

This discussion paper is/has been under review for the journal Atmospheric Chemistry and Physics (ACP). Please refer to the corresponding final paper in ACP if available.

# Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki<sup>1</sup>, P. Yang<sup>1</sup>, B. A. Baum<sup>2</sup>, S. Platnick<sup>3</sup>, K. G. Meyer<sup>4</sup>, M. D. King<sup>5</sup>, and J. Riedi<sup>6</sup>

Received: 13 October 2015 - Accepted: 19 November 2015 - Published: 7 December 2015

Correspondence to: S. Hioki (s.hioki@tamu.edu)

Published by Copernicus Publications on behalf of the European Geosciences Union.

Discussion Paper

Discussion Paper

Discussion Paper

Back

Printer-friendly Version

Interactive Discussion



**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

**Abstract** Introduction

Conclusions References

> **Figures Tables**



Close





<sup>&</sup>lt;sup>1</sup>Department of Atmospheric Sciences, Texas A&M University, College Station, TX, USA

<sup>&</sup>lt;sup>2</sup>Space Science and Engineering Center, University of Wisconsin-Madison, Madison, WI, USA

<sup>&</sup>lt;sup>3</sup>Earth Science Division, NASA Goddard Space Flight Center, Greenbelt, MD, USA

<sup>&</sup>lt;sup>4</sup>Goddard Earth Sciences Technology and Research, Universities Space Research Association, Columbia, MD, USA

<sup>&</sup>lt;sup>5</sup>Laboratory for Atmospheric & Space Physics, University of Colorado, Boulder, CO, USA

<sup>&</sup>lt;sup>6</sup>Laboratoire d'Optique Atmosphérique, Université de Lille – Sciences et Technologies, Villeneuve d'Ascq, France

The degree of surface roughness of ice particles within thick, cold ice clouds is inferred from multi-directional, multi-spectral satellite polarimetric observations over oceans, assuming a column-aggregate particle habit. An improved roughness inference scheme is employed in the analysis that provides a more noise-resilient roughness estimate than the conventional best-fit approach. The improvements include the introduction of a quantitative roughness parameter based on empirical orthogonal function analysis and proper treatment of polarization due to atmospheric scattering above clouds. A global one-month data sample supports the use of a severely roughened ice habit to simulate the polarized reflectivity associated with ice clouds over ocean. The density distribution of the roughness parameter inferred from the global one-month data sample and further analyses of a few case studies demonstrate the significant variability of ice cloud single-scattering properties. The present theoretical results are in close agreement with observations in the extratropics but not in the tropics. Potential improvements are discussed to enhance the depiction of the natural variability on a global scale.

#### Introduction

Satellite observations at visible and infrared wavelengths can characterize global cloud microphysical parameters and radiative properties. Numerous techniques have been developed to retrieve ice cloud optical and microphysical properties from radiometric measurements (e.g., Inoue, 1987; Nakajima and King, 1990; Minnis et al., 1993) and have been adopted in operational retrieval efforts (Rolland et al., 2000; Platnick et al., 2003; Minnis et al., 2011). A synergetic combination of satellite and in-situ observations bulk ice cloud optical properties for remote sensing implementations as well as general circulation models (GCMs).

Paper

Discussion Paper

**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Introduction

References

**Figures** 

M

Close

**Abstract** 

Conclusions

**Tables** 

Discussion Paper

Discussion Paper

Back Full Screen / Esc

Printer-friendly Version

Interactive Discussion



(e.g., Heymsfield et al., 2002, 2013) serves as a constraint for the parameterization of

The accuracy of these retrieval techniques and the validity of downstream applications including GCM radiation parameterization hinges on steady improvements in the single-scattering calculations involving ice crystals. As ice clouds consist of nonspherical particles with characteristic sizes much larger than the wavelengths of interest, the single-scattering properties depend on the size, shape, and microscopic morphology of the particles (Macke, 1996; Yang et al., 2008a; Xie et al., 2009; Baum et al., 2010; Um and McFarguhar, 2007, 2009). In the solar shortwave spectrum, particle shape, surface texture, and crystal imperfections have a substantial influence on the single-scattering properties. Recent improvements in scattering calculation techniques are being incorporated into models that represent diverse ice particle populations in clouds.

However, it is challenging to quantify some of these influential microphysical parameters, given current satellite sensors. As a result, little information of their variability is available. The discrepancies among climate models (Waliser et al., 2009) in terms of ice water path (IWP) indicate that the GCM parameterizations need more reliable constraints on IWP, and the ability of passive and lidar sensors to correctly infer IWP requires knowledge of ice cloud radiative properties. The application of an unrealistic ice model, e.g., one that incorporates only smooth (unroughened) surface, results in an overall global bias (Yang et al., 2007, 2008b; Holz et al., 2015) as well as a seasonal bias (Zhang et al., 2009) in cloud property retrievals. The overaching goal of this paper is to gain a better understanding of the constraints in the microphysical parameters of global ice clouds using angular polarimetric observations and state-of-the-art light-scattering computational capabilities.

Multidirectional polarimetric observations can constrain the representative particle shape and surface texture condition (specifically, the degree of surface roughness), owing to the sensitivity of the polarization state of reflected light to small-scale particle structures. These measurements have been used to infer both particle habit (Chepfer, 1998; Labonnote et al., 2001; Masuda et al., 2002; Knap et al., 2005; Baran and Labonnote, 2007) and surface roughness (Baran and Labonnote, 2006; Cole et al., 2013, 2014). Since polarized reflectivity saturates at relatively small optical thickness **ACPD** 

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** 

Back

Full Screen / Esc

 $\triangleright$ 

Close

Printer-friendly Version

Interactive Discussion



Paper

Paper

Discussion Paper

Printer-friendly Version

Interactive Discussion

(generally about  $\tau = 5$ , Masuda and Takashima, 1992), the conventional "best-fit" approach to this problem computes the residual sum of squares (RSS) from the multiangle observations of polarized reflectivity and reflectivity simulations, and selects the ice particle model that minimizes the RSS when  $\tau > 5$ .

The previous studies imply that the use of roughened particles is necessary to achieve the maximum consistency between observations and numerical scattering calculations. Furthermore, Liu et al. (2015) and Holz et al. (2015) report that ice cloud optical thicknesses from visible/near-infrared retrievals and thermal infrared (IR) retrievals are more consistent when a particle is roughened.

The treatment of particle surface roughness here is not a rigorous approach. Rather, it is an approximation of the effects of roughened surface texture (Neshyba et al., 2013) and other kinds of imperfections present in natural ice cloud particles. The scattering property calculated by this approximate method is in reasonable agreement with that calculated by rigorous ray-tracing methods (Yang et al., 2008a). Although previous studies suggest that some degree of roughness is desirable, the issue remains as to the amount of roughness that should be adopted for global satellite-based retrievals, or used in numerical models.

Recent work by van Diedenhoven et al. (2012, 2014) simultaneously infers both the aspect ratio and the degree of roughness from a combination of polarimetric and intensity observations over a virtually continuous parameter space, assuming that simple hexagonal ice particles can explain observations. The ability to infer a representative ice cloud particle aspect ratio adds yet another dimension to the problem. Such exploration into the variability of ice particle microphysical properties can lead to a more reliable satellite climatology of ice clouds. This study focuses on the quantitative inference of ice particle roughness parameter for a specific particle habit, and will not include a detailed investigation of aspect ratio.

While a conventional "best-fit" approach can constrain the range of the roughness parameter in global data, it is not suitable for analyzing local variability. This is because the signal-to-noise ratio for particle roughness is low, and in the conventional "best-fit"

#### **ACPD**

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page **Abstract** Introduction Conclusions References

> **Figures Tables**

▶1

Back Close

Full Screen / Esc

Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper

Printer-friendly Version

Interactive Discussion

approach, even random observational errors can modify the inferred histogram significantly. Figure 1 illustrates how such a modification takes place if the method is applied to a synthetic signal with random noise. To produce Fig. 1, viewing geometries are extracted from one month of cloud observations by the POLarization and Directionality 5 of the Earth's Reflectance (POLDER) sensor (Deschamps et al., 1994) onboard the Polarization and Anisotropy of Reflectances for Atmospheric Sciences coupled with Observation from Lidar (PARASOL) satellite (Fougnie et al., 2007). The "best-fit" inference is applied to synthetic multi-angle cloud polarized reflectivities ( $L_n$ , defined in Sect. 2.1) with and without random noise. In synthesizing the signal, a column aggregate particle shape (e.g. Yang et al., 2013) is assumed with a roughness parameter of  $\sigma^2 = 0.15$  (variance of the slope of random facet tilts, see Yang et al., 2008b for details), and the random error has a normal distribution with variance equivalent to the POLDER observational error, which is estimated in Sect. 2.1. The hatched bar is the histogram with noise and the gray bar is that without noise. Note that the distinct peak at  $\sigma^2 = 0.15$  is no longer apparent when instrumental noise is included, indicating the necessity of appropriate treatment of the error distribution in the analysis.

This paper demonstrates how a continuous parameter space for the roughness retrieval is constructed and how it can be used to infer the particle roughness of optically thick ice clouds. Section 2 provides the details of the data and inversion method we employed, and the result of the application to one month of global data is described in Sect. 3. Concluding remarks are given in Sect. 4.

# Methodologies

To establish a method resilient to observational error, we first scrutinize random errors in POLDER data and select pixels based on the MODIS Collection 6 cloud product, as given in Sect. 2.1. Then, a continuous parameter space for inferring roughness is constructed by using an empirical orthogonal function analysis, and used in the retrieval

#### **ACPD**

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page **Abstract** Introduction

Conclusions References

> **Figures Tables**

Back Close

Full Screen / Esc

#### 2.1 Observations

#### 2.1.1 Reflectivity from POLDER

The POLDER sensor onboard the PARASOL satellite provides multispectral polarimetric observations at up to 16 viewing geometries for a single overpass (Fougnie et al., 2007). The PARASOL satellite was in the A-train satellite constellation from 2004 to 2009 and continued operation in a separate orbit until late 2013, providing a total of nine years of global polarimetric observation data. The design of the instrument is inherited from previous POLDER sensors on the ADEOS (ADvanced Earth Observing Satellite) platforms. POLDER sensors provide the first three elements of the Stokes vector from three images taken successively with linear polarization filters (Deschamps et al., 1994).

This study uses the single-pixel data set in PARASOL Level 1B product (i.e. the approximate resolution is 6 km × 6 km).

PARASOL products report the intensity of reflection in terms of normalized radiance  $L_n$ , which is equal to the reflectivity R of the surface–atmosphere system multiplied by the factor  $\mu_0 = \cos\theta_0$  (cosine of solar zenith angle).

$$L_{n}(\mu, \mu_{0}, \varphi, \varphi_{0}) = \mu_{0} R(\mu, \mu_{0}, \varphi, \varphi_{0})$$
(1)

The reflectivity R is defined as

$$R(\mu, \mu_0, \varphi, \varphi_0) = \frac{\pi I(\mu, \mu_0, \varphi, \varphi_0)}{E_0 \mu_0}$$
 (2)

where  $I(\mu, \mu_0, \varphi, \varphi_0)$  is the radiance and  $E_0\mu_0$  is the irradiance of incoming unpolarized light (i.e., solar irradiance;  $E_0$  is the beam flux).

)iscussion

on Paper

scussion Paper

Discussion Paper

Discussion Pape

#### **ACPD**

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

|**4** | **>**|

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



$$L_{np}(\mu, \mu_0, \varphi, \varphi_0) = \mu_0 R_p(\mu, \mu_0, \varphi, \varphi_0) = \frac{\pi \sqrt{Q_i^2 + U_i^2}}{E_0 \mu_0},$$
 (3)

where  $Q_i$  and  $U_i$  are defined to form the first three Stokes parameters in terms of radiance  $(I, Q_i, U_i)$ . It is worth noting the similarity between Eqs. (1) and (3). We conduct the analysis in terms of  $L_{\rm np} = \mu_0 R_{\rm p}$  defined in Eq. (3) to simplify the error estimate.

The distribution of random errors in  $L_{np}$  observed with POLDER is estimated in the following procedure. A reflection property of an optically thick ice cloud is that the modified polarized reflectivity  $L_{\rm nmp} = \eta (\mu + \mu_0) L_{\rm p} / \mu_0$  (where  $\eta = \pm 1$ ; Labonnote et al., 2001) crosses zero at scattering angle  $\Theta \approx 170^{\circ}$  as shown in Fig. 2. This implies that the polarization signal at  $\Theta \approx 170^{\circ}$  is primarily due to the observational noise with additional contributions from the variation of cloud particle scattering properties. We utilize this reflection property to estimate the magnitude of observational noise from the POLDER data at the scattering angles between 168 and 172°, and further estimate the noise level at other angles with a typical polarization state of cloud reflection.

The POLDER observational noise consists of radiometric noise and misregistration noise. The misregistration noise is inherent in the POLDER sensor's design that extracts polarimetric information from three images successively taken with different polarizers. The co-registration process of these three images is an inevitable source of error. As the distribution of misregistration noise is unknown, our instrument model attempts to explain both noise components with a radiometric noise model in the following analysis.

The distribution of  $L_{\rm np}$  can be modeled in the form

$$L_{\rm np} = \sqrt{X_1^2 + X_2^2 + X_3^2 - X_1 X_2 - X_2 X_3 - X_3 X_1},$$

$$34289$$

**ACPD** 

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page **Abstract** Introduction Conclusions References Figures **Tables** 

Paper

Discussion Paper

Discussion Paper

Back Close

M

Full Screen / Esc

Printer-friendly Version



Discussion Paper

Printer-friendly Version

Interactive Discussion



where random variables  $X_1$ ,  $X_2$ , and  $X_3$  represent the radiances of a pixel in the original three images with different polarizers (not available in a product). In the derivation of Eq. (4), we assume that  $X_1$ ,  $X_2$ , and  $X_3$  follow the same normal distribution centered at 0.5 with variance  $s^2$  (i.e.,  $X_i \sim N(0.5, s^2)$ ) because the average polarization is assumed to be zero at scattering angles between 168 and 172°. With this assumption, we apply the parametric bootstrap method (e.g., Evans and Rosenthal, 2010) to obtain the distribution of  $L_{np}$  as a function of variance  $s^2$ . The observational distribution of  $L_{np}$  in the scattering angle between 168 and 172° (within the rectangular box in Fig. 2) is shown in the bar chart of Fig. 3, and compared with the theoretical distribution with s = 0.00095(solid line). Figure 4 justifies our selection of s = 0.00095 by showing that the sum of squared errors of the density in each bin of the histogram (Fig. 3) is minimized when s = 0.00095. Therefore, we take s = 0.00095 as the standard error for  $X_1$ ,  $X_2$ , and  $X_3$ . In Fig. 3, the distribution from observations is slightly more skewed than the distribution from bootstrapping, but their agreement is satisfactory for error estimation.

To obtain the approximate magnitude of the  $L_{np}$  error at other scattering angles, the same parametric bootstrap method is applied with the degree of linear polarization fixed at 5%, which is the upper limit for typical ice cloud reflection. This selection does not significantly affect the following analysis. When the signal is polarized, random variables  $X_1$ ,  $X_2$ , and  $X_3$  do not follow the same distribution, but we assume that the standard errors for  $X_1$ ,  $X_2$ , and  $X_3$  still stay the same. Figure 5 shows the estimated magnitude of error (variance) as a function of normalized radiance  $L_n$ . The variance of  $L_{np}$  asymptotes to a near-constant value once  $L_n$  reaches  $L_n = 0.2$ . As shown in insets, the distribution becomes closer to a normal distribution with increasing  $L_n$ . Based on the discussion above, we conclude that the error distribution of  $L_{np}$  approximately follows a normal distribution with variance var  $(L_{no}) = 1.35 \times 10^{-6}$  for a reflective target  $(L_n \ge 0.2)$ . This estimate of error is about the same magnitude as the value by Fougnie et al. (2007). Note that we assume that the error is purely from observational noise, neglecting any natural cloud variability. Therefore, the actual radiometric noise level

#### **ACPD**

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page **Abstract** Introduction

Conclusions References

**Tables Figures** 

Back Close

Full Screen / Esc

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I**∢** ►I

**■** Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

© (i)

# 2.1.2 Ancillary data from MODIS and AIRS

The MODerate resolution Imaging Spectroradiometer (MODIS) instruments onboard the Aqua and Terra satellites measure radiance at multiple visible and infrared wavelengths, providing various products (King et al., 2003) that are complementary to those from PARASOL. Of interest here is the Collection 6 Level 2 cloud product (MYD06) from Aqua MODIS, with which the PARASOL satellite was flying in formation until 2009. Cloud top temperature and thermodynamic phase are extracted from MYD06 and are collocated to POLDER data to be used in the analysis described later in this section. In addition, Level 3 monthly mean ozone concentration from the Atmospheric Infrared Sounder (AIRS) on the Aqua satellite is also used, in particular to account for absorption by ozone that attenuates reflected radiation in the visible.

should be somewhat smaller than our estimate. We apply the same variance to all

three POLDER channels used in the analysis (0.865, 0.67, and 0.49 µm).

#### 2.1.3 Collocation and selection

The PARASOL Level 1 radiometric data is first collocated with the MODIS Level 2 cloud product (Platnick et al., 2015) to select pixels containing ice clouds. Only PARASOL pixels that have corresponding MODIS observations are selected, and filtered by the criteria summarized in Table 1. The intent of the filtering process is to avoid cloud edge contamination, to avoid supercooled water droplets, and to select pixels where clouds are optically thick. The selection criterion of 208 K is a threshold used to identify convective precipitation in the tropics (Mapes and Houze, 1993). The analysis is applied only over oceans so the influence of surface reflection is minimal.

A "pixel" in the PARASOL Level 1 product contains multiple reflectivity data observed from up to 16 viewing geometries. Individual reflectivity data stored in a pixel is called a "view", and we select valid views using criteria relating to scattering angle and sunglint angle (see Table 1). When five or more valid views are contained in a pixel that satisfy

all pixel criteria previously mentioned, the pixel is marked as valid, and the roughness

**ACPD** 

15, 34283–34323, 2015

# Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

# Title Page **Abstract** Introduction Conclusions References

**Figures Tables** 





Close

Full Screen / Esc

Back

Printer-friendly Version

Interactive Discussion



inference is attempted.

#### Inversion methods

#### Selection of retrieval parameters

To overcome the problem of the conventional "best-fit" approach that uses a discrete set of roughness parameters, we construct a continuous parameter space for the particle roughness with empirical orthogonal functions (EOF). The goal of the EOF analysis is to find the parameter space that describes the variation of the  $-P_{12}$  element of the phase matrix when varying the particle roughness. An ideal approach would be to use a collection of  $-P_{12}$  values from observations (Rodgers, 2001), but such a dataset is unavailable. For this reason, we apply EOF analysis to the  $-P_{12}$  simulated with light scattering calculations. The first and second EOFs together explain 99.3% of the entire variation of  $-P_{12}$  in the scattering angle range from 60 to 160°, so  $-P_{12}$  for a particle of any roughness can be reconstructed almost exactly from the first and second EOFs by a simple linear combination. Also,  $-P_{12}$  for a mixture of particles with different roughness parameters can be reconstructed by the same linear combination.

The details of the particle model are as follows. The EOF analysis is applied to  $-P_{12}$  elements of the phase matrices calculated by the method described by Yang et al. (2013), which is a combination of the Improved Geometric Optics Method (IGOM, Yang and Liou, 1996) and the Amsterdam Discrete Dipole Approximation method (ADDA, Yurkin et al., 2007). Ten prescribed roughness parameter ( $\sigma^2$ ) values are used in calculations: 0, 0.03, 0.05, 0.1, 0.15, 0.2, 0.3, 0.4, 0.5, and 0.7. The column aggregate shape is chosen because the most extensive previous study on a global scale (Cole et al., 2014) implies that this habit produces the most consistent agreement with observations. In addition, this habit is used in the retrieval scheme for the operational MODIS Collection 6 cloud products. This particle shape is an aggregate of eight column elements that are solid hexagonal particles with slightly different particle aspect ratios (Yang et al., 2013). The choice of roughness parameter is somewhat arbitrary, but our intent is to outline the variation of  $-P_{12}$  over the course of roughness changes, including the roughness parameter used in MODIS Collection 6 ( $\sigma^2 = 0.5$ ). A gamma particle size distribution with an effective size (diameter) of 60 µm and an effective variance of 0.1 is used in this study since we expect little impact on our analysis due to this size distribution selection (Cole et al., 2014).

The weights for the EOFs (EOF scores) are displayed in Fig. 6, and some original and reconstructed  $-P_{12}$  curves are plotted in Fig. 7. Figure 6 shows that the EOF 1 score is a monotonic function of the roughness parameter. Since the first EOF explains most of the  $-P_{12}$  variation (85.6%), it can be considered as an effective roughness parameter for this shape. The relation between EOF 1 scores and the natural logarithm of roughness parameters is nearly linear (Fig. 8), indicating that the roughness parameter can be subsequently inferred after the inference of the EOF 1 score. The straight line in Fig. 8 is the regression line defined in the form

$$\sigma^2 = \exp[-115.755 \times (EOF 1 score) - 2.3543].$$
 (5)

In addition, the EOF 2 score provides constraints on the retrieval especially for large roughness parameters, where the EOF 1 score is less sensitive to the roughness variation. Therefore, the EOF 1 and EOF 2 scores are selected as retrieval parameters related to particle roughness.

Another factor that can impact the roughness retrieval is atmospheric Rayleigh scattering above the cloud. Above-cloud Rayleigh scattering has previously been used to infer cloud top pressure from polarimetric measurements (e.g., Buriez et al., 1996), with results comparable to those from  $O_2$  A band retrievals and ISCCP (Parol et al., 1999). With the POLDER instruments, Rayleigh scattering is primarily detected as a spectral and directional difference of polarized reflectivities. Figure 9 shows the change of  $L_{\rm np}$  at 0.865 µm, as a function of scattering angle, in response to a 300 hPa change in cloud top pressure (i.e., from 200 to 500 hPa, the red line) and a change of similar effect in roughness parameter (from  $\sigma^2 = 0.15$  to 0.5, the dashed green line). The ef-

### **ACPD**

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ✓ ▶I

Back

Printer-friendly Version

Full Screen / Esc

Close

Interactive Discussion



#### 5 2.2.2 Construction of forward model

Once the inverse problem is formulated, the next step is to construct a forward model that is fast enough to be embedded in the inversion algorithm. From the discussion in Sect. 2.1, the inverse problem is formalized as follows: (1) the parameters to be inverted are the EOF 1 and EOF 2 scores, and cloud top pressure; and (2) observations are MODIS-AIRS-collocated  $L_{\rm np}$  from POLDER at central channel wavelengths 0.865, 0.67, and 0.49 µm. To satisfy the requirements for numerical efficiency, the present forward model is based on a look up table. Technically, it is possible to build a forward model based on a three-dimensional lookup table, but the linearity between EOF scores and  $L_{\rm np}$  simplifies the forward model. The linear model for  $L_{\rm np}$  as a function of EOF scores  $x_1$  and  $x_2$  is defined by

$$L_{\text{np}, i} = a_i + b_i x_1 + c_i x_2. (6)$$

By linear regression, a set of coefficients  $a_i$ ,  $b_i$ , and  $c_i$  is obtained for each viewing geometry denoted in terms of index i. The viewing geometry is gridded as follows: solar zenith angles from 0 to 81°, viewing zenith angles from 0 to 75°, and relative azimuth angles from 0 to 180°, with an interval of 3° for each. The regression is repeated for seven atmospheric scattering optical thicknesses above the cloud: 0, 0.02, 0.05, 0.1, 0.15, 0.2, and 0.3, and stored in a file so that one can apply appropriate interpolations. In this way, once cloud top height and EOF scores are prescribed,  $L_{\rm np}$  can be obtained for each specific viewing geometry and wavelength.

The performance of this fast model is satisfactory for the present study. A typical difference between an exact calculation and our forward model is shown in Fig. 10.

ACPD

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page
Abstract Inti

Paper

Discussion

Discussion Paper

stract Introduction

Conclusions References

Tables Figures

I**4** ►I

Close

**→** 

Full Screen / Esc

Back

Printer-friendly Version



The overall accuracy is within  $1 \times 10^{-4}$  in terms of  $L_{np}$  and the peak-to-peak variation is  $5 \times 10^{-4}$  even in the worst case ( $\sigma^2 = 0.03$ ). The overall error of  $1 \times 10^{-4}$  implies that the model bias is less than 10% of the observation error given by  $\left(\sqrt{\text{var}(L_{np})} = \sqrt{1.35 \times 10^{-6}} = 1.16 \times 10^{-3}\right)$ . The bias may be detected in the residual of the inversion, but the influence on the roughness inference is negligible.

In calculating cloud reflectivity, a single-layer homogeneous cloud is assumed, and the cloud optical thickness is set to 5 (roughly the saturation point of polarized reflectance) No aerosol is assumed to be present above and below clouds. As optically thick cold ice clouds occur in the upper troposphere, the radiometric contribution from lower tropospheric aerosol is neglected. For the same reason, the surface is assumed to be dark. There may be an influence from aerosols above the cloud layer, such as transported mineral dusts and stratospheric sulfates, but we disregard them to be in line with previous studies. The influence of such aerosol layers on inferences of cloud properties is beyond the scope of this paper but should be investigated in the future.

The adding-doubling radiative transfer program formulated by de Haan et al. (1987) with significant improvements by Huang et al. (2015) is used in the calculation. The first-order scattering is calculated analytically and combined with the multiple scattering results from the adding-doubling model, following the TMS method (Nakajima and Tanaka, 1988). Further, the cloud reflectivity is multiplied by the transmissivity that changes due to ozone absorption; the transmissivity is calculated from the monthly mean AIRS ozone concentration.

#### 2.2.3 Maximum likelihood estimation

Once the inverse problem is formulated and the forward model is built, the last step is to find the set of parameters for each pixel based on observations. The simple but powerful maximum likelihood method with a normal error distribution is appropriate for our problem because we have little knowledge about the distribution of parameters. As

**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l< ≻l

1

Close

Full Screen / Esc

Back

**Printer-friendly Version** 

Interactive Discussion



each pixel typically contains five to eight valid views (Sect. 2.1.2) at three wavelengths, the number of observations in each pixel ranges from 15 to 24.

The standard deviation (SD) and correlation (Corr) of inferred parameters are calculated in the framework of maximum likelihood estimation, and used to avoid undersconstrained inferences. The pixel is rejected if SD (EOF 1 Score) > 0.02, SD (EOF 2 Score) > 0.02, or Corr (EOF 1 Score, EOF 2 Score) > 0.3. The standard deviation and the correlation depend only on the observation geometry and particle model and are independent of the observed polarized reflectivity. Therefore, this rejection process can be interpreted as the refinement of pixels based on the information content to achieve a reliable inference.

The error distribution is confirmed to be normal (see Sect. 2.1.1), so if the problem is not strongly nonlinear, the parameters' error distributions are expected to be normal as well (Rodgers, 2000). As expected, Fig. 11 demonstrates that the application of the maximum likelihood method with synthetic  $L_{\rm np}$  data results in a symmetric distribution about the EOF 1 score corresponding to the true roughness parameter  $\sigma^2$  = 0.15. The distribution is not strictly normal because the number of observations in each pixel varies, but the error distribution of each pixel is theoretically derivable, as well as the confidence interval.

For the synthetic retrieval in Fig. 11, the median of the inverted EOF 1 score is -0.00336 and the corresponding roughness parameter is  $\sigma^2 = 0.14$ . The interquartile range of the EOF 1 score distribution is [-0.01146:0.00476], which corresponds to the roughness parameter range of [0.05:0.36]. The result indicates that our approach has a practical skill in estimating the particle roughness parameter out of observations superimposed with noise. This is a remarkable contrast with the traditional "best-fit" approach (cf. Fig. 1).

The distribution of the  $\chi^2$  values for the synthetic retrieval is presented in Fig. 12. The  $\chi^2$  value is a variance-normalized residual squared sum that is defined for each pixel, and follows the  $\chi^2$  distribution with degrees of freedom  $N_{\rm d}$  if the inversion is successful, where  $N_{\rm d}$  is the observational degrees of freedom (approximately, the number

ACPD

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

l∢ ≯l

- ◆

Close

Full Screen / Esc

Back

Printer-friendly Version

Interactive Discussion



of observations in a pixel). As the  $\chi^2$  distribution of  $N_{\rm d}$  degrees of freedom has a peak about  $N_{\rm d}$ , the distribution of the  $\chi^2$  value indicates whether the inversion is successful. If the location of the peak of a distribution of  $\chi^2$  values is smaller than  $N_{\rm d}$ , the observation error may be overestimated, and if the location of the peak is larger than  $N_{\rm d}$ , the observation error is underestimated, or the forward model does not represent reality (Rodgers, 2000). The distribution in Fig. 12 has a peak at about 12, and very few pixels have a  $\chi^2$  value over 40. This is a reasonable distribution because the number of observations ( $\approx N_{\rm d}$ ) is about 15 to 24 for most pixels. Because the 95th percentile for the  $\chi^2$  distribution with 24° of freedom is 36.42, it is no surprise that very few pixels have a  $\chi^2$  value over 40.

Figures 11 and 12 demonstrate the validity of our inference framework under an idealized situation, where the error distribution and the true roughness parameter are constant. In application to actual satellite data, however, the true roughness parameter varies from pixel to pixel while the error distribution stays the same. Therefore, the distribution of the EOF 1 score must be more spread out as a result of convolution of the error distribution and the true roughness parameter distribution. In contrast, the  $\chi^2$  distribution is expected to be about the same. The result of the application to the actual data is given in the next section.

#### 3 Results and discussion

### 3.1 Roughness parameter of cold ice cloud over oceans

With the cloud selection criteria listed in Table 1, 79 132 pixels were selected for inversion. The information content was sufficient for full analysis of 23 359 pixels, for which results are presented in this section.

The histogram of the inferred EOF 1 score is presented in Fig. 13 based on one month of collocated PARASOL/MODIS data over extratropical (latitude  $> 30^{\circ}$ ) oceans during September 2005. The width of the histogram in Fig. 13 is broader than the

# ACPD

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ✓ ▶I

Back Close

Printer-friendly Version

Full Screen / Esc

Interactive Discussion



Discussion Paper









M

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

monodispersive roughness case (Fig. 11), indicating significant variability in the microphysical properties of clouds. The median of the distribution is -0.0293, corresponding to a surface roughness parameter of 2.82. The interquartile range of the EOF 1 score is [-0.0429:-0.0165], implying 50% of the data is within the roughness parameter ( $\sigma^2$ ) 5 range of [0.65:13.6]. The result supports the use of the roughened particle model in extratropical ice cloud retrievals as suggested by previous studies. While our analysis is limited to very cold ice clouds over ocean, the validity of using roughened crystals in the MODIS Collection 6 ice model is supported, although further explorations into warmer and optically thinner clouds are desirable. In general, cloud particles become more complex as the cloud temperature increases (Heymsfield et al., 2002), thus we expect more roughened particles in warmer clouds that are not included in our analysis.

As the roughness parameter of 2.82 lies outside of our prescribed roughness parameter range (0 to 0.7), it is an estimate by extrapolation. Yet, this projection of roughness parameter implies that the conventional degree of roughness may not be sufficient to represent actual cloud particles with the aggregate column model. As the accuracy of roughness approximation for such a large roughness parameter is questionable, a more complex and imperfect cloud particle habit may be suitable for the representation.

The distributions of the  $\chi^2$  value in the tropics and extratropics are separately presented in Fig. 14. As discussed in the previous section, a distribution of  $\chi^2$  values indicates the validity of the inversion. While the distribution of the  $\chi^2$  values in the extratropics shows a reasonable behavior (Fig. 14a), the distribution of the  $\chi^2$  values in the tropics has a very long tail with the mean  $\chi^2$  being 59.7, which is unacceptably large (Fig. 14b). This long tail implies that our forward model does not properly reproduce the observed  $L_{nn}$  field in the tropics, presumably because some underlying assumptions are not appropriate. Some possibilities that violate our underlying assumptions include sub-pixel scale cloud heterogeneity, the presence of ice particles with other habits or aspect ratios, their vertical heterogeneity, and cloud 3-D effects. The extension of the parameter space to include other habits will be investigated in future work.

**ACPD** 

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

**Abstract** Introduction

Conclusions

References **Figures** 

**Tables** 







To gain a better insight into the cause of the long tail in the tropics, a case study is conducted for two cloudy scenes: a typical extratropical scene and a tropical cloud scene with systematically large  $\chi^2$  values. Figure 15 displays true color composites from PARASOL with markers indicating the locations of detailed analysis. A green circle is shown where the  $\chi^2$  value is less than the 95th percentile of the  $\chi^2$  distribution (reasonable deviation from the forward model), and a magenta cross is shown where the  $\chi^2$  value is more than the 95th percentile (too far from the forward model). The locations of the magenta crosses in Fig. 15a (typical extratropics) are somewhat systematic; they appear at cloud boundaries or at isolated locations. This may suggest that cloud heterogeneity and cloud 3-D effects cause a small number of inference failures in the extratropics.

In contrast to the typical extratropical scene, magenta crosses are prevalent throughout the tropical scene in Fig. 15b. Since the cloud reflectivity is comparable to the typical extratropical scene, it is not likely that the inference failures are due to contamination by surface reflection. Also failures cannot be fully explained by 3-D effects of clouds as a few green circles appear randomly. Flaws in the assumptions that depend little on the relative location in a cloud, such as cloud particle shape and cloud heterogeneity (e.g. Oreopoulos, 2009), are therefore suspected as causes of the inference failure in the tropics.

# 3.3 Comparison with scattering properties in the MODIS retrieval scheme

By definition of our EOF scores, the inverted EOF scores translate into  $-P_{12}$  on a pixel-by-pixel basis. The reconstructed  $-P_{12}$  reflects a variation due to observation error and natural variability. To accurately interpret the result, we reconstructed  $-P_{12}$  from extratropical data with a precise EOF 2 score (SD (EOF2) < 0.01). The area shaded with gray in Fig. 16 shows the interquartile range of the reconstructed  $-P_{12}$  which indicates that 50% of our extratropical observations fall within the shade at a given

ACPD

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

C

Paper

Discussion Paper

Discussion Paper

Introduction References

Conclusions F

Figures







**Abstract** 







Full Screen / Esc

**Printer-friendly Version** 

Interactive Discussion



Discussion Paper

Paper

Back

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

scattering angle. The blue line is  $-P_{12}$  for the particle shape used in MODIS Collection 6, and the green line is that for the shape in MODIS Collection 5. Both particle models assume a gamma distribution with effective particle size of 60 µm and effective variance of 0.1. The blue line (Collection 6) is closer to our reconstruction, while the green line (Collection 5) significantly deviates from our reconstruction. This result indicates that the particle habit adopted for MODIS Collection 6 is more consistent with polarimetric observations than the habit mixture used for MODIS Collection 5, for which only one of the habits included a limited degree of roughness.

We also find that better consistency is obtained with a mixture of two habits: 70 % column aggregate particles with roughness parameter of  $\sigma^2 = 0.8$  and 30% severely roughened hollow bullet rosette particles ( $\sigma^2 = 0.5$ ) included in the scattering property library by Yang et al. (2013), as indicated by the thick magenta line in Fig. 16.

# **Summary and future directions**

In this study, the particle roughness parameter of very cold ice clouds over ocean is inferred by employing a new framework that is resilient to the observational error. The distinct feature of the framework is the continuous parameter space that is constructed with an empirical orthogonal function (EOF) analysis. Two EOFs are found to be sufficient to explain the variation of  $-P_{12}$  with a changing particle roughness parameter, substantially reducing the number of parameters for the forward model.

From unpolarized cloud reflection at the scattering angle of 170°, the observational error of the PARASOL data is empirically estimated. Supported by the error analysis with parametric bootstrapping, the maximum likelihood method is applied to the inverse problem. The method provides error estimates and correlations for inverted parameters, which are unavailable with the "best-fit" approach used in the previous studies. To correctly incorporate the effect of atmospheric Rayleigh scattering, the cloud-top height is inferred simultaneously.

**ACPD** 

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Introduction

References

**Figures** 

Close

**Abstract** Conclusions **Tables** 

The application of the present method to cold ice clouds over extratropical oceans results in a roughness parameter of 2.82, implying that the use of the roughened particle model is suitable for cloud property retrievals. By contrasting the distribution of  $\chi^2$  values in the tropics and extratropics, we find that the performance of our method needs to be enhanced in the tropics. Possible future technical improvements may be an extension of parameter space to include multiple particle shapes, application to optically thin clouds, and integration with unpolarized radiance observations.

The reconstructed  $-P_{12}$  curve shows better consistency with  $-P_{12}$  from the particle shape model used in MODIS Collection 6 than  $-P_{12}$  from MODIS Collection 5. The addition of roughness and a hollow bullet rosette particle shape further improves the consistency.

Since its launch in 2004, the PARASOL satellite observed global polarimetric reflectivity nearly simultaneously with MODIS for five years until leaving the A-train constellation in 2009. A large amount of PARASOL data is available to apply the framework described in this paper. Local variations of the roughness parameter, correlation of the roughness parameter to other meteorological data, and the impact of cloud heterogeneity are to be investigated in our future study.

Acknowledgements. The authors thank the ICARE Data and Service Center for providing POLDER/PARASOL data, the NASA LAADS system for providing MODIS atmosphere products, and the NASA GSFC GES DAAC for providing AIRS data. The ice particle scattering calculations are conducted at the Texas A&M University Supercomputing Facility. The authors are grateful to Lei Bi for help in light scattering computations. This work was funded by NASA Grants NNX11AR06G and NNX15A12H, and the authors are grateful for continued support from Hal Maring.

# ACPD

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ✓ ▶I

**→** 

Full Screen / Esc

Back

Printer-friendly Version

Close

Interactive Discussion



Baran, A. J. and Labonnote, L. C.: A self-consistent scattering model for cirrus. I: the solar region, Q. J. Roy. Meteor. Soc., 133, 1899–1912, 2007.

Baum, B. A., Yang, P., Hu, Y. X., and Feng, Q.: The impact of ice particle roughness on the scattering phase matrix, J. Quant. Spectrosc. Ra., 111, 2534–2549, 2010.

Chepfer, H., Brogniez, G., and Fouquart, Y.: Cirrus clouds' microphysical properties deduced from POLDER observations, J. Quant. Spectrosc. Ra., 60, 375–390, 1998.

Cole, B. H., Yang, P., Baum, B. A., Riedi, J., Labonnote, L. C., Thieuleux, F., and Platnick, S.: Comparison of PARASOL observations with polarized reflectances simulated using different ice habit mixtures, J. Appl. Meteorol. Clim., 52, 186–196, 2013.

Cole, B. H., Yang, P., Baum, B. A., Riedi, J., and Labonnote, L. C.: Ice particle habit and surface roughness derived from PARASOL polarization measurements, Atmos. Chem. Phys., 14, 3739–3750, doi:10.5194/acp-14-3739-2014, 2014.

Deschamps, P., Bréon, F., Leroy, M., Podaire, A., Bricaud, A., Buriez, J. C., and Sèze, G.: The POLDER mission – instrument characteristics and scientific objectives, IEEE T. Geosci. Remote, 32, 598–615, 1994.

de Haan, J. F., Bosma, P. B., and Hovenier, J. W.: The adding method for multiple scattering calculations of polarized light, Astron. Astrophys., 183, 371–391, 1987.

Evans, M. J. and Rosenthal, J. S.: Probability and Statistics: the Science of Uncertainty, 2nd Edn., W. H. Freeman and Company, New York, USA, 2010.

Fougnie, B., Bracco, G., Lafrance, B., Ruffel, C., Hagolle, O., and Tinell, C.: PARASOL in-flight calibration and performance, Appl. Optics, 46, 5435–5451, 2007.

Heymsfield, A. J., Bansemer, A., Field, P. R., Durden, S. L., Stith, J. L., Dye, J. E., Hall, W., and Grainger, C. A.: Observations and parameterizations of particle size distributions in deep tropical cirrus and stratiform precipitating clouds: results from in situ observations in TRMM field campaigns, J. Atmos. Sci., 59, 3457–3491, 2002.

Heymsfield, A. J., Schmitt, C., and Bansemer, A.: Ice cloud particle size distributions and pressure-dependent terminal velocities from in situ observations at temperatures from 0 to -86 °C, J. Atmos. Sci., 70, 4123–4154, 2013.

Discussion Paper

#### **ACPD**

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Discussion Paper

Discussion

Paper

Discussion Paper

Abstract
Conclusions
Tables

I 

Back

Full Sc

Full Screen / Esc

Introduction

References

**Figures** 

 $\triangleright$ 

Close

Printer-friendly Version



15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

- Title Page

  Abstract Introduction

  Conclusions References

  Tables Figures
  - l∢ ÞI

Close

4

Back

- Full Screen / Esc
- Printer-friendly Version
- Interactive Discussion
  - © BY

- Holz, R. E., Platnick, S., Meyer, K., Vaughan, M., Heidinger, A., Yang, P., Wind, G., Dutcher, S., Ackerman, S., Amarasinghe, N., Nagle, F., and Wang, C.: Resolving ice cloud optical thickness biases between CALIOP and MODIS using infrared retrievals, Atmos. Chem. Phys. Discuss., 15, 29455–29495, doi:10.5194/acpd-15-29455-2015, 2015.
- Huang, X., Yang, P., Kattawar, G., and Liou, K. N.: Effect of mineral dust aerosol aspect ratio on polarized reflectance, J. Quant. Spectrosc. Ra., 151, 97–109, 2015.
  - Inoue, T.: A Cloud type classification with NOAA 7 split-window measurements, J. Geophys. Res., 92, 3991–4000, 1987.
  - King, M. D., Menzel, W. P., Kaufman, Y. J., Tanré, D., Gao, B.-C., Platnick, S., Ackerman, S. A., Remer, L. A., Pincus, R., and Hubanks, P. A.: Cloud and aerosol properties, precipitable water, and profiles of temperature and water vapor from MODIS, IEEE T. Geosci. Remote, 41, 442–458, 2003.
  - Knap, W. H., Labonnote, L. C., Brogniez, G., and Stammes, P.: Modeling total and polarized reflectances of ice clouds: evaluation by means of POLDER and ATSR-2 measurements, Appl. Optics, 44, 4060–4073, 2005.
  - Labonnote, L. C., Brogniez, G., Buriez, J.-C., Doutriaux-Boucher, M., Gayet, J., and Macke, A.: Polarized light scattering by inhomogeneous hexagonal monocrystals: validation with ADEOS-POLDER measurements, J. Geophys. Res., 106, 12139–12153, 2001.
  - Liu, C., Yang, P., Minnis, P., Loeb, N., Kato, S., Heymsfield, A., and Schmitt, C.: A two-habit model for the microphysical and optical properties of ice clouds, Atmos. Chem. Phys., 14, 13719–13737, doi:10.5194/acp-14-13719-2014, 2014.
  - Macke, A., Mueller, J., and Raschke, E.: Single scattering properties of atmospheric ice crystals, J. Atmos. Sci., 53, 2813–2825, 1996.
  - Mapes, B. E. and Houze, R. A.: Cloud clusters and superclusters over the oceanic warm pool, Mon. Weather Rev., 121, 1398–1415, 1993.
  - Masuda, K. and Takashima, T.: Feasibility study of derivation of cirrus information using polarimetric measurements from satellite, Remote Sens. Environ., 39, 45–59, 1992.
  - Masuda, K., Ishimoto, H., and Takashima, T.: Retrieval of cirrus optical thickness and ice-shape information using total and polarized reflectance from satellite measurements, J. Quant. Spectrosc. Ra., 75, 39–51, 2002.
  - Minnis, P., Heck, P. W., and Young, D. F.: Inference of cirrus cloud properties using satellite-observed visible and infrared radiances. Part II: Verification of theoretical cirrus radiative properties, J. Atmos. Sci., 50, 1305–1322, 1993.

Paper

- - 15, 34283-34323, 2015

**ACPD** 

- Degree of ice particle surface roughness inferred from polarimetric observations
  - S. Hioki et al.
- Title Page

  Abstract Introduction

  Conclusions References

  Tables Figures

  I ◀ ▶I
  - **■** Back Close
    - Full Screen / Esc
  - Printer-friendly Version
  - Interactive Discussion
    - © BY

- Minnis, P., Sun-Mack, S., Young, D. F., Heck, P. W., Garber, D. P., Chen, Y., Spangenberg, D. A., Arduini, R. F., Trepte, Q. Z., Smith, Jr., W. L., Ayers, J. K., Gibson, S. C., Miller, W. F., Hong, G., Chakrapani, V., Takano, Y., Liou, K.-N., Xie, Y., and Yang, P.: CERES Edition-2 cloud property retrievals using TRMM VIRS and Terra and Aqua MODIS data Part I: Algorithms, IEEE T. Geosci. Remote, 49, 4374–4400, 2011.
- Nakajima, T. and King, M. D.: Determination of the optical thickness and effective particle radius of clouds from reflected solar radiation measurements. Part I: Theory, J. Atmos. Sci., 47, 1878–1893, 1990.
- Nakajima, T. and Tanaka, M.: Algorithms for radiative intensity calculations in moderately thick atmospheres using a truncation approximation, J. Quant. Spectrosc. Ra., 40, 51–69, 1988.
- Neshyba, S. P., Lowen, B., Benning, M., Lawson, A., and Rowe, P. M.: Roughness metrics of prismatic facets of ice, J. Geophys. Res., 118, 3309–3318, 2013.
- Oreopoulos, L., Platnick, S., Hong, G., Yang, P., and Cahalan, R. F.: The shortwave radiative forcing bias of liquid and ice clouds from MODIS observations, Atmos. Chem. Phys., 9, 5865–5875, doi:10.5194/acp-9-5865-2009, 2009.
- Parol, F., Buriez, J.-C., Vanbauce, C., Couvert, P., Sèze, G., Goloub, P., and Cheinet, S.: First results of the POLDER "Earth Radiation Budget and Clouds" operational algorithm, IEEE T. Geosci. Remote, 37, 1597–1612, 1999.
- Platnick, S., King, M. D., Ackerman, S. A., Menzel, W. P., Baum, B. A., Riedi, J. C., and Frey, R. A.: The MODIS cloud products: algorithms and examples from Terra, IEEE T. Geosci. Remote, 41, 459–473, 2003.
- Platnick, S., Ackerman, S., King, M. D., Meyer, K. G., Menzel, W. P., Holz, R. E., Baum, B. A., and Yang, P.: MODIS atmosphere L2 cloud product (06\_L2), NASA MODIS Adaptive Processing System, Goddard Space Flight Center, 10.5067/MODIS/MYD06\_L2.006, 2015.
- <sup>25</sup> Rodgers, C. D.: Inverse methods for atmospheric sounding: theory and practice, World Scientific Publishing, Singapore, 2000.
  - Rolland, P., Liou, K.-N., King, M. D., Tsay, S.-C., and McFarquhar, G. M.: Remote sensing of optical and microphysical properties of cirrus clouds using Moderate-Resolution Imaging Spectroradiometer channels: methodology and sensitivity to physical assumptions, J. Geophys. Res., 105, 11721–11738, 2000.
  - Um, J. and McFarquhar, G. M.: Single-scattering properties of aggregates of bullet rosettes in cirrus, J. Appl. Meteorol. Clim., 46, 757–775, 2007.

Paper

- Um, J. and McFarquhar, G. M.: Single-scattering properties of aggregates of plates, Q. J. Roy. Meteor. Soc., 135, 291–304, 2009.
- van Diedenhoven, B., Cairns, B., Geogdzhayev, I. V., Fridlind, A. M., Ackerman, A. S., Yang, P., and Baum, B. A.: Remote sensing of ice crystal asymmetry parameter using multi-directional polarization measurements Part 1: Methodology and evaluation with simulated measurements, Atmos. Meas. Tech., 5, 2361–2374, doi:10.5194/amt-5-2361-2012, 2012.
- van Diedenhoven, B., Fridlind, A. M., Cairns, B., and Ackerman, A. S.: Variation of ice crystal size, shape, and asymmetry parameter in tops of tropical deep convective clouds, J. Geophys. Res., 119, 11809–11825, 2014.
- Waliser, D. E., Li, J.-L. F., Woods, C. P., Austin, R. T., Bacmeister, J., Chern, J., Del Genio, A., Jiang, J. H., Kuang, Z., Meng, H., Minnis, P., Platnick, S., Rossow, W. B., Stephens, G. L., Sun-Mack, S., Tao, W.-K., Tompkins, A. M., Vane, D. G., Walker, C., and Wu, D.: Cloud ice: a climate model challenge with signs and expectations of progress, J. Geophys. Res., 114, D00A21, doi:10.1029/2008JD010015, 2009.
- Xie, Y., Yang, P., Kattawar, G. W., Minnis, P., and Hu, Y. X.: Effect of the inhomogeneity of ice crystals on retrieving ice cloud optical thickness and effective particle size, J. Geophys. Res., 114, D11203, doi:10.1029/2008JD011216, 2009.
  - Yang, P. and Liou, K. N.: Geometric-optics-integral-equation method for light scattering by non-spherical ice crystals, Appl. Optics, 35, 6568–6584, 1996.
- Yang, P., Zhang, L., Hong, G., Nasiri, S. L., Baum, B. A., Huang, H.-L., King, M. D., and Platnick, S.: Differences between collection 4 and 5 MODIS ice cloud optical/microphysical products and their impact on radiative forcing simulations, IEEE T. Geosci. Remote, 45, 2886–2899, 2007.
  - Yang, P., Kattawar, G. W., Hong, G., Minnis, P., and Hu, Y.: Uncertainties associated with the surface texture of ice particles in satellite-based retrieval of cirrus clouds Part I: Single-scattering properties of ice crystals with surface roughness, IEEE T. Geosci. Remote, 46, 1940–1947, 2008a.
  - Yang, P., Hong, G., Kattawar, G. W., Minnis, P., and Hu, Y.: Uncertainties associated with the surface texture of ice particles in satellite-based retrieval of cirrus clouds: Part II Effect of particle surface roughness on retrieved cloud optical thickness and effective particle size, IEEE T. Geosci. Remote, 46, 1948–1957, 2008b.

**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Back Close

Full Screen / Esc

Printer-friendly Version



B.: ice

Yang, P., Bi, L., Baum, B. A., Liou, K.-N., Kattawar, G. W., Mishchenko, M. I., and Cole, B.: Spectrally consistent scattering, absorption, and polarization properties of atmospheric ice crystals at wavelengths from 0.2 to 100 μm, J. Atmos. Sci., 70, 330–347, 2013.

Yurkin, M. A., Maltsev, V. P., and Hoekstra, A. G.: The discrete dipole approximation for simulation of light scattering by particles much larger than the wavelength, J. Quant. Spectrosc. Ra., 106, 546–557, 2007.

Zhang, Z., Yang, P., Kattawar, G., Riedi, J., Labonnote, L. C., Baum, B. A., Platnick, S., and Huang, H.-L.: Influence of ice particle model on satellite ice cloud retrieval: lessons learned from MODIS and POLDER cloud product comparison, Atmos. Chem. Phys., 9, 7115–7129, doi:10.5194/acp-9-7115-2009, 2009.

10

**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Table 1. PARASOL pixel and view selection criteria.

Parameters	Criteria	Applied to
MODIS Brightness Temperature at 11 μm	Median is less than 208 K	Pixel
MODIS Infrared Cloud Phase	Ice	Pixel
PARASOL Ocean/Land Flag	Ocean	Pixel
Number of Valid Views	At least 5	Pixel
Scattering Angle	60 to 160°	View
Sunglint Angle	Greater than 30°	View

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Back

Printer-friendly Version

Full Screen / Esc

Close





15, 34283-34323, 2015

# Degree of ice particle surface roughness inferred from polarimetric observations

**ACPD** 

S. Hioki et al.



Full Screen / Esc

**Printer-friendly Version** Interactive Discussion

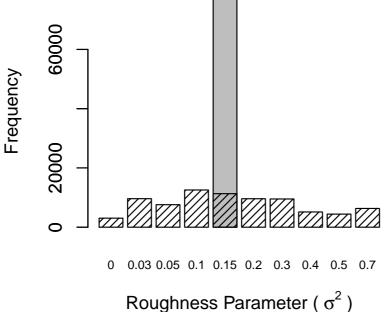


Figure 1. The response of the conventional "best-fit" approach to a synthetic signal with and without random measurement noise. The addition of noise to the synthetic signal results in a distribution of the roughness parameter (hatched bars), from which the true roughness cannot be inferred. This figure is to be compared to Fig. 11.





15, 34283-34323, 2015

**ACPD** 

# Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page Introduction **Abstract** References Conclusions

**Tables Figures** 

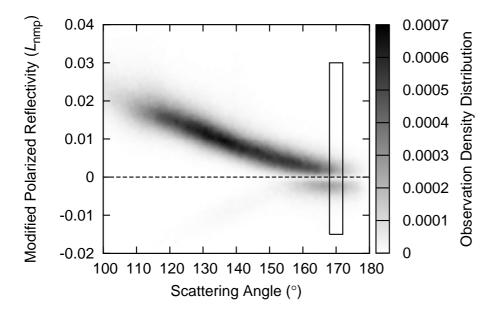
 $\triangleright$ I

Back Close

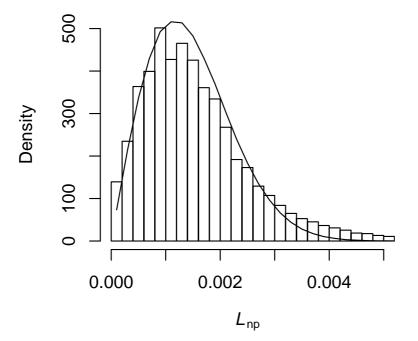
Full Screen / Esc

Printer-friendly Version





**Figure 2.** Observation density of modified polarized reflectivity ( $L_{nmp}$ ) over the Western Pacific during September 2005.  $L_{nmp}$  crosses zero at a scattering angle of approximately 170°. The data in the rectangular box is used to derive the histogram in Fig. 3.



**Figure 3.** Histogram of observed normalized polarized radiance  $(L_{np})$  from the data in the rectangular box in Fig. 2. The solid line is the simulated error using a parametric bootstrapping method with s=0.00095. The agreement is sufficient for estimating the noise level.

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I◀



Close

Back



Printer-friendly Version





15, 34283-34323, 2015

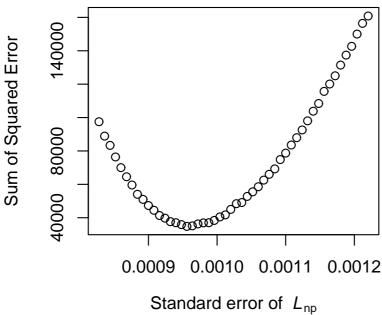
**ACPD** 

# Degree of ice particle surface roughness inferred from polarimetric observations

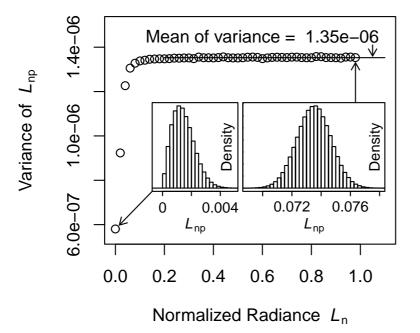
S. Hioki et al.



**Printer-friendly Version** Interactive Discussion



**Figure 4.** Sum of squared error as a function of standard error (s) of the original sensor noise. The minimum error is achieved when s = 0.00095.



**Figure 5.** The simulated variance of  $L_{np}$  as a function of  $L_{n}$ . The variance of  $L_{np}$  increases as the normalized radiance  $L_n$  (brightness of a pixel) increases, becoming nearly constant at var  $(L_{np}) = 1.35 \times 10^{-6}$  once  $L_n$  reaches  $L_n = 0.2$ . Insets show that the distribution of  $L_{np}$ tends to a normal distribution, justifying the use of a normal distribution as an error distribution of  $L_{nn}$  for a reflective cloudy pixel.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page Introduction **Abstract** Conclusions References **Figures Tables** 

Close

 $\triangleright$ 

Full Screen / Esc

Back

Printer-friendly Version





15, 34283-34323, 2015

# Degree of ice particle surface roughness inferred from polarimetric observations

**ACPD** 

S. Hioki et al.

Introduction

References

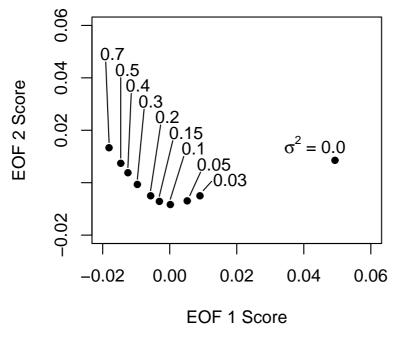
**Figures** 

 $\triangleright$ 

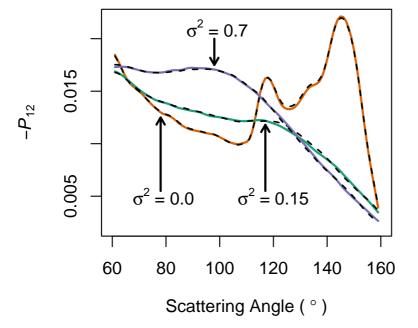
Close

Printer-friendly Version Interactive Discussion





**Figure 6.** The pairs of EOF scores needed to reconstruct the original  $-P_{12}$ . The EOF 1 score is a monotonic function of particle roughness parameter  $\sigma^2$ . The EOF 2 score reaches a minimum at particle roughness parameter of  $\sigma^2 = 0.1$ .



**Figure 7.** Comparison of the reconstruction and the original  $-P_{12}$  elements of the phase matrix. Reconstructed  $-P_{12}$  (colored solid lines) shows a satisfactory agreement with original  $-P_{12}$  (black dot lines). Only the first and second EOFs are used in the reconstruction. This confirms that two EOFs explain almost the entire variation of  $-P_{12}$  due to the particle roughness change.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

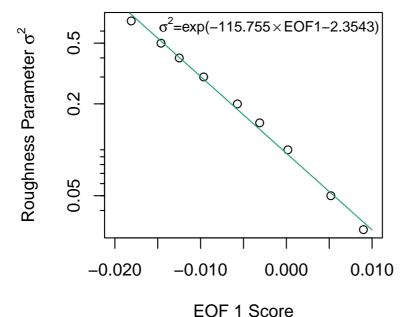
l∢ ≻l

Back Close

Full Screen / Esc

Printer-friendly Version





**Figure 8.** The relationship between the particle roughness parameter and EOF 1 score. The natural logarithm of particle roughness parameter is nearly linear to the EOF 1 score. This implies that the particle roughness can be directly inferred from the EOF 1 score.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

I

**Back** 

Conclusions References

Tables Figures

 $\triangleright$ 

Close

**→** 

Full Screen / Esc

Printer-friendly Version





15, 34283-34323, 2015

**ACPD** 

# Degree of ice particle surface roughness inferred from polarimetric observations

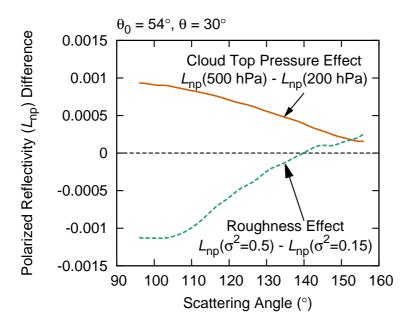
S. Hioki et al.





Printer-friendly Version





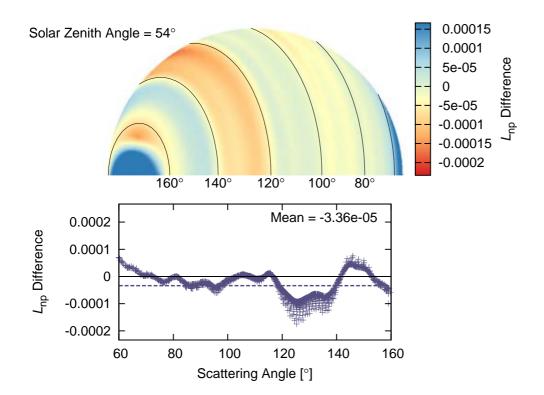
**Figure 9.** The impact of particle roughness parameter change ( $\sigma^2 = 0.15 \rightarrow 0.5$ ) and cloud top pressure change (200  $\rightarrow$  500 hPa). The magnitudes of the differences are comparable while the directional patterns are different. In this plot, the solar zenith angle is 54° and the viewing zenith angle is 30°.





Printer-friendly Version





**Figure 10.** Difference in  $L_{np}$  between exact radiative transfer calculations and our simplified forward model. At almost all angles, the difference is less than  $1 \times 10^{-4}$ . The polar plot shows the distribution of bias when the particle roughness parameter is  $\sigma^2 = 0.15$ . The bias is a function of scattering angle. However, the magnitude of error is acceptably small compared to the random observational error.

**ACPD** 

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Introduction **Abstract** 

Conclusions References

> **Figures Tables**

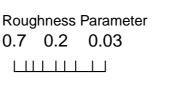


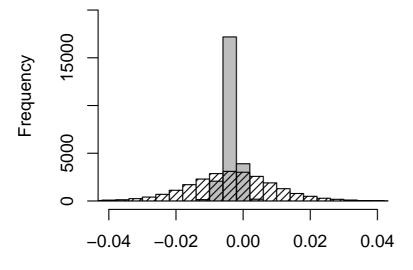




M

Full Screen / Esc





**EOF 1 Score** 

**Figure 11.** The distribution of inferred EOF 1 scores for synthetic data with and without noise. The distribution for the noise-added synthetic data is symmetric about the EOF 1 score corresponding to the true roughness. The median of EOF 1 score is -0.00336, corresponding to the roughness parameter of  $\sigma^2 = 0.14$ .

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

ables Figures

 $\triangleright$ 

Close

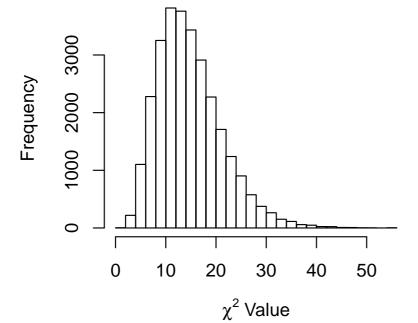
4 **>** 

Full Screen / Esc

**Back** 

**Printer-friendly Version** 





**Figure 12.** Frequency distribution of the  $\chi^2$  values (variance-normalized residual square sum). The distribution has a peak at about 12, tapering to nearly zero at approximately 40. This is a reasonable distribution because most pixels contain 15 to 24 observations.

15, 34283–34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

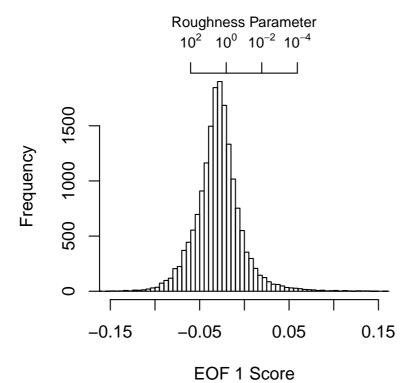
Tables Figures

Back Close

Full Screen / Esc

Printer-friendly Version





**Figure 13.** The distribution of EOF 1 scores obtained from cold ice clouds over ocean during September 2005. The median of the EOF 1 score is -0.0293, corresponding to a roughness parameter of 2.82. Consistent with previous studies, roughened particles better simulate the measured polarized reflectivity.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

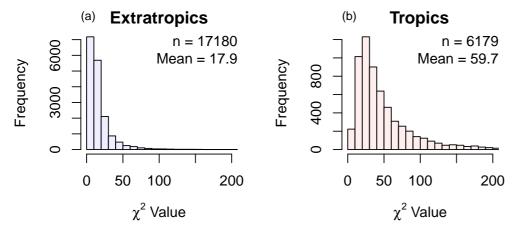
I**⊲** ▶I

■ Back Close

Full Screen / Esc

Printer-friendly Version





**Figure 14.** Distributions of  $\chi^2$  values in the tropics and extratropics. The distribution of the  $\chi^2$  value in the tropics (**b**) implies that the forward model is not correctly simulating the reflectivity in the tropics, while the distribution of the  $\chi^2$  value in the extratropics (**a**) indicates successful inversion.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

Back

Printer-friendly Version

Full Screen / Esc

Close





Discussion Paper













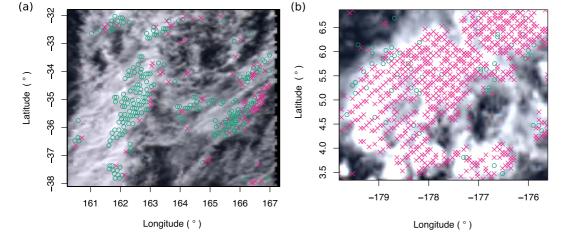


Figure 15. Comparison of (a) a typical cloud scene in the extratropics and (b) a cloud scene in the tropics where the  $\chi^2$  values are much larger than expected. Green circles are inference locations where the  $\chi^2$  value is less than 95th percentile of the  $\chi^2$  distribution, whereas magenta crosses are inference locations where the  $\chi^2$  value exceeds the 95th percentile. These figures indicate that the causes of a large  $\chi^2$  value may be different in the extratropics and tropics.

#### **ACPD**

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Introduction **Abstract** Conclusions References **Tables** 

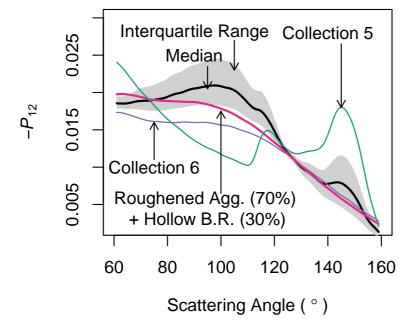


Figures

 $\triangleright$ 

Full Screen / Esc





**Figure 16.** Comparison of inferred  $-P_{12}$  and the counterparts used in MODIS Collections 5 and 6. The  $-P_{12}$  of MODIS Collection 6 (blue line) is more consistent with the reconstructed  $-P_{12}$  (black thick line) than the  $-P_{12}$  of MODIS Collection 5 (green line). However, better consistency is obtained with a two-habit model (thick magenta line), by increasing the roughness to  $\sigma^2 = 0.8$  and adding 30% of hollow bullet rosette particles.

15, 34283-34323, 2015

Degree of ice particle surface roughness inferred from polarimetric observations

S. Hioki et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

- ◀

Back Close
Full Screen / Esc

 $\triangleright$ 

Printer-friendly Version

