

1 The Role of Ice Nuclei Recycling in the Maintenance of Cloud Ice in  
2 Arctic Mixed-Phase Stratocumulus

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11 July 31, 2015

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## Abstract

13 This study investigates the maintenance of cloud ice production in Arctic mixed phase  
14 stratocumulus in large eddy simulations that include a prognostic ice nuclei (IN) formulation  
15 and a diurnal cycle. Balances derived from a mixed-layer model and phase analyses are used  
16 to provide insight into buffering mechanisms that maintain ice in these cloud systems. We  
17 find that for the case under investigation, IN recycling through subcloud sublimation  
18 considerably prolongs ice production over a multi-day integration. This effective source of  
19 IN to the cloud dominates over mixing sources from above or below the cloud-driven mixed  
20 layer. Competing feedbacks between dynamical mixing and recycling are found to slow the  
21 rate of ice lost from the mixed layer when a diurnal cycle is simulated. The results of this  
22 study have important implications for maintaining phase partitioning of cloud ice and liquid  
23 that determine the radiative forcing of Arctic mixed-phase clouds.

## 24 **1 Introduction**

25 Reliable climate projections require realistic simulations of Arctic cloud feedbacks. Of  
26 particular importance is accurately simulating Arctic mixed-phase stratocumuli (AMPS),  
27 which are ubiquitous and play an important role in regional climate due to their impact on the  
28 surface energy budget and atmospheric boundary layer structure through cloud-driven  
29 turbulence, radiative forcing, and precipitation (Curry et al., 1992; Walsh and Chapman,  
30 1998; Intrieri et al., 2002; Shupe and Intrieri, 2004; Sedlar et al., 2011; Persson, 2012). For  
31 example, Bennartz et al. (2012) showed that the extreme melt events observed at Summit,  
32 Greenland in July 2012 would not have occurred without the surface radiative forcing  
33 produced by AMPS.

34 AMPS are characterized by a liquid cloud layer with ice crystals that precipitate from cloud  
35 base even at temperatures well below freezing (Hobbs and Rangno, 1998; Intrieri et al.,  
36 2002; McFarquhar et al., 2007). Radiative cooling near cloud top generates turbulence that  
37 maintains the liquid layer and forms an approximately well-mixed layer that extends as far as  
38 500 meters below cloud base. These cloud-driven mixed layers are frequently decoupled  
39 from the surface layer, limiting the impact of fluxes of heat, moisture, and aerosols on the  
40 cloud layer from below (Solomon et al., 2011; Shupe et al., 2013). However, unlike  
41 subtropical cloud-topped boundary layers where decoupling enhances cloud breakup by  
42 cutting the cloud system off from the surface source of moisture, decoupled AMPS can  
43 persist for extended periods of time due to weak precipitation fluxes out of the mixed layer  
44 and relatively moist air entrained into the cloud layer at cloud top (Tjernström et al., 2004;  
45 Solomon et al., 2011; Sedlar et al., 2012; Solomon et al., 2014).

46 AMPS are challenging to model due to uncertainties in ice microphysical processes that  
47 determine phase partitioning between ice and radiatively important cloud liquid water  
48 (Sandvik et al., 2007; Tjernström et al., 2008; Klein et al., 2009, Karlsson and Svensson,  
49 2011; Barton et al., 2012; Birch et al., 2012; de Boer et al., 2012), which drives turbulence  
50 that maintains the system. Phase partitioning depends upon the number, shape, and size of ice  
51 crystals, since these determine the efficiency of water vapor uptake by ice and hence the  
52 availability of water vapor for droplet formation (Chen and Lamb, 1994; Sheridan et al.,  
53 2009; Ervens et al., 2011; Hoose and Möhler, 2012).

54 Since temperatures in AMPS are too warm for homogenous ice nucleation, ice must form  
55 through heterogeneous nucleation. Aerosols with properties to serve as seeds for  
56 heterogeneous ice crystal formation are referred to as ice nuclei (IN). A number of different  
57 aerosols such as mineral dust (Broadley et al., 2012; Kulkarni et al., 2012; Lüönd et al., 2010;  
58 Möhler et al. 2006; Pinti et al., 2012; Welti et al., 2009), soot (DeMott, 1990), sea salts (Wise  
59 et al., 2012), and bacteria (Kanji et al., 2011; Levin and Yankofsky, 1983) have been  
60 observed to act as IN, all of which nucleate at different temperatures and supersaturation  
61 ranges. In addition, observations indicate that nucleation properties are modified by aging  
62 and coating of aerosols (Möhler et al., 2005; Cziczo et al. 2009). Heterogeneous ice  
63 nucleation can occur by a number of modes: either in the presence of super-cooled droplets,  
64 when an aerosol comes into contact with a droplet (contact freezing), is immersed in a  
65 droplet (immersion freezing), or by vapor deposition on IN (deposition freezing) (Pruppacher  
66 and Klett, 1997).

67 IN can be entrained into the cloud-driven mixed layer through turbulent mixing from above  
68 and/or below. Recent studies indicate that entrainment alone cannot account for observed ice  
69 crystal number concentration ( $N_{ICE}$ ) (Fridlind et al., 2012), motivating the use of diagnostic  
70 formulations for ice formation to produce model simulations of AMPS with realistic phase  
71 partitioning (Ovchinnikov et al., 2011). While this modeling strategy constrains  $N_{ICE}$  to be  
72 close to the measured values it eliminates the dynamical-microphysical feedbacks that  
73 regulate ice/liquid phase partitioning (Avramov et al., 2011).

74 Here we investigate a relatively unexplored source of ice production--recycling of ice  
75 nuclei in regions of ice subsaturation. AMPS frequently have ice-subsaturated air near the  
76 cloud-driven mixed-layer base where falling ice crystals can sublimate, leaving behind IN.  
77 This feedback loop is referred to hereon as “recycling”. Recycling was found to be  
78 significant in large eddy simulations of a single-layer stratocumulus observed during the  
79 Department of Energy Atmospheric Radiation Measurement Program’s Mixed-Phase Arctic  
80 Cloud Experiment (M-PACE; Verlinde et al., 2007; Fan et al., 2009). AMPS observed during  
81 M-PACE formed due to a cold-air outbreak, where large fluxes of heat and moisture over the  
82 open ocean forced turbulent roll clouds that were coupled to the surface layer. This coupling  
83 with the surface layer prevented the identification of the role of dynamics internal to the  
84 cloud-driven mixed layer in maintaining phase-partitioning.

85 In this study we focus on the internal microphysics and dynamics of the cloud-driven mixed  
86 layer by investigating processes in an AMPS decoupled from surface sources of moisture,  
87 heat, and ice nuclei. We posit that recycling plays a significant role more generally since, for  
88 example, assuming an adiabatic vertical profile, a 650 meter-deep mixed layer with a cloud-

89 top temperature of  $-16^{\circ}\text{C}$  requires a water vapor mixing ratio of at least  $1.7 \text{ g kg}^{-1}$  at mixed-  
90 layer base to be saturated with respect to ice, i.e., in order for recycling to be a *negligible*  
91 source of ice nuclei in the mixed layer. This value is typically only seen in the Arctic  
92 between May-September (Serreze et al., 2012), while persistent AMPS frequently occur  
93 outside of these months (Shupe et al., 2011).

94 We examine the role of IN recycling in maintaining ice production using large eddy  
95 simulations of a springtime decoupled AMPS. Three simulations are analyzed; a “Control”  
96 with recycling turned on and shortwave radiation turned off (to compare with previous  
97 simulations of this case that use different IN formulations and shortwave radiation turned off),  
98 “NoRecycle” with IN recycling turned off to identify the impact of recycling on the cloud  
99 life-time and phase partitioning, and “SW” with recycling and shortwave radiation turned on  
100 to identify the impact of realistic diurnal heating and cooling tendencies on the recycling  
101 process. This study builds on previous studies of this case, all of which exclude shortwave  
102 radiation (Avramov et al., 2011; Solomon et al., 2011, 2014), by including a prognostic  
103 equation for IN and a diurnal cycle. Within this modeling framework we investigate the  
104 relative roles of recycling and entrainment of IN in maintaining cloud ice production.

## 105 **2 Case Description**

106 The case derives from observations of a persistent single-layer Arctic mixed-phase  
107 stratocumulus cloud observed near Barrow, AK on 8 April 2008 during the Indirect and  
108 Semi-Direct Aerosol Campaign (McFarquhar et al., 2011) (see Fig. 1). The adjacent Beaufort  
109 Sea was generally ice covered during this time, with significant areas of open water observed  
110 east of Barrow. A 4-K temperature inversion with inversion base at 1.05 km was observed

111 via a radiosonde at 17:34UTC; static stability was near neutral within the mixed layer  
112 overlaying a stable near-surface layer with static stability greater than  $2 \text{ K km}^{-1}$  below 500 m.  
113 The water vapor mixing ratio,  $q_v$ , decreased from  $1.7 \text{ g kg}^{-1}$  at the surface to  $1.2 \text{ g kg}^{-1}$  at  
114 cloud top, above which a secondary maximum of  $1.6 \text{ g kg}^{-1}$  was observed. Winds were east-  
115 southeasterly throughout the lowest 2 km.

116 Measurements from ground-based, vertically pointing, 35-GHz cloud radar, micropulse lidar,  
117 and dual-channel microwave radiometer at Barrow indicated a mixed-phase cloud layer  
118 starting at 8 UTC on 8 April 2008 with a cloud top at approximately 1.5km that slowly  
119 descended to approximately 0.5 km over a 26 hour period. At the time of the 17:34 sounding  
120 the cloud layer extended into the inversion by 100 m, had a cloud base at 0.9 km, and cloud  
121 top at 1.15 km. Cloud ice water path (IWP), derived from cloud radar reflectivity  
122 measurements, varied from  $20\text{--}120 \text{ g m}^{-2}$  within 10 min of the sounding, with an uncertainty  
123 of up to a factor of 2 (Shupe et al., 2006). Concurrently liquid water path (LWP), derived  
124 from dual-channel microwave radiometer measurements, was  $39\text{--}62 \text{ g m}^{-2}$ , with an  
125 uncertainty of  $20\text{--}30 \text{ g m}^{-2}$  (Turner et al., 2007).

126 Research flights were conducted by the National Research Council of Canada Convair-580 at  
127 22:27-23:00 UTC on 8 April 2008 over the ocean northwest of Barrow (McFarquhar et al.,  
128 2011). Droplet concentrations measured by a Particle Measuring Systems Forward Scattering  
129 Spectrometer Probe varied between  $100$  and  $200 \text{ cm}^{-3}$ . Ice crystal number concentrations  
130 measured by Stratton Park Engineering Company 2D-S and Particle Measuring Systems 2D-  
131 P optical array probes for sizes larger than  $100 \mu\text{m}$  together averaged  $0.4 \text{ L}^{-1}$ . IN  
132 concentrations measured with the Texas A&M Continuous Flow Diffusion Chamber varied

133 from  $0.1 \text{ L}^{-1}$  to above  $20 \text{ L}^{-1}$ . Ice crystal habit estimated using the automated habit  
134 classification procedure of Korolev and Sussman (2000) indicated primarily dendritic crystal  
135 habits.

### 136 **3 Model Description**

137 We use the large eddy simulation mode of the Advanced Research WRF model (WRFLES)  
138 Version 3.3.1 (Yamaguchi and Feingold, 2012) with the National Center for Atmospheric  
139 Research Community Atmospheric Model longwave radiation package (Collins et al., 2004),  
140 RRTMG shortwave package (Iacono et al., 2008), the Morrison two-moment microphysical  
141 scheme (Morrison et al., 2009), and a 1.5-order turbulent kinetic energy prediction scheme  
142 (Skamarock et al., 2008). Surface fluxes are calculated uses the modified MM5 similarity  
143 scheme with calculates surface exchange coefficients for heat, moisture, and momentum  
144 following Webb (1970) and uses Monin-Obukhov with Carlson-Boland viscous sub-layer  
145 and standard similarity functions following Paulson (1970) and Dyer and Hicks (1970).

146 All model runs are initialized with winds, temperature, and water vapor from the 17Z 8 April  
147 2008 sounding at Barrow, AK (see Fig.1). Initial surface pressure is 1020 hPa. Divergence is  
148 assumed to be  $2.5 \times 10^{-6} \text{ s}^{-1}$  below the temperature inversion and zero above, giving a linear  
149 increase in large-scale subsidence from zero at the surface to  $2.7 \text{ mm s}^{-1}$  at the base of the  
150 initial inversion ( $z=1.1 \text{ km}$ ). This value for divergence was chosen so that the height of the  
151 temperature inversion at cloud top is steady. The divergence used in this study is smaller than  
152 the divergence used in the WRFLES study of the same case by Solomon et al. (2014) due to

153 the reduced LWPs in this current study and therefore reduced turbulent entrainment that  
154 balances large-scale subsidence in a steady simulation.

155 All simulations are run on a domain of  $3.2 \times 3.2 \times 1.8$  km with a horizontal grid spacing of  
156 50 m and vertical spacing of 10 m. The domain has  $65(x) \times 65(y) \times 180(z)$  gridpoints and is  
157 periodic in both the x- and y-directions. The top of the domain is at 1.8 km, which is 0.7 km  
158 above cloud top in this case. The model time step is 0.75 s. The structure of the cloud layer is  
159 insensitive to changes in resolution and domain size. For example, tests run for Solomon et al.  
160 (2014) demonstrated that increasing the vertical and horizontal resolutions by a factor of two  
161 resulted in an increase in LWP and IWP by 5% and 1%, respectively, while increasing the  
162 domain size by a factor of two in both the x- and y-directions results in an increase in LWP  
163 and IWP of less than 1%.

164 Cloud droplets are activated using resolved and subgrid vertical motion (Morrison and Pinto  
165 2005) and a log-normal aerosol size distribution (assumed to be ammonium bisulfate and  
166 30% insoluble by volume) to derive cloud condensation nuclei spectra following Abdul-  
167 Razzak and Ghan (2000). The aerosol accumulation mode is specified with concentrations of  
168  $165 \text{ cm}^{-3}$ , modal diameter of  $0.2 \mu\text{m}$ , and geometric standard deviation of  $1.4 \mu\text{m}$ , based on in  
169 situ ISDAC measurements. In this formulation, IN and cloud condensation nuclei are treated  
170 as separate species.

171 Temperature and moisture profiles are nudged to the initial profiles in the top 400 m of the  
172 domain with a time scale of 1 hour. The model is initialized with winds, temperature, and  
173 water vapor similar to the Control integration from Solomon et al. (2014). Horizontal winds

174 are nudged to the initial profiles at and above the initial inversion base with a timescale of 2  
175 hours. Initial temperature and subgrid turbulent kinetic energy (TKE) are perturbed below the  
176 top of the mixed layer with pseudo-random fluctuations with amplitudes of +/- 0.1 K and 0.1  
177  $\text{m}^2 \text{s}^{-2}$ , respectively. The liquid layer is allowed to form in the absence of ice during the first  
178 hour of the integration to prevent potential glaciation during spinup.

179 The cloud-driven mixed layer is defined as the region where the liquid-ice water static energy  
180 is approximately constant with height. We define the boundaries of the mixed-layer top and  
181 base to occur where the slopes of liquid-ice static energy exceed  $7 \times 10^{-3} \text{ K m}^{-1}$  and  $1 \times 10^{-3} \text{ K}$   
182  $\text{m}^{-1}$ , respectively. Cloud top and base are defined as the heights where cloud water mixing  
183 ratio,  $q_c$ , is equal to  $1 \times 10^{-4} \text{ g kg}^{-1}$ .

184 Nested Weather Research and Forecasting (WRF) model simulations of this case performed  
185 with an inner grid at LES resolution (Solomon et al. 2011) demonstrate that moisture is  
186 provided to the cloud system by a total water inversion at cloud top and that the mixed layer  
187 does not extend to the surface, i.e., the mixed layer is largely decoupled from surface sources  
188 of moisture. In addition, the nested simulations indicate that cloud liquid water,  $q_c$ , is  
189 maintained within the temperature inversion by downgradient turbulent fluxes of  $q_v$  from  
190 above and direct condensation driven by radiative cooling. These processes cause at least  
191 20% of  $q_c$  to extend into the temperature inversion.

192 WRFLES has been modified to include a prognostic equation for IN number concentration  
193 ( $N_{IN}$ ),

$$\frac{\partial N_{IN}}{\partial t} + ADV + DIFF = \frac{\delta N_{IN}}{\delta t} \Big|_{activation} + \frac{\delta N_{IN}}{\delta t} \Big|_{sublimation} \quad (1)$$

194 where ADV represents advection and DIFF represents turbulent diffusion. Activation is also  
 195 referred to as nucleation of ice and sublimation is also referred to as recycling of IN.

196 Here we adopt an empirical approach by initializing  $N_{IN}$  with an observationally based  
 197 relationship expressing the number of available IN as a function of temperature in regions of  
 198 water-saturation (DeMott et al., 2010),

$$N_{IN} = F * 0.117 \exp(-0.125 * (T - 273.2)) \quad (2)$$

199 where F is an empirically derived scale factor and T is temperature in Kelvin. Sixteen  
 200 prognostic equations are integrated for  $N_{IN}$  in equally spaced temperature intervals with  
 201 nucleation thresholds between -20.2°C and -15.5°C (see Fig. 2). Therefore, additional IN  
 202 become available for activation as the cloud layer cools. Initial  $N_{IN}$  concentrations are a  
 203 function of the nucleation threshold temperatures and are independent of the in-situ  
 204 temperature. The in-situ temperature in regions of water saturation determines how many IN  
 205 are activated. To take deviations from the empirical derivation into account, IN are activated  
 206 with 50% efficiency (by multiplying the activation tendency in equation (1) by 0.5), however  
 207 results are insensitive to this parameter (not shown). Due to the pristine dendritic nature of  
 208 the observed crystals, ice shattering and aggregation are neglected in the simulations and  
 209 sublimation returns one  $N_{IN}$  per crystal.

210  $N_{IN}$  (in units of  $L^{-1}$ ) integrated over the domain in each temperature bin  $k$  at time  $t$  is equal to

$$\bar{N}_{IN}(k, t) = \iiint N_{IN}(x, y, z, k, t) dx dy dz. \quad (3)$$

211 Upon sublimation, the modification of activation thresholds that can occur for previously  
 212 nucleated IN, i.e. preactivation (Roberts and Hallett, 1967), is not considered and  $N_{IN}$  are  
 213 returned to each bin  $k$  with weighting

$$W_k = [\bar{N}_{IN}(k, 0) - \bar{N}_{IN}(k, t)] / \bar{N}_{IN}(k, 0) \quad (4)$$

214 where  $W_k$  is normalized such that  $\sum W_k = 1$ . The  $W_k$  are recalculated each time step. In this  
 215 way, IN are recycled preferentially to each of the 16 temperature bins from which they  
 216 originated (Feingold et al., 1996).

217 The factor  $F$  in Eq. (2) is set to 4 for all simulations yielding an initial  $N_{IN}$  summed over all  
 218 bins at every gridpoint equal to  $5.8 \text{ L}^{-1}$ , compared to  $10 \text{ L}^{-1}$  used in LES studies of the same  
 219 case presented in Avramov et al. (2011). In a discrete bin formulation this results in  $3.26 \text{ L}^{-1}$   
 220 in the warmest bin and  $0.23 \text{ L}^{-1}$  additional IN that are available for nucleation in the coldest  
 221 bin. Given the initial temperatures in the cloud layer, all IN from the first bin in the cloud  
 222 layer nucleate. This causes an initial spike in cloud ice number concentration, which also  
 223 causes a large precipitation flux out of the mixed layer. It takes approximately 6 hours for the  
 224 cloud layer to reach a quasi-equilibrium with steady cloud ice production. Supplementary  
 225 integrations were done to test for robustness of the results presented in Section 4 by varying  
 226 initial IN concentrations, i.e., the factor  $F$ , (shown in Fig. 3) and by varying snow density and  
 227 fall speeds (shown in Fig. 4). Fig. 3 shows that the simulation maintains ice production when  
 228 the initial  $N_{IN}$  is increased or decreased by  $\sim 3 \text{ L}^{-1}$  relative to Control. Fig. 4 shows that the

229 simulations maintain quasi-steady ice and liquid water paths after an initial spinup but the  
230 amount of ice produced is sensitive to the snow fall speed.

231 Crystal size distributions for averaged values of ice water mixing ratio and number  
232 concentration from the Control integration are shown in Fig. 5. These crystal size  
233 distributions are consistent with the Avramov et al. (2011) simulations of this case where  
234 crystal habits are assumed to be high-density pristine dendrites. The distribution shown in Fig.  
235 5 underestimates the number of large (greater than 5mm) crystals as estimated by the 2D-S  
236 and 2D-P probes (see Avramov et al. (2011) for a detailed discussion of the measurements).

237 The Control integration is run with shortwave radiation turned off in order to compare with  
238 previous LES studies of this case (Avramov et al. 2011; Solomon et al. 2014). The results of  
239 Control are compared to two additional simulations; one with IN recycling turned off  
240 (hereafter “NoRecycle”) and one with recycling and shortwave radiation both turned on  
241 (hereafter “SW”). SW is used to investigate how the diurnal cycle impacts IN recycling and  
242 ice formation. All runs use the same setup except SW has subsidence reduced by 30% to  
243 keep the mixed-layer top from lowering appreciably because of smaller LWPs. This allows  
244 for direct comparisons of mixed layer structure and fluxes at the mixed layer boundaries. The  
245 NoRecycle run is started from the Control run at hour 6 to prevent the two simulations from  
246 diverging due to spinup. The first six hours of integration are not used in the analysis to allow  
247 for the spinup of cloud ice. Hours 6-40 are used for analysis of the Control and NoRecycle  
248 simulations and hours 16-76 are used for analysis of the SW simulation to allow for multiple  
249 diurnal cycles.

## 250 **4 Model Results**

#### 251 *4.1 Control Integration*

252 In the quasi-steady Control integration, the mixed-layer depth is approximately 850 m and  
253 comprises a 375 m deep mixed-phase cloud layer (henceforth “the cloud layer”), extending  
254 above the mixed-layer top by 25 m, and a 500 m subcloud layer below (Fig. 6). IN are  
255 produced by sublimation of ice crystals below the cloud layer, advected to the cloud layer by  
256 turbulence, and activated as ice crystals (Fig. 6). Ice that forms in the cloud layer is  
257 transported vertically by turbulence, precipitates to cloud base and below, and sublimates  
258 below the cloud layer. At the mixed-layer base, an increase in  $N_{ICE}$  due to precipitation  
259 approximately balances a decrease in  $N_{ICE}$  due to sublimation. These processes constitute a  
260 feedback through which ice production and IN recycling are closely related. This feedback  
261 between ice production and IN in the mixed layer is linked to dynamic-thermodynamic  
262 tendencies, which sustain a subsaturated subcloud layer because the decrease in relative  
263 humidity due to an upward turbulent vapor flux exceeds the increase due to sublimation.

264 The time evolution of horizontally-averaged IN advection plus subsidence (Fig. 7a) shows  
265 that the majority of IN activate at cloud base, which is a bit warmer than cloud top but is  
266 sufficiently cold to activate many of the IN. However, IN from bins with colder threshold  
267 temperatures are advected higher into the cloud where they activate at their threshold  
268 temperature. A secondary maximum is seen at cloud top where the coldest temperatures are  
269 found. Also, it is seen that IN are advected into the cloud layer at cloud top for the first 15-18  
270 hours, but this source of IN decreases as IN in the upper entrainment zone are depleted. The  
271 turbulent mixing of snow and ice in the mixed-phase cloud layer is clearly seen in Fig. 7b,  
272 where ice plus snow number concentrations are well-mixed in the cloud layer. Given the

273 efficient mixing by the turbulent eddies, it is not possible to identify whether ice has  
274 nucleated at cloud base or cloud top from the ice number concentrations alone. Fig. 7 also  
275 shows the time-height cross sections of horizontally-averaged water vapor mixing ratio and  
276 relative humidity with respect to ice. These figures show that the continuous drying and  
277 cooling of the mixed layer results in continuous sublimation in the subcloud layer.

278 LWP and IWP remain steady until hour 16 of the simulation, and decrease slowly thereafter  
279 (solid lines in Fig. 8a). LWP and IWP magnitudes are within the observational estimates for  
280 this case. In addition, the cloud system is sustained over a multi-day period similar to  
281 measurements taken during ISDAC. Continuous cloud-top cooling causes the minimum  
282 horizontally-averaged temperature (near cloud top) to decrease from  $-17.5^{\circ}\text{C}$  to  $-20^{\circ}\text{C}$  from  
283 hour 10 to hour 40 (Fig. 8b).

284 Over the 40-hour integration, the cloud layer remains decoupled from the surface (Fig. 8c).  
285 However, this does not prevent the number concentration of ice crystals ( $N_{ICE}$ ) in the cloud  
286 layer from remaining relatively steady, decreasing from vertically integrated values of 372 to  
287  $365 \text{ m L}^{-1}$  (Fig. 8d, or in terms of vertically averaged cloud layer values,  $1.2 \text{ L}^{-1}$  to  $1.1 \text{ L}^{-1}$ ).  
288 By contrast, while  $N_{ICE}$  is maintained in the cloud layer,  $N_{IN}$  in the subcloud layer decreases  
289 significantly from  $2 \text{ L}^{-1}$  to  $0.2 \text{ L}^{-1}$  over the same period. Therefore, even though more  $N_{ICE}$   
290 are lost from the cloud than are activated (Fig. 9a), the relatively constant flux of IN into the  
291 cloud layer (Fig. 9b) allows  $N_{ICE}$  in the cloud to decrease at a slower rate than  $N_{IN}$  in the  
292 subcloud layer. The continuous loss of  $N_{IN}$  in the subcloud layer is due to the IN flux into the  
293 cloud layer exceeding the  $N_{IN}$  gained through sublimation and turbulent advection at mixed-

294 layer base (Fig. 9b). This loss is not mitigated by entrainment at mixed-layer top, which is  
295 found to be negligible (Fig. 9c), consistent with Fridlind et al. (2011).

296 The feedback loops discussed above are illustrated by the conceptual diagram in Fig. 10,  
297 where any change to one link in the cycle leads to an increase or decrease in ice production.  
298 For example, a decrease in the turbulent advection of  $N_{IN}$  into the cloud layer, slows the  
299 activation of IN, reduces the precipitation flux into the subcloud layer, reducing sublimation  
300 and availability of IN below cloud base. Both dynamics and thermodynamics play a role in  
301 the buffering aspect of these feedback loops since, for example, the slowing of IN activation  
302 in the example above would lead to increased cloud liquid production, cloud-top radiative  
303 cooling, and enhanced turbulent mixing, which would lead to increased transport of IN into  
304 the cloud layer and therefore increased activation of IN.

#### 305 ***4.2 Impact of turning off recycling***

306 When IN recycling is turned off, all IN that activate are lost from the system. This results in a  
307 more rapid loss of IN, a decrease in IWP, and a rapid increase in LWP (Fig. 8a,d, dashed  
308 lines), in contrast to the measurements that show a steady liquid layer and consistent ice  
309 production. Increased cloud liquid water when recycling is turned off results in increased  
310 radiative cooling at cloud top, which causes the cloud-driven mixed layer to cool more  
311 rapidly (Fig. 8b). These results demonstrate the importance of IN recycling in regulating  
312 phase partitioning. The rapid increase in LWP increases cloud-generated turbulence via  
313 enhanced radiative cooling and increases the turbulent mixing of IN from the subcloud layer  
314 into the cloud layer, contributing to a more rapid depletion of IN relative to the Control  
315 integration. This process eventually becomes limited due to depletion of IN in the reservoir

316 below (Fig. 9b). Due to the additional activation of IN as the cloud layer cools, ice  
317 production is maintained in the absence of recycling and the activation of IN in the cloud  
318 layer exceeds the upward IN flux at cloud base (Fig. 9a,b). However, the diminishing  $N_{IN}$  in  
319 the subcloud layer limits IN activation and  $N_{ICE}$  rapidly decreases in the cloud layer (Fig. 8d).

### 320 *4.3 Impact of diurnal cycle*

321 A diurnal cycle is added to the Control simulation in order to investigate how the feedback  
322 loops identified in the Control and NoRecycle runs are modified with realistic transient  
323 heating and cooling tendencies due to variations in incoming shortwave radiation. A question  
324 that is addressed in this diurnal simulation is, to what extent is the continuous production of  
325 ice in the Control simulation due to the lack of incoming shortwave radiation, which may  
326 overestimate the cooling tendencies in the cloud layer, resulting in an overestimate of IN  
327 activation? In addition, we investigate whether allowing for a realistic diurnal cycle provides  
328 for additional buffering feedbacks.

329 Adding a diurnal cycle to the Control simulation produces a diurnal peak in downwelling  
330 surface shortwave radiation of  $510 \text{ W m}^{-2}$  and 6 hours of total darkness per day (Fig. 11b).  
331 As shortwave radiation increases, the net radiative cooling near cloud top diminishes, which  
332 decreases cloud-generated turbulence, decreasing LWP and cloud-layer thickness. In addition,  
333 it is seen that the peak daily LWP coincides with zero shortwave radiation when in-cloud  
334 turbulence and cloud thickness are largest (Fig. 11a). These values are on the low end but  
335 within the measurements for this ISDAC case.

336 Fig. 11a,b shows that LWP and IWP variability is predominantly driven by the diurnal cycle.  
337 However, IWP variability is seen to lag LWP by 3-4 hours because as shortwave radiation  
338 decreases the cloud layer cools, which increases activation of IN, increasing  $N_{ICE}$ , allowing  
339 more ice crystals to grow, which increases IWP (Fig. 11a,b). Similar to the Control  
340 simulation subcloud  $N_{IN}$  decreases at a faster rate than cloud layer  $N_{ICE}$ , but allowing for the  
341 warming and cooling tendencies in the diurnal cycle results in cloud layer  $N_{ICE}$  that decreases  
342 40% more slowly than in the Control simulation (Fig. 11c).

343 Precipitation and turbulent mixing of  $N_{ICE}$  (hereafter turbulent mixing is referred to as  
344 " $T_{ICE}$ ") at cloud base are out of phase by 10 hours (Fig. 11d), with turbulence leading  
345 precipitation. When shortwave radiation is weak or absent, the increase in  $N_{ICE}$  eventually  
346 becomes limited by a decreasing turbulent mixing of IN (" $T_{IN}$ ") into the cloud layer from  
347 below, as recycling slows due to a decrease in  $N_{ICE}$  flux from the cloud layer (Fig. 11d,f).  
348 When shortwave radiation is strong, reduction in IWP is limited by weaker precipitation  
349 losses, and attendant weaker sublimation and IN flux into the cloud layer (Fig. 11d,f).  
350 Entrainment of  $N_{IN}$  at the mixed-layer top is insignificant throughout the integration (Fig.  
351 11e).

## 352 **5 Analysis from a mixed-layer perspective**

353 The results discussed in Section 4 can be understood from balances in a well-mixed layer  
354 with sources/sinks at the upper and lower boundaries. Total particle concentration  
355 ( $N_{IN}+N_{ICE}$ ) is only changed by fluxes at the mixed-layer boundaries when recycling is  
356 allowed. These fluxes are entrainment of  $N_{IN}$  at mixed-layer top and turbulent mixing of both

357  $N_{ICE}$  and  $N_{IN}$  ( $T_{ICE}$  and  $T_{IN}$ ) and precipitation of  $N_{ICE}$  ( $P$ ) at mixed-layer base. Since there  
 358 are no sources and sinks of  $N_{IN}+N_{ICE}$  within the mixed layer, the horizontally-averaged  
 359  $N_{IN}+N_{ICE}$  flux ( $f(z)$ ) must vary linearly from mixed-layer base to mixed-layer top (Lilly,  
 360 1968; Bretherton and Wyant, 1997). If it is assumed that  $f$  at the mixed-layer base is  
 361 downward (assumed negative in this formulation) and  $f$  at the mixed-layer top is negligible  
 362 (robust assumptions for a scenario where ice is precipitating from the mixed layer and  
 363 entrainment is weak), then

$$f(z) = R * \frac{H - z}{H - B}, \quad B \leq z \leq H \quad (5)$$

364 where  $H$  is the mixed-layer height,  $B$  is the mixed-layer base and  $R$  is the total  $N_{IN}+N_{ICE}$  flux  
 365 at the mixed-layer base,

$$R = f|_{\text{Mixed-Layer Base}} = [P + T_{ICE} + T_{IN}]_{\text{Mixed-Layer Base}}, \quad (6)$$

366 and

$$[T_{ICE} + T_{IN}]_{\text{Cloud Base}} \approx [f - P]_{\text{Cloud Base}}. \quad (7)$$

367 Since  $f < 0$ , the turbulent flux of  $N_{IN}$  into the cloud layer plus the turbulent flux of  $N_{ICE}$  into  
 368 the subcloud layer is always less than precipitation of  $N_{ICE}$  at cloud base. In addition, in a  
 369 slowly evolving state where  $T_{IN}|_{\text{Mixed-Layer Base}} > 0$ , total IN flux due to sublimation in the  
 370 mixed layer,  $S$ , can be written as

$$S \approx [P + T_{ICE}]_{\text{Mixed-Layer Base}} - [P + T_{ICE}]_{\text{Cloud Base}} \quad (8a)$$

$$371 \quad \approx [f - T_{IN}]_{\text{Mixed-Layer Base}} - [f - T_{IN}]_{\text{Cloud Base}} \quad (8b)$$

372 and since  $f|_{\text{Mixed-Layer Base}}$  is downward and  $f|_{\text{Mixed-Layer Top}}$  is negligible (eq. 5),

$$S < T_{IN}|_{\text{Cloud Base}} - T_{IN}|_{\text{Mixed-Layer Base}} \quad (8c)$$

$$< T_{IN}|_{\text{Cloud Base}}. \quad (8d)$$

373 Thus in a well-mixed layer with an upward  $T_{IN}|_{\text{Mixed-Layer Base}}$ , sublimation is always less than  
 374 the flux of  $N_{IN}$  into the cloud layer.

375 Based on results from Control, precipitation of  $N_{ICE}$  at cloud base is sufficient to balance the  
 376 upward turbulent flux of  $N_{IN}$  (i.e.,  $|T_{IN}| \gg |T_{ICE}|$  at cloud base). Therefore, in a well-mixed  
 377 layer with precipitation of  $N_{ICE}$  at the mixed-layer base that is larger in magnitude than an  
 378 upward turbulent  $N_{IN}$  flux at the mixed-layer base, and assuming negligible entrainment at  
 379 the mixed-layer top

$$|P|_{\text{Cloud Base}} > T_{IN}|_{\text{Cloud Base}} > S. \quad (9)$$

380 However, if all  $N_{ICE}$  sublimate in the mixed layer and the upward turbulent flux of  $N_{IN}$   
 381 dominates at the mixed-layer base then  $f > 0$  and

$$T_{IN}|_{\text{Cloud Base}} > |P|_{\text{Cloud Base}} = S, \quad (10)$$

382 the mixed layer gains  $N_{IN}+N_{ICE}$  over time, resulting in a continuously increasing ice  
383 production in the cloud layer. In the presence of shortwave radiation (i.e., in the SW  
384 simulation),  $T_{IN}|_{\text{Cloud Base}}$  is also greater than  $|P|_{\text{Cloud Base}}$  after a period of weakened  
385 turbulence and weaker precipitation at the mixed-layer base, due to increased activation of  
386  $N_{IN}$  due to decreasing shortwave radiation.

387 If IN entrainment at the mixed-layer top is not negligible then  $f(z)$  must be modified to  
388 include fluxes at the mixed-layer top and  $|f|_{\text{Cloud Base}}$  will increase. If  $|f|_{\text{Cloud Base}}$  increases  
389 such that  $f_{\text{Cloud Base}} < P_{\text{Mixed-Layer Base}}$ , then sublimation will exceed  $T_{IN}|_{\text{Cloud Base}}$ .

390 This mixed-layer analysis provides a framework to understand the results presented in  
391 Section 4. Specifically, sublimation being less than the turbulent flux of IN is seen to be a  
392 property of a well-mixed layer where the total flux at mixed-layer base is downward and the  
393 total flux at the mixed-layer top is negligible. In the case where the mixed layer is saturated  
394 with respect to ice, sublimation is equal to zero and the turbulent flux of IN at the mixed-  
395 layer base is less than the turbulent flux of IN at the cloud base, reducing the flux of IN into  
396 the cloud layer. The relationships outlined in this section are appropriate for any AMPS with  
397 weak entrainment at cloud top, weak large-scale advective fluxes, and net downward fluxes  
398 at the mixed-layer base.

## 399 **6 Analysis of Buffered Feedbacks in SW**

400 Phase diagrams highlight the processes involved in ice production when a diurnal cycle is  
401 allowed (following the arrows from green to blue to black to red in Fig. 12a,b). When  
402 incoming shortwave radiation is a maximum, recycling (sublimation) is seen to be at a

403 minimum. This is counterintuitive since subcloud relative humidity is low at this time, which  
404 would be expected to produce increased sublimation. However, due to weak turbulent mixing  
405 between the cloud and subcloud layers the net  $N_{ICE}$  flux into the subcloud layer is weak,  
406 resulting in weak sublimation and recycling. This situation is reversed as shortwave radiation  
407 decreases, since increased cloud-top cooling increases cloud-driven turbulent mixing, which  
408 allows recycling to increase in the regions of reduced subcloud relative humidity. As is seen  
409 in the conceptual diagram (Fig. 10), this then leads to an increased  $N_{ICE}$  flux into the  
410 subcloud layer (green arrows, Fig. 12). However,  $N_{ICE}$  in the cloud layer doesn't begin to  
411 increase until activation in the cloud layer exceeds the flux of  $N_{ICE}$  into the subcloud layer  
412 (green arrows). This cycle is further amplified as shortwave radiation decreases, namely,  
413 decreased shortwave radiation increases cloud-driven turbulence, increasing the flux of IN  
414 into the cloud layer, increasing the activation of IN, which increases  $N_{ICE}$  in the cloud layer  
415 and the  $N_{ICE}$  flux from the cloud layer into the subcloud layer (blue arrows).

416 When incoming shortwave radiation is a minimum, more  $N_{IN}$  are activated because the cloud  
417 layer cools. However, again we see that  $N_{ICE}$  tendencies due to thermodynamics are buffered  
418 by the slowing of turbulence-driven feedbacks due to a thickening of the cloud layer. Thus, a  
419 net increase in  $N_{ICE}$  in the cloud layer, commensurate with an increased IWP and  
420 precipitation (black arrows), is buffered by a decrease in the downward turbulent mixing of  
421  $N_{ICE}$ , which reduces recycling, slowing the feedback loop (see Fig. 10). During the morning  
422 hours, as the cloud layer warms and thins and ice activation becomes less efficient,  
423 turbulence continues to decline, slowing the recycling feedback process to the point where  
424 limited IN fluxes to the cloud layer inhibit ice production and  $N_{ICE}$  declines (red arrows).

425 **7 Summary**

426 We have demonstrated that sustained recycling of IN through a drying subcloud layer and  
427 additional activation of  $N_{IN}$  due to a cooling cloud layer are sufficient to maintain ice  
428 production, and regulate liquid production over multiple days in a decoupled AMPS.

429 This study provides an idealized framework to understand feedbacks between dynamics and  
430 microphysics that maintain phase-partitioning in AMPS. In addition, we have shown that  
431 modulation of the cooling of the cloud layer and the humidity of the subcloud layer by the  
432 diurnal cycle buffers the mixed-layer system from a loss of particles and promotes the  
433 persistence of a mixed-phase cloud system. The results of this study provide insight into the  
434 mechanisms and feedbacks that may maintain cloud ice in AMPS even when entrainment of  
435 IN at the mixed-layer boundaries is weak. While the balance of these processes changes  
436 depending upon the specific conditions of the cloud layer, for example whether the  
437 cloud layer is coupled to the surface layer, the mechanisms detailed in this paper will  
438 manifest to some degree and therefore the current study provides a framework for  
439 understanding the role of recycling in maintaining phase-partitioning in AMPS.

440 **Author Contributions:**

441 A.S., G.F., and M.D.S. conceived and designed the experiments; A.S. performed the  
442 simulations; A.S., G.F., and M.D.S. analyzed the model results and co-wrote the paper.

443 **Acknowledgements:**

444 The authors acknowledge discussions with Alex Avramov, Chris Cox, Gijs de Boer, Barbara  
445 Ervens, and Ann Fridlind, and Takanobu Yamaguchi for developing the software to run  
446 WRF as a large eddy simulation. This research was supported by the Office of Science  
447 (BER), U.S. Department of Energy (DE-SC0011918) and the National Science Foundation  
448 (ARC-1023366).

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655 **Figure Captions**

656 **Figure 1:** Sounding measured at 17:34 UTC 8 April 2008 at Barrow, Alaska (71.338N,  
657 156.68W). Left) Water vapor mixing ratio ( $q_v$ ), temperature (T), and potential temperature  
658 (Theta), in units of  $\text{g kg}^{-1}$ , degrees Kelvin, and degrees Kelvin respectively. Right) Zonal  
659 wind (U) and meridional wind (V), in units of  $\text{m s}^{-1}$ . Gray shading marks the extent of the  
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670 **Figure 4:** A,B,D) Sensitivity of LWP and IWP to snow density and fall speeds. LWP shown  
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677 **Figure 5:** Simulated ice particle number size distributions using in-cloud mass and number  
678 concentrations. Ice water mixing ratio =  $3e-4$  g/kg, ice number concentration =  $0.4/L$ , snow  
679 water mixing ratio =  $2.4e-2$  g/kg, snow number concentration =  $0.45/L$ .

680 **Figure 6:** (A)  $N_{IN}$  and (B)  $N_{ICE}$  averaged over 0.5 hours at hour 20, in units of  $L^{-1} hr^{-1}$ . Grey  
681 shading indicates the extent of the cloud layer. Green dash lines indicate the top and bottom  
682 of the mixed layer.

683 **Figure 7:** Time-height cross sections of horizontally-averaged (A) IN advection plus  
684 subsidence, in units of  $L^{-1}hour^{-1}$ , (B) ice plus snow number concentration, in units of  $L^{-1}$ , (C)  
685 water vapor mixing ratio, in units of  $g kg^{-1}$ , and (D) relative humidity with respect to ice, in  
686 units of percent, from CNT simulation. Temperature, in units of  $^{\circ}C$ , shown with black  
687 contour lines in (B,C,D).

688 **Figure 8:** Control and NoRecycle time series for hours 6-40 (smoothed with 90 minute  
689 running average). NoRecycle shown with red and black dashed lines. A) LWP (black) and  
690 IWP (red), in units of  $g m^{-2}$ . B) Minimum horizontally-averaged temperature in the column,  
691 in units of  $^{\circ}C$ . C) Mixed-layer depth (blue), top height (red), and base height (black), in units  
692 of km. D)  $N_{ICE}$  integrated over cloud layer (referred to as CL, red) and  $N_{IN}$  integrated over  
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695 6-40 (smoothed with 90 minute running average). NoRecycle shown with red and black  
696 dashed lines. A)  $N_{ICE}$  flux at cloud base due to turbulence+subsidence+precipitation (red),  
697 mixed-layer base due to turbulence+subsidence+precipitation (black), and due to activation  
698 (multiplied by -1, blue), in units of  $m L^{-1} hr^{-1}$ . B)  $N_{IN}$  flux at cloud base due to turbulence

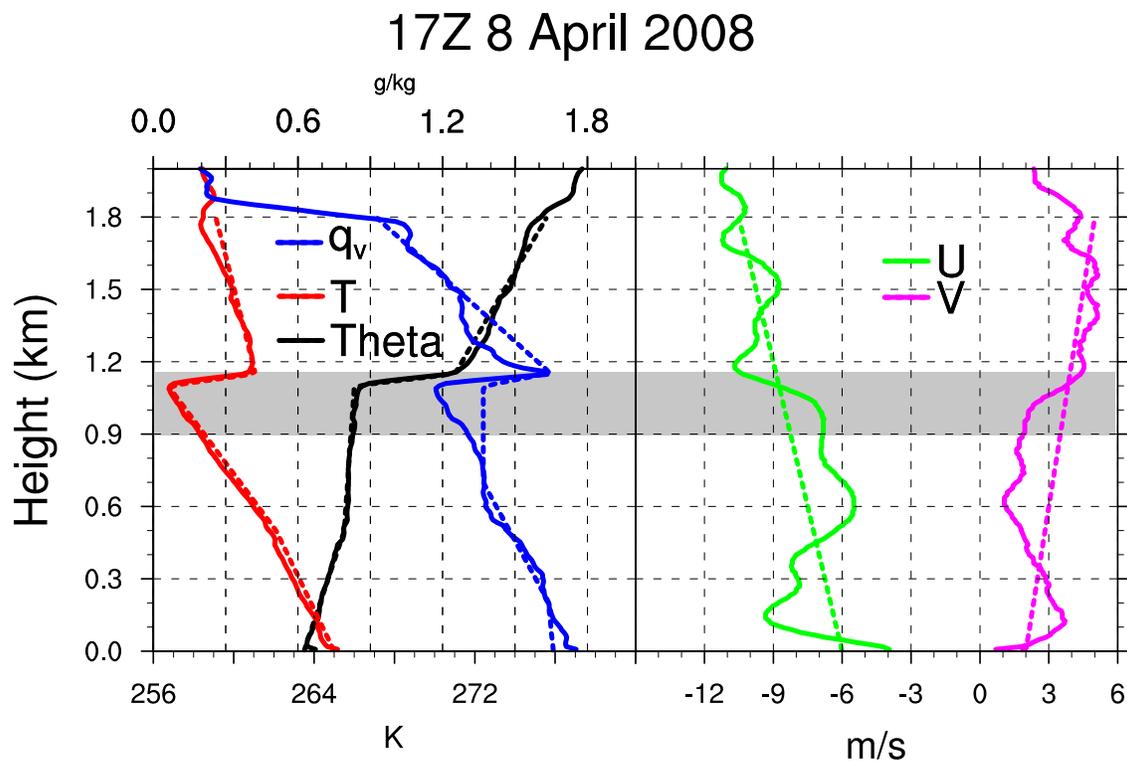
699 (red),  $N_{IN}$  flux due to sublimation (black), and precipitation of  $N_{ICE}$  at cloud base (multiplied  
700 by -1, blue), in units of  $\text{m L}^{-1} \text{hr}^{-1}$ . C)  $N_{IN}$  entrainment at mixed-layer top (red) and base  
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702 **Figure 10:** Schematic of feedback loops that maintain ice production and the phase-  
703 partitioning between cloud liquid and ice in an AMPS. Red colors denote  $N_{IN}$ . Blue colors  
704 denote  $N_{ICE}$ . The size of the arrow indicates the relative magnitude of the flux. Vertical  
705 profiles of  $N_{ICE}$ ,  $N_{IN}$ , relative humidity, and temperature shown with thin blue, red, green, and  
706 yellow lines, respectively.

707 **Figure 11:** A) LWP (black) and IWP (red), in units of  $\text{g m}^{-2}$ . (B) Downward surface  
708 shortwave radiation and turbulent kinetic energy (TKE) at cloud base, in units of  $\text{Wm}^{-2}$  and  
709  $\text{m}^2\text{s}^{-2}$ , respectively. C)  $N_{ICE}$  in cloud layer (referred to as CL, red) and  $N_{IN}$  in subcloud layer  
710 (referred to as SubCL, black), in units of  $\text{m L}^{-1}$ . (D) Total, turbulent, precipitation  $N_{ICE}$  flux at  
711 cloud base (referred to as CL base, red, green, blue, respectively) and total  $N_{ICE}$  flux at  
712 mixed-layer base (referred to as ML base, black), in units of  $\text{m L}^{-1} \text{hr}^{-1}$ , for the SW  
713 integration for hours 16-76. Grey shading indicates hours with zero downwelling surface  
714 shortwave radiation. E)  $N_{IN}$  entrainment at mixed-layer top (red) and base (black), in units of  
715  $\text{m L}^{-1} \text{hr}^{-1}$ . (F)  $N_{IN}$  flux at cloud base due to turbulence (red),  $N_{IN}$  flux due to sublimation  
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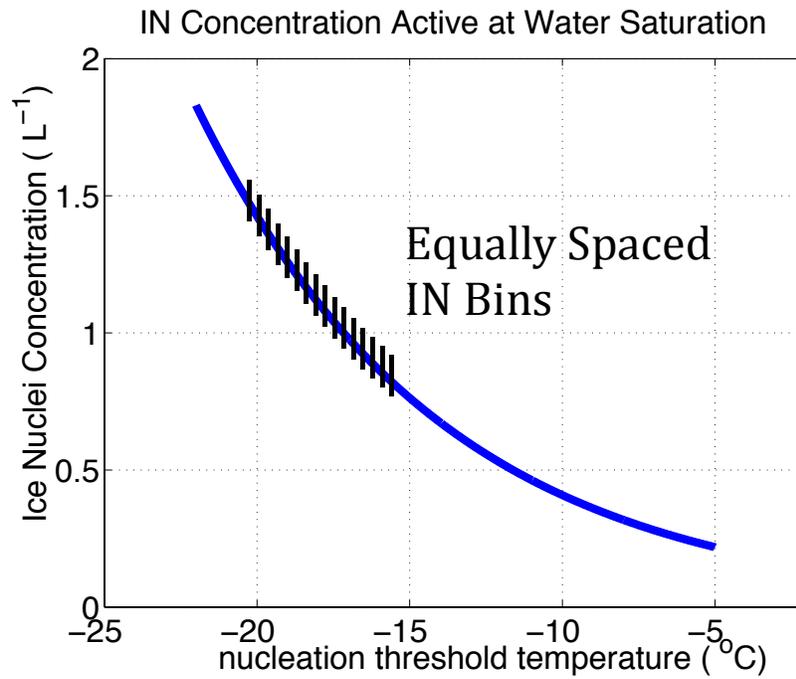
717 **Figure 12:** A) Phase diagram of TKE at cloud base vs.  $N_{ICE}$  in the cloud layer starting at  
718 peak shortwave hour 40, in units of  $\text{m L}^{-1}$  and  $\text{m L}^{-1} \text{hr}^{-1}$ , respectively. Colors show  
719 sublimation in units of  $\text{m L}^{-1} \text{hr}^{-1}$ . H) 24-hour phase diagrams of sublimation vs. minimum  
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722 47-50, 50-56, and 57-62 indicated with green, blue, black, red arrows, respectively.  
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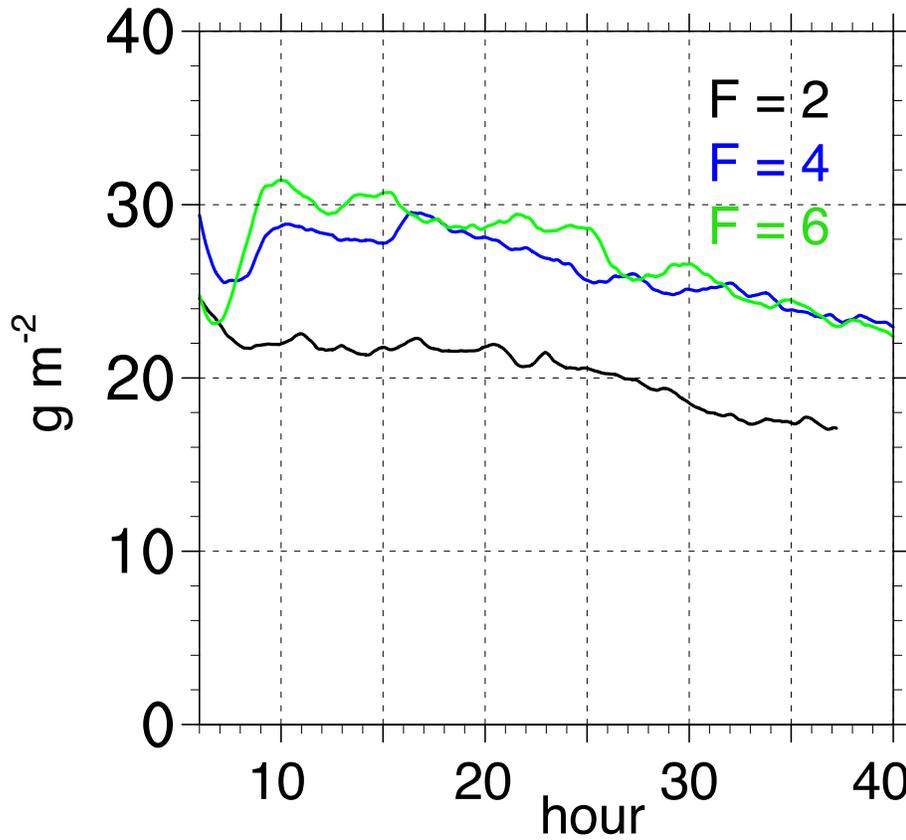
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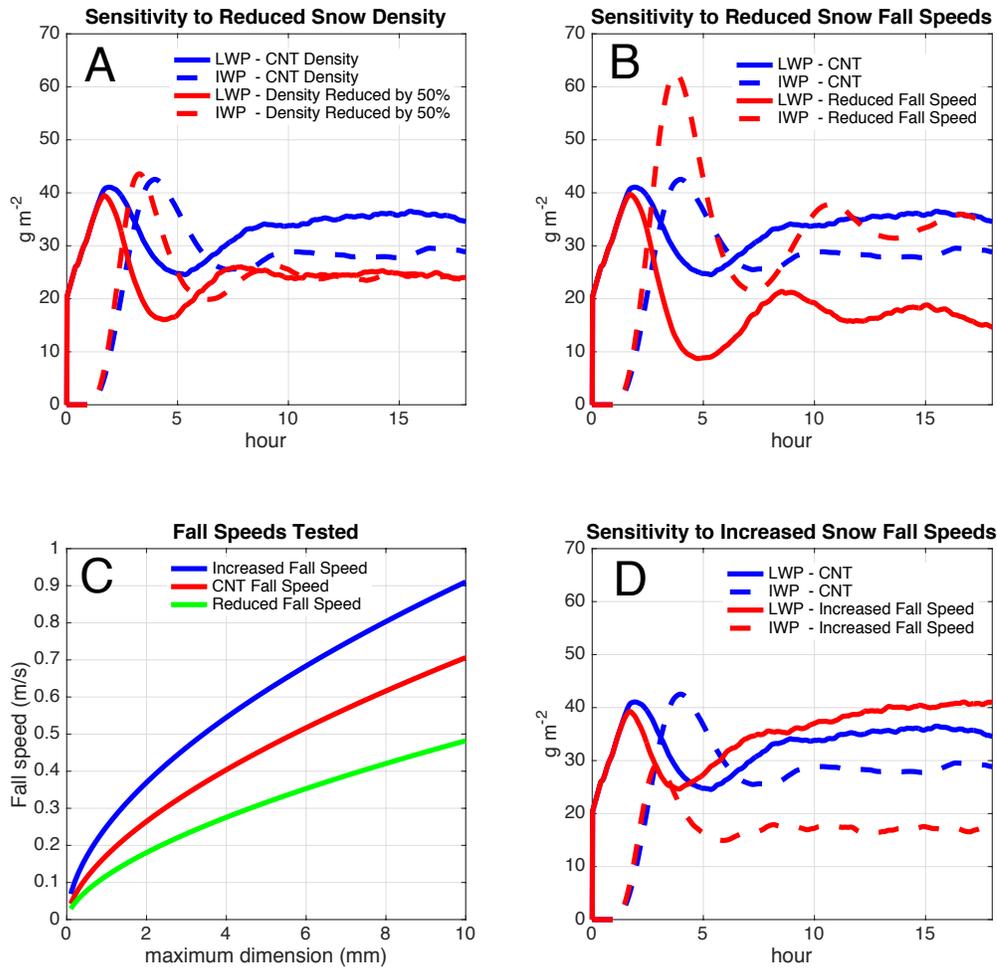
# Ice Water Paths



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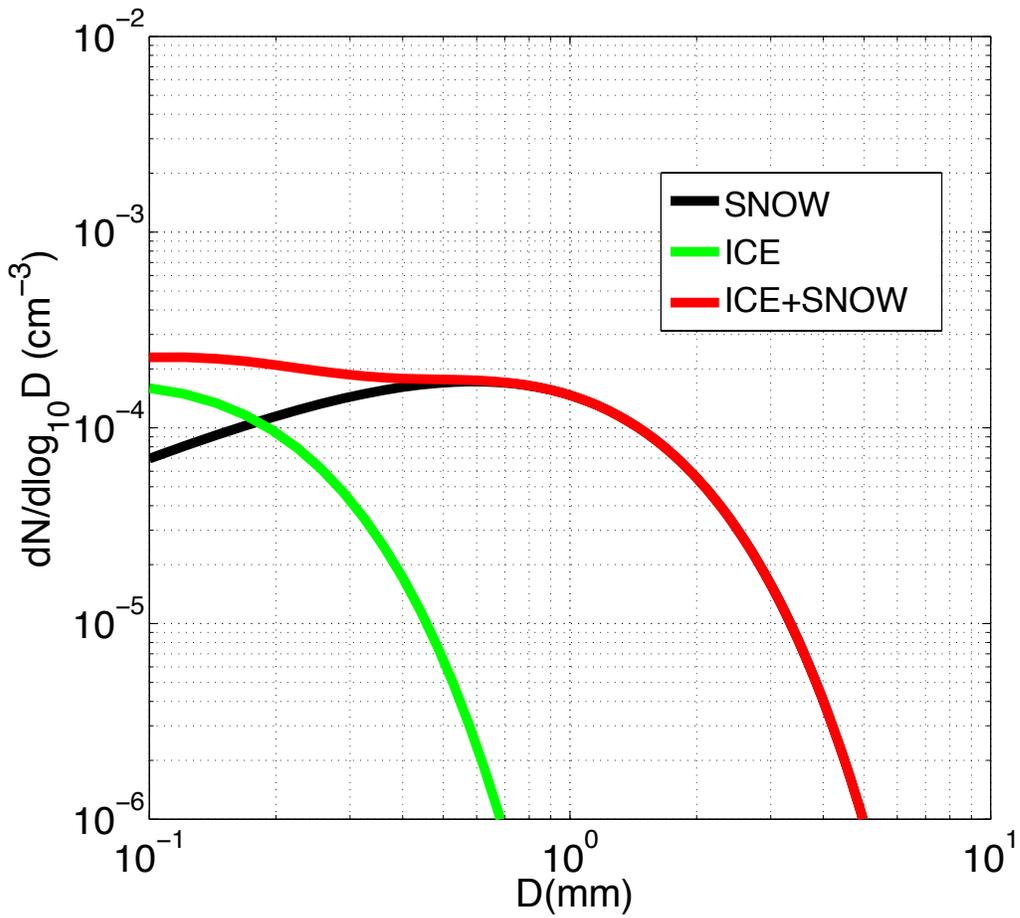
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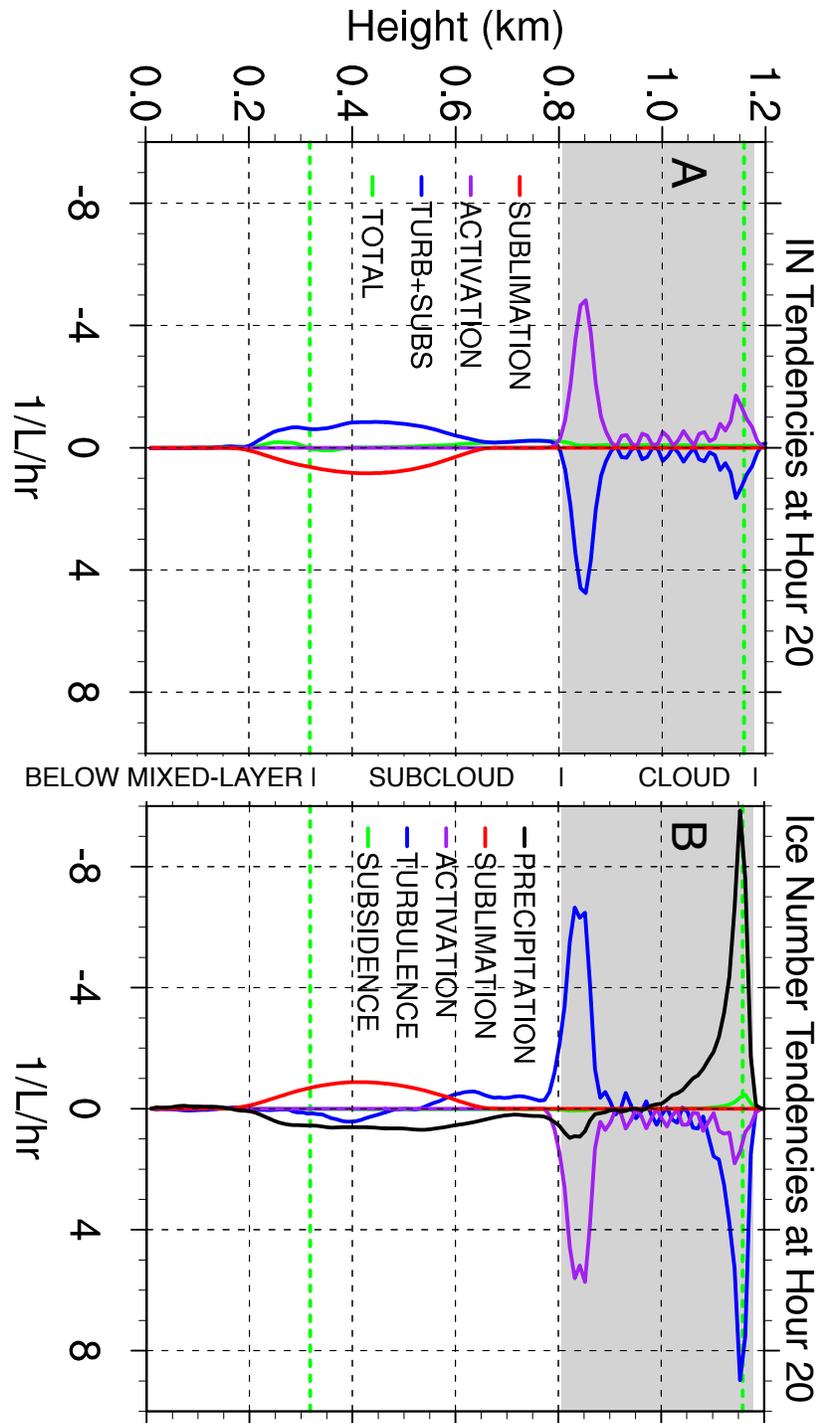
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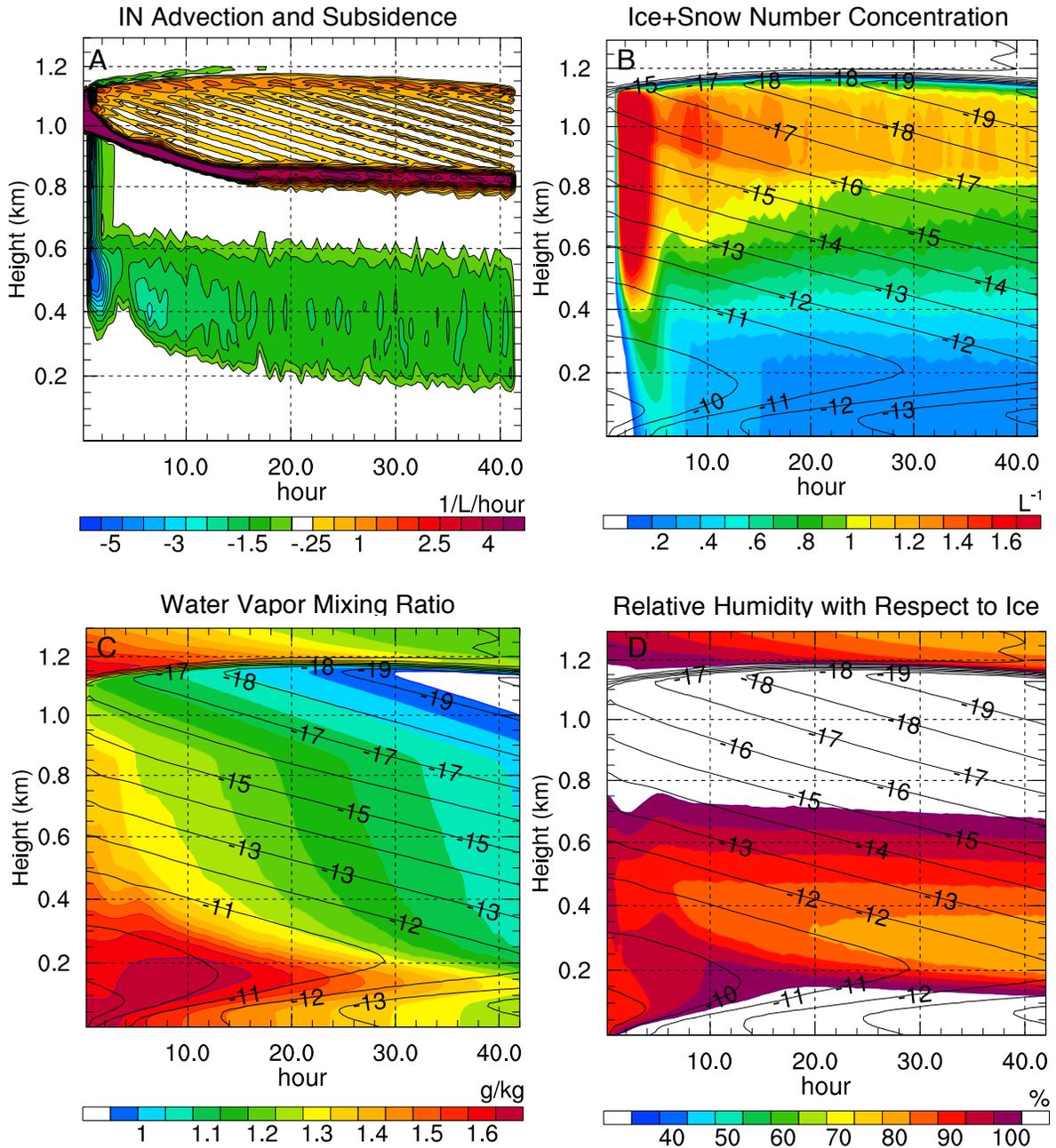
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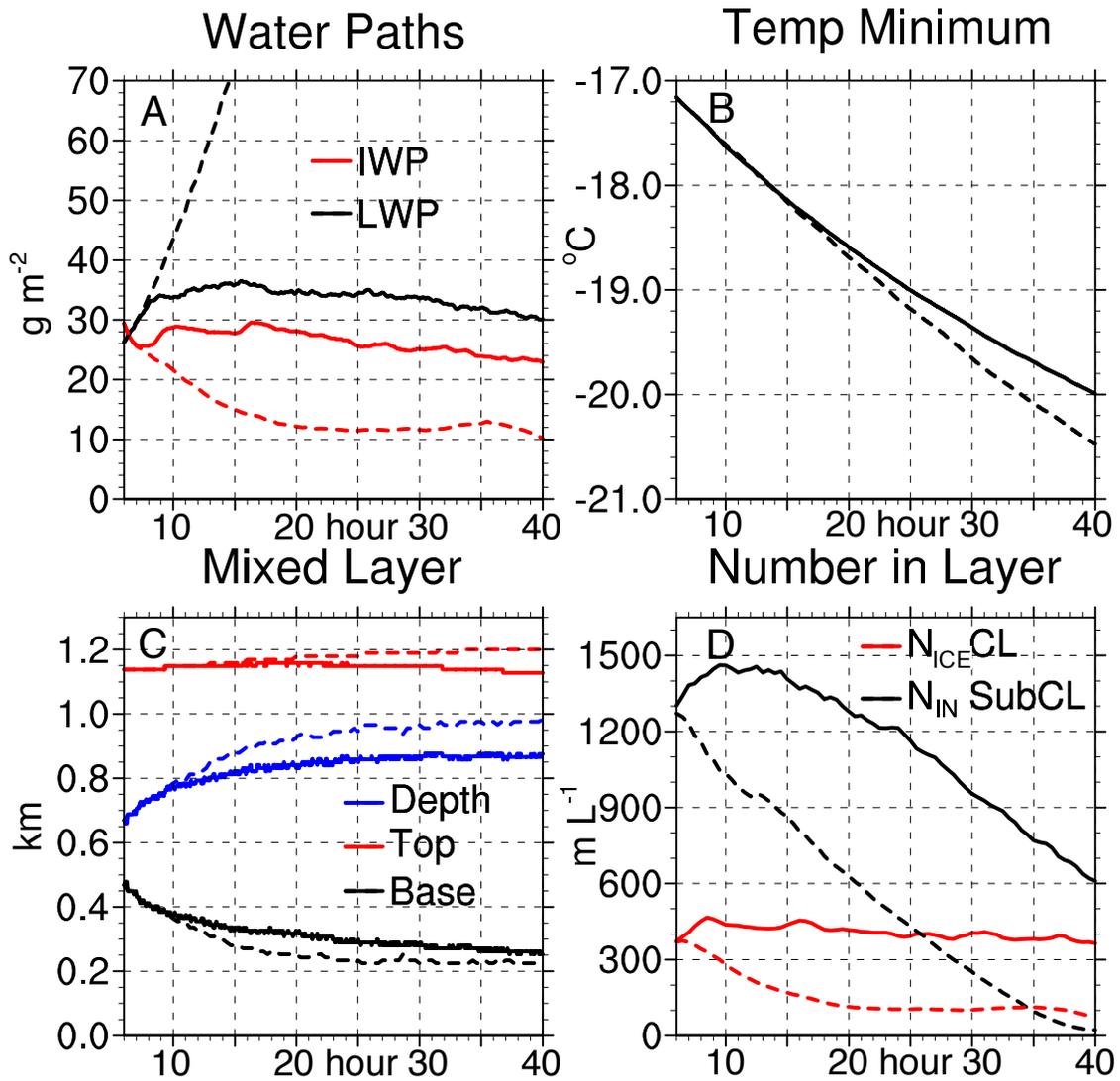
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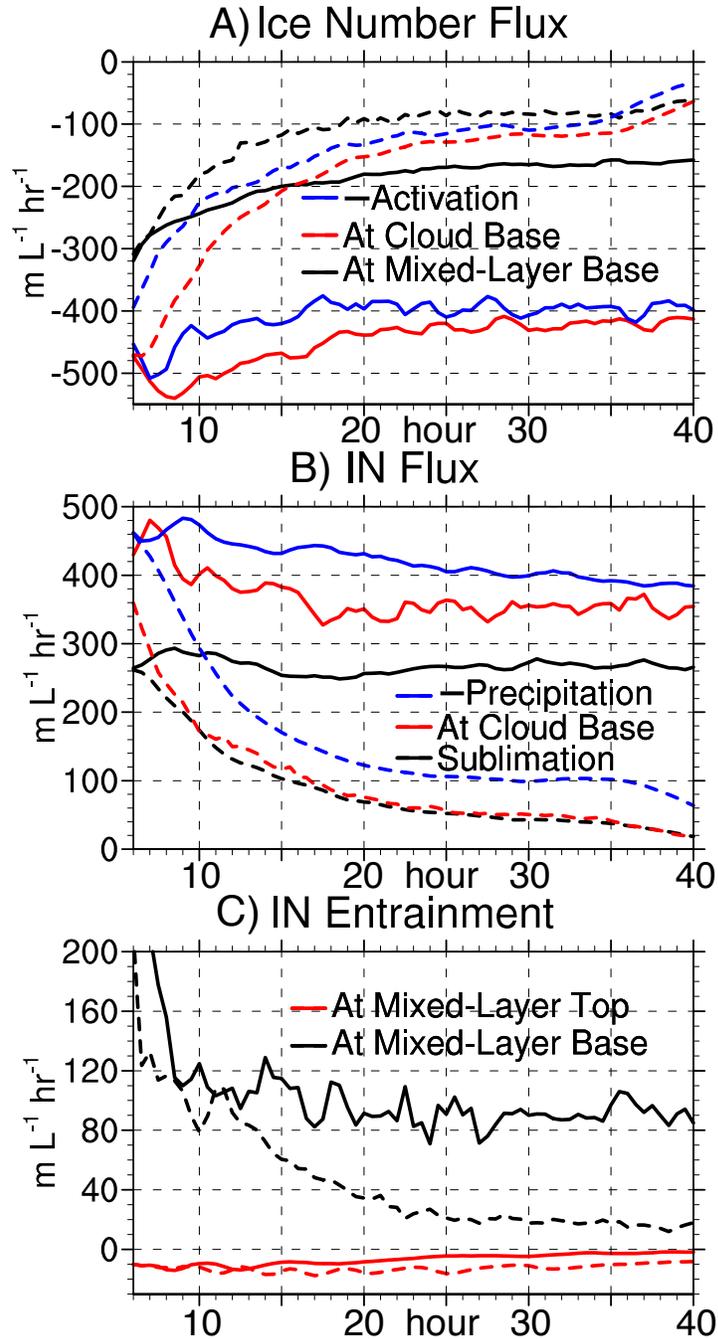
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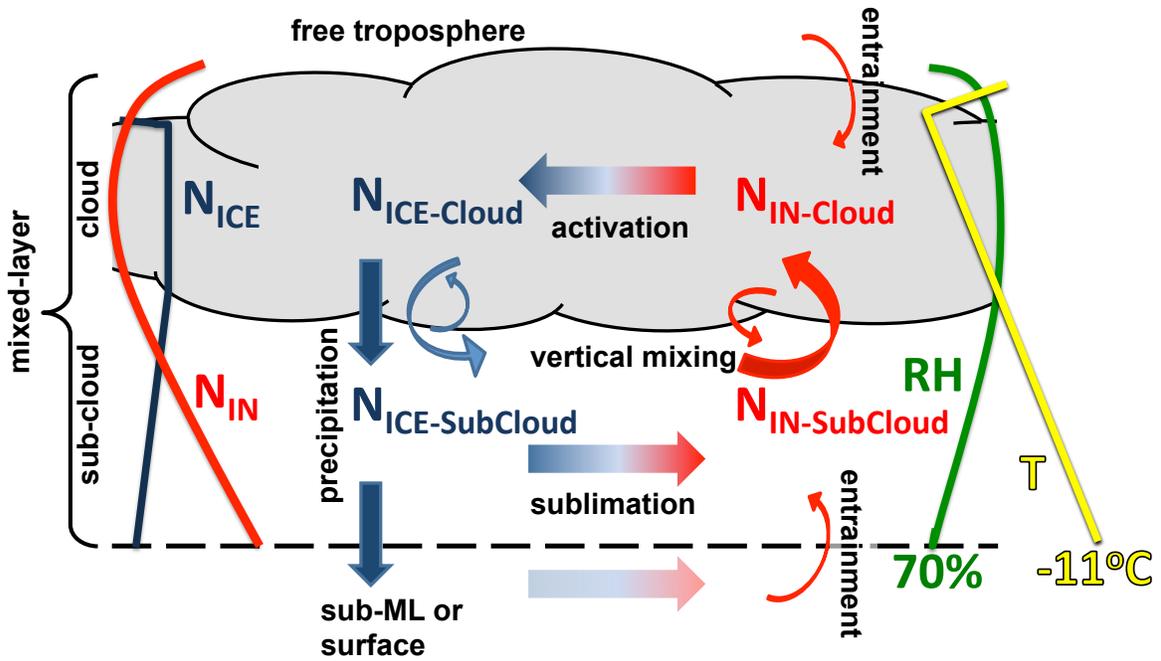
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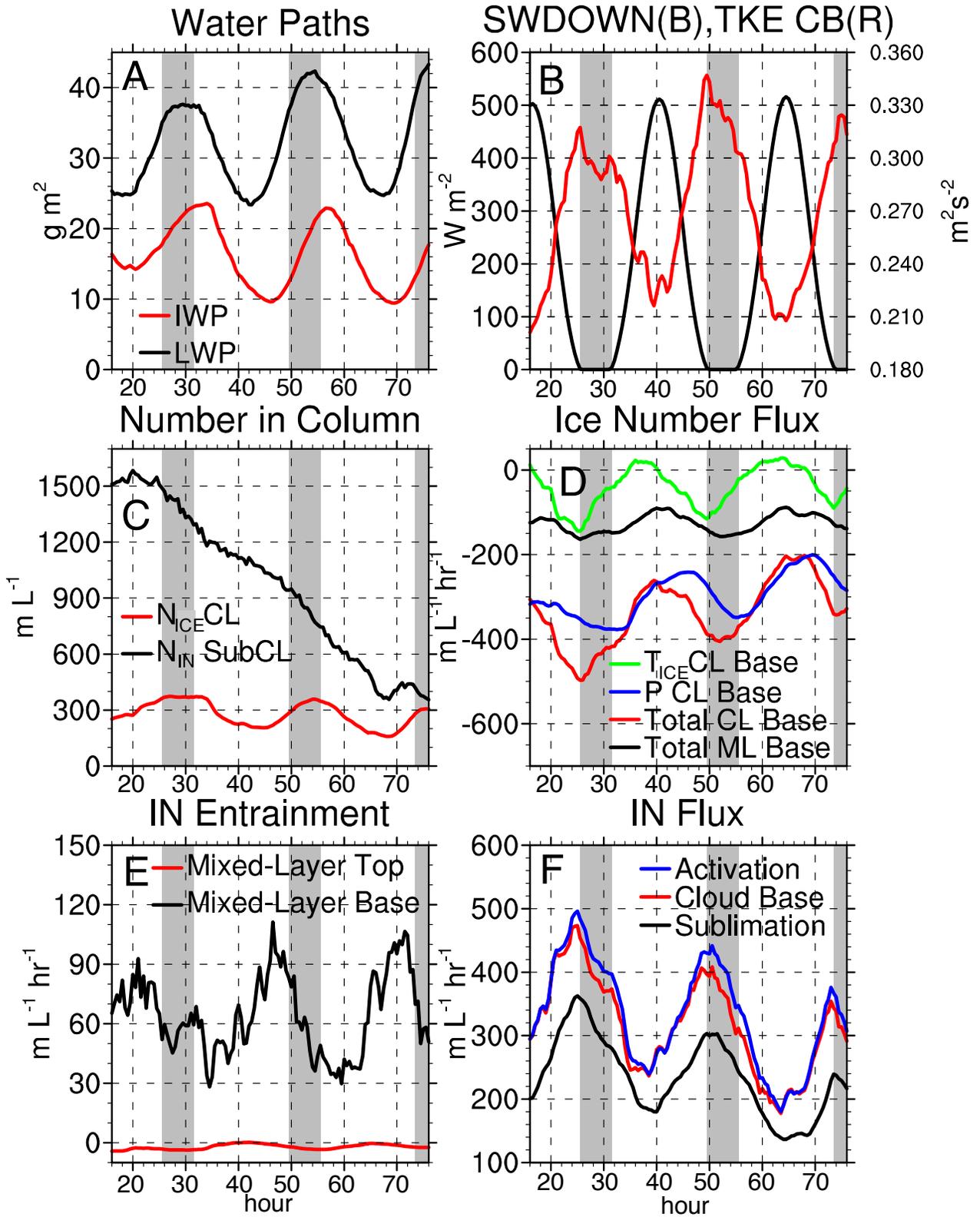
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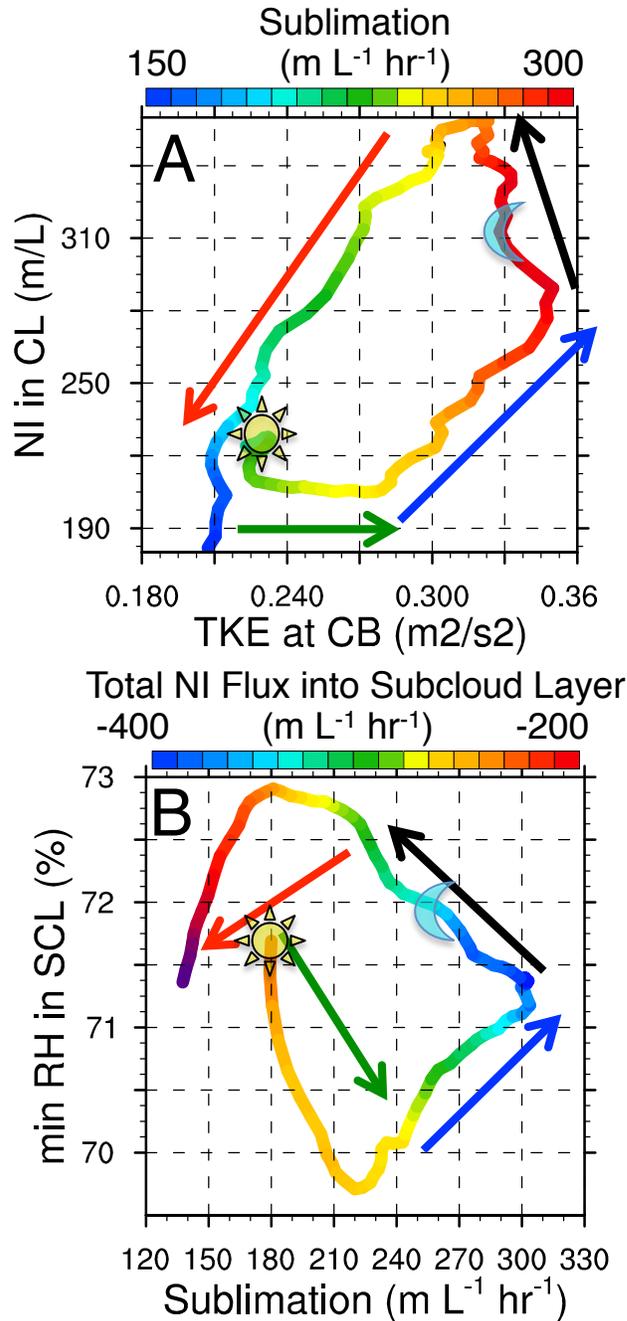
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789

790 **Figure 11:** SW time series (see Figure captions).



791

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