

# Experiments at FORD: Model including deuterated species

Model run using upper limit on CH3ONO impurity in CH2DONO of 0.00016, and updated rates from NIST, IUPAC, JPL.

## General description and conditions

Model of photochemistry of CH2DO + O<sub>2</sub> forming CH<sub>2</sub>O vs CHDO

Experiments with CH2DONO precursor in the FORD photochemical reactor

Modeling series starting 02-21-18

```
> restart;
> ppm := 1e-6: ppb := 1e-9: ppt := 1e-12:
> T:= 273 + 23:
Ptot := 700:
> P:= 101300*Ptot/760:
```

## Chemical equations

- 1a. CH3ONO + *hv* --> CH3O + NO
- 1b. CH2DONO + *hv* --> CH2DO + NO
- 2a. CH3O + O<sub>2</sub> --> CH<sub>2</sub>O + HO<sub>2</sub>
- 2b. CH2DO + O<sub>2</sub> --> CH<sub>2</sub>O + DO<sub>2</sub>
- 2c. CH2DO + O<sub>2</sub> --> CHDO + HO<sub>2</sub>
- 3a. HO<sub>2</sub> + NO --> OH + NO<sub>2</sub>
- 3b. DO<sub>2</sub> + NO --> OD + NO<sub>2</sub>
- 4a. OH + cC<sub>6</sub>H<sub>12</sub> --> H<sub>2</sub>O + RO<sub>2</sub>
- 4b. OD + cC<sub>6</sub>H<sub>12</sub> --> HDO + RO<sub>2</sub>
5. RO<sub>2</sub> + NO --> RO + NO<sub>2</sub>
6. NO<sub>2</sub> + *hv* --> NO + O
7. O + O<sub>2</sub> + M --> O<sub>3</sub> + M
- 8a. CH<sub>2</sub>O + *hv* --> CO + H<sub>2</sub>
- 8b. CHDO + *hv* --> CO + HD
- 9a. CH<sub>2</sub>O + *hv* --> CO + 2\*HO<sub>2</sub>
- 9b. CHDO + *hv* --> CO + HO<sub>2</sub> + DO<sub>2</sub>
- 10a. HO<sub>2</sub> + NO<sub>2</sub> + M --> PNA + M
- 10b. DO<sub>2</sub> + NO<sub>2</sub> + M --> PNAD + M
- 11a. HO<sub>2</sub> + CH<sub>2</sub>O --> HOCH<sub>2</sub>O<sub>2</sub>
- 11b. DO<sub>2</sub> + CH<sub>2</sub>O --> DOCH<sub>2</sub>O<sub>2</sub>
- 11c. HO<sub>2</sub> + CHDO --> HOCHDO<sub>2</sub>
- 11d. DO<sub>2</sub> + CHDO --> DOCHDO<sub>2</sub>
- 12a. HOCH<sub>2</sub>O<sub>2</sub> + RO<sub>2</sub> --> HCOOH + RO + HO<sub>2</sub>
- 12b. DOCH<sub>2</sub>O<sub>2</sub> + RO<sub>2</sub> --> HCOOD + RO + HO<sub>2</sub>
- 12c. HOCHDO<sub>2</sub> + RO<sub>2</sub> --> DCOOH + RO + HO<sub>2</sub>
- 12d. DOCHDO<sub>2</sub> + RO<sub>2</sub> --> DCOOD + RO + HO<sub>2</sub>
- 13a. CH3O + NO + M --> CH3ONO + M
- 13b. CH2DO + NO + M --> CH2DONO + M
- 14a. CH3O + NO<sub>2</sub> + M --> CH3ONO<sub>2</sub> + M
- 14b. CH2DO + NO<sub>2</sub> + M --> CH2DONO<sub>2</sub> + M
- 15a. OH + CH3ONO --> CH<sub>2</sub>O + NO + H<sub>2</sub>O
- 15b. OH + CH2DONO --> CHDO + NO + H<sub>2</sub>O

- 15c. OH + CH<sub>2</sub>DONO --> CH<sub>2</sub>O + NO + HDO  
 15d. OD + CH<sub>2</sub>DONO --> CH<sub>2</sub>O + NO + D<sub>2</sub>O  
 15e. OD + CH<sub>2</sub>DONO --> CHDO + NO + HDO  
 15f. OD + CH<sub>3</sub>ONO --> CH<sub>2</sub>O + NO + HDO  
 16a. CH<sub>2</sub>O + OH --> H<sub>2</sub>O + CO + HO<sub>2</sub>  
 16b. CHDO + OH --> H<sub>2</sub>O + CO + DO<sub>2</sub>  
 16c. CHDO + OH --> HDO + CO + HO<sub>2</sub>  
 16d. CHDO + OD --> D<sub>2</sub>O + CO + HO<sub>2</sub>  
 16e. CHDO + OD --> HDO + CO + DO<sub>2</sub>  
 16f. CH<sub>2</sub>O + OD --> HDO + CO + HO<sub>2</sub>  
 17a. HO<sub>2</sub> + HO<sub>2</sub> --> H<sub>2</sub>O<sub>2</sub>  
 17b. HO<sub>2</sub> + DO<sub>2</sub> --> HDO<sub>2</sub>  
 17c. DO<sub>2</sub> + DO<sub>2</sub> --> D<sub>2</sub>O<sub>2</sub>  
 18a. H<sub>2</sub>O<sub>2</sub> + *hv* --> 2OH  
 18b. HDO<sub>2</sub> + *hv* --> OH + OD  
 18c. D<sub>2</sub>O<sub>2</sub> + *hv* --> 2OD  
 19a. CH<sub>3</sub>O + NO<sub>2</sub> --> CH<sub>2</sub>O + HONO  
 19b. CH<sub>2</sub>DO + NO<sub>2</sub> --> CHDO + HONO  
 19c. CH<sub>2</sub>DO + NO<sub>2</sub> --> CH<sub>2</sub>O + DONO  
 20a. HOCH<sub>2</sub>O<sub>2</sub> + HOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> 2HCOOH + 2HO<sub>2</sub>  
 20b. HOCH<sub>2</sub>O<sub>2</sub> + HOCHDO<sub>2</sub> + O<sub>2</sub> --> 1.5HCOOH + 0.5DCOOH + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20c. HOCH<sub>2</sub>O<sub>2</sub> + DOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> HCOOH + HCOOD + 2HO<sub>2</sub>  
 20d. HOCH<sub>2</sub>O<sub>2</sub> + DOCHDO<sub>2</sub> + O<sub>2</sub> --> HCOOH + 0.5HCOOD + 0.5DCOOD + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20e. HOCHDO<sub>2</sub> + HOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOH + 1.5HCOOH + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20f. HOCHDO<sub>2</sub> + HOCHDO<sub>2</sub> + O<sub>2</sub> --> DCOOH + HCOOH + HO<sub>2</sub> + DO<sub>2</sub>  
 20g. HOCHDO<sub>2</sub> + DOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOH + HCOOD + 0.5HCOOH + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20h. HOCHDO<sub>2</sub> + DOCHDO<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOH + 0.5HCOOH + 0.5HCOOD + 0.5DCOOD + HO<sub>2</sub> + DO<sub>2</sub>  
 20i. DOCH<sub>2</sub>O<sub>2</sub> + HOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> HCOOD + HCOOH + 2HO<sub>2</sub>  
 20j. DOCH<sub>2</sub>O<sub>2</sub> + HOCHDO<sub>2</sub> + O<sub>2</sub> --> HCOOD + 0.5HCOOH + 0.5DCOOH + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20k. DOCH<sub>2</sub>O<sub>2</sub> + DOCHDO<sub>2</sub> + O<sub>2</sub> --> 2HCOOD + 2HO<sub>2</sub>  
 20l. DOCH<sub>2</sub>O<sub>2</sub> + DOCHDO<sub>2</sub> + O<sub>2</sub> --> 1.5HCOOD + 0.5DCOOD + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20m. DOCHDO<sub>2</sub> + HOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOD + 0.5HCOOD + HCOOH + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20n. DOCHDO<sub>2</sub> + HOCHDO<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOD + 0.5HCOOD + 0.5HCOOH + 0.5DCOOH + HO<sub>2</sub> + DO<sub>2</sub>  
 20o. DOCHDO<sub>2</sub> + DOCH<sub>2</sub>O<sub>2</sub> + O<sub>2</sub> --> 0.5DCOOD + 1.5HCOOD + 1.5HO<sub>2</sub> + 0.5DO<sub>2</sub>  
 20p. DOCHDO<sub>2</sub> + DOCHDO<sub>2</sub> + O<sub>2</sub> --> DCOOD + HCOOD + HO<sub>2</sub> + DO<sub>2</sub>  
 21a. CH<sub>3</sub>OH + OH --> CH<sub>2</sub>OH + H<sub>2</sub>O  
 21b. CH<sub>2</sub>DOH + OH --> CH<sub>2</sub>OH + HDO  
 21c. CH<sub>2</sub>DOH + OH --> CHDOH + H<sub>2</sub>O  
 21d. CH<sub>3</sub>OH + OD --> CH<sub>2</sub>OH + HDO  
 21e. CH<sub>2</sub>DOH + OD --> CHDOH + HDO  
 21f. CH<sub>2</sub>DOH + OD --> CH<sub>2</sub>OH + D<sub>2</sub>O  
 22a. CH<sub>2</sub>OH + O<sub>2</sub> --> CH<sub>2</sub>O + HO<sub>2</sub>  
 22b. CHDOH + O<sub>2</sub> --> CHDO + HO<sub>2</sub>  
 23. O<sub>3</sub> + NO --> NO<sub>2</sub>

- 24a. CO + OH --> CO<sub>2</sub> + HO<sub>2</sub>  
 24b. CO + OD --> CO<sub>2</sub> + DO<sub>2</sub>  
 25a. H<sub>2</sub> + OH --> H<sub>2</sub>O + HO<sub>2</sub>  
 25b. HD + OH --> H<sub>2</sub>O + DO<sub>2</sub>  
 25c. HD + OH --> HDO + HO<sub>2</sub>  
 25d. H<sub>2</sub> + OD --> HDO + HO<sub>2</sub>  
 25e. HD + OD --> HDO + DO<sub>2</sub>  
 25f. HD + OD --> D<sub>2</sub>O + HO<sub>2</sub>  
 26. RO<sub>2</sub> + RO<sub>2</sub> --> 2RO  
 27. RO<sub>2</sub> + RO<sub>2</sub> --> RO + cC<sub>6</sub>H<sub>12</sub>  
 28a. RO<sub>2</sub> + HO<sub>2</sub> --> cC<sub>6</sub>H<sub>12</sub> (recycle)  
 28b. RO<sub>2</sub> + DO<sub>2</sub> --> cC<sub>6</sub>H<sub>12</sub>  
 29. RO + O<sub>2</sub> --> cC<sub>6</sub>H<sub>12</sub> + HO<sub>2</sub>  
 30aa. HOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> HOCH<sub>2</sub>OOH + O<sub>2</sub>  
 30ab. HOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> HOCH<sub>2</sub>OOD + O<sub>2</sub>  
 30ac. DOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> DOCH<sub>2</sub>OOH + O<sub>2</sub>  
 30ad. DOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> DOCH<sub>2</sub>OOD + O<sub>2</sub>  
 30ae. HOCHDO<sub>2</sub> + HO<sub>2</sub> --> HOCHDOOH + O<sub>2</sub>  
 30af. HOCHDO<sub>2</sub> + DO<sub>2</sub> --> HOCHDOOD + O<sub>2</sub>  
 30ag. DOCHDO<sub>2</sub> + HO<sub>2</sub> --> HOCHDOOH + O<sub>2</sub>  
 30ah. DOCHDO<sub>2</sub> + DO<sub>2</sub> --> HOCHDOOD + O<sub>2</sub>  
 30ba. HOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> HCOOH + H<sub>2</sub>O + O<sub>2</sub>  
 30bb. HOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> HCOOH + HDO + O<sub>2</sub>  
 30bc. DOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> HCOOD + H<sub>2</sub>O + O<sub>2</sub>  
 30bd. DOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> HCOOD + HDO + O<sub>2</sub>  
 30be. HOCHDO<sub>2</sub> + HO<sub>2</sub> --> DCOOH + H<sub>2</sub>O + O<sub>2</sub>  
 30bf. HOCHDO<sub>2</sub> + DO<sub>2</sub> --> DCOOH + HDO + O<sub>2</sub>  
 30bg. DOCHDO<sub>2</sub> + HO<sub>2</sub> --> DCOOD + H<sub>2</sub>O + O<sub>2</sub>  
 30bh. DOCHDO<sub>2</sub> + DO<sub>2</sub> --> DCOOD + HDO + O<sub>2</sub>  
 30ca. HOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> HOCH<sub>2</sub>O + OH + O<sub>2</sub>  
 30cb. HOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> HOCH<sub>2</sub>O + OD + O<sub>2</sub>  
 30cc. DOCH<sub>2</sub>O<sub>2</sub> + HO<sub>2</sub> --> DOCH<sub>2</sub>O + OH + O<sub>2</sub>  
 30cd. DOCH<sub>2</sub>O<sub>2</sub> + DO<sub>2</sub> --> DOCH<sub>2</sub>O + OD + O<sub>2</sub>  
 30ce. HOCHDO<sub>2</sub> + HO<sub>2</sub> --> HOCHDO + OH + O<sub>2</sub>  
 30cf. HOCHDO<sub>2</sub> + DO<sub>2</sub> --> HOCHDO + OD + O<sub>2</sub>  
 30cg. DOCHDO<sub>2</sub> + HO<sub>2</sub> --> HOCHDO + OH + O<sub>2</sub>  
 30ch. DOCHDO<sub>2</sub> + DO<sub>2</sub> --> DOCHDO + OD + O<sub>2</sub>  
 31a. NO<sub>2</sub> + OH + M --> HNO<sub>3</sub>  
 31b. NO<sub>2</sub> + OD + M --> DNO<sub>3</sub>  
 32a. CH<sub>3</sub>ONO<sub>2</sub> + OH --> CH<sub>2</sub>O + H<sub>2</sub>O + NO<sub>2</sub>  
 32b. CH<sub>2</sub>DONO<sub>2</sub> + OH --> CH<sub>2</sub>O + HDO + NO<sub>2</sub>  
 32c. CH<sub>2</sub>DONO<sub>2</sub> + OH --> CHDO + H<sub>2</sub>O + NO<sub>2</sub>  
 32d. CH<sub>3</sub>ONO<sub>2</sub> + OD --> CH<sub>2</sub>O + HDO + NO<sub>2</sub>  
 32e. CH<sub>2</sub>DONO<sub>2</sub> + OD --> CH<sub>2</sub>O + D<sub>2</sub>O + NO<sub>2</sub>  
 32f. CH<sub>2</sub>DONO<sub>2</sub> + OD --> CHDO + HDO + NO<sub>2</sub>  
 33a. HOCH<sub>2</sub>O<sub>2</sub> --> HO<sub>2</sub> + CH<sub>2</sub>O  
 33b. DOCH<sub>2</sub>O<sub>2</sub> --> DO<sub>2</sub> + CH<sub>2</sub>O  
 33c. HOCHDO<sub>2</sub> --> HO<sub>2</sub> + CHDO  
 33d. DOCHDO<sub>2</sub> --> DO<sub>2</sub> + CHDO

## Parameters

Time unit in the calculations

```
> time_unit:= second:
```

Number of time steps in the calculations

```
> nrt:= 300:
```

```
> time_tot:= time_unit*nrt:
```

## Fundamental constants

Physical constants are present in Maple after the call:

```
with(ScientificConstants):
```

Avogadros number

```
> Na:= evalf(Constant(N[A])):
```

The gas contant

```
> R:= evalf(Constant(R)):
```

## Fixed concentrations and Rate constants

### Concentrations

Number of molecules per cm<sup>3</sup> is calculated from temperature and pressure

$$M_i := \frac{P_i 10^{(-6)} Na}{R T_i}$$

Torr is defined in units of molecules per cc.

```
> M := \frac{1}{1000000} \frac{P Na}{R T}; 1; Torr := \frac{1}{760} M; 1
```

$$M := 2.283066164 \cdot 10^{19}$$

1

$$Torr := 3.004034426 \cdot 10^{16}$$

1

Fixed concentrations

```
> O2:= 100*Torr:
```

```
N2 := 600*Torr:
```

```
> iso_impurity:=0.00016:#upper limit on CH3 contamination in  
CH2DONO/CH2DOH from IR spectra.
```

Initial concentrations of time-varying species, modeling series starting 02-21-18

```
> CH3ONO_zero := iso_impurity*36.8*Torr/1000:
```

```
> CH2DONO_zero := (1-iso_impurity)*36.8*Torr/1000:
```

```
> CH3OH_zero := iso_impurity*1.48*Torr/1000:
```

```
> CH2DOH_zero := (1-iso_impurity)*1.48*Torr/1000:
```

```
> C6H12_zero := 75.3*Torr/1000:
```

```
> NO2_zero := 0:  
> startconc := 0:
```

The rate constants:

1a.  $\text{CH}_3\text{ONO} + h\nu \rightarrow \text{CH}_3\text{O} + \text{NO}$   
>  $j1a:=1.44e-3: R1a:=j1a*\text{CH}_3\text{ONO}(t):$   
1b.  $\text{CH}_2\text{DONO} + h\nu \rightarrow \text{CH}_2\text{DO} + \text{NO}$   
>  $j1b:=1.44e-3: R1b:=j1b*\text{CH}_2\text{DONO}(t):$

The rates  $j1a$  and  $j1b$  are set to be equal since deuteration has little effect on the chromophore.

2a.  $\text{CH}_3\text{O} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{HO}_2$   
>  $k2a:= 1.9e-15: R2a:=k2a*\text{CH}_3\text{O}(t)*\text{O}_2:$   
2b.  $\text{CH}_2\text{DO} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{DO}_2$   
>  $k2b:=(1/7.593)*(2/3)*1.9e-15: R2b:=k2b*\text{CH}_2\text{DO}(t)*\text{O}_2:$   
2c.  $\text{CH}_2\text{DO} + \text{O}_2 \rightarrow \text{CHDO} + \text{HO}_2$   
>  $k2c:=(2/3)*1.9e-15: R2c:=k2c*\text{CH}_2\text{DO}(t)*\text{O}_2:$

The rate  $k2c$  is 2/3 that of  $k2a$  because there are two hydrogen atoms, not three. The rate  $k2b$  is  $(1/7.593)*(2/3)$  to match the first-order experimental result.

3a.  $\text{HO}_2 + \text{NO} \rightarrow \text{OH} + \text{NO}_2$   
>  $k3a:= 8.1e-12: R3a:=k3a*\text{HO}_2(t)*\text{NO}(t):$   
3b.  $\text{DO}_2 + \text{NO} \rightarrow \text{OD} + \text{NO}_2$   
>  $k3b:= 8.1e-12: R3b:=k3b*\text{DO}_2(t)*\text{NO}(t):$   
4a.  $\text{OH} + \text{C}_6\text{H}_{12} \rightarrow \text{H}_2\text{O} + \text{RO}_2$   
>  $k4a:= 6.7e-12: R4a:=k4a*\text{OH}(t)*\text{C}_6\text{H}_{12}(t):$   
4b.  $\text{OD} + \text{C}_6\text{H}_{12} \rightarrow \text{HDO} + \text{RO}_2$   
>  $k4b:= k4a: R4b:=k4b*\text{OD}(t)*\text{C}_6\text{H}_{12}(t):$   
5.  $\text{RO}_2 + \text{NO} \rightarrow \text{RO} + \text{NO}_2$   
>  $k5:= 3e-12: R5:=k5*\text{RO}_2(t)*\text{NO}(t):$   
6.  $\text{NO}_2 + h\nu \rightarrow \text{NO} + \text{O}$   
>  $j6:= 2*j1a: R6:=j6*\text{NO}_2(t):$   
7.  $\text{O} + \text{O}_2 + \text{M} \rightarrow \text{O}_3 + \text{M}$   
>  $k7:= 6.1e-34: R7:=k7*\text{O\_atom}(t)*\text{O}_2*\text{M}:$

8. Formaldehyde photolysis with the Ford chamber lamps is about 0.05 % as fast as that of methyl nitrite. It will be divided 1:3 between radical and molecular channels. The relative photolysis rates for the deuterated formaldehydes, channel specific, are taken from Feilberg et al., 2007: molecular  $\text{jhcho}/\text{jhcdo} = 1.82$ ; radical  $\text{jhcho}/\text{jhcdo} = 1.10$

8a.  $\text{CH}_2\text{O} + h\nu \rightarrow \text{CO} + \text{H}_2$   
>  $j8a:= 0.05*0.75*j1a: R8a:=j8a*\text{CH}_2\text{O}(t):$   
8b.  $\text{CHDO} + h\nu \rightarrow \text{CO} + \text{HD}$   
>  $j8b:= j8a/1.82: R8b:=j8b*\text{CHDO}(t):$   
9a.  $\text{CH}_2\text{O} + h\nu \rightarrow \text{CO} + 2*\text{HO}_2$   
>  $j9a:= 0.05*0.25*j1a: R9a:=j9a*\text{CH}_2\text{O}(t):$   
9b.  $\text{CHDO} + h\nu \rightarrow \text{CO} + \text{HO}_2 + \text{DO}_2$   
>  $j9b:= j9a/1.10: R9b:=j9b*\text{CHDO}(t):$   
10a.  $\text{HO}_2 + \text{NO}_2 + \text{M} \rightarrow \text{PNA} + \text{M}$   
>  $k10a:= 1.8e-31: R10a:=k10a*\text{HO}_2(t)*\text{NO}_2(t)*\text{M}:$   
10b.  $\text{DO}_2 + \text{NO}_2 + \text{M} \rightarrow \text{PNAD} + \text{M}$   
>  $k10b:= 1.8e-31: R10b:=k10b*\text{DO}_2(t)*\text{NO}_2(t)*\text{M}:$   
11a.  $\text{HO}_2 + \text{CH}_2\text{O} \rightarrow \text{HOCH}_2\text{O}_2$   
>  $k11a:= 8.01e-14: R11a:=k11a*\text{HO}_2(t)*\text{CH}_2\text{O}(t):$   
11b.  $\text{DO}_2 + \text{CH}_2\text{O} \rightarrow \text{DOCH}_2\text{O}_2$

```

> k11b := 8.01e-14: R11b:=k11b*DO2(t)*CH2O(t):
11c. HO2 + CHDO --> HOCHDO2
> k11c := 8.01e-14: R11c:=k11c*HO2(t)*CHDO(t):
11d. DO2 + CHDO --> DOCHDO2
> k11d := 8.01e-14: R11d:=k11d*DO2(t)*CHDO(t):
12a. HOCH2O2 + RO2 --> HCOOH + RO + HO2
> k12a := 5e-14: R12a:=k12a*HOCH2O2(t)*RO2(t):
12b. DOCH2O2 + RO2 --> HCOOD + RO + HO2
> k12b := 5e-14: R12b:=k12b*DOCH2O2(t)*RO2(t):
12c. HOCHDO2 + RO2 --> DCOOH + RO + HO2
> k12c := 5e-14: R12c:=k12c*HOCHDO2(t)*RO2(t):
12d. DOCHDO2 + RO2 --> DCOOD + RO + HO2
> k12d := 5e-14: R12d:=k12d*DOCHDO2(t)*RO2(t):
13a. CH3O + NO + M --> CH3ONO + M
> k13a := 1.4e-29: R13a:=k13a*CH3O(t)*NO(t)*M:
13b. CH2DO + NO + M --> CH2DONO + M
> k13b := 1.4e-29: R13b:=k13b*CH2DO(t)*NO(t)*M:
14a. CH3O + NO2 + M --> CH3ONO2 + M
> k14a := 5.3e-29: R14a:=k14a*CH3O(t)*NO2(t)*M:
14b. CH2DO + NO2 + M --> CH2DONO2 + M
> k14b := 5.3e-29: R14b:=k14b*CH2DO(t)*NO2(t)*M:
15a. OH + CH3ONO --> CH2O + NO + H2O
> k15a := 3.0e-13: R15a:=k15a*OH(t)*CH3ONO(t):
15b. OH + CH2DONO --> CHDO + NO + H2O
> k15b := (2/3)*k15a: R15b:=k15b*OH(t)*CH2DONO(t):
15c. OH + CH2DONO --> CH2O + NO + HDO, factor of 1/8 based on relative reactivity of
CD in methane.
> k15c := (1/3)*(1/8)*k15a: R15c:=k15c*OH(t)*CH2DONO(t):
15d. OD + CH2DONO --> CH2O + NO + D2O
> k15d := (1/3)*(1/8)*k15a: R15d:=k15d*OD(t)*CH2DONO(t):
15e. OD + CH2DONO --> CHDO + NO + HDO
> k15e := (2/3)*k15a: R15e:=k15e*OD(t)*CH2DONO(t):
15f. OD + CH3ONO --> CH2O + NO + HDO
> k15f := k15a: R15f:=k15f*OD(t)*CH3ONO(t):
16a. CH2O + OH --> H2O + CO + HO2
> k16a := 8.5e-12: R16a:=k16a*CH2O(t)*OH(t):
16b. CHDO + OH --> H2O + CO + DO2, from Feilberg 2004, k(OH+HCHO/kOH+HCDO)
1.28
> k16b := (8/9)*k16a/1.28: R16b:=k16b*CHDO(t)*OH(t):
16c. CHDO + OH --> HDO + CO + HO2
> k16c := (1/9)*k16a/1.28: R16c:=k16c*CHDO(t)*OH(t):
16d. CHDO + OD --> D2O + CO + HO2
> k16d := (1/9)*k16a/1.28: R16d:=k16d*CHDO(t)*OD(t):
16e. CHDO + OD --> HDO + CO + DO2
> k16e := (8/9)*k16a/1.28: R16e:=k16e*CHDO(t)*OD(t):
16f. CH2O + OD --> HDO + CO + HO2
> k16f := k16a: R16f:=k16f*CH2O(t)*OD(t):
17a. HO2 + HO2 --> H2O2
> k17a := 1.7e-12: R17a:=k17a*HO2(t)*HO2(t):
17b. HO2 + DO2 --> HDO2

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> k17b := 8.6e-13: R17b:=k17b*HO2(t)*DO2(t):
17c. DO2 + DO2 --> D2O2
> k17c := 2.0e-14: R17c:=k17c*DO2(t)*DO2(t):
18a. H2O2 + hv --> 2OH, the photolysis rates are 0.0038 that of methyl nitrite
> j18a:=0.0038*j1a: R18a:=j18a*H2O2(t):
18b. HDO2 + hv --> OH + OD
> j18b:=0.0038*j1a: R18b:=j18b*HDO2(t):
18c. D2O2 + hv --> 2OD
> j18c:=0.0038*j1a: R18c:=j18c*D2O2(t):
19a. CH3O + NO2 --> CH2O + HONO
> k19a := 2.0e-13: R19a:=k19a*CH3O(t)*NO2(t):
19b. CH2DO + NO2 --> CHDO + HONO
> k19b := (2/3)*k19a: R19b:=k19b*CH2DO(t)*NO2(t):
19c. CH2DO + NO2 --> CH2O + DONO
> k19c := (1/8)*(1/3)*k19a: R19c:=k19c*CH2DO(t)*NO2(t):
20a. HOCH2O2 + HOCH2O2 + O2 --> 2HCOOH + 2HO2
> k20a := 5.5e-12: R20a:=k20a*HOCH2O2(t)*HOCH2O2(t)*O2(t):
20b. HOCH2O2 + HOCHDO2 + O2 --> 1.5HCOOH + 0.5DCOOH + 1.5HO2 + 0.5DO2
> k20b := 5.5e-12: R20b:=k20b*HOCH2O2(t)*HOCHDO2(t)*O2(t):
20c. HOCH2O2 + DOCH2O2 + O2 --> HCOOH + HCOOD + 2HO2
> k20c := 5.5e-12: R20c:=k20c*HOCH2O2(t)*DOCH2O2(t)*O2(t):
20d. HOCH2O2 + DOCHDO2 + O2 --> HCOOH + 0.5HCOOD + 0.5DCOOD + 1.5HO2 +
0.5DO2
> k20d := 5.5e-12: R20d:=k20d*HOCH2O2(t)*DOCHDO2(t)*O2(t):
20e. HOCHDO2 + HOCH2O2 + O2 --> 0.5DCOOH + 1.5HCOOH + 1.5HO2 + 0.5DO2
> k20e := 5.5e-12: R20e:=k20e*HOCHDO2(t)*HOCH2O2(t)*O2(t):
20f. HOCHDO2 + HOCHDO2 + O2 --> DCOOH + HCOOH + HO2 + DO2
> k20f := 5.5e-12: R20f:=k20f*HOCHDO2(t)*HOCHDO2(t)*O2(t):
20g. HOCHDO2 + DOCH2O2 + O2 --> 0.5DCOOH + HCOOD + 0.5HCOOH + 1.5HO2 +
0.5DO2
> k20g := 5.5e-12: R20g:=k20g*HOCHDO2(t)*DOCH2O2(t)*O2(t):
20h. HOCHDO2 + DOCHDO2 + O2 --> 0.5DCOOH + 0.5HCOOH + 0.5HCOOD +
0.5DCOOD + HO2 + DO2
> k20h := 5.5e-12: R20h:=k20h*HOCHDO2(t)*DOCHDO2(t)*O2(t):
20i. DOCH2O2 + HOCH2O2 + O2 --> HCOOD + HCOOH + 2HO2
> k20i := 5.5e-12: R20i:=k20i*DOCH2O2(t)*HOCH2O2(t)*O2(t):
20j. DOCH2O2 + HOCHDO2 + O2 --> HCOOD + 0.5HCOOH + 0.5DCOOH + 1.5HO2 +
0.5DO2
> k20j := 5.5e-12: R20j:=k20j*DOCH2O2(t)*HOCHDO2(t)*O2(t):
20k. DOCH2O2 + DOCH2O2 + O2 --> 2HCOOD + 2HO2
> k20k := 5.5e-12: R20k:=k20k*DOCH2O2(t)*DOCH2O2(t)*O2(t):
20l. DOCH2O2 + DOCHDO2 + O2 --> 1.5HCOOD + 0.5DCOOD + 1.5HO2 + 0.5DO2
> k20l := 5.5e-12: R20l:=k20l*DOCH2O2(t)*DOCHDO2(t)*O2(t):
20m. DOCHDO2 + HOCH2O2 + O2 --> 0.5DCOOD + 0.5HCOOD + HCOOH + 1.5HO2 +
0.5DO2
> k20m := 5.5e-12: R20m:=k20m*DOCHDO2(t)*HOCH2O2(t)*O2(t):
20n. DOCHDO2 + HOCHDO2 + O2 --> 0.5DCOOD + 0.5HCOOD + 0.5HCOOH +
0.5DCOOH + HO2 + DO2
> k20n := 5.5e-12: R20n:=k20n*DOCHDO2(t)*HOCHDO2(t)*O2(t):
20o. DOCHDO2 + DOCH2O2 + O2 --> 0.5DCOOD + 1.5HCOOD + 1.5HO2 + 0.5DO2

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> k20o := 5.5e-12: R20o:=k20o*DOCHDO2(t)*DOCH2O2(t)*O2(t):
20p. DOCHDO2 + DOCHDO2 + O2 --> DCOOD + HCOOD + HO2 + DO2
> k20p := 5.5e-12: R20p:=k20p*DOCHDO2(t)*DOCHDO2(t)*O2(t):
21a. CH3OH + OH --> CH2OH + H2O
k21a := 8.8e-13: R21a:=k21a*CH3OH(t)*OH(t):
21b. CH2DOH + OH --> CH2OH + HDO
> k21b := (1/3)*(1/8)*k21a: R21b:=k21b*CH2DOH(t)*OH(t):
21c. CH2DOH + OH --> CHDOH + H2O
> k21c := (2/3)*k21a: R21c:=k21c*CH2DOH(t)*OH(t):
21d. CH3OH + OD --> CH2OH + HDO
> k21d := k21a: R21d:=k21d*CH3OH(t)*OD(t):
21e. CH2DOH + OD --> CHDOH + HDO
> k21e := (2/3)*k21a: R21e:=k21e*CH2DOH(t)*OD(t):
21f. CH2DOH + OD --> CH2OH + D2O
> k21f := (1/3)*(1/8)*k21a: R21f:=k21f*CH2DOH(t)*OD(t):
22a. CH2OH + O2 --> CH2O + HO2
> k22a := 9.6e-12: R22a:=k22a*CH2OH(t)*O2:
22b. CHDOH + O2 --> CHDO + HO2
> k22b := 9.6e-12: R22b:=k22b*CHDOH(t)*O2:
23. O3 + NO --> NO2
> k23 := 1.9e-14: R23:=k23*O3(t)*NO(t):
24a. CO + OH --> CO2 + HO2
> k24a := 2.3e-13: R24a:=k24a*CO(t)*OH(t):
24b. CO + OD --> CO2 + DO2
> k24b := 5.0e-14: R24b:=k24b*CO(t)*OD(t):
25a. H2 + OH --> H2O + HO2
> k25a := 6.7e-15: R25a:=k25a*H2(t)*OH(t):
25b. HD + OH --> H2O + DO2
> k25b := 2.5e-15: R25b:=k25b*HD(t)*OH(t):
25c. HD + OH --> HDO + HO2
> k25c := 6.7e-16: R25c:=k25c*HD(t)*OH(t):
25d. H2 + OD --> HDO + HO2
> k25d := 7.4e-15: R25d:=k25d*H2(t)*OD(t):
25e. HD + OD --> HDO + DO2
> k25e := 0.9*k25b: R25e:=k25e*HD(t)*OD(t):
25f. HD + OD --> D2O + HO2
> k25f := 0.9*k25c: R25f:=k25f*HD(t)*OD(t):
26. RO2 + RO2 --> 2RO
> k26 := 8.2e-15: R26:=k26*RO2(t)*RO2(t):
27. RO2 + RO2 --> RO + cC6H12
> k27 := 2.0e-14: R27:=k27*RO2(t)*RO2(t):
28a. RO2 + HO2 --> cC6H12
> k28a := 3.5e-11: R28a:=k28a*RO2(t)*HO2(t):
28b. RO2 + DO2 --> cC6H12
> k28b := k28a: R28b:=k28b*RO2(t)*DO2(t):
29. RO + O2 --> cC6H12 + HO2
> k29 := 2.0e-17: R29:=k29*RO(t)*O2:
30aa. HOCH2O2 + HO2 --> HOCH2OOH + O2
> k30aa := 6.0e-12: R30aa:=k30aa*HOCH2O2(t)*HO2(t):
30ab. HOCH2O2 + DO2 --> HOCH2OOD + O2

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> k30ab := k30aa: R30ab:=k30ab*HOCH2O2(t)*DO2(t):
30ac. DOCH2O2 + HO2 --> DOCH2OOH + O2
> k30ac := k30aa: R30ac:=k30ac*DOCH2O2(t)*HO2(t):
30ad. DOCH2O2 + DO2 --> DOCH2OOD + O2
> k30ad := k30aa: R30ad:=k30ad*DOCH2O2(t)*DO2(t):
30ae. HOCHDO2 + HO2 --> HOCHDOOH + O2
> k30ae := k30aa: R30ae:=k30ae*HOCHDO2(t)*HO2(t):
30af. HOCHDO2 + DO2 --> HOCHDOOD + O2
> k30af := k30aa: R30af:=k30af*HOCHDO2(t)*DO2(t):
30ag. DOCHDO2 + HO2 --> HOCHDOOH + O2
> k30ag := k30aa: R30ag:=k30ag*DOCHDO2(t)*HO2(t):
30ah. DOCHDO2 + DO2 --> HOCHDOOD + O2
> k30ah := k30aa: R30ah:=k30ah*DOCHDO2(t)*DO2(t):
30ba. HOCH2O2 + HO2 --> HCOOH + H2O + O2
> k30ba := 3.6e-12: R30ba:=k30ba*HOCH2O2(t)*HO2(t):
30bb. HOCH2O2 + DO2 --> HCOOH + HDO + O2
> k30bb := k30ba: R30bb:=k30bb*HOCH2O2(t)*DO2(t):
30bc. DOCH2O2 + HO2 --> HCOOD + H2O + O2
> k30bc := k30ba: R30bc:=k30bc*DOCH2O2(t)*HO2(t):
30bd. DOCH2O2 + DO2 --> HCOOD + HDO + O2
> k30bd := k30ba: R30bd:=k30bd*DOCH2O2(t)*DO2(t):
30be. HOCHDO2 + HO2 --> DCOOH + H2O + O2
> k30be := k30ba: R30be:=k30be*HOCHDO2(t)*HO2(t):
30bf. HOCHDO2 + DO2 --> DCOOH + HDO + O2
> k30bf := k30ba: R30bf:=k30bf*HOCHDO2(t)*DO2(t):
30bg. DOCHDO2 + HO2 --> DCOOD + H2O + O2
> k30bg := k30ba: R30bg:=k30bg*DOCHDO2(t)*HO2(t):
30bh. DOCHDO2 + DO2 --> DCOOD + HDO + O2
> k30bh := k30ba: R30bh:=k30bh*DOCHDO2(t)*DO2(t):
30ca. HOCH2O2 + HO2 --> HOCH2O + OH + O2
> k30ca := 2.4e-12: R30ca:=k30ca*HOCH2O2(t)*HO2(t):
30cb. HOCH2O2 + DO2 --> HOCH2O + OD + O2
> k30cb := k30ca: R30cb:=k30cb*HOCH2O2(t)*DO2(t):
30cc. DOCH2O2 + HO2 --> DOCH2O + OH + O2
> k30cc := k30ca: R30cc:=k30cc*DOCH2O2(t)*HO2(t):
30cd. DOCH2O2 + DO2 --> DOCH2O + OD + O2
> k30cd := k30ca: R30cd:=k30cd*DOCH2O2(t)*DO2(t):
30ce. HOCHDO2 + HO2 --> HOCHDO + OH + O2
> k30ce := k30ca: R30ce:=k30ce*HOCHDO2(t)*HO2(t):
30cf. HOCHDO2 + DO2 --> HOCHDO + OD + O2
> k30cf := k30ca: R30cf:=k30cf*HOCHDO2(t)*DO2(t):
30cg. DOCHDO2 + HO2 --> HOCHDO + OH + O2
> k30cg := k30ca: R30cg:=k30cg*DOCHDO2(t)*HO2(t):
30ch. DOCHDO2 + DO2 --> DOCHDO + OD + O2
> k30ch := k30ca: R30ch:=k30ch*DOCHDO2(t)*DO2(t):
31a. NO2 + OH + M --> HNO3
> k31a := 4.1E-11:R31a := k31a*NO2(t)*OH(t):#M is included in rate,
cf JPL
31b. NO2 + OD + M --> DNO3
> k31b := 9.3E-11:R31b := k31b*NO2(t)*OD(t):

```

32a.  $\text{CH}_3\text{ONO}_2 + \text{OH} \rightarrow \text{CH}_2\text{O} + \text{H}_2\text{O} + \text{NO}_2$   
 >  $k_{32a} := 3.0e-13: R_{32a} := k_{32a} * \text{OH}(t) * \text{CH}_3\text{ONO}_2(t):$   
 32b.  $\text{CH}_2\text{DONO}_2 + \text{OH} \rightarrow \text{CH}_2\text{O} + \text{HDO} + \text{NO}_2$   
 >  $k_{32b} := (1/3) * (1/8) * k_{32a}: R_{32b} := k_{32b} * \text{OH}(t) * \text{CH}_2\text{DONO}_2(t):$   
 32c.  $\text{CH}_2\text{DONO}_2 + \text{OH} \rightarrow \text{CHDO} + \text{H}_2\text{O} + \text{NO}_2$   
 >  $k_{32c} := (2/3) * k_{32a}: R_{32c} := k_{32c} * \text{OH}(t) * \text{CH}_2\text{DONO}_2(t):$   
 32d.  $\text{CH}_3\text{ONO}_2 + \text{OD} \rightarrow \text{CH}_2\text{O} + \text{HDO} + \text{NO}_2$   
 >  $k_{32d} := k_{32a}: R_{32d} := k_{32d} * \text{OD}(t) * \text{CH}_3\text{ONO}_2(t):$   
 32e.  $\text{CH}_2\text{DONO}_2 + \text{OD} \rightarrow \text{CH}_2\text{O} + \text{D}_2\text{O} + \text{NO}_2$   
 >  $k_{32e} := (1/3) * (1/8) * k_{32a}: R_{32e} := k_{32e} * \text{OD}(t) * \text{CH}_2\text{DONO}_2(t):$   
 32f.  $\text{CH}_2\text{DONO}_2 + \text{OD} \rightarrow \text{CHDO} + \text{HDO} + \text{NO}_2$   
 >  $k_{32f} := (2/3) * k_{32a}: R_{32f} := k_{32f} * \text{OD}(t) * \text{CH}_2\text{DONO}_2(t):$   
 33a.  $\text{HOCH}_2\text{O}_2 \rightarrow \text{HO}_2 + \text{CH}_2\text{O}$   
 >  $k_{33a} := 150: R_{33a} := k_{33a} * \text{HOCH}_2\text{O}_2(t):$   
 33b.  $\text{DOCH}_2\text{O}_2 \rightarrow \text{DO}_2 + \text{CH}_2\text{O}$   
 >  $k_{33b} := 150: R_{33b} := k_{33b} * \text{DOCH}_2\text{O}_2(t):$   
 33c.  $\text{HOCHDO}_2 \rightarrow \text{HO}_2 + \text{CHDO}$   
 >  $k_{33c} := 150: R_{33c} := k_{33c} * \text{HOCHDO}_2(t):$   
 33d.  $\text{DOCHDO}_2 \rightarrow \text{DO}_2 + \text{CHDO}$   
 >  $k_{33d} := 150: R_{33d} := k_{33d} * \text{DOCHDO}_2(t):$

REFERENCES: Photolysis rate for  $\text{CH}_3\text{ONO}$  is derived from experimental data, other photolysis rates calculated using estimated lamp flux curve and JPL cross section to derive a photolysis rate relative to methyl nitrite. Reaction rates are from JPL or NIST.

## Definition of differential equations with initial conditions

For example the equation  $d(\text{CH}_3\text{ONO})/dt = -R_{1a}+R_{13a}-R_{15a}-R_{15f}$  is written:

```

> D_CH3ONO:= diff(CH3ONO(t),t) = -R1a+R13a-R15a-R15f,
CH3ONO(0)=CH3ONO_zero:
> D_CH3O:= diff(CH3O(t),t) = R1a - R2a - R13a - R14a - R19a,
CH3O(0)=startconc:
> D_NO:= diff(NO(t),t) =
R1a+R1b-R3a-R3b-R5+R6-R13a-R13b+R15a+R15b+R15c+R15d+R15e+R15f-
R23, NO(0) = startconc:
> D_CH2DONO:= diff(CH2DONO(t),t) = -R1b+R13b-R15b-R15c-R15d-R15e,
CH2DONO(0)=CH2DONO_zero:
> D_CH2DO:= diff(CH2DO(t),t) = R1b-R2b-R2c-R13b-R14b-R19b-R19c,
CH2DO(0)=startconc:
> D_CH2O:= diff(CH2O(t),t) =
R2a+R2b-R8a-R9a-R11a-R11b+R15a+R15c+R15d+R15f-R16a-R16f+R19a+R
19c+R22a+R32a+R32b+R32d+R32e+R33a+R33b, CH2O(0)=startconc:
> D_HO2:= diff(HO2(t),t) =
R2a+R2c-R3a+2*R9a+R9b-R10a-R11a-R11c+R12a+R12b+R12c+R12d+R16a+
R16c+R16d+R16f-2*R17a-R17b+2*R20a+1.5*R20b+2*R20c+1.5*R20d+1.5
*R20e+R20f+1.5*R20g+R20h+2*R20i+2*R20j+2*R20k+1.5*R20l+1.5*R20
m+R20n+1.5*R20o+R20p+R22a+R22b+R24a+R25a+R25c+R25d+R25f-R28a+R
29-R30aa-R30ac-R30ae-R30ag-R30ba-R30bc-R30be-R30bg-R30ca-R30cc
-R30ce-R30cg+R33a+R33c, HO2(0)=startconc:

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> D_DO2:=diff(DO2(t),t) =
R2b-R3b+R9b-R10b-R11b-R11d+R16b+R16e-R17b-2*R17c+0.5*R20b+0.5*
R20d+0.5*R20e+0.5*R20f+0.5*R20g+0.5*R20h+0.5*R20j+0.5*R20l+0.5*
*R20m+0.5*R20n+0.5*R20o+R20p+R24b+R25b+R25e-R28b-R30ab-R30ad-R
30af-R30ah-R30bb-R30bd-R30bf-R30bh-R30cb-R30cd-R30cf-R30ch+R33
b+R33d, DO2(0)=startconc:
> D_CHDO:=diff(CHDO(t),t) =
R2c-R8b-R9b-R11c-R11d+R15b+R15e-R16b-R16c-R16d-R16e+R19b+R22b+
R32c+R32f+R33c+R33d, CHDO(0)=startconc:
> D_OH:=diff(OH(t),t) =
R3a-R4a-R15a-R15b-R15c-R16a-R16b-R16c+2*R18a+R18b-R21a-R21b-R2
1c-R24a-R25a-R25b-R25c+R30ca+R30cc+R30ce+R30cg-R31a-R32a-R32b-
R32c, OH(0)=startconc:
> D_NO2:=diff(NO2(t),t) =
R3a+R3b+R5-R6-R10a-R10b-R14a-R14b-R19a-R19b-R19c+R23-R31a-R31b
+R32a+R32b+R32c+R32d+R32e+R32f, NO2(0)=NO2_zero:
> D_OD:=diff(OD(t),t) =
R3b-R4b-R15d-R15e-R15f-R16d-R16e-R16f+R18b+2*R18c-R21d-R21e-R2
1f-R24b-R25d-R25e-R25f+R30cb+R30cd+R30cf+R30ch-R31b-R32d-R32e-
R32f, OD(0)=startconc:
> D_C6H12:=diff(C6H12(t),t) = -R4a-R4b+R27+R28a+R28b+R29,
C6H12(0)=C6H12_zero:
> D_H2O:=diff(H2O(t),t) =
R4a+R15a+R15b+R16a+R16b+R21a+R21c+R25a+R25b+R30ba+R30bc+R30be+
R30bg+R32a+R32c, H2O(0)=startconc:
> D_RO2:=diff(RO2(t),t) =
R4a+R4b-R5-R12a-R12b-R12c-R12d-2*R26-2*R27-R28a-R28b,
RO2(0)=startconc:
> D_HDO:=diff(HDO(t),t) =
R4b+R15c+R15e+R15f+R16c+R16e+R16f+R21b+R21d+R21e+R25c+R25d+R25
e+R30bb+R30bd+R30bf+R30bh+R32b+R32d+R32f, HDO(0)=startconc:
> D_RO:=diff(RO(t),t) = R5+R12a+R12b+R12c+R12d+2*R26+R27-R29,
RO(0)=startconc:
> D_O_atom:=diff(O_atom(t),t) = R6-R7, O_atom(0)=startconc:
> D_O3:=diff(O3(t),t) = R7-R23, O3(0)=startconc:
> D_CO:=diff(CO(t),t) =
R8a+R8b+R9a+R9b+R16a+R16b+R16c+R16d+R16e+R16f-R24a-R24b,
CO(0)=startconc:
> D_H2:=diff(H2(t),t) = R8a-R25a-R25d, H2(0)=startconc:
> D_HD:=diff(HD(t),t) = R8b-R25b-R25c-R25f-R25e,
HD(0)=startconc:
> D_PNA:=diff(PNA(t),t) = R10a, PNA(0)=startconc:
> D_PNAD:=diff(PNAD(t),t) = R10b, PNAD(0)=startconc:
> D_HOCH2O2:=diff(HOCH2O2(t),t) =
R11a-R12a-R20d-R20e-R20i-R20m-R30aa-R30ab-R30ba-R30bb-R30ca-R3
0cb-R33a, HOCH2O2(0)=startconc:
> D_DOCO2:=diff(DOCO2(t),t) =
R11b-R12b-R20c-R20g-R20i-R20j-2*R20k-R20l-R20o-R30ac-R30ad-R30
bc-R30bd-R30cc-R30cd-R33b, DOCO2(0)=startconc:
> D_HOCHDO2:=diff(HOCHDO2(t),t) =
R11c-R12c-R20b-R20e-2*R20f-R20g-R20h-R20j-R20n-R30ae-R30af-R30

```

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be-R30bf-R30ce-R30cf-R33c, HOCHDO2(0)=startconc:
> D_DOCHDO2:=diff(DOCHDO2(t),t) =
R11d-R12d-R20d-R20h-R20l-R20m-R20n-R20o-2*R20p-R30ag-R30ah-R30
bg-R30bh-R30cg-R30ch-R33d, DOCHDO2(0)=startconc:
> D_HCOOH:=diff(HCOOH(t),t) =
R12a+2*R20a+1.5*R20b+R20c+R20d+1.5*R20e+R20f+0.5*R20g+0.5*R20h
+R20i+0.5*R20j+R20m+0.5*R20n+R30ba+R30bb, HCOOH(0)=startconc:
> D_HCOOD:=diff(HCOOD(t),t) =
R12b+R20c+0.5*R20d+R20g+0.5*R20h+R20i+R20j+2*R20k+1.5*R20l+0.5
*R20m+0.5*R20n+1.5*R20o+R20p+R30bc+R30bd, HCOOD(0)=startconc:
> D_DCOOH:=diff(DCOOH(t),t) =
R12c+0.5*R20b+0.5*R20e+R20f+0.5*R20g+0.5*R20h+0.5*R20j+0.5*R20
n+R30be+R30bf, DCOOH(0)=startconc:
> D_DCOOD:=diff(DCOOD(t),t) =
R12d+0.5*R20d+0.5*R20h+0.5*R20l+0.5*R20m+0.5*R20n+0.5*R20o+R20
p+R30bg+R30bh, DCOOD(0)=startconc:
> D_CH3ONO2:=diff(CH3ONO2(t),t) = R14a-R32a-R32d,
CH3ONO2(0)=startconc:
> D_CH2DONO2:=diff(CH2DONO2(t),t) = R14b-R32b-R32c-R32e-R32f,
CH2DONO2(0)=startconc:
> D_D2O:=diff(D2O(t),t) = R15d+R16d+R21f+R25f+R32e,
D2O(0)=startconc:
> D_H2O2:=diff(H2O2(t),t) = R17a-R18a, H2O2(0)=startconc:
> D_HDO2:=diff(HDO2(t),t) = R17b-R18b, HDO2(0)=startconc:
> D_D2O2:=diff(D2O2(t),t) = R17c-R18c, D2O2(0)=startconc:
> D_HONO:=diff(HONO(t),t) = R19a+R19b, HONO(0)=startconc:
> D_DONO:=diff(DONO(t),t) = R19c, DONO(0)=startconc:
> D_CH2OHOH:=diff(CH2OHOH(t),t) = R20a+R20e+R20i+R20m,
CH2OHOH(0)=startconc:
> D_CHDOHOH:=diff(CHDOHOH(t),t) = R20b+R20f+R20j+R20n,
CHDOHOH(0)=startconc:
> D_CH2OHOD:=diff(CH2OHOD(t),t) = R20c+R20g+R20k+R20o,
CH2OHOD(0)=startconc:
> D_CHDOHOD:=diff(CHDOHOD(t),t) = R20d+R20h+R20l+R20p,
CHDOHOD(0)=startconc:
> D_CH3OH:=diff(CH3OH(t),t) = -R21a-R21d, CH3OH(0)=CH3OH_zero:
> D_CH2OH:=diff(CH2OH(t),t) = R21a+R21b+R21d+R21f-R22a,
CH2OH(0)=startconc:
> D_CH2DOH:=diff(CH2DOH(t),t) = R21b-R21c-R21e-R21f,
CH2DOH(0)=CH2DOH_zero:
> D_CHDOH:=diff(CHDOH(t),t) = R21c+R21e-R22b,
CHDOH(0)=startconc:
> D_CO2:=diff(CO2(t),t) = R24a+R24b, CO2(0)=startconc:
> D_HOCH2OOH:=diff(HOCH2OOH(t),t) = R30aa+R30ab,
HOCH2OOH(0)=startconc:
> D_DOCHEOOH:=diff(DOCHEOOH(t),t) = R30ac,
DOCHEOOH(0)=startconc:
> D_HOCHDOOH:=diff(HOCHDOOH(t),t) = R30ae+R30ag,
HOCHDOOH(0)=startconc:
> D_HOCHDOOD:=diff(HOCHDOOD(t),t) = R30af+R30ah,
HOCHDOOD(0)=startconc:

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> D_DOCH2OOD:=diff(DOCH2OOD(t),t) = R30ad,
DOCH2OOD(0)=startconc:
> D_HOCH2O:=diff(HOCH2O(t),t) = R30ca+R30cb,
HOCH2O(0)=startconc:
> D_DOCH2O:=diff(DOCH2O(t),t) = R30cc+R30cd,
DOCH2O(0)=startconc:
> D_HOCHDO:=diff(HOCHDO(t),t) = R30ce+R30cf,
HOCHDO(0)=startconc:
> D_DOCHDO:=diff(DOCHDO(t),t) = R30cg+R30ch,
DOCHDO(0)=startconc:
> D_HNO3:=diff(HNO3(t),t) = R31a, HNO3(0)=startconc:
> D_DNO3:=diff(DNO3(t),t) = R31b, DNO3(0)=startconc:

```

The following are markers used in making budgets for species components.

```

> D_mR02a:=diff(mR02a(t),t) = R2a, mR02a(0) = startconc:
> D_mR02b:=diff(mR02b(t),t) = R2b, mR02b(0) = startconc:
> D_mR02c:=diff(mR02c(t),t) = R2c, mR02c(0) = startconc:
> D_mR03a:=diff(mR03a(t),t) = R3a, mR03a(0) = startconc:
> D_mR04a:=diff(mR04a(t),t) = R4a, mR04a(0) = startconc:
> D_mR08a:=diff(mR08a(t),t) = R8a, mR08a(0) = startconc:
> D_mR08b:=diff(mR08b(t),t) = R8b, mR08b(0) = startconc:
> D_mR09a:=diff(mR09a(t),t) = R9a, mR09a(0) = startconc:
> D_mR09b:=diff(mR09b(t),t) = R9b, mR09b(0) = startconc:
> D_mR10a:=diff(mR10a(t),t) = R10a, mR10a(0) = startconc:
> D_mR10b:=diff(mR10b(t),t) = R10b, mR10b(0) = startconc:
> D_mR11a:=diff(mR11a(t),t) = R11a, mR11a(0) = startconc:
> D_mR11b:=diff(mR11b(t),t) = R11b, mR11b(0) = startconc:
> D_mR11c:=diff(mR11c(t),t) = R11c, mR11c(0) = startconc:
> D_mR11d:=diff(mR11d(t),t) = R11d, mR11d(0) = startconc:
> D_mR12a:=diff(mR12a(t),t) = R12a, mR12a(0) = startconc:
> D_mR12b:=diff(mR12b(t),t) = R12b, mR12b(0) = startconc:
> D_mR12c:=diff(mR12c(t),t) = R12c, mR12c(0) = startconc:
> D_mR12d:=diff(mR12d(t),t) = R12d, mR12d(0) = startconc:
> D_mR15a:=diff(mR15a(t),t) = R15a, mR15a(0) = startconc:
> D_mR15b:=diff(mR15b(t),t) = R15b, mR15b(0) = startconc:
> D_mR15c:=diff(mR15c(t),t) = R15c, mR15c(0) = startconc:
> D_mR15d:=diff(mR15d(t),t) = R15d, mR15d(0) = startconc:
> D_mR15e:=diff(mR15e(t),t) = R15e, mR15e(0) = startconc:
> D_mR15f:=diff(mR15f(t),t) = R15f, mR15f(0) = startconc:
> D_mR16a:=diff(mR16a(t),t) = R16a, mR16a(0) = startconc:
> D_mR16b:=diff(mR16b(t),t) = R16b, mR16b(0) = startconc:
> D_mR16c:=diff(mR16c(t),t) = R16c, mR16c(0) = startconc:
> D_mR16d:=diff(mR16d(t),t) = R16d, mR16d(0) = startconc:
> D_mR16e:=diff(mR16e(t),t) = R16e, mR16e(0) = startconc:
> D_mR16f:=diff(mR16f(t),t) = R16f, mR16f(0) = startconc:
> D_mR17a:=diff(mR17a(t),t) = R17a, mR17a(0) = startconc:
> D_mR17b:=diff(mR17b(t),t) = R17b, mR17b(0) = startconc:
> D_mR17c:=diff(mR17c(t),t) = R17c, mR17c(0) = startconc:
> D_mR18a:=diff(mR18a(t),t) = R18a, mR18a(0) = startconc:
> D_mR18b:=diff(mR18b(t),t) = R18b, mR18b(0) = startconc:
> D_mR19a:=diff(mR19a(t),t) = R19a, mR19a(0) = startconc:

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> D_mR19b:=diff(mR19b(t),t) = R19b, mR19b(0) = startconc:
> D_mR19c:=diff(mR19c(t),t) = R19c, mR19c(0) = startconc:
> D_mR20a:=diff(mR20a(t),t) = R20a, mR20a(0) = startconc:
> D_mR20b:=diff(mR20b(t),t) = R20b, mR20b(0) = startconc:
> D_mR20c:=diff(mR20c(t),t) = R20c, mR20c(0) = startconc:
> D_mR20d:=diff(mR20d(t),t) = R20d, mR20d(0) = startconc:
> D_mR20e:=diff(mR20e(t),t) = R20e, mR20e(0) = startconc:
> D_mR20f:=diff(mR20f(t),t) = R20f, mR20f(0) = startconc:
> D_mR20g:=diff(mR20g(t),t) = R20g, mR20g(0) = startconc:
> D_mR20h:=diff(mR20h(t),t) = R20h, mR20h(0) = startconc:
> D_mR20i:=diff(mR20i(t),t) = R20i, mR20i(0) = startconc:
> D_mR20j:=diff(mR20j(t),t) = R20j, mR20j(0) = startconc:
> D_mR20k:=diff(mR20k(t),t) = R20k, mR20k(0) = startconc:
> D_mR20l:=diff(mR20l(t),t) = R20l, mR20l(0) = startconc:
> D_mR20m:=diff(mR20m(t),t) = R20m, mR20m(0) = startconc:
> D_mR20n:=diff(mR20n(t),t) = R20n, mR20n(0) = startconc:
> D_mR20o:=diff(mR20o(t),t) = R20o, mR20o(0) = startconc:
> D_mR20p:=diff(mR20p(t),t) = R20p, mR20p(0) = startconc:
> D_mR21a:=diff(mR21a(t),t) = R21a, mR21a(0) = startconc:
> D_mR21b:=diff(mR21b(t),t) = R21b, mR21b(0) = startconc:
> D_mR21c:=diff(mR21c(t),t) = R21c, mR21c(0) = startconc:
> D_mR22a:=diff(mR22a(t),t) = R22a, mR22a(0) = startconc:
> D_mR22b:=diff(mR22b(t),t) = R22b, mR22b(0) = startconc:
> D_mR24a:=diff(mR24a(t),t) = R24a, mR24a(0) = startconc:
> D_mR25a:=diff(mR25a(t),t) = R25a, mR25a(0) = startconc:
> D_mR25b:=diff(mR25b(t),t) = R25b, mR25b(0) = startconc:
> D_mR25c:=diff(mR25c(t),t) = R25c, mR25c(0) = startconc:
> D_mR25d:=diff(mR25d(t),t) = R25d, mR25d(0) = startconc:
> D_mR25e:=diff(mR25e(t),t) = R25e, mR25e(0) = startconc:
> D_mR25f:=diff(mR25f(t),t) = R25f, mR25f(0) = startconc:
> D_mR28a:=diff(mR28a(t),t) = R28a, mR28a(0) = startconc:
> D_mR28b:=diff(mR28b(t),t) = R28b, mR28b(0) = startconc:
> D_mR29:=diff(mR29(t),t) = R29, mR29(0) = startconc:
> D_mR30aa:=diff(mR30aa(t),t) = R30aa, mR30aa(0) = startconc:
> D_mR30ab:=diff(mR30ab(t),t) = R30ab, mR30ab(0) = startconc:
> D_mR30ac:=diff(mR30ac(t),t) = R30ac, mR30ac(0) = startconc:
> D_mR30ad:=diff(mR30ad(t),t) = R30ad, mR30ad(0) = startconc:
> D_mR30ae:=diff(mR30ae(t),t) = R30ae, mR30ae(0) = startconc:
> D_mR30af:=diff(mR30af(t),t) = R30af, mR30af(0) = startconc:
> D_mR30ag:=diff(mR30ag(t),t) = R30ag, mR30ag(0) = startconc:
> D_mR30ah:=diff(mR30ah(t),t) = R30ah, mR30ah(0) = startconc:
> D_mR30ba:=diff(mR30ba(t),t) = R30ba, mR30ba(0) = startconc:
> D_mR30bb:=diff(mR30bb(t),t) = R30bb, mR30bb(0) = startconc:
> D_mR30bc:=diff(mR30bc(t),t) = R30bc, mR30bc(0) = startconc:
> D_mR30bd:=diff(mR30bd(t),t) = R30bd, mR30bd(0) = startconc:
> D_mR30be:=diff(mR30be(t),t) = R30be, mR30be(0) = startconc:
> D_mR30bf:=diff(mR30bf(t),t) = R30bf, mR30bf(0) = startconc:
> D_mR30bg:=diff(mR30bg(t),t) = R30bg, mR30bg(0) = startconc:
> D_mR30bh:=diff(mR30bh(t),t) = R30bh, mR30bh(0) = startconc:
> D_mR30ca:=diff(mR30ca(t),t) = R30ca, mR30ca(0) = startconc:
> D_mR30cb:=diff(mR30cb(t),t) = R30cb, mR30cb(0) = startconc:

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> D_mR30cc:=diff(mR30cc(t),t) = R30cc, mR30cc(0) = startconc:
> D_mR30cd:=diff(mR30cd(t),t) = R30cd, mR30cd(0) = startconc:
> D_mR30ce:=diff(mR30ce(t),t) = R30ce, mR30ce(0) = startconc:
> D_mR30cf:=diff(mR30cf(t),t) = R30cf, mR30cf(0) = startconc:
> D_mR30cg:=diff(mR30cg(t),t) = R30cg, mR30cg(0) = startconc:
> D_mR30ch:=diff(mR30ch(t),t) = R30ch, mR30ch(0) = startconc:
> D_mR31a:=diff(mR31a(t),t) = R31a, mR31a(0) = startconc:
> D_mR32a:=diff(mR32a(t),t) = R32a, mR32a(0) = startconc:
> D_mR32b:=diff(mR32b(t),t) = R32b, mR32b(0) = startconc:
> D_mR32c:=diff(mR32c(t),t) = R32c, mR32c(0) = startconc:
> D_mR32d:=diff(mR32d(t),t) = R32d, mR32d(0) = startconc:
> D_mR32e:=diff(mR32e(t),t) = R32e, mR32e(0) = startconc:
> D_mR32f:=diff(mR32f(t),t) = R32f, mR32f(0) = startconc:
> D_mR33a:=diff(mR33a(t),t) = R33a, mR33a(0) = startconc:
> D_mR33b:=diff(mR33b(t),t) = R33b, mR33b(0) = startconc:
> D_mR33c:=diff(mR33c(t),t) = R33c, mR33c(0) = startconc:
> D_mR33d:=diff(mR33d(t),t) = R33d, mR33d(0) = startconc:
The differential equations are gathered into a system of differential equations, Dsys
> Dsys:= [D_CH3ONO, D_CH3O, D_NO, D_CH2DONO, D_CH2DO, D_CH2O,
D_HO2, D_DO2, D_CHDO, D_OH, D_NO2, D_OD, D_C6H12, D_H2O, D_RO2,
D_HDO, D_RO, D_O_atom, D_O3, D_CO, D_H2, D_HD, D_PNA, D_PNAD,
D_HOCH2O2, D_DOCH2O2, D_HOCHDO2, D_DOCHDO2, D_HCOOH, D_HCOOD,
D_DCOOH, D_DCOOD, D_CH3ONO2, D_CH2DONO2, D_D2O, D_H2O2, D_HDO2,
D_D2O2, D_HONO, D_DONO, D_CH2OHOH, D_CHDOHOH, D_CH2OHOD,
D_CHDOHOD, D_CH3OH, D_CH2OH, D_CH2DOH, D_CHDOH, D_CO2, D_HOCH2OOH,
D_DOCH2OOH, D_HOCHDOOH, D_HOCHDOOD, D_DOCH2OOD, D_HOCH2O,
D_DOCH2O, D_HOCHDO, D_DOCHDO, D_HNO3, D_DNO3, D_mR02a, D_mR02b,
D_mR02c, D_mR03a, D_mR04a, D_mR08a, D_mR08b, D_mR09a, D_mR09b,
D_mR10a, D_mR10b, D_mR11a, D_mR11b, D_mR11c, D_mR11d, D_mR12a,
D_mR12b, D_mR12c, D_mR12d, D_mR15a, D_mR15b, D_mR15c, D_mR15d,
D_mR15e, D_mR15f, D_mR16a, D_mR16b, D_mR16c, D_mR16d, D_mR16e,
D_mR16f, D_mR17a, D_mR17b, D_mR17c, D_mR18a, D_mR18b, D_mR19a,
D_mR19b, D_mR19c, D_mR20a, D_mR20b, D_mR20c, D_mR20d, D_mR20e,
D_mR20f, D_mR20g, D_mR20h, D_mR20i, D_mR20j, D_mR20k, D_mR20l,
D_mR20m, D_mR20n, D_mR20o, D_mR20p, D_mR21a, D_mR21b, D_mR21c,
D_mR22a, D_mR22b, D_mR24a, D_mR25a, D_mR25b, D_mR25c, D_mR25d,
D_mR25e, D_mR25f, D_mR28a, D_mR28b, D_mR29, D_mR30aa, D_mR30ab,
D_mR30ac, D_mR30ad, D_mR30ae, D_mR30af, D_mR30ag, D_mR30ah,
D_mR30ba, D_mR30bb, D_mR30bc, D_mR30bd, D_mR30be, D_mR30bf,
D_mR30bg, D_mR30bh, D_mR30ca, D_mR30cb, D_mR30cc, D_mR30cd,
D_mR30ce, D_mR30cf, D_mR30cg, D_mR30ch, D_mR31a, D_mR32a, D_mR32b,
D_mR32c, D_mR32d, D_mR32e, D_mR32f, D_mR33a, D_mR33b, D_mR33c,
D_mR33d]:

```

## Solution and plotting

```
> with(plots):
```

### Examples

The first step is to define the calculation procedure, p. Maxfun=0 is necessary for long time plots, stiff = true is used for so-called stiff initial value problems (IVP), where different

magnitudes will reach steady state at very different time scales.

```
> p:= dsolve(Dsys,numeric,maxfun=0,stiff=true):
```

Next the solution is found at specific times using the procedure p.

Result after 1 second:

```
> p(1);
```



Finally, extract the concentrations of each species/reaction marker at 20 s intervals.

```
> j:=0;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
> j:=1;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
> j:=2;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 0$

$t, C6H12(t), CH2DO(t), CH2DOH(t)$

1, 1, 2261924302033252, 305983027, 44451484179374

21, 21, 2261962885784088, 145893615, 44427838474640

41, 41, 2261979465300249, 122496318, 44406009863028

61, 61, 2261988062330461, 109698684, 44385174005110

81, 81, 2261993679706693, 100813991, 44365133962064

101, 101, 2261997788663464, 93957304, 44345792822875

121, 121, 2262000998771187, 88345018, 44327090136815

141, 141, 2262003616363769, 83577982, 44308981257732

161, 161, 2262005815897461, 79425200, 44291430160234

181, 181, 2262007705737800, 75740808, 44274406402386  
201, 201, 2262009357453107, 72426706, 44257883519362  
221, 221, 2262010820731693, 69413620, 44241838042623  
241, 241, 2262012131345547, 66650750, 44226248854936  
261, 261, 2262013315859383, 64099671, 44211096741079  
281, 281, 2262014394542761, 61730559, 44196364061873  
301, 301, 2262015383213589, 59519748, 44182034510229

$$j := 1$$

$CH2DONO(t)$ ,  $CH2DONO2(t)$ ,  $CH2O(t)$ ,  $CH2OH(t)$   
1, 1103754465501489, 93532123338, 168234236264, 3  
21, 1074785382172814, 12933851521359, 1956757482858, 3  
41, 1047255506289755, 28833265724039, 3185454776173, 2  
61, 1020769653423665, 45166134375267, 4222446654299, 2  
81, 995191117159882, 61513004800625, 5138528734783, 2  
101, 970436595294673, 77713580265725, 5965665557232, 2  
121, 946445898503886, 93690583570436, 6722335687947, 2  
141, 923171761626396, 109402439897230, 7420698875554, 2  
161, 900575098229859, 124825749151100, 8069420714784, 2  
181, 878622426716879, 139947426313867, 8675018633512, 2  
201, 857284344346478, 154760680490524, 9242588535868, 2  
221, 836534558418005, 169262759753392, 9776233050838, 2

241, 816349235158197, 183453598619288, 10279331223821, 2  
261, 796706541969554, 197334964458282, 10754717221704, 2  
281, 777586313460270, 210909896653667, 11204803701623, 2  
301, 758969800012376, 224182325872888, 11631669933042, 2

$$j := 2$$

*CH<sub>2</sub>OHO<sub>D</sub>(t), CH<sub>2</sub>OHOH(t), CH<sub>3</sub>O(t), CH<sub>3</sub>OH(t)*

1, 73629920, 1274152270, 38561, 7113273210

21, 2558249456, 78402045800, 20613, 7107278196

41, 5669245521, 184127999569, 17584, 7101740258

61, 9161371737, 302474321256, 15872, 7096455627

81, 12931655661, 428230557933, 14661, 7091374719

101, 16914558734, 558537134682, 13712, 7086472926

121, 21063015669, 691570571504, 12928, 7081734797

141, 25341104817, 826082171138, 12256, 7077148868

161, 29720372727, 961179020273, 11667, 7072705859

181, 34177713336, 1096203807603, 11142, 7068397913

201, 38694030563, 1230662986063, 10666, 7064218190

221, 43253339932, 1364181102943, 10232, 7060160620

241, 47842133160, 1496470248198, 9833, 7056219741

261, 52448911787, 1627308843242, 9463, 7052390578

281, 57063834442, 1756526458415, 9119, 7048668568

301, 61678443210, 1883992659680, 8796, 7045049492

```
> j:=3;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 3$

$CH_3ONO(t), CH_3ONO_2(t), CHDO(t), CHDOH(t)$

1, 176626568923, 11650949, 1281458441139, 47

21, 171919384967, 1785919789, 14979701629258, 41

41, 167447665057, 4052793975, 24440778350661, 39

61, 163146863756, 6407124133, 32455361375546, 37

81, 158994746473, 8778199343, 39558741593042, 36

101, 154977779110, 11137895818, 45992046215840, 35

121, 151086171135, 13472125546, 51894379530673, 34

141, 147312215170, 15772972402, 57357126594549, 33

161, 143649520772, 18035723479, 62445327909177, 32

181, 140092601071, 20257516531, 67207851219393, 31

201, 136636628078, 22436638541, 71682876540861, 30

221, 133277277315, 24572127508, 75901125360154, 29

241, 130010623318, 26663530871, 79887892112226, 28

261, 126833066093, 28710751350, 83664388901002, 27

281, 123741277396, 30713944539, 87248672872260, 27

301, 120732160225, 32673448613, 90656307964011, 26

```
> j:=4;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 4$

$CHDOHOD(t)$ ,  $CHDOHOH(t)$ ,  $CO(t)$ ,  $CO_2(t)$

1, 560278459, 4289054147, 301871281, 1094

21, 19549613819, 249128764203, 75241179607, 5882307

41, 43394293479, 583231260259, 233362241349, 34476106

61, 70213100561, 958240668141, 451781027089, 96743508

81, 99216364443, 1358129078837, 718898237635, 199829262

101, 129900943380, 1773981096316, 1026652870893,  
348568148

121, 161904883614, 2200037149559, 1368847260677,  
546147924

141, 194951342825, 2632299487518, 1740494189649,  
794534464

161, 228820514412, 3067868438465, 2137466835108,  
1094764184

181, 26333444503, 3504576921309, 2556282672636,  
1447153595

201, 298341834460, 3940771103013, 2993960426728,  
1851455894

221, 333721194751, 4375170341645, 3447920324797,  
2306981678

241, 369366004123, 4806773040943, 3915911363513,  
2812693902

261, 405186156961, 5234790953425, 4395956454134,  
3367283678

281, 441104276122, 5658601903038, 4886309910142,  
3969231471

301, 477053627794, 6077714857374, 5385423739294,  
4616856905

```
> j:=5;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 5$

$D2O(t), D2O2(t), DCOOD(t), DCOOH(t)$

1, 83191165, 10906750, 560278460, 4289054156

21, 1585459647, 17183551, 19549613827, 249128764284

41, 3316259179, 18112558, 43394293489, 583231260385

61, 5315971788, 18667663, 70213100574, 958240668304

81, 7555912414, 19071008, 99216364458, 1358129079033

101, 10008484364, 19390077, 129900943397, 1773981096542

121, 12649022109, 19654687, 161904883634, 2200037149811

141, 15455666071, 19880781, 194951342847, 2632299487794

161, 18408961091, 20077959, 228820514435, 3067868438764

181, 21491481227, 20252491, 263333444528, 3504576921628

```

201, 24687531634, 20408724, 298341834486, 3940771103351
221, 27982915925, 20549807, 333721194779, 4375170342002
241, 31364750751, 20678111, 369366004152, 4806773041317
261, 34821314819, 20795468, 405186156991, 5234790953815
281, 38341923447, 20903329, 441104276154, 5658601903443
301, 41916822478, 21002867, 477053627827, 6077714857793

> j:=6;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 6$$

$$DNO3(t), DO2(t), DOCH2O(t), DOCH2O2(t)$$

$$1, 133570904, 13838560691, 0, 0$$

$$21, 19156877614, 1828974810, 1, 0$$

$$41, 45991402012, 1302614261, 1, 0$$

$$61, 76132063342, 1077490063, 1, 0$$

$$81, 108445873904, 944040950, 1, 0$$

$$101, 142334372819, 852241760, 1, 0$$

$$121, 177406091405, 783448515, 2, 0$$

$$141, 213377398077, 728959635, 2, 0$$

$$161, 250030253161, 684105195, 2, 0$$

$$181, 287190512586, 646125805, 2, 0$$

```

201, 324715418053, 613273270, 2, 0
221, 362485764630, 584377669, 2, 0
241, 400400671184, 558622419, 2, 0
261, 438373912405, 535417325, 3, 0
281, 476331242580, 514322934, 3, 0
301, 514208378432, 495003690, 3, 0

> j:=7;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 7$

$DOCH2OOD(t)$ ,  $DOCH2OOH(t)$ ,  $DOCHDO(t)$ ,  $DOCHDO2(t)$

1, 0, 0, 1, 2

21, 0, 1, 5, 2

41, 0, 2, 7, 2

61, 0, 3, 8, 2

81, 0, 3, 10, 2

101, 0, 3, 11, 2

121, 0, 4, 13, 2

141, 0, 4, 14, 2

161, 0, 5, 15, 2

181, 0, 5, 16, 2

```

201, 0, 5, 17, 2
221, 0, 5, 18, 3
241, 0, 6, 19, 3
261, 0, 6, 20, 3
281, 0, 6, 21, 3
301, 1, 6, 21, 3

> j:=8;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 8$$

$$DONO(t), H2(t), H2O(t), H2O2(t)$$

$$1, 644149, 4698551, 609771698617, 50973299482$$

$$21, 89082255, 1262988458, 14344935699541, 118641330020$$

$$41, 198606976, 4062769682, 27204071277149, 134135832489$$

$$61, 311135687, 8076018109, 39531601709379, 143387715194$$

$$81, 423778591, 13140008413, 51421632323505, 149928527252$$

$$101, 535430508, 19143221890, 62921775827631, 154929884479$$

$$121, 645557987, 26000348538, 74062183558392, 158933573917$$

$$141, 753873498, 33642253543, 84865544287747, 162237351508$$

$$161, 860214731, 42010882664, 95350481425345, 165023329293$$

181, 964490484, 51056295413, 105532948541651,  
167411329673

201, 1066652967, 60734774125, 115426966448352,  
169484507910

221, 1166682270, 71007538734, 125045079731725,  
171302968638

241, 1264577043, 81839830144, 134398661172373,  
172911574164

261, 1360348621, 93200231444, 143498126671656,  
174344691959

281, 1454017152, 105060149913, 152353092934781,  
175629220622

301, 1545608972, 117393411866, 160972496528969,  
176786595685

```
> j:=9;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 9$

$HCOOD(t), HCOOH(t), HD(t), HDO(t)$

1, 707538300, 6837358689, 19648213, 80802114023

21, 24666112733, 405932855827, 5305740608, 1179114232728

41, 54732784522, 951487259436, 17097333232, 2106925911329

61, 88535844037, 1563189310704, 34032453110,  
3000373109815

81, 125079675767, 2214590194764, 55436918865,  
3876452499346

101, 163730060850, 2891055365752, 80849067395,  
4740364697628

121, 204030914954, 3583178292646, 109915757817,  
5593933544548

141, 245633552462, 4284463829881, 142350697569,  
6437761790701

161, 288261259869, 4990226479104, 177913318984,  
7271952343188

181, 331688871179, 5696984536615, 216396497361,  
8096393117685

201, 375729895590, 6402097075245, 257618734071,  
8910884454115

221, 420227874618, 7103532547643, 301418850522,  
9715200621702

241, 465050270446, 7799713537457, 347652208546,  
10509120350722

261, 510083980538, 8489408640030, 396187914630,  
11292441882186

281, 555231945011, 9171654819993, 446906688638,  
12064989905835

301, 600410514217, 9845700176864, 499699198362,  
12826618116715

```
> j:=10;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 10$

$HDO2(t)$ ,  $HNO3(t)$ ,  $HO2(t)$ ,  $HOCH2O(t)$

```

1, 3473724691, 460941898, 118404461708, 2
21, 6481087915, 111159355313, 25354322196, 16
41, 7040748290, 279647011929, 18298300173, 26
61, 7375080413, 469013298318, 14975538144, 33
81, 7614723670, 669555832265, 12908533095, 40
101, 7801116738, 876560622342, 11447936250, 46
121, 7952997912, 1087226922280, 10337873621, 51
141, 8080537768, 1299717494970, 9453633468, 56
161, 8189917677, 1512752161799, 8725766952, 60
181, 8285196442, 1725401689159, 8111904958, 65
201, 8369193680, 1936972036634, 7584461159, 68
221, 8443954061, 2146934369171, 7124526583, 72
241, 8511011266, 2354880155513, 6718630222, 75
261, 8571547468, 2560491019604, 6356861786, 79
281, 8626494531, 2763517730009, 6031727712, 82
301, 8676600883, 2963765092534, 5737430213, 84

> j:=11;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=11

```

$HOCH2O2(t)$ ,  $HOCH2OOH(t)$ ,  $HOCHDO(t)$ ,  $HOCHDO2(t)$

1, 5, 4, 6, 16  
 21, 8, 41, 53, 26  
 41, 9, 64, 82, 28  
 61, 9, 83, 106, 29  
 81, 9, 100, 127, 30  
 101, 9, 114, 146, 30  
 121, 10, 128, 163, 31  
 141, 10, 140, 179, 31  
 161, 10, 151, 193, 31  
 181, 9, 161, 206, 31  
 201, 9, 171, 219, 31  
 221, 9, 180, 231, 31  
 241, 9, 188, 242, 30  
 261, 9, 196, 252, 30  
 281, 9, 204, 262, 30  
 301, 9, 211, 271, 30  
  
 $> j:=12;$   
 $\text{lhs}(\text{p}(1)[4*j+1]), \text{lhs}(\text{p}(1)[4*j+2]), \text{lhs}(\text{p}(1)[4*j+3]), \text{lhs}(\text{p}(1)[4*j+4]);$   
 $\text{for } i \text{ from 1 by 20 while } i < 302 \text{ do}$   
 $i, \text{round}(\text{rhs}(\text{p}(i)[4*j+1])), \text{round}(\text{rhs}(\text{p}(i)[4*j+2])), \text{round}(\text{rhs}(\text{p}(i)[4*j+3])), \text{round}(\text{rhs}(\text{p}(i)[4*j+4]));$   
 $\text{end do};$   
 $j := 12$

$HOCHDOOD(t)$ ,  $HOCHDOOH(t)$ ,  $HONO(t)$ ,  $NO(t)$

1, 2, 15, 10308317, 748247829118  
 21, 11, 131, 1425611309, 3251763249358  
 41, 17, 205, 3178381646, 4310984772655  
 61, 21, 265, 4979230387, 5080138672938  
 81, 25, 318, 6781909054, 5703189570048  
 101, 28, 365, 8568730132, 6233494906760  
 121, 32, 407, 10331156090, 6697991645688  
 141, 34, 446, 12064585081, 7112549426221  
 161, 37, 482, 13766419411, 7487398404099  
 181, 40, 516, 15435199352, 7829567307690  
 201, 42, 547, 17070159970, 8144129274700  
 221, 45, 576, 18670982535, 8434888131321  
 241, 47, 604, 20237645401, 8704786721781  
 261, 49, 630, 21770329874, 8956160500327  
 281, 51, 654, 23269358342, 9190902031233  
 301, 53, 677, 24735152261, 9410572443005  

```

> j:=13;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=13

```

$$NO_2(t), O_3(t), OD(t), OH(t)$$

1, 536439215853, 687703109, 5419270, 46450900  
 21, 4348790891062, 118477693498, 3023230, 42513129  
 41, 5475948533292, 177941915801, 2823407, 40375020  
 61, 6172295589330, 185405065934, 2730999, 38722294  
 81, 6681638064450, 180386714557, 2669708, 37297873  
 101, 7085279625882, 174566581265, 2620489, 36007905  
 121, 7420215430546, 169667660982, 2576685, 34814124  
 141, 7706451865626, 165609518979, 2535527, 33697111  
 161, 7956120911298, 162181543965, 2495722, 32644679  
 181, 8177180066961, 159232118693, 2456627, 31648161  
 201, 8375150369160, 156658193636, 2417920, 30701056  
 221, 8554031728718, 154387196712, 2379443, 29798221  
 241, 8716821297288, 152366051254, 2341127, 28935508  
 261, 8865827659063, 150554715299, 2302957, 28109490  
 281, 9002870821075, 148922192568, 2264941, 27317263  
 301, 9129414035039, 147443965040, 2227102, 26556320  

```

> j:=14;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 14$$

$$O\_atom(t), PNA(t), PNAD(t), RO(t)$$

1, 36927, 154710390524, 20029801582, 4036928862  
 21, 299370, 9135350431629, 723994056647, 10483932727  
 41, 376963, 17768173869427, 1340273512116, 10355969107  
 61, 424899, 25671089133757, 1905367661299, 10089720106  
 81, 459962, 33005503472160, 2437235174096, 9807467993  
 101, 487749, 39877380629110, 2944223036944, 9527397026  
 121, 510806, 46358780665491, 3431030758144, 9254741351  
 141, 530510, 52501841616715, 3900625635915, 8991330910  
 161, 547697, 58346169445637, 4355038180460, 8737619247  
 181, 562915, 63922981188114, 4795745021454, 8493462018  
 201, 576543, 69257594111162, 5223872506053, 8258497361  
 221, 588857, 74371009984874, 5640313420583, 8032268780  
 241, 600064, 79280971641117, 6045798007152, 7814312541  
 261, 610321, 84002695364497, 6440939276144, 7604182773  
 281, 619755, 88549395055303, 6826263071741, 7401454507  
 301, 628467, 92932667774861, 7202228691428, 7205726987  

```

> j:=15;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 15$$

$$RO2(t), mR02a(t), mR02b(t), mR02c(t)$$

1, 109584037860, 236912389, 168621781606, 1280345188601

21, 64553283160, 3119229545, 2019483348353,  
15333937074456

41, 48101730618, 5277841483, 3349053618122,  
25429364139673

61, 39770949407, 7180651773, 4507970352834,  
34229018912315

81, 34435825284, 8920121656, 5560711664847,  
42222483699859

101, 30606939479, 10537650488, 6535497025781,  
49624028950460

121, 27669487433, 12056944946, 7448238896601,  
56554477980300

141, 25315305291, 13493496990, 8309211199028,  
63091840677070

161, 23369483262, 14858301916, 9125632738158,  
69290929427891

181, 21723800150, 16159616731, 9902877572916,  
75192549462216

201, 20307049500, 17403902087, 10645118424414,  
80828384251470

221, 19069999496, 18596373214, 11355700532286,  
86223834200205

241, 17977341881, 19741344190, 12037373926481,  
91399780285848

261, 17002957813, 20842454355, 12692445392067,  
96373737927420

281, 16127002701, 21902823482, 13322882126603,  
101160644056002

301, 15334059392, 22925161839, 13930384944508,  
105773412955488

```
> j:=16;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 16$

$mR03a(t), mR04a(t), mR08a(t), mR08b(t)$

1, 610911995041, 599782801110, 4698552, 19648214

21, 14476121265933, 14062416657612, 1262991466,  
5305746500

41, 27528392109314, 26605783070536, 4062787870,  
17097368926

61, 40073814547465, 38585398416720, 8076070321,  
34032555699

81, 52195985271866, 50102331787025, 13140118337,  
55437135040

101, 63937224535477, 61209318516003, 19143416906,  
80849451197

121, 75324432101547, 71940540244988, 26000658873,  
109916368969

141, 86378096024523, 82321937876893, 33642711611,  
142351600184

161, 97115259587352, 92374811660150, 42011522542,  
177914580527

181, 107550695173258, 102117354730922, 51057152406,  
216398187800

201, 117697515074746, 111565485154595, 60735884411,  
257620925169

221, 127567550630707, 120733369843142, 71008939058,  
301421615237

241, 137171606307271, 129633778688692, 81841557568,  
347655620530

261, 146519640358279, 138278337268875, 93202323126,  
396192047793

281, 155620898298108, 146677713966227, 105062642921,  
446911616780

301, 164484014310334, 154841762460557, 117396343024,  
499704994858

```
> j:=17;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$$j := 17$$

$$mR09a(t), mR09b(t), mR10a(t), mR10b(t)$$

1, 1566184, 10836288, 154710390524, 20029801582

21, 420997155, 2926199584, 9135350431629, 723994056647

41, 1354262623, 9429458011, 17768173869427, 1340273512116

61, 2692023440, 18769470109, 25671089133757,  
1905367661299

81, 4380039446, 30574419925, 33005503472160,  
2437235174096

101, 6381138969, 44589697317, 39877380629110,  
2944223036944

121, 8666886291, 60620542873, 46358780665491,  
3431030758144

141, 11214237204, 78509064327, 52501841616715,  
3900625635915

161, 14003840847, 98122586815, 58346169445637,  
4355038180460

181, 17019050802, 119346879307, 63922981188114,  
4795745021454

201, 20245294804, 142081843548, 69257594111162,  
5223872506053

221, 23669646353, 166238587763, 74371009984874,  
5640313420583

241, 27280519189, 191737342191, 79280971641117,  
6045798007152

261, 31067441042, 218505917222, 84002695364497,  
6440939276144

281, 35020880974, 246478527990, 88549395055303,  
6826263071741

301, 39132114341, 275594875894, 92932667774861,  
7202228691428

```
> j:=18;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 18$

$mR11a(t), mR11b(t), mR11c(t), mR11d(t)$

1, 1127258759, 147259875, 8578110254, 1120557174

21, 65191966585, 5116499651, 498257599205, 39099233282

41, 152371951034, 11338492533, 1166462672149, 86788598371

61, 250033450163, 18322745763, 1916481573553,  
140426218660

81, 354000799468, 25863314445, 2716258483365,  
198432752835

101, 461957435656, 33829121454, 3547962608469,  
259801917361

121, 572411264103, 42126036212, 4400074806178,  
323809804682

141, 684330083375, 50682215417, 5264599573958,  
389902730127

161, 796967999961, 59440752164, 6135737568044,  
457641080469

181, 909769872415, 68355434325, 7009154626025,  
526666947945

201, 1022313990747, 77388069734, 7881543081651,  
596683735261

221, 1134275494999, 86506689436, 8750341650928,  
667442463336

241, 1245401802425, 95684276867, 9613547141220,  
738732089653

261, 1355495473484, 104897835104, 10469583057483,  
810372402970

281, 1464401892618, 114127681404, 11317205047542,  
882208648991

301, 1572000176287, 123356899933, 12155431046528,  
954107360080

```

> j:=19;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 19$$

$$mR12a(t), mR12b(t), mR12c(t), mR12d(t)$$

$$1, 0, 0, 0, 0$$

$$21, 1, 0, 2, 0$$

$$41, 1, 0, 3, 0$$

$$61, 1, 0, 5, 0$$

$$81, 2, 0, 6, 0$$

$$101, 2, 0, 7, 1$$

$$121, 2, 0, 8, 1$$

$$141, 3, 0, 8, 1$$

$$161, 3, 0, 9, 1$$

$$181, 3, 0, 10, 1$$

$$201, 3, 0, 11, 1$$

$$221, 3, 0, 11, 1$$

$$241, 4, 0, 12, 1$$

$$261, 4, 0, 12, 1$$

$$281, 4, 0, 13, 1$$

$$301, 4, 0, 13, 1$$

```

> j:=20;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 20$$

$$mR15a(t), mR15b(t), mR15c(t), mR15d(t)$$

$$1, 2098317, 8741645543, 546352846, 71832765$$

$$21, 48545903, 202284473691, 12642779606, 1022907601$$

$$41, 90678858, 377921018293, 23620063643, 1793927123$$

$$61, 129877433, 541391520206, 33836970013, 2510771879$$

$$81, 166598265, 694590816547, 43411926034, 3190857150$$

$$101, 201113850, 838647651795, 52415478237, 3840592378$$

$$121, 233621656, 974378955343, 60898684709, 4463149909$$

$$141, 264282058, 1102447719391, 68902982462, 5060464624$$

$$161, 293232220, 1223420799759, 76463799985, 5633913335$$

$$181, 320592497, 1337795483536, 83612217721, 6184589752$$

$$201, 346470143, 1446014905027, 90375931564, 6713431201$$

$$221, 370961782, 1548478273225, 96779892077, 7221282227$$

$$241, 394155155, 1645548135127, 102846758446, 7708928174$$

$$261, 416130436, 1737555798646, 108597237415, 8177113522$$

$$281, 436961242, 1824805525072, 114050345317, 8626552098$$

$$301, 456715439, 1907577859525, 119223616220, 9057932789$$

```

> j:=21;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 21$$

$$mR15e(t), mR15f(t), mR16a(t), mR16b(t)$$

$$1, 1149324244, 275880, 33814241, 178735579$$

$$21, 16366521609, 3927838, 8712647223, 46258742448$$

$$41, 28702833967, 6887163, 26913568019, 143141240792$$

$$61, 40172350071, 9637436, 51856762126, 276170922002$$

$$81, 51053714408, 12245624, 82125851835, 437872784988$$

$$101, 61449478047, 14736416, 116737738490, 623049622343$$

$$121, 71410398541, 17122067, 154939300509, 827711949863$$

$$141, 80967433984, 19410075, 196127869241, 1048660467608$$

$$161, 90142613353, 21605793, 239808078397, 1283259727751$$

$$181, 98953436032, 23713484, 285564967638, 1529297099055$$

$$201, 107414899217, 25736805, 333046074048, 1784888885841$$

$$221, 115540515632, 27679056, 381948900952, 2048414651828$$

$$241, 123342850778, 29543305, 432011759057, 2318469221100$$

$$261, 130833816348, 31332460, 483006850345, 2593826429434$$

$$281, 138024833565, 33049310, 534734905813, 2873411012924$$

$$301, 144926924618, 34696541, 587020934558, 3156276314090$$

```

> j:=22;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 22$

$$mR16c(t), mR16d(t), mR16e(t), mR16f(t)$$

1, 22341947, 2875469, 23003749, 4352151

21, 5782342806, 435656477, 3485251817, 656486441

41, 17892655098, 1285703092, 10285624734, 1934048295

61, 34521365248, 2452676308, 19621410469, 3684514885

81, 54734098120, 3888731047, 31109848376, 5835039801

101, 77881202788, 5559531809, 44476254473, 8333384773

121, 103463993726, 7437361588, 59498892705, 11137453233

141, 131082558442, 9498730380, 75989843044, 14211642109

161, 160407465958, 11723195661, 93785565293, 17525035547

181, 191162137369, 14092668153, 112741345232, 21050338526

201, 223111110715, 16590964114, 132727712923, 24763187115

221, 256051831461, 19203495934, 153627967483, 28641670481

241, 289808652618, 21917045094, 175336360764, 32665979388

261, 324228303657, 24719587730, 197756701854, 36818135704

281, 359176376591, 27600155666, 220801245346, 41081776714

301, 394534539235, 30548722458, 244389779677, 45441978182

```

> j:=23;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 23$$

$$mR17a(t), mR17b(t), mR17c(t), mR18a(t)$$

$$1, 50973451453, 3473735212, 10906783, 151971$$

$$21, 118652387643, 6481726314, 17185318, 11057623$$

$$41, 134160813649, 7042129978, 18116262, 24981160$$

$$61, 143427916233, 7377252125, 18673381, 40201039$$

$$81, 149984796301, 7617716239, 19078792, 56269049$$

$$101, 155002846367, 7804953241, 19399967, 72961888$$

$$121, 159023717894, 7957696739, 19666713, 90143976$$

$$141, 162345075376, 8086114139, 19894971, 107723867$$

$$161, 165148964964, 8196384513, 20094336, 125635671$$

$$181, 167555159372, 8292564909, 20271075, 143829699$$

$$201, 169646775116, 8377473569, 20429533, 162267205$$

$$221, 171483885832, 8453154042, 20572857, 180917194$$

$$241, 173111328520, 8521139086, 20703417, 199754356$$

$$261, 174563449645, 8582610101, 20823043, 218757686$$

$$281, 175867130130, 8638498288, 20933186, 237909508$$

$$301, 177043790461, 8689551507, 21035018, 257194776$$

```

> j:=24;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 24$

$$mR18b(t), mR19a(t), mR19b(t), mR19c(t)$$

1, 10521, 1926, 10306391, 644149

21, 638399, 295224, 1425316085, 89082255

41, 1381688, 670034, 3177711613, 198606976

61, 2171711, 1059390, 4978170997, 311135687

81, 2992569, 1451601, 6780457453, 423778591

101, 3836503, 1842013, 8566888119, 535430508

121, 4698827, 2228292, 10328927798, 645557987

141, 5576372, 2609123, 12061975958, 753873498

161, 6466835, 2983722, 13763435689, 860214731

181, 7368468, 3351610, 15431847742, 964490484

201, 8279889, 3712499, 17066447470, 1066652967

221, 9199981, 4066226, 18666916308, 1166682270

241, 10127821, 4412712, 20233232689, 1264577043

261, 11062633, 4751935, 21765577939, 1360348621

281, 12003757, 5083918, 23264274424, 1454017152

301, 12950624, 5408714, 24729743548, 1545608972

```

> j:=25;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 25$$

$$mR20a(t), mR20b(t), mR20c(t), mR20d(t)$$

$$1, 262011012, 881896181, 15128156, 115116920$$

$$21, 17585295639, 55869035074, 572520914, 4375194173$$

$$41, 41532078692, 131542781090, 1277157461, 9775982326$$

$$61, 68277840663, 216293225490, 2066360392, 15836894712$$

$$81, 96598281639, 306348428238, 2915427547, 22368420510$$

$$101, 125832204523, 399643580347, 3808975227, 29252374586$$

$$121, 155564514543, 494864880369, 4736128844, 36405047747$$

$$141, 185515575670, 591114590490, 5688705052, 43763299926$$

$$161, 215488889590, 687752170319, 6660307661, 51277652703$$

$$181, 245342508512, 784307162111, 7645808766, 58908328213$$

$$201, 274972034357, 880427162964, 8641023239, 66622765503$$

$$221, 304299871112, 975844779283, 9642491199, 74393961349$$

$$241, 333268078718, 1070355541492, 10647324968, \\82199303020$$

$$261, 361833443687, 1163802586109, 11653097350, \\90019716096$$

281, 389963974660, 1256065702829, 12657757589,  
97839023336

301, 417636346333, 1347053296840, 13659566561,  
105643449946

```
> j:=26;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$$j := 26$$

$$mR20e(t), mR20f(t), mR20g(t), mR20h(t)$$

1, 881896181, 2968536340, 50946766, 387674861

21, 55869035074, 177517778805, 1821593124, 13920357200

41, 131542781090, 416652923281, 4048297467, 30987258421

61, 216293225490, 685205546997, 6549087396, 50192808257

81, 306348428238, 971569319970, 9249021970, 70962308659

101, 399643580347, 1269305438246, 12100646222,  
92931431502

121, 494864880369, 1574263415380, 15069984432,  
115838869378

141, 591114590490, 1883568495133, 18131167487,  
139485234408

161, 687752170319, 2195139978172, 21263747139,  
163712542836

181, 784307162111, 2507426198660, 24451149172,  
188392411366

201, 880427162964, 2819245609915, 27679699489,  
213418630645

221, 975844779283, 3129685405179, 30937970825,  
238702186358

241, 1070355541492, 3438033435041, 34216321289,  
264167743121

261, 1163802586109, 3743730744124, 37506556077,  
289751067116

281, 1256065702829, 4046337449444, 40801671911,  
315397078854

301, 1347053296840, 4345507557653, 44095659020,  
341058343861

```
> j:=27;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 27$

$mR20i(t)$ ,  $mR20j(t)$ ,  $mR20k(t)$ ,  $mR20l(t)$

1, 15128156, 50946766, 877561, 6677437

21, 572520914, 1821593124, 18996282, 145139136

41, 1277157461, 4048297467, 39730607, 304059987

61, 2066360392, 6549087396, 63018386, 482905563

81, 2915427547, 9249021970, 88474748, 678731397

101, 3808975227, 12100646222, 115787331, 889149954

121, 4736128844, 15069984432, 144700068, 1112202324

141, 5688705052, 18131167487, 174997157, 1346235121  
 161, 6660307661, 21263747139, 206493139, 1589824788  
 181, 7645808766, 24451149172, 239026482, 1841728916  
 201, 8641023239, 27679699489, 272455146, 2100852689  
 221, 9642491199, 30937970825, 306653362, 2366224546  
 241, 10647324968, 34216321289, 341509182, 2636977720  
 261, 11653097350, 37506556077, 376922558, 2912335803  
 281, 12657757589, 40801671911, 412803802, 3191601140  
 301, 13659566561, 44095659020, 449072321, 3474145309

```

> j:=28;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 28$

$mR20m(t)$ ,  $mR20n(t)$ ,  $mR20o(t)$ ,  $mR20p(t)$

1, 115116920, 387674861, 6677437, 50809241  
 21, 4375194173, 13920357200, 145139136, 1108923311  
 41, 9775982326, 30987258421, 304059987, 2326992745  
 61, 15836894712, 50192808257, 482905563, 3700492029  
 81, 22368420510, 70962308659, 678731397, 5206903877  
 101, 29252374586, 92931431502, 889149954, 6827987339  
 121, 36405047747, 115838869378, 1112202324, 8548764165

141, 43763299926, 139485234408, 1346235121, 10356573371  
 161, 51277652703, 163712542836, 1589824788, 12240494085  
 181, 58908328213, 188392411366, 1841728916, 14190976008  
 201, 66622765503, 213418630645, 2100852689, 16199585623  
 221, 74393961349, 238702186358, 2366224546, 18258822498  
 241, 82199303020, 264167743121, 2636977720, 20361980261  
 261, 90019716096, 289751067116, 2912335803, 22503037946  
 281, 97839023336, 315397078854, 3191601140, 24676572792  
 301, 105643449946, 341058343861, 3474145309, 26877688678

```

> j:=29;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 29$

$mR21a(t), mR21b(t), mR21c(t), mR22a(t)$

1, 247740, 64505732, 1032091706, 73266902

21, 5806046, 1511996266, 24191940252, 1640478728

41, 10980550, 2859940475, 45759047600, 3088634315

61, 15918701, 4146677533, 66346840522, 4470938477

81, 20662648, 5383144417, 86130310676, 5800312140

101, 25234505, 6575067464, 105201079422, 7083154244

121, 29648679, 7726170366, 123618725844, 8323474247

141, 33916141, 8839285069, 141428561099, 9524243028  
161, 38045918, 9916739973, 158667839567, 10687862938  
181, 42045731, 10960525584, 175368409333, 11816366712  
201, 45922341, 11972384538, 191558152596, 12911522960  
221, 49681769, 12953868368, 207261893883, 13974900789  
241, 53329446, 13906375922, 222502014747, 15007912421  
261, 56870316, 14831180811, 237298892966, 16011842974  
281, 60308914, 15729451761, 251671228165, 16987872108  
301, 63649430, 16602268132, 265636290095, 17937090266

```
> j:=30;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 30$

$mR22b(t), mR24a(t), mR25a(t), mR25b(t)$

1, 1167785449, 1065, 1, 1  
21, 26147254445, 5789964, 2783, 4359  
41, 49229136831, 33954312, 16871, 26467  
61, 71261449335, 95285781, 48447, 76088  
81, 92450133399, 196803087, 101958, 160281  
101, 112897178373, 343243426, 180766, 284413  
121, 132666488363, 537719233, 287435, 452598

141, 151805414002, 782139187, 423915, 667986  
161, 170352244410, 1077497554, 591668, 932959  
181, 188339377653, 1424081341, 791754, 1249269  
201, 205795002061, 1821624944, 1024907, 1618147  
221, 222744126204, 2269429243, 1291584, 2040384  
241, 239209258247, 2766455192, 1592008, 2516407  
261, 255210880494, 3311398448, 1926208, 3046323  
281, 270767794477, 3902749556, 2294046, 3629978  
301, 285897379782, 4538842885, 2695241, 4266988

```
> j:=31;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$$j := 31$$

$$mR25c(t), mR25d(t), mR25e(t), mR25f(t)$$

$$1, 0, 0, 0, 0$$

$$21, 1168, 225, 288, 77$$

$$41, 7093, 1317, 1683, 451$$

$$61, 20392, 3765, 4818, 1291$$

$$81, 42955, 7965, 10204, 2735$$

$$101, 76223, 14250, 18270, 4896$$

$$121, 121296, 22900, 29384, 7875$$

141, 179020, 34153, 43855, 11753  
 161, 250033, 48210, 61948, 16602  
 181, 334804, 65239, 83885, 22481  
 201, 433663, 85378, 109848, 29439  
 221, 546823, 108741, 139991, 37518  
 241, 674397, 135416, 174433, 46748  
 261, 816415, 165473, 213269, 57156  
 281, 972834, 198962, 256569, 68760  
 301, 1143553, 235917, 304381, 81574  
  
 $\text{> } j := 32;$   
 $\text{lhs}(\text{p}(1)[4*j+1]), \text{lhs}(\text{p}(1)[4*j+2]), \text{lhs}(\text{p}(1)[4*j+3]), \text{lhs}(\text{p}(1)[4*j+4]);$   
 $\text{for } i \text{ from 1 by 20 while } i < 302 \text{ do}$   
 $i, \text{round}(\text{rhs}(\text{p}(i)[4*j+1])), \text{round}(\text{rhs}(\text{p}(i)[4*j+2])), \text{round}(\text{rhs}(\text{p}(i)[4*j+3])), \text{round}(\text{rhs}(\text{p}(i)[4*j+4]));$   
 $\text{end do;}$   
 $j := 32$   
 $mR28a(t), mR28b(t), mR29(t), mR30aa(t)$   
 1, 401213388950, 52788951251, 110895363672, 4  
 21, 3105280707095, 281739533783, 11733627778583, 38  
 41, 3932919725149, 340856064895, 24286580303408, 59  
 61, 4437252017450, 376908141379, 36574183188898, 77  
 81, 4796625857921, 402960833078, 48528805473237, 93  
 101, 5072558290980, 423313031383, 60144751501236, 106  
 121, 5294016163818, 439942747607, 71428317672158, 119

141, 5477089456761, 453934883780, 82389717945139, 130  
 161, 5631687484268, 465953443873, 93040421363786, 140  
 181, 5764361389591, 476436593674, 103392031818425, 150  
 201, 5879673085591, 485689833042, 113455825216063, 159  
 221, 5980928093216, 493935301553, 123242575839434, 167  
 241, 6070598144358, 501339966296, 132762504587054, 175  
 261, 6150579266862, 508032727450, 142025281342476, 182  
 281, 6222356868742, 514115311227, 151040050089253, 189  
 301, 6287115483103, 519669490137, 159815462226544, 195

```

> j:=33;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*
j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(
i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 33$

$mR30ab(t)$ ,  $mR30ac(t)$ ,  $mR30ad(t)$ ,  $mR30ae(t)$

1, 1, 0, 0, 13

21, 3, 1, 0, 121

41, 5, 2, 0, 189

61, 6, 3, 0, 246

81, 7, 3, 0, 295

101, 8, 3, 0, 338

121, 9, 4, 0, 378

```

141, 10, 4, 0, 414
161, 11, 5, 0, 448
181, 12, 5, 0, 479
201, 12, 5, 0, 508
221, 13, 5, 0, 535
241, 14, 6, 0, 560
261, 14, 6, 0, 584
281, 15, 6, 0, 606
301, 15, 6, 1, 628

> j:=34;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 34$$

$$mR30af(t), mR30ag(t), mR30ah(t), mR30ba(t)$$

- 1, 2, 2, 0, 2
- 21, 11, 11, 1, 23
- 41, 15, 15, 1, 36
- 61, 19, 19, 2, 46
- 81, 23, 23, 2, 56
- 101, 26, 26, 2, 64
- 121, 29, 29, 2, 71

141, 32, 32, 3, 78  
 161, 35, 35, 3, 84  
 181, 37, 37, 3, 90  
 201, 39, 39, 3, 95  
 221, 42, 42, 3, 100  
 241, 44, 44, 3, 105  
 261, 46, 46, 4, 109  
 281, 48, 48, 4, 113  
 301, 49, 49, 4, 117  
  
**> j:=35;**  
 $\text{lhs}(\text{p}(1)[4*j+1]), \text{lhs}(\text{p}(1)[4*j+2]), \text{lhs}(\text{p}(1)[4*j+3]), \text{lhs}(\text{p}(1)[4*j+4]);$   
**for i from 1 by 20 while i < 302 do**  
  
 $i, \text{round}(\text{rhs}(\text{p}(i)[4*j+1])), \text{round}(\text{rhs}(\text{p}(i)[4*j+2])), \text{round}(\text{rhs}(\text{p}(i)[4*j+3])), \text{round}(\text{rhs}(\text{p}(i)[4*j+4]));$   
**end do;**

$$j := 35$$

$$mR30bb(t), mR30bc(t), mR30bd(t), mR30be(t)$$

$$1, 0, 0, 0, 8$$

$$21, 2, 1, 0, 73$$

$$41, 3, 1, 0, 114$$

$$61, 4, 2, 0, 147$$

$$81, 4, 2, 0, 177$$

$$101, 5, 2, 0, 203$$

$$121, 5, 2, 0, 227$$

```

141, 6, 3, 0, 249
161, 6, 3, 0, 269
181, 7, 3, 0, 287
201, 7, 3, 0, 305
221, 8, 3, 0, 321
241, 8, 3, 0, 336
261, 9, 4, 0, 350
281, 9, 4, 0, 364
301, 9, 4, 0, 377

> j:=36;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 36$$

$$mR30bf(t), mR30bg(t), mR30bh(t), mR30ca(t)$$

1, 1, 1, 0, 2  
21, 6, 6, 1, 15  
41, 9, 9, 1, 24  
61, 12, 12, 1, 31  
81, 14, 14, 1, 37  
101, 16, 16, 1, 43  
121, 18, 18, 1, 47

141, 19, 19, 2, 52  
 161, 21, 21, 2, 56  
 181, 22, 22, 2, 60  
 201, 24, 24, 2, 64  
 221, 25, 25, 2, 67  
 241, 26, 26, 2, 70  
 261, 27, 27, 2, 73  
 281, 29, 29, 2, 76  
 301, 30, 30, 2, 78  
  
**> j:=37;**  
**lhs(p(1)[4\*j+1]),lhs(p(1)[4\*j+2]),lhs(p(1)[4\*j+3]),lhs(p(1)[4\*j+4]);**  
**for i from 1 by 20 while i < 302 do**  
  
**i,round(rhs(p(i)[4\*j+1])),round(rhs(p(i)[4\*j+2])),round(rhs(p(i)[4\*j+3])),round(rhs(p(i)[4\*j+4]));**  
**end do;**

*j :=37*

*mR30cb(t), mR30cc(t), mR30cd(t), mR30ce(t)*

1, 0, 0, 0, 5

21, 1, 1, 0, 48

41, 2, 1, 0, 76

61, 2, 1, 0, 98

81, 3, 1, 0, 118

101, 3, 1, 0, 135

121, 4, 2, 0, 151

```

141, 4, 2, 0, 166
161, 4, 2, 0, 179
181, 5, 2, 0, 192
201, 5, 2, 0, 203
221, 5, 2, 0, 214
241, 5, 2, 0, 224
261, 6, 2, 0, 234
281, 6, 2, 0, 243
301, 6, 3, 0, 251

> j:=38;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 38$

$$mR30cf(t), mR30cg(t), mR30ch(t), mR31a(t)$$

1, 1, 1, 0, 460941898

21, 4, 4, 0, 111159355313

41, 6, 6, 1, 279647011929

61, 8, 8, 1, 469013298318

81, 9, 9, 1, 669555832265

101, 10, 10, 1, 876560622342

121, 12, 12, 1, 1087226922280

```

141, 13, 13, 1, 1299717494970
161, 14, 14, 1, 1512752161799
181, 15, 15, 1, 1725401689159
201, 16, 16, 1, 1936972036634
221, 17, 17, 1, 2146934369171
241, 17, 17, 1, 2354880155513
261, 18, 18, 1, 2560491019604
281, 19, 19, 2, 2763517730009
301, 20, 20, 2, 2963765092534

> j:=39;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=39

mR32a(t), mR32b(t), mR32c(t), mR32d(t)

1, 49, 16520, 264318, 6
21, 207799, 63541958, 1016671323, 15322
41, 927058, 278168872, 4450701946, 65789
61, 2164561, 643072648, 10289162367, 152645
81, 3893853, 1149334699, 18389355181, 275524
101, 6082097, 1786770229, 28588323663, 433495
121, 8695116, 2545104753, 40721676043, 625314

```

141, 11699366, 3414425231, 54630803701, 849560  
161, 15062724, 4385340866, 70165453856, 1104707  
181, 18754762, 5449026047, 87184416753, 1389173  
201, 22746827, 6597218341, 105555493455, 1701353  
221, 27012027, 7822198794, 125155180701, 2039639  
241, 31525175, 9116764687, 145868234989, 2402442  
261, 36262711, 10474199682, 167587194905, 2788196  
281, 41202620, 11888243705, 190211899272, 3195375  
301, 46324340, 13353063636, 213649018179, 3622492

```
> j:=40;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 40$

$$mR32e(t), mR32f(t), mR33a(t), mR33b(t)$$

1, 2069, 33104, 568, 33

21, 4688352, 75013638, 22161, 735

41, 19747934, 315966938, 47693, 1487

61, 45359256, 725748092, 74681, 2283

81, 81332560, 1301320957, 102453, 3116

101, 127349094, 2037585506, 130670, 3978

121, 183017578, 2928281246, 159127, 4865

141, 247906005, 3966496082, 187689, 5774  
161, 321560188, 5144963013, 216260, 6700  
181, 403515319, 6456245100, 244775, 7641  
201, 493303786, 7892860576, 273183, 8596  
221, 590460724, 9447371591, 301445, 9561  
241, 694528015, 11112448240, 329534, 10535  
261, 805057189, 12880915021, 357427, 11517  
281, 921611526, 14745784418, 385107, 12506  
301, 1043767551, 16700280810, 412560, 13499

```
> j:=41;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]);
for i from 1 by 20 while i < 302 do
    i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2]));
end do;
```

$$j := 41$$

$$mR33c(t), mR33d(t)$$

$$1, 1913, 251$$

$$21, 70509, 5618$$

$$41, 151190, 11377$$

$$61, 236708, 17493$$

$$81, 325020, 23898$$

$$101, 415070, 30542$$

$$121, 506207, 37388$$

$$141, 597990, 44405$$

161, 690110, 51568

181, 782335, 58856

201, 874491, 66252

221, 966443, 73741

241, 1058084, 81310

261, 1149331, 88946

281, 1240116, 96640

301, 1330383, 104383

>  
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**Comments:**

