Response to the comment by the Anonymous Referee #1

The authors thank the referee #1 for his/her valuable comments. In the revised paper, we clarify what the referee pointed out. The responses to each of the referee's comments are listed below.

Comment (1) *p.5176, l.4ff: Zonal wind tendencies are generally given in m/s/month. Because calendar months can have varying numbers of days, the unit m/s/day is more commonly used.*
It should therefore be clarified once in the text that "month" in this context refers to a fixed number of 30days, for example on p.5181, l.18. Once this has been clarified, numbers can easily be converted.

Response: We clarify this point in the revised manuscript [L147], following the referee's comment.

Comment (2) *p.5177, l.26: suggestion: inertio-gravity waves → gravity waves*
For inertio-gravity waves, it is usually assumed that $\hat{\omega} \sim f$*. Satellite observations, however, cover a larger range of intrinsic frequencies. As shown in Alexander et al., QJRMS, 2010, their Fig. 8b, satellites can observe gravity waves with intrinsic periods as short as ~1–2hours, much shorter than the intrinsic period given by the Coriolis parameter.*
Reference:
Alexander, M. J., et al.: Recent developments in gravity-wave effects in climate models and the global distribution of gravity-wave momentum flux from observations and models, Q. J. R. Meteorol. Soc., 136, 1103–1124, doi:10.1002/qj.637, 2010.

Response: We correct this point in the revised manuscript [L45], following the referee's suggestion.

Comment (3) *p.5179, l.20: It should be mentioned that comparison with observations shows that the ECMWF model strongly underestimates temperature fluctuations of mesoscale gravity waves (for example, Schroeder et al., 2009). Therefore reanalyses based on the ECMWF model, as well as other reanalyses, are also expected to generally underestimate such small-scale fluctuations.*
Citation;
Schroeder, S., Preusse, P., Ern, M., and Riese, M.: Gravity waves resolved in ECMWF and measured by SABER, Geophys. Res. Lett., 36, L10805, doi:10.1029/2008GL037054, 2009.

Response: Following the suggestion, we mention this point and add the reference in the revised manuscript [L94–95].

Comment (4) *p.5179: Not all parameters in equations (1)–(3) are defined in the text. Instead, it is referred to Andrews et al. (1987).*
Omitting these definitions is comprehensible because this is textbook knowledge. Including all these

definitions would considerably lengthen this section and reduce legibility. Further, I suppose that most readers interested in the topic of this study will be familiar with this notation. Therefore, I leave it to the authors whether the parameters should be explained here again, or not.

Response: For the reasons the referee mentioned, we do not change this part in the revised manuscript.

Comment (5) *Fig.1: The text in the lower left of each panel describing the different wave types is not easy to recognize.*
Suggestion: Either use a different color for this text, maybe red, or move this text to the left of the panels.

Response: The text in Fig. 1 is moved to the top of the panels in the revised figure.

Comment (6a) *p.5180, ll.3/4: Here, all zonal wavenumbers $|k| \leq 20$ are attributed to RGW waves. Usually, however, only $k < 0$ waves are attributed to the RGW wave band.*
By combining all $|k| \leq 20$, the wave bands of westward propagating RGW waves, and of eastward propagating n=0 inertia-gravity waves are mixed.
It is not clear whether:
(a) RGW waves and n=0 inertia-gravity waves are summarized in one contribution
This could be justified by the fact that the combined spectral band of RGW and n=0 inertia-gravity waves runs continuously from negative to positive zonal wavenumbers.
or:
(b) The further restriction of $F^{(z,H)}$ $F^{(z,M)} < 0$ suppresses most or all contributions of n=0 inertia-gravity waves.

Response: We clarify that the MRG wave refers to both of the westward and eastward propagating $n = 0$ waves in the revised manuscript [L107].

Comment (6b) *p.5180, ll.9/10: This comment is related to (6a). On p.5180, ll.9/10 it is stated that all remaining non-Kelvin and non-RGW waves with $|k| \leq 20$ are assumed to be Rossby waves, if $\omega <$ 0.4cycle/day.*
This, however, includes also eastward propagating waves that are no Rossby waves, for example n=0 inertia-gravity waves, if they have not been classified as RGW waves before.
On the other hand, the contribution of n=0 inertia-gravity waves may be negligible compared to the RGW or to the Rossby waves, and therefore would not be relevant for the exact definition of wave types.
Please clarify!

Response: Although the Rossby wave can have only negative k in the theory based on the nontransient solution, in reality, part of the Rossby wave can have some spectral power in $k > 0$ (see Figs. 3 and 4 in

KC15) when the wave packet is confined to a short time period. In the spectral domain of $\omega < 0.4$ cycle/day and $0 < k < 20$, after removing the Kelvin and MRG waves (i.e., n = 0 eastward wave), the remaining waves are primarily the Rossby waves because the inertia-gravity waves with $n > 0$ have much higher frequencies. We also confirmed that these low-frequency waves are in rotational mode (not shown). We refer to KC15 in the manuscript [L101, L109] for the details of the wave separation, because including the explanation of the details in this paper requires additional figures and repetition of a lengthy discussion which was already done in KC15.

Comment (7) *p.5180, l.18: It should be mentioned that in all figures the x-axis ticks correspond to 1st of January of the given year.*

Response: We mention this point in the revised manuscript [L120–121] following the referee's comment.

Comment (8) *p.5182, l.26: It should be mentioned that the net resolved wave forcing obtained for ERA-I_ml is similar to previous ERA-I estimates by Ern et al. (2014). Somewhat lower values in Ern et al. (2014) may arise from the larger latitude range of 10S–10N in their study.*

Response: Because the net resolved wave forcing is calculated using the same formulation of E–P flux and the same dataset as in Ern et al. (2014), the results must be similar. We do not point out this in the revised manuscript.

Comment (9) *p.5184, l.16:*
zonal wind shear → vertical shear of the zonal wind

Response: It is changed in the revised manuscript [L219] following the correction.

Comment (10) *p.5184, l.26: SD → standard deviation (SD)*

Response: It is changed in the revised manuscript [L228] following the correction.

Comment (11) *p.5184, l.26/27: Suggested rewording:*
This represents the magnitude of $\overline{u}_z$ *alternating → These values are governed by the magnitude of* $\overline{u}_z$ *that alternates*

Response: It is changed in the revised manuscript [L229] following the suggestion.

Comment (12) *p.5185, l.9: It should be pointed out more clearly that relative differences of ADVz between ERA-I and ERA-I_ml in Fig.4b may appear small. However, these differences of 2–4m/s/month can still be*

an important effect when calculating the residual drag from the tendency equation, which has typical values of ~10m/s/month.

Response: We clarify this point in the revised manuscript [L239–241] as the referee pointed out.

Comment (13) *p.5186, l.1: It should be more clearly mentioned that all terms in the curly brackets are from ERA-I_ml. Only the EP flux divergence of the resolved waves is from the other respective reanalysis.*

Response: We clarify this point in the revised manuscript [L257–258] as the referee pointed out.

Comment (14) *p.5186, ll.6/7: It should be mentioned that these values of* $\overline{X}^*$ *are similar to estimates by Ern et al. (2014). Somewhat higher values in Ern et al. (2014) may arise from a larger latitude range in their study.*

Response: We mention this point in the revised manuscript [L264] as the referee suggested.

Comment (15) *p.5186, ll.9/10: Some care has to be taken with this statement. Kelvin wave forcing is not a net forcing, while* $\overline{X}^*$ *is a net forcing. However, I have the impression that not only the Kelvin wave forcing, but also positive values of the ERA-I_ml net resolved forcing in Fig. 3 show somewhat stronger peak values than* $\overline{X}^*$.
For clarification, I would suggest to just add the word "net":
the mesoscale gravity wave forcing → the net mesoscale gravity wave forcing

Response: It is changed in the revised manuscript [L265–266] following the referee's suggestion.

Comment (16) *p.5187, l.18: the mesoscale gravity wave forcing → the net mesoscale gravity wave forcing*

Response: It is changed in the revised manuscript [L302] following the suggestion.

Comment (17) *p.5187, l.26:* $(2–4\Delta_V) \rightarrow (2\Delta_V – 4\Delta_V)$

Response: It is changed in the revised manuscript [L309] following the correction.

Comment (18) *p.5191, ll.16–19: Reference Kobayashi et al., 2015 should be updated. The final version of this article is now available at J. Meteorol. Soc. Jpn.*

Response: It is updated in the reference section of the revised manuscript.

Response to the comment by the Anonymous Referee #2

The authors thank the referee #2 for his/her valuable comments. Following the comments, we append a discussion on the wave forcing estimates averaged over 10°N-10°S in the revised manuscript, and provide the figures for the estimates over 10°N-10°S as a supplementary material. We also include the results at 50 hPa. The responses to each of the referee's comments are listed below.

Comment 1: *The relative roles of equatorial waves and large, medium, small-scale gravity waves depend on height as well as easterly/westerly shears (e.g. Kawatani et al. 2010). In the introduction and main results in this paper, the authors discussed the wave forcing only at 30 hPa and 10hPa. I believe the author should include more detailed discussion at 50 hPa and/or 70 hPa, which must be very useful information and required for the QBO community, since climate models failed to simulate the realistic amplitude of the QBO in the lower stratosphere.*

Response: Following the referee's suggestion, we include the results at 50 hPa in the revised manuscript [Table 3, L272–278].

Comment 2: *In addition, I believe that including other reanalysis datasets, such as ERA40 (although data available until August 2002), JRA-25, NCEP-1 and NCEP-2, must make this paper much more interesting and useful, for example, for the S-RIP (SPARC reanalysis Intercomparison project) activity.*

Response: We plan to calculate the estimates using the other reanalysis datasets that the referee mentioned, as we are involved in the S-RIP activity. However, the inclusion of the results from these datasets to this paper is not possible during the process of the paper, because download of the datasets takes too long time (several months). In this study, we discussed that the equatorial wave amplitude is damped in the p level datasets of the reanalyses, and the damping rate depends on the vertical resolution of the native models. The models of the old reanalyses have coarser vertical resolutions than those of the four most recent datasets used in this study. Thus, we expect that the wave forcing from the old datasets may be more underestimated than that from the recent datasets. No changes are applied in the revised manuscript regarding this comment.

Comment 3: *Another concern is to include the CFSR reanalysis in this paper. The previous CFSR model failed to simulate the QBO, and ERA-40 stratospheric wind profiles were used as bogus observations in CFSR data, at least from 1981 to 1998. I am not sure the latest CFSR model quality, but the authors should check this point.*

Response: As the referee commented, the early CFSR assimilation failed to capture the QBO in its streams 2 and 3, and the ERA-40 stratospheric wind profiles were used as bogus observations for the period of 1981-1998 to include a reasonable QBO signature (Saha et al., 2010). As a result, the QBO in the zonal mean

zonal wind is successfully captured in the CFSR. There does not exist enough information about the quality of the CFSR in terms of the equatorial wave perturbations. Somehow the CFSR exhibits some interesting features: for example, in Fig. 2, it is shown that the IG wave forcing in the E-W phase in CFSR is always larger than that in the other datasets. We keep including these CFSR results in the paper, taking into consideration the uncertainty of this reanalysis.

Comment 4: *Other major points are the latitudinal width (5S-5N) the authors discuss about wave forcing relevant to the QBO. As shown in your recent paper (Kim and Chun 2015, JGR), EP-flux divergences of equatorial waves and gravity waves distribute much wider latitudinal width. For example, E-MRG show eastward (small westward) wave forcing around 10 degree (over the equator), and W-MRG show westward (eastward) forcing over (off) the equator. The 5S-5N average is the reason why MRG show westward forcing both in easterly and westerly shear phase of the QBO (Fig. 1). Because the amplitude of the QBO is approximately Gaussian about the equator with a 12 degree half width (Baldwin et al. 2001), 5S-5N average is too narrow, at least for contents of this paper. The author should show results averaged in 10S-10N, for example. Related with this comment, how the authors treat n=0 eastward waves (eastward MRG) in this paper? Please clarify in the manuscript.*

Response: We calculate the wave forcing estimates over 5°S-5°N because 1) the wave forcing at higher latitudes (e.g., 10° or 15°) induces residual meridional circulation (v^*), and thus, is partly compensated by the Coriolis force (e.g., Haynes, 1998), and 2) the Coriolis force and meridional advection induced by v^* can be another source of uncertainty in the reanalyses. Over 5°S-5°N, these terms are small and can be ignored. Thus, we keep the estimates for 5°S-5°N in the manuscript. However, we also agree the referee's comment that the wave forcing is distributed in a wider latitudinal band. We provide the figures for the equatorial wave forcing and X averaged over 10°S-10°N as a supplementary material, and discuss them briefly at the end of the result section in the revised manuscript [L283–286]. Regarding the n = 0 eastward waves, we clarify that the MRG wave in this study includes the n = 0 eastward waves in the revised manuscript [L107].

Reference:

Haynes, P. H.: The latitudinal structure of the quasi-biennial oscillation, Q. J. R. Meteorol. Soc., 124, 2645–2670, 1998.

Saha, S., Moorthi, S., Pan, H.-L., Wu, X., Wang, J., Nadiga, S., Tripp, P., Kistler, R., Woollen, J., Behringer, D., Liu, H., Stokes, D., Grumbine, R., Gayno, G., Hou, Y.-T., Chuang, H., Juang, H.-M. H., Sela, J., Iredell, M., Treadon, R., Kleist, D., Delst, P. V., Keyser, D., Derber, J., Ek, M., Meng, J., Wei, H., Yang, R., Lord, S., van den Dool, H., Kumar, A., Wang, W., Long, C., Chelliah, M., Xue, Y., Huang, B., Schemm, J.-K., Ebisuzaki, W., Lin, R., Xie, P., Chen, M., Zhou, S., Higgins, W., Zou, C.-Z., Liu, Q., Chen, Y., Han, Y., Cucurull, L., Reynolds, R. W., Rutledge, G., and Goldberg, M.: The NCEP climate forecast system reanalysis, Bull. Am. Meteor. Soc., 91, 1015–1057, 2010.

Response to the comment by the Anonymous Referee #3

The authors thank the referee #3 for his/her valuable comments. In the revised manuscript, we clarify what the referee pointed out. The responses to each of the referee's comments are listed below.

Comment 1: *End of Sec 2: In Fig 1 you calculate EP fluxes for ERA-I at model-levels resolution. As I understand it, based on http://old.ecmwf.int/products/data/technical/model_levels/model_def_60.html, the ERA-I model levels are equivalent to pressure levels from 73 hPa upward. This would correspond to 18.3 km altitude for a log-pressure scale height of 7 km, just below the 19 km lower cutoff of your Fig 1. Based on this, it should be ok to apply the TEM equations for pressure coordinates to the ERA-I data on model levels, and I presume this is what you've done. But, please add a sentence or two here to clarify for the reader that this is the case. Or, if I've got it wrong, please explain what has been done.*

Response: As the referee presumed, we used the TEM equations for pressure coordinates to the ERA-I_ml. We clarify this in the revised manuscript [L96–98].

Comment 2: *Temporal resolution of the data: if I recall correctly, MERRA data is available at 3-hourly frequency and the other reanalyses at 6-hourly frequency. I'm not sure about that, but at any rate, please state in Sec 2 what is the temporal resolution of the data. If it differs between reanalyses, did you use the same frequency for all of them when doing the spectral analysis? If not, does it affect the results?*

Response: As the referee mentioned, MERRA data is available at 3-hourly frequency, and we used the MERRA data at this frequency. We also calculated the wave forcing estimates using 6-hourly subsampled MERRA data, and confirmed that the difference between the estimates from 3- and 6-hourly data is negligible. We include this information in the revised manuscript [L73–76].

Comment 3: *MRG wave phase speeds: in Fig 1, I was surprised to see westward forcing by MRG waves occurring in both westerly shear (E-W transition phase) and easterly shear (W-E transition phase). E.g. in mid-2007, westward forcing is occurring simultaneously in the lower (18-21 km) easterly shear zone and the upper (28-35 km) westerly shear zone. Is this due to there being MRG waves of both westward and eastward phase speeds included in the MRG group? From Fig 9b,c of KC15 I see that both westward and eastward propagating MRG waves give westward forcing at the equator (at least, in HadGEM2), within the 5S-5N band that your Fig 1 covers. In that case, I presume the westward forcing in easterly shear would be due to westward propagating MRG waves, and the westward forcing in westerly shear would be due to eastward propagating MRG waves. Is this the correct interpretation? It would be helpful to add a brief comment to clarify this (or whatever is the explanation, if I've got it wrong) in the discussion of Fig 1, perhaps at line 21 on p 6.*

Response: Figure A1 shows the westward (W) and eastward (E) propagating MRG wave forcing averaged over 5°N–5°S. As the referee mentioned, the forcing in the easterly shear is by the W-MRG wave. However, in the westerly shear also, the W-MRG wave forcing is larger than the E-MRG wave forcing. It implies that the W-MRG wave exists above the easterly jet core. The existence of the W-MRG wave above the easterly QBO wind was also reported by Maury and Lott (2014) using ERA-I. One possible explanation for this is the stratospheric generation of the W-MRG wave (Maury and Lott, 2014). Figure A2 shows the latitude–height cross section of the E–P flux and its divergence by the W-MRG wave in June 2007. It is shown in Fig. A2 that the E–P flux from the W-MRG wave is small around the easterly jet core (around z ~ 28 km), and it suddenly increases above the jet core (cf. Fig. 9c in KC15). This may support the hypothesis of the stratospheric generation of W-MRG wave, which merits further study in the future. We discuss this point in the revised manuscript [L124–126].

Technical corrections:

p2, 2: suggest: "momentum forcing by equatorial waves to the QBO" –> "momentum forcing of the QBO by equatorial waves"

Response: The correction is applied in the revised manuscript [L2].

p2, 5: suggest move "(3– 11 m s−1 month−1)" to right after "all equatorial wave modes", so as to be clear that this is the net forcing by all equatorial wave modes during the 30 hPa E-to-W transition.

Response: The correction is applied in the revised manuscript [L5].

P2, 12: "easterly-to-westerly phase" –> "easterly-to-westerly transition phase"

Response: The correction is applied in the revised manuscript [L11].

p3, 5: convections –> convection

Response: The correction is applied in the revised manuscript [L27].

p6, 26: suggest add "at altitudes below 30 km" following "phases of the QBO". Strong Rossby wave forcing in Fig 1 does coincide with easterly onsets at very high altitudes.

Response: The correction is applied in the revised manuscript [L131].

p12, 18-19: "The increase in forcing from other waves at 10 hPa is not large (see also Fig. 1).": I find this sentence a little unclear, suggest rephrase as: "For other waves, the forcing at 10 hPa not much larger than that at 30 hPa (see also Fig. 1)."

Response: This sentence is removed while rewriting this paragraph in the revised manuscript.

P12, 24-25: "due to the less constraints on" –> "due to fewer constraints acting on"

Response: The correction is applied in the revised manuscript [L281–282].

Reference:

Maury, P., and Lott, F.: On the presence of equatorial waves in the lower stratosphere of a general circulation model, Atmos. Phys. Chem., 14, 1869–1880, doi:10.5194/acp-14-1869-2014, 2014.

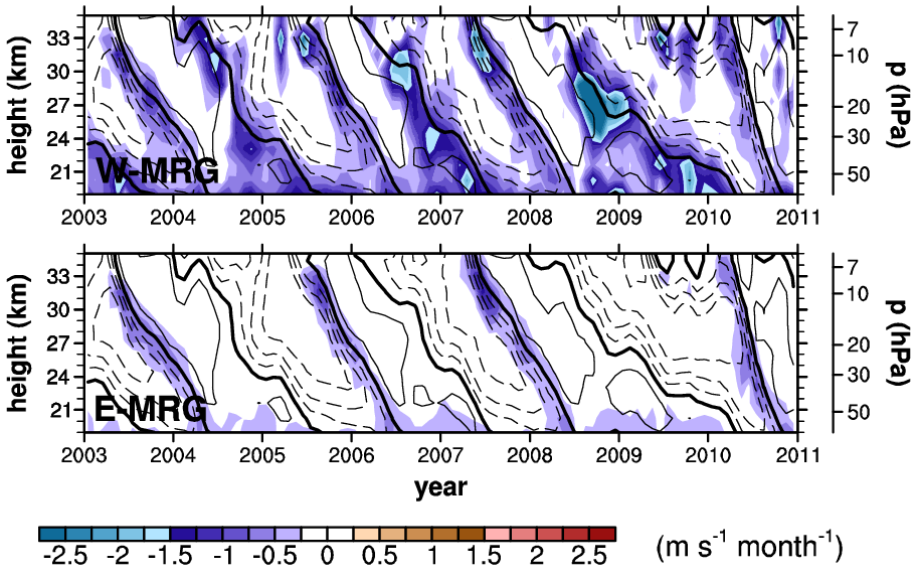

Figure A1. Time–height cross-sections of the zonal momentum forcing by the (upper) westward and (lower) eastward propagating MRG waves averaged over 5°N–5°S, obtained using the model-level data of ERA-I over the period 2003–2010 (shading). The zonal mean wind over the same latitudinal band is superimposed at intervals of 10 m s^{-1} (contour). The thin solid, dashed, and thick solid lines indicate westerly, easterly, and zero wind, respectively.

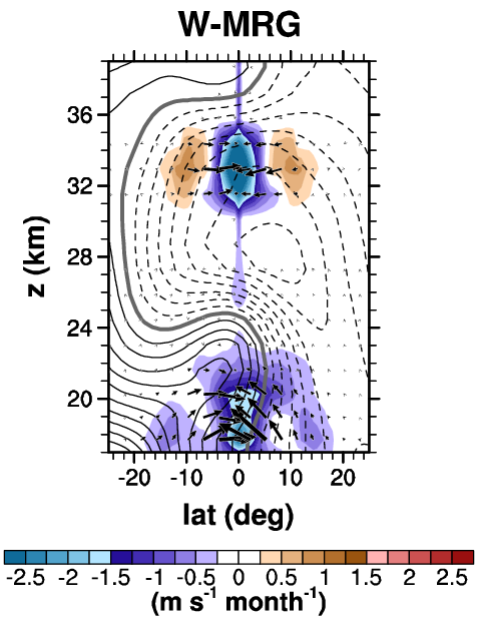

Figure A2. Latitude–height cross sections of the E–P flux (arrow) and its divergence forcing (shading) for the westward MRG wave from the model-level data of ERA-I in June 2007. The westerly (thin solid), easterly (dashed), and zero winds (thick solid) are superimposed with an interval of 5 m s^{-1}. The E–P flux is multiplied by exp(z/2H) for display purposes (H = 6.6 km).

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with version 2014/07/29 7.12 Copernicus papers of the LaTeX class copernicus.cls.
Date: 20 May 2015

Momentum forcing of the QBO by equatorial waves in recent reanalyses

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Abstract. The momentum forcing of the QBO by equatorial waves ~~to the QBO~~ is estimated using recent reanalyses. Based on the estimation using the conventional pressure level datasets, the forcing by the Kelvin waves (3–9 $\mathrm{m\,s^{-1}\,month^{-1}}$) dominates the net forcing by all equatorial wave modes (3–11 $\mathrm{m\,s^{-1}\,month^{-1}}$) in the easterly-to-westerly transition phase at 30 hPa~~(3–11)~~. In the opposite phase, the net forcing by equatorial wave modes is small (1–5 $\mathrm{m\,s^{-1}\,month^{-1}}$). By comparing the results with those from the native model-level dataset of the ERA-Interim reanalysis, it is suggested that the use of conventional-level data causes the Kelvin wave forcing to be underestimated by 2–4 $\mathrm{m\,s^{-1}\,month^{-1}}$. The momentum forcing by mesoscale gravity waves, which are unresolved in the reanalyses, is deduced from the residual of the zonal wind tendency equation. In the easterly-to-westerly transition phase at 30 hPa, the mesoscale gravity wave forcing is found to be smaller than the resolved wave forcing, whereas the gravity wave forcing dominates over the resolved wave forcing in the opposite phase. Finally, we discuss the uncertainties in the wave forcing estimates using the reanalyses.

1 Introduction

The quasi-biennial oscillation (QBO) is the predominant variability of the tropical stratosphere with periods of about 20–35 months (Baldwin et al., 2001). The QBO is most prominent in the zonal wind field, alternating between easterly and westerly. The alternating jets modulate interannual extratropical wave activities, and impact on the strength of the polar stratospheric vortex (Holton and Tan, 1980; Watson and Gray, 2014). The QBO also induces the secondary meridional circulation (Plumb and Bell, 1982), which modulates the distribution of chemical species in the tropics and extratropics (Hilsenrath and Schlesinger, 1981; Li and Tung, 2014). For these reasons, it is important to understand and model the QBO. In practice, such modulations of the polar vortex and chemical species distributions cannot be reproduced by global models in which the QBO is not simulated.

The QBO is driven by equatorial waves interacting with the stratospheric mean flow (Lindzen and Holton, 1968; Holton and Lindzen, 1972). It is thought that these equatorial waves are mainly generated by tropical ~~convections~~ convection (e.g., Salby and Garcia, 1987; Garcia and Salby, 1987; Hayashi and Golder, 1997). Thus, realistic simulations of the QBO require a suitable parameterization of the convection, a spatial resolution that can resolve the large-scale equatorial waves, and an appropriate parameterization of unresolved-scale convective gravity waves. Recently, robust QBO signals (i.e., persistent oscillation with periods close to the observed values) have been generated in several general circulation models (e.g., Scaife et al., 2000; Giorgetta et al., 2002; Shibata and Deushi, 2005; Kim et al., 2013; Kawatani et al., 2014; Schirber et al., 2014; Richter et al., 2014; Aquila et al., 2014; Rind et al., 2014). However, the QBO simulated by each model exhibits different features (e.g., different vertical structures or period ranges). Furthermore, the forcings driving the QBO are model-dependent. For example, at 20 hPa, Giorgetta et al. (2006) showed that the large-scale (model-resolved) wave forcing is larger than the forcing produced by parameterized

gravity waves (PGWs) in the easterly-to-westerly transition (E–W) phase, whereas the PGW forcing is dominant in the westerly-to-easterly transition (W–E) phase in the MAECHAM5 model. In contrast, in the HadGEM2 (Bushell et al., 2010; Kim and Chun, 2015) and CAM5 (Richter et al., 2014) models, the PGW forcing is dominant in both phases at this altitude. Therefore, it is necessary to quantitatively constrain the forcing due to equatorial waves based on observations, which motivates this study.

It is difficult to directly measure the momentum forcing due to equatorial waves from observations, as this requires the simultaneous measurement of horizontal and vertical winds. Instead, for the Kelvin and ~~inertio-gravity~~ gravity waves, momentum forcing has been estimated from temperature measurements (and sometimes along with the zonal wind) given by radiosonde and satellites using gravity wave theory (e.g., Sato et al., 1997; Ern and Preusse, 2009; Alexander and Ortland, 2010; Ern et al., 2014). An alternative to estimations from measurements is to use reanalyses. In the equatorial lower stratosphere, the horizontal wind and temperature data from radiosonde observations are assimilated in the reanalyses, along with satellite-observed temperature data from after 1979. It should be noted, however, that the vertical velocity is poorly constrained in the reanalyses. This might result in a spread of estimated wave forcings between the reanalyses, along with many other factors (e.g., different assimilation processes).

This study aims to estimate the momentum forcing due to equatorial waves in the reanalysis datasets. The equatorial waves resolved in the reanalyses are classified into Kelvin, mixed Rossby-gravity, inertio-gravity, and Rossby waves, and the forcing from each wave type is estimated. In addition, the forcing by smaller-scale waves that are unresolved in the reanalyses is also estimated by comparing the resolved wave forcing with the total forcing required for the QBO progression.

2 Data and method

Four recent reanalyses are used: the ECMWF (European Centre for Medium-Range Weather Forecasts) Interim Reanalysis (ERA-I, Dee et al., 2011), Modern-Era Retrospective Analysis for Research and Applications (MERRA, Rienecker et al., 2011), Climate Forecast System Reanalysis (CFSR, Saha et al., 2010), and Japanese 55 year Reanalysis (JRA-55, Kobayashi et al., 2015). The resolutions of these reanalyses are presented in Table 1. The horizontal resolutions of the native models for these reanalyses range from 0.38 to 0.7°. The models have 10–13 vertical levels between about 70 and 10 hPa. The reanalysis datasets are available for variables that are interpolated vertically to the conventional pressure (p) levels (e.g., 100, 70, 50, 30, 20, 10, and 7 hPa) from the model levels. In this study, we use p level datasets with horizontal resolutions reduced to around $2\Delta_{\mathrm{h}}$, where Δ_{h} is the native resolution of the model (see Table 1). Provided that the effective resolution of weather prediction models is typically coarser than $4\Delta_{\mathrm{h}}$ (e.g., Skamarock et al., 2014), a horizontal resolution of $\sim 2\Delta_{\mathrm{h}}$ is sufficient to analyze the equatorial waves resolved by these reanalyses. To examine the sensitivity of the wave forcing estimation to the vertical level of the reanalysis datasets, we also use the native model-level dataset of ERA-I. The ~~data~~ temporal resolution of the data used is 3 hours for MERRA and 6 hours for the others. Additionally, we calculated the wave forcing estimates using 6-hourly subsampled MERRA data (not shown), and confirmed that the difference between the results from 3- and 6-hourly data is negligible. The data in all reanalyses cover the period 1979–2010.

The zonal momentum forcing due to stratospheric waves is calculated in the transformed Eulerian-mean (TEM) equation (Andrews et al., 1987):

$$\overline{u}_{\mathrm{t}} = \overline{v}^{*}\left[f - (a\cos\phi)^{-1}\left(\overline{u}\cos\phi\right)_{\phi}\right] - \overline{w}^{*}\overline{u}_{z} + (\rho_0 a\cos\phi)^{-1}\nabla\cdot\boldsymbol{F} + \overline{X}. \tag{1}$$

The notation follows the conventions described in Andrews et al. (1987). Here, $\boldsymbol{F} = \left(F^{(\phi)}, F^{(z)}\right)$ is the Eliassen–Palm (E–P) flux, defined by

$$F^{(\phi)} = \rho_0 a \cos\phi \left(\overline{u}_z \overline{v'\theta'}/\overline{\theta}_z - \overline{v'u'}\right), \tag{2}$$

$$F^{(z)} = \rho_0 a \cos\phi \left\{ \left[f - (a\cos\phi)^{-1} (\overline{u}\cos\phi)_\phi\right] \overline{v'\theta'}/\overline{\theta}_z - \overline{w'u'} \right\}. \tag{3}$$

The first term on the right-hand side of Eq. (1) is the sum of the Coriolis force and meridional advection, and the second term is the vertical advection. The third term represents the net momentum forcing by the waves resolved in the data. The term $\overline{X}$ represents any other zonal forcing, which can be obtained by subtracting the Coriolis force, the meridional and vertical advection, and the net resolved wave forcing from the zonal wind tendency (i.e., residual of the tendency equation). This term incorporates small-scale processes unresolved in the reanalysis, including mesoscale gravity waves and smaller-scale turbulent diffusion. It can also include resolved-scale waves if they are erroneously assimilated so that the other terms in Eq. (1) are under- or over-estimated. For example, it has been reported that the amplitude of the resolved-scale gravity waves in (re)analysis datasets is smaller than that of the observed waves with the similar scale (e.g., Schroeder et al., 2009) , which may affect the estimates of not only the E–P flux forcing term but also $\overline{X}$. Equation (1), the TEM equation for pressure coordinates, is used for the model-level dataset as well as for the p level datasets, as the model level of ERA-I above 73 hPa ($\sim$ 18 km) is on the constant pressure level.

The momentum forcing produced by each of the equatorial modes can be calculated after separating the perturbations in Eqs. (2)–(3) into each wave mode, following Kim and Chun (2015, KC15 hereafter). The separation of wave modes is explained in detail in Sect. 4 of KC15, and is briefly described here. The perturbation variables are split into symmetric and anti-symmetric components with respect to the equator, and each component is transformed to the zonal wavenumber–frequency

(k–ω) domain. In the symmetric spectrum, the perturbations for the Kelvin waves are restricted to $0 < k \leq 20$ and $\omega < 0.75\,\mathrm{cycle\,day^{-1}}$, and those for the mixed Rossby-gravity (MRG) waves are restricted to $|k| \leq 20$ and $0.1 \leq \omega \leq 0.5\,\mathrm{cycle\,day^{-1}}$ in the anti-symmetric spectrum. These two In this paper, the MRG waves refer to both of the westward and eastward propagating $n = 0$ waves. The two equatorial modes are further restricted in the spectral components (k, ω) by requiring $|F^{(z,H)}| < |F^{(z,M)}|$ (Kelvin waves) and $F^{(z,H)}F^{(z,M)} < 0$ (MRG waves) (see KC15), where $F^{(z,H)}$ and $F^{(z,M)}$ are the contributions of the meridional heat flux and vertical momentum flux to $F^{(z)}$ (i.e., the first and second terms on the right-hand side of Eq. 3), respectively, for a given (k, ω). Spectral components that are not defined as Kelvin or MRG waves are classified as Rossby waves if $|k| \leq 20$ and $\omega \leq 0.4\,\mathrm{cycle\,day^{-1}}$, and as inertio-gravity (IG) waves otherwise. After separating the perturbations into the four wave modes, the forcing is calculated by $(\rho_0 a \cos\phi)^{-1}\nabla \cdot \boldsymbol{F}^{\mathrm{W}}$, where $\boldsymbol{F}^{\mathrm{W}}$ represents the E–P flux due to each mode.

3 Results

3.1 Momentum forcing by the waves resolved in the reanalyses

The time–height cross-sections of the forcing by equatorial waves, averaged over 5° N–5° S regions, are shown in Fig. 1, where model-level data from ERA-I has been used for recent years (2003–2010). For all figures in this paper except Fig. 5, the ticks on the horizontal axis correspond to the 1st of January of the given years. The eastward forcing by the Kelvin waves appears in the QBO phase of strong westerly shear. The MRG waves induce westward forcing in both phases of the westerly and easterly shear, with comparable magnitudes between the phases (Kawatani et al., 2010a, b, and KC15). The MRG wave forcing is primarily by the westward propagating mode not only in the easterly shear but also in the westerly shear (not shown), which may suggest the possibility of

stratospheric generation of the wave above the easterly jet (see Maury and Lott, 2014, and KC15) . For the Kelvin and MRG waves, the altitude and magnitude of the maximum forcing in each QBO cycle vary significantly. The IG waves provide eastward and westward forcing in the westerly and easterly shear phases, respectively. The Rossby wave forcing is strong in the upper stratosphere. Unlike the other waves, the Rossby wave forcing is not aligned with the strong-shear phases of the QBO at altitudes below 30 km. Rather, it has significant magnitudes in the northern winters and summers, and is weakened in the following seasons. In addition, this forcing does not appear in the strong easterlies of the QBO, as the Rossby waves do not propagate easily with the easterly background wind. These features in the vertical structure of the equatorial wave forcing are generally similar between the reanalysis datasets (not shown). Here, we select ~~two levels,~~ three levels, 50, 30, and 10 hPa, to assess the wave forcing in the reanalyses in detail. Note that the level of 10 hPa is close to the upper limit of the sonde sounding assimilated to the reanalyses.

Figure 2 shows the zonal forcing given by the Kelvin, MRG, IG, and Rossby waves at 30 hPa in 1979–2010, as obtained using the p level data of the four reanalyses, as well as the net forcing due to all resolved waves. The spread between the four reanalyses (i.e., the difference between upper and lower bounds of the wave forcing estimated from each dataset) is also indicated (gray shading). The phases of the maximum easterly (westerly) in each QBO cycle at 30 hPa are indicated by the dashed (solid) vertical lines in Fig. 2. The temporal evolution of the equatorial wave forcing is, at the first order, consistent between the datasets. The peak magnitude of the Kelvin wave forcing in the E–W phase shows similar cycle-to-cycle variations in all reanalyses. For instance, the Kelvin wave forcing in the four reanalyses is strong in 2010 (7.1–8.7 $\mathrm{m\,s^{-1}\,month^{-1}}$) and weak in 1992 (2.8–4.7 $\mathrm{m\,s^{-1}\,month^{-1}}$; here, the month in the unit of forcing refers to 30 days regardless of the month). Prior to around 1993, the MRG wave forcing in the reanalyses seems relatively sporadic and weak compared to afterward, although the forcing in 1980 and 1985 has exceptionally large

peaks in MERRA. The magnitude of the MRG wave forcing reaches $\sim 2\,\mathrm{m\,s^{-1}\,month^{-1}}$. The IG wave forcing varies between -3 and $4\,\mathrm{m\,s^{-1}\,month^{-1}}$, following the QBO phase. The Rossby wave forcing magnitude is less than or similar to $\sim 2\,\mathrm{m\,s^{-1}\,month^{-1}}$ in most years, except in 1980, 1988, and 2008 for CFSR and ERA-I (3–3.5 $\mathrm{m\,s^{-1}\,month^{-1}}$). The net wave forcing has large positive peaks in the E–W phases (3.4–11 $\mathrm{m\,s^{-1}\,month^{-1}}$), due mainly to the Kelvin waves, and is negative during the W–E phases (1.5–5.2 $\mathrm{m\,s^{-1}\,month^{-1}}$) by the IG, MRG, and Rossby waves (Fig. 2). The peak forcing ranges during the E–W and W–E phases are summarized for each wave in Table 2.

Although the evolution of the wave forcing is generally consistent between the reanalyses, some robust differences in forcing magnitude are shown in Fig. 2. The positive peaks of the IG wave forcing are always larger in CFSR than in the other datasets, and the Rossby wave forcing tends to be larger in CFSR and ERA-I than in MERRA and JRA-55. There are differences between the reanalyses of up to about $2\,\mathrm{m\,s^{-1}\,month^{-1}}$ for the Kelvin, IG, and Rossby waves, and about $1\,\mathrm{m\,s^{-1}\,month^{-1}}$ for the MRG waves (Fig. 2). The difference in the net wave forcing is up to about $4\,\mathrm{m\,s^{-1}\,month^{-1}}$. There are many potential causes for this spread of forcing magnitudes between the reanalyses. For instance, each reanalysis used a different assimilation method, assimilated different observational data, and essentially used a different forecast model (e.g., in terms of model dynamics and resolutions). In addition, the species and numbers of assimilated observational data for a single reanalysis are dependent on time, particularly the satellite data. This makes the further investigation of temporal variations in wave forcing complicated. Therefore, in this study, we focus on assessing the range of wave forcing revealed by the reanalyses, and do not speculate on the causes of the spread, or temporal variations, in the reanalyses.

Figure 3 shows the wave forcing at 30 hPa calculated using the model-level data of ERA-I (ERA-I_ml), along with that using the p level data of ERA-I. The plot exhibits robust differences in Kelvin and IG wave forcing between the two datasets. The peaks of the Kelvin wave forcing in the E–W

phase from ERA-I_ml range from 6.7 to 13 $\mathrm{m\,s^{-1}\,month^{-1}}$ which are 2–4 $\mathrm{m\,s^{-1}\,month^{-1}}$ larger than those from ERA-I. The IG wave forcing from ERA-I_ml has positive and negative peaks that are 0.8–2.7 $\mathrm{m\,s^{-1}\,month^{-1}}$ larger than those from ERA-I. The differences in the MRG and Rossby wave forcing depend on the year, and are typically less than $\sim 1\,\mathrm{m\,s^{-1}\,month^{-1}}$. The net wave forcing in the E–W (W–E) phase is 4–9 $\mathrm{m\,s^{-1}\,month^{-1}}$ (1–4 $\mathrm{m\,s^{-1}\,month^{-1}}$) larger in the model-level result than in the p level output.

The differences in forcing magnitude between the two ERA-I datasets are mainly a result of the vertical interpolation process. When perturbations in the model-level data are interpolated to the p levels, those parts of waves with short vertical wavelengths are inevitably damped. For example, when a p level is centered between two model levels, waves with a vertical wavelength of $2\Delta_{\mathrm{v}}$ are totally filtered out by the interpolation, where Δ_{v} is the vertical spacing between the two model levels. The filtering rate of waves with larger vertical wavelengths depends on the interpolation method. Waves with a wavelength of $4\Delta_{\mathrm{v}}$ will be filtered at a rate of 50 % in terms of their variance under linear interpolation, although this will decrease if a higher-order method is used. Given that Δ_{v} in the lower stratosphere is approximately 1.4 km in ERA-I, waves with vertical wavelengths shorter than about 5.6 km might be significantly damped in the ERA-I p level data. These wavelengths are close to the lower bound of the dominantly observed Kelvin waves (6–10 km) and MRG waves (4–8 km) (Andrews et al., 1987). It is important that radiative damping, which induces the wave forcing in the atmosphere, is more prevalent in short vertical-scale waves (e.g., Fels, 1982; Krismer and Giorgetta, 2014) than in longer waves that may be contained in both datasets. This results in substantial differences between the two datasets, as shown in Fig. 3. The same may also be true for the other reanalyses. Unfortunately, not all the reanalyses provide model-level datasets. However, the vertical resolution of the native models in the lower stratosphere is comparable across all reanalyses (Table 1). Thus, the magnitude of the wave forcing obtained from the p level datasets of reanaly-

ses other than ERA-I (Fig. 2) should also be considered as underestimated, potentially by amounts comparable to those in ERA-I.

3.2 Estimated momentum forcing by the waves unresolved in the reanalyses

As mentioned in Sect. 2, the term $\overline{X}$ in Eq. (1) represents the zonal forcing by unresolved mesoscale gravity waves and turbulent diffusion, and is also influenced by the resolved-scale processes that are erroneously represented in the reanalyses. If one assumes that the resolved-scale processes are well represented in the reanalyses, the forcing by unresolved processes can be approximated as $\overline{X}$. In this section, we calculate the vertical advection of zonal wind (the second term on the right-hand side of Eq. (1), ADVz hereafter), and estimate the range of $\overline{X}$ in the reanalyses. A discussion of the above assumption is included in the next section.

Figure 4a shows ADVz, obtained using the p level data of the four reanalyses. The peak magnitude of ADVz in the W–E phase is around $10\,\mathrm{m\,s^{-1}\,month^{-1}}$, and that in the E–W phase is typically 1–4 $\mathrm{m\,s^{-1}\,month^{-1}}$ (excluding the anomalously large peaks in 1983 and 1986–1987 in CFSR). Note that ADVz in the W–E phase is much larger than the net resolved wave forcing in the same phase (1.5–5.2 $\mathrm{m\,s^{-1}\,month^{-1}}$, Table 2), and the two terms have opposite signs. There exist some robust ADVz features in the W–E phase: ADVz is very similar in ERA-I and JRA-55, and ADVz in MERRA is about half of that in ERA-I or JRA-55 in many years. As a result, the spread between the reanalyses is quite large ($\sim 10\,\mathrm{m\,s^{-1}\,month^{-1}}$) in this phase (Fig. 4a).

The large spread in the W–E phase between the different reanalyses suggests that the ADVz values obtained from the reanalyses are highly uncertain. Moreover, it is speculated that this spread may result in a large spread in $\overline{X}$, as will be seen later. Therefore, the difference in ADVz between the reanalyses is further investigated by comparing $\overline{w}^*$ and the ~~zonal wind shear~~ vertical shear of zonal wind ($\overline{u}_z$). Figure 5a shows the climatologies of $\overline{w}^*$ obtained from each dataset. The profiles of $\overline{w}^*$

from ERA-I and JRA-55 are in good agreement. However, below 30 hPa, $\overline{w}^*$ in MERRA is much smaller than in the other datasets, and that in CFSR is much larger than in the others above 10 hPa. The profiles of $\overline{w}^*$ in ERA-I show only slight differences between the p and model-level data. In previous studies by Niwano et al. (2003) and Schoeberl et al. (2008), the annual-mean ascent rate was inferred from the observed H_2O to be about 0.26–0.35 $\mathrm{mm\,s^{-1}}$ near 30 hPa. In Fig. 5a, $\overline{w}^*$ at 30 hPa in ERA-I, CFSR, and JRA-55 is within this range of values. The smaller value of $\overline{w}^*$ in MERRA causes ADVz to be underestimated (see Fig. 4a), and contributes to the large spread of ADVz.

Figure 5b shows the ~~SD~~ standard deviation of $\overline{u}_z$ obtained from each reanalysis dataset. ~~This represents~~ These values are governed by the magnitude of $\overline{u}_z$ ~~alternating~~ that alternates between positive and negative with the QBO phase. Note that the difference in monthly and zonal mean wind between the reanalyses is small (not shown). Therefore, $\overline{u}_z$ is mainly dependent on the intervals between the p levels. The ~~SD~~ standard deviation of $\overline{u}_z$ in ERA-I, CFSR, and JRA-55 is similar, as they have the same p levels. MERRA has one more p level, at 40 hPa, and thus the magnitude of $\overline{u}_z$ near 40 hPa in MERRA is larger than in the others. In all of the reanalyses, the limited sampling across vertical levels causes the magnitude of $\overline{u}_z$ obtained from the p level datasets to be underestimated compared to $\overline{u}_z$ from the model-level data (Fig. 5b). This implies that, as for the wave forcing, the ADVz values from the p level datasets should also be considered as underestimations. The ADVz obtained from ERA-I_ml is presented in Fig. 4b. It can be seen that ADVz in the W–E phase from ERA-I_ml is consistently 2–4 $\mathrm{m\,s^{-1}\,month^{-1}}$ greater than that from the p level data. Although this magnitude of difference between the p and model-level data seems small in Fig. 4b, it can have a significant effect in the estimation of $\overline{X}$ which has typical values of $\sim 10\,\mathrm{m\,s^{-1}\,month^{-1}}$ as will be shown later. The Coriolis force and meridional advection terms in Eq. (1) are generally small near the equatorial lower stratosphere (not shown).

Figure 6a shows the value of $\overline{X}$ at 30 hPa obtained from the p level datasets of the reanalyses. The positive peaks of $\overline{X}$ in the E–W phase range from 5.8 to 17 $\mathrm{m\,s^{-1}\,month^{-1}}$, and the negative peaks in the W–E phases vary from 6.6 to 21 $\mathrm{m\,s^{-1}\,month^{-1}}$. $\overline{X}$ in the E–W phase is about 50 % larger than the net resolved wave forcing (3.4–11 $\mathrm{m\,s^{-1}\,month^{-1}}$), and that in the W–E phase is much larger than the net resolved wave forcing (1.5–5.2 $\mathrm{m\,s^{-1}\,month^{-1}}$). The spread in $\overline{X}$ between the reanalyses is up to 10 $\mathrm{m\,s^{-1}\,month^{-1}}$, except in 1983 and 1986–1987, when the ADVz in CFSR has abnormally large peaks (Fig. 4a). The large spread in $\overline{X}$ could be expected because of the large spread in ADVz (Fig. 4a). From Fig. 5a, we can see that a large portion of the spread in ADVz is due to the underestimated vertical velocity in MERRA. Additionally, the zonal wind shear is underestimated in all of the p level datasets. Therefore, we attempt to partly correct the estimates of $\overline{X}$ via an additional calculation ($\overline{X}^*$). In this calculation, ERA-I_ml is considered as reference data for all the terms in Eq. (1), except for the wave-forcing term. $\overline{X}^*$ is estimated as:

$$\overline{X}^* = \left\{\overline{u}_\mathrm{t} - \overline{v}^* \left[f - (a\cos\phi)^{-1}\left(\overline{u}\cos\phi\right)_\phi\right] + \overline{w}^*\overline{u}_z\right\}^\mathrm{r} - (\rho_0 a\cos\phi)^{-1}\nabla\cdot\boldsymbol{F}, \tag{4}$$

where a superscript r denotes terms calculated using the reference data, and the E–P flux divergence term is calculated using the respective reanalyses. $\overline{X}^*$ is plotted in Fig. 6b. The negative peaks of $\overline{X}^*$ in the W–E phase are larger than those of $\overline{X}$ by 5–12 $\mathrm{m\,s^{-1}\,month^{-1}}$, particularly for MERRA. The changes in positive peaks do not appear to be large. The spread in $\overline{X}^*$ is up to $\sim 4\,\mathrm{m\,s^{-1}\,month^{-1}}$, which results from the spread in resolved wave forcing (see Eq. 4). Finally, $\overline{X}^*$ in ERA-I_ml is shown in Fig. 6c. The positive peaks of $\overline{X}^*$ in the E–W phase in ERA-I_ml are 3.1–11 $\mathrm{m\,s^{-1}\,month^{-1}}$, and the negative peaks in the W–E phase are 11–18 $\mathrm{m\,s^{-1}\,month^{-1}}$. These values of $\overline{X}^*$ are comparable with those estimated by Ern et al. (2014) . The positive peaks are smaller than those of the Kelvin wave forcing, suggesting that the peak magnitudes of the net

mesoscale gravity wave forcing in the E–W phase at 30 hPa might be smaller than those of the Kelvin wave forcing. In contrast, the large negative values of $\overline{X}^*$ suggest that gravity waves are the dominant contributors to QBO in the W–E phase, assuming that the turbulent diffusion is not of comparable magnitude. These results are consistent with those from previous studies using mechanistic, general circulation, or mesoscale models (e.g., Dunkerton, 1997; Giorgetta et al., 2006; Evan et al., 2012).

The ~~forcing due to equatorial wave modes, net resolved wave forcing , $\overline{X}$, and $\overline{X}^*$ at~~ wave forcing estimates at 50 and 10 hPa are also presented in ~~Table 3. The significant difference between the wave forcing~~ Tables 3 and 4, respectively. From Tables 2–4, it is shown that the Kelvin wave forcing in the E–W phase tends to increase with height from 2.7–9.2 $\mathrm{m\,s^{-1}\,month^{-1}}$ at 50 hPa to 2.2–15 $\mathrm{m\,s^{-1}\,month^{-1}}$ at 10~~and 30~~ hPa~~is the large forcing by the Rossby waves in the W–E phase, which~~ , and the IG wave forcing from 0.5–2.5 to 0.5–6.2 $\mathrm{m\,s^{-1}\,month^{-1}}$. The Rossby wave forcing exhibits an abrupt change between 30 and 10 hPa, and it reaches 14 $\mathrm{m\,s^{-1}\,month^{-1}}$ ~~. The increase in forcing from other waves~~ at 10 hPa ~~is not large~~ in the W–E phase (see also Fig. 1). $\overline{X}^*$ ~~becomes~~ depends significantly on the height, so that it is twice larger at 10~~than at 30 , particularly in the W–E phase, where the difference is about~~ hPa than at 50 hPa in both phases. This may reflect an increase in mesoscale gravity wave forcing at 10 hPa in both phases of the QBO. However, it should be noted that the spread in resolved wave forcing, ADVz, and $\overline{X}^*$ at 10 hPa across all reanalyses is 2–3 times larger than that at 30 hPa (not shown), implying less reliability of the forcing estimates at this altitude. This result might be due to ~~the less constraints~~ fewer constraints acting on the wind and temperature fields near 10 hPa in the reanalyses, owing to the vertical coverage of radiosonde observations. We additionally calculated the wave forcing estimates averaged over 10°N–10°S at 30 hPa (Figs. S1–S3 in the Supplement). The results are generally similar with those for 5°N–5°S

(Figs. 2, 3, and 6), except that the Kelvin (MRG) wave forcing is about 31 % (10–70 %) smaller when averaged over 10°N–10°S.

4 Summary and discussions

We have examined four reanalyses with the aim of estimating the momentum forcing of the QBO due to equatorial waves over the period 1979–2010. The temporal evolution of the forcing by equatorial wave modes is generally consistent between the reanalyses. The range of forcing by each wave mode is summarized in Tables ~~2–3~~2–4. In the estimates for the E–W phase using the p level datasets from the four reanalyses, the Kelvin wave forcing at 30 hPa (2.8–8.7 $\mathrm{m\,s^{-1}\,month^{-1}}$) was found to dominate the net wave forcing resolved in the datasets (3.4–11 $\mathrm{m\,s^{-1}\,month^{-1}}$). The forcing due to the MRG, IG, and Rossby waves in the W–E phase was found to be small, with a net forcing of 1.5–5.2 $\mathrm{m\,s^{-1}\,month^{-1}}$. The momentum forcing by processes that are not resolved in the reanalyses, which may be dominated by the mesoscale gravity waves, was also estimated. The unresolved forcing in the E–W phase ranges from 5.8 to 14 $\mathrm{m\,s^{-1}\,month^{-1}}$, and that in the W–E phase from 11 to 21 $\mathrm{m\,s^{-1}\,month^{-1}}$.

The wave forcing was also calculated using the native model-level data from ERA-I. This calculation indicated that the Kelvin and IG wave forcing obtained from the p level datasets was underestimated by at least 2–4 and 1–3 $\mathrm{m\,s^{-1}\,month^{-1}}$, respectively. On the other hand, the unresolved forcing might be overestimated by a similar amount. Considering this, the net mesoscale gravity wave forcing of the QBO in the E–W phase would appear to be smaller than the Kelvin wave forcing, whereas in the W–E phase the gravity wave forcing is the dominant forcing term.

There exist uncertainties in the resolved-scale waves in the reanalyses even for the model-level data. As discussed in Sect. 3.1, the substantial difference between the wave forcing from the model-level data and from the interpolated p level data implies that a significant amount of waves with ver-

tical wavelengths of about 2.8–5.6 km are present in the model-level data. Given that these vertical wavelengths are at the lower bound of the ranges captured by the forecast models (~~2–4Δ_v~~ $2\Delta_v$–$4\Delta_v$), we can speculate that a substantial fraction of short-wavelength waves could remain under-represented in the reanalyses at the native model levels. The MRG and IG waves have vertical wavelengths that may be affected by this phenomenon. In a previous study by Ern et al. (2008), it was shown that the amplitudes of the MRG and IG waves in the ECMWF analysis are smaller than those from the SABER observations. A number of studies using general circulation models (Boville and Randel, 1992; Giorgetta et al., 2006; Choi and Chun, 2008; Richter et al., 2014) have also demonstrated the need for high vertical resolutions (500–700 km) to capture equatorial waves; these are twice the resolution of the reanalyses used in this study.

There is another important source of uncertainty. The unresolved gravity wave forcing has been deduced from the other forcing terms in the zonal wind tendency equation. In the W–E phase, the estimate of the unresolved forcing is highly dependent on the vertical advection term. However, as seen in Fig. 5a, the vertical velocity is poorly constrained in the reanalyses, and this introduces a large uncertainty in the vertical advection term. The spread in vertical advection between the reanalyses reaches $\sim 10\,\mathrm{m\,s^{-1}\,month^{-1}}$. The validation of the vertical velocity field in the equatorial lower stratosphere in the reanalyses might be crucial for deducing the unresolved-scale wave contribution to the QBO (Ern et al., 2014).

Acknowledgements. The authors would like to thank Seok-Woo Son for providing the motivation for this work. The ERA-I dataset was obtained from the ECMWF data server (http://apps.ecmwf.int/datasets/). The MERRA dataset was provided by the Global Modeling and Assimilation Office at NASA Goddard Space Flight Center through the NASA GES DISC online archive. The CFSR dataset was from NOAA's National Operational Model Archive and Distribution System which is maintained at NOAA's National Climatic Data Center. The JRA-55

dataset was provided from the JRA-55 project carried out by the Japan Meteorological Agency. This study was funded by the Korea Meteorological Administration Research and Development Program under Grant CATER 2012-3054.

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Table 1. Horizontal resolution of the native models and pressure-level datasets for the four reanalyses used in this study, along with the number of vertical levels at 70–10 hPa.

	Model resolution (Number of levels at 70–10 hPa)	Data resolution used
ERA-I	TL255 $\sim 0.7°$ (10)	1.5° (5)
MERRA	$0.5° \times 0.667°$ (12)	1.25° (6)
CFSR	T382 $\sim 0.38°$ (13)	1.0° (5)
JRA-55	TL319 $\sim 0.56°$ (10)	1.25° (5)

Table 2. Phase-maximum magnitudes of the Kelvin, MRG, IG, and Rossby wave forcing, net resolved wave forcing, $\overline{X}$, and $\overline{X}^*$ [$\mathrm{m\,s^{-1}\,month^{-1}}$] at 30 hPa in the E–W and W–E phases for the period 1979–2010, obtained using the p level datasets and the ERA-I model-level dataset. Details of $\overline{X}$ and $\overline{X}^*$ can be found from the text along with Eqs. (1) and (4). Positive forcing is denoted by bold font.

	E–W		W–E	
	p level	model-level	p level	model-level
Kelvin	**2.8–8.7**	**6.7–13**		
MRG	0.6–2.1	0.6–1.8	0.2–1.8	0.6–2.6
IG	**0.9–3.9**	**2.5–4.3**	0.6–3.0	1.9–5.4
Rossby	0.7–2.7	0.6–2.9	0.7–3.5	0.9–3.8
Net_resolved	**3.4–11**	**8.0–19**	1.5–5.2	3.3–7.5
$\overline{X}$	**5.8–17**	**3.1–11**	6.6–21	11–18
$\overline{X}^*$	**5.8–14**		11–21	

Table 3. The same as in Table 2, except at 50 hPa.

	E–W		W–E	
	p level	model-level	p level	model-level
Kelvin	**2.7–6.8**	**4.6–9.2**		
MRG	0.6–1.6	0.6–1.7	0.6–2.3	0.8–2.2
IG	**0.5–2.3**	**1.3–2.5**	0.4–2.4	1.4–3.7
Rossby	1.1–5.0	1.3–3.6	0.7–4.0	1.2–3.1
Net_resolved	**2.8–8.8**	**5.4–11**	0.9–6.4	2.7–6.2
$\overline{X}$	**3.7–10**	**2.2–4.3**	0.5–17	6.9–13
$\overline{X}^*$	**3.5–8.7**		7.7–16	

Table 4. The same as in Table 2, except at 10 hPa.

	E–W		W–E	
	p level	model-level	p level	model-level
Kelvin	**2.2–12**	**3.6–15**		
MRG	0.4–5.3	0.2–3.6	0.4–2.3	0.5–1.8
IG	**0.5–4.9**	**2.7–6.2**	0.6–4.5	2.7–5.9
Rossby	0.7–8.0	2.2–8.4	4.3–12	6.1–14
Net_resolved	**2.8–17**	**4.1–21**	6.2–15	8.0–17
$\overline{X}$	**5.5–31**	**4.7–16**	3.1–35	5.9–25
$\overline{X}^*$	**4.1–17**		6.3–30	

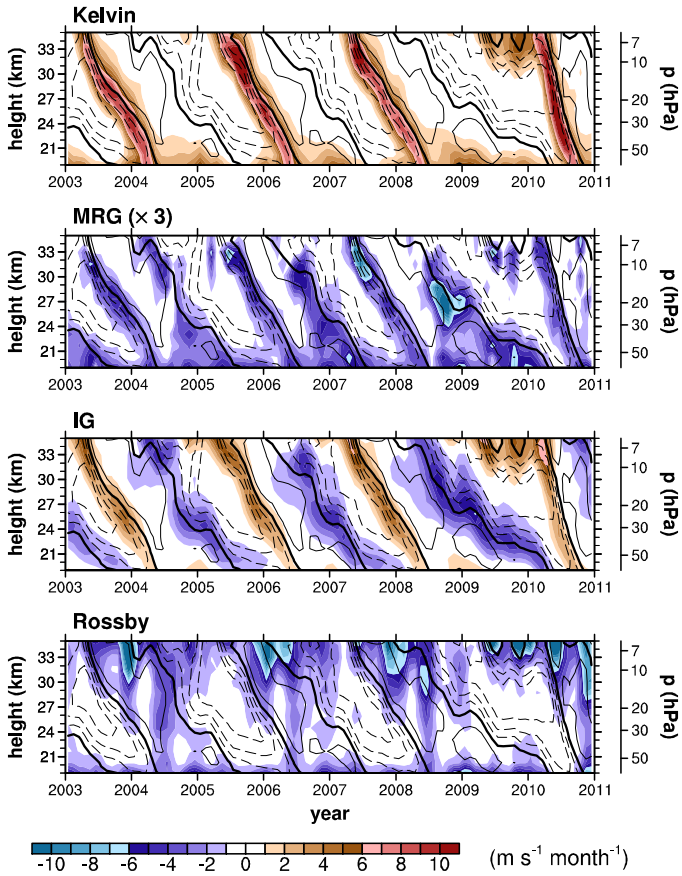

Figure 1. Time–height cross-sections of the zonal momentum forcing by the Kelvin, MRG, IG, and Rossby waves (from top to bottom) averaged over 5° N–5° S, obtained using the model-level data of ERA-I over the period 2003–2010 (shading). The MRG ~~and IG~~ wave forcing is multiplied by ~~4 and 2, respectively.~~ 3. The zonal mean wind over 5° N–5° S is superimposed at intervals of $10\,\mathrm{m\,s^{-1}}$ (contour). The thin solid, dashed, and thick solid lines indicate westerly, easterly, and zero wind, respectively.

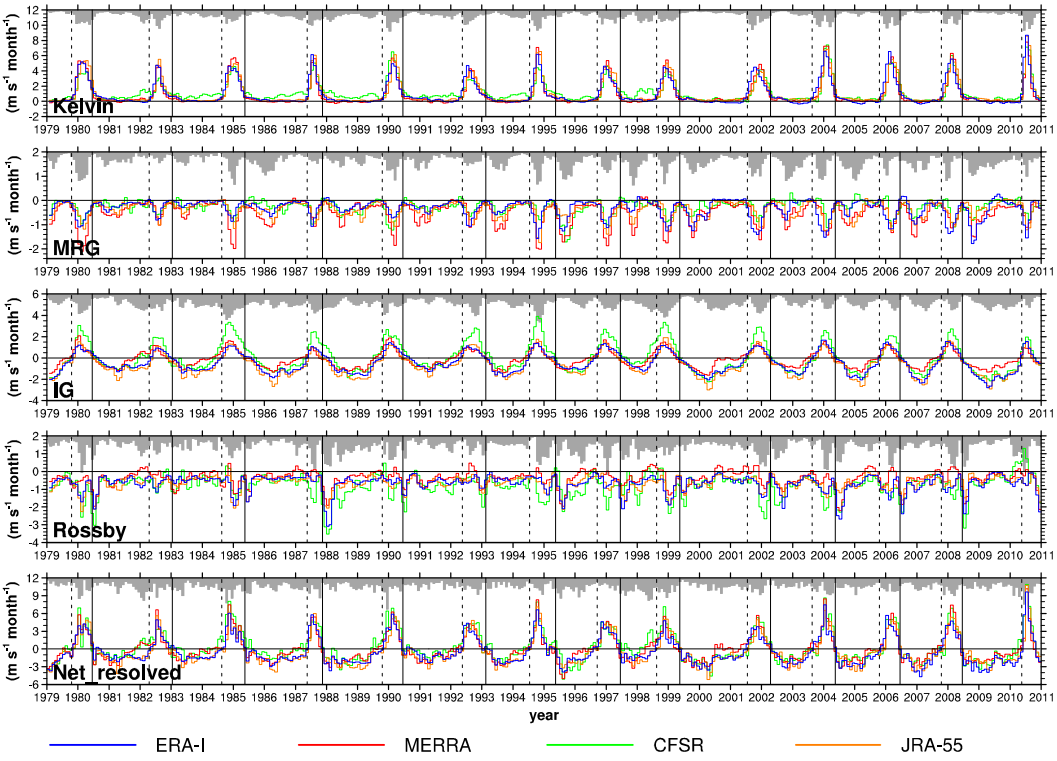

Figure 2. Zonal momentum forcing by the Kelvin, MRG, IG, and Rossby waves averaged over 5° N–5° S at 30 hPa for the period 1979–2010, as well as the net forcing by all resolved waves (from top to bottom) obtained using the p level data of ERA-I (blue), MERRA (red), CFSR (green), and JRA-55 (orange). The phase of the maximum easterly and westerly in each QBO cycle at 30 hPa is indicated by the dashed and solid vertical lines, respectively. The difference between upper and lower bounds of the wave forcing calculated from each dataset is also indicated (gray shading).

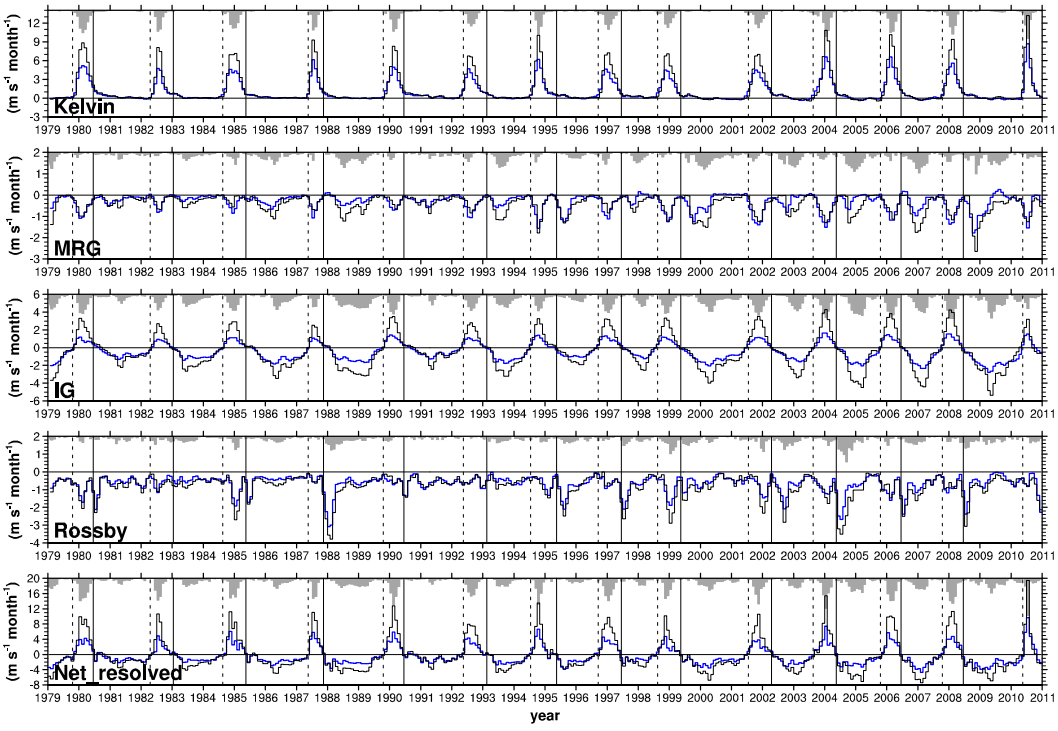

Figure 3. The same as in Fig. 2, except using the model-level data (black) along with the *p* level data (blue) for ERA-I.

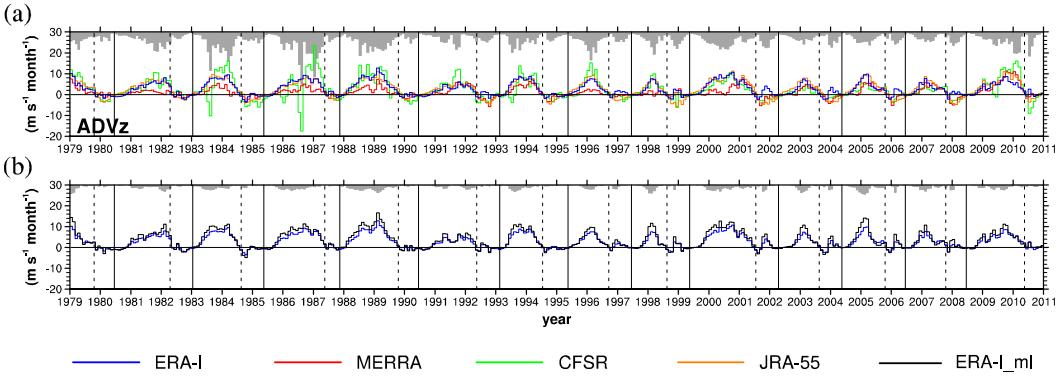

Figure 4. The same as in **(a)** Fig. 2 and **(b)** Fig. 3, except for the vertical advection of zonal wind.

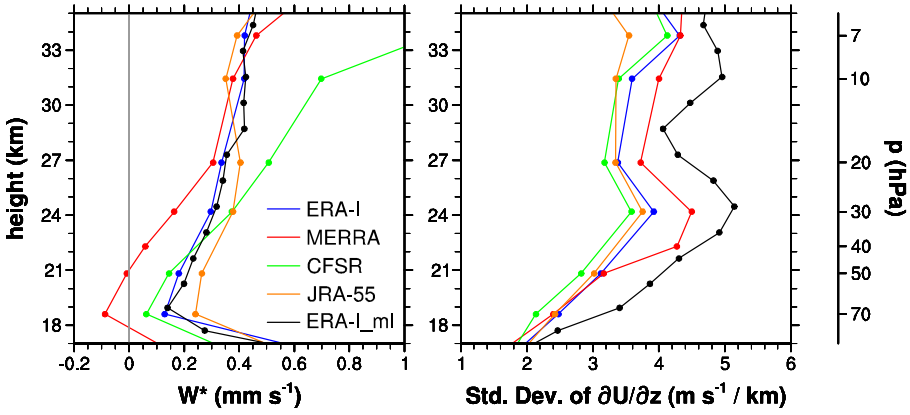

Figure 5. **(a)** Mean residual vertical velocity and **(b)** ~~SD~~ standard deviation of the monthly and zonal mean wind shear for the period 1979–2010 averaged over 5° N–5° S, obtained using the p level data of ERA-I (blue), MERRA (red), CFSR (green), and JRA-55 (orange) as well as the model-level data of ERA-I (black).

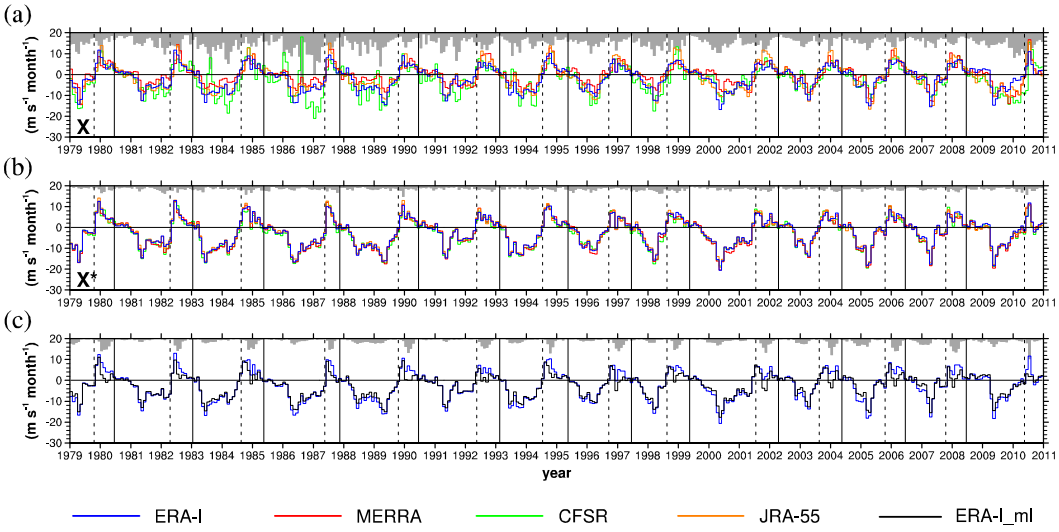

Figure 6. The same as in Fig. 2, except for the terms **(a)** $\overline{X}$, **(b)** $\overline{X}^*$, and **(c)** as in Fig. 3 for $\overline{X}^*$ (see the text for a definition of these terms).