

1 Drizzle Formation in Stratocumulus Clouds: Effects of 2 Turbulent Mixing

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8 **Abstract**

9 The mechanism of drizzle formation in shallow stratocumulus clouds and the effect of
10 turbulent mixing on this process are investigated. A Lagrangian-Eulerian model of the cloud-
11 topped boundary layer is used to simulate the cloud measured during flight RF07 of the
12 DYCOMS-II field experiment. The model contains ~2000 air parcels that are advected in a
13 turbulence-like velocity field. In the model all microphysical processes are described for each
14 Lagrangian air volume, and turbulent mixing between the parcels is also taken into account. It
15 was found that the first large drops form in air volumes that are closest to adiabatic and
16 characterized by high humidity, extended residence near cloud top, and maximum values of
17 liquid water content, allowing the formation of drops as a result of efficient collisions. The
18 first large drops form near cloud top and initiate drizzle formation in the cloud. Drizzle is
19 developed only when turbulent mixing of parcels is included in the model. Without mixing,
20 the cloud structure is extremely inhomogeneous and the few large drops that do form in the
21 cloud evaporate during their sedimentation. It was found that turbulent mixing can delay the
22 process of drizzle initiation but is essential for the further development of drizzle in the cloud.

23

24 **1 Introduction**

25 Understanding the mechanism of drizzle formation in stratocumulus clouds (Sc) is a long-
26 standing problem in cloud physics. Formation of drizzle in the cloud leads to changes in the
27 radiative properties of Sc (Nakajima and King, 1990; Gerber, 1996; Feingold et al., 1999;
28 Brenguier et al., 2000; Rosenfeld et al., 2006, 2012). Sc cover large areas of the globe and as
29 a result microphysical processes occurring within them have a profound effect on global

1 radiation balance. The problem of drizzle formation is also interesting from a theoretical point
2 of view. In Sc, drizzle forms within narrow cloud layers of a few hundred meters, which
3 contain only little liquid water compared to more developed cumulus. Studies have shown
4 that both an increase in cloud depth (Pawlowska and Brenguier, 2003; Kostinski, 2008) and
5 an increase in the drop residential time in the cloud (Feingold et al., 1996; Magaritz et al.,
6 2009) foster drizzle formation.

7 Warm stratocumulus clouds were investigated numerically using Large Eddy Simulations
8 (LES) with different levels of complexity to describe microphysical processes (Stevens et al.,
9 2003b, 2005; Ackerman et al., 2009). Among these, LES models of Sc with spectral bin
10 microphysics were used to parameterize the rates of auto-conversion and drizzle formation
11 (Khairoutdinov and Kogan, 1999). These parameterizations are widely used in large-scale
12 models (Randall et al., 2003). And still, many LES models fail to reproduce the observed
13 structure of Sc. Specifically, LES tend to substantially underestimate values of liquid water
14 content (LWC) near cloud top (Stevens et al., 2005). Stevens et al. (2005) attributed these
15 results to uncertainties in the description of small-scale turbulent motion in LES models. That
16 study concluded that a realistic structure of Sc can be simulated only if the LES has a spatial
17 resolution as low as 1m, i.e. in configurations in which most turbulent motions are described
18 explicitly.

19 Pinsky et al. (2008) and Magaritz et al. (Magaritz et al., 2009) described a new Sc model that
20 can be referred to as a Lagrangian-Eulerian model (LEM). In the model several thousand
21 adjacent parcels (Lagrangian) move within a turbulence-like flow, with statistical parameters
22 measured in the Stratocumulus-Topped Boundary Layer (STBL). The initial model version
23 (Pinsky et al., 2008; Magaritz et al., 2009) did not include turbulent mixing of adjacent
24 parcels and did not consider the effects of mixing and entrainment at the upper cloud
25 boundary. Nonetheless, the model successfully simulated many observed properties, such as
26 LWC, droplet size distribution, and drizzle formation. It was found that drizzle forms initially
27 in 'lucky' parcels that ascend from the ocean surface and spend the most time near cloud top.
28 Such lucky parcels were estimated to comprise about 1% of all air parcels. The large droplets
29 falling from 'lucky' parcels trigger collisions and drizzle formation in parcels located below
30 them. It was found that drizzle tends to fall in downdrafts created by large eddies in the
31 STBL.

1 In the previous model version, consideration of a more realistic STBL geometry,
2 characterized by a dry and warm inversion layer above the cloud top led to the formation of
3 an unrealistic cloud structure. The extremely inhomogeneous structure was caused by
4 entrainment of dry and warm air volumes into the cloud layer. The radius of correlation of all
5 microphysical variables became equal to parcel size selected in the model, which is much
6 lower than the radii of correlation calculated from observed data.

7 In order to make cloud structure realistic and represent processes resulting from interaction
8 with the inversion layer, it was necessary to take into account processes of entrainment and
9 mixing of adjacent parcels (Magaritz-Ronen et al. 2014). It was shown that turbulent mixing
10 of parcels leads to realistic spatial variability of microphysical quantities characterized by a
11 spatial correlation scale of ~200 m. It was also shown that mixing increases the width of the
12 droplet size distribution (DSD). The characteristic time period during which an air parcel
13 maintains its identity was found to be 15-20 min. Magaritz-Ronen et al. (2014) successfully
14 simulated the structure of a non-drizzling stratocumulus maritime cloud observed during
15 research flight RF01 of the Second Dynamics and Chemistry of Marine Stratocumulus field
16 study (DYCOMS-II).

17 In the present paper we simulate a slightly drizzling cloud observed during research flight
18 RF07 of the same field campaign. The study presented here addresses two questions. The
19 first, given that turbulent mixing limits the life-time of separate cloud volumes, does the
20 concept of ‘lucky’ parcels as triggers of drizzle formation remains valid? The second question
21 is what is the role of mixing in this process? Especially, what is the effect of mixing of dry
22 and warm air from the inversion on drizzle formation in the cloud? We also address the
23 question whether DSD broadening caused by mixing at the cloud top favors drizzle formation,
24 or delays the process.

25

26 **2 Model description**

27 The model used in this study was first described in Pinsky et al. (2008) and Magaritz et al.
28 (Magaritz et al., 2009). It has been modified since the first studies were described in those
29 papers. New processes such as surface fluxes, radiative cooling from cloud top, and most
30 important, turbulent mixing of air parcels, have been incorporated. Some main model
31 developments as were first presented in Magaritz-Ronen et al. (2014) are further described
32 below.

1 The model contains about 2000 adjacent Lagrangian parcels with a characteristic linear size of
2 40m. The parcels cover the entire 2D model domain of $2500 \times 1250 \text{ m}^2$ and describe all parts
3 of an STBL, from the ocean surface, where latent and sensible heat flux is calculated, to the
4 top of an approximately 300 m deep warm and dry inversion layer. Parcels are advected
5 throughout the domain by a turbulence-like velocity field.

6 The velocity field is represented as the sum of a large number of harmonics with random
7 time-dependent amplitudes. The velocity field is assumed quasi-stationary during the entire
8 simulation, statistically uniform in the horizontal direction and obeys the Kolmogorov $-5/3$
9 law. Energetic and statistical properties of the velocity field are taken from observations using
10 two measured quantities, the vertical profile of r.m.s. of velocity fluctuations, $\sigma_w(z) =$
11 $\langle w'^2 \rangle^{1/2}$ (where w' are the fluctuations of vertical wind velocity and brackets indicate
12 horizontal averaging) and the lateral structure function (Pinsky et al., 2008; Magaritz et al.,
13 2009). Microphysical processes such as diffusion growth, collisions, and sedimentation are
14 calculated in each individual parcel. At $t = 0$ min, each Lagrangian parcel contains only
15 wetted aerosols (haze particles) and the entire boundary layer (BL) is cloud-free. Parcels are
16 advected in the velocity field, so that some parcels may cross the lifting condensation level
17 (LCL) and become cloudy. These parcels will contain drops as well as wetted aerosols.
18 During the parcels' motion droplets may continue to grow or evaporate, resuming to the form
19 of haze particles. Aerosol and drop distributions are calculated using a single 500-bin mass
20 grid with a $0.01 \mu\text{m}$ to $1000 \mu\text{m}$ radius range. The single bin grid allows explicit separation
21 between haze particles in equilibrium with the environment and cloud drops with no
22 specialized nucleation parameterization. Nucleation, diffusion growth, and partial or full
23 evaporation are described by the full diffusion growth equation, with a small time step of
24 0.01s to accurately describe the growth of the smallest particles (Pinsky et al., 2008; Magaritz
25 et al., 2010). Diffusion growth of droplets is calculated on a movable mass grid, in which each
26 bin shifts along the mass axis, according to the solution of the equation. The use of movable
27 bins eliminates numerical spectrum broadening, while increasing the accuracy of droplet size
28 distribution calculations.

29 Droplet growth by collisions is described using the stochastic equation for collisions and $1 \mu\text{m}$
30 resolution tables for collision efficiencies presented by Pinsky et al (2001). Collisions are
31 performed on a regular 500-bin mass grid using the Kovetz and Olund method (1969). The

1 great number of bins assures a high degree of accuracy in the calculation of collision growth
2 of droplets.

3 One of the most prominent features of this model is that parcels are not isolated and there are
4 two types of interaction between Lagrangian parcels: droplet sedimentation and turbulent
5 mixing. Droplet sedimentation through parcel boundaries allows larger droplets that form in
6 cloud parcels to act as drop collectors during their fall and reach the surface as drizzle. To
7 calculate sedimentation the entire computational area is covered by an auxiliary regular grid
8 with a 5m resolution. Droplet flux is calculated through each of 5m grid increments
9 separating adjacent parcels.

10 Turbulent mixing between adjacent Lagrangian parcels is described using an expansion of K-
11 theory for cases of mixing of conservative and non-conservative values (such as DSD) given
12 on a non-regular spatial grid formed by parcel centers. The algorithm was first presented in
13 Pinsky et al. (2010) and applied by Magaritz-Ronen (2014). The turbulent coefficient K is
14 calculated as $K(l) = C\varepsilon^{\frac{1}{3}}l^{\frac{4}{3}}$ (Richardson's law), where l is the distance between parcel
15 centers, ε is the turbulent kinetic energy dissipation rate taken from observations, and $C = 0.2$
16 (Monin and Yaglom, 1975).

17 To calculate mixing of DSDs, droplet flux is calculated between parcels. Because DSDs are
18 not conservative variables, the increase or decrease in droplet size during transport from one
19 parcel to another is taken into account according to the equation of diffusion growth. Thus,
20 mixing at sub-grid scales is accompanied by latent heat release. This process differs from
21 latent heat release at the resolvable scales, where supersaturation is determined by the parcel's
22 vertical motion and droplet concentration.

23 Since the parcels move within an Eulerian coordinate system and droplet sedimentation is
24 performed at the regular Eulerian finite-difference grid, the model is regarded as a
25 Lagrangian-Eulerian Model (LEM).

26 Sensible and latent heat surface flux is calculated using the bulk-aerodynamic formulas, with
27 a Dalton number of $C_E = 0.002$ (Smith, 1988) and background wind at 10 m of $10m s^{-1}$.
28 The model's computational area is assumed perpendicular to the background wind so the
29 wind affects only the surface flux.

30 Parameterization of long wave radiative cooling based on the two-stream approximation
31 following Khvorostyanov (1995) and Khvorostyanov et al. (2003) is used in the model.

1 The model has periodic boundary conditions in the horizontal direction. There is no averaged
2 air subsidence above cloud top in the model. In the STBL large-scale subsidence sharpens
3 gradients of temperature and humidity at the upper cloud boundary and can reduce the rate of
4 increase of cloud top height. In the model, the rate of mixing and entrainment at cloud top is
5 determined by the slope of the ε profile. With the profile used in the simulations presented
6 here, mixing of cloud and inversion air increases cloud top height, indicating an active
7 process of turbulence-induced entrainment.

8 **3 Design of simulations**

9 For this study the cloud observed during flight RF07 of the DYCOMS-II field campaign
10 (Stevens et al., 2003a) was simulated in the model. The stratocumulus cloud measured during
11 this night flight was ~500 m thick and capped by a strong inversion at 825 m. Drizzle flux at
12 the surface in this flight was evaluated at 0.6 mm/day (VanZanten et al., 2005).

13 Measurements of the vertical profile of $\sigma_w(z) = \langle w'^2 \rangle^{1/2}$ (Stevens et al., 2005) and the lateral
14 structure function (Lothon et al., 2005) were implemented in the model to generate the
15 turbulence-like velocity field, with observed statistical properties. The $\sigma_w(z)$ maximum was
16 equal to 0.5 m/s at $z = 500$ m and zero in the inversion layer, above $z=800$ m. The method for
17 determining parameters of the turbulence-like model using these observed values is described
18 by Pinsky et al. (2008) in detail.

19 The dissipation rate of turbulent kinetic energy (ε) was used to calculate mixing of parcels.
20 The dissipation rate is set to a constant value of $10 \text{ cm}^2 \text{ s}^{-3}$ in the BL and decreases above
21 cloud-top. The profile and values are typical of the stratocumulus clouds under consideration
22 (Lothon et al., 2005; Siebert et al., 2010; Katzwinkel et al., 2011).

23 Initial aerosol distribution was derived from observations (total concentration 200 cm^{-3} ,
24 radius range 0.01-1.3 μm) and assumed to be the same for all parcels at $t = 0$ min in the
25 boundary layer (Magaritz et al., 2009). Initial concentration of aerosols in parcels within the
26 inversion layer was set to zero. Initial temperature and humidity profiles are assumed to be
27 horizontally uniform at $t=0$. Initial relative humidity (RH) is set to approximately 90% below
28 the inversion level. It decreases rapidly at heights above that level.

29 In this study we investigate the formation the first large-sized drops and drizzle in shallow
30 stratocumulus clouds and the role of turbulent mixing in this process. To this end several
31 simulations were performed. The control run (CON) included all processes and simulated the

1 cloud measured during flight RF07. Supplemental simulations included a simulation with no
2 turbulent mixing between the parcels (NoMI), a simulation with no sedimentation between
3 the parcels (NoSd), and a simulation without mixing and sedimentation (NoMIS).
4 Measurements from flight RF07 of the DYCOMS-II field experiment were used for validation
5 of the model results.

6

7 **4 Results and discussion**

8 **4.1 Mean cloud structure**

9 Turbulent mixing at cloud boundaries and inside the cloud layer has a strong effect on the
10 macroscopic properties of the cloud and drizzle formation, especially homogenization of
11 clouds in the horizontal direction, as discussed in detail by Magaritz-Ronen et al. (2014).

12 A snapshot of the field of LWC at $t = 270$ min in the CON and NoMI simulations is presented
13 in Fig. 1. The time instance in the figure corresponds to the time just before drizzle formation.
14 In the CON simulation, LWC increases with height but decreases at cloud top because of
15 mixing with the dry and warm air above.

16 It is seen that in some parcels LWC exceeds $1g\ m^{-3}$. The cloud is continuous in the horizontal
17 direction, and mixing leads to a clear cloud base at ~ 400 m. The velocity field is also
18 presented in Fig. 1, it can be seen that in areas of updraft cloud thickness is larger. Vertical
19 velocity reaches $1.5\ m\ s^{-1}$ in updraft areas ($x=1100$ m) and $-1.5\ m\ s^{-1}$ in downdraft areas
20 ($x=500$ m). In the study by Magaritz-Ronen et al. (2014) the spatial correlation length for
21 several microphysical properties was calculated and found to be on the order of a few hundred
22 meters. This value agrees with the correlation length calculated from observations for the
23 same case.

24 In the NoMI case, the LWC field is highly inhomogeneous throughout the cloud, indicating a
25 smaller radius of correlation on the order of the linear size of one parcel. Substantial
26 inhomogeneity is also seen near cloud base, indicating a high variability in the LCL of
27 separate parcels. One can see that in CON cloud is thicker than in NoMI, with higher cloud
28 top and lower cloud base. This difference is the result of turbulent mixing between parcels.

29 Figure 2 compares the profiles of LWC, concentration, temperature and total humidity (q_t) in
30 the model and observations. On average the profiles are in close agreement with observations.

1 The inversion is well preserved for single time step and cloud and BL properties are simulated
2 correctly. Total humidity (q_t) and temperature increase in the model in a layer that is thicker
3 than seen in observations between cloud top and the inversion. As mentioned, changes in the
4 cloud top gradient are caused by turbulence-induced mixing. Supplemental simulations
5 indicate that minor underestimation of temperature and humidity gradient above the cloud
6 layer does not change the description of the physical mechanism of drizzle formation. Sharper
7 temperature and q_t gradients can be achieved in the model by using a sharper gradient of
8 dissipation rate just above cloud top. Our choice of linear profile is based on the formation of
9 a realistic mixing (Paluch) diagram. Note that smoother transition between cloud layer and
10 inversion is often observed in Sc, including during the DYCOMS-II field experiment (for
11 instance, RF03).

12 **4.2 Initiation of drizzle - lucky parcels**

13 Fig. 3 shows the evolution of the median profile of the effective radius (r_e) in two
14 simulations, CON (top) and NoMI (bottom). Only parcels with $LWC > 0.01 \text{ g/m}^3$ were used
15 for the calculation of the median. In CON, large values of r_e are first seen near cloud top at
16 ~ 120 min. The median of the effective radius increases in the lower levels of the cloud in the
17 following time steps. The development of the median r_e is seen throughout the cloud as large
18 drops first form near cloud top and then initiate the formation of larger droplets in the rest of
19 the cloud. After 300 minutes, large values of r_e below cloud base indicate the presence of
20 drizzle in the BL. Drizzle formation begins when r_e at cloud top reaches $\sim 11\text{-}12 \text{ }\mu\text{m}$. This
21 value corresponds with measurements (VanZanten et al., 2005).

22 Examination of profiles of the median r_e at individual time steps in the CON case reveals
23 another effect of turbulent mixing. The effective radius does not increase monotonically in the
24 cloud and larger values of r_e can be seen close to cloud base (for example $t = 100\text{-}130$ min).
25 These larger values are not evident in the NoMI case and are a result of turbulent mixing. One
26 of the mechanisms able to lead to larger r_e near cloud base is lateral mixing between
27 descending volumes containing droplets of larger sizes with ascending volumes containing
28 smaller droplets (Korolev et al., 2013; Pinsky et al., 2013). Effects of turbulent mixing inside
29 the cloud on drizzle formation are further described in section 4.5 and in the discussion,
30 below.

1 The evolution of the r_e median profile in the NoMI case is presented in Fig. 3 (bottom panel).
2 In the NoMI case the change in the r_e profile throughout the simulation is quite different.
3 Parcels in this simulation are almost adiabatic; they do not mix with each other and are
4 affected only by sedimentation of the largest droplets. Microphysical properties of each parcel
5 in this case are determined by its initial conditions and trajectory in the BL. Using the LWC
6 as a limit for the calculation of the median, dry parcels penetrated from the inversion layer
7 (Fig. 1) are excluded from consideration. The profile from NoMI resembles the profile
8 expected from an ascending adiabatic parcel where the effective radius is determined
9 primarily by the distance above the LCL. In the NoMI case, cloud base is on average higher
10 than in CON, and maximum values of r_e in NoMI do not exceed $10\mu\text{m}$, indicating that large
11 drops and drizzle do not form in this case.

12 Larger values of r_e in the CON case are also a result of increasing cloud depth in the
13 simulation. During the simulation, surface fluxes lead to an increase in humidity in the
14 subcloud layer and a lower cloud base height. In addition cloud top height increases during
15 the CON simulation. This is a classic manifestation of the entrainment process (Garratt,
16 1992). These two processes increase cloud depth and result in larger r_e near cloud top. We
17 refer to parcels in which large droplets first form as ‘lucky’ parcels and seek to formulate the
18 conditions leading to their formation.

19 Several studies have shown that for the formation of large droplets in the DSD, efficient
20 collisions are crucial (Pinsky and Khain, 2002; Khain et al., 2013). The rate of collisions can
21 be characterized by the product of the square of droplet concentration and collision kernel.
22 This product represents the gain integral in the stochastic equation of collisions (Pruppacher
23 and Klett, 1997). Evaluations of the collision kernel conducted by Freud and Rosenfeld
24 (2012) found that the kernel is proportional to r_e^5 . Accordingly, for a given DSD the collision
25 rate can be characterized by a collision parameter in the form of $N^2 r_e^5$. Figure 4 describes the
26 dependence of the collision parameter on LWC. Each parcel during 200-220 min of the
27 simulation is represented by a dot on the diagram; colors denote the height of the parcel.
28 There is clear dependence between the two parameters and as LWC increases so do the
29 collisions in the parcel. An increase is also seen as the height of the parcel in the cloud
30 increases. This is expected, given the strong LWC-height correlation. According to results
31 presented in Fig. 4, as LWC increases the probability of the formation of large drops
32 increases. The importance of maximum LWC values in the formation of drizzle was also

1 stressed by Khairoudinov and Kogan (2000) and Magaritz et al (Magaritz et al., 2009) and is
2 the first characteristic of a ‘lucky’ parcel.

3 Figure 5 illustrates the mechanism of formation of parcels with maximum values of
4 LWC. This figure shows the field of humidity at $t = 150$ min (top panel). The dry inversion
5 and the well-mixed BL are clearly seen. Moisture flux from the ocean surface lead to an
6 increase in humidity in parcels located at the lower levels of the domain. These high humidity
7 areas expand upwards towards the cloud in updrafts related to large eddies (convective cells,
8 rolls). Large eddies are a typical feature of marine boundary layers (Stevens et al., 2003b,
9 2005; Ginis et al., 2004) and are reflected in the velocity field of the model. The updraft
10 velocities in such cells can exceed $2m s^{-1}$ and the width of the updraft can be as large as a
11 few hundred meters.

12 A previous study (Magaritz-Ronen et al., 2014) found that with turbulent mixing the lifetime
13 of a single 40 m parcel is on the order of $\sim 15-20$ min. The lifetime of a parcel is defined here
14 as the time it takes for a parcel to mix with its environment and conservative properties of the
15 parcel become similar to those in its surrounding. During this time period the parcel can be
16 distinguished from surrounding parcels, and can be tracked and analyzed. But gradual
17 changes occur during its lifetime. Examination of a conservative value such as total water
18 content (q_t) enables us to evaluate the extent to which an air volume mixes with its
19 neighboring parcels. The middle panel in Fig. 5 presents the ratio between $q_t(150min)$ to
20 $q_t(140min)$ for all parcels in the model. Parcel locations in the figure are according to their
21 location at $t = 150min$. Parcels mix with their environment at different rates, as a function of
22 the gradient between the parcel and its immediate environment. For some of the parcels near
23 the surface q_t increases during this period. The ascending branch of humidity, as identified in
24 the top panel, is wider than a single parcel, allowing the parcels in the center of the branch to
25 lose less q_t than adjacent parcels. During their ascent (here of 10 min), parcels may lose up to
26 10% of q_t . These ascending parcels also have a lower lifting condensation level (LCL)
27 (bottom panel). Parcels with high q_t will later have a high LWC in the cloud. The trajectory
28 of a single parcel between 140-150 min is marked in black in the middle panel. The trajectory
29 of the same parcel between 150-160 min is marked in gray. After a rapid ascent, the selected
30 parcel moves along the cloud top. As emphasized in the following sections this is the
31 preferred trajectory for a ‘lucky’ parcel forming the first large drops in the cloud.

1 The process of lucky parcel formation is further illustrated in Fig. 6a. All parcels located at
2 the bottom of the domain, near sea surface at $t = 145$ min, were selected. These parcels have
3 varying humidity values, depending on flux from the ocean surface and the history of the
4 parcel. This is the x- axis of the plot. The y-axis is the LWC marked at 5-min increments. The
5 colors denote the height of the parcel. After 5 min, small values of LWC are seen in some
6 parcels. The LCL of these parcels is about ~ 300 m, although the cloud base has an average
7 height of ~ 400 m. These parcels have maximum values of humidity. Parcels of this type are
8 similar to the one marked in Fig. 5. After another 5 min, more parcels ascend and the ones
9 reaching 600m have largest LWC. Parcels with the highest initial humidity will have the
10 highest LWC as well. This trend also continues for a further 5 min. As expected, a strong
11 dependence on the height of the parcel is evident in the scatter. In the last panel, after 20 min
12 of simulation, the clear slope disappears and the LWC is determined mostly by the height of
13 the parcel in the boundary layer. Only parcels with maximum values of LWC are shown in
14 panel *b*. In the figure it is shown that even with the strong dependence on the height of the
15 parcel, parcels with maximum LWC at cloud top have maximal initial humidity values. The
16 mechanism described can be summarized as follows. In adiabatic (or close to adiabatic)
17 parcels LWC increases inside the cloud as adiabatic LWC. For maximum LWC values at
18 cloud top, the LCL should be minimal for such a parcel. The low LCL is determined by high
19 RH in the parcel. Such high RH can be obtained from the ocean surface.

20 Figure 7 presents the evolution of microphysical parameters of a single parcel. This
21 parcel, which is marked in Fig. 6a by black circles in all panels, ascends from cloud base to
22 800m in 13 min (panel *b*). The effective radius in the parcel increases to $12\mu\text{m}$ during this
23 time. The formation of drizzle-sized drops (droplets with radius exceeding $25 - 30\mu\text{m}$)
24 substantially accelerates at $t=160$ min, when $r_e = 11\mu\text{m}$ and LWC reaches 1g m^{-3} . In the
25 DSD (panel *b*) an elongated tail of largest droplets is formed. Towards $t = 166$ min, the parcel
26 contains drizzle droplets with radii as large as $40\mu\text{m}$ (Fig. 7b). A tail of large drops was also
27 reported in observations (VanZanten et al., 2005). The concentration of these drops remains
28 small and does not increase r_e significantly. The peak of the DSD appears at $r \approx 11 - 12\mu\text{m}$.
29 After the time steps shown in the figure, large droplets are lost from the DSD by
30 sedimentation.

31 In Fig. 8 we examine only those parcels that reach a value of LWC greater than 0.8g/m^3 .
32 Along the x-axis, the time each parcel retained the high LWC value is plotted. The maximum

1 collision parameter value during this period is shown along the y-axis in the diagram. The
2 color denotes the maximum value of LWC during the same time period. As the length of time
3 the parcel has high LWC increases, the collision rate in the parcel increases as well. However,
4 after the parcel has a residence time of more than 10-12 min with high LWC, the collision
5 parameter no longer increases. Sedimentation of the larger drops forming in the parcel
6 reduces the LWC and collision parameter. Not all parcels can retain the high LWC and
7 intense collisions for the duration presented in Fig. 8. For this to occur a parcel needs to first
8 be located near cloud top, where LWC is maximal, but not too close to the inversion layer,
9 where mixing with dry air may lead to loss of LWC.

10 **4.3 Interaction between cloud top and inversion**

11 The first large droplets form near cloud top, where mixing with dry environment is most
12 pronounced. Inhomogeneous mixing is often suggested as a mechanism leading to increase in
13 the maximum drop size in ascending cloud volumes mixing with the environmental in
14 cumulus clouds (Baker et al., 1980; Baker and Latham, 1982; Lasher-Trapp et al., 2005;
15 Cooper et al., 2013), it is therefore of interest to investigate the possibility that turbulent
16 mixing at cloud top of Sc may accelerate the formation of these droplets.

17 Fig. 9 shows a scatter diagram of droplet concentration and LWC (LWC-N). Each point in the
18 diagram marks a single parcel at $t = 185$ min. Colors denote the height of the parcels. Parcels
19 in the diagram can be separated into three zones. In zone 1 air parcels are close to adiabatic,
20 as indicated by the high droplet concentration. Parcels in this zone are ascending in the cloud
21 and droplets grow by diffusional growth. Droplet concentration in the parcels remains nearly
22 the same, but LWC increases with height. In zone 2 cloud parcels are located near cloud top
23 for longer periods of time. Turbulent mixing of these parcels with parcels from the inversion
24 layer leads to a decrease in droplet concentration and LWC. However, LWC decreases more
25 substantially than concentration, indicating partial evaporation of droplets in the DSD and
26 penetration of small droplets from neighboring initially dry parcels. The decrease in droplet
27 concentration is only on the order of 10%. In zone 3 the slope of the relationship changes. In
28 this zone parcels initially from the inversion layer become cloud parcels, due to mixing with
29 adjacent cloud parcels. Both droplet concentration and LWC in these parcels are smaller than
30 in the initially adiabatic cloud parcels. Since LWC and concentration are initially zero in these
31 parcels, every droplet that enters the parcel and does not evaporate completely increases these
32 values substantially, leading to the larger slope of data points in zone 3. Changes in droplet

1 concentration also lead to changes in the DSD spectrum width, which is demonstrated in Fig.
2 10.

3 Figure 10 compares DSD widths (standard deviation of the distribution) as a function of LWC
4 in simulations with (CON, panels *a, c*) and without mixing (NoMI, panels *b, d*). In the CON
5 case the spectrum width values are higher than in the NoMI case. In CON, DSD width is
6 maximal in zone 2, where mixing leads to the formation of small droplets and broadening of
7 DSD. These parcels correspond to the parcels in zone 2 in Fig. 9, where the decrease in LWC
8 is seen to be greater than the concentration. As mentioned above, partial evaporation of
9 droplets in these parcels is the principal process leading to broadening of DSD toward smaller
10 drops and increasing spectrum width. While spectrum width is greatest in parcels at cloud top,
11 the strongest collisions are in the most adiabatic parcels with the largest LWC (zone 1). These
12 parcels may have lower DSD width, because they contain fewer small droplets. In parcels that
13 interact with the inversion air, mixing with dry environmental air increases spectrum width
14 towards smaller drops and decreases the rate of collisions. If sufficiently large drops formed
15 in the parcel before it mixed with the dry inversion air, collisions can still be efficient and
16 drizzle-size drops may form.

17 In adiabatic parcels, the spectrum width is determined by a combination of the initial
18 spectrum at cloud base and the path of the parcel in the cloud. The initial DSD is a function of
19 the supersaturation at the LCL and the aerosol distribution. Further ascent of the parcel is
20 accompanied by diffusion growth and, if conditions permit, the beginning of collisions and
21 widening of the DSD towards large drops. Variability of spectrum width values increases
22 when the parcels are not adiabatic (Fig. 10). In the case of turbulent mixing, the width of an
23 individual spectrum is not a direct result of the parcel's history but also of the history of
24 adjacent parcels. These wider DSD may expedite drizzle formation in the cloud. But in
25 general, we see that the DSD width is not the main factor that fosters intense collisions and in
26 our case first drizzle drops. Diffusion growth leads to DSD narrowing in the space of drop
27 radius, in the space of r^2 DSDs are shifted to large sizes without change in the shape of the
28 distribution. Since relative velocities between droplets are proportional to r^2 , diffusion
29 growth leads to increase in the collision kernel and collision rate despite DSD narrowing in
30 the radii space. The main conclusion from this analysis is that maximum drop size are reached
31 in parcels close to adiabatic, but not in parcels with wide DSD formed under effects of
32 mixing.

1 It is interesting to note that in addition to a higher collision parameter, LWC maximum
2 values are greater in the CON case than in the NoMI case as well. These higher LWC values
3 indicate a deeper cloud. During the simulation, sensible and latent heat fluxes from the
4 surface increase the humidity in the boundary layer and lead to a decrease in cloud base
5 height as was mentioned above. These changes result in an increase of the LWC max near
6 cloud top.

7 Conclusions inferred from the previous figures regarding the shape of the DSD are
8 supported by Fig. 11, where DSDs at 100m layers near cloud top are presented. The DSDs are
9 separated by LWC value and averaged in the horizontal direction. For all presented DSDs the
10 distribution peak is located at similar radii. The concentration of drops around $10\mu\text{m}$ increases
11 with the increase in the LWC at each height. In addition, DSDs with lower LWC have a
12 higher concentration of small droplets. DSDs in this figure all come from near cloud top and
13 the decrease in LWC, decrease in the larger drop concentration, and formation of smaller
14 droplets result from turbulent mixing with the dry inversion air. These DSDs correspond to
15 the parcels in zone 2, in figures 9 and 10. So, according to our results, mixing does not lead to
16 the formation of superadiabatic droplets that trigger collisions. On the contrary, droplets of
17 maximum size arise in parcels close to adiabatic (undiluted).

18 Note that mixing between parcels in the model is inhomogeneous, because it takes
19 significant time (15-20 min) for homogenization (according to homogeneous mixing
20 homogenization is instantaneous). At the same time mixing leads to DSD broadening. This
21 contrasts with the classical theory that assumes the shape of DSD unchangeable in case of
22 extreme inhomogeneous mixing. We attribute this difference to simplifying assumption of
23 about monodisperse DSD in the classical mixing concepts.

24 **4.4 The dual role of turbulent mixing in formation of drizzle**

25 In previous sections we discussed the properties of ‘lucky’ parcels where first drizzle is
26 formed. ‘Lucky’ parcels have high absolute humidity. They originate from near the surface
27 and reach the upper levels of the cloud quickly, not allowing sufficient time for mixing with
28 the surrounding air. In these parcels collisions lead to the formation of drizzle followed by
29 sedimentation of the largest drops.

30 In this section we wish to observe the effects of turbulent mixing on the formation of ‘lucky’
31 parcels as well as on the further development of drizzle in the cloud. Figure 12 present the

1 accumulated mass (left) and accumulated number (right) of drops larger than $20\mu\text{m}$ in all
2 parcels in the domain. Several different simulations are compared: the control (CON) and no
3 mixing (NoMI) cases and two simulations in which sedimentation is switched off in the
4 model, one for the CON case (NoSD) and one for the NoMI case (NoMISD).

5 Large droplets first form in cases where drop sedimentation is removed. In these simulations
6 drops become very large and grow by collisions to unrealistically large sizes, and yet they
7 provide insight into the process of first drizzle drop formation.

8 In the NoMISD case the mass increases faster and earlier in the simulation than in the NoSD
9 case. When the parcels are adiabatic, parcels initially located near the surface where humidity
10 is maximal will have the lowest LCL and maximum LWC. In the NoMISD these parcels
11 retain their extreme values of humidity and large drops form earlier. Inclusion of mixing
12 between the parcels leads to a reduction of maximum values, homogenization of the BL, and
13 a subsequent delay in the formation of large droplets (NoSd, left panel). From these results it
14 can be seen that the first large droplets will form in adiabatic parcels with initially high
15 humidity. The accumulated number of large drops (right) further supports this conclusion. In
16 NoMISD the number of large drops increases until ~ 150 min and then remains almost
17 constant. Following the formation of large droplets in parcels with appropriate conditions no
18 more parcels are able to reach these conditions. In contrast, the number of large drops in the
19 NoSD run continues to increase after 150 min of simulation. The absence of turbulent mixing
20 is the only difference between the two simulations and yet the changes in the mass and
21 number of larger drops are significant. Results indicate that the direct effect of mixing on
22 parcels with initially high humidity and low LCL is to retard the formation of large droplets.

23 When sedimentation is included in the simulations, after some drops become large enough
24 they may fall through the cloud. In the NoMI case large drops forming in a small number of
25 parcels sediment through the cloud and evaporate in other parcels, especially in dry and warm
26 parcels penetrated from the inversion (Fig. 1). As a result, the amount of large droplets that
27 form in the cloud remains very low and the mass of these large drops is negligible. This
28 evaporation process prevents the formation of drizzle at the surface in the NoMI case. In CON
29 simulation, when mixing is included, the cloud structure changes dramatically. As a result,
30 droplets falling from parcels close to adiabatic do not evaporate but grow by collisions within
31 the cloud. In this simulation drizzle develops and reaches the surface. After the initial
32 formation of large drops in the most humid parcels in the cloud, the number of large drops in

1 the CON case continues to increase, indicating that turbulent mixing facilitates the formation
2 of drizzle in the cloud.

3 In general, Fig. 12 shows the two main phases of drizzle formation in Stratocumulus clouds.
4 First, larger droplets form in the most adiabatic parcels in the cloud layer. Second, turbulent
5 mixing leads to further formation of more large droplets and drizzle-sized drops. In these two
6 phases turbulent mixing plays a contradicting role, delaying the first while enhancing the
7 second (see further detail in the discussion).

8 **4.5 Further drizzle development in the cloud**

9 In the cloud's latter stages of drizzle development, large drops forming in 'lucky' parcels
10 sediment through the cloud, leading to further development of drizzle. In Fig. 3 this process is
11 first seen as an increase of r_e throughout the cloud layer. The horizontally-averaged mass
12 distribution in the simulated cloud at the drizzle stage ($t = 360$ min) is shown in Fig. 13. At
13 this time drizzle drops reach the surface. Figure 13 shows that large drops form first at the top
14 (700-800m) and then sediment through the cloud. During their descent the drops grow and
15 their relative proportion in the mass distribution increases. As the droplets from cloud top
16 sediment through the cloud they act as drop collectors, growing in size through collisions and
17 coalescence. Near the surface (100-200m) there are only large drops in the distribution which
18 were large enough to reach these levels and not evaporate in the sub-cloud layer. The radius
19 of drizzle drops ranges from 40 μm to 350 μm , with a peak at 200 μm . These radii agree with
20 observations (Pinsky et al., 2008).

21 The dynamic structure of the BL and the presence of large eddies effect the continuation of
22 drizzle development in Sc clouds as well. They determine areas of updraft and downdraft and
23 are the controlling factor in the preferable trajectory of 'lucky' parcels. As larger drops form
24 along cloud top, droplets in parcels reaching areas of downdraft are more prone to
25 sedimentation. Drizzle does not develop in the entire cloud simultaneously so that areas of
26 more intense drizzle flux form. These areas coincide with downdraft areas in the cloud. Figure
27 14 presents the averaged rain flux near cloud base (450 m) throughout the simulation. Each
28 bar shows the drizzle flux separated into downdraft and updraft areas. It can be seen that most
29 of drizzle falls in these areas. Areas of enhanced drizzle were seen in observations of RF07 as
30 well (VanZanten et al., 2005).

1 In Fig. 14 it was shown that the mass and number concentration of larger drops increase when
2 turbulent mixing is taken into account – far beyond those seen with no mixing. In addition to
3 the inhibiting effect mixing has on the initiation of drizzle, turbulent mixing is needed for
4 continued drizzle development in the cloud.

5 Among possible mechanisms able to lead to this effect we first consider changes to the
6 aerosol size distribution. One of the specific features of the model used in this study is
7 accounting for the aerosol distribution in each parcel. In addition to accounting for aerosols
8 when the parcel is sub-saturated and all aerosols are in equilibrium with the environment, the
9 model tracks aerosols in the drops themselves. Aerosol size does not change during processes
10 of diffusion growth or evaporation, but in cases of collisions aerosol size grows and may
11 reach larger sizes than initially found in the BL. Figure 15 presents the development through
12 time of the maximum aerosol size in cloud parcels. The median profile of the maximum
13 aerosol size in each parcel for the CON (top) and NoMI (bottom) cases is presented.

14 First, it is clear that the changes in the maximum aerosol size are very different in the two
15 cases. In the NoMI case, largest aerosols are present at the beginning of the simulation. These
16 aerosols have an average size of $1.3\mu\text{m}$, corresponding to the largest aerosol in the input
17 spectrum. As the largest aerosols in the spectrum they will be in the largest drops in the DSD.
18 After about 150 min, aerosol size diminishes. In NoMI, sedimentation of the largest droplets
19 from parcels with the lowest LCL results in the largest aerosols in drier and warmer parcels.
20 These parcels do not have the conditions required for larger drop formation in the following
21 time steps. Because of the comparatively small number of parcels with appropriate initial
22 conditions, sedimentation of the largest drops renders the largest aerosols unavailable for
23 further collisions.

24 As seen in the previous section, initial conditions are a governing factor in the formation of
25 large drops when the parcels are adiabatic, and drop formation will be much more rapid
26 without mixing than in the case of mixing.

27 As the development of the cloud progresses in the CON case the maximum aerosol size
28 increases and reaches an average of more than $3\mu\text{m}$. When turbulent mixing is included
29 maximum values of humidity and LWC are reduced and initial droplets forming in the cloud
30 are somewhat smaller. These drops do not sediment to the surface, but evaporate in the sub-
31 cloud layer. The aerosols can now be advected back into the cloud in ascending branches of
32 large eddies. As aerosols recirculate in the BL, their size increases when they are inside

1 droplets growing by collisions and coalescence. The mechanism for aerosols size increase is
2 presented in a study by Magaritz et al. (2010) showing that the evolution of large drops in Sc
3 leads to a corresponding increase in the aerosol size distribution as a result of collisions inside
4 the cloud.

5 Mixing between parcels gives rise to the recirculation of aerosols in the cloud. Collisions lead
6 to the formation of increasingly large droplets and aerosols during the recirculation. As a
7 result, the maximum size of aerosols at cloud base increases which fosters the formation of
8 larger droplets at cloud base (large haze particles) and above in ascending parcels. We believe
9 that the droplets formed on the largest aerosols contribute to the formation of the tail of
10 largest droplets in lucky parcels shown in Fig. 7b. After initiation of drizzle in the cloud,
11 enhanced collisions and formation of drizzle leads to a rapid increase in aerosol size as clearly
12 shown in Fig. 15. Larger aerosols continue to circulate in the BL, fostering further drizzle
13 formation at the drizzle stage of cloud evolution.

14 Spectral broadening and formation of the largest droplets in Sc due to turbulent mixing during
15 vertical recycling of cloud air is discussed in a study by Korolev et al. (Korolev et al., 2013).
16 In that study it is suggested that mixing of the DSD of parcels ascending and descending in
17 the cloud should lead to the presence of larger droplets in the ascending branch of the cloud
18 near cloud base and result in more efficient collisions as the parcel ascends. The results seen
19 in fig. 15 can also foster formation of larger droplets in ascending parcels, during the course
20 of diffusion growth and collisions. In combination with the increased spectral width seen in
21 Fig. 10 and the increase in the median profile of r_e near cloud base that is shown in Fig. 3 we
22 believe that lateral mixing near cloud base and inside the cloud layer can have a strong effect
23 on the drizzle formation process in Sc.

24

25 **5 Conclusions**

26 The process of drizzle formation in stratocumulus clouds is investigated using LEM, with an
27 accurate description of microphysical processes. The new version of the model includes
28 process of mixing between parcels and surface flux of heat and moisture. Lightly drizzling
29 stratocumulus clouds observed during flight RF07 of the DYCOMS-II field campaign were
30 successfully simulated.

1 Clouds observed in flight RF07 were simulated by an earlier version of LEM, where there
2 was no mixing between parcels and no inversion layer above cloud top (Magaritz et al.,
3 2009). In that study the hypothesis that first drizzle forms in a small number of air volumes
4 near cloud top in which LWC is maximal was expressed and justified. The consideration of a
5 more realistic geometry of the STBL with an inversion layer required the implementation of
6 turbulent mixing between the Lagrangian parcels. The question arose, whether the hypothesis
7 of ‘lucky’ parcels can also be justified under conditions of mixing. Results of the present
8 study show that the hypothesis of ‘lucky parcels’ remains valid also when turbulent mixing is
9 taken into account.

10 It was further shown that mixing creates a realistic structure of stratocumulus clouds but does
11 not prevent the appearance of nearly adiabatic LWC values at cloud top. Among these air
12 volumes in the cloud ‘lucky’ parcels are the most humid and have the highest LWC and the
13 most intense collisions.

14 It is shown that without mixing taken into account drizzle cannot form in stratocumulus
15 clouds. Maximum LWC values are not as high and large drops can form only in a smaller
16 portion of the parcels that reach cloud-top. Effective radius in the cloud is lower and its linear
17 profile remains nearly constant throughout the lifetime of the cloud.

18 In conclusion, turbulent mixing plays a dual role in the process of drizzle formation. On the
19 one hand, the formation of the first large drops in Sc is an adiabatic process in which turbulent
20 mixing is an inhibiting factor. It reduces maximal values of humidity and delays the formation
21 of the first drops. On the other hand, turbulent mixing leads to the creation of generally
22 favorable background conditions and increased aerosol size within clouds, allowing drizzle
23 growth and development during drop sedimentation. In addition, mixing leads to an increase
24 in the drop size (haze size) at cloud base leading to faster formation of largest drops in the
25 ascending nearly adiabatic cloud volumes.

26

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1

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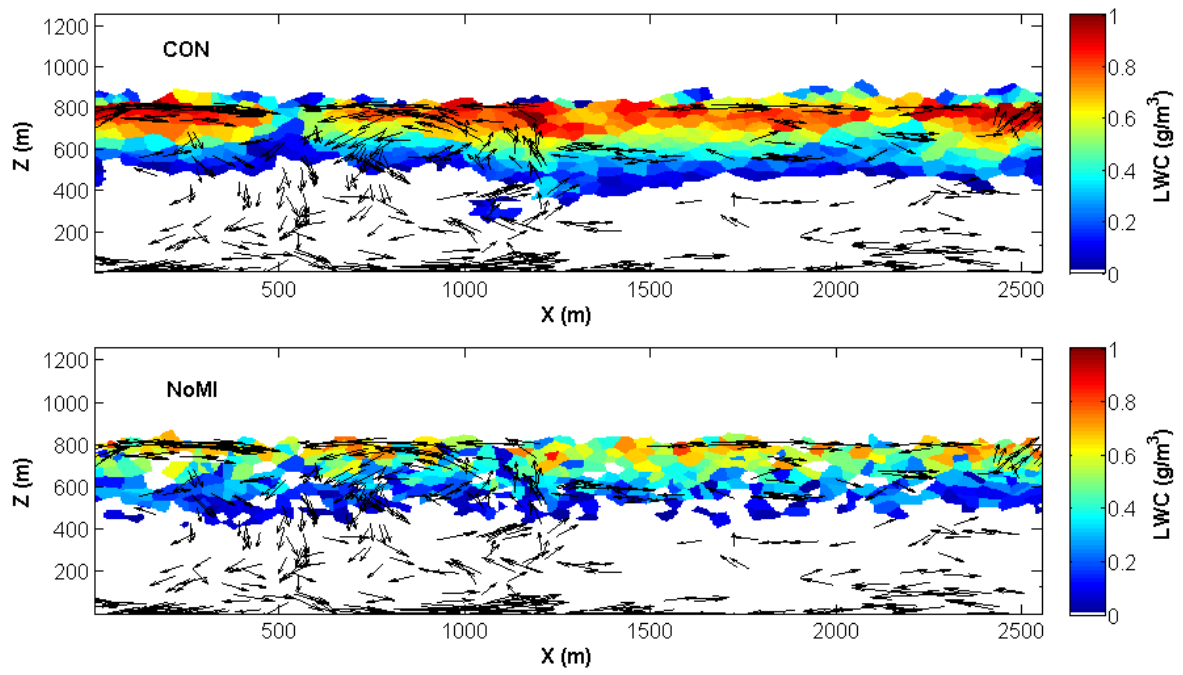
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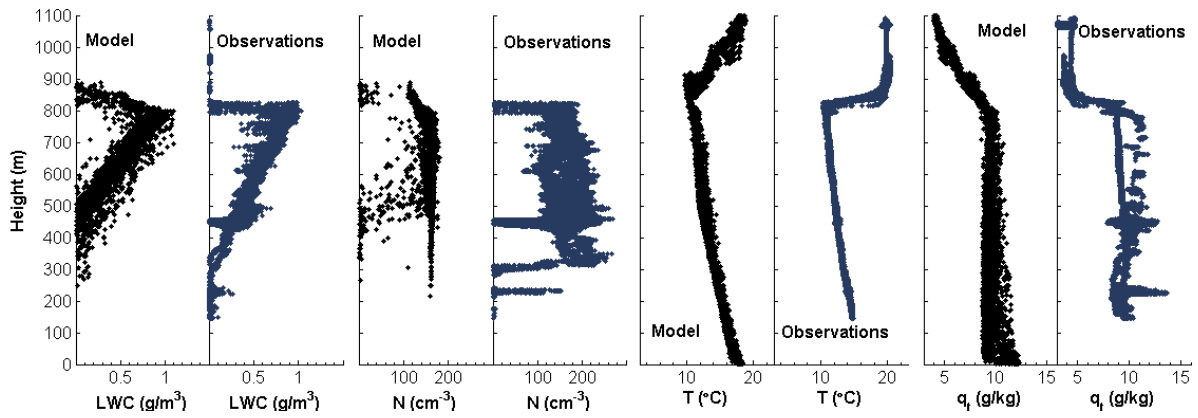
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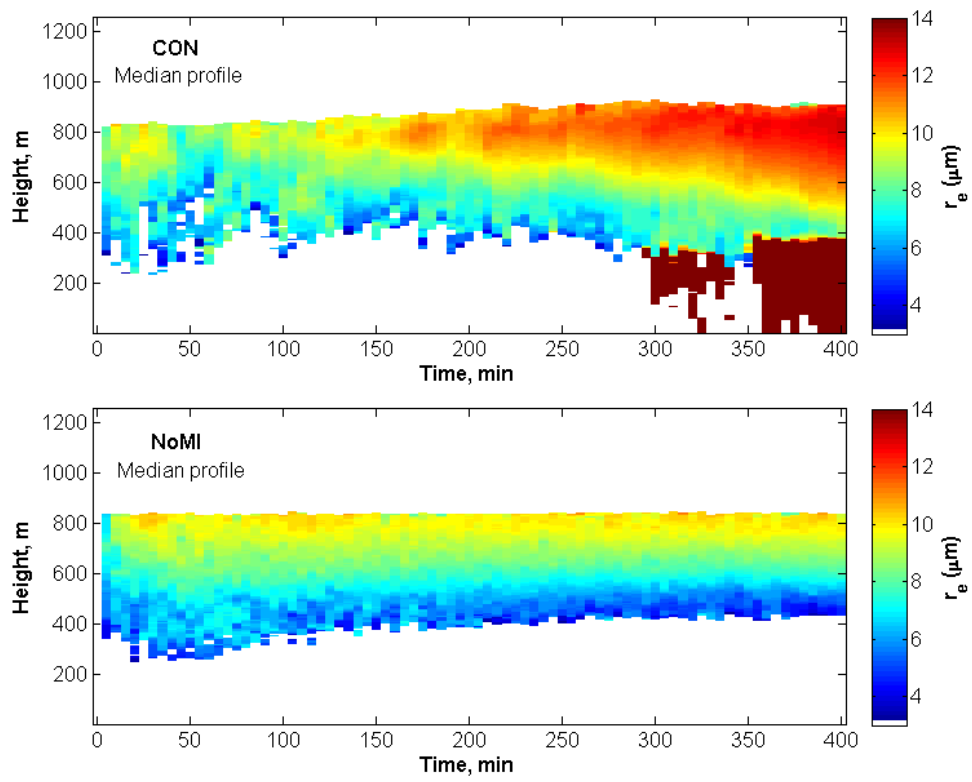
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2 **Figure 1.** Fields of LWC in the CON and NoMI simulations plotted at $t = 270$ min. The
3 velocity field at the same time step is presented as well



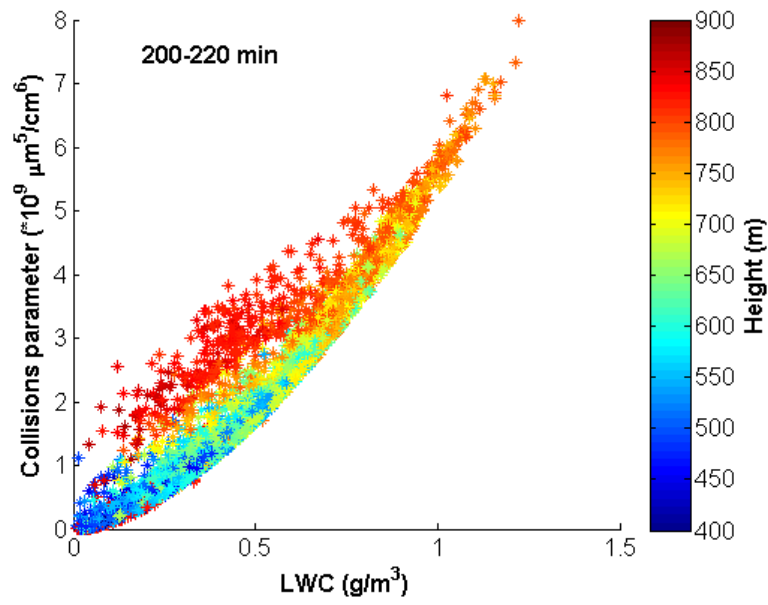
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 2 **Figure 2.** Profiles of LWC, droplet concentration (N), Temperature (T) and total water mixing
 3 ratio (q_t) from the model simulation and observations. From the model all parcels from three
 4 time steps between 270-280 min are presented. All observations between 0845-1135 UTC are
 5 presented.

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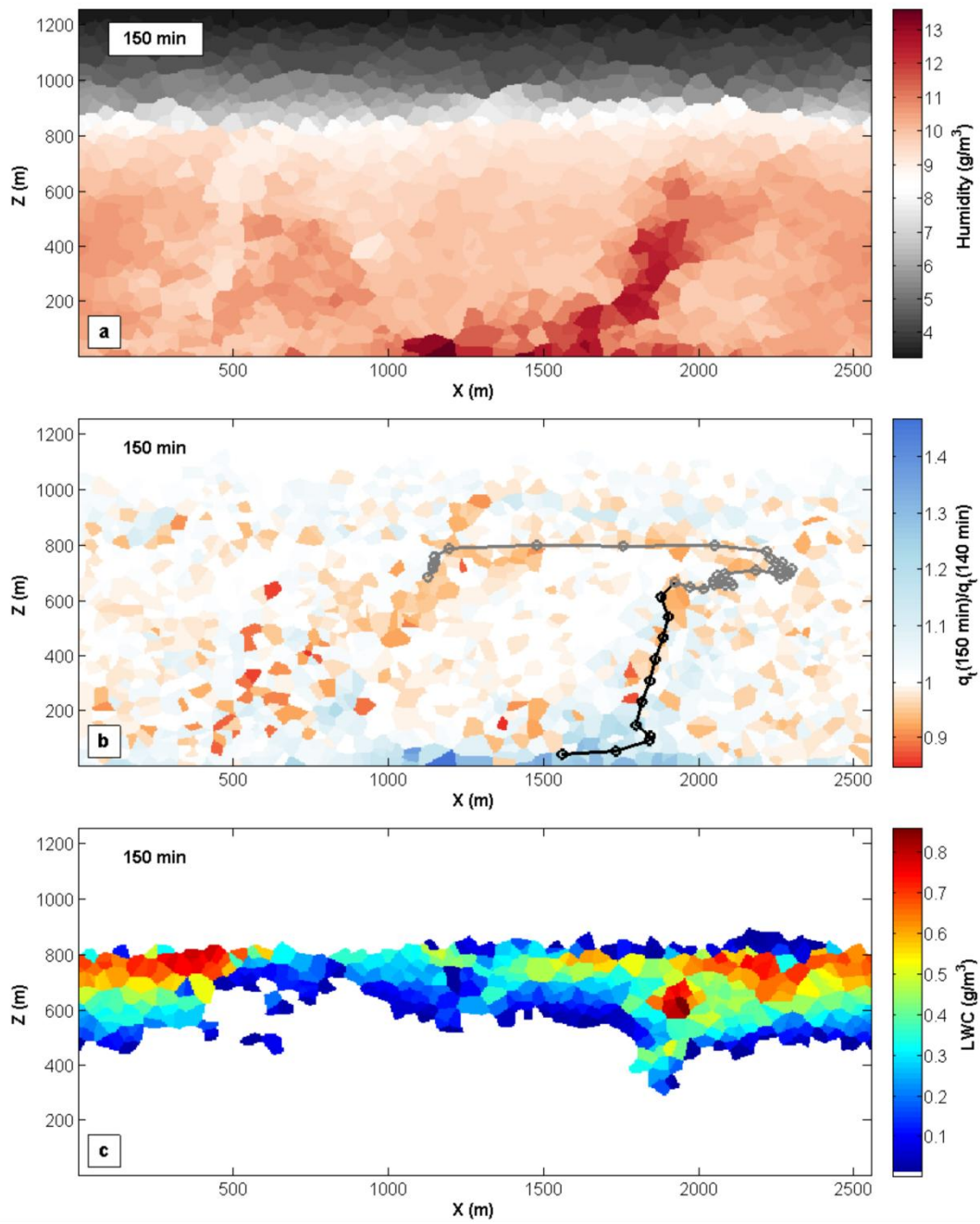
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3 **Figure 3.** Changes in the effective radius median profile in the CON (top) and NoMI (bottom)
4 simulations.



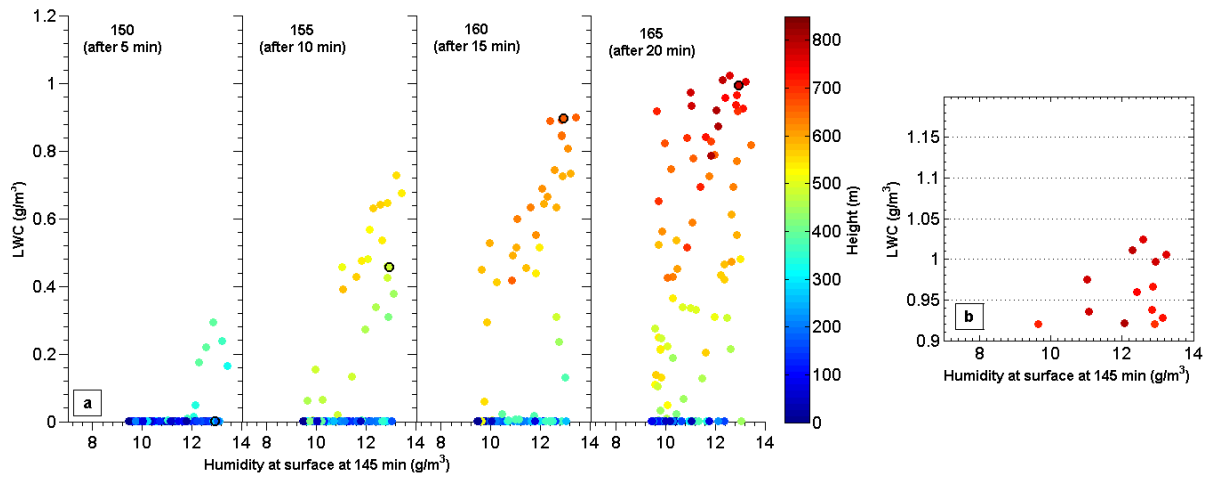
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2 **Figure 4.** LWC – collision parameter scatter plot for all cloud parcels at 200-220 min of
3 simulation in the CON case. Color denotes the height of the parcel.

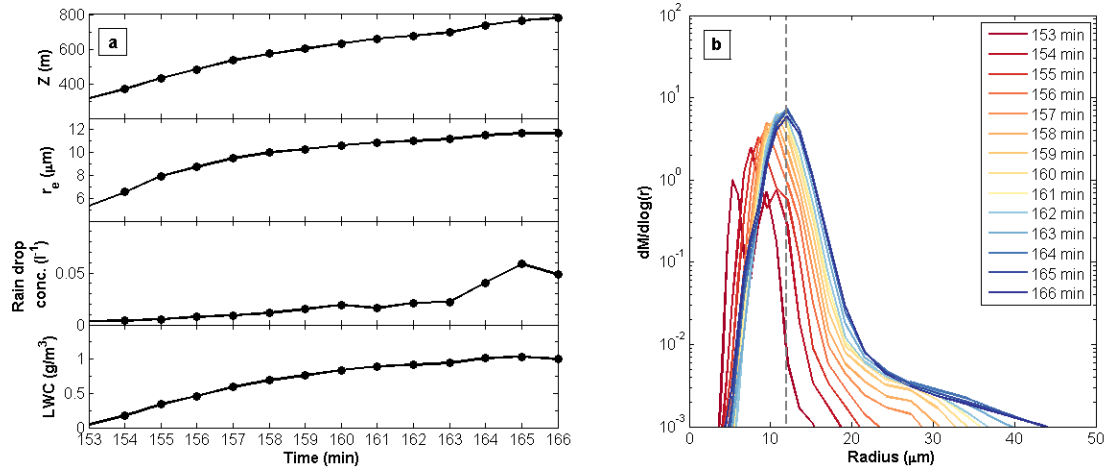


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 2 **Figure 5.** Fields of different parameters plotted at $t = 150$ min. (a) humidity (b) ratio of total
 3 water mixing ratio: $q_t(150 \text{ min})/q_t(140 \text{ min})$ (c) LWC.

4

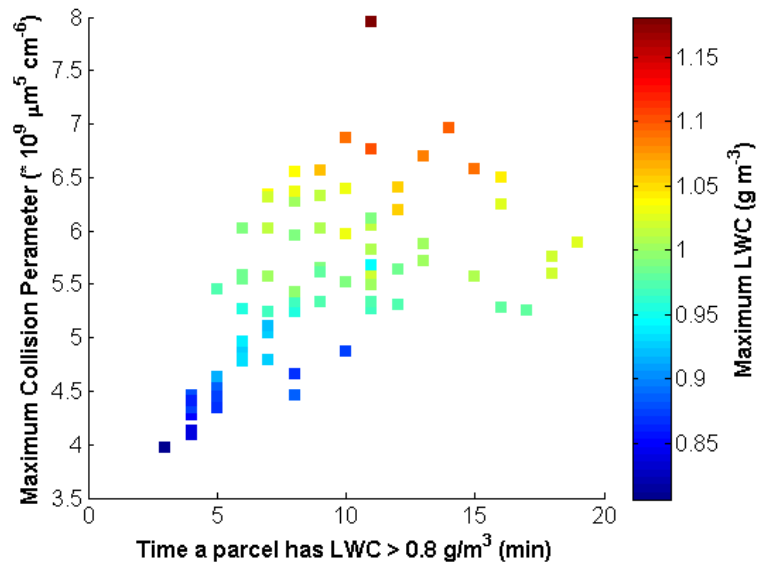


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 2 **Figure 6.** (a) LWC as a function of humidity at the surface at 5 min intervals, starting at 145
 3 min of simulation in the CON case. A single selected parcel used in Fig. 8 is marked in black
 4 in all panels. (b) Magnification of the top part of the last panel in (a).

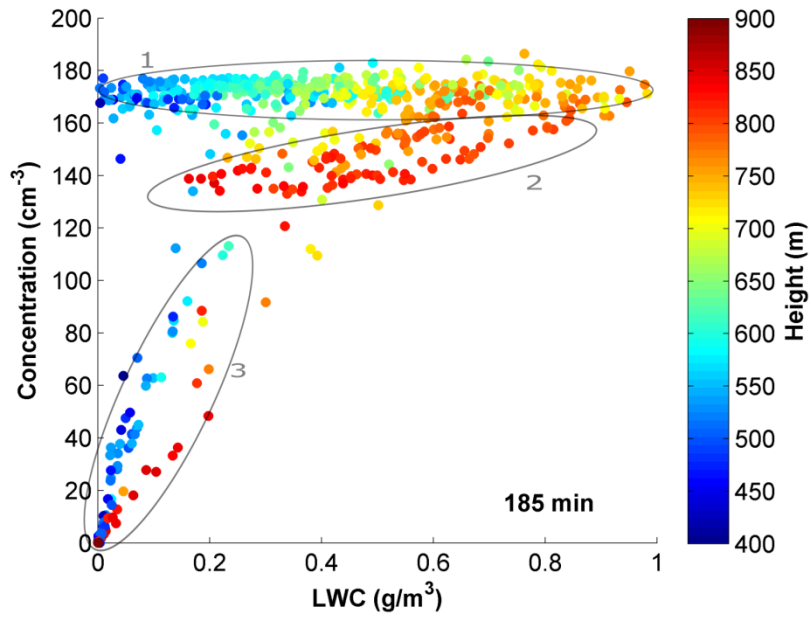


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2 **Figure 7.** History of a single parcel marked in Fig. 6. (a) Change in the height, effective
 3 radius, rain drop concentration and LWC of the parcel. (b) Changes in the mass distribution of
 4 the parcel.

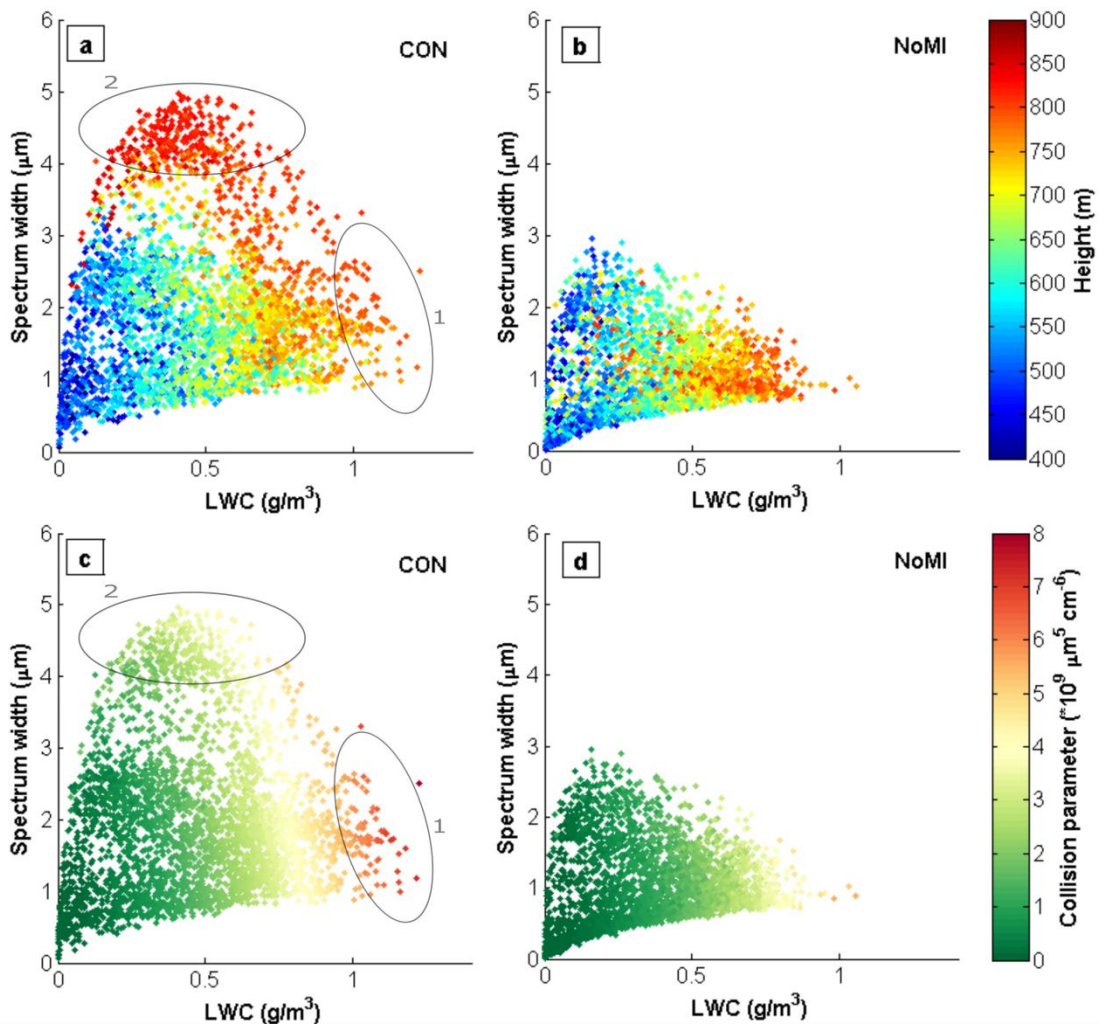


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- 2 **Figure 8.** Maximum collision parameter as a function of the accumulated time a parcel has
- 3 $\text{LWC} > 0.8 \text{ g/m}^3$. Colors denote the maximum value of LWC during the same time period.



1

2 **Figure 9.** LWC-N scatter plot at $t = 185$ min. Colors denote the height of the parcel.

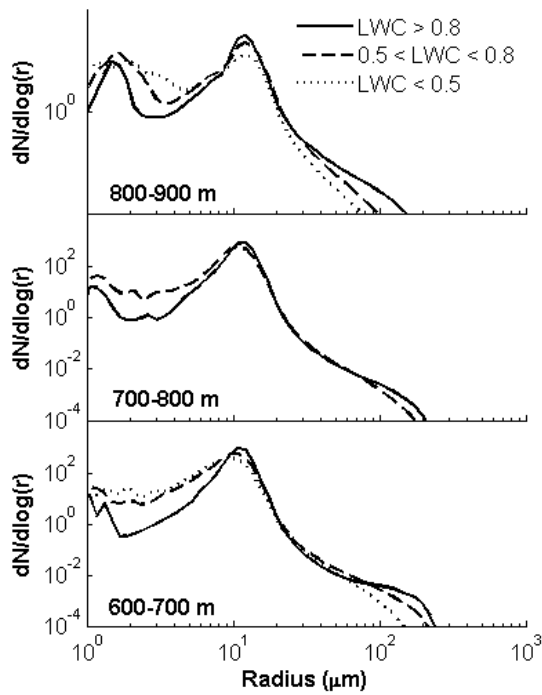


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2 **Figure 10.** LWC-spectrum width scatter diagrams for the CON (left) and NoMI (right) cases.

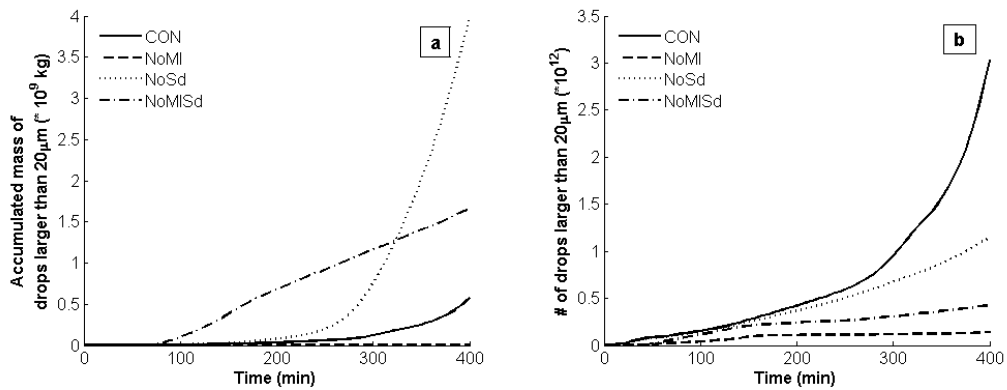
3 Each dot represents a parcel during 195-220 min of simulation. In the top row (a, b) colors

4 denote the height of the parcel. In the bottom row (c, d) colors denote the collision parameter.

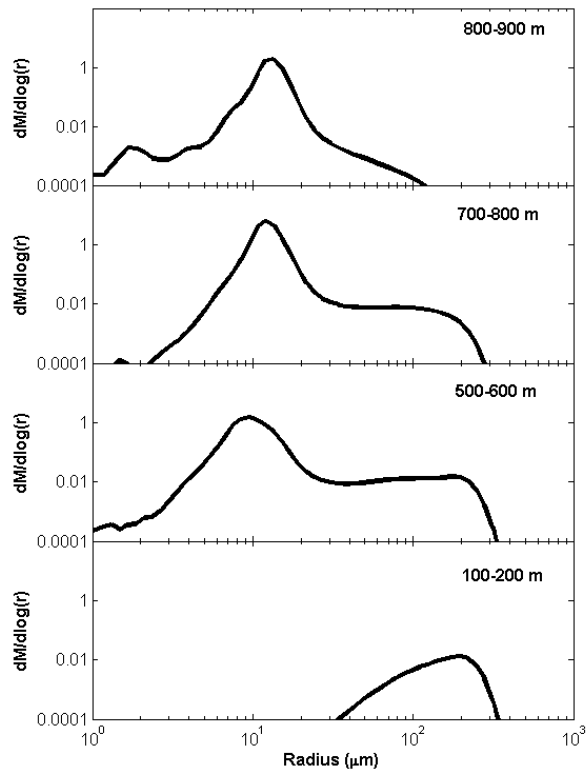


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 2 **Figure 11.** Averaged DSD at three layers near cloud top. At each level DSD is averaged
 3 according to LWC value.

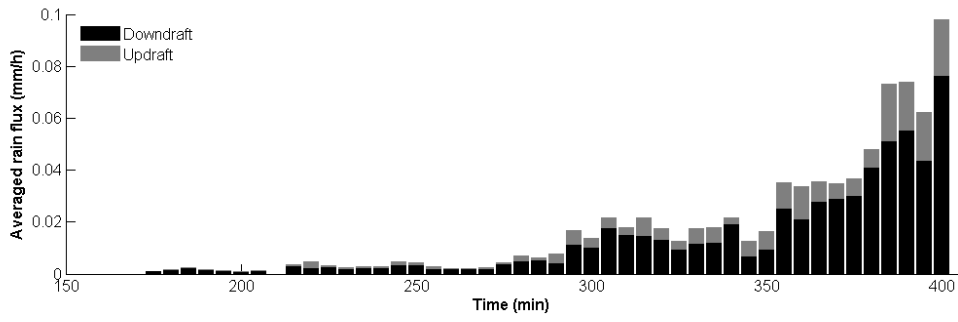
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6
 7 **Figure 12.** Accumulated mass (a) and concentration (b) of drops larger than $20\mu\text{m}$. Four
 8 simulations are presented: control (CON), no-mixing (NoMI), control and no sedimentation
 9 (NoSd) and no-mixing and no sedimentation (NoMISd).



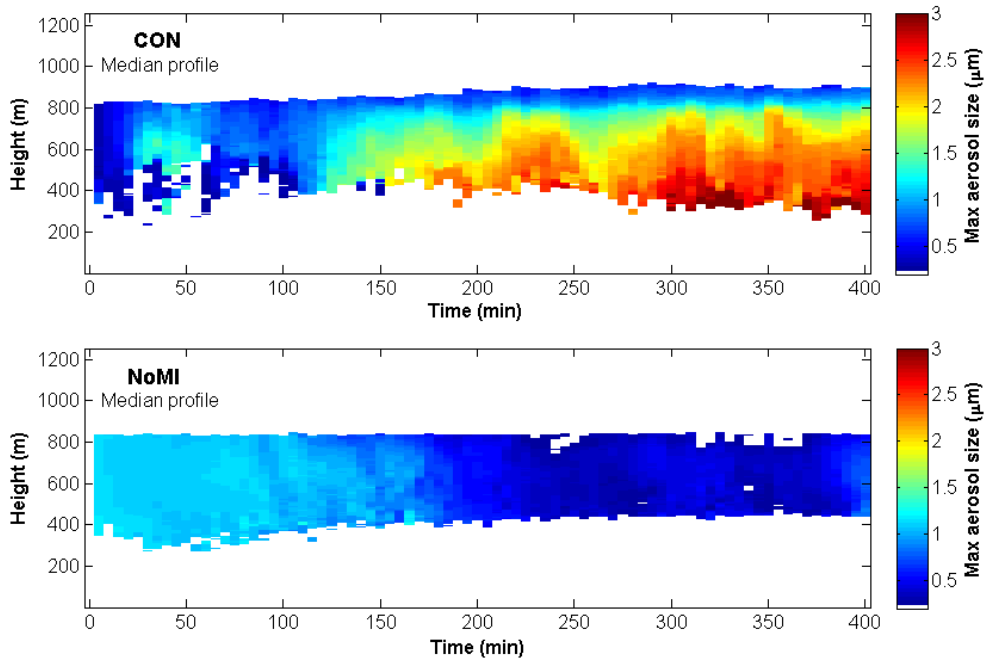
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 2 **Figure 13.** Averaged mass distribution for 100m layers, plotted at $t = 360$ min in the CON
 3 simulation.



1

2 **Figure 14.** Averaged rain flux at 450 m near cloud base, separated into downdraft (black) and

3 updraft (gray) areas.



1

2 **Figure 15.** Change in the median profile of the maximum aerosol size in cloud parcels in the
3 CON (top) and NoMI (bottom) case.