

Response to Review #1

We thank the reviewer for his/her positive assessment of the paper and for the corrections.

Below, we provide point-by-point answers to each of the comments.

We mark the reviewers' comments/questions and the authors comments/responses by "**RC:**" and "**AC:**", respectively.

RC: Abstract: line 6. "which sufficiently well represents the IWC profiles". Shouldn't it be "which represents the IWC profiles sufficiently well"?

AC: fixed, thanks.

RC: Page 16331, lines 24–25. "AIRS footprint can up to CALIPSO L2 samples at 5km resolution". A word is missing. Should it be "can collocate with up to"?

AC: in the updated version, this part of the phrase sounds as follows: "...for favorable conditions, the AIRS footprint can cover up to three CALIPSO L2 samples at 5 km resolution and up to ten GEOPROF/DARDAR L2 samples at the spatial resolution of a CPR footprint..."

RC: Page 16337, l. 22–24. I think something happened to this sentence, as I can't make sense of it.

AC: Thanks for pointing this out. We have modified the phrase to make it readable: "As one can see from the normalized IWP histogram values presented in Table 5a and 5b, the relative frequency of thick ice cloud occurrence is higher in single- rather than in multi-layer system".

Response to Review #3

We thank the reviewer for his/her analysis and helpful suggestions.

Below, we provide point-by-point answers to each of the comments/questions.

We mark the reviewers' comments/questions and the authors comments/responses by “**RC:**” and “**AC:**”, respectively.

1. Specific comments/questions

RC: p 16329 l. 11-13: In this paragraph you state that CALIPSO measure also thin clouds. For example in a paper by Davis et al. 2010 it is shown that CALIPSO miss a significant fraction of sub-visible cirrus clouds ($OD < 0.03$) in the CALIPSO L2 cloud product. Especially in the tropics a large amount of sub-visible cirrus clouds occur, which have a radiative impact. Parts of these clouds and their IWC profiles are most likely not included in your analysis. I would suggest to write a short sentence, where you state that CALIPSO could underestimate sub-visible clouds and cite e.g. Davis or other.

AC: We agree with this comment. However, since we use a joint colocated database, the filtering is done using the “logical AND” condition, so if any of the contributors (AIRS, DARDAR, CALIPSO, GEOPROF) does not mark the scene as a cloud, it is excluded from the consideration. In this dataset, AIRS is known to be less sensitive to thin cirrus than CALIPSO, so the filtering of aforementioned sub-visible cirrus clouds is automatic. The properties and statistics of a joint colocated product are discussed in Sect. 3.1. As the reader knows by the end of the paper, all radiative effects related to IWC vertical profile are negligible for thin clouds, and there is no need for additional discussion on cloud filtering, so we have modified only the text of the paragraph and added the reference to Davis et al., 2010.

RC: p.16332 l. 3-7 and Table 2: In this paragraph you describe the amount of selected data. In the later analysis you use latitudinal averages of different ice cloud variables. Therefore the question, if there is any latitudinal dependence on the data coverage with some poorly covered regions? Can you please comment on this?

AC: Since the instruments share the same orbit and the geometry of the observations does not change, the coverage does not change with latitude, either (except for the very poles). However, filtering out the clear sky scenes and sub-visible cirrus clouds leads to changes in latitudinal coverage of the product we analyze. It becomes modulated by the cloud cover and the detection threshold, and the joint effect is roughly equal to IWP modulation (areas with large IWP are taken more often than the dry ones). Still, the number of cases under consideration for each latitude remains large (on the order of hundreds per month per 1-degree belt) and the observed picture remains representative.

RC: p. 16337 l. 4: Cirrus formation mechanism are not only by in-situ formation and anvil cirrus. Warm conveyor belts (with relative slow updraft) can also produce completely frozen ice clouds from the mixed phase regime in the cirrus altitude range (e.g. Spichtinger et al. 2005). Maybe you add an "e.g." in the bracket or list more formations mechanism.

AC: We opted to add “e.g.”, thanks for pointing this out.

RC: p. 16337 l. 11-12: You used the best fit of the four shapes for the ice water profiles in your analysis. Could all observed profiles assigned clearly to one profile or are there some shapes which are not or hardly be represented by your set of the four shapes?

AC: This is a good point. The closest shape selection algorithm always makes its choice based on the r.m.s. of the deviation between the model IWC profile and the real one, and for the sake of simplicity we do not provide the analysis of the goodness-of-fit for the cloud types w.r.t. their IWP

or geometrical thickness. Indeed, some of the DARDAR shapes show a zig-zag-like structure like the one in Fig. 2a or Fig. 5d and it's obvious that fitting these profiles with a model one will give worse r.m.s. of the deviation than, for example, that of Fig. 5e. Still, all IWC profiles fit well into one of the 4 patterns: increasing top-to-base, increasing base-to-top, constant, or "high middle fading to the edges". As one can see in the Table 4, other shapes we tested are linearly dependent with one of 4 shapes and introducing wave-like profiles is impossible due to their variety.

RC: -p. 16338 l. 18-25: Aggregation in cirrus plays only a role in warm cirrus or completely frozen mixed phase clouds at $T > -40^{\circ}\text{C}$ (see Kienast-Sjogren et al. 2013). I would explain the lower triangle in downdraft regions in another way. The top of cirrus clouds is mostly known as cirrus formation region with small ice crystals. In case of a downdraft the whole cloud becomes sub-saturated and the small ice crystals at the top sublime much faster than the lower parts with larger crystals increasing the amount of lower triangle cases. In addition, I don't like the explanation with the wash out of particles in a large updraft. In large updrafts homogeneous freezing is triggered and a lot of small ice crystals appear (see Kärcher et al. 2002) within the whole cloud. Because the whole cloud consists of small particles which need more time to grow to larger sizes, the probability to find upper and lower triangles profiles is reduced.

AC: Thanks for a very reasonable suggestion – we have made it the first explanation and left the one given by us as a second one, accompanied by a reference to (Kienast-Sjogren et al. 2013). As for the updrafts, we have updated the text in accordance with the mechanism suggested in the comment.

RC: -p. 16339 l. 18: In this paragraph you describe the common understanding of ice nucleation. The general understanding of the term "ice nuclei" means insoluble particles which triggers heterogeneous freezing. For homogeneous freezing, predominantly happens at temperature below -40°C , supercooled water droplets are responsible for ice formation. There I would recommend to avoid using the word "ice nuclei".

AC: We agree with this comment. On the other hand, one should not exclude the heterogeneous mechanism from this description, so we have specified the conditions for heterogeneous freezing in the text.

RC: p. 16339 l. 19: Clustering (see comment above) happens only in warm cirrus. In in-situ cirrus the number concentrations are usually not high enough to cluster ice particles. In this case the ice crystals grow only by water uptake in super-saturation regions to sizes where they start to sediment.

AC: We have replaced the word "clustering" with "growing".

2. Technical comments

RC: p. 16336 l. 21-22: From Figure 6a I cannot confirm the $k_{ab}=1.1$ value for $\text{IWP} < 10\text{gm}^{-2}$. For me it looks more like 1.2 for $\text{IWP} < 10\text{ gm}^{-2}$ or 1.1 for $\text{IWP} < 2\text{ gm}^{-2}$. I suggest to correct the number in the text.

AC: This is correct. We have modified the text and included both IWP limits.

RC: Table A1: The acronym LWC (liquid water content) is missing in the table.

AC: Fixed, thanks.

RC: Figure 2: Maybe add the location of each profile in the header

AC: We have added the latitude / longitude values to figure caption. All examples correspond to tropical latitudes and the selection was done solely on the closeness to even numbers (10, 30, 100, 300 g/m^2) for illustration purposes.

Ice Water Content Vertical Profiles of High-level Clouds: Classification and Impact on Radiative Fluxes

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Abstract

In this [workarticle](#), we discuss the shape of ice water content (IWC) vertical profiles in high ice clouds and its effect on radiative properties of these clouds, both in short- and in long-wave bands (SW and LW). Based on the analysis of colocated satellite data, we [suggestpropose](#) a minimal set of primitive shapes (rectangular, isosceles trapezoid, lower and upper triangle), which [sufficiently well](#)—represents the IWC profiles [sufficiently well](#). About 75% of all high-level ice clouds ($P < 440$ hPa) have an ice water path smaller than 100 g/m^2 , with a 10% smaller contribution from single layer clouds. Most IWC profiles (80%) can be represented by a rectangular or isosceles trapezoid shape. However, with increasing IWP, the number of lower triangle profiles (IWC rises towards cloud base) increases, reaching up to 40% for IWP values greater than 300 g/m^2 . The number of upper triangle profiles (IWC rises towards cloud top) is in general small and decreasing with IWP, with the maximum occurrence of 15% in cases of IWP less than 10 g/m^2 . We propose a statistical classification of the IWC shapes using ice water path (IWP) as a single parameter. We have estimated the radiative effects of clouds with the same IWP and with different IWC profile shapes for five typical atmospheric scenarios and over a broad range of IWP, cloud height, cloud vertical extent, and effective ice crystal diameter (D_e). We explain changes in outgoing LW fluxes at the top of the atmosphere (TOA) by the cloud thermal radiance while differences in TOA SW fluxes relate to the D_e vertical profile within the cloud. Absolute differences in net TOA and surface fluxes associated with these parameterized IWC profiles instead of assuming constant IWC profiles are in general of the order of $1\text{--}2 \text{ W/m}^2$: they are negligible for clouds with $\text{IWP} < 30 \text{ g/m}^2$, but may reach 2 W/m^2 for clouds with $\text{IWP} > 300 \text{ g/m}^2$.

1 Introduction

Clouds play an important role in the energy budget of our planet: optically thick clouds reflect the incoming solar radiation, leading to cooling of the Earth, while thinner clouds act as “greenhouse films”, preventing escape of the Earth’s long-wave (LW, see also Acronyms section for the abbreviations not explained in the text for readability’s sake) radiation to space. Understanding the Earth’s radiative energy budget requires knowing the cloud cover, thermodynamic phase (ice, liquid, mixed phase), height, temperature, and thickness, as well as the optical properties of cloud particles and their concentration. In this article, we address the shape of the ice water content profile, $IWC(z)$, for high ice clouds (defined by pressure less than 440 hPa and including only ice particles).

Satellite observations provide a continuous survey of clouds over the whole globe. IR sounders have been observing our planet since 1979: from the TOVS sounders (Smith et al., 1979) onboard the NOAA polar satellites to the AIRS spectrometer (Chahine et al., 2006) onboard Aqua (since 2002) and to the IASI interferometers (Chalon et al., 2001; Hilton et al., 2012) onboard MetOp (since 2006), with increasing spectral resolution. Their spectral resolution along the CO_2 absorption band makes IR sounders sensitive to cirrus, day and night (Stubenrauch et al., 1999, 2006, 2008, and 2010; Wiley et al., 2005). In addition, they provide atmospheric temperature and water vapor profiles, surface temperature, and dust aerosol properties. Vertical profiles of the cloud parameters are available from active sensors: since 2006, the CALIPSO lidar (Winker et al., 2003) and CloudSat radar (Stephens et al., 2002), together, observe the atmosphere. Whereas the lidar is highly sensitive and can even detect sub-visible cirrus, its beam reaches cloud base only for clouds with an optical depth less than 3. When the optical depth is larger, the radar is still capable of penetrating the cloud down to its base. The LiDARraDAR products (DARDAR, Delanoë and Hogan, 2010), retrieved from these radar and lidar measurements, provide vertical profiles of thermodynamic cloud phase, $IWC(z)$ and $De(z)$ with a fine vertical resolution, essential for our analysis.

The structure of the article is as follows. In Section 2, we describe the datasets used in this study and the collocation approach. Section 3 presents the statistical results of the colocated data and describes the classification into different types of ice cloud profiles and their occurrence in dependence of different atmospheric parameters. In Section 4, we estimate the radiative effects on the $IWC(z)$ profile shape. Section 5 summarizes the [paper results](#).

2 Datasets

The analysis builds on the synergy of the NASA Afternoon Constellation (A-Train) mission (Stephens et al., 2002), providing observations at 01:30 and 13:30 local time (LT), at the equator crossing. Table 1 lists the Level 2 datasets and the specific variables used in this analysis. The following subsections provide brief information on the corresponding instrument, and retrieval methodology.

2.1 AIRS-LMD cloud properties

The spatial resolution of the AIRS measurements is 13.5 km at nadir. Nine AIRS measurements (3×3), called a "golf ball" (see grey circles in Fig. 1), correspond to one footprint of the Advanced Microwave Sounder Unit (AMSU). NASA AIRS L2 standard products include atmospheric temperature and water vapor profiles as well as surface skin temperature and ice / snow flag (Susskind et al., 2003, 2006, Chahine et al., 2006) at the spatial resolution of an AMSU footprint. The AIRS-LMD cloud retrieval makes use of these products as ancillary data and has been described in (Stubenrauch et al., 2010). Briefly, the retrieval methodology is based on a weighted χ^2 method using radiances measured along the wing of the $15 \mu\text{m}$ CO_2 absorption band. The χ^2 method determines the cloud pressure level (p_{cld}), for which the measured radiances provide the most coherent cloud emissivity. The method also yields IR cloud emissivity defined as $\epsilon_{\text{cld}} = (I_{\text{clear}} - I_{\text{meas}}) / (I_{\text{clear}} - I_{\text{cld}}(p_{\text{cld}}))$, where I_{meas} is the measured radiance, I_{clear} is the clear sky radiance and I_{cld} the radiance of an optically thick cloud at the p_{cld} level estimated for the observed situation from a minimum in the χ^2 vertical profile. The AIRS-LMD dataset participated in the GEWEX cloud assessment (Stubenrauch et al., 2012, 2013) and showed a good performance. In the case of multiple cloud layers, the retrieved properties correspond to those of the highest cloud layer, as far as its optical depth is above 0.1.

2.2 CALIPSO cloud data at 5 km spatial resolution

CALIOP, a two-wavelength polarization-sensitive nadir viewing lidar, provides high-resolution vertical profiles of aerosols and clouds. It uses three receiver channels: one measuring the 1064 nm backscatter intensity and two channels measuring orthogonally polarized components of the 532 nm backscattered signal. Cloud and aerosol layers are detected by comparing the measured 532 nm signal return with the return expected from a molecular atmosphere. The method utilizes an adaptive threshold test (Vaughan et al., 2009) and retrieved the height of the physical top height,

rather than the effective radiative height. ~~Remarkably, the~~The method is capable of detecting the clouds with visible extinction as small as $\sim 0.01 \text{ km}^{-1}$ though the detection efficiency decreases in this domain and, as Davis et al., (2010) have shown, the CALIPSO misses a certain fraction of sub-visible cirrus clouds. The retrieval algorithm is the same for the daytime and nighttime portions of the orbit, except that different detection thresholds are used for day and night. Analysis of the parallel and perpendicular polarization of 532 nm backscatter signals provides vertically-resolved identification of cloud water phase according to the algorithm of Hu et al., (2007). For this analysis, we utilize z_{top} and z_{base} from version 3 of the CALIPSO L2 cloud data averaged to 5 km along the track (release v.3.01).

2.3 CloudSat Geometrical Profiling Product (GEOPROF)

The GEOPROF L2 product (Haynes and Stephens, 2007; Haladay and Stephens, 2009; Mace et al., 2009) of version P1_R04 merges the millimeter wavelength cloud profiling radar (CPR) radar data (footprint of 2.5 km x 1.4 km) with those collected by CALIOP. CloudSat shares an orbit with CALIPSO, so that they probe nearly the same volumes of the atmosphere within 10–15 s of each other. This configuration combined with the capacity for millimeter radar to penetrate optically thick hydrometeor layers and the ability of the lidar to detect optically thin clouds has allowed Mace et al., (2009) to develop an approach for retrieving the vertical and horizontal structure of hydrometeor layers with unprecedented precision, ranging from optically thin cirrus and boundary layer clouds to deep optically thick precipitating systems. In this study, the GEOPROF product helps us to verify if the cloud base height for the selected overlap is consistent with the IWC profile provided in the DARDAR dataset (see next section) and use the z_{top} values to "align" the IWC(z) profiles for the classification (Sect. 3.2).

2.4 Lidar-Radar synergy of the DARDAR dataset

Delanoë and Hogan (2010) have adapted a variational method using the synergy of radar, lidar, and infrared radiometer from airborne and ground-based measurements (Delanoë and Hogan, 2008) to CALIPSO-CloudSat-MODIS satellite observations to retrieve vertical profiles of visible extinction coefficient, IWC, and D_e . The variational scheme finds a state vector \mathbf{x} , which minimizes the square-root-sum of the differences between the observed (\mathbf{y}) and calculated radiances. The components of the observation vector \mathbf{y} are: radar reflectivity factor, apparent lidar backscatter as well as IR radiance and IR radiance difference if the radiometer is used. Note that in the version we are using the IR radiances are not assimilated. The components of \mathbf{x} are the visible extinction

coefficients at different altitudes, extinction-to-backscatter ratio, and number concentration parameters at different altitudes.

The solution (state vector \mathbf{x}) is found by minimizing a cost function using Gauss–Newton iteration, as described fully by Delanoë and Hogan, (2008). A key input to the retrieval algorithm is an observational error covariance matrix, which includes both instrument and forward–model errors (Delanoë and Hogan, 2008, 2010). The resulting DARDAR (for liDAR+raDAR) products contain the profiles of the ice cloud related parameters on a 60 m vertical grid, which have been used in a number of studies (Bardeen et al., 2013; Battaglia and Delanoë, 2013; Ceccaldi et al., 2013; Delanoë et al., 2011, 2013; Deng et al., 2012, 2013; Eliasson et al., 2012; Faijan et al., 2012; Gayet et al., 2014; Huang et al., 2012; Jouan et al., 2012, 2014; Maso et al., 2015; Stein et al., 2011a,b).

2.5 ERA-Interim

ERA-Interim global atmospheric reanalysis is produced by the European Centre for Medium-Range Weather Forecasts (ECMWF), covering the period from 1989 until now. Dee et al., (2011) give a detailed description of the approach and the data. The data assimilation scheme is sequential: at each time step, it assimilates available observations to constrain the model built with forecast information obtained in the previous step. The analyses are then used to make a short-range model forecast for the next assimilation time step. Gridded data products (at a spatial resolution of 0.75° latitude \times 0.75° longitude) also include 6-hourly dynamic parameters such as horizontal and vertical large-scale winds. A common proxy for the intensity of the vertical motions in the atmosphere is the vertical pressure velocity at 500 hPa level, w_{500} (e.g. Bony and Dufresne, 2005, Martins et al., 2011). In addition, we also use vertical winds just underneath the cloud (w_{base}) and at the radiative height of the cloud (w_{cloud}) to study correlations between the shape of the cloud IWC profile and the atmospheric dynamics.

2.6 Colocation of the datasets

Fig. 1 illustrates a typical single-day coverage of AIRS and CALIPSO-CloudSat at a specific observation time (1h30PM at the equator crossing time). Whereas the AIRS swaths cover areas about 1000 km, the active instruments only cover a 90 m – 1.4 km wide track near the middle of the AIRS swaths. Since the instruments share the same orbit, one can impose strict overlapping criteria to get a high-quality dataset.

Our colocation starts with the AIRS data and searches the other datasets for the observations closest to the centers of individual AIRS footprints (usually, [3three](#) per each golf ball). A blown-up part in the upper-right corner of Fig. 1 shows an example of the overlapping measurements: for favorable conditions, the AIRS footprint can [cover](#) up to [3three](#) CALIPSO L2 samples at 5 km resolution and up to [10ten](#) GEOPROF/DARDAR L2 samples at the spatial resolution of a CPR footprint (1.7x1.4 km). One has to keep in mind that “ideal” overlaps like the one shown in Fig. 1 are not so frequent: if the closest CALIPSO or DARDAR footprint lies outside the AIRS footprint, then the case is skipped.

Table 2 complements Fig. 1 and shows the statistics for the components of the colocated dataset. As one can see, with the rigid colocation criteria used in this work the average distance between the centers of the samples is about 6 km. The fraction of the data selected is small, but the number of overlaps per day is still on the order of $\sim 1 \cdot 10^4$. The temporal deviation between the observations is defined by the distance between the satellites and is less than 2 minutes. The ERA-Interim atmospheric reanalysis deviates on average much more because of its rather coarse spatial and time resolution. The resulting colocated dataset comprises the variables listed in Table 1.

3 Analysis

3.1 Selecting high-level ice clouds

Fig. 2 illustrates the information available in the colocated dataset, for typical examples of high-level ice clouds, with IWP increasing from 9.0 g/m² to 303 g/m². In this figure, we supplement the IWC vertical profiles with ~~the~~ AIRS z_{cld} (horizontal red lines), CALIPSO z_{top} and z_{base} (blue lines), and GEOPROF z_{top} and z_{base} (green lines). It is interesting to trace the behavior of these values with changing IWP: whereas CALIPSO and GEOPROF z_{top} match on all four panels, [CALIPSO](#) and GEOPROF z_{base} match at IWP < 100 g/m² while the CALIPSO lidar cannot probe the lower boundary of thicker clouds; AIRS z_{cld} corresponds to the radiative height close to the maximum backscatter signal from CALIPSO (Stubenrauch et al., [20122013](#) 2010); for high-level ice clouds it lies in general 1 to 2 km below cloud top, depending on the vertical accumulation of optical depth (Liao et al., 1995; Holz et al., 2008); it seems to correspond to the IWC peak height up to IWP of about 30 g/m² while for thicker clouds the corresponding optical depth is already reached earlier. We explain all these features by the capabilities of the instruments and by physics of observations, and we find them consistent with the results presented elsewhere (e.g. Stubenrauch et al., [20122013](#) and references therein). For the analysis, we have selected only high ice clouds, using AIRS cloud

pressure ($p_{\text{cld}} < 440$ hPa) and DARDAR profile information on the occurrence of liquid or ice. To ensure high quality of the selected subset, we filtered out the cases, for which DARDAR ice cloud peak height is beyond the GEOPROF z_{top} and z_{base} limits of the layer, ~~which is the closest one~~ to the AIRS cloud. This removes 18% of the colocated data, and the mismatches are explained by different spatial resolution of the compared datasets, by the uncertainties of $p_{\text{cld}} \rightarrow z_{\text{cld}}$ conversion associated with temperature/H₂O profiles, and by the GEOPROF cloud boundary thresholds.

Figure 3 shows the comparison of height for all high ice clouds in the colocated and filtered dataset. In Fig. 3a, we compare the AIRS cloud height with the DARDAR IWC(z) peak height. As one can see, for clouds above ~ 10 km the highest probability density (in red) almost follows [a](#) 1:1 line while for the lower clouds AIRS tends to be $\sim 2\text{--}3$ km higher. This is linked to the optical thickness of the cloud and its correlation with the vertical extent: for [geometrically](#) thicker clouds, AIRS retrieves [the](#) radiative height while active instruments are capable of penetrating deeper. In Fig. 3b, AIRS cloud height is compared with the CALIPSO top: 80% of the clouds are below the CALIPSO cloud top boundary: we assign the remaining 20% to difference in sample size of these two instruments (5 km x 0.06 km vs 15 km x 15 km) and to accuracy in AIRS cloud height determination (1 km). The purpose of Fig. 3c is to show the spread of the IWC(z) profile within the cloud: for the clouds peaking in the 8–13 km region, their z_{top} is usually just 1 km higher than the peak; however, the distribution is broad and for a significant fraction of clouds [with smaller emissivity](#) the IWC(z) [peakmaximum](#) is much lower than the z_{top} . This is consistent with the AIRS versus DARDAR peak plot in Fig. 3a: the IWC peak of extended cloud layers is closer to cloud base.

Figure 4 presents average cloud emissivity and vertical extent in relation to IWP. As one can see, average IR cloud emissivity increases with IWP and then saturates at $\sim 0.7\text{--}0.9$ for IWP values greater than ~ 100 g/m². However, for the same large IWP the mean is smaller in winter midlatitudes than in summer midlatitudes. It is interesting to note the peculiarity of $\varepsilon(\text{IWP})$ curves in the low IWP domain (Fig. 4a,c) where ε increases for IWP values less than $\sim 4\text{--}7$ g/m². One has to keep in mind that the same amount of water can form clouds of different optical depths (and emissivities): for thin clouds, the ice crystal size distribution centers around lower values compared to that of thicker clouds. We justify this explanation by building the $\varepsilon(\text{IWP})$ distributions only for $De > 40$ μm (not shown for the sake of clarity): these distributions do not have a feature at $\text{IWP} \approx 4\text{--}7$ g/m²; instead, the $\varepsilon(\text{IWP})$ increases monotonically and then reaches saturation. The relationship between the vertical extent of the ice cloud (Δz_{cld}) and its IWP is shown in Fig. 4b,d. Here one has to note the difference between the summer and winter hemispheres: both single and

multi-layer clouds show a saturation of Δz_{cld} in the winter hemisphere at $\text{IWP} \approx 70 \text{ g/m}^2$ that corresponds to higher ice water densities in the storm tracks. Another remarkable feature of the $\Delta z_{\text{cld}}(\text{IWP})$ is a nearly linear dependence on $\log(\text{IWP})$ (with the exception for aforementioned saturation effects in winter hemispheres). This allows reducing the number of variables in the statistical classification we seek to develop.

Table 3 shows the latitudinal behavior of cloud emissivity, IWP, vertical extent and proportion of ice within the cloud, separately for single-layer and multi-layer cloud scenes (identified by GEOPROF). We draw the readers' attention to two types of IWP values in Table 3: median and mean IWPs. The median IWPs are calculated over the ensemble of corresponding cloudy scenes while the mean IWPs represent both cloudy and clear sky scenes together. The latter distribution shows a common three-peak pattern (c.f. Eliasson et al., 2011) while the median values are more representative for strongly skewed distributions, which is the case of the IWP. As one can see, single layer high clouds are thicker both in geometrical and in optical sense. One can note the following differences: a) median IWP values differ stronger than cloud emissivities that is related to cloud emissivity saturation for thick clouds; b) the vertical extent Δz_{cld} of single layer clouds is $\sim 0.7 \text{ km}$ larger than that of top ice clouds in multi-cloud scenes; c) the geometrical ratio of ice layer thickness w.r.t. total layer thickness ($\Delta z_{\text{ice}}/\Delta z_{\text{cld}}$) is larger for single layer clouds. We associate the latter difference with multi-layer mixed-phase clouds, for which the conditions at the lower boundary of high ice cloud are favorable for changing the phase from ice to water.

3.2 Approximating the ice water content profiles with primitive shapes

We have analyzed the IWC profiles with respect to cloud IWP, vertical extent, latitude, and atmospheric dynamics. The objectives of this analysis [were are](#): a) establishing a minimal basis of primitive shapes, which one can use for approximating $\text{IWC}(z)$, b) building a statistical model for these primitive profiles, and c) estimating the energetic effects of clouds with the same ice water path (IWP), but different $\text{IWC}(z)$. A "minimal basis" in this context means that the individual elements of the suggested set of IWC profiles should not be linearly dependent with respect to any of the atmospheric and cloud variables. We have "aligned" the IWC profiles using the GEOPROF z_{top} values, calculated the vertical extent of the ice cloud using the GEOPROF z_{base} and z_{top} values, determined the IWP by integrating the DARDAR $\text{IWC}(z)$ within these limits, normalized the IWC profiles to IWP, and compared them with a set of primitive shapes. An initial set of shapes consisted of: (1) "rectangular" or constant IWC; (2) "upper triangle"; (3) "isosceles triangle"; (4) "tilted triangle"; (5) "lower triangle"; (6) "trapezoid"; and (7) "isosceles trapezoid", illustrated in

Fig. 5a. The "tilted triangle" was built using the average top-to-peak and base-to-peak IWC(z) gradients normalized by the IWP. The other shapes are empirical approximations. It is important to note here that using a fixed set of profile shapes does not mean using the same IWC gradient within the same type: the real IWC values are always bound to the IWP of the cloud through normalizing.

To check the redundancy within these seven primitive profile shape types, we have used the statistics built over the globe for one month, January 2007 (the results do not change significantly for any other period). For each colocated event and for each primitive shape, we have calculated ζ , a standard r.m.s. of the model IWC profile deviation from the real IWC(z) profile. As a result, we have obtained seven sequences of ζ values and performed a "round robin" correlation analysis of these sequences. As the linear correlation coefficients in Table 4 show, a set of seven profile shapes appears to be redundant since some pairs of profile shapes are strongly correlated, with the correlation coefficients of about 0.8–0.9 (marked in bold), so it is logical to reduce the basis. The first profile to keep is a standard one (rectangular), which is approximated by a constant-within-layer IWC and which corresponds to an assumption currently used in the retrieval of cirrus bulk microphysical properties (e.g. Guignard et al., 2012). The profiles #2 (upper triangles) and #5 (lower triangles) are uncoupled from the others, so they should also be included to a reduced basis. In addition, we keep shape #7, which fills a gap between #2 and #5 and which is more physically sound compared to #1 (sharp changes in concentration are unlikely in high ice clouds, especially in the tropics, (e.g. Liao et al., 1995)). The reduced set of profiles #1, #2, #5, and #7, illustrated by representative examples of the data and their approximations in Fig. 5, does not contain linearly dependent elements.

3.3 Ice crystal size profile

Besides IWC, another important radiative characteristic of the cloud is the effective ice crystal size and its changes with height. The analysis of DARDAR $De(z)$ profiles shows that they are not as diverse as the IWC profiles and can be represented with a trapezoid similar to profile #6 in Fig. 5a. Here, the only parameter needed to describe the vertical profile is the ratio of the upper and lower edges of the trapezoid (k_{AB} , see a sketch in Fig. 6a). We have studied the best fit of this parameter for different IWPs and seasons, varying k_{AB} in a broad range from 0.1 (almost the "upper triangle") through 1.0 (rectangular) to 10 (almost "lower triangle"). As one can see in Fig. 6, for $IWP < 10 \text{ g/m}^2$ $De(z)$ is almost constant ($k_{AB} \approx 1.1$) and this coefficient demonstrates only a moderate increase up to $IWP \approx 10 \text{ g/m}^2$. This is explained by the low density of the ice particles, which hinders the aggregation and buoyancy stratification. For $IWP > 30 \text{ g/m}^2$, $De(z)$ is best

represented by a trapezoid with a ratio of edges $k_{AB} = 1.35\text{--}1.5$. For these densities, the probability of ice particle aggregation is higher and the sedimentation of heavier particles increases their concentration towards the cloud base. It is interesting to compare the behavior of k_{AB} for winter and summer midlatitudes as we did for $\Delta z_{\text{clid}}(\text{IWP})$ distributions in Fig. 4: in winter, k_{AB} is larger than in summer, meaning stronger vertical $De(z)$ gradients during this period. This behavior is consistent with denser clouds in the storm tracks discussed above. However, De also depends on the mechanism of cirrus formation (e.g. in situ or as an anvil of a convective system), on the life stage of the system and on the environmental temperature and humidity. In this article, we do not study the De profiles in further detail, but, as the estimates in the next section show, the vertical profile of De affects the radiative properties of the cloud and should be taken into account in the analysis and modeling.

4 Results

4.1 Relating IWC profile shapes to cloud and atmospheric parameters

We have analyzed three years (2007–2009) of colocated data by searching for the best fit within the four primitive $\text{IWC}(z)$ shapes: rectangular, isosceles trapezoid, lower triangle, and upper triangle. Then we have studied their relative occurrence with respect to IWP, cloud layering (single or multi), cloud vertical extent, vertical wind, latitude and underlying surface (land or ocean). As a first step, we have studied the probability of occurrence of these specific IWC profile shapes as a function of IWP. Table 5 presents the statistics separately for single-layer and multi-layer cloud scenes, respectively. As the median values of Table 3 have already indicated, about 75% of all high ice clouds lie within the range of $\text{IWP} < 100 \text{ g/m}^2$. Within this IWP range, about 60 to 80% of the IWC profiles may be represented by rectangular (constant IWC) and isosceles trapezoid shapes.

~~The~~As one can see from the normalized IWP histogram values presented in Table 5a and 5b, the relative frequency of thick ice cloud occurrence ~~distribution-of-is higher in~~ single-layer clouds is slightly tilted towards thicker high ice clouds rather than in ~~the case of~~ multi-layer scenes, in agreement with Table 3 ~~system~~. Qualitatively, the IWC profile shape type fractioning behaves the same way for single- and multi-layer cloud scenes: if joined, rectangular and trapezoid IWC shapes make up more than 70% of all the shapes. Between these two types, trapezoid-like IWC shapes dominate both single- and multi-layer scenes, unless $\text{IWP} < 10 \text{ g/m}^2$. The remaining 20 – 40% split into profiles with increasing (lower triangle) and decreasing (upper triangle) IWC towards cloud base. We observe, as expected, an increasing occurrence probability of lower triangle with

increasing IWP. Upper triangle shapes mostly occur in clouds with $IWP < 30 \text{ g/m}^2$. This is consistent with the currently accepted ice cloud formation model: if the amount of ice in the cloud is low, the particles may form an “inverse” IWC profile, stimulated by updraft or by a favorable combination of water vapor and temperature profiles. If the cloud is thicker, the sedimentation of larger particles leads to a decrease of occurrence of this shape.

To address the influence of large-scale vertical winds, we have analyzed the IWC profile shape statistics with respect to vertical wind w_{500} , w_{base} (at GEOPROF z_{base}), and w_{cloud} (at the AIRS z_{cld}) and split it to three dynamic situations: strong updraft ($w < -175 \text{ hPa/day}$, 6% of all the cases), “calm atmosphere” ($-175 \text{ hPa/day} < w < 175 \text{ hPa/day}$, 93%), and strong downdraft ($w > 175 \text{ hPa/day}$, 1%), like those used in (Stubenrauch et al., 2004). The analysis shows that changes in relative occurrence of IWC profile shapes are only noticeable for strong downdraft within the cloud (see values in brackets in Table 5) while filtering the statistics based on w_{500} and w_{base} did not lead to conclusive results. As one can see in Table 5, dynamic effects are only well traceable with lower triangles: strong downdrafts ~~are associated with~~ correspond to additional 3–11% occurrence, and the added occurrence grows with IWP: ~~we assign~~ these effects to the following mechanisms: (a) in the case of a downdraft, the whole cloud becomes sub-saturated and the small ice crystals at the top sublimate much faster than the large ones (the size of crystals in the ice cloud increases from top to bottom, see Fig. 6), giving rise to lower triangle profiles; (b) downdraft leads to more intensive aggregation of ice crystals within an existing layer of less buoyant ice crystals beneath, ~~and the thicker the layer, the stronger the effect. However, – this works only when the ice crystal aggregation is noticeable (warm cirrus and completely frozen mixed phase clouds (Kienast-Sjogren et al., 2013)). It is interesting to note that~~ the situation does not inverse in the case of strong updrafts: ~~more buoyant particles in and the occurrence of upper layer are more easily washed out while less buoyant particles just move up, so this triangle profiles does not increase the upper triangle occurrence.~~ When a strong updraft takes place, a homogeneous freezing is triggered and a lot of small ice crystals appear within the whole cloud (Kärcher and Lohmann, 2002) that leads to an increase in the occurrence of rectangular-type profiles.

In a further step, we address the effects of other factors, which might be important for the statistical IWC profile classification. These are cloud vertical extent Δz_{cld} , latitude (season), and underlying surface type (land or ocean). The ultimate goal is to reduce the number of variables to a necessary minimum. We already know from Fig. 4b,d that cloud vertical extent is almost linearly dependent

on the logarithm of IWP, so we only keep IWP for the classification. As for the latitude, Fig. 7 presents the fraction of lower triangles as a function of latitude and IWP. This profile shape is the third one in frequency of occurrence (Table 5) and its radiative effects are expected to differ from those of the first two types (see Section 4.2 for the discussion). In Fig. 7, we separate the statistics for single-layer and multi-layer cloud scenes and for ocean and land. As the comparison of Fig. 7a,c with Fig. 7b,d shows, the surface does not have a significant influence on the relative occurrence, thus allowing to merge the statistics for land and ocean. On the other hand, single- and multi-layer scenes in Fig. 7a,b and Fig. 7c,d show different patterns, justifying considering them separately. Latitudinal variability for single-layer scenes (Fig. 7a,b) is noticeable in the high IWP domain ($>300 \text{ g/m}^2$), but as Table 5 shows, these cases represent less than 20% of single layer clouds and less than 10% of all clouds.

Summarizing, we suggest using the statistical classification of the IWC profile shape based solely on IWP. We explain relative consistency of the IWC profile shape type fractioning by a similarity of cloud formation processes in the atmosphere: regardless of the pressure/temperature/humidity profile, geographic location, and season, the physics of ice nucleation remains the same: once the supersaturation conditions and [\(in the case of a heterogeneous freezing\)](#) the ice nuclei exist, the clouds start forming; once formed, ice crystals start [clusteringgrowing](#) and sedimenting; reaching the zone with kinetic temperature greater than frost point temperature leads to ice sublimation.

4.2 The impact of IWC profile shape on cloud radiative effects

As mentioned above, ice clouds affect radiative energy balance in the atmosphere in several ways: reflecting and scattering the incoming solar radiation, reflecting and scattering terrestrial and atmospheric radiation coming from below, emitting infrared radiation in all directions. For a fixed IWP, each of the aforementioned components can depend on the profile of absorbing/scattering/emitting particle concentration. In this section, we address radiative effects in the long-wave (LW, $10\text{--}3280 \text{ cm}^{-1}$) and shortwave (SW, $820\text{--}50000 \text{ cm}^{-1}$) bands. To quantify them, we will use surface radiative flux (SRF), top of the atmosphere radiative flux (TOA), and atmospheric contribution ($\text{ATM} = \text{TOA} - \text{SRF}$). In a numerical experiment described below, we estimate the effects of the shape of IWC profiles using 5 typical atmospheric scenarios: subarctic and midlatitude summer and winter as well as the tropics. The atmospheres were considered up to the mesopause region. The detailed description of atmospheric scenarios and vertical profiles of temperature and atmospheric constituents can be found in (Feofilov and Kutepov, 2012).

4.2.1 Radiative transfer model RRTM

The calculations have been performed with the help of RRTM (Rapid Radiative Transfer Model), which utilizes the correlated-k approach to calculate fluxes. The software package consists of RRTM LW (Mlawer et al., 1997a; Iacono et al., 2000; Morcrette, 2001) and RRTM SW (Mlawer et al., 1997b, 1998) modules, both of which use k-distributions obtained from an exact line-by-line radiative transfer code, LBLRTM (Clough et al., 2005). The RRTM LW algorithm calculates the fluxes and cooling rates over sixteen LW bands with accuracy at all levels better than 1.5 W/m^2 and 0.3 K/day , correspondingly. The optical properties of ice clouds are calculated for each spectral band using the Streamer model v3.0 (Key and Schweiger, 1998). The RRTM SW algorithm calculates the fluxes over fourteen SW bands with accuracy at all levels better than 1.0 W/m^2 for direct and 2.0 W/m^2 for diffuse irradiances (Oreopoulos et al., 2012). Scattering calculations are performed using the DISORT package (Stamnes et al., 1988). For each spectral band, the optical properties of water and ice clouds are calculated using the Hu and Stamnes (1993) and Fu (1996) parameterizations, respectively. With the help of the RRTM code, we have performed a series of radiative transfer calculations, varying the atmospheric scenario, $De(z)$ (10 values), IWC(z) profile shape, IWP (7 intervals), cloud vertical extent (Δz_{cld} , 7 values), and cloud top height (5 values). In addition, we doubled the number of simulations by adding an underlying optically thick water cloud to estimate the IWC profile effects when the terrestrial radiance is "blocked". Overall, the number of simulations is equal to $5 \times 10 \times 4 \times 7 \times 7 \times 5 \times 2 = 98,000$. Since the spread of tropical IWP values is larger than that at other latitudes (e.g. Eliasson et al., 2011), we present comparisons for the tropical scenario.

4.2.2 Relative differences in LW radiative fluxes

As we have already seen before, in 75% of all high ice clouds one can approximate the IWC profile by a rectangular or isosceles trapezoid shape. For the rest of the cases, however, we want to estimate the radiative impact of using a "realistic" (DARDAR) IWC profile instead of a constant IWC profile and see how much this will affect the difference in fluxes at the TOA, SRF and atmosphere (ATM). Correspondingly, we compare SRF, TOA, and ATM values for each combination of IWP, z , De , and Δz for three IWC profile types versus the results obtained with a rectangular profile. Figure 8 shows a representative example of such a comparison for the TOA_LW flux differences built for the three IWC profile shapes vs rectangular one. For these plots, Δz_{cld} varied from 3 to 7 km and IWP varied from 1 to 1000 g/m^2 . As one can see, the radiative effects of the isosceles trapezoid type (Fig. 8a) are almost identical to that of the

rectangular type. On the other hand, there are noticeable effects in TOA_LW fluxes for lower and upper triangle IWC profile types (Fig. 8b,c) for Δz larger than 3 km and IWP larger than 30 g/m².

We explain the observed differences by the nature of the LW cloud radiance: the LW fluxes are composed of terrestrial, atmospheric, and cloud components. The terrestrial and atmospheric radiances originating below the cloud are absorbed by clouds with the same IWP in the same way. The atmospheric radiance above the cloud is the same in all compared cases. However, the emitted cloud radiance depends on the shape of the IWC profile: temperature in the troposphere decreases with height, so the effective altitude of the upper and lower triangles will differ from that of the cloud with a constant IWC. Correspondingly, the lower triangle type cloud will emit more radiance than the rectangular type, which, in turn, will emit more than the upper triangle type. As for the trapezoid, its effective radiative height is about the same as that of the rectangular-type cloud. The magnitude of the effect (Fig. 8b,c) increases with Δz since the difference between kinetic temperatures of effective radiative cloud layer increases. However, for optically thick clouds (see large IWP values in the right-hand side of Fig 8b,c panels) the effect washes out since high optical thickness “moves” the effective radiative heights upwards, making the differences between them smaller. The same considerations apply for the SRF_LW fluxes (not shown), but in this case atmospheric absorption and emission in the thick lower atmosphere mask the changes and the differences are smaller than 1%. Adding optically thick water cloud underneath the ice cloud does not significantly change either of the conclusions made above: TOA_LW is still modulated by the effective radiative height, while the surface becomes more isolated from the ice cloud, further reducing the sensitivity of SRF_LW to IWC(z).

4.2.3 Relative differences in SW radiative fluxes

In a similar manner, we have analyzed the sensitivity of SW fluxes to IWC profile type (Fig. 9). The effects in TOA_SW are opposite to those in TOA_LW (Fig. 8): the radiance escaping the atmosphere is smaller in the case of lower triangle IWC(z) compared to the cloud of a rectangular type. The study shows that this effect is related to the De profile. Small and large particles scatter solar radiance differently. Correspondingly, convolving De(z), which increases towards the cloud base (see Sect. 3.3 and Fig. 6), with the IWC profiles of a different type changes the amount of radiance scattered backwards. To justify this explanation, we have performed a test with a constant De within the cloud layer (not shown), which reduced the differences in Fig. 9a–c to less than 1%. The same mechanism and explanation apply to SRF_SW fluxes differences in Fig. 9d–f where the effects are the opposite to that in TOA_SW: lower triangles cause larger SRF_SW than rectangular

type IWC profiles in thick clouds. As for the TOA_SW, the effect is gone if a constant De is used. Both the TOA_SW and SRF_SW fluxes show weak sensitivity to substituting rectangular IWC profile with trapezoid one due to an obvious reason: the contributions of particles with De significantly different from the average De in the cloud layer are reduced by IWC(z) profile. Adding a water cloud beneath the ice cloud reduces the effects in TOA_SW for the IWP values less than 50 g/m². This is due to a contribution of the water cloud to the TOA_SW flux: a part of solar radiance, which has passed through an ice cloud, is reflected back, increasing the TOA_SW and washing out the effects of the ice cloud itself. As for the SRF_SW in the case of an underlying water cloud, the sensitivity of the flux to the IWC profile change reduces by a factor of ~2 because of the absorption in the water cloud.

4.2.4 Absolute differences of IWC-profile-shape-weighted SW and LW fluxes

Even though some of the panels in Fig. 8 and 9 show noticeable changes in TOA and SRF fluxes, this knowledge alone is not enough to estimate the energetic effects of using the rectangular type IWC(z) in all the cases instead of using real (or more realistic) profiles. To do that, we have used a pre-calculated set of 98,000 fluxes as a big lookup table (LUT) (see Sect. 4.2.1) and applied it to each of the events in the colocated dataset. For clear-sky cases, we used a corresponding clear-sky profile to obtain realistic cloud-amount weighted fluxes (we used cloud amount from AIRS). For cloudy cases, we used the fluxes corresponding to the best fit IWC model profile (if the best fit returned the rectangular profile it was included to keep the statistics unbiased). In Table 6, we compare net SW+LW fluxes at the TOA, SRF, and their difference, ATM, averaged for both approaches. The table contains net flux differences estimated, separately for single-layer high clouds and for all scenes, including multiple layer clouds and clear sky cases. Correspondingly, the first part can be used for estimating the average radiative effects in the cloudy cases, while the second part represents high ice cloud amount weighted differences in fluxes acting globally.

Obviously, the LUTs we have used to make these estimates cannot cover all possible permutations of ice clouds and water clouds of variable optical depth at different distances from the ice clouds, not speaking about different water and ice particle size distributions, but the values in Table 6 give an estimate of the significance of the effect. The sign and magnitude of the values are related to an interplay between the effects in the ratios of the fluxes considered in Sect. 4.2.2. and Sect. 4.2.3 convolved with the occurrence frequencies of different IWC profile shapes and with occurrence frequencies of corresponding IWPs, cloud top heights, and Δz . We highlight several features. From the comparison of TOA_LW and TOA_SW flux sensitivity (Fig. 8 and Fig. 9a–c), one can see that

SW and LW flux responses are in counter-phase: using lower triangle instead of constant IWC profile increases LW flux, but decreases SW flux. As discussed above, a cloud underlying the ice cloud reduces the surface radiative effect both in SW and in LW. Small TOA values for the SAW atmosphere are linked to polar night conditions and associated with a lack of both reflected solar radiance and high level ice clouds on the poles. Cloud-amount-weighted net flux differences are significantly smaller than those estimated for only cloudy cases: all values in the second part of Table 6 are smaller than 1 W/m^2 while the ATM flux differences in the first part reach $\sim 4 \text{ W/m}^2$ and TOA and SRF net flux differences reach $\sim 2 \text{ W/m}^2$. These estimates should be supplemented by differences related to IWC profile shapes in low thick ice clouds as well as to LWC profiles in water clouds that can be a subject of a separate study. However, the vertical extent of these clouds is much smaller compared to that of high clouds, so the radiative effects are expected to be smaller, too.

5 Conclusion

Since IR sounders only determine bulk cirrus microphysical properties, we added the data from active instruments to get a deeper insight into vertical profiles of IWC and De. The primary object of this analysis was to find out if the IWC profiles can be classified according to simple shapes, ideally as a function of parameters determined by IR sounders alone, and to determine the effect on the radiative properties of the cloud. Below we list the most important findings of our analyses.

1. A minimal and sufficient set of primitive shapes representing the IWC profiles in high ice clouds consists of four elements: rectangular, isosceles trapezoid, upper triangle, and lower triangle. The statistical analysis shows that rectangular and trapezoid IWC shapes together make up more than 70% of all the cases with trapezoid-like IWC profiles dominating both single- and multi-layer scenes. The fraction of lower triangles increases with IWP, reaching 33% for $\text{IWP} > 300 \text{ g/m}^2$. The fraction of upper triangles is 19% for multi-layer scenes at $\text{IWP} < 10 \text{ g/m}^2$ and decreases with IWP increase.
2. The main variable, which should be used for the IWC profile shape statistical classification is IWP. Cloud vertical extent strongly correlates with a logarithm of IWP, land/ocean distributions demonstrate similar behavior, and latitudinal variability of the most frequent shape is moderate. However, the dependence of the profile shape on IWP is strong, consistent with the current understanding of cirrus formation physics. Single-layer high clouds and multi-layer scenes demonstrate qualitatively similar behavior, but the relative occurrence of lower triangle shapes is slightly larger for the former and the relative occurrence of upper triangle shapes is slightly

larger for the latter. We have observed a correlation between the lower triangle fraction and strong downdrafts within the cloud ($w_{\text{cloud}} > 175 \text{ hPa/day}$), leading to 3–11% anomalies (up to 50% relative change).

3. The effective ice crystal diameter of high ice clouds in general increases towards cloud base (i.e. Heymsfield and Iaquinta, 2000). We found that its vertical profile can be parameterized by a trapezoid shape. The ratio of its lower and upper edges is 1.1 for $\text{IWP} < 10 \text{ g/m}^2$ and 1.35–1.5 for $\text{IWP} > 50 \text{ g/m}^2$.
4. We have estimated the radiative effects of clouds with the same IWP but with different IWC profile shape for five typical atmospheric scenarios and over a broad range of IWP, cloud height, cloud thickness, and D_e values. In this analysis, lower triangle-, upper triangle- and trapezoid- IWC profiles were compared to a “reference” rectangular profile. We explain the observed differences in TOA_{LW} fluxes by thermal radiance of the cloud and by changes of the “effective radiative layer” height depending on the IWC profile. The differences in TOA_{SW} fluxes are related to D_e vertical profiles: changing the IWC profile shape leads to a different effective value of D_e that, in turn, leads to different scattering characteristics of the cloud. Adding a thick water cloud beneath the ice cloud reduces effects in surface radiance. Absolute differences in net fluxes associated with realistic IWC distributions versus clouds with constant IWC are of the order of 2–4 W/m^2 for cloudy scenes while weighting them by their occurrence reduces the effects to less than 1 W/m^2 .

Summarizing, the total impact of the shape of ice cloud profiles on the estimates of the Earth’s radiative balance is small. On the other hand, a correlation between the most frequent primitive shape and the cloud IWP affects the interpretation of bulk microphysical properties retrieved from passive satellite observations. We have shown that for clouds with $\text{IWP} < 100 \text{ g/m}^2$ (80% of all high ice clouds), it is feasible to use a constant IWC profile in the retrieval. However, for clouds containing more ice, the radiative effects of different shapes are noticeable. This may also affect the atmospheric heating profiles which is a subject of our future studies.

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retrieved from the ICARE Data and Service Center at the University of Lille, and the authors thank the personnel of both centers for a continuous support of the work.

Appendix A: Abbreviations

AIRS:	Atmospheric Infrared Radiation Spectrometer
AMSU:	Advanced Microwave Sounder Unit
ATM:	Atmosphere
CALIOP:	Cloud-Aerosol Lidar with Orthogonal Polarization
CALIPSO:	Cloud Aerosol Lidar and Infrared Pathfinder Satellite Observations
CNES:	National Center of Space Research
CPR:	Cloud Profiling Radar
DARDAR:	liDAR + raDAR product
DISORT:	Discrete Ordinates Radiative Transfer program
ECMWF:	European Centre for Medium-Range Weather Forecasts
ERA:	ECMWF's re-analysis
GEOPROF:	Geometric profiling
IASI:	Infrared Atmospheric Sounding Interferometer
IR:	Infrared
IWC:	Ice water content
LBLRTM:	Line by line RRTM
LMD:	Laboratory of Dynamic Meteorology
LT:	Local time
LUT:	Look-up table
LW:	Long-wave
<u>LWC:</u>	<u>Liquid water content</u>
MLS:	Midlatitude summer type atmosphere
MLW:	Midlatitude winter type atmosphere
MODIS:	Moderate Resolution Imaging Spectroradiometer

NOAA:	National Oceanic and Atmospheric Administration
RRTM:	Rapid Radiative Transfer Model
SAS:	Subarctic summer type atmosphere
SAW:	Subarctic winter type atmosphere
SRF:	Surface
SW:	Short-wave
TIROS:	Television Infrared Observation Satellite
TOA:	Top of atmosphere
TOVS:	TIROS Operational Vertical Sounder
TROP:	Tropical type atmosphere

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Figures

Fig. 1. Latitude/longitude coverage for 1st July 2008, observation time 1h30PM (at the equator crossing time). Grey: AIRS footprints; red: CALIPSO L2 cloud data at 5 km resolution; blue: CloudSat footprints. The center of a blown-up part of the orbit corresponds to ($\text{lat} = -25^\circ$; $\text{lon} = 154^\circ$).

Fig. 2. Examples of the IWC profiles of high ice clouds, including information on cloud height from the colocated AIRS-LMD, CALIPSO, GEOPROF, and DARDAR data, for clouds with increasing IWP values. Black curves: DARDAR IWC(z) profile; colored horizontal lines mark the position of the AIRS cloud, CALIPSO and GEOPROF cloud top and cloud base heights. [All profiles obtained for July 2007: a\) \$\text{lat}=2.3^\circ\$, \$\text{lon}=-15.9^\circ\$; b\) \$\text{lat}=23.9^\circ\$, \$\text{lon}=101.7^\circ\$; c\) \$\text{lat}=0.3^\circ\$, \$\text{lon}=101.8^\circ\$; d\) \$\text{lat}=-2.5^\circ\$, \$\text{lon}=120.6^\circ\$.](#)

Fig. 3. Probability density plots of height comparisons for high ice clouds for the whole globe in January 2007: a) AIRS z_{cld} vs DARDAR peak height; b) AIRS z_{cld} vs CALIPSO z_{top} ; c) CALIPSO z_{top} – DARDAR peak vs DARDAR. Dashed lines in a) and b): one-to-one correlation.

Fig. 4. Average cloud emissivity and ice cloud layer vertical extent as a function of ice water path, separately for single and multi-layer clouds and three latitude zones, for 2 months (January 2007: (a), (b), and July 2007: (c), (d)). All 4 panels share the same legend, SH, TROP, and NH correspond to latitude zones 90S–30S, 30S–30N, and 30N–90N, respectively.

Fig. 5. Cloud IWC(z) examples and their approximation with primitive shapes: a) initial set of 7 profiles; b) constant-within-layer or rectangular; c) upper triangle; d) lower triangle; e) isosceles trapezoid. Solid lines: DARDAR IWC(z) profile, dashed lines: best fit profile. Height is shown with respect to GEOPROF z_{top} .

Fig. 6. Values of k_{AB} (ratio of the lower and upper edges of the trapezoid fitting $\text{De}(z)$ vertical profile) for single and multi-layer cloud scenes for three latitudinal zones for a) January and b) July. The legend is the same as in Fig. 4.

Fig. 7. Lower triangles fraction w.r.t. ice water path and latitude: a) single layer, ocean; b) single layer, land; c) multi-layer scenes, ocean; d) multi-layer scenes, land. The relative occurrence of IWP bins can be found in Table 5.

Fig. 8. The relative difference in calculated TOA_LW fluxes w.r.t. rectangular IWC(z) profile type estimated for 3 to 7 km thick clouds with average $De=50\text{ }\mu\text{m}$ ($k_{AB}=1.5$, see Sect. 3.3) and with a cloud top at 15 km: a) isosceles trapezoid; b) lower triangles; c) upper triangles.

Fig. 9. The relative difference in SW fluxes w.r.t. rectangular IWC(z) profile type estimated for 3 to 7 km thick clouds with average $De=50\text{ }\mu\text{m}$ and with a cloud top at 15 km. a)–c): TOA; d)–f): SRF; a,d) isosceles trapezoid; b,e) lower triangles; c,f) upper triangles.

Tables

Table 1. L2 datasets and products used in this analysis

L2 Dataset	Variables
AIRS-LMD	Cloud pressure (p_{cld}), cloud temperature (T_{cld}), cloud emissivity (ϵ_{cld}), cloud height (z_{cld})
CALIPSO 5km clouds	cloud top height (z_{top}), effective cloud base height (z_{base}) for multiple cloud layers
Radar-lidar GEOPROF	z_{top} and z_{base} for multiple cloud layers
DARDAR	IWC(z), $De(z)$, cloud type vertical profiles
ERA-Interim	vertical wind

Table 2. Colocation statistics corresponding to the data illustrated in Fig. 1

Dataset	N_{day}	% selected w.r.t. orig.	r.m.s. dist [km]
AIRS-LMD	1.5×10^6	0.4	0 (self)
CALIPSO	1.1×10^5	9.4	6.1
GEOPROF	5.5×10^5	2.0	5.78
DARDAR	5.5×10^5	2.0	5.78
ERA-Interim	4.6×10^5	3.6	24.0

Table 3. Latitudinal averages of different ice cloud variables

Latitude zone	Single layer high cloud				High cloud + any cloud				Mean IWP [g/m ²]
	ϵ_{cld}	Median IWP [g/m ²]	Δz_{cld} [km]	$\Delta z_{\text{ice}}/\Delta z_{\text{cld}}$ [%]	ϵ_{cld}	Median IWP [g/m ²]	Δz_{cld} [km]	$\Delta z_{\text{ice}}/\Delta z_{\text{cld}}$ [%]	
90S–60S	0.69	122	3.1	97	0.61	37	2.3	96	65
60S–35S	0.74	191	2.9	95	0.63	38	2.3	95	103
35S–15S	0.61	50	2.5	94	0.57	23	2.0	90	44
15S–15N	0.56	38	2.8	96	0.56	21	2.1	86	79
15N–35N	0.57	39	2.5	94	0.55	22	2.0	89	46
35N–60N	0.68	122	2.8	95	0.59	33	2.1	94	95
60N–90N	0.61	116	2.9	96	0.53	33	2.1	95	67

Table 4. Linear correlation coefficients for a monthly series (30000 samples, January 2007) of ζ deviation values for 7 test cloud profiles

Profile #	1	2	3	4	5	6	7
1	1.00	0.62	0.40	0.35	0.43	0.88	0.44
2	–	1.00	0.46	0.08	-0.31	0.22	0.43
3	–	–	1.00	0.82	-0.26	0.15	0.99
4	–	–	–	1.00	0.08	0.31	0.85
5	–	–	–	–	1.00	0.79	-0.22
6	–	–	–	–	–	1.00	0.21
7	–	–	–	–	–	–	1.00

Table 5a. Normalized occurrence of basic IWC profile shapes for different IWP intervals, for single layer high ice clouds. The rightmost column shows the relative occurrence per IWP interval. All values are in percent. Values in brackets refer to anomalies associated with strong downdraft ($>175\text{hPa/day}$) within the cloud (at AIRS z_{cld}). If no value in brackets is given, the change is smaller than 2%.

IWP [g/m^2]	Rectangular	Isosceles trapezoid	Lower triangle	Upper triangle	Relative occurrence
0–10	42	32	12 (+4)	14 (–3)	18
10–30	28	51	14 (+3)	7	21
30–100	25	55	16 (+4)	3	23
100–300	18	59	21 (+9)	2	17
300–1000	13	53	33 (+11)	1	12
>1000	13	37	50	0	8

Table 5b. Same as Table 5a, but for multi-layer cloud scenes, for which the uppermost layer contains high ice cloud.

IWP [g/m^2]	Rectangular	Isosceles trapezoid	Lower triangle	Upper triangle	Relative occurrence
0–10	39	31	11	19	22
10–30	29	47	14	10	29
30–100	27	51	16 (+3)	6	27
100–300	21	56	20 (+10)	3	13
300–1000	19	52	27 (+9)	2	6
>1000	19	41	40	1	2

Table 6. Differences in radiative fluxes for July: real IWC(z) profiles vs constant IWC(z), supplemented with interannual variability for 2007–2009 (values in brackets). Global average is area weighted

	Only single-layer high cloud scenes			Cloud amount weighted		
Atm. type	TOA [W/m ²]	SRF [W/m ²]	ATM [W/m ²]	TOA [W/m ²]	SRF [W/m ²]	ATM [W/m ²]
SAW	-0.03±0.04	-2.08±0.08	2.05±0.05	0.00±0.01	-0.31±0.01	0.32±0.01
MLW	0.92±0.02	-1.96±0.04	2.89±0.06	0.16±0.00	-0.35±0.01	0.52±0.01
TROP	1.07±0.02	-1.10±0.06	2.17±0.08	0.27±0.01	-0.28±0.02	0.56±0.02
MLS	2.06±0.07	-2.17±0.14	4.23±0.21	0.49±0.03	-0.49±0.04	0.98±0.06
SAS	1.63±0.08	-2.66±0.12	4.29±0.19	0.20±0.02	-0.32±0.03	0.51±0.05
Glob. avg.	1.25±0.02	-1.68±0.06	2.93±0.08	0.24±0.01	-0.38±0.01	0.62±0.01