2014). Therefore we have used simulations and observations of real turbulent ABL to develop a stochastic downscaling method suitable for limited area model.

First the framework is presented. The BLLAST field experiment and the experience of particle system and grid-point model coupling are introduced. A description of the models follows in the section 3. Then section 4 details the forcing procedure. A brief presentation of the turbulent kinetic energy computation is given in section 5. The results obtained using the suggested downscaling method are then presented. We finally discuss their sensitivity to the resolution of the forcing fields in section 7.

2   The framework

2.1   The BLLAST experiment

The BLLAST (Boundary Layer Late Afternoon and Sunset Turbulence) field campaign was conducted from 14 June to 8 July 2011 in southern France, in an area of complex and heterogeneous terrain. The BLLAST experiment resulted from a collaboration of several European laboratories spearheaded by the Laboratoire d'Aérologie. The experiment aim is to study the turbulence in the boundary layer during the late afternoon transition (Lothon et al., 2014).

To perform this study, all turbulence sources were investigated. A wide range of integrated instrument platforms including full-size aircraft, remotely piloted aircraft systems (RPAS), remote sensing instruments, radiosoundings, tethered balloons, surface flux stations, and various meteorological towers were deployed over different surface types (Pardyjak et al., 2011). In addition to the numerous observations, high resolution simulations of the boundary layer have been done using Large Eddy Simulation (LES) models. Then the model ability to simulate turbulence has been evaluated (Jimenez et al., 2014).

The BLLAST experiment addresses a wide range of scientific issues such as the turbulence decrease (Darbieu et al., 2015), or the wind direction variability (Nilsson et al., 2014). The diversity of the available observations and simulations, and the dynamism of the BLLAST community lead us to choose this experiment to develop the presented downscaling method.

2.2   The coupling experience

Our experience is a first step in coupling particle systems and grid-point models. Here, we work on the downscaling from the grid-point model to the particle system in one way, so the information flow goes only from the grid-point model to the particles. We have used simulations of convective boundary layer to force a particle system which models sub-grid turbulent phenomena.

The particle systems are forced with a large scale grid-point meteorological fields. The large scale used in our work is later described in details. The aim of the experience is to compare the turbulent fields represented by the particles to the same fields simulated by a fine grid-point simulation.

The experience holds in three steps as outlined in figure 2. First, we have performed high resolution simulations with the model Meso-NH. These simulations are the finest available simulations. So they are considered as a reference and represent the real atmosphere. The fine simulations are not directly used to force the particles. Thus, they can be used to
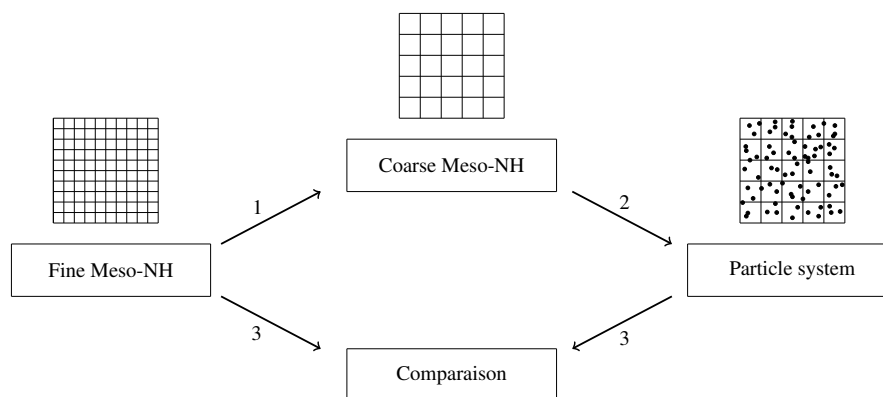
Figure 2. Our study framework. We use a fine model, which is degraded to get a coarse one. Particles are forced with coarse fields. Then we compare fine fields to particle fields.

independently assess the turbulence modeled by the particle system.

Now that we have a reference simulation, a coarser simulation is built in order to force the particle system. To this end, we have chosen to average the grid-point fields on few cells. To be consistent, we have also applied a temporal average. The obtained coarse Meso-NH fields have thus lower spatial and temporal resolutions than the reference simulation while being consistent with it.

In each cell of the coarse grid and during each coarse time step, the particle average behavior is forced. If the forcing method works, the average of the particles should be in good agreement with the coarse fields.

To assess the method, we have worked on wind fields and turbulent kinetic energy (TKE) fields. As it is explained in section 4, the TKE and the horizontal wind are not directly forced by the coarse model. The models and the data we used are presented in the two following sections.

3 Models

Now that the global framework is given, let us introduce the two models used in this work. First the grid point model is presented. Then the focus is put on the particle system and its evolution model.

3.1 Grid-point model Meso-NH

To perform the grid-point simulation of the ABL, we have used the research model Meso-NH. It is a non-hydrostatic mesoscale atmospheric model jointly developed by the Laboratoire d'Aérologie and by CNRM-GAME (Lafore et al., 1997). It incorporates a non-hydrostatic system of equations, and deals from large (synoptic) to small (large eddy) scales. Meso-NH has a complete set of physical parametrizations for sub-grid modeling. The Meso-NH model is thus a reference tool to model turbulence. It has already been used to evaluate the quality of the turbulence representation in models at kilometric scale (Honnert et al., 2011). Futhermore, Meso-NH can be used in a LES mode (Couvreux et al., 2005). Then its high effective resolution enables to model the main turbulent processes.

The equation system resolved by the Meso-NH model is an approximated form of the Durran (1989) version of the anelastic system. Meso-NH is an Eulerian model which uses a fourth-order centered advection scheme for the momentum components and a finite-volume method for advection of meteorological variables (e.g. temperature, water species, turbulent kinetic energy) and passive scalars (Colella and Woodward, 1984). In order to suppress the very short wavelength modes, the model uses a fourth-order diffusion scheme applied only to the fluctuations of the wind variables.

For our simulations, the 3D turbulence scheme is a one and a half order closure scheme (Cuxart et al., 2000). Thus the sub-grid TKE is a prognostic variable whereas the mixing length is a diagnostic variable. The mixing length and the dissipative length are computed separately according to Redelsperger et al. (2001). The mixing length is given by the mesh size depending on the model dimensionality. This length is limited to the ground distance and also by the Sommeria and Deardorff (1977) mixing length, which is pertinent in the stable cases.

All the BLLAST simulations used here have been performed with the 4.9 version of Meso-NH.

3.2 Meso-NH simulation

As Meso-NH is a research model, its grid size and its time step may differ from one simulation to an other. For the simulation used here, the horizontal grid size is $\Delta_x = 40$m, and the vertical one is $\Delta_z = 12$m. This simulation uses the set up of Darbieu et al. (2015), and uses a 256x256x256 points
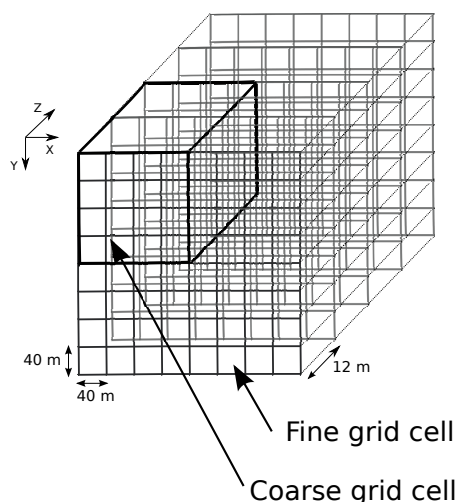
Figure 3. The domain of simulation : 8x8x4 fine cells which are grouped in 2x2x2 coarse cells.

domain with cyclic conditions. The simulation starts at 06h00 and lasts 15 hours. Because of the high computational time of the simulations, we present here only 15 minutes of simulation with a $\delta_t = 5$s time step. Moreover, to avoid the explosion of the computational time of the forcing procedure, we have only kept a 8x8x4 grid points. The first vertical level altitude is around 360 meters. The data are chosen in the middle of the ABL for two reasons. First, at these heights, issues linked to the vicinity of the ground are avoided. In addition, in convective conditions, the turbulence is well established in the middle of the ABL. In the following sections, this configuration of Meso-NH is called the fine reference configuration. It will be used to evaluate the fields reconstructed with the particle system.

To force the particles, averaged fields are used. They are deduced from the reference fields. The averaged fields, called coarse fields, are obtained by averaging several grid points, on 12 time steps (Δ_t=1min). Each average is made on a 4x4x2 grid-points domain (figure 3). So, the coarse grid size is 160mx160mx24m.

We have selected data from 13h55 to 14h10 during the convective period, the 06/20/2011. Among all the available variables in Meso-NH, we have extracted the atmospheric pressure, the 3 components of the wind, the TKE and the eddy dissipation rate (EDR), for the reference configuration. The pressure gradient is computed using the pressure field. The previously described average has been applied to these reference fields to obtain the coarse fields. We underline that only the coarse fields are used to force the particle system. The reference fields are simply used to evaluate the fields obtained from the particles.

To ensure its consistency with the real case, the high resolution Meso-NH simulation has been compared to another LES simulation performed with the LES model of the National Center for Atmospheric Research (NCAR) for the same case and shows close results (Darbieu et al., 2012)

3.3 The particle system

In order to model the sub-grid processes, an applied mathematical technique is used : the probability density functions are described using a particle system. In this experience, the particles sample the wind probability density function. The particle technique is widespread in research fields such as mechanical system modeling (automotive, aeronautics), but it is not yet currently used for atmospheric modeling. However, particle models for dispersion have been discussed for quite a long time. Guidelines to evaluate the relevance of a stochastic model have been given by Thomson (1987), and different particle pair models for dispersion and concentration fluctuations are described in Thomson (1990) and Durbin (1980). These models have then been improved and generalized to particle system models for dispersion and air pollution modeling (Uliasz, 1994; Stohl and Thomson, 1999).

Here, a particle is a realization of the surrounding atmosphere. Depending on the complexity of the evolution model, the particles carry physical properties, such as fluid velocity, temperature or humidity rate. In our experience, the evolution model is simple, and each particle is a position/velocity couple. Using the particle approximation of the probability density function and the physical properties of the particles, the statistics of the turbulence are computed. In particular, the wind variance can be computed. Thus using the particle wind, the TKE is directly available.

The suggested stochastic downscaling method completes the long list of downscaling techniques developed to improve geophysical model resolutions. Among them, we find the adaptive mesh refinement for oceanic and atmospheric models (Blayo and Debreu, 1999; Debreu et al., 2005; Andrews, 2012). Our downscaling method offers an other point of view. Instead of refining the grid, the sub-grid atmosphere is modeled using a particle system which lives inside the grid cells.

Previous studies have already explored stochastic downscaling methods for the meteorological model MM5 (see Rousseau et al. (2007), Bernardin et al. (2009), and Bernardin et al. (2010)). As these studies, our work aims at modeling the wind at very small scales on a limited area. The same particle evolution model is used. In these studies, the downscaling is performed by imposing the boundary conditions. The conditions are given by a large scale Eulerian model. It ensures the consistency of the particle system with the large scale model. Moreover, it enables to keep particles inside the simulation domain. Indeed, the forcing induces a reflection of the particles against boundary.

Different choices have been made to develop the presented downscaling method. We have chosen to force the particles cell by cell using the grid-point fields, but there is no imposed condition to the edge of the domain. The particles live freely in the domain and may go from one cell to another. When some particles go out the domain, they are deleted and replaced by new particles inside the domain. For each new particle, the particle position is randomly chosen. Then the new particle velocity is computed using the velocities of the particles which are in the same cell. Thus the particle system contains information relative to different scales, including local components of the fields associated to sub-grid scale and large or mean components coming from the forcing, associated to the grid scale.

To compare the fields represented by the particles to the grid-point fields modeled with Meso-NH, an average on the particle values is made cell by cell. For instance, the wind $\mathbf{V}_\alpha$ represented by the particles in the cell α is given by the following expectation :

$$\mathbf{V}_\alpha = \frac{1}{N} \sum_{i=1}^{N} \mathbf{V}_\alpha^i$$

where N is the number of particles in the cell α, and $\mathbf{V}_\alpha^i$ is the velocity of the particle i. If the sub-grid processes are rightly modeled by the particle system, the fields represented by the particles should be similar to the fine Meso-NH fields. The results of the sub-grid modeling are presented section 6. They are obtained with 75 particles in each fine grid cell. Thus the whole system contains 19200 particles.

3.4 The Stochastic Lagrangian Model

For the particles to be realizations of the surrounding atmosphere, the particle evolution is driven by a local turbulence model. It is a Stochastic Lagrangian Model (SLM) inspired from Pope (2000) and introduced for atmospheric turbulence estimation purpose by Baehr (2009, 2010). The model is consistent with the Kolmogorov laws for turbulence (Kolmogorov, 1941). It describes the evolution of the position, X, and the 3D velocity of each particle. The position evolution is done by integrating the velocity. The velocity is split in one term for the horizontal velocity, V, and an other for the vertical velocity, W. Their evolutions depend on the local properties of the atmosphere and also on the atmospheric large scale characteristics.

In the evolution equations, the large scale influence is given by the pressure gradient $\nabla_x \overline{p}$ for the horizontal velocity, and by the mean vertical velocity increment $\Delta_k W$ for the vertical velocity. The velocity evolution depends on the local properties through a term of wind fluctuation around the locally averaged wind, $<V>$ and $<W>$. The local average operator $<.>$ is described in the next section. Then, for the vertical velocity, the buoyancy effect is taken into account. The last term of the equations is a dispersion term. It is rep-

resented by a Wiener process $\Delta B^\bullet$ normalized by the time step δt. Finally, the SLM equations are given by :

$$\begin{cases} X_{k+1} &=& X_k + \mathbf{V}_k \, \delta t + \sigma^X \Delta B_{k+1}^X \\ V_{k+1} &=& V_k - \nabla_x \overline{p} \, \delta t \, - \, C_1 \frac{\varepsilon_k}{K_k} \left[V_k - <V> \right] \delta t \\ && + \sqrt{C_0 . \varepsilon_k} \, \Delta B_{k+1}^V \\ W_{k+1} &=& W_k + \Delta_k W \, - \, C_1 \frac{\varepsilon_k}{K_k} \left[W_k - <W> \right] \delta t \\ && + \frac{g}{\beta} \Gamma_k^\theta \, \delta t + \sqrt{C_0 . \varepsilon_k} \, \Delta B_{k+1}^W \end{cases}$$

where g is the standard gravity, ε_k is the EDR and K_k the TKE. C_0 is the constant of Kolmogorov. The constant C_1 is given by $C_1 = \frac{1}{2} + \frac{3}{4} C_0$ as Pope suggested it (Pope, 1994).

The buoyancy effect term $\frac{g}{\beta} \Gamma_k^\theta$ is not directly modeled here. It is replaced by a random variable. We have chosen to use a centered Gaussian variable. This choice has been done for a sake of simplicity. However an equation for the temperature evolution may be added to improve the buoyancy effect modeling.

The stochastic Lagrangian model has two control parameters for the velocity equation. The EDR, ε, and pressure gradient, $\nabla_x \overline{p}$, are the control parameters for the horizontal velocity. For the vertical velocity, they are the EDR ε and the velocity increment $\Delta_k W$. In our downscaling method, they are given by the Meso-NH coarse simulation : it is how the coarse model forces the particle system. The two control parameters are related to the different scales modeled in the Meso-NH simulation. The pressure gradient and the vertical velocity increment are related to large scales, whereas the EDR is related to small scales. Thus each parameter is associated to an extremity of the energy cascade described by Kolmogorov. We underline that the EDR used to force the system is a diagnostic variable of Meso-NH. Therefore, it is computed using a closure scheme. This choice is discussed in section 8. Contrary to the EDR, the TKE, noted K in the equations, does not come from the Meso-NH simulation. Instead we use the TKE computed using the particle system and the local average operator described in the next section.

3.5 Structure function computation

As we have seen, the SLM equations contain some locally averaged terms. In our framework, the fields are represented by the particle system. Thus only discrete representations on irregularly spaced points of the fields are available. It leads to a tricky implementation of the average. A regularization function G^δ is introduced. To compute the average at a point x, this function gives a weight to the particles depending on their distance to x. Then the local average is the weighted average of the particle values. The regularization function G^δ is a Gaussian which is centered at the computation point x. The variance of the function is noted δ^2. The standard deviation δ is a length which depends on the homogeneity of the medium. Therefore, if the medium is homogeneous, the average can be computed using all the particles. In this simple case, the length δ can be long. On the contrary, if the medium presents strong spatial variations, only very close points have

to be taken in account to get a representative average. Then the length δ has to be short.

To validate the downscaling method, the particle fields are compared to the fine Meso-NH simulation. In a grid-point model, the characteristic length of the modeled processes is twice larger than the grid size according to the Shannon's theorem (Shannon, 1949). Thus the grid size may be seen as the characteristic length, and we set the length δ at the finest Meso-NH grid size. As the horizontal grid and the vertical grid have different sizes, the horizontal characteristic length is set at $\delta_h = 40$m and the vertical one is set at $\delta_v = 12$m.

The average operator is used to compute any needed structure functions. In particular the velocity variance may be computed using the local average and the particle system. The TKE is thus available at each time step. The structure function computation is independent of the forcing model grid. The particle system is viewed as a whole, and the local average may be computed using particles which are in different cells. To compare the particle TKE to the TKE simulated by Meso-NH, the particle values are averaged cell by cell as explained in section 3.3.

4   The particle system forcing

The aim of this work is to study the ability of a particle system forced by grid-point data to model the sub-grid processes. To do so, we use two grid-point simulations : a coarse one to force the particle system and a fine one to assess the fields reconstructed by the particles.

The starting point of our downscaling experience is having the large Meso-NH simulations on a 3D domain including N_c coarse cells. The time step of these simulations is denoted Δt. The particles evolve freely in the N_c cells with a time step δt, shorter than Δt. The downscaling method used in this paper involves the following four steps :

1. initializing the particles in each cell using ε, $\nabla_x \overline{p}$ and ΔW given by the coarse Meso-NH simulations,

2. performing particle evolution with the SLM model and the time step δt,

3. calculating the sub-grid wind and the sub-grid turbulent parameters using the local average operator,

4. updating the values of ε, $\nabla_x \overline{p}$ and ΔW when the time Δt is reached, otherwise going back to step 2.

At the scale of the particles, the coarse grid-point data represent an averaged forcing. We may notice that the particle horizontal velocities are not directly forced with coarse winds. The horizontal velocities are forced with the pressure gradient and the dissipation rate. For the vertical velocities, the forcing is slightly different : it uses the vertical velocity coarse fields instead of the pressure fields. We may notice
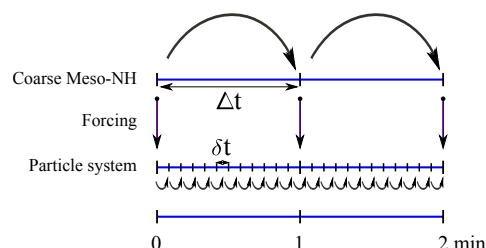
Figure 4. The different time scales used in this work. The forcing is applied at each coarse time step Δt. Between two coarse time steps, particles evolution is performed with a fine time step δt and sub-grid processes are modeled.

that in this work, the EDR used to force the particles is considered isotropic.

During 12 time steps, the values of the control parameters remain constant. To compute the particle simulation, the steps 2 and 3 are repeated in a continuous loop until the time Δt is reached. Then, the control parameter values are updated before computing the next 12 time steps δt (figure 4).

In this procedure, the particle management is hidden. In our simulations, the particle number is constant. In practice, we have to ensure that all the particles are in the simulation domain. In our work, the particles follow the simulated airflow. So, at each time step some particles leave the domain. The outside particles are replaced by new particles with consistent positions and velocities as explained in section 3.3.

As the particles evolve freely in the domain, we also have to ensure a homogeneous repartition of the particles inside the domain. To do so, for each cell of the fine grid we keep the particle number between a minimal value and a maximal value which are given at the beginning of the simulation.

5   Turbulent kinetic energy

In this section we remind first how the TKE is computed in Meso-NH model. Then, we present the TKE computation using the particle system.

5.1   The TKE in Meso-NH

To characterize turbulence, the TKE and the EDR are the two parameters usually used. The TKE is the kinetic energy associated to the small scale turbulent structures, while the EDR quantifies the energy transfer from the large scale structures to the small scale structures.

In this work, the two turbulent parameters play different roles. The EDR is used to force the particle system, whereas the TKE is used to assess the particle representation. For the EDR fields, we use directly the Meso-NH variable. It is computed from the TKE using a closure hypothesis based on the

mixing length. We give now details about how the TKE is computed.

The TKE modeled by Meso-NH is made of two terms : the resolved TKE and the sub-grid TKE. The resolved TKE is a diagnostic variable. It is calculated using the grid-point 3D wind field (u, v, w) :

$$K_{res} = \frac{1}{2}(\overline{(u - \overline{u})^2} + \overline{(v - \overline{v})^2} + \overline{(w - \overline{w})^2})$$

where the bar holds for the spatial average. Here, as the domain of simulation is very small, we choose to compute the average on all the grid points.

The sub-grid TKE e is a prognostic variable of Meso-NH which is computed using a parametrization Cuxart et al. (2000). In Meso-NH, the total TKE for the cell α is given by the sum of the sub-grid TKE and the resolved TKE :

$$K_{\alpha} = K_{res} + e_{\alpha}$$

where e^{α} is the sub-grid TKE for the cell α.

In the Meso-NH simulations we used, the grid size is fine and the resolved TKE is the major contribution to the total TKE, expected in the surface layer.

5.2 The TKE modeled by the particle system

The particle system is used here to model the wind inside the grid Meso-NH model. As detailed in section 3.5, using the wind modeled by the particles the total TKE is directly available. The TKE associated to the particle i is computed at each time step as follows :

$$K^i = \frac{1}{2} < (u^i - <u>)^2 + (v^i - <v>)^2 + (w^i - <w>)^2 >$$

where $< . >$ represents the local average. For the cell α, the TKE is thus given by :

$$K_{\alpha}^i = \frac{1}{N} \sum_{i=1}^{N} K^i$$

where N is the particle number in the cell α. Therefore, the TKE computation may be adapted to the grid size, and the particle fields may be compared to coarse and fine fields. Thus by construction, the TKE modeled by the particles contains small scale contributions –sub-grid for Meso-NH– and large scale contribution –resolved by Meso-NH.

6 Downscaling results

In the previous sections, the downscaling algorithm has been described in details. The obtained results are now presented. To assess the behavior of the particle system, we compare the 3D wind and the TKE given by the particle and by Meso-NH. First results on the coarse grid are shown. Then we present the comparison between the particle fields and the fine Meso-NH fields.
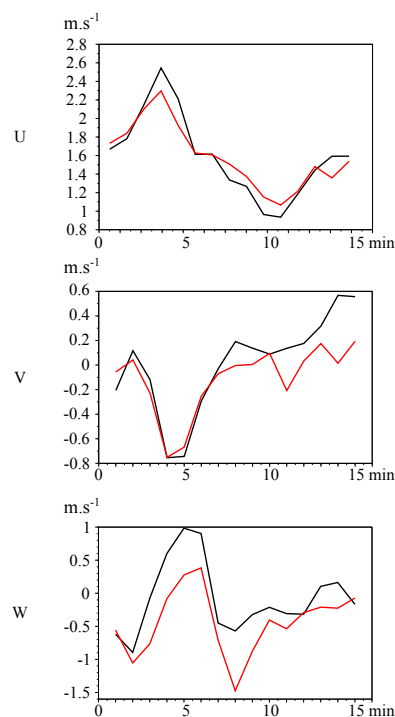
Figure 5. Time evolution of the three wind components obtained from the coarse Meso-NH simulation (black) and by the particle model (red) for one cell of the coarse grid.

6.1 3D wind results

To illustrate the results of the downscaling experience, the wind results on the coarse grid and on the fine grid are illustrated for one cell and for the 3 dimensions.

6.1.1 On the coarse grid

To model the sub-grid fields, the particles are forced by coarse grid-point fields of pressure gradient, EDR, and mean vertical velocity increment.

To assess the downscaling method, the first thing to look at is the agreement between the coarse wind and the average of the sub-grid wind modeled by the particle system. This verification is important, especially for the horizontal velocity which is not directly forced by the coarse horizontal velocity fields. We remind that to compare the particle wind to the coarse wind fields, the particle values are averaged coarse cell by coarse cell.

Figure 5 compares the three components of the wind modeled by the particles and by Meso-NH on one cell of the coarse grid. The averaged particle wind is consistent with the coarse wind, especially for the horizontal wind. For the
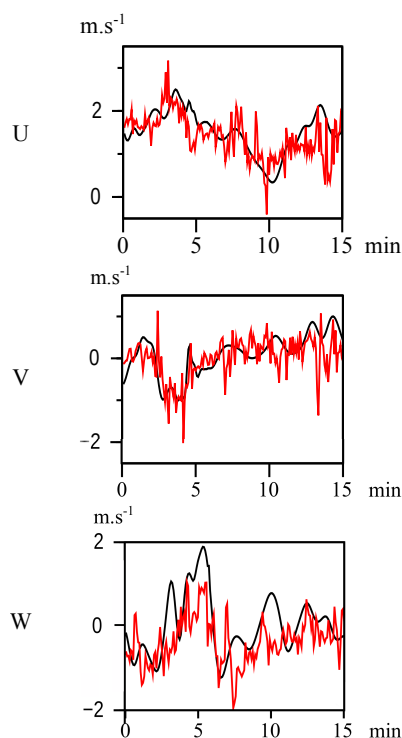
Figure 6. Time evolution of the three wind components obtained from the fine Meso-NH simulation (black) and by the particle model (red) for one cell of the fine grid.

vertical wind, there is more discrepancy between the particle wind and the Meso-NH wind, but they present the same variations. Similar results have been obtained for the other coarse cells (not shown). Thus, as expected, the 3D wind modeled by the particles is in good agreement with the wind modeled by the coarse Meso-NH model.

6.1.2   On the fine grid

We are now interested in the particle behaviors at the fine scale. Here, the particle values are average fine cell by fine cell to obtain wind fields at the fine Meso-NH resolution. The particles are forced using only coarse Meso-NH fields. Thus the particle fields could differ from the reference fine Meso-NH fields.

In figure 6, the three wind components are represented for one cell of the fine grid. First, we notice the more turbulent profile of the 3D wind represented by the particles than the fine Meso-NH wind profile. Indeed, the Meso-NH wind appears smoother while the particle wind presents more temporal fluctuations.
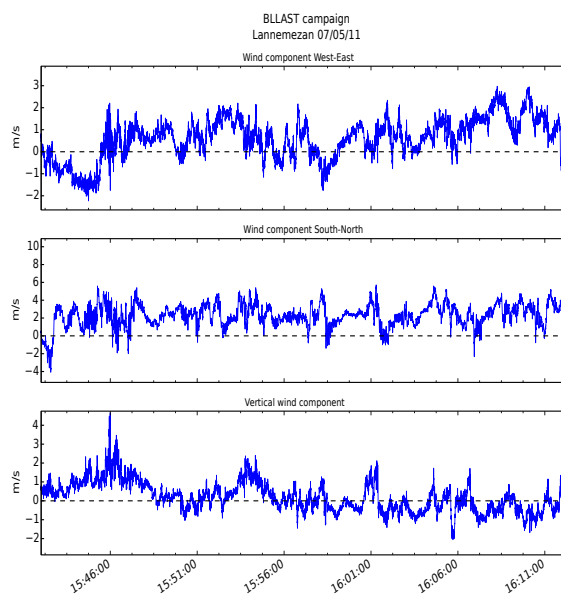
Figure 7. Time series of the observed wind in three dimensions, from tethered balloon observations at 550m, the 06/20/2011. The wind observation frequency is 10Hz.

The reference fields are represented with a 5 second time step. At this frequency, it appears that the Meso-NH wind is smoother than wind usually observed in the boundary layer. By comparison, the fluctuating profile of the particle wind seems consistent with wind observations obtained by a 3D sonic anemometer mounted above tethered balloon (figure 7).

To explain the smoothness of the Meso-NH wind, two comparisons have been done. First we have compared the wind fields on the studied area to fields on different areas on the same vertical level. Subsiding or ascending areas have been chosen.It appears that Meso-NH models a smooth wind, in both ascending and subsiding areas. Then, a simulation without numerical diffusion has been performed, and the winds modeled with and without diffusion have been compared. This comparison shows that the smoothness is not due to the numerical diffusion used in the simulations.

Coming back to figure 6, we can see that the particle wind seems to follow the fluctuations of the Meso-NH wind. This remark leads us to look at the low frequency component of the particle wind. In section 6.1.3, the difference between the particle wind and its low frequency component is also investigated.

To check that the particle wind follows mainly the Meso-NH wind fluctuations, we apply a low pass filter on the particle wind. The aim is to suppress the fast fluctuations and then to assess the low frequency component of the particle
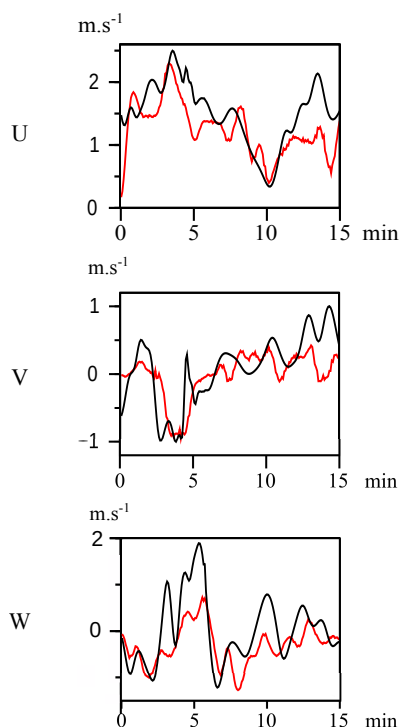
Figure 8. Components of the fine Meso-NH wind in black and components of the particle wind in red, for one cell on the second level of the fine grid.

555 wind. A second order low pass filter with a cutoff frequency of $2.10^{-2} s^{-1}$ available in the Scilab library has been used.

The results are presented in figure 8. Thanks to the low pass filter we are able to compare easily the particle wind time series to the Meso-NH wind time series. The low fre-
560 quency component of the particle wind presents the same variations than the reference Meso-NH wind. According to these results, the filtered particle wind seems consistent with the fine Meso-NH wind.

The particle wind fields do contain the same low frequency
565 information than the fine Meso-NH wind fields. Thus the suggested downscaling method and the model coupling have worked. Comparing to the Meso-NH wind, the particle wind has a faster fluctuating component. The question is now to determine if the fast fluctuations are due to smaller turbu-
570 lent structures than those modeled by Meso-NH or if they are only a noise added to the low frequency signal.

To propose a beginning of an answer, we present the study of the power spectrum densities (PSDs) of the wind and its low and high frequency components in section 6.1.3.

6.1.3 Validation using PSD and wind anomalies

To further the comparison between the Meso-NH wind and the particle wind, we have computed the wind PSDs. First, spectra of time series have been studied. Then, the PSD of the wind anomalies – differences between the particle
580 wind and its low frequency component– are shown. Finally, we discuss briefly the effective resolution of the Meso-NH model by comparison with the LES model of the NCAR.

To assess the temporal variability of the particle wind, time
585 PSDs are computed. For each vertical level, the PSDs are computed using groups of 4x4 fine grid cells. Each of these groups contains fine cells which are forced by a same coarse cell. A Fourier transform has been applied on time series of each fine cell. Then the Fourier coefficients of the 4x4 cells
590 are averaged. This operation gives 4 PSDs per vertical level. The aim is to check the consistency of the different winds with the K41 laws (Kolmogorov, 1941).

Figure 9 presents the PSDs of the three components of the fine Meso-NH wind and of the particle wind. It appears that
595 none of the particle wind or the fine Meso-NH wind follows perfectly the energy cascade given by the Kolomogorov's theory and represented by the -5/3 slope. But we may notice that the particle wind spectra present a regular slope. The regularity of the slope is a good point to assess the particle wind
600 and its fast fluctuations. It shows that the energy cascades are the same whatever the considered scales. However the slope is sightly more gentle than the energy cascade. There may be too much energy associated to the turbulence modeled by the particles at high frequencies.
605 Contrary to the particle wind, the Meso-NH wind spectra have a shape of spoon : they follow the -5/3 slope at low frequencies, then the spectrum slopes become steeper and finally the slopes are almost horizontal at high frequencies. Thus, the PSDs show that Meso-NH correctly represents the low frequency components of the wind but the modeling worsens gradually following the frequency increase. At high frequency, the Meso-NH wind PDSs look like low energetic white noises. From the spectral analysis, we may deduced an effective temporal resolution of Meso-NH about 50 seconds
615 or $10.\delta t$. It leads that Meso-NH does not model the high frequency components of the wind. Therefore it may explain the difference between the particle wind and the Meso-NH wind we have seen in the previous section.

The spectral analysis of the time series has clarified the
620 validity domain –in terms of temporal resolution– of the two simulations. It also shows the limit of the grid-point model for high frequency wind fluctuation modeling.

To have an idea of the Meso-NH effective spatial resolu-
625 tion, we have compared the Meso-NH simulations to other simulations performed for the BLLAST experiment. Spatial PSDs are computed for a given time step on the whole domain –256x256x256 cells– using rows or columns of the fine
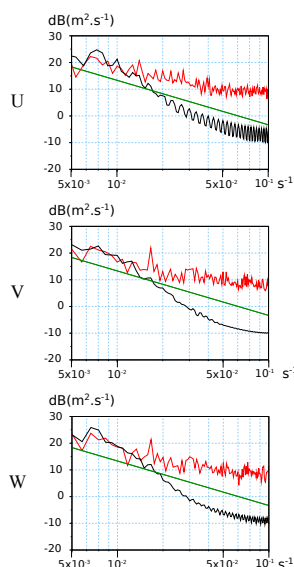
Figure 9. Power spectrum densities of the components of the fine Meso-NH wind in black and of the components of the particle wind in red, calculated on a 4x4 grid cells domain, for the second level of the fine grid. In green we have the -5/3 slope according to the K41 laws.
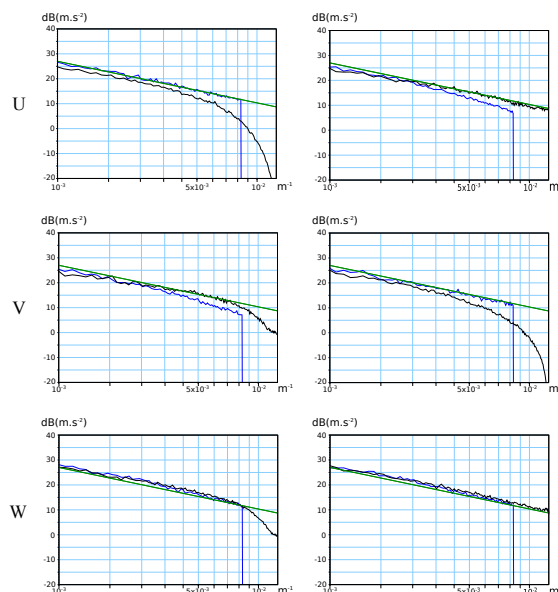
Figure 10. "Row-average" (left) and "Column-average" (right) spatial PSD on the 256x256 cells grid of the components of the wind for Meso-NH in black and the LES model of the NCAR in blue. In green we have the -5/3 slope according to the K41 laws.

grid. As for the time PSD, spatial PSD are performed using averages of Fourier coefficients. The PSDs along the x-axis are based on the averages of the Fourier transforms of the rows. Respectively, for the PSDs along the y-axis we use the averages of the Fourier transforms of the columns.

In this paragraph, the particle wind PSDs are not available. Indeed, the downscaling experience has been performed on a restricted domain which is far too small to compute the spatial PSDs.

Thus to have a comparative element, simulations of the NCAR LES are used (Moeng, 1984). These simulations have been performed by Darbieu et al. (2015). The spatial PSDs are computed for the two models using the data of the 06/20/2011 at 14h00 for the vertical level around 360 meters. Figure 10 shows the PSDs obtained for the three components of the wind following the two horizontal directions. The Meso-NH spectra and the NCAR LES spectra follow perfectly the energy cascade at low and medium frequencies.

At high frequencies, their shapes differ. From its formulation, the NCAR LES model spectra show a clear cutting frequency. This frequency is around $8.10^{-3} m^{-1}$. The Meso-NH spectra show instead gradual decreases, but the spatial resolution seems almost equivalent to the NCAR LES model. According to the NCAR LES cutting frequency, the effective spatial frequency of the Meso-NH model is about 125m.

Thus it leads to an effective resolution of $3.\Delta x$, which is in good agreement with previous studies (Ricard et al., 2013).

We may also notice the asymmetry of the spectra. It shows that the structures in the boundary layer are organized following preferential directions.

The study of the spatial spectra has shown that Meso-NH is able to model the spatial variability of the wind with a $3.\Delta x$ resolution. However Meso-NH is not able to model the local wind fluctuations under its effective resolution. Once again, it explains why the Meso-NH wind simulation is smoother than the particle simulation.

To end the validation of the particle wind, we have studied the wind anomaly PSDs. The wind anomalies are defined here as the difference between the wind and its low frequency component. The study shows that the time PSDs of the anomalies follow the energy cascade. So, the anomalies are not a white noise. Thus the particles do not add a simple noise to the coarse wind. The added information is in good agreement with the Kolmogorov K41 laws. It illustrates the effective working of the suggested downscaling method.

6.2 Turbulent kinetic energy results

In this section, the TKE simulated using the particle system is presented. As explained in section 4, the TKE is not directly
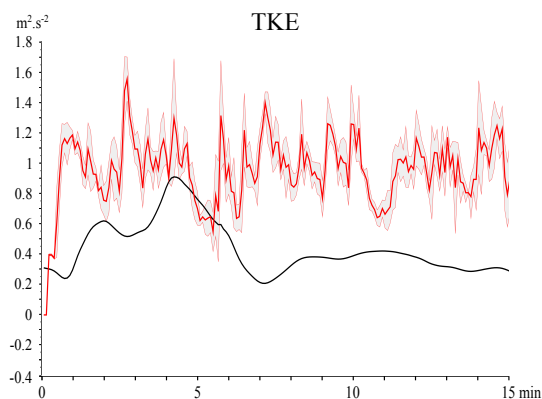
Figure 11. Fine Meso-NH TKE in black and particle TKE in red, for one cell of the fine grid. The gray zone represents the standard deviation of the particle TKE, for the particles in the cell.

forced by the coarse Meso-NH model. The particle TKE is computed at each fine time step δt, as it has been described in section 5. Then the particle TKE is compared to the fine Meso-NH TKE.

The results are presented in figure 11. In this figure, we focus on the same cell than the one shown in the previous sections. First, we may notice that the particle TKE is twice higher than the Meso-NH TKE. The particle system models also an important time variability for the TKE, whereas the Meso-NH TKE is rather smooth. The particle system models more small scale turbulence than Meso-NH. Thus the results for the TKE modeling are in good agreement with our previous remarks on the wind results and the Meso-NH effective resolution.

In Lothon et al. (2012) and Canut et al. (2016), a study of the TKE evolution during the BLLAST experiment is presented. The authors give several observations time series of TKE. During the afternoon, TKE values are around $1 m^2.s^2$, before decreasing at the end of day.

To force the particle system, we have used data from 360m and 400m high, from 13h55 UTC to 14h10 UTC. There is no TKE observation at this precise height during this period, but sonic anemometer and tethered balloon observations are available at several heights from 30m to 550m depending on the time. The TKE observations obtained using these instruments for the 06/20/2011 are given in (Canut et al., 2016).

Comparing the particle TKE to the TKE observations, we may see that the particle TKE has the same order of magnitude than the TKE observed during the afternoon, from 0.6 $m^2.s^{-2}$ to 1.7 $m^2.s^{-2}$. A look at the Meso-NH TKE shows that the Meso-NH model seems to underestimate the TKE. This underestimation has already been described in previous works (Darbieu et al., 2015).

The comparison of the particle TKE with the observations shows encouraging results. These results are a first step to demonstrate the ability of the particle system to model very small scale turbulence. However, to end the validation, the suggested downscaling method will be applied to a larger domain and to other field experiment cases.

7 Sensitivity to the forcing grid

In the previous section, all the presented results have been obtained using the same forcing scale. Here, we suggest to briefly look at the influence of the forcing scale on the fields modeled with the particle system. As a first approach to qualify this influence, the particle system has been forced by two different scales.

The previously used grid was 160mx160mx24m large. The new grid used to evaluate the forcing scale influence is 80mx80mx24m large. The temporal resolution of the forcing is the same for the two experiences ($\Delta t = 1$min).

First the particle winds are compared to the fine Meso-NH wind. The root mean square error (RMSE) between each particle wind and the Meso-NH wind are presented in table 1. The RMSEs of the low frequency components are also presented. To compute these RMSEs, we have only used the first 5 minutes of our downscaling simulations.

Table 1. Wind RMSE depending on the forcing scale.

	160m	80m
RMSE – signal total	0.520	0.462
RMSE – signal basse fréq.	0.523	0.429

As we can expect, the particle wind obtained with the finest forcing grid is the closest to the Meso-NH wind. However, the difference between the two forcing methods are rather small. Using the finest grid reduces the RMSE of 12% for the total wind, and of 20% for the low frequency component.

The influence of the forcing scale on the TKE is illustrated in figure 12. The differences between the two forcing methods are mostly visible for the first minute of the simulation, which correspond to the first large time step. The TKE obtained with the finest forcing is closest to the forcing model TKE. This particle TKE is also less fluctuating than the TKE obtained with the largest scale forcing, but they reach the same order of magnitude.

According to these results, the two particle simulations are consistent. Reducing the forcing scale reduces the difference between the particle fields and the model fields. However, for the two forcing scales, the particle fields are more turbulent than the Meso-NH fields.

To complete the work on the sensitivity to the forcing scale, a forcing grid of 40mx40mx12m has also been used. The fields modeled with this forcing grid represent sub-grid

a closure scheme. The closure scheme may induce errors on the EDR modeling due to the underlying assumptions. To control the assumptions which are made, we could compute the EDR from the grid point wind field, and compare it to the EDR calculated using different closure schemes. As the EDR controls the particle dispersion, an improvement in the EDR modeling will directly lead to an improvement in the sub-grid turbulence modeling.

Among the future works, there is first the application of the downscaling method to a larger domain, and the comparison of the sub-grid fields to observations. Then, there is the study of the TKE parametrization used in Meso-NH by comparison with the TKE modeled by the particles. In a long-term perspective, we may also think to experiences where the sub-grid parametrization used in Meso-NH will be replaced by sub-grid particle modeling.

Figure 12. 5 minutes time series of TKE depending on the forcing scale : the TKE obtained with 160mx160mx24m is drawn in red, and the TKE obtained with 80mx80mx24m is drawn in blue. The fine Meso-NH TKE is drawn in black.

fields for the fine Meso-NH simulation. As expected, the particle fields are more turbulent than the fine Meso-NH fields, but they are similar to the previous sub-grid simulations (not shown).

8   Discussion

This article suggests a new way to model sub-grid processes using particle systems . One of the major improvement is the use of a simple turbulence model instead of complex model such as LES or DNS.

This experience has been realized on a small domain, with a reduced number of particles in each cell. These two constraints were related to the long computational time. Extending the domain and the duration of the simulation should be one of the next steps. It would improve the PSD quality, and limit the influence of the edges. Then, a supplementary work on the spatial resolution of the particle simulations might be done. Extending the duration of the simulation would also enable us to compare the particle wind and the particle TKE to the in-situ observations.

In this work, the coarse fields were computed by averaging the fine Meso-NH fields. In a more advanced experience, the coarse fields would be real Meso-NH fields computed with a coarse grid. To further this study, we could also add to the SLM an equation to model the temperature evolution. Therefore the sub-grid buoyancy effect could be modeled and compared to a high resolution Meso-NH simulation.

We would like to underline an important point about the EDR fields used to force the particle system. Here, the chosen EDR is the Meso-NH variable. The advantage of this choice is that the EDR is directly available. However, as it is a diagnostic variable of the Meso-NH model, it is computed using

9   Conclusions

We present here a new downscaling method based on the coupling of a grid-point model and a particle model. The downscaling method have been applied to a simulation performed for the BLLAST experiment.

The particle system has been forced by a coarse model. Then the particle fields have been assessed against a high resolution simulation. The particle wind seems in good agreement with the high resolution wind, but higher resolution simulations should be performed. The same conclusions are given for the TKE simulations.

Even if the domain size is a limitation of the present study, the presented results are very encouraging. They prove the relevance of the suggested forcing method. Forcing particle system is a quite simple process, and the sub-grid fields seem consistent with observations. Therefore, the first step to couple the SLM model and the Meso-NH model is achieved.

In a longer term, this work may be used to compare and to test the different turbulent schemes, parameterizations, or closure hypothesis available in the research models and in the operational weather forecast models.

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