

I thank the editor again for his latest recommendations that help polishing the paper. They are copied hereafter and my responses are inserted where appropriate.

The remark table 1/2 versus figure.

Because the decision is left to me, I would strongly suggest a map. I go along with the remark, that the sense of the table is questionable.

Probably one needs even both, if the PI's insist on the names of the stations appearing in the list.

Because it does not really belong to the content of the article, I would suggest to put both, the table and a figure in the supplement.

I have done it.

In the introduction, line 43: I would suggest to define (again) what you mean by XCO₂.

I have done it.

I wonder if the expression (line 192)

"The ... matrix should consistently be diminished" is correct. Please check this again.

I have changed the sentence to "The retrieval error variances should consistently be reduced".

line 262

What do you mean by: "... is usually about the ppm"

I have changed the expression to "... is usually about 1 ppm"

I found the axis labels in figures 1-4 rather small and difficult to read. I would suggest to enlarge the figure, so that the width of the figures spans the width of the page (in online mode), as has been done for figures 5-8.

I have done it.

Additionally, I have added "In the usual case when $\check{\mathbf{H}} \neq \mathbf{I}$," before Eq. (7) to be exhaustive on the topic.

9 Abstract

10 The extending archive of the Greenhouse Gases Observing SATellite (GOSAT) measurements
11 (now covering about six years) allows increasingly robust statistics to be computed, that
12 document the performance of the corresponding retrievals of the column-average dry air-mole
13 fraction of CO₂ (XCO₂). Here, we demonstrate that atmospheric inversions cannot be rigorously
14 optimal when assimilating current XCO₂ retrievals, even with averaging kernels, in particular
15 because retrievals and inversions use different assumption about prior uncertainty. We look for
16 some practical evidence of this sub-optimality from the view point of atmospheric inversion by
17 comparing a model simulation constrained by surface air-sample measurements with one of the
18 GOSAT retrieval products (NASA's ACOS). The retrieval-minus-model differences result from
19 various error sources, both in the retrievals and in the simulation: we discuss the plausibility of
20 the origin of the major patterns. We find systematic retrieval errors over the dark surfaces of
21 high-latitude lands and over African savannahs. More importantly, we also find a systematic
22 over-fit of the GOSAT radiances by the retrievals over land for the high-gain detector mode,
23 which is the usual observation mode. The over-fit is partially compensated by the retrieval bias-
24 correction. These issues are likely common to other retrieval products and may explain some of
25 the surprising and inconsistent CO₂ atmospheric inversion results obtained with the existing
26 GOSAT retrieval products. We suggest that reducing the observation weight in the retrieval
27 schemes (for instance so that retrieval increments to the retrieval prior values are halved for the
28 studied retrieval product) would significantly improve the retrieval quality and reduce the need
29 for (or at least reduce the complexity of) ad-hoc retrieval bias correction.

30

31

1. Introduction

CO₂ surface fluxes at the Earth's surface can be inferred from accurate surface measurements of CO₂ concentrations, but the sparseness of the current global network still leaves the flux horizontal and temporal gradients, and even their latitudinal distribution, very uncertain (Peylin et al. 2013). This limitation has provided a major incentive to develop the monitoring of CO₂ concentrations from space. First retrievals were obtained from existing instruments measuring either the thermal infrared radiation emitted by the atmosphere (Chédin et al. 2003) or the reflected sunlight in the near-infrared (NIR)/ shortwave infrared (SWIR) spectral regions (Buchwitz et al. 2005). The latter technique allows retrieving the column-average dry air-mole fraction of CO₂ (XCO₂) while the former is not sensitive to CO₂ in the lower atmosphere, near the CO₂ sources and sinks. Since active (lidar) measurement techniques for XCO₂ from space are still in development (e.g., Ingmann et al. 2009), NIR/SWIR measurements currently offer the best prospect to provide “retrievals of CO₂ of sufficient quality to estimate regional sources and sinks”, as phrased by objective A.8.1 of the Global Climate Observing System programme (GCOS, 2010), in the short term. However, they are hampered by uncertain knowledge about scatterers in the atmosphere at the corresponding wavelengths (aerosols and cirrus clouds) with an effect that varies with surface albedo, which is itself uncertain (e.g., Aben et al. 2007). Such interference in the XCO₂ signal seen in the NIR/SWIR measurements is of concern because even sub-ppm systematic errors (corresponding to less than 0.25% of the signal) can severely flaw the inversion of CO₂ surface fluxes (Chevallier et al. 2007, Miller et al. 2007). This risk motivated dedicated developments of the retrieval algorithms in order to de-convolve the spectral signatures of the involved compounds as much as possible (e.g., Reuter et al. 2010, Guerlet et al. 2013b).

54 The Japanese GOSAT, launched in January 2009, and the USA second Orbiting Carbon
55 Observatory (OCO-2), launched in July 2014, observe the NIR/SWIR radiation with unprecedented
56 spectral resolution in order to specifically address this remote sensing challenge. The GOSAT
57 archive already covers six years and can provide good insight into the adequacy of NIR/SWIR
58 retrievals for CO₂ source-sink inversion. In terms of random errors, raw GOSAT retrievals now
59 reach single shot precision better than 2 ppm (one sigma) in fair measurement conditions (e.g.,
60 Nguyen et al. 2014). This performance is better than what pre-launch studies suggested: for
61 instance Maksuytov et al. (2008) expected 2.5-10 ppm single shot precision only. Systematic errors
62 are difficult to quantify or else they would be removed. They are likely state-dependent with
63 absolute values varying in time and space about the ppm before any bias correction (Nguyen et al.
64 2014). They also depend on the retrieval algorithm (e.g., Oshchepkov et al. 2013). As expected,
65 the remaining uncertainty has profound impact on CO₂ source-sink inversions (Basu et al. 2013,
66 Chevallier et al. 2014), but XCO₂ retrievals have already served as a basis to study the carbon
67 budgets of some regions (Guerlet et al. 2013a, Basu et al. 2014, Reuter et al. 2014). For instance,
68 25 scientists analysed several XCO₂ retrievals over continental Europe and concluded that the
69 current understanding of the European carbon sink brought by bottom-up inventories had to be
70 revisited (Reuter et al. 2014).

71 This paper aims at contributing to the debate about the relevance of current GOSAT retrievals
72 for atmospheric inversions. Our starting point is a critical review of the basic principles behind the
73 current processing chains that go in successive steps from GOSAT measured radiance spectra to
74 surface flux estimates (Section 3). We then focus on the GOSAT retrievals provided by NASA's
75 Atmospheric CO₂ Observations from Space project (ACOS, build 3.4, described in Section 2) for
76 the period between June 2009 and May 2013. They are of particular interest because they have
77 been processed in a way that prefigures the official OCO-2 retrievals in terms of spectral bands and

78 available simultaneous observations (O'Dell et al. 2012). In Section 4, we analyse the residuals
79 between the ACOS-GOSAT retrievals and the simulated CO₂ concentration fields of the
80 Monitoring Atmospheric Chemistry and Climate atmospheric inversion product (MACC, version
81 13r1, also described in Section 2) that assimilated surface air sample measurements from various
82 networks. Concluding discussion follows in Section 5.

83

84 **2. Retrievals and model simulation**

85

86 **2.1. ACOS-GOSAT retrievals**

87

88 GOSAT is a joint venture by the Japan Aerospace Exploration Agency (JAXA), the National
89 Institute for Environmental Studies (NIES) and the Ministry of the Environment (MOE) in Japan.
90 This spacecraft is operated in a sun-synchronous polar orbit that crosses the Equator at about 13:00
91 local time during daytime and that repeats every 3 days. As described by O'Dell et al. (2012) and
92 Osterman et al. (2013), the ACOS algorithm retrieves XCO₂ from a selection of GOSAT
93 measurements of reflected sunlight made in the same spectral bands than OCO-2. Over land, such
94 measurements are made by pointing the instrument to the Earth on both sides of the satellite track.
95 Given the low reflectivity of water surfaces, ocean measurements are only possible when the
96 instrument is pointed to the sun-glint spot, which is only done within 40° from the Equator in the
97 summer hemisphere. GOSAT also carries a cloud and aerosol imager that can help filtering difficult
98 scenes out, but unlike other GOSAT retrieval algorithms, ACOS does not use it since OCO-2 does
99 not contain a similar instrument.

100 Following Boesch et al. (2006) and Connor et al. (2008), the ACOS algorithm relies on optimal
101 estimation (i.e. Bayesian methods) to retrieve the vertical profile of the CO₂ dry air mole fraction

together with variables interfering in the measurements: the surface pressure and the surface albedo, some variables describing temperature, water vapour, clouds and aerosols in the atmosphere, and channel offsets for the instrument. The retrieved XCO_2 is simply obtained by integrating the retrieved CO_2 profile. In this Bayesian formulation of the retrieval, prior information about CO_2 is given an artificially small weight in order to maximize the observation contribution to the result: for instance, the standard deviation of the uncertainty assigned to the prior XCO_2 is larger than 10 ppm (O'Dell et al., 2012), i.e. larger than typical variations of XCO_2 at the continental scale (e.g., Keppel-Aleks et al. 2011). We will discuss the impact of this choice later and for simplicity, we will call XCO_2^b and XCO_2^a the prior (*background*) and the retrieved (*analysed*) XCO_2 , respectively. XCO_2^a can be compared with model simulations, as will be done here, or with other measurements via the associated CO_2 averaging kernel profiles and prior profiles (e.g., Connor et al., 1994). For nadir viewing, XCO_2^a is representative of a volume that has a circular footprint at the Earth's surface of diameter about 10 km.

Previous comparisons between XCO_2^a and model simulations or reference ground-based XCO_2 measurements from Total Carbon Column Observing Network (TCCON) highlighted some systematic dependency of the error of XCO_2^a as a function of a series of internal variables of the algorithm (Wunch et al. 2011b). This feature reveals some limitations of the algorithm but also allows correcting them empirically, for instance before they are assimilated in atmospheric inversion systems (Crisp et al. 2012). We will call $\text{XCO}_2^{a,c}$ the bias-corrected retrievals.

2.2. MACC CO_2 inversion

Since year 2011, the MACC pre-operational service (www.copernicus-atmosphere.eu) has been delivering a CO_2 inversion product with biannual updates. Release 13r1 primarily describes the

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CO₂ surface fluxes over more than three decades, from 1979 to 2013, at resolution $3.75^\circ \times 1.9^\circ$ (longitude-latitude) and 3-hourly, based on 131 CO₂ dry air mole fraction station records (See Fig. S1) from three large databases:

- the NOAA Earth System Research Laboratory archive (NOAA CCGG, <http://www.esrl.noaa.gov/gmd/ccgg/index.html>),
- the World Data Centre for Greenhouse Gases archive (WDCGG, <http://ds.data.jma.go.jp/gmd/wdcgg/>),
- the Réseau Atmosphérique de Mesure des Composés à Effet de Serre database (RAMCES, <http://www.lsce.ipsl.fr/>).

The three databases include both in situ measurements made by automated quasi-continuous analysers and irregular air samples collected in flasks and later analyzed in central facilities. The detailed list of sites is provided in Tables S1 and S2.

The MACC Bayesian inversion method is formulated in a variational way in order to estimate the CO₂ surface fluxes at the above-described relatively high resolution over the globe (Chevallier et al. 2005, 2010). For v13r1, the system used a single 35-year inversion window, therefore enforcing physical and statistical consistency in the inverted fluxes. Fluxes and mole fractions are linked in the system by the global atmospheric transport model of the Laboratoire de Météorologie Dynamique (LMDZ, Hourdin et al. 2006) with 39 layers in the vertical and with the same horizontal resolution than the inverted fluxes. LMDZ is nudged to ECMWF-analysed winds for flux inversion.

The MACC inversion product also contains the 4D CO₂ field that is associated to the inverted surface fluxes through the LMDZ transport model. Simulating the GOSAT retrievals from this field is nearly straight-forward. The only difficulty lies in the interpolation from the LMDZ 39-level vertical grid to the 20-level vertical grid of the retrievals, before the retrieval averaging kernels are applied. Indeed, the model orography at resolution $3.75^\circ \times 1.9^\circ$ significantly differs

from the high-resolution orography seen by the retrievals. For the interpolation, we assume that CO₂ concentrations vary linearly with the pressure in the vertical. When the model surface pressure is smaller than the retrieved surface pressure, the profile is artificially extended at constant value below the model surface. In the opposite case, model levels below the sounding surface are ignored. We compensate this artificial change of mass in the profile by systematically adjusting the interpolated profile so that its pressure-weighted mean equals that of the profile before the interpolation.

3. Theoretical aspects

Like the other retrieval and inversion systems (see, e.g., Oshchepkov et al., 2013, and Peylin et al., 2013), ACOS-GOSAT and MACC both follow the Bayesian paradigm in its Gaussian linear form (e.g., Rodgers, 2000) in order to estimate the most likely state, in a statistical sense, of the CO₂ profile and of the CO₂ surface fluxes, respectively. In mathematical terms, given \mathbf{x} the vector that gathers the variables to be inferred (either a 1D CO₂ profile or 2D+1D CO₂ surface fluxes), given \mathbf{x}^b an a priori value of \mathbf{x} (coming from a climatology or from a model), and given \mathbf{y} the vector that gathers all relevant observations (either radiances or retrievals), the most likely state of \mathbf{x} is written:

$$\mathbf{x}^a = \mathbf{x}^b + \mathbf{K}(\mathbf{y} - \mathbf{H} \mathbf{x}^b) \quad (1)$$

\mathbf{H} is a linearized observation operator that links variables \mathbf{x} and \mathbf{y} (i.e. essentially a radiative transfer model or a transport model). \mathbf{K} is the following “Kalman gain” matrix:

$$\mathbf{K} = \mathbf{B} \mathbf{H}^T (\mathbf{H} \mathbf{B} \mathbf{H}^T + \mathbf{R})^{-1} \quad (2)$$

\mathbf{B} and \mathbf{R} are the error covariance matrices of \mathbf{x}^b and \mathbf{y} , respectively.

The error covariance matrix of \mathbf{x}^a is obtained by:

$$\mathbf{A} = (\mathbf{I} - \mathbf{KH}) \mathbf{B} \quad (3)$$

with \mathbf{I} the identity matrix with appropriate dimension.

For simplicity, Eq. (1) does not make other variables that are simultaneously inferred appear, like clouds, aerosols or surface variables for the retrievals, or the 3D state of CO₂ at the start of the assimilation window for the inversion.

The current processing chains that go from radiances to surface fluxes are two-step processes (let aside some attempts to introduce an additional intermediate step in the form of a short-window analysis of the 3D concentrations; Engelen et al. 2009). We now distinguish the retrieval process and the inversion process by putting breves $\tilde{}$ on all symbols related to the former and hats $\hat{}$ on all symbols related to the latter. In a first step, the CO₂ profiles and their uncertainty $\{\tilde{\mathbf{x}}^a, \tilde{\mathbf{A}}\}$ are retrieved for each sounding $\{\tilde{\mathbf{y}}, \tilde{\mathbf{R}}\}$ separately. The resulting ensemble forms the observations to be simultaneously assimilated $\{\hat{\mathbf{y}}, \hat{\mathbf{R}}\}$ for the second step. The presence of prior information \mathbf{x}^b in both steps complicates the transition between the two. Following Connor et al. (1994) and the current practice, we can technically eliminate the influence of \mathbf{x}^b (but not of its uncertainty) by the following adaptation of Eq. (1) in the second step: we assimilate $\hat{\mathbf{y}}' = \tilde{\mathbf{x}}^a - (\mathbf{I} - \tilde{\mathbf{K}}\tilde{\mathbf{H}})\tilde{\mathbf{x}}^b = \tilde{\mathbf{K}}\tilde{\mathbf{y}}$ rather than $\hat{\mathbf{y}}$ and change the observation operator from $\hat{\mathbf{H}}$ to $\hat{\mathbf{H}}' = \tilde{\mathbf{K}}\tilde{\mathbf{H}}\hat{\mathbf{H}}$. $\tilde{\mathbf{K}}\tilde{\mathbf{H}}$ is called the retrieval averaging kernel. The retrieval error ~~covariance matrix~~ variances should consistently be ~~diminished~~ reduced (e.g., Connor et al., 2008, paragraph 37) and is then called $\hat{\mathbf{R}}'$ hereafter.

For simplicity, and without loss of generality in our linear framework, let us consider the assimilation of a single sounding $\{\tilde{\mathbf{y}}, \tilde{\mathbf{R}}\}$ using its averaging kernel. By definition, given the changes made to $\hat{\mathbf{H}}$ and $\hat{\mathbf{R}}$, the gain matrix changes as well and we call $\hat{\mathbf{R}}'$ the new one. By applying Eq. (1) in this configuration, the analysed surface fluxes can be directly expressed in a concise form:

$$\hat{\mathbf{x}}^a = \hat{\mathbf{x}}^b + \hat{\mathbf{R}}' \tilde{\mathbf{K}} (\tilde{\mathbf{y}} - \tilde{\mathbf{H}} \hat{\mathbf{H}} \hat{\mathbf{x}}^b) \quad (4)$$

This equation has the desired shape of Eq. (1), i.e. the sum of the prior value and of a linear function of model-minus-measurement misfits. By construction, it does not depend on the retrieval prior $\tilde{\mathbf{x}}^b$. However, to follow the optimal estimation framework, we still need to be able to develop the product of the gain matrices consistently with Eq. (2), i.e. like (neglecting errors in the observation operators):

$$\mathbf{K} = \mathbf{B} \mathbf{H}^T \mathbf{H}^T (\mathbf{H} \mathbf{H} \mathbf{B} \mathbf{H}^T \mathbf{H}^T + \mathbf{R})^{-1} \quad (5)$$

In practice, we see that:

$$\mathbf{K}' \mathbf{K} = \mathbf{B} \mathbf{H}'^T (\mathbf{H}' \mathbf{B} \mathbf{H}'^T + \mathbf{R}')^{-1} \mathbf{B} \mathbf{H}^T (\mathbf{H} \mathbf{B} \mathbf{H}^T + \mathbf{R})^{-1} \quad (6)$$

~~Eqs.~~ In the usual case when $\mathbf{H} \neq \mathbf{I}$, Eqs. (5-6) can be made consistent in general provided

$$\mathbf{H} \mathbf{B} \mathbf{H}^T = \mathbf{H} \mathbf{H} \mathbf{B} \mathbf{H}^T \mathbf{H}^T \quad (7)$$

and (by developing \mathbf{H}' and using Eq. (7))

$$\mathbf{H}^T \mathbf{K}' (\mathbf{K}' \mathbf{H} \mathbf{B} \mathbf{H}^T \mathbf{K}' + \mathbf{R}')^{-1} \mathbf{B} = \mathbf{I} \quad (8)$$

Equation (7) simply expresses consistency between the prior error statistics within the information content of the retrievals: the uncertainty of the retrieval prior and of the flux prior should be the same in radiance space. This condition is not achieved by current satellite retrieval algorithms, at least because they artificially maximize the measurement contribution in the retrievals through the use of very large prior error variances (see Section 2.1 or Butz et al. 2009, Reuter et al. 2010). However, if enough intermediate variables were saved by the retrieval schemes, it would be possible to reconstruct the retrievals with appropriate prior error variances and correlations.

Equation (8) can be satisfied in general if the retrieval averaging kernel $\mathbf{K}' \mathbf{H}$ is close to unity.. In practice, the retrieval averaging kernel for profiles is far from unity because current radiance measurements do not provide any vertical resolution for CO₂. The situation is better if the state

vector $\tilde{\mathbf{x}}$ is the integrated column (in that case $\tilde{\mathbf{H}}$ includes an operator to distribute the column in the vertical).

As a consequence of deviations from Eqs (7-8), the effective gain matrix $\tilde{\mathbf{R}}' \tilde{\mathbf{K}}$ significantly differs from the optimal one for GOSAT, resulting in a wrong balance between prior flux information and measured radiances. Overall, $\tilde{\mathbf{K}}$ pulls too much towards the measured radiances and $\tilde{\mathbf{R}}'$ pulls too much towards the prior. This suboptimality very likely flaws the 4D information flow from the radiance measurements to the surface flux estimates. In particular, the sub-optimality of $\tilde{\mathbf{K}}$ affects the retrieval averaging kernel, that may not peak at the right height.

Migliorini (2012) proposed a sophisticated alternative to the averaging kernel assimilation of Connor et al. (1994), where the retrievals are assimilated after a linear transformation of both the retrievals and the observation operator. The transformation is heavier to implement than the above approach because it involves the retrieval signal-to-noise matrix $\tilde{\mathbf{R}}^{-1/2} \tilde{\mathbf{H}} \tilde{\mathbf{B}}^{1/2}$. It avoids the requirement of Eq. (8), but still requires consistent prior error statistics (Eq. (7)).

The situation complicates even further if we account for the facts that inversion systems assimilate bias-corrected retrievals (thereby implicitly re-introducing $\tilde{\mathbf{x}}^b$ that had been neutralised by the use of averaging kernels, in the equations), that $\tilde{\mathbf{H}}$ and $\tilde{\mathbf{H}}$ are imperfect operators, the uncertainty of which should be reported in $\tilde{\mathbf{R}}$, following Eq. (5), and that $\tilde{\mathbf{H}}$ is usually non-linear. The need to report all observation operator uncertainties in $\tilde{\mathbf{R}}$ means that retrieval configuration should in principle be tailored to the retrieval end-application, i.e. to the precision of the observation operator that is used in this end-application. For flux inversion, the transport model uncertainty in XCO₂ space is about 0.5 ppm (1 σ , Houweling et al. 2010). When optimizing parameters of a flux model rather than for the flux themselves (in Carbon Cycle Data Assimilation Systems, Rayner et al. 2005), the uncertainty of the flux model equations has also to be reported in

$\tilde{\mathbf{R}}$: when projected in the space of XCO_2 , they are comparable to transport model uncertainties (Kuppel et al. 2013).

4. Practical aspects

Given the particular concerns raised about the optimality of XCO_2 retrievals and of their averaging kernels in the previous section, we now focus on one specific retrieval product, ACOS-GOSAT, in order to look for some practical evidence of this sub-optimality.

4.1. Mean differences

Fig. 1 shows the mean bias-corrected retrievals $\text{XCO}_2^{\text{a,c}}$ and the mean corresponding posterior XCO_2 field of the MACC inversion over the June 2009 – May 2013 period per $3.75^\circ \times 1.9^\circ$ grid cell. All retrievals are used, provided they are found good by the ACOS standard quality control. The data density (Fig. 2b) follows the frequency of favourable retrieval conditions: more sunlight in the Tropics, less cloud over desert areas or over subsidence ocean regions. The long-term mean of the retrieval-minus-model differences (Fig. 2a) is usually about ~~the~~ 1 ppm. Interestingly, it appears to be organized spatially. Over land, large positive values (> 0.5 ppm, ACOS-GOSAT being larger) are seen over boreal forests, over most of South America, over grassland/cropland regions in Central Africa and over the West coast of the USA. Negative values occur over most of the other lands, with smaller values (up to ~ -1 ppm) mostly over South and East Asia. Over the oceans, values are mostly positive north of 30°N and south of 10°S , and negative in between. Both errors in ACOS-GOSAT and errors in the model simulations contribute to these differences, which complicates the interpretation of Fig. 2a. For instance, the zonal structure of the differences over

the oceans could well be caused by the model, either because of too few surface air-sample sites in the Tropics or because the LMDZ transport model would not represent the inter-hemispheric exchange well enough (Patra et al. 2011). Alternatively, misrepresented clouds around the convergence zones could also induce them in the retrievals. Some of the patterns of Fig. 2a are similar to the surface cover, like the gradient between the Sahel and the African savannahs, or the one between the equatorial Atlantic and the African savannahs, while we expect the true XCO₂ fields to be first driven by large-scale horizontal advection (Keppel-Aleks et al. 2011). The main local spatial gradients in the mean differences are also seen on monthly means despite less data density (Fig. 3). They mostly reflect the retrieval gradients (Fig. 1a), because the model XCO₂ simulation is spatially smoother (Fig. 1b), even though it uses the retrieval averaging kernels (that change from scene to scene as a function, among other factors, of surface conditions) and even though it is sampled like the retrievals (i.e. with a spatially heterogeneous data density, also varying as a function, among other things, of surface conditions).

The jump of the long-term mean difference from the African savannahs to Sahel or equatorial Atlantic (while there is no jump between subtropical Atlantic and Western Sahara for instance) mostly corresponds to data from March (Fig. 3a), at the end of the savannah burning season (e.g. van der Werf et al. 2010). The model shows elevated values (Fig. 1b), but much less than the retrievals (Fig. 1a). If the model was underestimating the intensity of the fire, we would expect the mean difference to take the shape of a plume, i.e. to spread downstream the source region, but this is not the case. This suggests that the retrievals are affected by systematic errors over this region.

The positive differences of Fig. 2a in Eurasia notably follow the boreal forests, while negative values are found over the neighbouring regions of sparse tundra vegetation north of Siberia, or those of grassland/cropland south of them. The same remark applies to North America. The link with boreal forests is less obvious when looking at one isolated year because of the relatively small

291 number of retrievals in these regions (not shown). The misfit pattern in Siberia and in North
292 America contains many values larger than 1 ppm corresponding to relatively large retrieved XCO₂
293 (Fig. 1a). These large values are all the more surprising that retrievals in these high latitudes are
294 obtained during the growing season and that boreal forests in Eurasia are identified as large carbon
295 sinks by bottom-up inventories (Pan et al. 2011, Dolman et al. 2012). By comparison, we can look
296 at agricultural regions, where the model could miss gradients during crop growth, both because the
297 MACC inversion prior fluxes do not explicitly represent agricultural practices and because the
298 location of the assimilated surface air-sample measurements only provides rough information about
299 crop fluxes: the differences are marginal (-0.1 ppm on average, whether we compute the mean at
300 the global scale or only for latitudes above 40°N) for retrievals located in crop regions, as identified
301 by the high-resolution land cover map of ESA's Land Cover Climate Change Initiative project
302 (<http://www.esa-landcover-cci.org/>). In the Corn Belt, the intensively agricultural region in the
303 Midwest of the USA, differences are negative, but they are much smaller in absolute value (the
304 differences are larger than -0.4 ppm) than over the boreal forests, and the Corn Belt boundaries do
305 not sharply appear, in particular on its eastern side. The Corn Belt does not particularly appear in
306 monthly means either (e.g., Fig. 3b). These elements suggest that the long-term mean differences
307 over boreal forests come from a retrieval artifact rather than from the MACC inversion product.

308 From a radiative transfer point of view, boreal forests are largely covered with needle-leaved
309 trees with low albedo in the strong CO₂ spectral band of GOSAT near 2.1 μm (Fig. 4): these low
310 values hamper the XCO₂ retrieval. O'Dell et al. (2012) already showed that large positive biases
311 can occur for needle-leaved evergreen forests, with the retrieval exchanging surface albedo for very
312 thin cloud or aerosol. Extreme cases are filtered out by the ACOS-GOSAT quality control, but Fig.
313 2a suggests that the remaining retrievals over boreal forests, including the region in Siberia East of
314 100°E which is dominated by deciduous needle-leaved trees with slightly larger albedos, are still

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biased. In temperate regions, south of 50°N, the differences for needle-leaf cover (mainly in Southeast USA and Southeast China) have the opposite sign, but they do not show up distinctly in the difference map like the boreal forests. Tropical forests in South America and in Africa also have low albedo and correspond to negative differences. They are more identifiable in Fig. 2a, but could be explained by an insufficient carbon sink in the model as well as by a retrieval artifact.

4.2. Link to the retrieval increment

We now look at the XCO₂ misfit statistics over land and for the high-gain mode as a function of the size of the retrieval increment to its prior information (XCO₂^a - XCO₂^b) in Fig. 5. We look at the misfits of the model to XCO₂^a, to XCO₂^{a,c} and to XCO₂^b, in order to visualize the added value brought by the retrieval process and by the bias correction, successively, on top of the prior estimate. This prior estimate about atmospheric CO₂ has been provided to the retrieval scheme by a data-driven empirical model (Wunch et al. 2011a). In Fig. 5, each bin along the abscissa encompasses a large diversity of times during the four years and a large diversity of locations over the globe, over which the model simulation should be overall more accurate (smaller root mean square error) than XCO₂^b, XCO₂^a and even XCO₂^{a,c} (Chevallier and O'Dell 2013). Further, we expect the model error to be uncorrelated with the error of XCO₂^b, XCO₂^a and XCO₂^{a,c} so that a smaller standard deviation of the misfits (e.g., using XCO₂^a rather than XCO₂^b) can be interpreted in terms of better precision of the corresponding retrieval quantity.

The mean difference significantly varies with the increment size: starting at 0.7 ppm for the smallest increments it reaches about 2 ppm and -1 ppm, for XCO₂^b and XCO₂^a respectively. As expected, the mean difference is systematically better with XCO₂^a than with XCO₂^b. The bias correction (XCO₂^{a,c}) further reduces the mean difference to a small extent.

339 The standard deviation for XCO_2^b is 1.1 ppm for small increments and smoothly increases to 2
340 ppm for retrieval increments of size 6 ppm. This trend demonstrates some skill of the retrieval
341 algorithm to characterize the error of XCO_2^b from the GOSAT radiances and to generate a sizeable
342 increment accordingly. By comparison, the model variability for a given increment size over the
343 four years ranges between 3 and 4 ppm (1σ), the prior variability is about 3 ppm and the retrieval
344 variability ranges between 3 and 7 ppm. The standard deviation that uses XCO_2^a is 1.1 ppm for
345 small increments. It smoothly increases to 4 ppm for retrieval increments of size 6 ppm: it is
346 systematically larger than the standard deviation that uses XCO_2^b (despite a smaller mean
347 difference). The standard deviation that uses $\text{XCO}_2^{a,c}$ is also 1.1 ppm for small increments and is
348 also systematically larger than the standard deviation that uses XCO_2^b , but it performs better than
349 XCO_2^a . The worse standard deviation of the misfit of XCO_2^a and $\text{XCO}_2^{a,c}$ to the model compared
350 to XCO_2^b cannot be explained by a common lack of variability in the model and in XCO_2^b (that
351 would correlate the model error with the that of XCO_2^b), because (i) at the large scale, thinning the
352 retrievals (for instance by keeping only one retrieval every nine model grid boxes for a given day)
353 only marginally changes the figure (not shown), and (ii) at the sub-grid scale, the variability of
354 XCO_2 is usually well below the ppm (Alkhaled et al. 2008, Corbin et al. 2008), i.e. one order of
355 magnitude smaller than the prior-to-retrieval degradation. Some, but not all, of the degradation is
356 purely random and disappears after enough averaging (see Fig. 6 of Kulawik et al. 2015).

357 The fact that the standard deviation smoothly increases with increment size suggests that the
358 increment size is systematically overestimated. Fig. 6 presents a simple test where we halve the
359 retrieval increments, without any bias correction: we call $\text{XCO}_2^{a,r} = \text{XCO}_2^b + (\text{XCO}_2^a - \text{XCO}_2^b)/2$
360 the result. The reduction is seen to cancel most of the dependency of the statistics of the
361 observation-minus-model misfits to the increment size: the standard deviation and the mean are
362 then stable around 1.1 ppm and -0.3 ppm, respectively for increments up to 4 ppm without any bias

correction. The standard deviation is systematically better than for XCO_2^b , which shows added value brought by the radiance measurements, in contrast to the previous results. This result also empirically confirms that the initial increments are in the right direction but are too large.

For the medium-gain retrievals (Fig. 7) and for the ocean glint retrievals (Fig. 8), the standard deviation of the misfits using $\text{XCO}_2^{a,c}$ is not significantly larger than that using XCO_2^b .

5. Discussion and conclusions

Small uncertainties in aerosols, cirrus cloud or surface albedo are known to heavily affect the quality of the XCO_2 satellite retrievals and to propagate into biases in the fluxes inverted from them, even when the parasite signal in XCO_2 is sub-ppm. This weakness led the science team of NASA's OCO, a satellite that failed at launch in February 2009, to conclude that the space-based NIR/SWIR measurements of XCO_2 could not be used alone for CO_2 source-sink inversions and that they had to be combined with observations from a reasonable number of surface stations (Miller et al. 2007). However, so much improvement has been obtained in these issues by various institutes during the last few years, that it is sometimes thought that the space-borne XCO_2 retrievals have reached sufficient quality for source-sink inversion. The present paper discusses where we stand in this respect both from general theoretical considerations and from one of the most advanced GOSAT retrieval products.

From the theory, we have shown that a two-step approach to infer the surface fluxes from the GOSAT measured radiances, with CO_2 retrievals as an intermediate product, cannot be optimal. This suboptimality corrupts the 4D information flow from the radiance measurements to the surface flux estimates. It is amplified by the current retrieval strategy where prior errors are much larger (by an order of magnitude in terms of variances) than the performance of prior CO_2 simulations

387 used in atmospheric inversions. Indeed, the use of averaging kernels makes atmospheric inversion
388 insensitive to the choice of a particular retrieval prior CO₂ profile (Connor et al. 1994) if retrievals
389 are assimilated without any bias correction, but it does not make the retrieval prior error statistics
390 disappear from the inverse modelling equations. The current strategy likely generates retrieval
391 averaging kernels that are inappropriate for atmospheric inversions in their default configurations,
392 with a wrong vertical distribution and an excessive weight towards the measured radiances.
393 Paradoxically, empirical bias correction of the retrievals (e.g., Wunch et al., 2011b) also contributes
394 to the degradation of the 4D information flow, because it carries the imprint of the retrieval prior
395 and of the retrieval prior error statistics. Direct assimilation of the measured radiances would solve
396 the inconsistency, but would increase the computational burden of atmospheric inversions by
397 several orders of magnitude. Alternatively, we could adapt the inversion systems to the current
398 retrieval configuration by using minimal prior information about the surface fluxes, typically a flat
399 prior flux field, but the result would still over-fit the measured radiances due to the absence of other
400 (compensating) information.

401 We have compared the ACOS-GOSAT retrievals with a transport model simulation constrained
402 by surface air-sample measurements in order to find some evidence of retrieval sub-optimality.
403 Flaws in this transport model and in these inverted surface fluxes necessarily flaw the simulation
404 in many places over the globe and at various times of the year. We therefore carefully selected
405 some of the relatively large discontinuities in the XCO₂ fields that the simulation unlikely generated.
406 We found some evidence of retrieval systematic errors over the dark surfaces of the high-latitude
407 lands and over African savannahs. We note that the mean differences over the African savannahs
408 during the burning season could be explained by retrieval averaging kernels not peaking low
409 enough in the atmosphere further to the assignment of inappropriate prior error correlations.
410 Biomass burning aerosols that would not be well identified by the retrieval scheme could also play

411 a role. We also found some evidence that the high-gain retrievals over land systematically over-fit
412 the measured radiances, as a consequence of the prior uncertainty overestimation and of an
413 underestimation of the observation uncertainty (as seen by the underlying radiative transfer model).
414 This over-fit is partially compensated by the bias correction. An empirical test indicates that
415 halving the retrieval increments without any posterior bias correction actually cancels the
416 dependency of the statistics of the observation-minus-model misfits to the increment size and
417 makes the standard deviation systematically better than for the retrieval prior XCO_2^b , which shows
418 added value brought by the radiance measurements, in contrast to the previous results. We argue
419 here that the optimal-estimation retrieval process and, consequently, its posterior bias correction
420 need retuning.

421 Given the diversity of existing satellite retrieval algorithms, our conclusions cannot be easily
422 extrapolated to other GOSAT retrieval products and even less to XCO_2 retrievals from other
423 instruments, but we note that such mistuning like the one highlighted here is common practice,
424 both because the errors of the retrieval forward model are difficult to characterize and because
425 satellite retrievals are usually explicitly designed to maximize the observation contribution, at the
426 risk of over-fitting radiance and forward model noise. A primary consequence of this mistuning is
427 the usual underestimation of retrieval errors: for instance, O'Dell et al. (2012) recommended
428 inflating this error by a twofold factor for ACOS-GOSAT b2.8. More importantly, our results show
429 that the mistuning generates excessive (unphysical) space-time variations of the retrievals up to
430 ~1%. This noise level would not matter for short-lived species, but for CO_2 it is enough to
431 significantly degrade the assimilation of the retrievals for flux inversion and may explain some of
432 the inconsistency seen between GOSAT-based top-down results and bottom-up results for CO_2
433 (Chevallier et al. 2014, Reuter et al. 2014). Therefore, with the current mistuning, we reiterate
434 previous recommendations to take GOSAT-based CO_2 inversion results particularly cautiously.

435 But we also suggest that this situation may dramatically improve by simply retuning the retrieval
436 schemes. Ultimately, internal statistical consistency of the retrievals and of the inversion schemes
437 is needed to establish the credibility of their end product.

438

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Locality (indentifier)	Period	Source
Alert, Nunavut, CA (ALT)	1988-2012	WDCGG/EC
Amsterdam Island, FR (AMS)	1981-2011	LSCE
Argyle, Maine, US (AMT)	2003-2011	NOAA/ESRL
Anmyeon-do, KR (AMY)	1999-2012	WDCGG/KMA
Barrow, Alaska, US (BRW)	1979-2013	NOAA/ESRL
Candle Lake, CA (CDL)	2002-2012	WDCGG/EC
Monte Cimone, IT (CMN)	1996-2010	WDCGG/IAFMS
Cape Ochi-ishi, JP (COI)	1995-2002	WDCGG/NIES
Cape Point, SA (CPT)	1993-2013	WDCGG/SAWS
Egbert, CA (EGB)	2005-2012	WDCGG/EC
East Trout Lake, CA (ETL)	2005-2012	WDCGG/EC
Frasedale, CA (FSD)	1990-2012	WDCGG/EC
Hateruma, JP (HAT)	1993-2002	WDCGG/NIES
Hegyhatsal tower, 115m level, HU (HUN0115)	1994-2013	WDCGG/HMS
Tenerife, Canary Islands, ES (IZO)	1984-2013	WDCGG/AEMET
Jubany, Antarctica, AR (JBN)	1994-2009	WDCGG/ISAC-IAA WDCGG/Univ. Of
Jungfraujoeh, CH (JFJ)	2004-2013	Bern
K-pusztá, HU (KPS)	1981-1999	WDCGG/HMS
Park Falls, Wisconsin, US (LEF)	2003-2011	NOAA/ESRL
Mace Head, County Galway, IE (MHD)	1992-2012	LSCE

Mauna Loa, Hawaii, US (MLO)	1979-2013	NOAA/ESRL
Minamitorishima, JP (MNM)	1993-2013	WDCGG/JMA
Pallas-Sammaltunturi, GAW Station, FI (PAL)	1999-2013	WDCGG/FMI WDCGG/CESI
Plateau Rosa, IT (PRS)	2000-2013	RICERCA
Puy de Dôme, FR (PUY)	2000-2010	LSCE
Ryori, JP (RYO)	1987-2013	WDCGG/JMA
Tutuila, American Samoa (SMO)	1979-2013	NOAA/ESRL
Sonnblick, AU (SNB)	1999-2013	WDCGG/EEA
South Pole, Antarctica, US (SPO)	1979-2013	NOAA/ESRL
Tsukuba tower, 200m level, JP (TKB)	1986-2000	WDCGG/MRI
Westerland, DE (WES)	1979-2013	WDCGG/UBA
Moody, Texas, US (WKT)	2003-2011	NOAA/ESRL
Yonagunijima, JP (YON)	1997-2013	WDCGG/JMA

Table 1: List of the continuous sites used in the MACC CO₂ inversion v13r1 together with the period of coverage (defined as the period between the first sample and the last one), and the data source. Each station is identified by the name of the place, the corresponding country (abbreviated) and the code used in the corresponding database.

Locality (identifier)	Period	Source
Alert, Nunavut, CA (ALT)	1985–2013	NOAA/ESRL
Amsterdam Island, FR (AMS)	1979–1990	NOAA/ESRL
Amsterdam Island, FR (AMS)	2003–2013	LSCE
Ascension Island, GB (ASC)	1979–2013	NOAA/ESRL
Assekrem, DZ (ASK)	1995–2013	NOAA/ESRL
St. Croix, Virgin Islands, USA (AVI)	1979–1990	NOAA/ESRL
Terceira Island, Azores, PT (AZR)	1979–2013	NOAA/ESRL
Baltic Sea, PL (BAL)	1992–2011	NOAA/ESRL
Bering Island, RU (BER)	1986–1994	WDCGG/MGO
Begur, ES (BGU)	2000–2013	LSCE/IC3
Baring Head, NZ (BHD)	1999–2013	NOAA/ESRL
Baring Head, NZ (BHD)	1979–2011	WDCGG/NIWA
Bukit Kototabang, ID (BKT)	2004–2013	NOAA/ESRL
St. Davids Head, Bermuda, GB (BME)	1989–2009	NOAA/ESRL
Tudor Hill, Bermuda, GB (BMW)	1989–2013	NOAA/ESRL
Barrow, Alaska, US (BRW)	1979–2013	NOAA/ESRL
Portsall, FR (BZH)	1998–2001	CarboEurope/LSCE
Cold Bay, Alaska, US (CBA)	1979–2013	NOAA/ESRL
Cape Ferguson, AU (CFA)	1991–2013	WDCGG/CSIRO
Cape Grim, Tasmania, AU (CGO)	1984–2013	NOAA/ESRL
Christmas Island, Republic of Kiribati (CHR)	1984–2013	NOAA/ESRL

Cape Meares, Oregon, US (CMO)	1982–1998	NOAA/ESRL
Crozet Island, FR (CRZ)	1991–2013	NOAA/ESRL
Cape St. James, CA (CSJ)	1979–1992	WDCGG/EC
Casey Station, AU (CYA)	1996–2013	WDCGG/CSIRO
Drake Passage (DRP)	2003–2013	NOAA/ESRL
Easter Island, CL (EIC)	1994–2013	NOAA/ESRL
Estevan Point, British Columbia, CA (ESP)	1992–2012	WDCGG/EC
Estevan Point, British Columbia, CA (ESP)	1993–2001	WDCGG/CSIRO
Finokalia, Crete, GR (FIK)	1999–2013	LSCE
Mariana Islands, Guam (GMI)	1979–2013	NOAA/ESRL
Dwejra Point, Gozo, MT (GOZ)	1993–1999	NOAA/ESRL
Halley Station, Antarctica, GB (HBA)	1983–2013	NOAA/ESRL
Hohenpeissenberg, DE (HPB)	2006–2013	NOAA/ESRL
Hegyhatsal, HU (HUN)	1993–2013	NOAA/ESRL
Storhofdi, Vestmannaeyjar, IS (ICE)	1992–2013	NOAA/ESRL
Grifton, North Carolina, US (ITN)	1992–1999	WDCGG/ESRL
Tenerife, Canary Islands, ES (IZO)	1991–2013	NOAA/ESRL
Key Biscayne, Florida, US (KEY)	1979–2013	NOAA/ESRL
Kotelny Island, RU (KOT)	1986–1993	WDCGG/MGO
Cape Kumukahi, Hawaii, US (KUM)	1979–2013	NOAA/ESRL

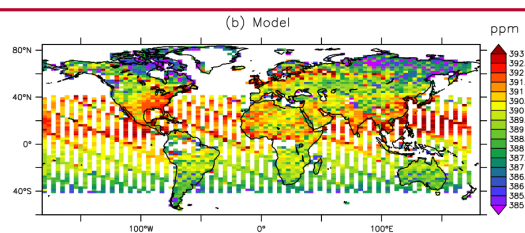
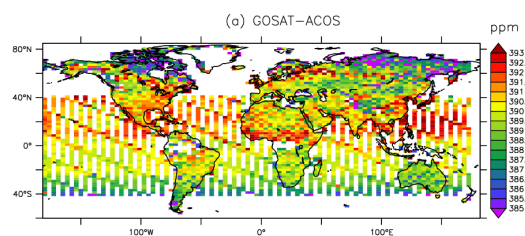
Sary-Taukum, KZ (KZD)	1997-2009	NOAA/ESRL
Plateau Assy, KZ (KZM)	1997-2009	NOAA/ESRL
Lulin, TW (LLN)	2006-2013	NOAA/ESRL
Lampedusa, IT (LMP)	2006-2013	NOAA/ESRL
He grande, FR (LPO)	2004-2013	LSCE
Mawson, AU (MAA)	1990-2013	WDCGG/CSIRO
Mould Bay, Nunavut, CA (MBC)	1980-1997	NOAA/ESRL
Mace Head, County Galway, IE		
(MHD)	1991-2013	NOAA/ESRL
Mace Head, County Galway, IE		
(MHD)	1996-2013	LSCE
Sand Island, Midway, US (MID)	1985-2013	NOAA/ESRL
Mt. Kenya, KE (MKN)	2003-2011	NOAA/ESRL
Mauna Loa, Hawaii, US (MLO)	1979-2013	NOAA/ESRL
Macquarie Island, AU (MQA)	1990-2013	WDCGG/CSIRO
Gobabeb, NA (NMB)	1997-2013	NOAA/ESRL
Niwot Ridge, Colorado, US		
(NWR)	1979-2013	NOAA/ESRL
Olympic Peninsula, WA, USA		
(OPW)	1984-1990	NOAA/ESRL
Ochsenkopf, DE (OXK)	2003-2013	NOAA/ESRL
Pallas-Sammaltunturi, GAW		
Station, FI (PAL)	2001-2013	NOAA/ESRL

Pie du Midi, FR (PDM)	2001-2013	LSCE
Pacific Ocean, 0N (POC000)	1987-2011	NOAA/ESRL
Pacific Ocean, 5N (POCN05)	1987-2011	NOAA/ESRL
Pacific Ocean, 10N (POCN10)	1987-2011	NOAA/ESRL
Pacific Ocean, 15N (POCN15)	1987-2011	NOAA/ESRL
Pacific Ocean, 20N (POCN20)	1987-2011	NOAA/ESRL
Pacific Ocean, 25N (POCN25)	1987-2011	NOAA/ESRL
Pacific Ocean, 30N (POCN30)	1987-2011	NOAA/ESRL
Pacific Ocean, 5S (POCS05)	1987-2011	NOAA/ESRL
Pacific Ocean, 10S (POCS10)	1987-2011	NOAA/ESRL
Pacific Ocean, 15S (POCS15)	1987-2011	NOAA/ESRL
Pacific Ocean, 20S (POCS20)	1987-2011	NOAA/ESRL
Pacific Ocean, 25S (POCS25)	1987-2011	NOAA/ESRL
Pacific Ocean, 30S (POCS30)	1987-2011	NOAA/ESRL
Pacific Ocean, 35S (POCS35)	1987-2011	NOAA/ESRL
Palmer Station, Antarctica, US (PSA)	1979-2013	NOAA/ESRL
Point Arena, California, US (PTA)	1999-2011	NOAA/ESRL
Puy de Dome, FR (PUY)	2001-2013	LSCE
Ragged Point, BB (RPB)	1987-2013	NOAA/ESRL
South China Sea, 3N (SCSN03)	1991-1998	NOAA/ESRL
South China Sea, 6N (SCSN06)	1991-1998	NOAA/ESRL
South China Sea, 9N (SCSN09)	1991-1998	NOAA/ESRL
South China Sea, 12N (SCSN12)	1991-1998	NOAA/ESRL
South China Sea, 15N (SCSN15)	1991-1998	NOAA/ESRL

South China Sea, 18N (SCSN18)	1991-1998	NOAA/ESRL
South China Sea, 21N (SCSN21)	1991-1998	NOAA/ESRL
Mahe Island, SC (SEY)	1980-2013	NOAA/ESRL
Southern Great Plains, Oklahoma, US (SGP)	2002-2013	NOAA/ESRL
Shemya Island, Alaska, US (SHM)	1985-2013	NOAA/ESRL
Ship between Ishigaki Island and Hateruma Island, JP (SIH)	1993-2005	WDCGG/Tohoku University
Shetland, Scotland, GB (SIS)	1992-2003	WDCGG/CSIRO
Tutuila, American Samoa (SMO)	1979-2013	NOAA/ESRL
South Pole, Antarctica, US (SPO)	1979-2013	NOAA/ESRL
Ocean Station M, NO (STM)	1980-2009	NOAA/ESRL
Summit, GL (SUM)	1997-2013	NOAA/ESRL
Syowa Station, Antarctica, JP (SYO)	1986-2013	NOAA/ESRL
Tae-ahn Peninsula, KR (TAP)	1991-2013	NOAA/ESRL
Tierra Del Fuego, Ushuaia, AR (TDF)	1994-2013	NOAA/ESRL
Trinidad Head, California, US (THD)	2002-2013	NOAA/ESRL
Tromelin Island, F (TRM)	1998-2007	LSCE
Wendover, Utah, US (UTA)	1993-2013	NOAA/ESRL
Ulaan-Uul, MN (UUM)	1992-2013	NOAA/ESRL

Sede Boker, Negev Desert, IL		
(WIS)	1995-2013	NOAA/ESRL
Sable Island, CA (WSA)	1979-2012	WDCGG/EC
Mt. Waliguan, CN (WLG)	1990-2013	NOAA/ESRL
Western Pacific Cruise (WPC)	2004-2013	NOAA/ESRL
Ny Alesund, Svalbard, Norway		
and Sweden (ZEP)	1994-2013	NOAA/ESRL

Table 2: Same as Table 1 but for the flask sampling sites.



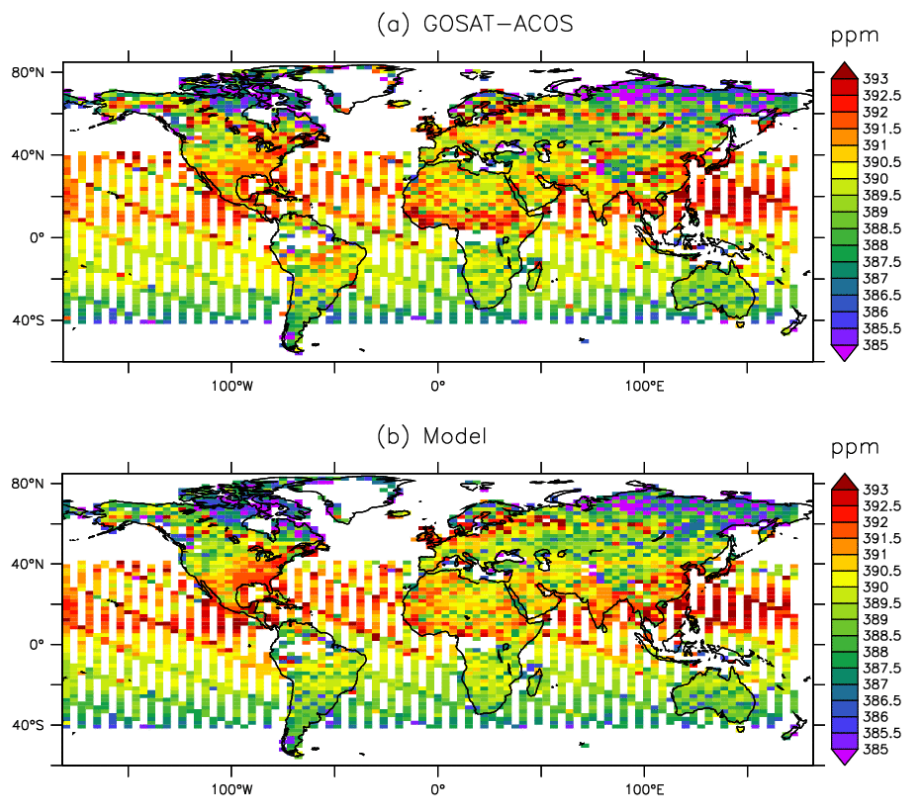
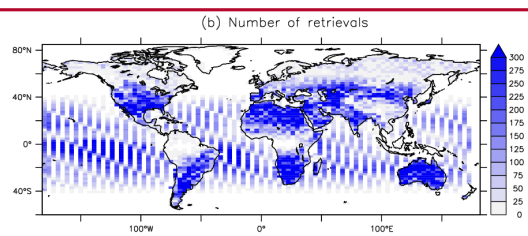
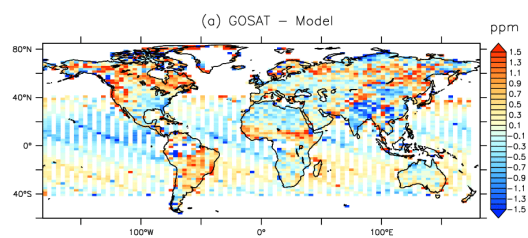


Fig. 1. (a) Mean ACOS-GOSAT bias-corrected retrievals in the model grid over 4 years (June 2009-May 2013). (b) Corresponding mean CO₂ 4D field associated to the MACC CO₂ inversion (computed using the averaging kernels and the prior profiles of the retrievals).



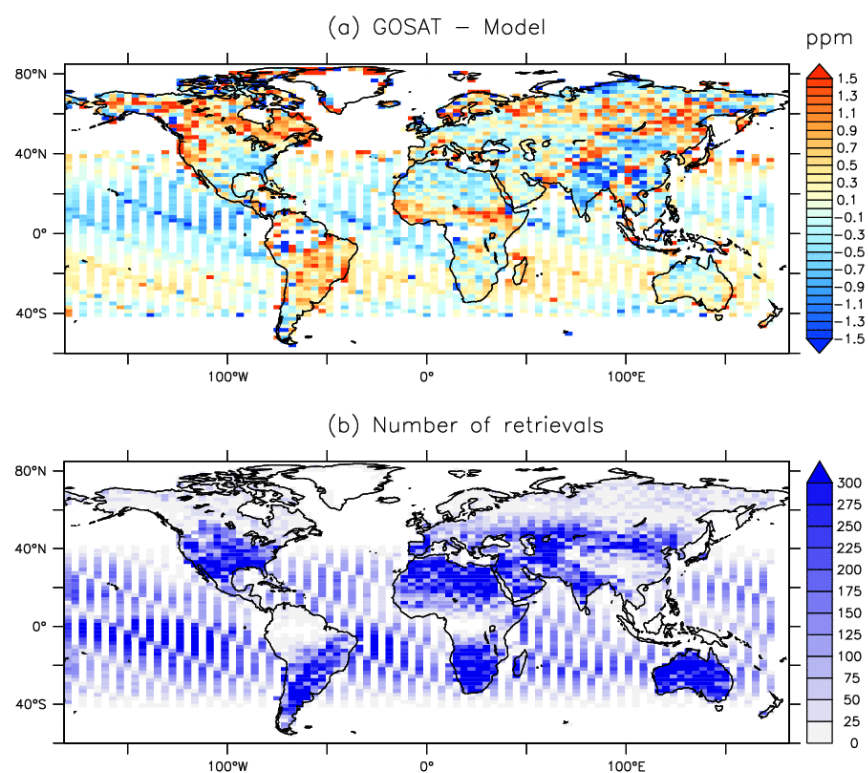
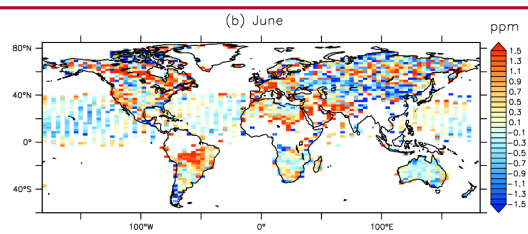
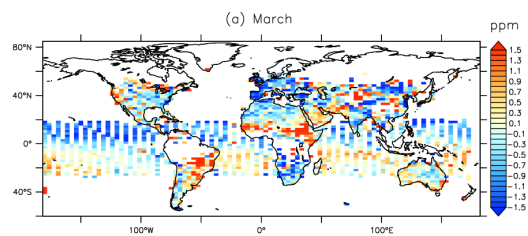


Fig. 2. (a) Mean difference between the maps of Fig. 1 (retrievals minus model). (b) Corresponding number of retrievals.



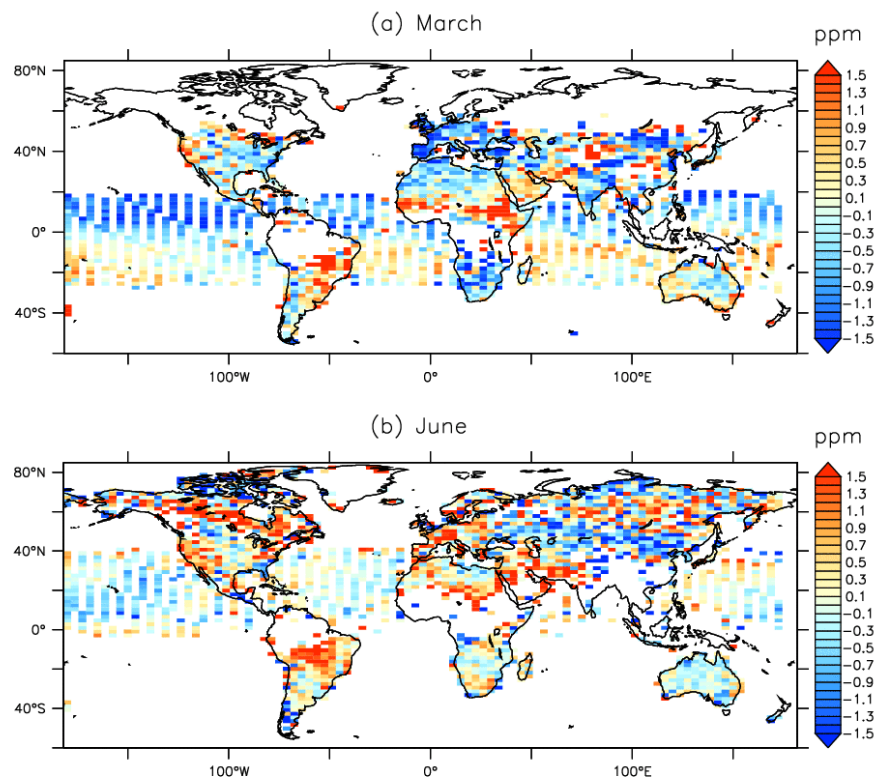
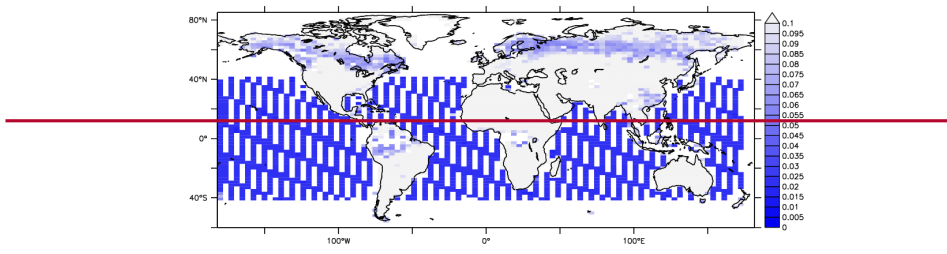


Fig. 3. Same as Fig. 2(a) (retrievals minus model), but focussing on the months of March and June.



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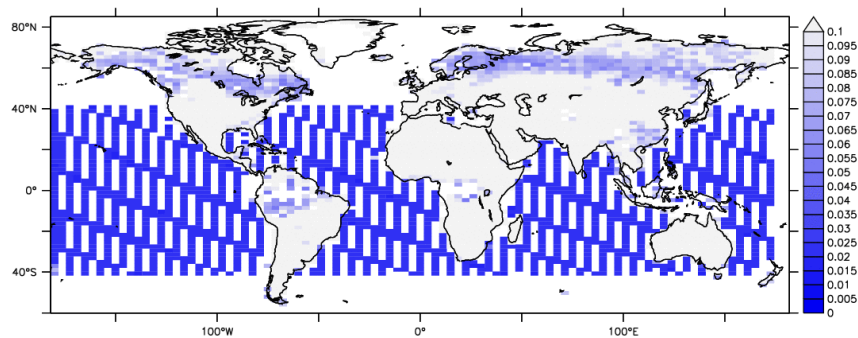
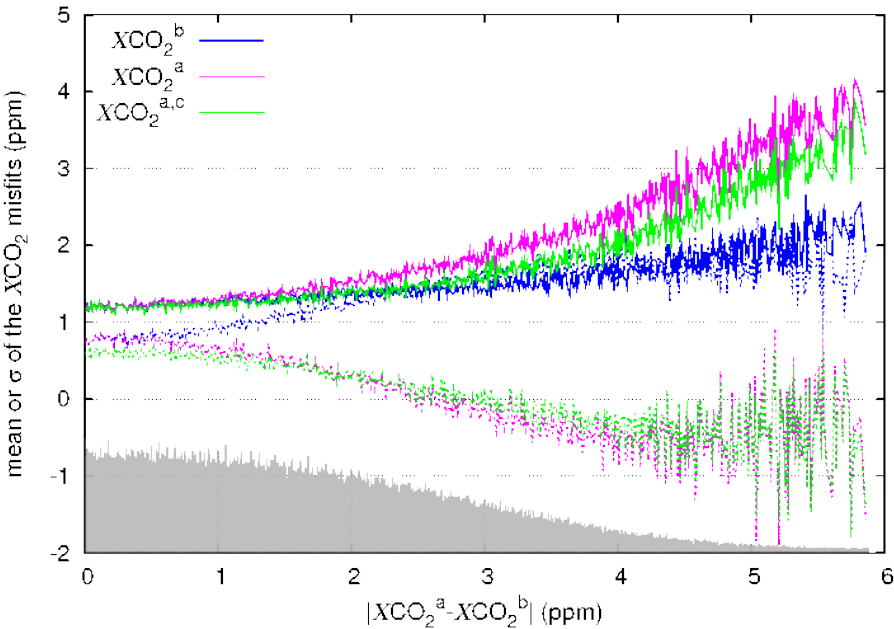


Fig. 4. Mean surface albedo retrieved in the strong CO₂ band by ACOS-GOSAT in the model grid over 4 years (June 2009-May 2013). The blue scale focuses on the values less than 0.1.

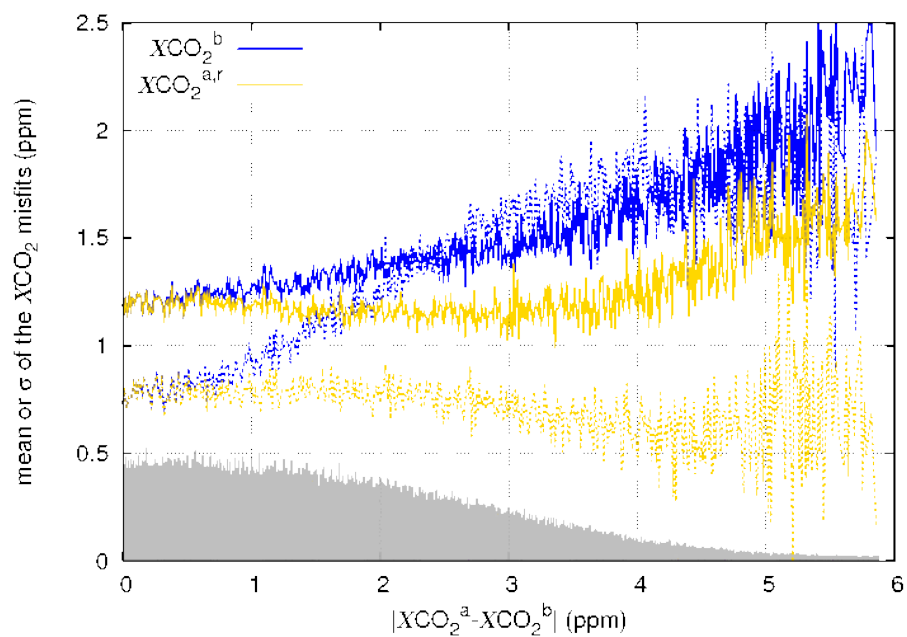
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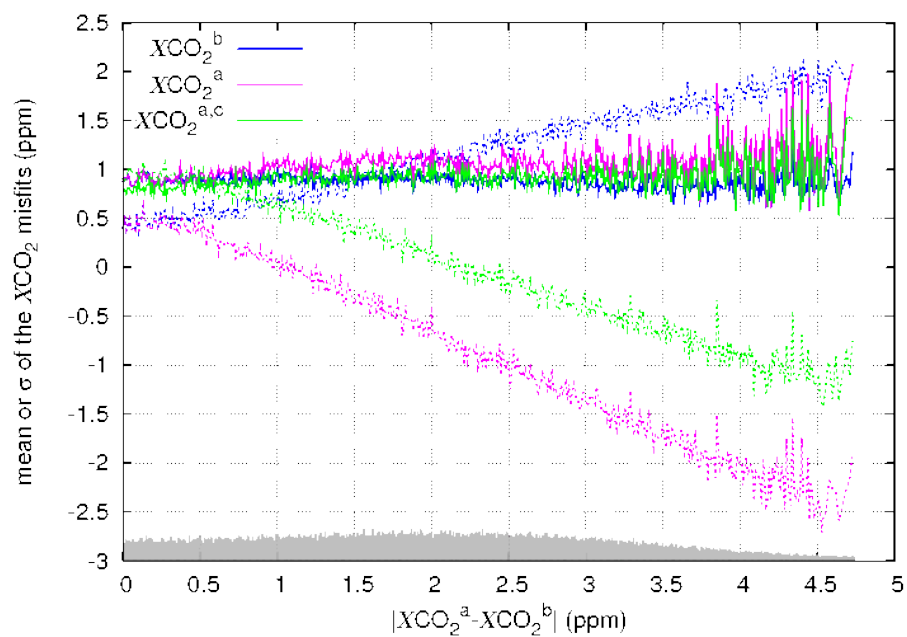
682 **Fig. 5. Mean and standard deviation of the retrieval-minus-model misfits between June**
683 **2009 and May 2013 for the high-gain mode retrievals over land as a function of the retrieval**
684 **increment size. The statistics are also shown for the prior-minus-model misfit. The model**
685 **values are raw pressure-weighted columns and do not account for the averaging kernels in**
686 **order not to correlate the two axes (in practice, using the averaging kernels actually does**
687 **not significantly affect the standard deviations shown). The grey shade shows the**
688 **distribution of the retrieval density (axis not shown).**

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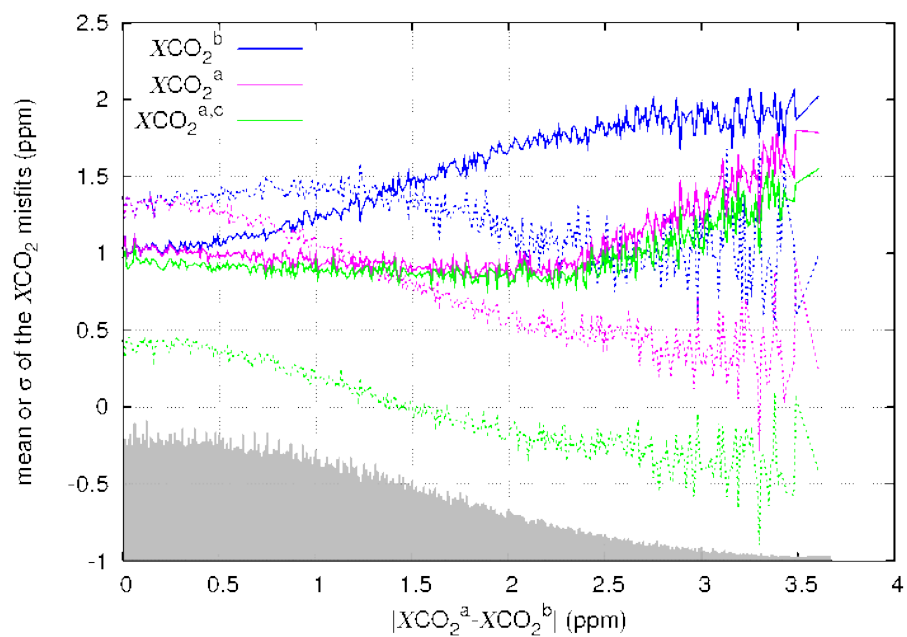
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 691 **Fig. 6. Same as Fig. 5 (high-gain mode over the lands) but we reduce the retrieval increment**
 692 **size by 50% without any bias correction (we call $XCO_2^{a,r}$ the result). The abscissa shows the**
 693 **unperturbed increment.**

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 695



696

697 **Fig. 7.** Same as Fig. 5 for the medium-gain mode.



698

699 **Fig. 8. Same as Fig. 5 for the glint mode over the ocean.**

700