Atmos. Chem. Phys. Discuss., 15, 35881–35906, 2015 www.atmos-chem-phys-discuss.net/15/35881/2015/ doi:10.5194/acpd-15-35881-2015 © Author(s) 2015. CC Attribution 3.0 License.



This discussion paper is/has been under review for the journal Atmospheric Chemistry and Physics (ACP). Please refer to the corresponding final paper in ACP if available.

# Response of OH airglow emissions to the mesospheric gravity waves and its comparisons with full wave model simulation at a low latitude Indian station

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Received: 12 October 2015 – Accepted: 8 December 2015 – Published: 21 December 2015

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Published by Copernicus Publications on behalf of the European Geosciences Union.



### Abstract

The quasi-monochromatic gravity wave induced oscillations, monitored using the mesospheric OH airglow emission over Kolhapur (16.8° N and 74.2° E), India during January to April 2010 and January to December 2011, have been characterized using
the Krassovsky method. The nocturnal variability reveals prominent wave signatures with periods ranging from 5.2–10.8 h as the dominant nocturnal wave with embedded short period waves having wave periods 1.5–4.4 h. The results show that the magnitude of the Krassovsky parameter, viz., |η| ranged from 2.1 to 10.2 for principal or long nocturnal waves (5.2 to10.8 h observed periods), and, from 1.5 to 5.4 for the short waves (1.5 to 4.4 h observed periods) during the years of 2010 and 2011, respectively. The phase, i.e., Φ values of the Krassovsky parameters exhibited larger variability and varied from -8.1 to -167°. The deduced mean vertical wavelengths are found to be approximately -60.2 ± 20 and -42.8 ± 35 km for long and short wave periods for the year 2010. Similarly, for 2011 the mean vertical wavelengths are found to be approximately -60.2 ± 20 and -42.8 ± 35 km for long and short wave periods for the year 2010. Similarly, for 2011 the mean vertical wavelengths are found to be approximately -60.2 ± 20 and -42.8 ± 35 km

<sup>15</sup> mately  $-77.6 \pm 30$  km and  $-59.2 \pm 30$  km for long and short wave periods, respectively, indicating that the observations over Kolhapur were dominated by upward propagating waves. We use a full wave model to simulate the response of OH emission to the wave motion and compare the results with observed values. In the present report, we discuss the observed wave characteristics and cause of the noted differences.

#### 20 **1** Introduction

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Often the observed temporal variations in the mesospheric hydroxyl OH night airglow intensities and rotational temperatures are caused by the propagating gravity waves from the lower to the upper atmosphere. The interaction of these upward propagating waves with the ambient and other waves contribute to the dynamical variability, which in turn is reflected in observed airglow intensity and temperature perturbations (Hines, 1997). Krassovsky (1972) introduced a quantity "n" to characterize the wave-induced



perturbations. This parameter, termed as "Krassovsky's parameter", can be defined as  $\eta = |\eta|e^{-i\Phi}$ , where  $|\eta|$  indicates the ratio of the amplitude variation between the emission intensity and temperature perturbations normalized to their time averages and  $\Phi$  is a phase difference between the intensity wave and its temperature counterpart (e.g.,

- <sup>5</sup> Walterscheid et al., 1987; Taylor et al., 1991). It should also be mentioned here that apart from the pure dynamical processes  $\eta$  can also be affected by various other unknown parameters, such as the variation of local oxygen photochemistry (Hickey et al., 1993) and height variation of the emission layer which affects emission rates and temperature directly (Liu and Swenson, 2003; Vargas et al., 2007). Although this can com-
- plicate studies of Krassovsky's parameter, it offers an opportunity to study the above aspects at the same time. Overall, once the physics and chemistry of emissions are well understood, the  $\eta$  values would offer a good tool to study the perturbations caused in a parameter (temperature, brightness/intensity) by measuring one under adiabatic conditions.
- <sup>15</sup> Utilizing the above, many investigators have carried out observational as well as the theoretical studies on the identification and characterization of gravity wave and tidal signatures with wave periodicities ranging from few minutes to several hours (e.g., Walterscheid et al., 1987; Hecht et al., 1987; Hickey, 1988a, b; Taylor et al., 1991; Takahashi et al., 1992; Reisin and Scheer, 1996; Taori and Taylor, 2006; Guharay et al.,
- <sup>20</sup> 2008; Ghodpage et al., 2012, 2013). However, observational studies of the magnitude and phase of  $\eta$  over a range of wave periods for a given location and season are sparse. Some of the notable observations of  $\eta$  for the OH emission have been performed by Viereck and Deehr (1989) in the wave period range of ~ 1–20 h and by Reisin and Scheer (1996) near to the semidiurnal tidal fluctuations.
- <sup>25</sup> In the present work, we utilize the mesospheric OH emission intensity and temperature data obtained during January–April 2010 and January–December 2011, when clear and moonless nights allowed observations to exceed 5 h duration. We deduce the Krassovsky parameters as a function of observed wave period and also infer the vertical wavelengths for the observed mesospheric waves. Further, we compare our



estimates with the earlier results reported by various investigators. We also employ a full-wave model to simulate the effects of wave motions on the OH airglow. This model has been used previously to compare observations and theory of airglow fluctuations (e.g., Hickey et al., 1998; Hickey and Yu, 2005). Here, the model is used to estimate the values of the amplitudes and phases of Krassovsky's ratio which are compared to those derived from the observations, making the present study unique and the first of its kind over Indian latitudes.

#### 2 Instrumentation and observations

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The mesospheric OH observations used in the present study are made using the multispectral photometer from Kolhapur (16.8° N, 74.2° E) (Ghodpage et al., 2013, 2014). We use the period of January–April 2010 and January–December 2011 when the availability of clear sky conditions prevailed for several nights. In particular, for 2010 data, out of 45 nights of OH airglow measurements, 14 nights clearly showed wavelike features, while in the 2011 year data, 60 nights out of 30 nights exhibited wavelike variations.

#### **2.1** The multispectral photometer

The multi-spectral photometer monitors airglow emissions at 731 and 740 nm rotational lines of OH (8,3), O(<sup>1</sup>S) 557.7 nm and O(<sup>1</sup>D) 630.0 nm emissions near simultaneously. The low temperature coefficient interference filters (10 cm aperture) used in the photometer have full width at half maximum ~ 1 nm (transmission ~ 40–70% at 24°C).
<sup>20</sup> We kept the integration time for each filter 10 s which results in repetition time of 90 s. The photometer has F/2 optics with full field of view ~ 10°. The stepper motor rotation and sensing of the initial position is performed by computer controlled software. As the detector, the EMI9658B photomultiplier tube is used. An amplifier (high gain transimpedance) is used to to convert and amplify photomultiplier's very weak (in the range)



of nA) output current in to corresponding voltage form. This output is recorded in digital format in term of arbitrary units along with time which is used for further processing.

#### 2.2 Full-wave model

The full-wave model is a linear, steady-state model that solves the linearized Navier– Stokes equations on a high resolution vertical grid to describe the vertical propagation of acoustic-gravity waves in a windy background atmosphere including molecular viscosity and thermal conduction, ion drag, Coriolis force and the eddy diffusion of heat and momentum in the mesosphere. The model description, including equations, boundary conditions and method of solution has been described elsewhere (Hickey et al., 1997; Walterscheid and Hickey, 2001; Schubert et al., 2003). The neutral perturbations are used as input to a linear, steady-state model describing OH airglow fluctuations (Hickey and Yu, 2005).

The model solves the equations on a high resolution vertical grid subject to boundary conditions, and allows quite generally for the propagation in a height varying atmo-

- sphere (non-isothermal mean state temperature and height varying mean winds and diffusion). The linearized equations are numerically integrated from the lower to the upper boundary using the tri-diagonal algorithm described by Bruce et al. (1958) and Lindzen and Kuo (1969). The lower boundary is set well below the region of interest and a sponge layer is implemented to avoid effects of wave reflection in the airglow
- <sup>20</sup> response. In this study the lower boundary (the bottom of the lower sponge layer) is placed at 250 km below z = 0 (i.e., -250 km). The wave forcing is through the addition of heat in the energy equation. The heating is defined by a Gaussian profile with a full-width-at-half-max of 0.125 km. It is centered at an altitude of 10 km. A Rayleigh– Newtonian sponge layer in addition to natural absorption by viscosity and heat con-
- <sup>25</sup> duction prevents spurious reflection from the upper boundary. At the upper boundary (here 300 km altitude) a radiation condition is imposed using a dispersion equation that includes viscous and thermal dissipation (Hickey and Cole, 1987). The mean state is defined using the Mass Spectrometer Incoherent Scatter (MSIS) model (Hedin, 1991).



A set of linear perturbation equations for the minor species involved in the OH emission chemistry is solved using the approach described in Hickey (1988). This assumes that these minor species have the same velocity and temperature perturbations as the major gas (which are deduced from the full-wave model). A vertical integration of the volume emission rates through the vertical extent of the OH layer provides the brightness and brightness-weighted temperature perturbations, from which Krassovsky's ratio is determined. The OH chemistry we use is the same as that used previously (Hickey et al., 1997) and is for the OH (8–3) emission. We also determine the vertical wavelength at the peak of the OH emission layer evaluated from the phase variations of the

<sup>10</sup> temperature perturbations determined by the full-wave model.

#### 2.3 Space borne measurements

The sounding of the atmosphere using broadband emission radiometry (SABER), onboard the thermosphere ionosphere mesosphere energetic and dynamics (TIMED) satellite, is a high-precision broadband radiometer which measures limb radiance (at

- <sup>15</sup> 74°) of the terrestrial at in 10 selected spectral bands ranging from 1.27 to 15  $\mu$ m. In the present study, we note larger values of  $|\eta|$  occur during 2011 compared to 2010 for long/principal waves, which indicates a larger intensity to temperature perturbation ratio over Kolhapur during the passage of the waves during 2011. This could be due to the differences in either the background atmosphere or the dynamical processes
- of 2010 and 2011 years. To identify this, we scrutinize the OH volume emission rate profile for Kolhapur region (obtained from the SABER instrument on-board the thermosphere ionosphere mesosphere energetic and dynamics (TIMED) satellite). The selected latitude–longitude grids are 10 to 20° N and 70 to 90° E representing Kolhapur. The criteria for the selection of SABER data are such that: (i) the SABER pass should are such that in the selection of SABER data are such that in the selection of the selection of
- <sup>25</sup> be during typical observation times (i.e. nighttime), (ii) it should not be at twilight.



#### Results and discussion 3

To identify the wave structures in the data, we utilize the perturbation amplitudes normalized to their time averaged values (hereafter referred to as mean values) in the intensity and temperature data to calculate the Krassovsky ratio. To illustrate this, we

show a typical example corresponding to the data obtained on 26-27 January 2011 in Fig. 1. We plot the temperature deviations (circles with connecting lines) from their mean values in Fig. 1a, while, the intensity deviations (circles with connecting lines) from their mean values are plotted in Fig. 1b. We note that night airglow intensity variations show a long-period wave with embedded short-period oscillatory features. On this night, the mean of airglow intensity is found to be  $\sim 1.83$  arbitrary units and the mean of the temperature data is ~ 195.75 K. To identify the nocturnal variability plotted together with data are the results (shown as red solid lines) of best-fit cosine model (e.g., Taori et al., 2005) as follows.

$$Y = A\cos\left[\pi \frac{(X - Xc)}{T}\right]$$

- where, A is the amplitude of the fitted wave of half-period T with phase Xc, and X is the time. Note that the solid red lines in Fig. 1 show the results of the best-fit cosine model. We observed the presence of  $\sim 8.2 \pm 1.1$  and  $8 \pm 1.3$  h waves with relative amplitudes  $\sim$  7.57 and 54.5%, in the nocturnal temperature and intensity variability, respectively. Given the uncertainties involved in the observations, we consider these to be the same
- waves. Further, we compute the  $|\eta|$  value for this wave to be 7.2 ± 1.3. To identify the 20 shorter period features in the data we obtain residuals from the best-fit model values (Fig. 1c). The bottom-left (Fig. 1c) and bottom-right (Fig. 1d) panels show the nocturnal variability of the residual temperature and intensity, respectively. The best-fit model reveals the presence of  $\sim 4.0 \pm 0.2$  and  $3.0 \pm 0.8$  h wave in the temperature and intensity
- residuals, respectively. Once again we treat these as the same wave for the reason ex-25 plained above. The best-fit analysis shows the percentage amplitudes of this wave to be ~ 4.1 K and 15.1 arbitrary units in the temperature and intensity data, respectively.

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(1)

Hence, the  $|\eta|$  value for short period waves is estimated to be  $3.7\pm0.9$ . The phase difference between the intensity and temperature waves is obtained with the help of best-fit parameters which were also verified with a cross correlation analysis. The phase of the principal waves (maxima) (period ~ 8.2 h) was ~ 25.02 h in the temperature data and 24.6 h in the intensity data, which results in the phase difference of ~ 0.4 h, i.e.,  $\Phi$ 

values of  $-18.0 \pm 10^{\circ}$ . Similarly, for the shorter period (period ~ 4 h) the  $\Phi$  values are estimated to be  $-100.8 \pm 22^{\circ}$ .

We can also estimate the vertical wavelength with the help of Krassovsky's parameter following the approach of Tarasick and Hines (1990):

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$$\lambda z = \frac{2\pi\gamma H}{(\gamma - 1)|\eta|\sin(\varphi)}$$

where  $\gamma = C_p/C_v = 1.4$  is the ratio of specific heats, and H = 6 km is the scale height. This formula is valid for zenith observations and for plane waves. It is not valid for the evanescent waves. Using the above relation we find that vertical wavelength for the two cases discussed above are  $\sim -39 \pm 15$  and  $-35.5 \pm 10$  km for long period and short period waves, respectively. Note that the long period wave estimates may be

short period waves, respectively. Note that the long period wave estimates may be biased when the data length is comparable to that of the wave period and therefore in our study we have considered only those waves whose periods are substantially less than the length of the available data.

The above analysis was carried out on nighttime events recorded during 2010 and 2011 when the prominent wave features were visible. One may note that during the 2010 period, the principal nocturnal waves in the data show the wave periods vary from 5.2 to 10.8 h with corresponding temperature amplitudes ranging from 0.2 to 13.8 K. Similarly for 2011, wave periods vary between 5.2 and 8.4 h with corresponding temperature amplitudes lying between 0.7 and 15.7 K. However, the intensity amplitudes

of the principal waves vary from 1.5% to 56.5 and 5 to 90% for 2010 and 2011, respectively. We note that the estimated  $|\eta|$  values were found to range from 2.1–10.5 for the principal wave. In the case of the short period waves, the periods varied from 1.5 to



(2)

4.4 h (for 2010) and 2.8 to 4.4 h (for 2011) with corresponding temperature amplitudes ranging from 0.2 to 12.5 and 0.4 to 14.4 K. The corresponding intensity amplitudes varied from ~ 1.8 to 56 and 0.8 to 46.8 % for 2010 and 2011, respectively. The phase ( $\Phi$ ) values also exhibit large variability for long (short) period waves, varying between

- 5 -27 and -167° (-27 and -150°) for 2010 and -8.1 and -65.2° (-39.1 and -122.6°) for 2011. For 2010 the deduced vertical wavelengths are found to vary from -32.2 to -140 and -24 to -88 km for the long and short period waves, respectively. Similarly, for 2011 the deduced vertical wavelengths are found to vary from -40 to -102, and -26 to -92.4 km for the long and short period waves, respectively.
- <sup>10</sup> In Fig. 2a we plot our results for  $|\eta|$  (hereafter  $\eta$ ) with pink half-filled squares indicating the estimates for the year 2010 and olive half-filled squares for the year 2011. We plot  $\Phi$  in Fig. 2b using the same symbols as used in Fig. 2a. For a comparison, we also show the values of  $\eta$  and  $\Phi$  reported by other investigators (Viereck and Deehr, 1989; Takahashi et al., 1992; Oznovich et al., 1995, 1997; Drob, 1996; Reisin and <sup>15</sup> Scheer, 1996; Taylor et al., 2001; Lopez-Gonzalez et al., 2005). Also shown in the figure
- <sup>15</sup> Scheer, 1996; Taylor et al., 2001; Lopez-Gonzalez et al., 2005). Also shown in the figure are the model estimates of Schubert et al. (1991), Tarasick and Shepherd (1992a, b), Walterscheid and Schubert (1995). In general, we observe that the parameter  $\eta$ increases with wave period. It is evident that the observed  $\eta$  and  $\Phi$  values in our study show a large spread in their distribution as compared to the model values. A similar
- <sup>20</sup> spread in the distribution of observed values of  $\eta$  (Fig. 2a) from 1.03 to 7.85 has also been observed by other investigators (e.g., Takahashi et al., 1992). It may be noted that the values of  $\eta$  for the OH data in our study lie somewhere between the model estimates and the values observed by other investigators. Also noteworthy in this figure is that our  $\eta$  values are closer to the model values reported by Tarasick and Shepherd
- (1992a) for the waves with horizontal wavelength 500 km. The phase "Φ" values, on the other hand show significantly larger deviations from this model for 2010, while for 2011 the match between measured and modeled phases appear to be better. We note that our measurements of Φ matches somewhat with those reported by Viereck and Deehr (1989), while large differences with other investigators can be easily noted. The



variation of  $\Phi$  values with respect to the wave periodicity, obtained in the 2010 year clearly shows that most of the time we observe values to be higher than those obtained by different models.

- In particular, Reisin and Scheer (1996) found mean (arithmetic) value of  $\eta$  to be 5.5 ± 0.6 and the mean  $\Phi$  value to be -66° for OH. Our observed values of  $\eta$  (arithmetic mean, 4.4 ± 1 for 2010 year and 5.7 ± 1.7 for 2011 year) near by agree with the values reported by Reisin and Scheer (1996) for OH measurements. In a further report, based on 5 year observations, Reisin and Scheer (2004), found the mean value of  $\eta$ to be ~ 5.6 for the nightly semidiurnal type waves and ~ 3.4 for the waves of 3000 s periodicity; which is in agreement with our values. In another study based on long-term
- observations with a spectral airglow temperature imager (SATI) from a mid-latitude station, Lopez-Gonzalez et al. (2005) reported a mean value of  $\eta$  of approximately ~ 8.6 for the OH measurements with a larger variability than our observations show. In another report, Guharay et al. (2008), found that for wave periods ranging from 6 to 13 h,
- values of η varied from 1.7 to 5.4, while the phase varied from -13 to -90°. Similarly, Aushev et al. (2008) presented amplitudes of the Krassovsky parameter for wave periods of 2.2 to 4.7 h which varied from 2.4 to 3.6 while the phase varied from -63 to -121°. It is noteworthy that our derived values broadly agree with Guharay et al. (2008, 2009), Reisin and Scheer (1996, 2004) and Viereck and Deehr (1989) while they are
  somewhat different from the values reported by Lopez-Gonzalez et al. (2005) (which
- may be due to the fact that their observations corresponded to higher latitude than ours).

In general, the results shown in Fig. 2 emphasize that there are significant in the Krassovsky parameters derived from one study to another. This we suspect to be

<sup>25</sup> caused by the variations in the altitudinal profile of oxygen and its effect on the  $\eta$  through the complex OH chemistry (Walterscheid et al., 1994). Another possibility over low latitudes was discussed by Makhlouf et al. (1995) who suggested the quenching caused by the perturbed molecules during their transitions from several vibrational lev-



els. Winds also affect the OH response to gravity waves and therefore they will also contribute to the spread of values seen between the various observation studies.

Note that our observations as well as models show the phase  $\Phi$  for OH to be a negative value indicating the upward propagating waves. In general we note that our  $\Phi$ 

- values, although on some occasions are closer to Viereck and Deehr (1989) observations, show large deviations from other investigators and are larger than the model values on most occasions. Differences in theory and observation may be due to the horizontal wavelength assumed in the model and or the Prandtl number (ratio of kinematic viscosity to thermal diffusivity) assumed. The Prandtl number is important in theoret-
- <sup>10</sup> ical calculations and modeling, especially when in terms of dissipating waves owing to molecular viscosity and thermal diffusivity while they propagate in the atmosphere (Hickey, 1988). An error in the Prandtl number assumption will affect the derived wave parameters ( $\lambda_z$ ,  $\eta$  etc.), which will successively mask the actual ones. In this regard, Makhlouf et al. (1995) studied the variations in the  $\eta$  values by modifying the model
- <sup>15</sup> proposed by Hines and using a photochemical dynamical model; however, they were still unable to explain the appearance of the negative phases appropriately. Hines and Tarasick (1987) found a wide range of  $\eta$  variability, a result supported by our measurements. Further, Hines and Tarasick (1997) subsequently discussed the necessary correction for thin and thick layer approximations for the calculation of  $\eta$  from airglow
- <sup>20</sup> emissions due to gravity waves interaction. They also pointed out that OH emission intensity, which affects the derived  $\eta$  values, does not depend on the oxygen profile and other minor species, which contradicts the theory of Walterscheid et al. (1994), Schubert et al. (1991) and Offermann et al. (1981).

The calculated vertical wavelengths (VW) for all the nights of the observation are shown in Fig. 2c as pink half filled squares indicating the estimates for the year 2010 and olive half filled squares for the year 2011. Large differences exist from one night to another. The VW has a large variability varying from -41 to -102 km (2010) and -36.2 to -140 km (2011) for long period waves, and, -26 to -92.4 and -24 to -88 km for short period waves period of 2010 and 2011 years respectively. In 2010 (and 2011)



years, the mean VW values for long and short period waves are calculated to be  $-60.2 \pm 20 \text{ km} (-77.2 \pm 40 \text{ km})$  and  $-42.8 \pm 15 \text{ km} (-59.2 \pm 30)$  respectively. All the observations show negative values for  $\Phi$  and  $\lambda_z$ , indicating upward propagating waves. Further, unlike the clear dependency on the wave period noted in the Krassovaky pa-

- <sup>5</sup> rameters ( $\eta$  and  $\Phi$ ) no clear trend is noted in the calculated VW. We also plot the values reported by Reisin and Scheer (1996) and Lopez-Gonzalez et al. (2005) for a comparison. It is noteworthy that for all the days the VW for the long period wave are higher than the VW of short period waves. We also observed that VW values calculated for 2011 year are larger than 2010 year calculated values.We note that the values reported by
- Reisin and Scheer (1996) are approximately –30 km with about 40 km variability, which is a good agreement with our values. However, Lopez-Gonzalez et al. (2005) observed VW values to be approximately –10 km deduced from their OH observations, which do not agree with our values. Further, Ghodpage et al. (2012) analyzed the long-term nocturnal data of 2004–2007 and also observed that the VW lies between 28.6 and
- 15 163 km. Recently, Ghodpage et al. (2013) studied the simultaneous mesospheric gravity wave measurements in the OH emission from Gadanki and Kolhapur, inferring mean VWs varying from –26 to –60 km for the Kolhapur observations. Takahashi et al. (2011) reported vertical wavelengths varying from 20 to 80 km, which is in agreement with our values.

#### <sup>20</sup> 4 Comparison with the full wave model results

Wave simulations were performed using the full-wave model (FWM). The observations were conducted over an approximate one month period spanning 8 February and 13 March, and accordingly we used the middle date of this observation period (25 February) in the MSIS model to represent the undisturbed mean state. The latitude used was 16.8° N, and the local time was midnight. Because the speed and direction of wave propagation were not determined from the observations, several simulations were performed for each wave period in which the direction of propagation (eastward,



northward and westward propagation) and the phase speed (50, 100 and  $150 \text{ m s}^{-1}$ ) were varied. Note that the mean winds (not shown) in these simulations were derived from the Horizontal Wind Model (HWM) using the same input parameters as used for the MSIS model. The derived meridional winds (not shown) are far smaller than the zonal winds for the conditions considered here, and so while results for eastward and westward propagation differed quite markedly, those for northward and southward prop-

agation did not. Hence we considered only a single direction (northward) for meridional propagation.

We also performed a tidal simulation using an equivalent gravity wave model
 (Lindzen, 1970; Richmond, 1975), as implemented in an earlier study (Walterscheid and Hickey, 2001). The horizontal wavelength and Coriolis parameter are adjusted to give maximal correspondence with a given tidal mode. Here, we performed calculations for the terdiurnal (3,3), (3,4), (3,5) and (3,6) modes using parameters provided by Richmond (1975). The simplifications inherent in this approach are discussed by
 Walterscheid and Hickey (2001).

Comparisons between the full wave model results for  $\eta$ ,  $\Phi$  and  $\lambda_z$  and the values inferred from the observations are shown in Fig. 3a–c, respectively. In Fig. 3a we compare the observed values of  $\eta$  for 2010 and 2011. show The observed values of  $\eta$  are represented as pink and olive lower half-filled squares for 2010 and 2011, respectively.

- <sup>20</sup> In Fig. 3a we note that at few of the longer wave periods, the observed values of  $\eta$  are in good agreement with the full wave model results. For short period waves the values of  $\eta$  inferred from the observations appear to be bounded by the model values for waves with horizontal phase velocities are 50–100 m s<sup>-1</sup>, respectively. For example, for 3.6 h wave periods, the average of the values of  $\eta$  inferred from the observations is 3.7,
- while the full wave model values lie between about 0.5 (for the  $100 \text{ m s}^{-1}$  wave) and 7 (for the 50 m s<sup>-1</sup>, eastward propagating wave). For the 8 h wave periods, the average of the values of  $\eta$  inferred from the observations is 5.7, which is bounded by the full wave model estimates for waves having a horizontal phase velocity of 50 m s<sup>-1</sup> and different propagation directions.



Overall, we note that that the comparison between the observed  $\eta$  values and the modeled values can be explained by gravity waves whose horizontal phase velocities range from 50 to  $100 \text{ ms}^{-1}$ . In this regard, an earlier investigation by Pragati Sikha et al. (2010) reported observed gravity wave horizontal phase speeds (for periods 5 to 17 min) varying between 10 and  $48 \text{ ms}^{-1}$ . The propagation directions were reported to be preferentially towards the north. More recently, Taori et al. (2013) studied mesospheric gravity wave activity in the OH and OI 558 nm emissions from Gadanki. They observed that the gravity waves were moving in the north-west direction. The average phase velocity of the ripple-type waves was found to be 23.5 m s<sup>-1</sup>. The other, band-type waves, with horizontal scales of about 40 km, were found to be propagating from

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south to north with an estimated phase speed of 90 m s<sup>-1</sup>. The vertical wavelengths ( $\lambda_z$ ) calculated using the observed values of  $\eta$  and  $\Phi$  differ significantly from the full wave model estimate for waves with phase velocities below

100 m s<sup>-1</sup>. More typically, a comparison between those values inferred from the observations and those derived from the model tend to agree for phase velocities in the 100–150 m s<sup>-1</sup> range. However, it should be noted that vertical wavelengths inferred from the observations are based on the use of the inferred Krassovsky's ratio,  $\eta$ , in Eq. (2). Errors in the determination of the phase ( $\Phi$ ) of  $\eta$  can lead to significant errors (proportional to cot $\Phi$ ) in the determination of  $\lambda_{z}$ , especially as  $\Phi$  approaches ±180°.

<sup>20</sup> The differences noted in the observed and modeled estimates of Krassovsky ratio magnitudes  $\eta$  and phase ( $\Phi$ ) may be associated with the limitation arising due to dynamics as well as the measurements. In terms of measurements limitation, the parameters achieved with the best fit method may have leaked contribution from other wave components which may be dynamically varying within a wave period. In terms of

dynamics, that full wave model uses climatological density (both major gas and minor airglow-related species) and wind profiles which will introduce uncertainties. This point has been previously elaborated by Walterscheid et al. (1994) with respect to the effect of a change in the [O] profile on the OH response to wave motions.

## Discussion Paper **ACPD** 15, 35881-35906, 2015 **Characterization of** gravity waves using **OH airglow Discussion** Paper investigation R. N. Ghodpage et al. **Title Page** Introduction Abstract Discussion Paper Conclusions References **Figures** Tables Back Close **Discussion** Paper Full Screen / Esc **Printer-friendly Version** Interactive Discussion

The differences noted in the magnitude of the observed Krassovsky ratio  $\eta$  between 2010 and 2011 may be associated with variations in the height and shape of the undisturbed OH emission profile. To check whether there was a difference in the OH emission layer structure, we selected the nighttime OH emission profile for a grid encompassing 10 to 20° N latitudes and 70 to 90° E latitudes during February, March and April months of the years 2010 and 2011. We have selected the February to March period

- because the optical airglow data used in this study was acquired primarily during these months. The monthly mean values of OH emission rates are plotted in Fig. 4. The solid curves correspond to 2010 data while the dashed curves correspond to 2011 data
  for. We note that the peaks of OH emission layer during February, March and April of Content and April of the solid curves correspond to 2010 and the solid curves correspond to 2011 data
- 2010 occurred at 84.2, 82.8 and 85.1 km altitude, respectively, while the corresponding peaks for 2011 were found to occur at 85.8, 85.6 and 85.2 km altitude. This suggests that the peak of the emission layer occurred at a somewhat lower altitude in 2010 compared to 2011. Also, the mission rates during February and March were found to be
- <sup>15</sup> higher in 2010. It is important to note that in an earlier study, Ghodpage et al. (2013) compared the Krassovsky ratios at two different latitudes, Gadanki (13.5° N, 79.2° E) and Kolhapur (16.8° N and 74.2° E) and noted a lower OH emission layer peak over Kolhapur and also larger estimated  $\eta$  values over Kolhapur. In the present case, instead of the location, it is the difference in the measurement year where the peak
- emission altitudes of the OH emission layer are somewhat different. As the peak emission layer arise due to the chemical reactions involving odd oxygen, it is proposed that chemical constutents composition were different from the year 2010 to the year 2011. Therefore, the noted emission rates may be responsible for the observed differences in the Krassovsky parameters. A further question arise here is why the peaks
- should be different from one year to the other. As these months are pre-monsoon, when a large scale oscillation namely, El Niño/Southern Oscillation (ENSO) sweeps through the south Asian continent, we looked at the ENSO strength based on the Multivariate ENSO Index (MEI). This index is shown in Table 1, where it is noteworthy that the MEI index for 2010 (January to May) is of opposite sign to that for the corresponding



months in 2011. We postulate that these large scale processes have a profound impact on the observed wave energetics and dynamics at mesospheric altitudes. Large scale processes induced the wave oscillations associated with the ENSO. The ENSO generates a spectrum of waves which are of planetary scales. These are expected to generate a secular variation in temperature and density structure throughout the atmosphere. A difference in ENSO suggests that these forcing are different in the two years (2010, 2011). At present, we do not know through which process the ENSO may have implications in the observed wave characteristics. However, we believe that further investigation is required in order to confirm whether or not any such associations really

10 do exist.

#### 5 Concluding remarks

We report the Krassovsky parameters for the observed gravity waves from Kolhapur  $(16.8^{\circ} \text{ N} \text{ and } 74.2^{\circ} \text{ E})$  and their comparison with the full wave model. Following are the concluding remarks of the present investigations.

- 1. It is evident that the observed values of Krassovsky parameters in our study show a large spread in their distribution as compared to the model values (shown in Fig. 2a). A similar spread in the distribution has also been reported by other investigators. We have also observed that more magnitude of  $\eta$  values in 2011 year than 2010 year.
- 20 2. It is also notable that the values of  $\eta$  for the OH data in our study lie between the model estimates and the values observed by other investigators. Whereas the phase values are more than the model values on most occasions. We note that our  $\Phi$  measurements match with those reported by Viereck and Deehr (1989), while they show large differences with other investigators values.
- Observed vertical wavelength (VW) values broadly agree with the range reported by other investigators and are found to vary from -26 to -140 km.We also noted 35896



that VW values calculated for 2011 year are larger than 2010 year calculated values. Most of wave propagating upward in direction.

4. Comparison of observed  $\eta$  and  $\Phi$  values agree fairly well with the full wave model results for waves with 50–100 ms<sup>-1</sup> horizontal phase velocities. Vertical wavelengths tend to agree for waves with 100–150 ms<sup>-1</sup> horizontal phase velocities, except for the longest period waves for which vertical wavelength cannot be reliably inferred from the observations.

The database used in the present study is limited in terms of the length and locations and based on the above conclusions, more rigorous study using coordinated observations and modeling are underway with an aim to uncover the physics occurring at upper mesosphere.

Acknowledgements. This work is carried out under the research grant funded by Ministry of Science and Technology and Department of Space, Govt. of India. R. N. Ghodpage thank the Director, Indian Institute of Geomagnetism (IIG), Navi Mumbai for encouragement to carry out this work. The night airglow observations at Kolhapur were carried out under the scientific collaboration program (MoU) between IIG, Navi Mumbai and Shivaji University, Kolhapur. M. P. Hickey acknowledges the support of NSF grant AGS-1001074.

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**Table 1.** Comparisons of deduced wave parameters in 2010, 2011 years with MEI index and OH altitudes. The observed quantities are mean for their representative wave periods (JFM - January, February and March months like this).

Year	r Mean η (± Errors)		Mean η Mear (± Errors) (D		n (-Ф) Mean (-VW) veg.) (km)		OH altitude (km)	MEI index				
	Long wave period	Short wave period	Long wave period	Short wave period	Long wave period	Short wave period	_	JFM	FMA	MAM	SON	OND
2010	4.4 ± 1	$2.3 \pm 0.9$	$90.6 \pm 40$	$70.4 \pm 45$	$60.2 \pm 20$	42.8 ± 15	82 to 85.1 km during Feb–Apr	1.1	0.8	0.5	-1.4	-1.3
2011	5.7±1.7	$2.7 \pm 0.6$	$33.8\pm40$	$64.4\pm40$	$77.6 \pm 40$	59.2 ± 30	85.1 to 86 km during Feb–Apr	-1.1	-0.8	-0.6	-0.9	-0.9









Figure 2. (a) A comparison of Krassovsky parameters of data to their respective wave periods. The x axis shows the wave periodicity and the y axis is for Krassovsky parameters ( $\eta$  and  $\Phi$ ) in each plot. A close resemblance between the observational values and discrepancy between the observational and theoretical estimates are notable. The legends in the figure are as following: ( $\eta$ : 1 (for 2010 year), 2 (for 2011 year), present study; 3, Schubert et al., 500 km; 4, Schubert et al., 1000 km; 5, Tarasick and Shepherd, 500 km; 6, Tarasick and Shepherd, 1000 km; 7, Takahashi et al., 1992; 8, Oznovich et al., 1995; 9, Drob et al., 1996; 10, Reisin and Scheer, 1996; 11, Taylor et al., 2001; 12, Guhary et al., 2008; 13, Walterscheid and Schubert, 1995; 14, Lopez-Gonzalez et al., 2005; 15, Oznovich et al., 1997; 16, Viereck and Deehr, 1989). (b) A comparison of phi values to their respective wave periods ( $\Phi$ : 1, 2, present study; 3, Schubert et al., 500 km; 4, Schubert et al., 1000 km; 5, Tarasick and Shepherd 500 km; 6, Tarasick and Shepherd 1000 km; 7, Viereck and Deehr, 1989; 8, Oznovich et al., 1995; 9, Drob et al., 1996; 10, Reisin and Scheer, 1996; 11, Taylor et al., 2001; 12, Walterscheid and Schubert, 1995; 13, Guhary et al., 2008; 14, Lopez-Gonzalez et al., 2005; 15, Oznovich et al., 1997). (c) Deduced vertical wavelength (VW) for both the short and long period wave as function of wave periodicity. Also shown comparison with values obtained by other investigators.





**Figure 3. (a)** Shown comparison with  $\eta$  calculated by observation of both year and Full wave model simulation with their respective wave period. Pink and olive lower half filled square shows the 2010 and 2011 year  $\eta$  observations. **(b)** Phase values for both the short and long period wave as function of wave periodicity comparison with values obtained full wave model simulation. **(c)** Deduced vertical wavelength (VW) for both the short and long period wave as function of wave periodicity comparison with values obtained full wave model simulation of wave periodicity comparison with values obtained full wave model simulation of wave as function of wave periodicity comparison with values obtained full wave model simulation (VW: 1, FWM simulation of VW for 50 m s<sup>-1</sup> horizontal phase velocity; 2, FWM simulation of VW for 100 m s<sup>-1</sup> horizontal phase velocity; 3, FWM simulation of VW for 150 m s<sup>-1</sup> horizontal phase velocity; 4 and 5 present study (for 2010 and 2011 year)).







