



**Particle-dependent
parameterizations of
heterogeneous
freezing processes**

K. Diehl and S. K. Mitra

This discussion paper is/has been under review for the journal Atmospheric Chemistry and Physics (ACP). Please refer to the corresponding final paper in ACP if available.

New particle-dependent parameterizations of heterogeneous freezing processes: sensitivity studies of convective clouds with an air parcel model

K. Diehl and S. K. Mitra

Institute of Atmospheric Physics, University of Mainz, Germany

Received: 23 April 2015 – Accepted: 28 May 2015 – Published: 17 June 2015

Correspondence to: K. Diehl (kdiehl@uni-mainz.de)

Published by Copernicus Publications on behalf of the European Geosciences Union.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Abstract

Based on the outcome of laboratory results, new particle-dependent parameterizations of heterogeneous freezing were derived and used to improve and extend a two-dimensional spectral microphysics scheme. They include (1) a particle-type dependent parameterization of immersion freezing using the numbers of active sites per mass, (2) a particle-type and size-resolved parameterization of contact freezing, and (3) a particle-type dependent description of deposition freezing. The modified microphysical scheme was embedded in an adiabatic air parcel model with entrainment. Sensitivity studies were performed to simulate convective situations and the impact of ice nuclei concentrations and types on ice formation. As a central diagnostic parameter the ice water fraction IWF was selected which is the relation of the ice water content to the total water content. The following parameters were varied: initial aerosol particle number size distributions, types of ice nucleating particles, strength of convection, and the fractions of potential ice nucleating particles. Single and coupled freezing processes were investigated. The results show that immersion freezing seems to be the most efficient process and, in competition with contact freezing, the dominant process. Contact freezing is constrained by the collision kernel between supercooled drops and potential ice nucleating particles and becomes relevant at temperatures lower than -25°C . The importance of deposition freezing lies in secondary ice formation, i.e. small ice particles produced by deposition nucleation trigger the freezing of supercooled drops by collisions. Thus, a broader ice particle spectrum is generated than by immersion and contact freezing. Competition of contact and deposition freezing is negligible because of involved particle sizes. As already suggested in literature, mineral dust particles seem to be the most important ice nucleating particles. Biological particles are probably not involved in significant ice formation.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



1 Introduction

The importance of the ice phase in mixed-phase convective clouds is indisputable. The additional release of the latent heat of freezing enforces not only the strength of the convection; the presence of ice particles in the cloud also substantially modifies the dynamical structure and the amount of precipitation (e.g., Gilmore et al., 2004). Hence, studying the ice phase in convective mixed-phase clouds is highly relevant for the understanding of such clouds and their atmospheric impact. With the convective updraft water drops are transported into regions where the temperature is low enough to allow them to freeze. Homogeneous freezing (i.e., freezing that does not require the presence of ice nuclei) becomes efficient at temperatures below -35°C (Pruppacher and Klett, 2010). Thus, at warmer temperatures in the troposphere heterogeneous freezing (which involves ice nucleating particles) is the only process of ice initiation, potentially triggering secondary ice formation. Heterogeneous freezing significantly changes the availability of liquid water in the upper parts of the cloud since ice particles grow at the expense of liquid drops by the deposition of water vapor (Bergeron–Findeisen process) and by riming (i.e., collection of liquid water). Thus, the number of ice nucleating particles and their efficiency to initiate ice formation at temperatures above the level of homogeneous freezing determines the nature of convective clouds as it modifies cloud microphysical processes and cloud development (e.g., van den Heever et al., 2006; Ekman et al., 2007; Phillips et al., 2007; Lee et al., 2009).

For detailed investigations of cloud microphysical processes adiabatic parcel models with entrainment are often employed (e.g., Simmel et al., 2005; Leroy et al., 2006; Diehl et al., 2006, 2010; Ervens and Feingold, 2012). Air parcel models describe a rising bubble of air whose volume increases with height. Dry air is mixed with moist air into the parcel through entrainment. The advantage of parcel models is that they allow a detailed description of the cloud microphysical processes, usually achieved by the use of spectral bin-microphysical models that explicitly solve the microphysical equations (see Khain et al., 2000, for an overview).

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

of the model was improved in the way that now it contains all heterogeneous freezing processes (deposition, contact, coupled condensation/immersion). This allows to investigate the competition of the freezing modes to understand the importance of deposition freezing in comparison to immersion and contact freezing, in particular with respect to the updraft velocity of the air parcel. The effects of various ice nucleating particles were compared to each other, also considering the different freezing modes, to estimate their importance.

2 Model description

The impact of ice nucleating particles on mixed-phase convective clouds is investigated with a microphysical scheme embedded in an air parcel model. The previous version of Diehl et al. (2006) was further developed in the way that new parameterizations were added or existing ones were modified or completely replaced.

The model of Diehl et al. (2006) contains a two-dimensional spectral microphysics scheme which divides the hydrometeor spectra into size bins (Simmel and Wurzler, 2006). These describe the number and mass of the drops or ice particles within the corresponding size range. A fixed bin structure is used combining the wetted aerosol particles and the drops in one spectrum where the soluble and total mass of aerosol particles is explicitly considered in every bin. An initial dry aerosol particle number size distribution is given where the particles are internally mixed with variable insoluble and soluble fractions. After starting the rise of the air parcel, the particles grow into the droplet part of the spectrum by condensation. The size spectra are allowed to evolve freely, they are not constrained by an underlying distribution function.

Two-dimensional means here that the microphysics is not a function of the drop size only (one-dimensional case) but a function of both drop and aerosol particle size (Simmel and Wurzler, 2006). In the one-dimensional case, it is affected that equal sized drops contain only equal sized particles which affects that drops of the same sizes freeze at the same temperature (Diehl and Wurzler, 2004). However, in real clouds

collision/coalescence, impaction scavenging of particles by drops, contact freezing of supercooled drops, growth of ice particles by riming, and secondary ice formation., i.e. freezing of supercooled drops by collision with an ice germ.

Because of these explicit descriptions the microphysical scheme is a useful tool to study in detail the link between aerosol particles and the evolution of cloud properties. The incorporation into an air parcel model has the advantage that all changes in the microphysical evolution of the cloud can be attributed to microphysical processes. The model improvements presented in the next sections include the following:

1. an updated particle-type dependent description of immersion freezing which is now related to the mass of insoluble particles contained in drops,
2. a modified description of contact freezing which is not only dependent on particle type but also particle size-resolved,
3. a new particle-type dependent description of deposition freezing.

All parameterizations are directly based on previous and new laboratory measurements as described in the following sections.

2.1 Immersion freezing

The previous description of immersion freezing (Diehl and Wurzler, 2004) gave the freezing rate of pure water drops containing ice nucleating particles as function of the drop volume V_{drop} according to:

$$-\frac{dN_f}{dt} = N_{\text{liq}} B_{\text{imm}} V_{\text{drop}} \exp(-a_{1,\text{imm}} T) \frac{dT}{dt} \quad (1)$$

with N_f the number of frozen drops, N_{liq} the number of liquid drops, and the constants $a_{1,\text{imm}}$ and B_{imm} . This parameterization implicitly reflected the fact that larger drops contain more particles because of collision and coalescence of drops and impaction

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



scavenging of aerosol particles. The previous version was replaced by a new one which is coupled directly to the mass of insoluble particles in the drops. This is possible because of the sectional distribution of drops and particles into size classes (Diehl et al., 2006).

2.1.1 Parameterizations based on laboratory data

The experimental data used as basis for the parameterizations include the following ice nucleating particle types: bacteria, pollen, feldspar, illite, and kaolinite. The number of active sizes per unit mass n_m was measured in a number of laboratory experiments. Murray et al. (2011) investigated kaolinite KGa-1b, Atkinson et al. (2013) K-feldspar. Illite NX was studied by Broadley et al. (2012) and recently by Hiranuma et al. (2015). The latter publication summarized the results from seventeen experimental techniques. Wex et al. (2015) includes the results from seven experimental techniques using Snomax[®] as a proxy for bacteria. Previous data for pollen (Diehl et al., 2002; v. Blohn et al., 2005) were newly evaluated.

For kaolinite KGa-1b, K-feldspar, tree and grass pollen, an exponential increase of n_m with temperature T was found which is described by

$$n_m = \exp(a_{imm} + b_{imm}T_s) \quad (2)$$

with n_m in g^{-1} , a_{imm} and b_{imm} particle-related constants, $T_s = T_0 - T$, $T_0 = 0^\circ\text{C}$, with T in $^\circ\text{C}$. The constants for all particle types are listed in Table 1. Given in Table 1 are also the parameters T_{ini} and T_{lim} , representing the onset of immersion freezing during experiments and the lowest temperature which was investigated in the experiments, respectively.

Based on the best fit of the data of Murray et al. (2011) the constants in Eq. (2) were derived for kaolinite KGa-1b by using an average specific particle surface area of $11.8\text{m}^2\text{g}^{-1}$ as given by Murray et al. (2011); the result is shown in Fig. 1 as orange line. The solid part of the line represents the range which is validated by measurements of Murray et al. (2011) while the dotted part shows an extrapolation towards

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



higher temperatures. The value of T_{ini} is based on earlier measurements of Pitter and Pruppacher (1973). The same was performed for K-feldspar by using the best fit to the experimental data given by Atkinson et al. (2013) which was changed into Eq. (2) by using the specific particle surface area of $3.2 \text{ m}^2 \text{ g}^{-1}$ from Atkinson et al. (2013). The parameters are listed in Table 1, the result of Eq. (2) is shown in Fig. 1 as red line. Regarding pollen, previous data from Diehl et al. (2002) and v. Blohn et al. (2005) were evaluated. From the frozen fractions of drops, the drop volume, and the mass of pollen in the drops the numbers of active sites n_m as functions of temperature were calculated according to (e.g., Murray et al., 2011):

$$n_m = - \frac{\ln(1 - f_{ice}(T))}{c_{pollen} V_{drop}} \quad (3)$$

where $f_{ice}(T)$ is the fraction of frozen drop at temperature T , c_{pollen} the pollen concentration per drop, and V_{drop} the drop volume. Data for tree and grass pollen were summarized leading to two parameterizations for tree and grass pollen as given in Eq. (2). The constants are listed in Table 1 and the results of Eq. (2) are shown in Fig. 1 as light green lines. The solid parts of the lines represent the ranges which are validated by measurements while the dotted parts show extrapolations towards lower temperatures.

Regarding illite NX and Snomax[®], parameterizations were suggested by Broadley et al. (2012), Hiranuma et al. (2015), and Wex et al. (2015). To come to analogue descriptions as in the cases of the other particle types, these parameterizations were replaced by new ones following Eq. (2). Regarding illite NX, the parameterization was derived from the data reported by Hiranuma et al. (2015). The fit as given by Hiranuma et al. (2015) was changed into an expression for n_m by using the specific particle surface area of $124.4 \text{ m}^2 \text{ g}^{-1}$ of the illite NX sample (Hiranuma et al., 2015). From the non-linear curve (solid blue line in Fig. 2) a linear regression line was derived which is included in Fig. 1 (blue solid line). For Snomax[®], it was concluded in Wex et al. (2015) that the average n_m values (given in Fig. 2 as open green symbols) are very well

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



represented by the Hartmann et al. (2012) parameterization (solid green line in Fig. 2). One can notice a linear increase in the temperature range down to approximately -9°C and a further progress on a maximum value of $1.4 \times 10^{12} \text{g}^{-1}$. Thus, a linear regression curve was derived for the increase of n_m until the maximum value was reached; it is included in Fig. 2 as solid green line.

It can be noted from Fig. 1 that bacteria act at the highest temperatures starting not far below 0°C . Pollen lie in the range of the mineral dust particles. The differences between the mineral dust types are significant with feldspar the most efficient one, kaolinite the least efficient one.

2.1.2 Treatment of immersion freezing in the model

The previous Eq. (1) which gives the freezing rate of the supercooled drops had to be replaced by a similar expression which couples the number of active sites and the mass of insoluble particles in the drops. According to the singular description of heterogeneous freezing (Vali, 1971; Broadley et al., 2012) the frozen fraction of drops f_{ice} is given by

$$f_{\text{ice}}(T) = \frac{N_f(T)}{N_{\text{liq}}} = 1 - \exp(-n_m(T)m_{\text{pid}}) \quad (4)$$

with $N_f(T)$ the number of frozen drops at temperature T , N_{liq} the number of liquid drops, m_{pid} the mass of particles immersed in the drops, and $n_m(T)$ the number of active sites per unit mass at temperature T which is related to the cumulative nucleus spectrum $K(T)$ per unit mass per unit temperature:

$$n_m(T) = - \int_{T_0}^T K(T) dT \quad (5)$$

when lowering the temperature from $T_0 = 0^{\circ}\text{C}$ to T . From Eqs. (4) and (5) an expression for the change of the number of frozen drops ΔN_f per temperature interval ΔT can be

derived (Connolly et al., 2009):

$$\Delta N_f = N_{liq}(1 - \exp(-K(T)m_{pid}\Delta T)) \quad (6)$$

with N_{liq} the number of supercooled liquid drops and m_{pid} the mass of particles immersed in the drop. Thus, Eq. (1) can be replaced by

$$\frac{dN_f}{dt} = N_{liq} \frac{1 - \exp(-K(T)m_{pid}dT)}{dt} \quad (7)$$

As the aerosol particles are internally mixed one can assume that only a fraction of the insoluble mass per drop consists of ice nucleating material. Thus, the mass m_{pid} was reduced by a factor F_{INP} so that only this mass fraction accounts for possible numbers of active sites n_m and Eq. (7) was modified to

$$\frac{dN_f}{dt} = N_{liq} \frac{1 - \exp(-K(T)m_{pid}F_{INP}dT)}{dt} \quad (8)$$

A similar treatment was actualized in Diehl and Wurzler (2010). From Eqs. (2) and (5) it follows:

$$K(T) = \frac{dn_m(T)}{dT} = b_{imm} \exp(a_{imm} + b_{imm}T_s) \quad (9)$$

In Eq. (9) the freezing point depression due to the content of soluble material in the drops is considered, for details see Diehl and Wurzler (2004). In the model simulations, immersion freezing starts at the particle-related temperature T_{ini} , and at temperatures below T_{lim} it is assumed that the numbers of active sites stay constant. The sizes of possibly ice nucleating particles are restricted, i.e., dust particles must be larger than 0.1 μm in diameter, bacteria are limited to their typical diameters of 0.3 to 2 μm (Matthias-Maser and Jaenicke, 1995). Pollen are large particles of 10 μm at least (Straka, 1975), however, for the present simulations a lower limit of 2 μm was selected

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

⏪

⏩

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



to allow at least some freezing by pollen (see Sect. 3, initial dry particle number size distributions).

During the model simulations the content of insoluble particles per drop varies by several orders of magnitude which is due to the sizes of the condensation particles, the uptake of particles by the drops via impaction scavenging, and the drop collisions followed by coalescence. Thus, not all drops of the same sizes freeze at certain temperatures which describes the situation in real clouds (Diehl and Wurzler, 2004).

2.2 Contact freezing

In Diehl et al. (2006) contact freezing was described for several particle types independent on their sizes. However, measurements indicate that the size of the involved particles affects the contact freezing efficiency in the way that efficiency increases with increasing particle size (e.g., Gorbunov et al. (2001); Hoffmann et al., 2013a; Ladino et al., 2013). Therefore, the description of Diehl et al. (2006) was modified in the way that it is now particle-size dependent.

2.2.1 Parameterizations based on laboratory data

Measurements which give a direct correlation between particle size and contact freezing efficiency are not yet available for a wider range of ice nucleating particle types. Therefore, for the present parameterization different size classes were examined. Hoffmann et al. (2013a, b), and Hoffmann and Kiselev (personal communication, 2014) performed contact freezing experiments using an electrodynamical balance with monodisperse particles of 150 to 750 nm diameter. The results showed rather low median freezing temperatures T_{50} (the temperature where 50% of an observed drop population freeze), e.g., -34°C for illite NX, -32.5°C for kaolinite Fluka and less than -25°C for Snomax[®], in comparison to measurements with polydisperse particle samples.

Those experiments were performed at the UCLA vertical wind tunnel by Levin and Yankofsky (1983) and Pitter and Pruppacher (1973). The latter studied kaolinite and

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



montmorillonite with particle diameters between 0.1 and 10 μm with a mode between 1 and 2 μm and measured median freezing temperatures of -12 and -8°C , respectively. Levin and Yankofsky found a median freezing temperature of -4.5°C for bacteria. Diehl et al. (2012) investigated polydisperse mineral particles with supercooled drops suspended in an acoustic levitator. Median freezing temperatures were -11.5°C for illite NX and -8.7°C for montmorillonite K10. The latter agrees very well with the value found by Pitter and Pruppacher (1973) within the measurement error (1 K). Extrapolating the data of Hoffmann et al. (2013b) for illite NX towards larger particle sizes as shown in Fig. 3 indicates that a median freezing temperature of -11.5°C dust could be affected by particles with sizes between 2.3 and 3.0 μm in diameter (Diehl et al., 2012). Those particles are part of the polydisperse particle spectrum of illite NX (Hiranuma et al., 2015). Thus, one might conclude that the median freezing temperatures determined for polydisperse particle samples are affected by larger particles present in the size spectrum. This is probably the case also for previous findings measured with polydisperse particle samples.

Therefore, as an approximation, data obtained from polydisperse particle samples were used in the present parameterizations for particles with diameters mostly larger than 1 μm , at least larger than 0.7 μm . Data obtained from monodisperse particle samples were taken for ranges around the respective particle sizes.

The experimental data used as basis for the parameterizations include the following ice nucleating particle types: bacteria, feldspar, montmorillonite, illite, and kaolinite. In most cases, a linear correlation between the frozen fraction of drops and the temperature was found. From the experimental data, regression lines were calculated which are shown in Fig. 4 for various particle types (marked by different colors) and particle sizes (marked by different line styles).

Bacteria

Particle sizes of bacteria were restricted to their typical sizes with diameters between 0.3 and 2 μm (Matthias-Maser and Jaenicke, 1995). Measurements of Hoffmann and

Kiselev (personal communication, 2104) were performed with monodisperse Snomax[®] particles of 0.32 and 0.55 μm diameter. These data were used for size ranges from 0.3 to 0.5 μm and from 0.5 to 0.7 μm . For particles between 0.7 and 2 μm the data of Levin and Yankofsky were taken. The results are given in Fig. 4 as green lines.

5 Mineral dust particles

For mineral dust particles, a lower size limit of 0.1 μm in diameter was assumed. Illite NX particles were investigated by Hoffmann et al. (2013b) with 0.15, 0.32, 0.55, and 0.75 μm particles. These data were taken for size ranges from 0.1 to 0.2, 0.2 to 0.4, 0.4 to 0.6, and 0.6 to 0.8 μm . For larger particles, data from Diehl et al. (2012) were used. The results are shown in Fig. 4 as blue lines. K-feldspar was investigated by Hoffmann and Kiselev (personal communication, 2014) with 0.32 and 0.55 μm particles and by Diehl and Mitra (personal communication, 2014) with polydisperse particles. Here three size ranges were defined, from 0.1 to 0.4, 0.4 to 0.8 μm , and larger than 0.8 μm . The data are marked in Fig. 4 as red lines. For kaolinite and montmorillonite, also two size ranges were specified, from 0.1 and 1 μm and larger than 1 μm . The data for the larger particles sizes were both taken from Pitter and Pruppacher (1973, polydisperse particle samples). Results from Hoffmann et al. (2013a) were used for the smaller size range of kaolinite. Under the assumption that the differences between larger and smaller INP are similar for kaolinite and montmorillonite the data for the smaller size range of montmorillonite were obtained by a parallel shifting analogue to kaolinite. In Fig. 4, results for kaolinite are given in orange, results for montmorillonite in cyan.

From Fig. 4 it can be noted that particles in the larger size ranges affect freezing already at temperatures around -10°C while smaller particles become active in a temperature range around -25°C . Bacteria act at the highest temperatures, kaolinite and illite at the lowest. For all particle types and sizes except bacteria smaller than 0.7 μm the frozen fraction of drops increases linearly with temperature T (given in $^\circ\text{C}$) accord-

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



ing to Diehl et al. (2006):

$$\frac{N_f}{N_{\text{liq}}} = a_{\text{con}}T + b_{\text{con}} \quad (10)$$

with N_f the number of frozen drops, N_{liq} the number of liquid drops colliding with dry particles at temperature T , and the constants a_{con} and b_{con} . Note that in Eq. (10) the frozen fraction is limited to values between 0 and 1. In Diehl et al. (2006), the constants were given for several particle types independent of their sizes while in the present parameterization the constants a_{con} and b_{con} are size-resolved. They are listed in Tables 2 and 3. In case of small bacteria the equation to calculate the frozen fraction of drops with respect to the temperature T (in °C) has the form

$$\frac{N_f}{N_{\text{liq}}} = a_{\text{con}} + b_{1,\text{con}}T + b_{2,\text{con}}T^2 + b_{3,\text{con}}T^3 \quad (11)$$

The size-resolved constants a_{con} , $b_{1,\text{con}}$, $b_{2,\text{con}}$, and $b_{3,\text{con}}$ are given in Table 2.

2.2.2 Treatment of contact freezing in the model

The description of contact freezing includes the following conditions: (1) dry particles have to be present, and (2) particles and supercooled drops have to collide with each other. Furthermore, the sizes of the particles allowed as activating ice nucleating particles are restricted as for deposition freezing (i.e., dust particles $> 0.1 \mu\text{m}$ in diameter, bacteria 0.3 to $2 \mu\text{m}$ in diameter).

The presence of dry particles is always the case during the air parcel ascent because of entrainment, i.e. new inactivated particles are continuously mixed in at the edges of the simulated cloud. However, in the presently employed air parcel model the particles are in equilibrium with respect to the water vapor in their environment and, thus, they take up some water due to their size and soluble fraction. As introduced in Diehl et al. (2006) the dryness of a potential ice nucleating particle is defined by the assumption that the water mass should be smaller than half of the dry particle mass.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



The second condition is considered by a collision kernel K calculated for supercooled drops and particles (Kerkweg et al., 2003; for more details see Diehl et al., 2006):

$$K = E_{\text{coll}} |V_{\infty, \text{drop}} - V_{\infty, \text{ap}}| \cdot \pi (r_{\text{drop}} - r_{\infty})^2 \quad (12)$$

where $V_{\infty, \text{drop}}$ and $V_{\infty, \text{ap}}$ are the terminal velocities of the drop and the particle, respectively, r_{drop} and r_{ap} the drop and particle radii, respectively. The collision kernel shows highest values for collisions between large drops and particles (Diehl et al., 2006), i.e. contact freezing is the most efficient when large supercooled drops and particles are present. If during the model simulations dry particles collide with supercooled drops the number of frozen drops is calculated. It is assumed that only a fraction F_{INP} of the aerosol particles is able to act as ice nucleating particles. Only drops which collide with those INP are allowed to freeze which is included in the following modified Eqs. (13) and (14):

$$N_f = F_{\text{INP}} N_{\text{liq}} (a_{\text{con}} T + b_{\text{con}}) \quad (13)$$

$$N_f = F_{\text{INP}} N_{\text{liq}} (a_{\text{con}} + b_{1, \text{con}} T + b_{2, \text{con}} T^2 + b_{3, \text{con}} T^3) \quad (14)$$

This is under the requirement that these equations are based on measurements with one drop–particle collision per freezing event so that the fraction of frozen drops in Eqs. (13) and (14) can be set equal to the freezing probability (Ladino et al., 2013). This requirement is fully achieved in the experiments of Hoffmann et al. (2013a, b), and Hoffmann and Kiselev (personal communication, 2014). During the experiments of Pitter and Pruppacher (1973), Levin and Yankofsky (1983), and Diehl et al. (2012) the number of collisions per freezing event is not documented. Single supercooled drop were freely levitated (in a wind tunnel or an acoustic levitator) while one burst of INP was blown on it. Therefore, as the particles collided almost simultaneously with the supercooled drop one could assume that in case the drop froze this was triggered by the first collision.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



a part F_{INP} of the available particles is able to act as ice nucleating particles. Therefore, the total number of particles in Eq. (15) is reduced:

$$N_{\text{act}} = F_{\text{INP}} N_{\text{total}} \exp(a_{\text{dep}} + b_{\text{dep}} S_{\text{ice}}) \quad (17)$$

The activated particles are moved to the ice particle spectrum and grow further by water vapor deposition and they may serve as germs for secondary ice formation, i.e. they may initiate freezing of supercooled drops by collision (Diehl et al., 2006).

3 Model initiation and sensitivity studies

During the present sensitivity studies, convective clouds were simulated. In those clouds the initiation of precipitation takes place mainly via the ice phase because liquid drops are transferred into higher regions in the atmosphere and supercooled. Once frozen the ice particles grow further by riming (i.e. collision with other supercooled droplets) and by the deposition of water vapour (i.e. at the expense of liquid drops, the Bergeron–Findeisen process, which is typically much faster than condensation). Due to the vertical velocity large precipitation-sized ice particles can form in convective clouds and fall out as graupels, hailstones or, when they fall through the melting layer, as large raindrops. The present model simulations were initialized with a convective vertical profile where temperatures in higher altitudes were low enough to assure ice formation. It has an average lapse rate of approximately 0.6 K per 100 m without any maxima or minima (Langmann, personal communication, 2004), see Fig. 7. The ascent of the air parcel is driven by a temperature difference between the air bubble and its environment. Depending on the temperature difference the updraft of the air parcel proceeds at various speeds and various heights with corresponding temperatures are reached.

Two different dry aerosol particle number size distributions were used to compare the effects on ice formation. One was an average continental distribution (OPAC database, Hess et al., 1998) which is a rather broad spectrum and characterized by a large

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

number of small particles, see black line in Fig. 8; its parameters are $N = 7000 \text{ cm}^{-3}$, $d = 42.4 \text{ nm}$, and $\sigma = 2.24$ (with N the particle number, d the diameter, and σ the standard deviation). The other one was a regional haze distribution (Reid et al., 1998) which is a rather narrow spectrum and characterized by larger particle sizes. The parameters are $N = 6000 \text{ cm}^{-3}$, $d = 0.1 \mu\text{m}$, and $\sigma = 1.65$, see red line in Fig. 8. Both rather simple mono-modal distributions were selected to avoid a mixture of effects due to ice physics and activation of aerosol particles. Thus, the effects of ice physics should be emphasized. The soluble fraction ε of the aerosol particles was set to 0.5 which is a typical value of atmospheric particles (Busch et al., 2002).

Regarding the conditions on the sizes of the ice nucleating particles as given in Sect. 2 (mineral dust particles larger than $0.1 \mu\text{m}$, bacteria larger than $0.3 \mu\text{m}$, pollen larger than $2 \mu\text{m}$), one can conclude from Fig. 8 that – in particular in the average continental case – the majority of the continental particles is too small to affect ice formation. The dry particle spectrum influences the drop spectrum which is important for immersion and contact modes. Figure 9 shows the number concentrations as function of diameter for two different altitudes and corresponding temperatures of zero and -29°C for the two cases, average continental and regional haze particles. Because the liquid water content is the same during both model simulations, less but large drops develop with the regional haze distribution and numerous but smaller drops with average continental distribution. On the other hand, as the continental spectrum is broader, collision and coalescence processes are more effective and, thus, larger drops evolve. Also given in Fig. 9 are the number concentrations of the interstitial aerosol particles. Note that during the updraft dry aerosol particles are available for ice formation in deposition contact modes.

With these initial conditions, a multitude of sensitivity studies was performed to demonstrate the impact of ice nuclei concentrations and types on ice formation in convective mixed-phase clouds. First, single freezing processes were studied while the following parameters were varied:

- dry aerosol particle number size distribution: average continental and regional haze,
- ice nucleating particle type – biological particles and mineral dust,
- strength of convection: three levels of convection, simulated by a temperature difference of 3, 2 K, and 1.5 K, leading to final temperatures of –40, –30, and –24.5 °C, respectively,
- fraction of potential ice nucleating particles F_{INP} – variation between 0.001 and 10 %.

Afterwards, coupled freezing processes were investigated to study the competition between the different freezing processes. These were undertaken only with those parameters which resulted in higher ice formation.

4 Results and discussion

4.1 Ice water fractions and single freezing processes

To evaluate the efficiency of the different freezing processes and ice nucleating particle types, as a central diagnostic parameter the ice water fraction IWF was selected which is calculated from the ice water content IWC and the liquid water content LWC:

$$IWF = \frac{IWC}{LWC + IWC} \quad (18)$$

According to Korolev et al. (2003) an ice cloud is defined by $IWF > 0.9$, a liquid cloud by $IWF < 0.1$, and mixed-phase clouds by $0.1 \leq IWF \leq 0.9$. Note that in an air parcel model, the IWF is only influenced by in-situ ice formation processes and not by sedimentation of ice into or out of the considered parcel. In the following Tables 5 to 7, the ice water fractions as results from the sensitivity studies are listed for immersion,

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



or 0.1 % (kaolinite) were necessary. Ice formation was sensitive to the type of mineral dust as well as to the potential fraction of INP. For instance, under the same conditions an ice cloud could form with feldspar but a mixed-phase cloud with only a small ice water fraction with kaolinite.

5 In the contact mode, there is very little ice formation (Table 6). Only liquid clouds formed with the regional haze particle distribution but in case of the average continental distribution at least some mixed-phase clouds formed with ice water fractions between 0.1 and 0.3. High potential fractions of INP F_{INP} of 10 % were required. Bacteria did not affect ice formation, this probably results from the restricted particle sizes.
10 The type of mineral dust decides whether mixed-phase clouds are formed (feldspar, montmorillonite) or not (illite, kaolinite).

Effective deposition INP are bacteria, feldspar, and illite while the mixed particle samples Saharan and Asian dust form liquid clouds only. Mixed-phase clouds formed with high potential INP fractions F_{INP} between 1 and 10 %. The results for the different mineral dust types are rather similar but mixed-phase clouds were formed with pure minerals only but not with mixtures (Saharan and Asian dust) which are dominated by quartz (see Sect. 2.3.1).
15

4.1.3 Strength of convection and ambient temperature

In all freezing modes, cases with the weakest convection ($\Delta T = 1.5 \text{ K}$) and the corresponding highest final temperature of -25°C showed hardly ice formation. Exceptions are only cases with bacteria and feldspar in the immersion mode (Table 5). Contact ice formation did not occur with the weaker convection as the temperatures were not low enough to give the more effective smaller particles the chance to act (Table 6). In the deposition mode, obviously temperatures below -25°C are required to develop mixed-phase clouds (Table 7) as at higher temperatures the ice supersaturation is still too low. On the other hand, the strongest convection ($\Delta T = 3 \text{ K}$) also hindered ice formation in contact and deposition modes which might be affected by the presence of less interstitial particles.
20
25

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



4.2 Comparison to measured INP numbers

In this section a discussion is included how realistic the assumed concentrations of INP are which lead to partial or complete cloud glaciation.

4.2.1 Immersion freezing

Regarding the cases of immersion freezing listed in Table 5, one has to look at the composition of cloud residuals which was investigated in several field campaigns. E.g., Kamphus et al. (2010) measured 8% minerals in cloud droplet residuals; Hiranuma et al. (2013) found 3% mineral dust particles in cloud droplet residuals for all particle sizes and particle-size resolved measurements indicated enhanced fractions for larger particles up to 17%. In the model simulations mixed-phase clouds were formed already with potential INP fractions between 0.01 and 1%. Thus, the dominant role of immersion freezing with mineral dust seems to be validated. It is confirmed by the fact that during INUIT field campaigns (Worringen et al., 2014; Schmidt et al., 2015) fractions of mineral dust up to 40% in ice residuals were observed. Similar numbers between 30 and 40% are reported by Kamphus et al. (2010) in ice particle residuals.

Bacteria need to be present as potential INP only as low as 0.001 to 0.01% to affect mixed-phase clouds, pollen with 1% potential INP. For pollen these numbers do probably not represent realistic cases; however, the pollen cases were anyway rather artificial as such large particles ($> 10 \mu\text{m}$) were actually not part of the aerosol particle spectrum. Bacteria concentrations in cloud water are given as average values of, e.g., $1.5 \times 10^9 \text{ m}^{-3}$ (Sattler et al., 2001), $2 \times 10^{10} \text{ m}^{-3}$ (Bauer et al., 2002), and $7 \times 10^4 \text{ m}^{-3}$ (Amato et al., 2005). Unfortunately, field measurements which give the number fractions of bacteria or primary biological aerosol particles (PBAP) related to the total concentrations of in-droplet particles are not available so far. An estimation was undertaken based on the results of Bauer et al. (2002). From field measurements in a continental background site they determined the numbers of bacterial and fungi cells in cloud water and calculated the corresponding amount which would contribute to the

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

$2 \times 10^6 \text{ m}^{-3}$ for the regional haze distribution. Thus, fractions of potential ice nucleating particles F_{INP} of 10% resulted in particle concentrations available for deposition and contact nucleation of at the most $4 \times 10^4 \text{ m}^{-3}$ and $2 \times 10^5 \text{ m}^{-3}$, respectively.

In Saharan dust events, Bangert et al. (2012) measured particle number concentrations up to $5 \times 10^7 \text{ m}^{-3}$. In Hande et al. (2014), simulated mineral dust number concentrations are $4 \times 10^5 \text{ m}^{-3}$ on average up to extreme values of $5.8 \times 10^6 \text{ m}^{-3}$. Thus, the numbers of potential INP used in the model simulations do not exceed realistic particle concentrations of mineral dust.

Near-surface concentrations of bacteria range between $1 \times 10^3 \text{ m}^{-3}$ and $5 \times 10^5 \text{ m}^{-3}$ depending on ecotypes (Burrows et al., 2009) but these values are certainly not reached in upper cloud regions. On the other hand, DeLeon-Rodriguez et al. (2013) reported from field measurements in low- and high-altitude air masses that bacterial cells represented nearly 20% of the total particles in the diameter range between 0.25 and $1 \mu\text{m}$. This is approximately the size range of potential ice nucleating particles in the present model simulations. For even larger particles in the coarse mode high fractions of PBAP (primary biological particles) are also reported by Manninen et al. (2014). However, the numbers of potential INP used in the model simulations probably overestimate real bacteria concentrations.

Considering these factors one may conclude that the conditions for atmospheric deposition and contact freezing could be sufficient in some cases to form mixed-phase clouds from primary ice formation by mineral dust particles. In some extreme cases, the formation of mixed-phase clouds might be possible via deposition nucleation on bacteria. On the other hand, the initial particle spectra used for the present model simulations contain little amounts of particles larger than $1 \mu\text{m}$ (see Fig. 8) which would be able to act as contact ice nucleating particles much more efficiently (see Sect. 2.2.1). Thus, in cases where larger INP are present in or around atmospheric clouds contact freezing might be significantly enhanced.

4.3 Ice particle spectra, single and coupled freezing processes

In this section only simulations with the most efficient ice formation are treated, i.e. using the average continental particle distribution and a medium strength of convection with $\Delta T = 2$ K leading to final temperatures of -30°C . The potential fractions F_{INP} were set to 10% for feldspar, illite, montmorillonite, and kaolinite. Bacteria and pollen were not considered here as those high values of F_{INP} are not realistic (see discussion in Sect. 4.2). Figure 10 shows the ice particle number size distributions at different altitudes and corresponding temperatures for single deposition, contact, and immersion freezing processes.

The ice particle spectra affected by immersion freezing are rather narrow starting with a particle diameter of $1\ \mu\text{m}$ due to the smallest drop size. However, larger drops around $30\ \mu\text{m}$ in diameter were frozen first as their content of insoluble particles is higher. With decreasing temperature, also smaller drops can freeze while ice particles grow by the deposition of water vapour and by riming, i.e. the ice particle spectra broadens in both directions. Finally, they are still smaller than the ones formed by deposition freezing. The differences between the dust types are much more evident than in the other modes and the final ice particle numbers are higher, in particular for feldspar.

In the contact mode, the simulated ice particle spectrum is still somewhat narrower. At temperatures around -20°C , the maximum of the drop number concentration lies at $30\ \mu\text{m}$. This indicates that large supercooled drops froze by collisions with larger particles as in this temperature range smaller particles are hardly efficient as contact INP. Lowering the temperature down to -30°C enhances the ice particle spectra towards larger sizes, i.e. the ice particles grow by the deposition of water vapor and by riming but still only little amounts of small drops are freezing. Thus, contact freezing is strongly controlled by the collision kernel. The number concentrations of feldspar and montmorillonite are rather similar at -30°C but strongly different at -21°C . This is due to the fact that smaller feldspar particles are active at higher temperatures as smaller montmorillonite particles (see Fig. 4).

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

The ice particle spectra due to deposition freezing start with small sizes and develop towards larger sizes during the ascent of the cloud. This indicates that firstly, as primary ice formation, small ice particles are formed due to the size of the involved particles (0.1 μm at least). Afterwards, these pristine ice particles serve as nuclei for secondary ice formation, i.e. by collisions with supercooled liquid drops. This process produces ice particles of larger sizes, see maximum around 40 μm . All ice particles grow further by the deposition of water vapor and by riming leading to ice particles larger than 100 μm . Thus, a broad spectrum of ice particles evolved from deposition freezing. The number concentrations vary by one order of magnitude from illite 2 to feldspar. The oscillations of the spectra on the left hand side are an artefact effect of the size classes of the particles acting as INP starting with 0.1 μm diameter; they vanish if the lower size of the INP is limited by the critical radius only (Eq. 16).

Coupled cases were simulated to investigate the competition between contact and immersion modes as both freeze supercooled drops, and the competition between contact and deposition freezing as both interact with dry particles. The following combinations were studied: (1) feldspar and (2) illite 1 as for these particle types parameterizations for all freezing modes are available based on INUIT measurements. Additionally, some mixed cases were investigated, i.e. one INP type for one freezing mode, another INP type for the other freezing mode. These were for coupled contact and immersion freezing (3) montmorillonite + kaolinite, (4) feldspar + kaolinite and for coupled deposition and contact freezing (3) illite 2 + montmorillonite, (4) Saharan dust + feldspar. As can be noted from Tables 5 to 7, the ice water fractions evolved from feldspar INP are similar for deposition and contact freezing but significantly higher for immersion freezing. The effects from illite 1 INP differ between the freezing modes (immersion highest, contact lowest). The combination illite 2 + montmorillonite in deposition and contact modes was selected because the resulted ice water fractions were similar which is also the case for the combination montmorillonite + kaolinite in contact and immersion modes.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

the collision efficiencies between potential INP and supercooled drops (see Sect. 2.2) while deposition freezing is ruled by the ice supersaturation (see Sect. 2.3) which, of course, increases with decreasing temperature. From the differences between the total liquid drop numbers and the total ice particle numbers one can conclude that the glaciation of the clouds proceeds mainly by the growth of ice particles at the expense of liquid drops (Bergeron–Findeisen process or riming). Here, some effects are presumably overestimated as from the air parcel no cloud particle sedimentation is possible.

Figure 12b shows results for the coupled freezing processes. It is obvious that in those cases where one process is inferior the ice particle numbers are completely determined by the dominant process. This is the case in coupled immersion and contact freezing with feldspar and illite 1 but not with kaolinite + feldspar and kaolinite + montmorillonite where the effects of contact freezing are visible at lower temperatures ($< -20^{\circ}\text{C}$). Coupled deposition and contact freezing shows the same results as for deposition freezing alone in case of illite. In the other cases, feldspar, illite 2 + montmorillonite, and Saharan dust + feldspar, there are at least some small enhancements visible at temperatures lower than -20°C when contact freezing becomes more efficient.

5 Summary and conclusions

In this paper improvements and modifications of the spectral-bin microphysics embedded in an adiabatic air parcel model as described in Diehl et al. (2006) are presented. They include (1) a particle-type dependent parameterization of immersion freezing, (2) a particle-type and size-resolved parameterization of contact freezing, and (3) a particle-type dependent description of deposition freezing.

Sensitivity studies with the modified version of the microphysics package demonstrated the impact of ice nuclei concentrations and types on ice formation in convective mixed-phase clouds. As a central diagnostic parameter the ice water fraction IWF was selected which is the relation of the ice water content to the total water content. Sin-

and, thus, contact freezing becomes relevant near this temperature range only. Contact freezing might be enhanced in atmospheric situations where particles larger than 1 μm are present in higher amounts.

The importance of deposition freezing lies in secondary ice formation: at first, small pristine ice particles are formed due to the sizes of the involved particles. They trigger the freezing of supercooled drops by collisions. Thus, a broader ice particle spectrum is generated than by immersion and contact freezing. Regarding coupled contact and deposition freezing, there is hardly competition because of involved particle sizes. Small particles are less efficient in the contact mode because (1) they collide less with supercooled drops, (2) they act at rather low temperatures. Therefore, small particles are available for deposition freezing while the larger particles are involved in the contact mode as they are more effective INP and collision partners.

One should consider that during the cloud model runs each drop contains insoluble material serving as immersion ice nucleus because the particles in the model are internally mixed. In a real cloud there might be drops which do not contain any potential ice nucleating material. In contrast, the amount of interstitial dry particles serving as deposition or contact freezing nuclei is limited in an air parcel model while in a real cloud there might be more potential ice nuclei at the edges or beneath the cloud.

As already suggested in literature, mineral dust particles seem to be the most important INP. The model results indicate that ice formation by immersion freezing is similarly sensitive to the mineral dust types as to the potential fractions of INP. Therefore, the investigation of atmospheric mixtures of mineral dust is relevant and will decide about the actual immersion freezing effects which will lay between the effects of kaolinite and feldspar. Biological particles such as bacteria and pollen are found to be very effective INP in laboratory; however, the critical factor are the amounts of biological particles in atmospheric environment and clouds. The present model simulations together with estimations of their atmospheric occurrence indicate that they are probably not involved in significant ice formation. This has been suggested already by Phillips et al. (2009), Diehl and Wurzler (2010), and Paukert and Hoose (2014).

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



**Particle-dependent
parameterizations of
heterogeneous
freezing processes**

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[⏪](#)[⏩](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

The microphysical package presented here with improvements and modifications of previous descriptions of heterogeneous freezing was included into an air parcel model which has the advantage that all changes in the microphysical evolution of the cloud can be attributed to microphysical processes. On the other hand, some compromises are required concerning the cloud dynamics including some well-known weaknesses as precipitation sized cloud particles do not sediment but stay inside the parcel. Therefore, the further goal is to implement the new microphysical scheme into to a more complex state-of-the-art model system, for instance the 3-D cloud model COSMO-SPECS (Grützun et al., 2008). This model contains the microphysical scheme as used in Diehl et al. (2006) within the adiabatic parcel model which could be replaced by the microphysical scheme presented here. Such an improvement will allow more complex model simulations including the formation of precipitation which will enlighten the role of ice nucleating particles in atmospheric clouds.

Acknowledgements. This work is part of the research group INUIT (Ice Nuclei research UniT) FOR1525 and was supported by the Deutsche Forschungsgemeinschaft under grant DI 1539/1-1. We appreciate the INUIT laboratory and field groups for providing their experimental data as base of parametrizations and for helpful discussions. Thanks to Karin Ardon-Dryer for providing unpublished material. We would like to thank Corinna Hoose for fruitful discussions and helpful comments and suggestions.

References

- Amato, P., Ménager, M., Sancelme, M., Laj, P., Mailhot, G., and Delort, A.-M.: Microbial population in cloud water at the Puy de Dôme: implications for the chemistry of clouds, *Atmos. Environ.*, 39, 4143–4153, 2005.
- Ansmann, A., Althausen, D., Müller, D., Seifert, P., Freudenthaler, V., Heese, B., Wiegner, M., Pisani, G., Knippertz, P., and Dubovik, O.: Influence of Saharan dust on cloud glaciation in southern Morocco during Saharan mineral dust experiment, *J. Geophys. Res.*, 113, D04210, doi:10.1029/2007JD008785, 2008.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



- Atkinson, J. D., Murray, B. J., Woodhouse, M. T., Whale, T. F., Baustian, K. J., Carslaw, K. S., Dobbie, S., O'Sullivan, D., and Malkin, T. L.: The importance of feldspar for ice nucleation by mineral dust in mixed-phase clouds, *Nature*, 498, 355–358, doi:10.1038/nature12278, 2013.
- 5 Bangert, M., Nenes, A., Vogel, B., Vogel, H., Barahona, D., Karydis, V. A., Kumar, P., Kottmeier, C., and Blahak, U.: Saharan dust event impacts on cloud formation and radiation over Western Europe, *Atmos. Chem. Phys.*, 12, 4045–4063, doi:10.5194/acp-12-4045-2012, 2012.
- Bauer, H., Kasper-Giebl, A., Löflund, M., Giebl, H., Hitzemberger, R., Zibuschka, F., and Puxbaum, H.: The contribution of bacteria and fungal spores to the organics content of cloud water, precipitation and aerosols, *Atmos. Res.*, 64, 109–119, 2002.
- 10 Broadley, S. L., Murray, B. J., Herbert, R. J., Atkinson, J. D., Dobbie, S., Malkin, T. L., Condliffe, E., and Neve, L.: Immersion mode heterogeneous ice nucleation by an illite rich powder representative of atmospheric mineral dust, *Atmos. Chem. Phys.*, 12, 287–307, doi:10.5194/acp-12-287-2012, 2012.
- 15 Burrows, S. M., Elbert, W., Lawrence, M. G., and Pöschl, U.: Bacteria in the global atmosphere – Part 1: Review and synthesis of literature data for different ecosystems, *Atmos. Chem. Phys.*, 9, 9263–9280, doi:10.5194/acp-9-9263-2009, 2009.
- Busch, B., Kandler, K., Schütz, L., and Neusüß, C.: Hygroscopic properties and water soluble volume fraction of atmospheric particles in the diameter range from 50 nm to 3.8 μm during LACE 98, *J. Geophys. Res.*, 107, LAC 2-1–LAC 2-11, 2002.
- 20 Connolly, P. J., Möhler, O., Field, P. R., Saathoff, H., Burgess, R., Choularton, T., and Gallagher, M.: Studies of heterogeneous freezing by three different desert dust samples, *Atmos. Chem. Phys.*, 9, 2805–2824, doi:10.5194/acp-9-2805-2009, 2009.
- DeLeon-Rodriguez, N., Latham, T. L., Rodriguez-R, L. M., Barazesh, J. M., Anderson, B. E., Beyersdorf, A. J., Ziemba, L. D., Bergin, M., Nenes, A., and Konstantinidis, K. T.: Microbiome of the upper troposphere: species composition and prevalence, effects of tropical storms, and atmospheric implications, *P. Natl. Acad. Sci. USA*, 110, 2575–2580, doi:10.1073/pnas.1212089110, 2013.
- 25 DeMott, P. J., Prenni, A. J., McMeeking, G. R., Sullivan, R. C., Petters, M. D., Tobo, Y., Niemand, M., Möhler, O., Snider, J. R., Wang, Z., and Kreidenweis, S. M.: Integrating laboratory and field data to quantify the immersion freezing ice nucleation activity of mineral dust particles, *Atmos. Chem. Phys.*, 15, 393–409, doi:10.5194/acp-15-393-2015, 2015.
- 30

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Diehl, K. and Wurzler, S.: Heterogeneous drop freezing in the immersion mode: model calculations considering soluble and insoluble particles in the drops, *J. Atmos. Sci.*, 61, 2063–2072, 2004.

Diehl, K. and Wurzler, S.: Air parcel model simulations of a convective cloud: bacteria acting as immersion ice nuclei, *Atmos. Environ.*, 44, 4622–4628, 2010.

Diehl, K., Matthias-Maser, S., Mitra, S. K., and Jaenicke, R.: The ice nucleating ability of pollen. Part II: Laboratory studies in immersion and contact freezing modes, *Atmos. Res.*, 61, 125–133, 2002.

Diehl, K., Simmel, M., and Wurzler, S.: Numerical simulations of the impact of aerosol properties and drop freezing modes on the glaciation, microphysics, and dynamics of clouds, *J. Geophys. Res.*, 111, D07202, doi:10.1029/2005JD005884, 2006.

Diehl, K., Simmel, M., and Wurzler, S.: Effects of drop freezing on microphysics of an ascending cloud parcel under biomass burning conditions, *Atmos. Environ.*, 41, 303–314, 2007.

Diehl, K., Schmithüsen, H., Debertshäuser, M., Borrmann, S., and Mitra, S. K.: Laboratory investigations of contact and immersion freezing of mineral dust using an acoustic levitator, *Proceedings European Aerosol Conference, 2–7 September 2012, Granada, Spain, 2012.*

Duft, D. and Leisner, T.: Laboratory evidence for volume-dominated nucleation of ice in supercooled water microdroplets, *Atmos. Chem. Phys.*, 4, 1997–2000, doi:10.5194/acp-4-1997-2004, 2004.

Ekman, A. M. L., Engström, A., and Wang, C.: The effect of aerosol composition and concentration on the development and anvil properties of a continental deep convective cloud, *Q. J. Roy. Meteor. Soc.*, 133, 1439–1452, 2007.

Ervens, B. and Feingold, G.: On the representation of immersion and condensation freezing in cloud models using different nucleation schemes, *Atmos. Chem. Phys.*, 12, 5807–5826, doi:10.5194/acp-12-5807-2012, 2012.

Gilmore, M. S., Straka, J. M., and Rasmussen, E. N.: Precipitation and evolution sensitivity in simulated deep convective storms: comparisons between liquid-only and simple ice and liquid phase microphysics, *Mon. Weather Rev.*, 132, 1897–1916, 2004.

Gorbunov, B., Baklanov, A., Kakutkina, N., Windsor, H. L., and Toumi, R.: Ice nucleation on soot particles, *J. Aerosol Sci.*, 32, 199–215, 2001.

Grützun, V., Knoth, O., and Simmel, M.: Simulation of the influence of aerosol particle characteristics on clouds and precipitation with LM-SPECS: model description and first results, *Atmos. Res.*, 90, 233–242, 2008.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Hande, L. B., Engler, C., Hoose, C., and Tegen, I.: Seasonal variability of Saharan desert dust and ice nucleating particles over Europe, *Atmos. Chem. Phys.*, 15, 4389–4397, doi:10.5194/acp-15-4389-2015, 2015.

Hess, M., Koepke, P., and Schult, I.: Optical properties of aerosols and clouds: the software package OPAC, *B. Am. Meteorol. Soc.*, 79, 831–844, 1998.

Hiranuma, N., Brooks, S. D., Moffet, R. C., Glen, A., Laskin, A., Gilles, M. K., Liu, P., Macdonald, A. M., Strapp, J. W., and McFarquar, G. M.: Chemical characterization of individual particles and residuals of cloud droplets and ice crystals collected on board research aircraft in the ISDAC 2008 study, *J. Geophys. Res.*, 118, 6564–6579, doi:10.1002/jgrd.50484, 2013.

Hiranuma, N., Augustin-Bauditz, S., Bingemer, H., Budke, C., Curtius, J., Danielczok, A., Diehl, K., Dreischmeier, K., Ebert, M., Frank, F., Hoffmann, N., Kandler, K., Kiselev, A., Koop, T., Leisner, T., Möhler, O., Nillius, B., Peckhaus, A., Rose, D., Weinbruch, S., Wex, H., Boose, Y., DeMott, P. J., Hader, J. D., Hill, T. C. J., Kanji, Z. A., Kulkarni, G., Levin, E. J. T., McCluskey, C. S., Murakami, M., Murray, B. J., Niedermeier, D., Petters, M. D., O'Sullivan, D., Saito, A., Schill, G. P., Tajiri, T., Tolbert, M. A., Welti, A., Whale, T. F., Wright, T. P., and Yamashita, K.: A comprehensive laboratory study on the immersion freezing behavior of illite NX particles: a comparison of 17 ice nucleation measurement techniques, *Atmos. Chem. Phys.*, 15, 2489–2518, doi:10.5194/acp-15-2489-2015, 2015.

Hoffer, T. E.: A laboratory investigation of droplet freezing, *J. Meteorol.*, 18, 766–778, 1961.

Hoffmann, N., Kiselev, A., Rzesanke, D., Duft, D., and Leisner, T.: Experimental quantification of contact freezing in an electrodynamic balance, *Atmos. Meas. Tech.*, 6, 2373–2382, doi:10.5194/amt-6-2373-2013, 2013a.

Hoffmann, N., Duft, D., Kiselev, A., and Leisner, T.: Contact freezing efficiency of mineral dust aerosols studied in an electrodynamic balance: quantitative size and temperature dependence for illite particles, *Faraday Discuss.*, 165, 383–390, doi:10.1039/C3FD00033H, 2013b.

Hoose, C., Lohmann, U., Erdin, R., and Tegen, I.: The global influence of dust mineralogical composition on heterogeneous ice nucleation in mixed-phase clouds, *Environ. Res. Lett.*, 3, 025003–025017, 2008.

Joly, M., Amato, P., Deguillaume, L., Monier, M., Hoose, C., and Delort, A.-M.: Quantification of ice nuclei active at near 0 °C temperatures in low-altitude clouds at the Puy de Dôme atmospheric station, *Atmos. Chem. Phys.*, 14, 8185–8195, doi:10.5194/acp-14-8185-2014, 2014.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Kamphus, M., Ettner-Mahl, M., Klimach, T., Drewnick, F., Keller, L., Cziczo, D. J., Mertes, S., Borrmann, S., and Curtius, J.: Chemical composition of ambient aerosol, ice residues and cloud droplet residues in mixed-phase clouds: single particle analysis during the Cloud and Aerosol Characterization Experiment (CLACE 6), *Atmos. Chem. Phys.*, 10, 8077–8095, doi:10.5194/acp-10-8077-2010, 2010.

Kerkweg, A., Wurzler, S., Reisin, T., and Bott, A.: On the cloud processing of aerosol particles: an entraining air parcel model with two-dimensional spectral cloud microphysics and a new formulation of the collection kernel, *Q. J. Roy. Meteor. Soc.*, 129, 1–18, 2003.

Khain, A., Ovtchinnikov, M., Pinsky, M., Pokrovsky, A., and Krugliak, H.: Notes on the state-of-the-art numerical modeling of cloud microphysics, *Atmos. Res.*, 55, 159–224, 2000.

Koop, T., Bertram, A. K., Molina, L. T., and Molina, M. J.: Phase transitions in aqueous NH_4HSO_4 solutions, *J. Phys. Chem. A.*, 103, 9042–9048, 1999.

Koop, T., Beiping, L., Tsias, A., and Peter, T.: Water activity as the determinant for homogeneous ice nucleation in aqueous solutions, *Nature*, 406, 611–614, 2000.

Korolev, A. V., Isaac, G. A., Cober, S. G., Strapp, J. W., and Hallett, J.: Microphysical characterization of mixed-phase clouds, *Q. J. Roy. Meteor. Soc.*, 129, 39–65, 2003.

Ladino Moreno, L. A., Stetzer, O., and Lohmann, U.: Contact freezing: a review of experimental studies, *Atmos. Chem. Phys.*, 13, 9745–9769, doi:10.5194/acp-13-9745-2013, 2013.

Lee, S. S., Donner, L. J., and Phillips, V. T. J.: Impacts of aerosol chemical composition on microphysics and precipitation in deep convection, *Atmos. Res.*, 94, 220–237, 2009.

Leroy, D., Monier, M., Wobrock, W., and Flossmann, A. I.: A numerical study of the effects of the aerosol particle spectrum on the development of the ice phase and precipitation formation, *Atmos. Res.*, 80, 15–45, doi:10.1016/j.atmosres.2005.06.007, 2006.

Levin, Z. and Yankofsky, S. A.: Contact versus immersion freezing of freely suspended droplets by bacterial ice nuclei, *J. Clim. Appl. Meteorol.*, 22, 1964–1966, 1983.

Lohmann, U. and Diehl, K.: Sensitivity studies of the importance of dust nuclei for the indirect aerosol effect on stratiform mixed-phase clouds, *J. Atmos. Sci.*, 63, 968–982, 2006.

Manninen, H. E., Bäck, J., Sihto-Nissilä, S.-L., Huffman, J. A., Pessi, A.-M., Hiltunen, V., Aalto, P. P., Hidalgo, P. J., Hari, P., Saarto, A., Kulmala, M., and Petäjä, T.: Patterns in air-borne pollen and other primary biological aerosol particles (PBAP), and their contribution to aerosol mass and number in a boreal forest, *Boreal Environ. Res.*, 19, 383–405, 2014.

Matthias-Maser, S. and Jaenicke, R.: Size distribution of primary biological aerosol particles with radii $\geq 0.2 \mu\text{m}$, *Atmos. Res.*, 39, 279–286, 1995.

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Möhler, O., Field, P. R., Connolly, P., Benz, S., Saathoff, H., Schnaiter, M., Wagner, R., Cotton, R., Krämer, M., Mangold, A., and Heymsfield, A. J.: Efficiency of the deposition mode ice nucleation on mineral dust particles, *Atmos. Chem. Phys.*, 6, 3007–3021, doi:10.5194/acp-6-3007-2006, 2006.

5 Murray, B. J., Broadley, S. L., Wilson, T. W., Atkinson, J. D., and Wills, R. H.: Heterogeneous freezing of water droplets containing kaolinite particles, *Atmos. Chem. Phys.*, 11, 4191–4207, doi:10.5194/acp-11-4191-2011, 2011.

Niemand, M., Möhler, O., Vogel, B., Vogel, H., Hoose, C., Connolly, P., Klein, H., Bingemer, H., DeMott, P., Skrotzki, J., and Leisner, T.: A particle-surface-area-based parameterization of immersion freezing on desert dust particles, *J. Atmos. Sci.*, 69, 3077–3092, 2012.

10 Paukert, M. and Hoose, C.: Modeling immersion freezing with aerosol-dependent prognostic ice nuclei in Arctic mixed-phase clouds, *J. Geophys. Res.-Atmos.*, 119, 9073–9092, doi:10.1002/2014JD021917, 2014.

Phillips, V. T. J., Donner, L. J., and Garner, S. T.: Nucleation processes in deep convection simulated by a cloud-system-resolving model with double-moment bulk microphysics, *J. Atmos. Sci.*, 64, 738–761, 2007.

Phillips, V. T. J., DeMott, P. J., and Andronache, C.: An empirical parameterization of heterogeneous ice nucleation for multiple chemical species of aerosol, *J. Atmos. Sci.*, 65, 2757–2783, 2008.

20 Phillips, V. T. J., Andronache, C., Christner, B., Morris, C. E., Sands, D. C., Bansemer, A., Lauer, A., McNaughton, C., and Seman, C.: Potential impacts from biological aerosols on ensembles of continental clouds simulated numerically, *Biogeosciences*, 6, 987–1014, doi:10.5194/bg-6-987-2009, 2009.

Pitter, R. L. and Pruppacher, H. R.: A wind tunnel investigation of freezing of small water drops falling at terminal velocity in air, *Q. J. Roy. Meteor. Soc.*, 99, 540–550, 1973.

25 Pratt, K. A., DeMott, P. J., French, J. R., Wang, Z., Westphal, D. L., Heymsfield, A. J., Twohy, C. H., Prenni, A. J., and Prather, K. A.: In situ detection of biological particles in cloud ice-crystals, *Nat. Geosci.*, 2, 398–401, doi:10.1038/ngeo521, 2009.

30 Pruppacher, H. R. and Klett, J. D.: *Microphysics of Clouds and Precipitation*, 2nd edn., Atmospheric and Oceanographic Sciences Library, 18, Springer Science & Business Media, New York, USA, 2010.

- Reid, J. S., Hobbs, P. V., Ferek, R. J., Blake, D. R., Martins, J. V., Dunlap, M. R., and Liousse, C.: Physical, chemical, and optical properties of regional hazes dominated by smoke in Brazil, *J. Geophys. Res.*, 103, 32059–32080, 1998.
- Sattler, B., Puxbaum, H., and Psenner, R.: Bacterial growth in supercooled cloud droplets, *Geophys. Res. Lett.*, 28, 239–242, 2001.
- Schmidt, S., Schneider, J., Klimach, T., Mertes, S., Schenk, L. P., Curtius, J., Kupiszewski, P., Hammer, E., Vochezer, P., Lloyd, G., Ebert, M., Kandler, K., Weinbruch, S., and Borrmann, S.: In-situ single submicron particle composition analysis of ice residuals from mountain-top mixed-phase clouds in Central Europe, *Atmos. Chem. Phys. Discuss.*, 15, 4677–4724, doi:10.5194/acpd-15-4677-2015, 2015.
- Simmel, M. and Wurzler, S.: Condensation and nucleation in sectional cloud microphysical models based on the linear discrete method, *Atmos. Res.*, 80, 218–236, 2006.
- Simmel, M., Trautmann, T., and Tetzlaff, G.: Numerical solution of the stochastic collection equation – comparison of the linear discrete method with other methods, *Atmos. Res.*, 61, 135–148, 2002.
- Simmel, M., Diehl, K., and Wurzler, S.: Numerical simulation of the microphysics of an orographic cloud: comparison with measurements and sensitivity studies, *Atmos. Environ.*, 39, 4365–4373, 2005.
- Storelvmo, T., Kristjánsson, J. E., and Lohmann, U.: Aerosol influence on mixed-phase clouds in CAM-Oslo, *J. Atmos. Sci.*, 65, 3214–3230, 2008.
- Straka, H.: *Pollen- und Sporenkunde*, Fischer Verlag, Stuttgart, 1975.
- Twohy, C. H. and Anderson, J. R.: Droplet nuclei in non-precipitating clouds: composition and size matter, *Environ. Res. Lett.*, 3, 045002, doi:10.1088/1748-9326/3/4/045002, 2008.
- van den Heever, S. C., Carrió, G. G., Cotton, W. R., DeMott, P. J., and Prenni, A. J.: Impacts of nucleating aerosol on Florida storms. Part I: Mesoscale simulations, *J. Atmos. Sci.*, 63, 1752–1775, 2006.
- v. Blohn, N., Mitra, S. K., Diehl, K., and Borrmann, S.: The ice nucleating ability of pollen. Part III: New laboratory studies in immersion and contact freezing modes including more pollen types, *Atmos. Res.*, 78, 182–189, 2005.
- Weber, D.: *Eisnukleation von Aerosolen: laborexperimente und Messung von Schiffsemissionen*, M.S. thesis, Goethe University, Frankfurt/ M., 2014.
- Wex, H., Augustin-Bauditz, S., Boose, Y., Budke, C., Curtius, J., Diehl, K., Dreyer, A., Frank, F., Hartmann, S., Hiranuma, N., Jantsch, E., Kanji, Z. A., Kiselev, A., Koop, T., Möhler, O., Nie-

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)

[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


dermeier, D., Nillius, B., Rösch, M., Rose, D., Schmidt, C., Steinke, I., and Stratmann, F.: Intercomparing different devices for the investigation of ice nucleating particles using Snomax[®] as test substance, *Atmos. Chem. Phys.*, 15, 1463–1485, doi:10.5194/acp-15-1463-2015, 2015.

- 5 Worringen, A., Kandler, K., Benker, N., Dirsch, T., Mertes, S., Schenk, L., Kästner, U., Frank, F., Nillius, B., Bundke, U., Rose, D., Curtius, J., Kupiszewski, P., Weingartner, E., Vochezer, P., Schneider, J., Schmidt, S., Weinbruch, S., and Ebert, M.: Single-particle characterization of ice-nucleating particles and ice particle residuals sampled by three different techniques, *Atmos. Chem. Phys.*, 15, 4161–4178, doi:10.5194/acp-15-4161-2015, 2015.
- 10 Yakobi-Hancock, J. D., Ladino, L. A., and Abbatt, J. P. D.: Feldspar minerals as efficient deposition ice nuclei, *Atmos. Chem. Phys.*, 13, 11175–11185, doi:10.5194/acp-13-11175-2013, 2013.
- 15 Zimmermann, F., Weinbruch, S., Schütz, L., Hofmann, H., Ebert, M., Kandler, K., and Worringen, A.: Ice nucleating properties of the most abundant mineral dust phases, *J. Geophys. Res.*, 113, D23204, doi:10.1029/2008JD010655, 2008.

ACPD

15, 16401–16460, 2015

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Table 1. Values of immersion freezing constants in Eq. (7). Based on data from (1) Wex et al. (2015); (2) Diehl et al. (2002); (3) v. Blohn et al. (2005); (4) Atkinson et al. (2013); (5) Hiranuma et al. (2015); (6) Murray et al. (2011).

particle type	a_{imm}	b_{imm}	$T_{\text{ini}}^{\circ\text{C}}$	$T_{\text{lim}}^{\circ\text{C}}$
bacteria (1)	6.41344	2.33592	−2	−9.139
tree pollen (2; 3)	7.16249	0.62053	−9	−38
grass pollen (2; 3)	9.9731	0.030301	−12	−38
feldspar (4)	2.10379	1.038	−5	−25
illite (5)	−1.77473	0.89507	−10	−37
kaolinite (6)	−4.61608	0.8881	−13	−37

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures



Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Table 2. Values of contact freezing constants in Eqs. (3) and (4). Based on data from (1) Hoffmann and Kiselev (2014), who used Snomax[®] as a proxy for bacteria and (2) Levin and Yankofsky (1983). The latter values were used in Diehl et al. (2006).

particle type and size	a_{con}	$b_{1,\text{con}}$	$b_{2,\text{con}}$	$b_{3,\text{con}}$
bacteria				
(1) $0.3 \mu\text{m} \leq d_{\text{ap}} < 0.5 \mu\text{m}$	-1.36581	-0.26367	-0.01511	-2.84911
(1) $0.5 \mu\text{m} \leq d_{\text{ap}} < 0.7 \mu\text{m}$	-0.55381	-0.10712	-0.00616	-1.16822
	a_{con}	b_{con}		
(2) $0.7 \mu\text{m} \leq d_{\text{ap}} < 2 \mu\text{m}$	-0.264	-0.742		

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Table 4. Values of deposition freezing constants a_{dep} and b_{dep} in Eq. (1) and values of lower limits of temperature T_{ini} and ice supersaturation $s_{\text{ice, ini}}$. Based on data from (1) Danielczok and Bingemer (2014); (2) Yakobi-Hancock et al. (2013); (3) Ardon-Dryer and Levin (2012).

particle type	a_{dep}	b_{dep}	T_{ini} °C	$s_{\text{ice, ini}}$ %
bacteria (1)	-12.65977	0.33382	-10 (1)	3 (1)
feldspar (2)	-14.58404	0.23576	-13 (1)	6 (1)
illite 1 (1)	-12.79648	0.15451	-13 (1)	6 (1)
illite 2 (2)	-15.11871	0.19669	-13 (1)	6 (1)
Saharan dust (3)	-13.39669	0.10058	-18 (3)	11 (3)
Asian dust (3)	-14.98495	0.09756	-15 (3)	8 (3)

[Title Page](#)
[Abstract](#)
[Introduction](#)
[Conclusions](#)
[References](#)
[Tables](#)
[Figures](#)
[Back](#)
[Close](#)
[Full Screen / Esc](#)
[Printer-friendly Version](#)
[Interactive Discussion](#)


Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Table 5. Ice water fractions from sensitivity studies with immersion freezing. Liquid clouds with IWF < 0.1, mixed-phase clouds with $0.1 \leq \text{IWF} \leq 0.9$ (in bold), ice clouds with IWF > 0.9 (in bold).

AP F_{INP} (%)	regional haze					immersion freezing				
	0.001	0.01	0.1	1	10	0.001	0.01	0.1	1	10
$\Delta T = 3 \text{ K}$ $T_{\text{fin}} = -40^\circ \text{C}$										
bacteria	0.27	0.94	0.99	1.0	1.0	0.03	0.27	0.91	0.99	1.0
pollen	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02	0.08	0.15	0.17
feldspar	< 0.01	0.12	0.74	1.0	1.0	< 0.01	0.10	0.37	0.9	1.0
illite	< 0.01	0.01	0.14	1.0	1.0	< 0.01	0.19	0.43	0.70	1.0
kaolinite	< 0.01	< 0.01	< 0.01	0.64	0.81	< 0.01	< 0.01	0.12	0.34	0.60
$\Delta T = 2 \text{ K}$ $T_{\text{fin}} = -30^\circ \text{C}$										
bacteria	0.26	0.86	0.99	1.0	1.0	0.13	0.43	0.86	0.99	1.0
pollen	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02	0.13	0.33
feldspar	< 0.01	0.02	0.21	0.71	1.0	0.08	0.34	0.56	0.80	0.93
illite	< 0.01	< 0.01	< 0.01	< 0.01	0.02	< 0.01	< 0.01	0.04	0.24	0.47
kaolinite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02	0.15
$\Delta T = 1.5 \text{ K}$ $T_{\text{fin}} = -25^\circ \text{C}$										
bacteria	0.11	0.61	0.96	1.0	1.0	0.05	0.25	0.69	0.97	1.0
pollen	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.03
feldspar	< 0.01	< 0.01	< 0.01	0.03	0.24	< 0.01	< 0.01	0.03	0.35	0.59
illite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.01
kaolinite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract Introduction

Conclusions References

Tables Figures

⏪ ⏩

◀ ▶

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Table 6. Ice water fractions from sensitivity studies with contact freezing. Liquid clouds with IWF < 0.1, mixed-phase clouds with $0.1 \leq \text{IWF} \leq 0.9$ (in bold).

AP F_{INP} (%)	contact freezing			average continental		
	regional haze	0.1	1	10	0.1	1
$\Delta T = 3 \text{ K}$ $T_{\text{fin}} = -40^\circ \text{ C}$						
bacteria	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.06
montmorillonite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.04
illite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
kaolinite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
$\Delta T = 2 \text{ K}$ $T_{\text{fin}} = -30^\circ \text{ C}$						
bacteria	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.23
montmorillonite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.12
illite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
kaolinite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
$\Delta T = 1.5 \text{ K}$ $T_{\text{fin}} = -25^\circ \text{ C}$						
bacteria	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.01
montmorillonite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
illite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
kaolinite	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Table 7. Ice water fractions from sensitivity studies with deposition freezing. Liquid clouds with IWF < 0.1, mixed-phase clouds with $0.1 \leq \text{IWF} \leq 0.9$ (in bold).

AP F_{INP} (%)	deposition freezing							
	0.01	regional haze			average continental			
	0.01	0.1	1	10	0.01	0.1	1	10
$\Delta T = 3 \text{ K}$ $T_{\text{fin}} = -40^\circ \text{C}$								
bacteria	< 0.01	< 0.01	0.05	0.52	< 0.01	0.02	0.14	0.42
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02	0.10	0.31
illite 1	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02	0.13
illite 2	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.01	0.10
Saharan dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.01
Asian dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
$\Delta T = 2 \text{ K}$ $T_{\text{fin}} = -30^\circ \text{C}$								
bacteria	< 0.01	< 0.01	< 0.01	0.06	< 0.01	0.04	0.27	0.51
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.07	0.34
illite 1	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.03	0.22
illite 2	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.01	0.11
Saharan dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	0.02
Asian dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
$\Delta T = 1.5 \text{ K}$ $T_{\text{fin}} = -25^\circ \text{C}$								
bacteria	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
feldspar	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
illite 1	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
illite 2	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
Saharan dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01
Asian dust	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01	< 0.01

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

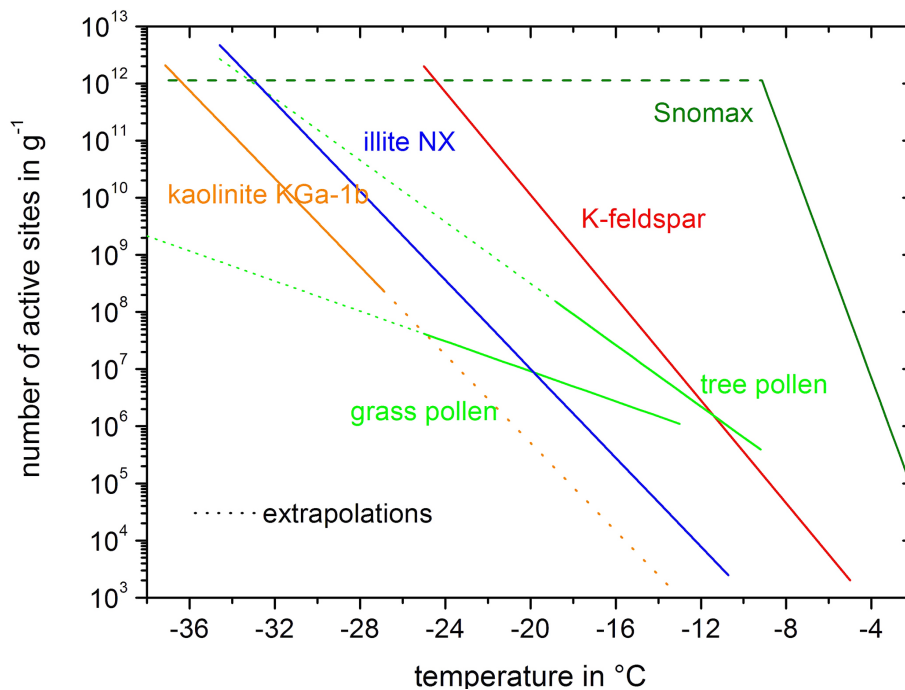


Figure 1. Numbers of active sites per unit mass as function of temperature calculated by Eq. (2) with constants given in Table 1 for various particle types.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

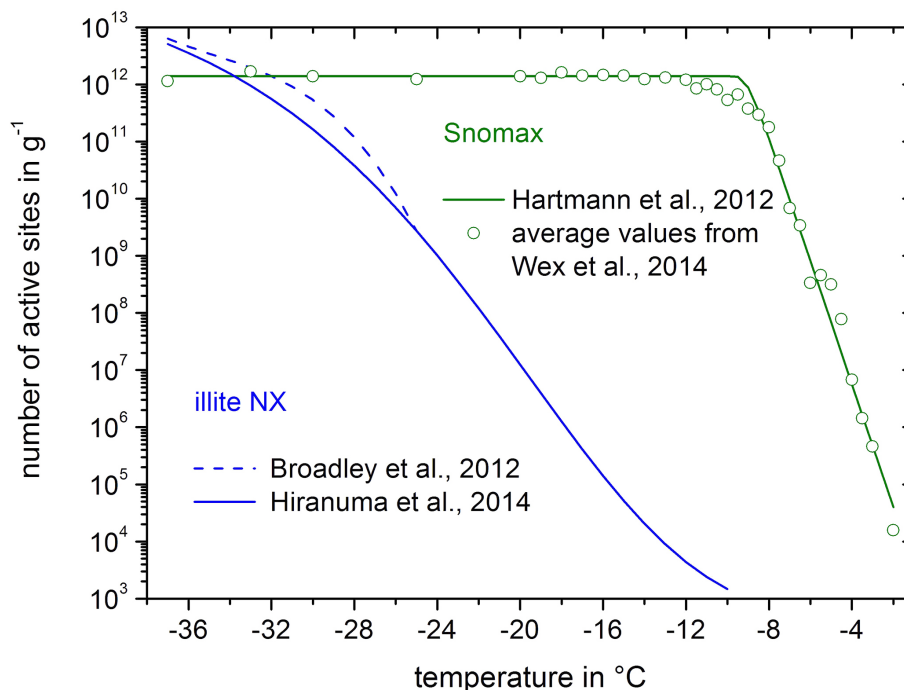
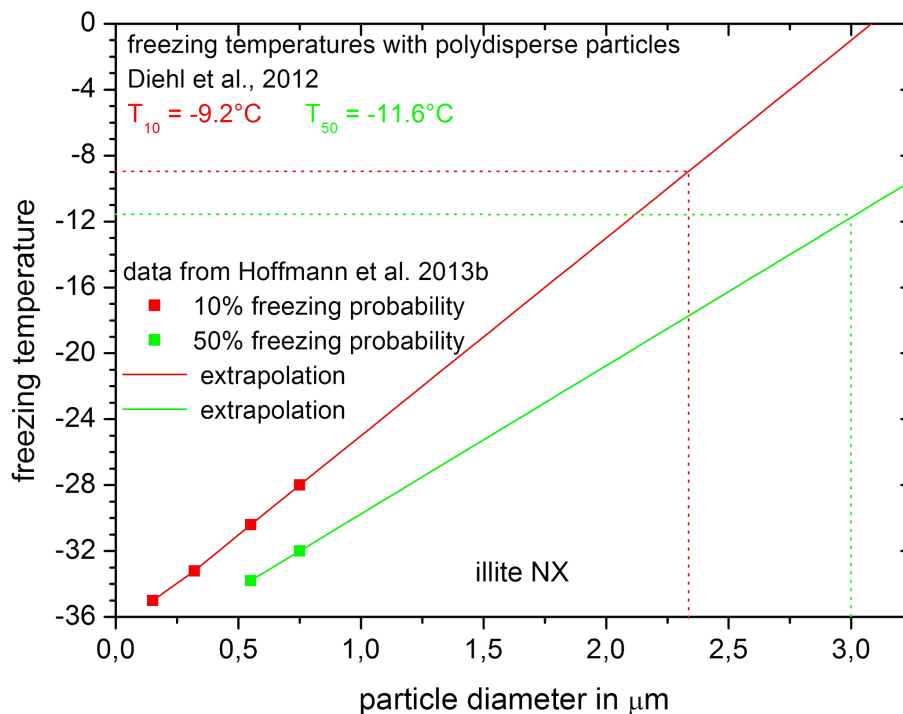


Figure 2. Numbers of active sites per unit mass as function of temperature. Parameterizations for illite NX and Snomax[®].

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

**Figure 3.** Freezing temperature as function of particle diameter for illite NX.[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

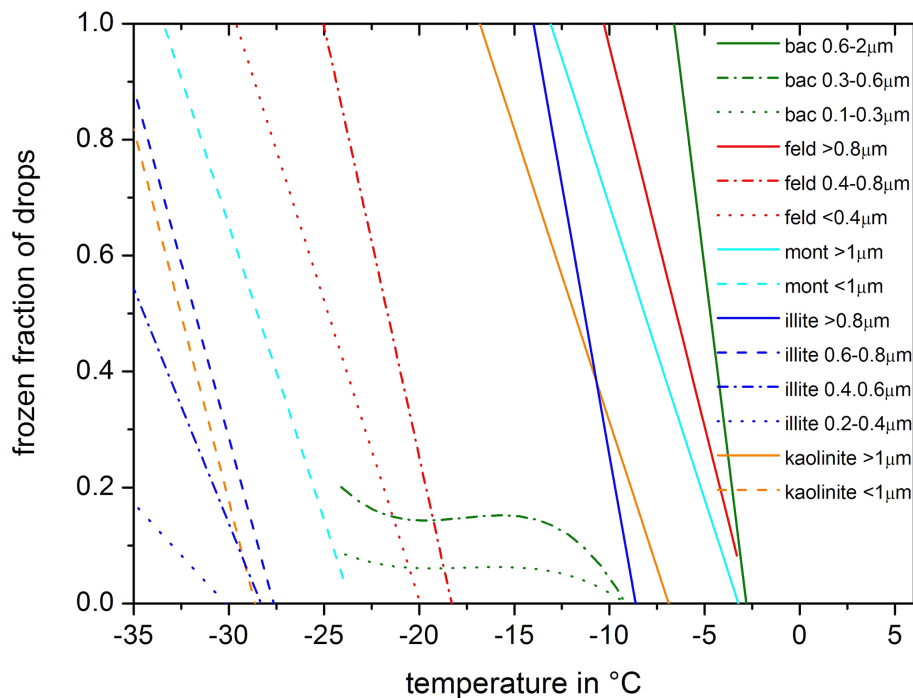


Figure 4. Frozen fraction of drops as function of temperature for various particle types and sizes, marked by different colors and line styles.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

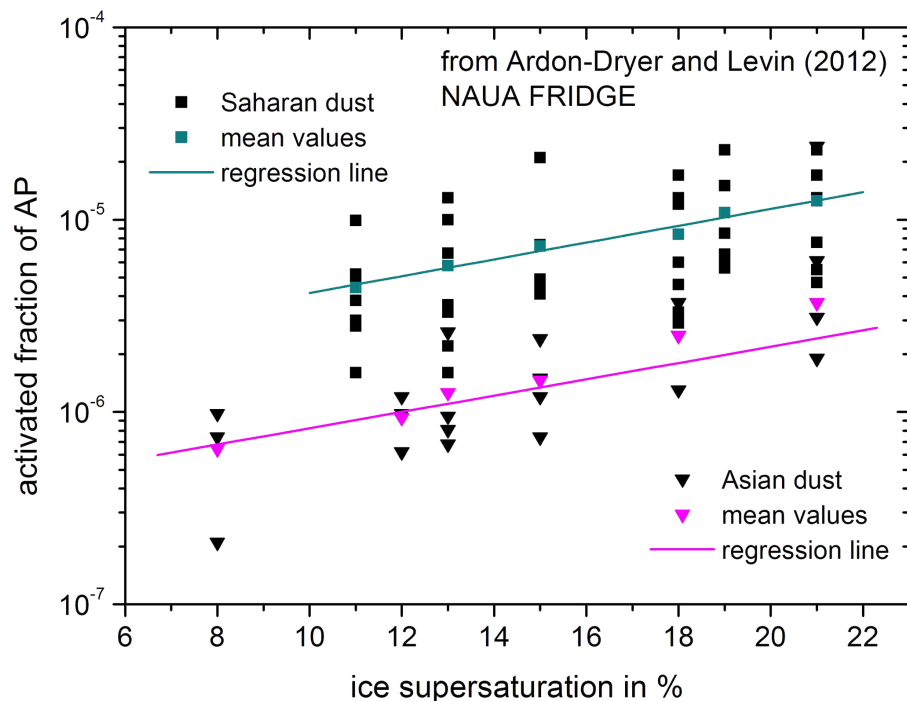


Figure 5. Activated fraction of particles as function of ice supersaturation for Saharan and Asian dust. Data from Ardon-Dryer and Levin (2012).

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

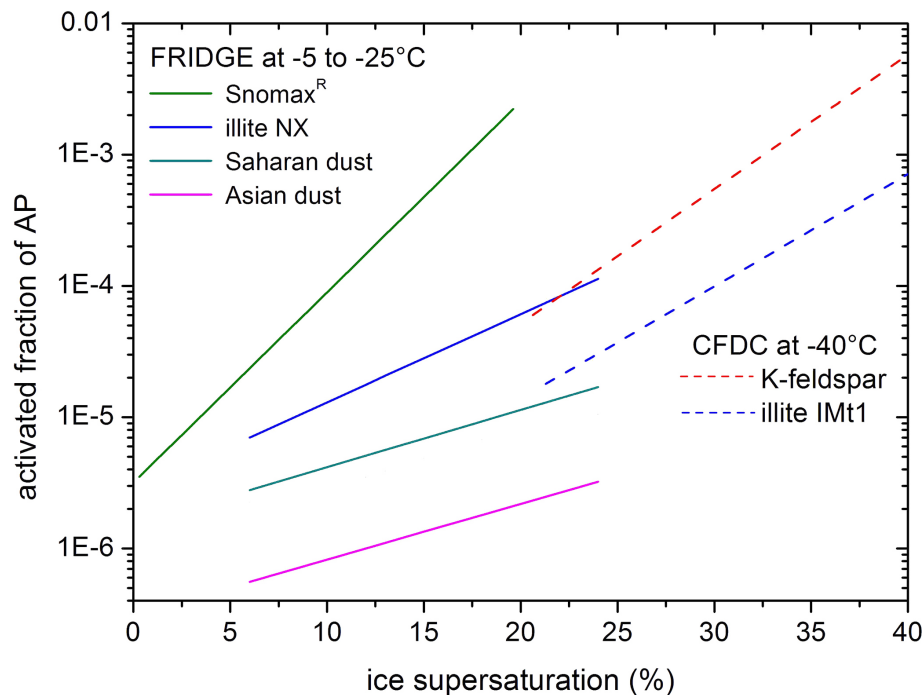


Figure 6. Activated fraction of particles as function of ice supersaturation for various particle types. Regression lines based on data from Ardon-Dryer and Levin (2012; Saharan and Asian dust), Yakobi-Hancock et al. (2013; K-feldspar and illite IMt1), Danielczok and Bingemer (2014, Snomax[®] and illite NX).

**Particle-dependent
parameterizations of
heterogeneous
freezing processes**

K. Diehl and S. K. Mitra

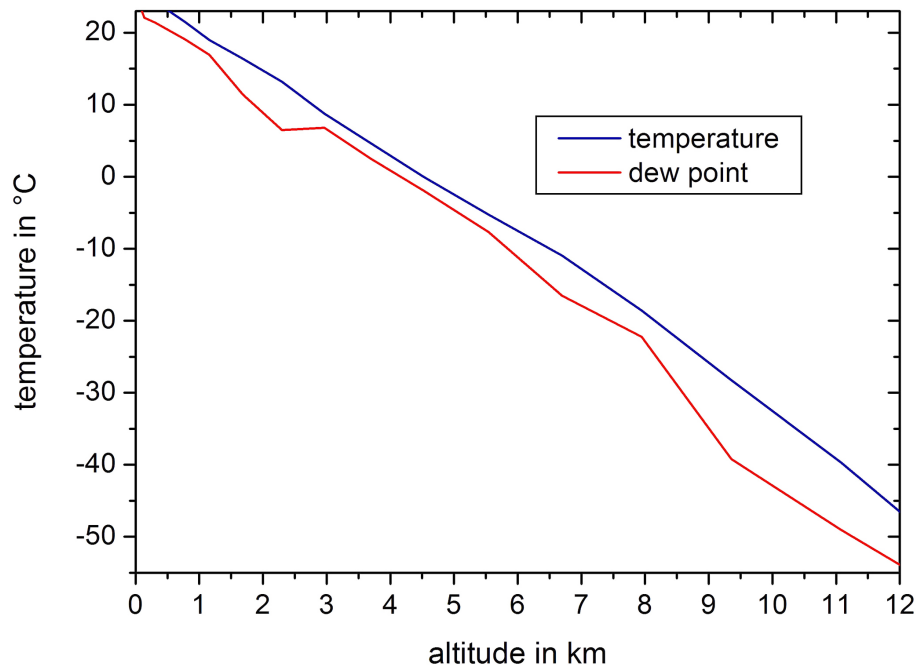


Figure 7. Development of temperature and dew point with altitude (Langmann, personal communication, 2004, REMO calculations).

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

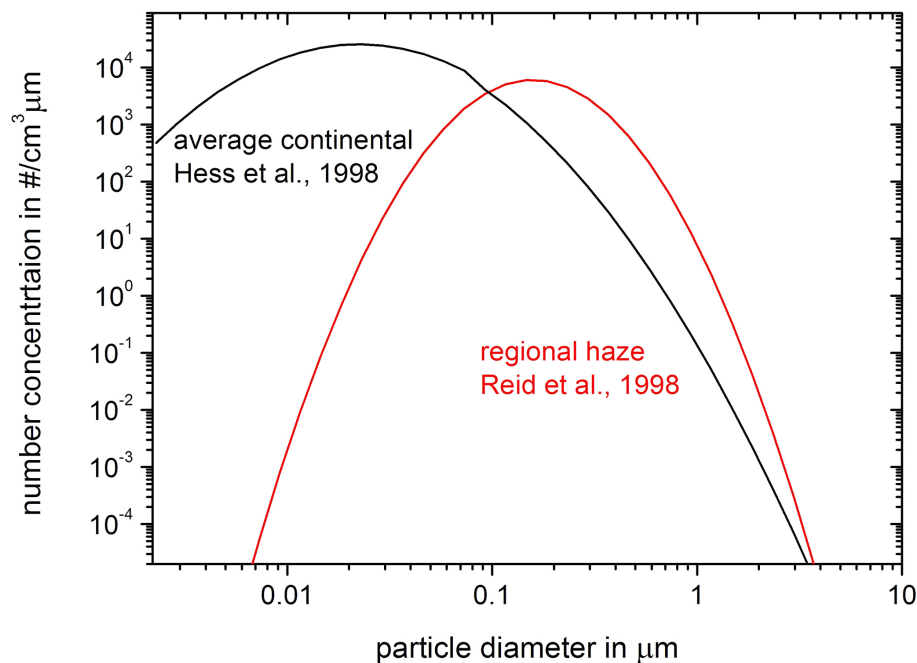


Figure 8. Initial dry aerosol particle number size distributions: number concentrations of per cm³ and μm as function of particle diameter.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

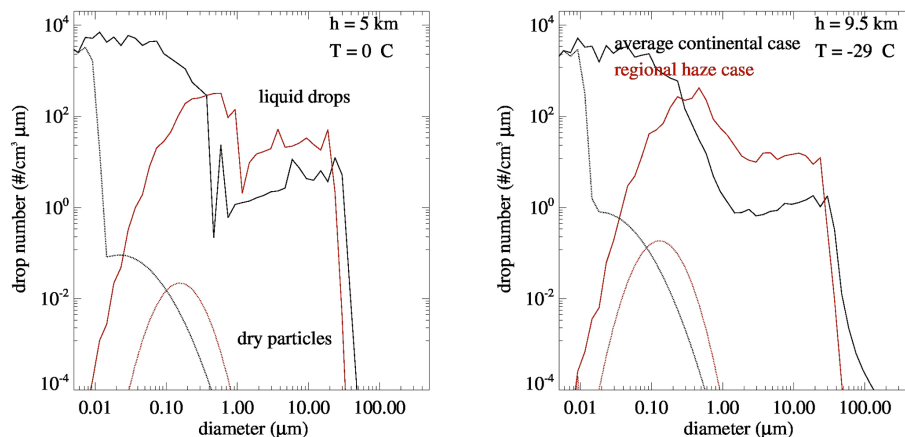


Figure 9. Results from model runs without freezing. Development of liquid drop (solid lines) and interstitial particle numbers (dotted lines) with altitude for two initial aerosol particle number size distributions, average continental (black lines), regional haze (red lines), with $\Delta T = 2$ K. Number concentrations of per cm^3 and μm as function of particle diameter.

[Title Page](#)[Abstract](#)[Introduction](#)[Conclusions](#)[References](#)[Tables](#)[Figures](#)[◀](#)[▶](#)[◀](#)[▶](#)[Back](#)[Close](#)[Full Screen / Esc](#)[Printer-friendly Version](#)[Interactive Discussion](#)

Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

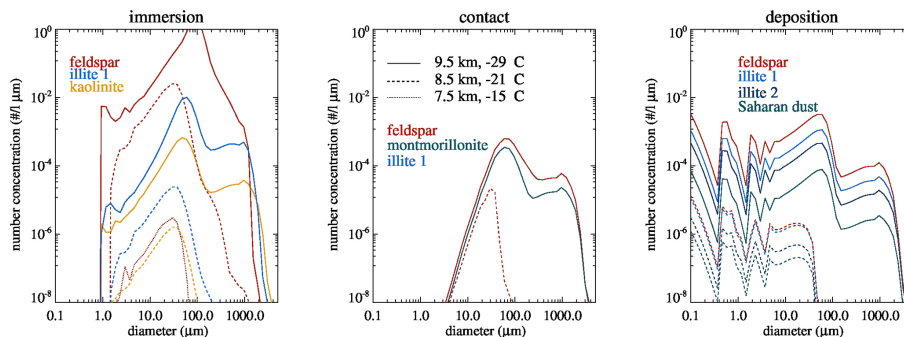


Figure 10. Development of ice particle numbers with altitude and corresponding temperature, marked by different line styles, for deposition, contact and immersion freezing. Types of INP marked by colors. Model simulations with average continental number size distribution, and with $\Delta T = 2$ K. Number concentrations of per cm^3 and μm as function of particle diameter.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

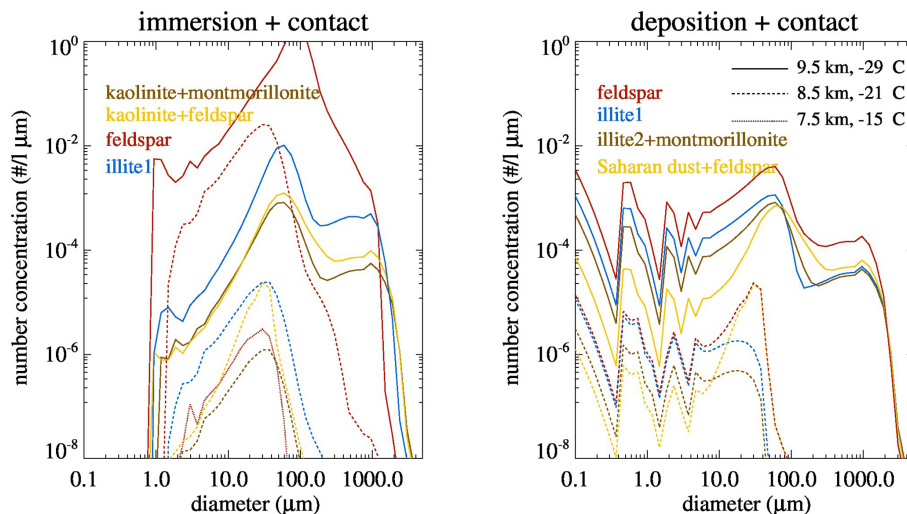


Figure 11. Development of ice particle numbers with altitude and corresponding temperature, marked by different line styles, for coupled freezing processes. Types of INP marked by colors. Model simulations with average continental number size distribution, and with $\Delta T = 2$ K. Number concentrations of per cm^3 and μm as function of particle diameter.

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Particle-dependent parameterizations of heterogeneous freezing processes

K. Diehl and S. K. Mitra

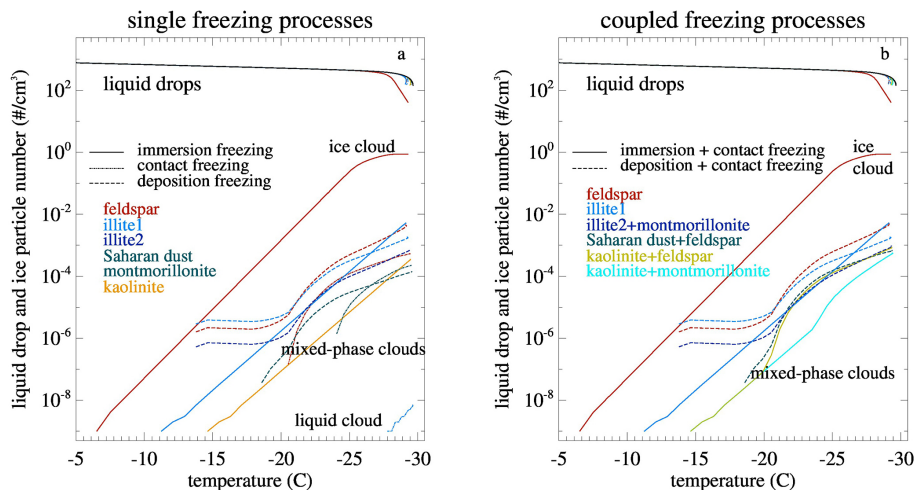


Figure 12. Total numbers of liquid drops and ice particles as function of temperature for single and coupled freezing processes which are marked by different line styles. Types of INP marked by colors. Model simulations with average continental number size distribution, and with $\Delta T = 2$ K. Numbers of per cm^3 .

Title Page

Abstract

Introduction

Conclusions

References

Tables

Figures

◀

▶

◀

▶

Back

Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

