

## ***Interactive comment on “Error correlation between CO<sub>2</sub> and CO as constraint for CO<sub>2</sub> flux inversions using satellite data” by H. Wang et al.***

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This study addresses the important question of how to improve inverse modeling techniques for the estimation of sources and sinks that suffer from transport model uncertainties. Transport model uncertainties are difficult to quantify and account for in inversions, and therefore methods to deal with this problem are of great interest. The authors take the novel approach of reducing the impact of transport errors by performing a joint inversion of two tracers, where the added mutual constraint comes only from the fact that the transport model errors can be considered similar for the two tracers. The idea is initially a bit counter intuitive and it also raises the suspicion that we are dealing here with a theoretical trick that could never work in practical applications. Regarding the latter, it should be mentioned that the study that first introduced this concept did target a practical application. However, as confirmed by the authors of the present study, there were some conceptual problems: 1) the confusion of concentration covari-

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ance and error covariance 2) the conclusion that reduced a posterior flux uncertainties necessarily imply improved a posterior fluxes.

My main concern with this theoretical investigation is that it builds on the conclusions of previous work, while some fundamental questions regarding the approach itself have not yet been sufficiently addressed. This makes it difficult for the reader to judge how relevant the conducted experiments are in the first place. As will be explained in further detail below, to make this study suitable for publication in ACP it should either take a step backwards by addressing these more fundamental questions or it should acknowledge that there are still potentially important limitations of the approach.

### GENERAL COMMENTS

#### Posterior fluxes versus posterior flux uncertainties

My fundamental question about the CO-CO<sub>2</sub> cross correlation approach is whether the gain in posterior flux uncertainty is accompanied by the expected improvement in the estimated CO<sub>2</sub> fluxes. Inverse modelers are generally careful about interpreting posterior uncertainties. It is a useful indicator of the information-flow within the inversion, however, it is only a faithful measure of actual uncertainties if the statistics of all the ingredients of the inversion are well represented. Usually the off-diagonal part of the covariance matrices is poorly defined. The CO-CO<sub>2</sub> cross correlation approach relies entirely on the off-diagonals, which makes it potentially vulnerable to crude assumptions in the inversion set-up.

The way I would explain the constraint from CO on CO<sub>2</sub> in the joint inversion is by the fact that the CO inversion not only tightens the CO flux uncertainties, but also the CO posterior measurement uncertainties. Since the CO and CO<sub>2</sub> uncertainties are correlated this also reduces the CO<sub>2</sub> measurement uncertainty, etc. The problem is that the inversion has only degrees of freedom in the space of the fluxes, not in the space of uncertain transport model parameters. Therefore misfits between model and data can only be projected on the fluxes. The inversion set-up is in fact inappropriate

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to optimize tracer transport, and therefore the fit with the data is partially improved for the wrong reason. In that case, it is not clear that the posterior data are really an improvement over the prior data, even though the posterior data uncertainties suggest that it should.

In my view a much better way to test the benefit of the CO-CO<sub>2</sub> cross correlation method would be to perform an inversion where pseudo data are generated using one version of the GEOS-CHEM model, and inverted using another model version. This way one could directly test if the skill of the inversion in reproducing the true CO<sub>2</sub> fluxes improves when the CO-CO<sub>2</sub> cross correlation method is applied. I realize that such a test involves quite some work, and would therefore be hard to require for the present study. However, not knowing the outcome of such a test puts the effort within this study in quite a different perspective. It should be made much clearer that this method is still in an experimental phase and needs further investigation before it can be applied to real-world applications.

#### Data covariance

The CO-CO<sub>2</sub> cross-correlation is only one of several directions for which the covariances should formally be specified. It is unclear why the CO-CO<sub>2</sub> cross correlation receives much attention here, whereas the spatial and temporal correlation of transport model error within the CO and CO<sub>2</sub> inversions seem to be ignored. This should be explained. It is not easy to think of how such correlations might influence the benefit of a joint CO-CO<sub>2</sub> inversion, but there may well be an important effect.

#### The role of prior flux covariance

I find it hard to believe that the uncertainties of CO<sub>2</sub> and CO fluxes from biomass burning can be considered uncorrelated. The size of the emissions from individual burning events is very uncertain, which affects CO<sub>2</sub> and CO in the same manner and therefore contributes a positive correlation to their uncertainties. The question is if such correlations have any relevance for constraining CO<sub>2</sub> fluxes in a joint CO-CO<sub>2</sub>

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inversion. I think it does, as I will try to explain below.

The impact of accounting for data covariance in single tracer source/sink inversions has been investigated by a few authors in the past (see e.g. Chevallier et al, 2007). For spatial correlations decaying with distance, the posterior uncertainties of 'local' fluxes are reduced by the off-diagonals, whereas the posterior uncertainty at the large scale increases. The latter can be explained by the fact that the data covariance reduces the number of independent measurements. At the local scale, however, this effect is dominated by the number of measurements that address the local flux, which increases when the measurements become correlated.

In a joint inversion I suppose 'local' and 'large-scale' in the example above can be replaced as 'independent tracer' and 'dependent tracer'. The implication is the following: if the CO and CO<sub>2</sub> fluxes are correlated this extends their 'scale' (they become dependent tracers). In that case, the uncertainty gain by adding data covariance is expected to become less. If the prior fluxes are correlated strongly enough then adding data covariance will increase rather than decrease the posterior flux uncertainty. I'm not sure what Palmer et al. (2006) meant by stating that a priori error correlation was not useful in their inversion, but it could have reduced the benefit of adding CO<sub>2</sub>-CO data covariance.

In this study it should be made clear that the level of uncertainty reduction gained by the joint inversion approach may be different in real-world applications because of the choice of independent prior flux uncertainties.

#### SPECIFIC COMMENTS

Page 11791: It is not clear why the paired forecast method uses daily averaged biospheric fluxes and no biomass burning.

#### REFERENCES

Chevallier, F. (2007), Impact of correlated observation errors on inverted CO<sub>2</sub>

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