Response to comments on *Simplifying the calculation of light scattering properties for black carbon fractal aggregates*, ACPD **14**, 3537–3562, 2014.

A. J. A. Smith & R. G. Grainger

We are greatful for the submissions from referees and short commenters. All comments have been instructive and we feel have helped improve the structure and content of the paper. Responses will be made to each commenter in turn, starting with the referees. The original comments are provided in *italics* for reference. Modifications to the text have been highlighted.

Response to referee #1

1. One of the simplest and most popular algorithms for light scattering properties of the fractal aggregates is known as the Rayleigh-Debye-Gans (RDG) method, which has simple formulae and is highly efficient for calculations of any circumstance. Thus, before evaluating any parameterization on light scattering properties of the fractal aggregates, its accuracy compared with the direct approximations from the RDG should be checked. If the RDG can give similar accuracy, it becomes really meaningless to carry out any of those parameterizations. I think it is of great interest to add RDG results in the comparison, since RDG is a much more flexible and practical method.

As previously mentioned in Bond and Bergstrom (AST, 2006, §5.2 and references therein), the RDG method can under-predict absorption by 30 %. Using the descriptions from Sorensen (AST, 2001) with a structure factor parameterized as suggested by Lin et al. (Phy. Rev. A, 1990), this indeed seems to be the case. In Fig R1, we show the comparison of these RDG calculations and our parameterisaton to the MSTM calculations for scattering and absorption cross-sections. At longer wavelengths, differences between absorption in RDG and MSTM can be greater than 35 %. As such, we feel that the parameterisation presented in this paper is a useful improvement on RDG calculations. A brief summary of RDG has been added to Section 1.3, *Light scattering methods*, including discussion of the under-prediction of absorption. It reads: "An intermediate step between the rigour of MSTM and the simplicity of assuming spherical aerosols is Rayleigh-Debye-Gans theory (RDG) which assumes that the individual scattering spherules are small enough to be Rayleigh scatterers, and that these scatterers have a negligible multiple scattering interaction with each other. Further details can be found in the review paper by Sorensen (2001). However, as noted by Bond and Bergstrom (2006, §5.2 and references therein),

several studies have shown an underprediction of fractal aggregate absorption by RDG compared to rigourous light scattering calculations, particularly at longer wavelengths."

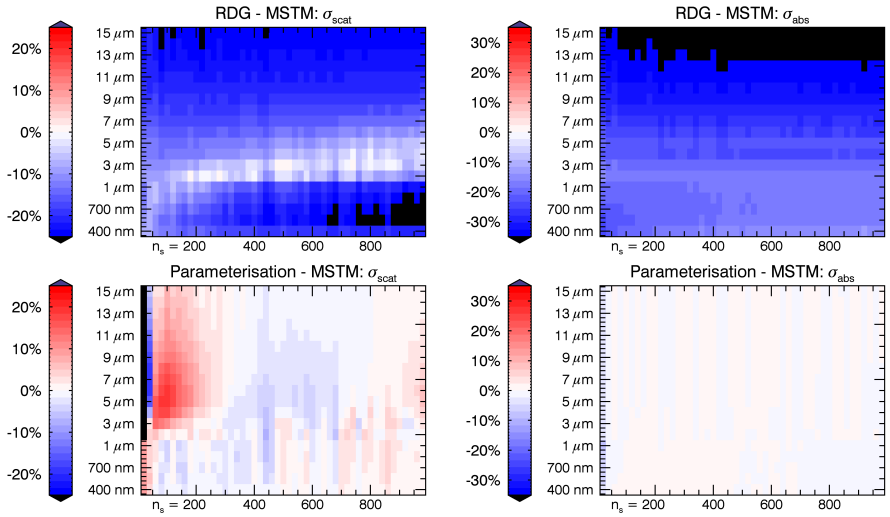

Figure R1: Differences in the scattering and absorption cross-sections of RDG and the parameterisation defined in the paper to MSTM calculations. The top row shows RDG relative differences to MSTM. The bottom row parameterisation differences.

2. Page 3540: The authors discuss the aging of BC as well as its effects. Yin and Liu (JQSRT 2010; 11: 2115-2126) and Liu et al. (AST 2012; 46: 31-43) built a simple model to study the scattering properties of coated aggregates, and can be easily adapted for this study (by also applying the effective medium approximations). From their work, the coating enhances not only the absorption but also the scattering of the aggregates, and their work should be mentioned.

A description of recent investigations of coating of BC has been added to the introduction at the end of section 1.1. This includes the suggested references, as well as discussion of the reduced absorption enhancement seen when aggregates are not fully embedded, as suggested by Referee #2. The additioal sentences read: "Once the BCFAs become hydrophilic, they can take on moisture and collapse into much more tightly packed "globules" (Mikhailov et al., 2006). These have greatly increased scattering and absorption cross-sections and greater forward scattering (Yin and Liu, 2010; Liu et al., 2012). Some recent discussions have focused on apparent discrepancy in absorption enhancement by the coating of BCFAs between measurement and models (Cappa et al., 2013). It has been noted that both the compactness and positioning of the BCFA within a coating medium have significant effects on mass absorbing cross-section (MAC) (Adachi et al., 2010; Scarnato et al., 2013)."

3. The right panel of Fig. 5: The asymmetry parameters for most aggregates shown in the figure are less than 0.4, whereas the color bar chosen can hardly show the details of their values.

Agreed. The colour bar has been adjusted.

4. Page 3544: The authors try to use the scattering properties of spheres to represent those of fractal aggregates, and it should be noticed: even appropriate spheres can be found for the cross sections and asymmetry parameters, the accuracy of such approximations is significantly challenged for the phase function, which was investigated in Li et al. (JQSRT 2010; 111: 2127–2132 that is cited in the manuscript).

Agreed. We had hoped that using a simpler property than the phase function, we might be more easily able to find a match, but this was not the case. A mention of this aspect of Li et al.'s work has been added at the end of section 3.2: "Earlier work by Li et al. (2010) had found that it was not possible to represent the phase function for a reasonable size distribution of BCFAs with a similar distribution of spheres at wavelengths of $\lambda = 0.628$ and $1.1\,\mu$m, so even had a good fit of σ_{ext}, σ_{sca}, and g been found, it is unlikely that the full phase function resulting would have been appropriate."

5. In Fig. 7, the authors show only the performance of the spherical approximation at wavelength of 550 nm, and demonstrate that the errors do not improve with increased wavelength. However, as the wavelength increases, the size parameter of the particle decreases, and the scattering properties should be simple and close to those of Rayleigh scattering. How do the errors distribute at large wavelengths (e.g. 12 μm), and are they still over 15% for most cases or just for few special n_s or D_f? A figure similar to Fig. 7 but for large wavelength will be interesting to discuss if the spherical approximation shows difference performance.

A very good point. At larger wavelengths, the fits are indeed better, but still not acceptable. Taking the case of 12 μm, the principal issue is that in the Rayleigh limit, the phase function is symmetric about scattering angles of $\pi/2$ forward and backwards scattering are equal, but this is not the case for the less compact aggregate particles. As such, one can either fit the extinction and scattering cross-sections but not the asymmetry, or vice-versa. This can be seen in the requested Fig. R2 where errors in scattering and extinction have been reduced to less than 5 % in almost all cases, but with resultant absolute errors in asymmetry of up to 0.2 for less compact BCFAs (with very large relative errors).

Discussion of this, and the figure have been added to the manuscript: "One might expect that at longer wavelengths as the scattering BCFAs approached the Rayleigh limit, the ability to fit spheres would improve. However, the asymmetry parameter at these wavelengths is non-negligible for the less compact and larger BCFAs (unlike Rayleigh scatterers) as can be seen in Figures 6 and 7. This means that it is not possible to find spheres that can match $\ln \sigma_{\text{ext}}$ and $\ln \sigma_{\text{sca}}$, whilst also having a large enough g. As such, a trade off between large errors in either the cross-sections, or asymmetry must be made. The fit with large errors in g is shown in Fig. 9."

6. Table 1 shows that coefficients 1 for SSA and g are both zero at 550 nm, and this indicates that it is not necessary to consider the linear term in Equations 3 and 4 for SSA and g. Is it true for all wavelengths or just for this single case, and this should be clarified in the paper.

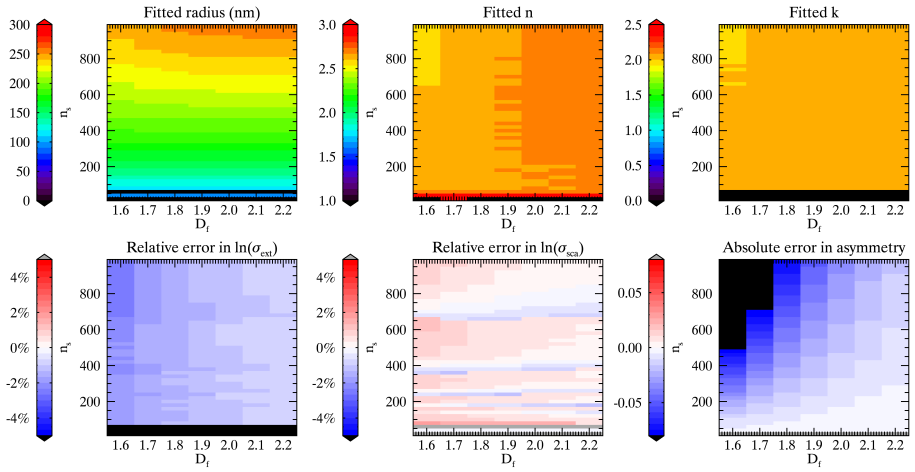

Figure R2: Fitted spheres for BCFA MSTM calculations with a wavelength of $\lambda = 12$ μm. In order to correctly characterise scattering and extinction, asymmetry errors had to be significantly increased. This figure has been added to the manuscript.

This is the case at shorter wavelengths only, as can be seen from inspecting the supplementary material. In general, for both SSA and g, at shorter wavelengths the linear coefficients are small, while at longer wavelengths, the logarithmic coefficents are small. A short discussion of this has been added to the caption for Table 1: "While the values of coefficient 1 (the linear term) in the fits of SSA and g are negligible at 550 nm, they increase at longer wavelengths while the values of coefficient 2 (the logarithmic term) decrease."

7. The bottom panels of Fig. 7 have some curves, which are not explained in the paper, and the numbers listed in Fig. 9 are not well discussed. All those should be detailed in the captions or the manuscript.

The curves in Fig. 7 marked the value (also represented by that data point's colour) at each data point in the image with a line at the extent of the box showing that the value was exactly equal to the maximum of the colour range for the plot. These were accidentally left in from a previous iteration of the plot (to check that the colours were correctly representing the values) and have now been removed. This definitely improves the clarity of the plot. Apologies.

The values in Fig. 9 are areas under the curves, and differences between areas. A description of their meanings has been added to the caption for Fig. 9. It reads: "The MSTM calculations (Data) are blue, the fitted data for the same radii (Fit) are orange, and the missing area covered by the fit, but not the MSTM calculations (Missing) are red. Numbers in these colours give the area under the respective curves. Δ gives the difference in areas between Data and Fit."

8. Page 3548/Conclusions: Although the spheres cannot be used to model the optical properties of fractal aggregates accurately, there are still other approximations that are efficient enough for GCMs (such as RDG mentioned above). Furthermore, considering the uncertainties on the parameters of the fractal ag-

gregates (e.g. k_f, D_f, and size distribution), the errors cased by the RDG or even the spherical approximations may be much smaller. Thus, the parameterization should not be the only way to consider the BC aerosol in GCMs.

Agreed. A comment following this gist has been added to the conclusions: "Other approximations such as RDG can improve greatly the representation of BCFA optical properties but generally do not provide sufficient absorption. With this in mind, a prudent step for GCMs requiring constantly changing distributions of BC aerosol could be to include a parameterisation such as this one which is computationally trivial to implement and is valid within the range of black carbon particles seen in the atmosphere. Uncertainties in the size distribution, shape, and composition of these particles should not be forgotten and will certainly cause differences at least as large as the simplification of optical properties to spheres or RDG."

Response to referee #2

1. There is a general inconsistency of how an aggregate of black carbon spheres is referred in the text (BC, BCFAs or soot).

Agreed. On inspection, all references to soot could be replaced with BC and this has been done.

2. In a subsection of the introduction, section 1.1, the authors present a physical description of aerosol formation and ageing. The authors mention the absorption enhancement due to coating and refer to few papers (Fuller 1999, Jacobson 2001, Bond 2006). Absorption properties of black carbon and appropriate parameterization are a major topic, due to climatological relevance and there could be cited more recent literature, i.e. Liu et al., 2012; Kahnert et al., 2012; Adachi et al., 2010. Also, it has been found both in field campaign and using numerical computations that, when black carbon aggregates are not fully embedded in the transparent coating there is no or little absorption enhancement, please add in the text, as well, Cappa et al, (2012, 2013) and Scarnato et al., (2013), as references.

Based on this and the comments by reviewer #1, the description of aggregate coating has been extended to include these points, at the end of section 1.1. It now reads: "Once the BCFAs become hydrophilic, they can take on moisture and collapse into much more tightly packed "globules" (Mikhailov et al., 2006). These have greatly increased scattering and absorption cross-sections and greater forward scattering (Yin and Liu, 2010; Liu et al., 2012). Some recent discussions have focused on apparent discrepancy in absorption enhancement by the coating of BCFAs between measurement and models (Cappa et al., 2013). It has been noted that both the compactness and positioning of the BCFA within a coating medium have significant effects on mass absorbing cross-section (MAC) (Adachi et al., 2010; Scarnato et al., 2013)."

It would have been interesting a discussion of the authors numerical computations of absorptions properties of BC aggregates, which are not specifically addressed in the paper.

The numerical computations were carried out using MSTM with no bells

or whistles. This basically involved generating input files with the positions of each spherule in a BCFA defined, and passing this to MSTM along with refractive index and wavelength. To clarify this, the following sentence has been added after the first sentence in the methods section: "This required the input of individual spherule positions and radii within an aggregate, wavelength, and the refractive index."

3. I, personally, would find more "clear" having the equations that are currently in sec 3.3 and 3.4, instead presented in the method section, in this way there would be more space for discussion of results.

Initially these equations have been put in the Methods section, but we felt that the narrative of the paper was less clear in this form so changed to the current order. Discussion of results has been extended in response to several referee's comments, e.g. fitting of spheres in IR, additional comparisons with literature, conversion to MAC. These are highlighted elsewhere in this response.

4. In my opinion, generally, the results could be discussed more in the details and compared, where possible, with relevant literature. For example, results in fig, 2 and 3 could be compared with the work of Liu et al., 2008, Kahnert, 2010a,b; Kahnert and Devasthale, 2011; Wu et al., 2012, Scarnato et al, 2013.

Discussion has been increased. In particular, Figs. 2 & 3 and a new figure showing MAC at 550 nm are compared to several of the papers mentioned. e.g. "The mass absorption cross-section (MAC) is another common parameter used to describe black carbon aerosols. Values of MAC at $\lambda = 550\,\mathrm{nm}$ obtained by these calculations are shown in Fig. 4 and are consistent with similar calculations in the literature (Bond and Bergstrom, 2006; Kahnert, 2010a) which found calculated MAC values of around $6\,\mathrm{m^2/g}$. There is a discrepancy between this and measured values of MAC which are around $7.5\,\mathrm{m^2/g}$. Results also agree with the work of Scarnato et al. (2013) who found that 'lacy' aggregates had a higher MAC and lower SSA than more compact aggregates."

Discussion of other aspects of the results have been highlighted elsewhere in this response.

An increase in the font size in the plot would help in reading figures. Figures results are not discussed in detail in the text (for example Fig. 7).

Font sizes for Figures 2, 5, 6, and 7 have been increased. Discussion of the figures in the section "Finding appropriate spheres" has been greatly increased and is twice the length that it was previously. Explicit alterations are mentioned elsewhere in these responses, and we will also provide a copy of the altered manuscript showing all of our changes to the text highlighted.

Introduction section 1.2 page 3541: Line 3: Please, consider to rewrite the sentence Particles are defined by equation with Fractal aggregates can be described in terms of

Since the previous sentence refers to fractal aggregates, we have rewritten the sentence as: "They can be described in terms of the equation:"

Line 7: Please, consider to rewrite the sentence with the following: "The fractal dimension gives a measure of the compactness of the aggregate, a D_f value of 1 describe an open chain structure, while a D_f value of 3 describe a

compact aggregate"

Done. The sentence has been rewritten as: "The fractal dimension gives a measure of the compactness of an aggregate. A D_f value of 1 describes an open chain structure, whilst a D_f value of 3 describes a compact aggregate."

Line 22: instead of "correct" write "considered as reference values ". Remove quotations.

Done.

Method Please, explain the author choice to use different set of refractive indexes for different wavelengths ranges. Chang and Charalapopolous refractive index are provided, as well, in the 400 nm to 1um wavelength region.

While it is true that Chang and Charalapopolous' refractive index data extend down to 400 nm, the review paper by Bond and Bergstrom amalgamated these values along with many others into a best estimate of visible refractive index of BC lying along a "void fraction line" with their "best guess [being that] the high values [...] are the most promising." As such, we selected the B&B highest value of $1.95+0.79i$ and switched from C&C values to B&B values at the wavelength where this value intersected with the B&B value. This was between 1 and 2 μm. We acknowledge that this choice was a little ad hock but preferred it to a sudden discontinuity in RI that would have occurred if we had switched over at a different wavelength closer to the visible.

Results: The scattering cross section increase with increase of fractal dimension has also been found and discussed by Scarnato et al., (2013) and Liu et al. (2008), please add references.

A sentence discussing scattering cross-section in the first paragraph of the results section has been extended to read: "The scattering cross-section is more pronounced at higher D_f as the fractals become more densely packed and so a more coherent scattering entity as also reported by Liu et al. (2008); Scarnato et al. (2013)."

Response to the short comment by J. C. Corbin

1. A single value was used for the spherule radius a (25 nm). For atmospheric BCFAs, the value of a may vary considerably between different combustion sources. The current value of 25 nm would be representative of wood-combustion aerosol (Gwaze et al. 2006; Zelenay et al., 2011). Since diesel soot typically has smaller spherules about 7.520 nm in radius, with more-modern engines having smaller a (Burtscher, 2005) it would be interesting to see results or discussion on the impact of smaller a.

An interesting question. While we weren't able to run additional calculations in time for this response, previous studies by Kahnert (2010, AST) and Liu (2008, JQSRT) have found that in the visible, MAC is not affected by changes in spherule size $15 \leq a \leq 25$ nm while SSA decreases with smaller a. As a decreases, we would expect that the results would tend towards the Rayleigh limit at larger values of n_s and shorter λ, so it seems plausible to suggest that

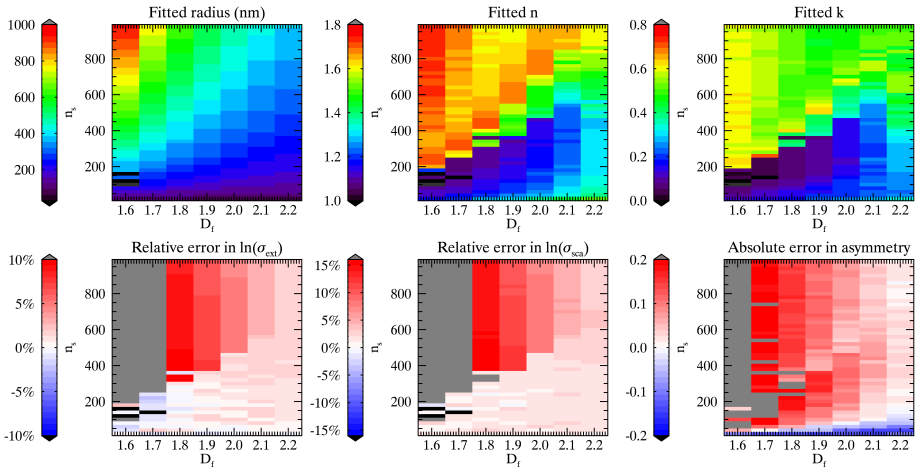

Figure R3: The optimum fitted sphere parameters (r, n, and k) and their resultant errors relative to the reference MSTM calculations in $\ln \sigma_{\text{ext}}$, $\ln \sigma_{\text{sca}}$ and g for BCFAs with $\lambda = 550\,\text{nm}$.

(ignoring changes in refractive index) optical properties will translate, to longer wavelengths and larger numbers of spherules for the same effect.

In the near future, we are intending to run calculations for the smaller values of a valid for diesel burning. For the purposes of this work, an additional comment has been added to the methods section, reading: "The burning of diesel fuels creates BCFAs with smaller spherules. More modern engines working in optimised combustion conditions can have spherules as small as $a = 6.5\,\text{nm}$, whilst emissions from black smoking diesel engines have sizes of $a = 17.5\,\text{nm}$ (Su, 2004). Future work will investigate the light scattering properties of these much smaller particles."

2. What was the motivation for choosing D_f as low as 1.6? Although this low value would reflect a DLCA-formed aggregate (Diffusion-Limited Cluster-Cluster Aggregation) of highly-polydisperse spherules (Eggersdorfer et al., 2012), to our knowledge natural soot aerosols have always been observed to consist of nearmonodisperse spherules so that $D_f = 1.8$ (Sorensen, 2011). This would be significant to Figs. 7 and 8, since the errors there are largest for the lowest D_f. The authors will probably agree that $D_f = 1.8$ is most relevant, as they have already focussed on this case in general.

We agree. It is very unlikely that BCFAs this open are seen often, although some BCFAs have been observed with D_f as low as 1.2 (Heinson, 2010). It was more an attempt to get a feel for how optical properties would change in an arbitrary fractal aggregate as it became more compact. The limits of error plots in Fig. 7 have been adjusted (see Fig. R3) so that the large errors from $D_f < 1.8$ are now beyond the scale of the colour bar. Even still, errors of > 10 % in both $\ln \sigma_{\text{ext}}$ and $\ln \sigma_{\text{sca}}$ are far too large to be acceptable. In order to keep $\ln \sigma$ errors below 5 % and g errors below 0.10, we would have to impose limits of $D_f \geq 1.8$ and $n_s < 100$.

3. As the authors have noted, the fractal dimension of soot particles may increase to 2.3 (Bambha et al., 2013) or higher (Zhang et al., 2008) following coating. The value of 2.3 is already outside the range of the D_f studied, presumably because the clustering algorithm does not represent subsequent restructuring. But since the coating-induced increase in D_f was prescribed during cluster formation and not afterwards, even the $D_f = 2.2$ aggregates may not have the same structure as restructured DLCA soot with $D_f = 2.2$. In particular, the anisotropy (Heinson et al. 2010; Eggersdorfer and Pratsinis, 2013) and fine structure (Mitchell et al., 2003) of restructured aggregates are not constrained by D_f alone. So the higher D_f values of restructured BCFAs may not be precisely captured by tuning the clustering algorithm to produce higher D_f values. This theoretical expectation is confirmed by a comparison of microscopy images (Bambha et al., 2013; Zhang et al., 2008) with the authors modelled BCFAs (shown in their Fig. 1). The modelled BCFAs appear to have a different, less-compact structure than the real restructured BCFAs. This would imply that the real restructured BCFAs may have smaller deviations from Mie theory than calculated in the manuscript. Would it be possible for the authors to somehow synthesize aggregates that are more spherical to provide an upper bound? We realize that this may be quite challenging without a quantitative restructuring model, but if the clustering algorithm is not representing the restructuring process, a manually-synthesized BCFA would not necessarily be less physical than the current high-D_f BCFAs.

It is definitely outside the scope of this work to attempt such restructuring or generating such a large number of particles manually, but we would be very interested in pursuing this avenue in future work. A short summary of the literature above has been added to the end of the section discussing fractal dimension (§1.2): It reads: "When aggregates collapse into more tightly packed, higher D_f clusters, they are restructured by the changes in humidity, and the coatings covering them. In these cases, the new shapes have formed in a fundamentally different manner from particles formed by the cluster-cluster algorithm used in this work (Thouy and Jullien, 1994) which gradually aggregates clusters to other clusters, never reordering previously added spherules within the aggregate. As such, the larger valued D_f aggregates should not be taken as realistic models for compact BCFAs after atmospheric processing. This can be seen in comparisons of real compact BCFAs (e.g. Mikhailov et al., 2006; Zhang et al., 2008; Bambha et al.,2013) with Fig. 1d generated by the cluster-cluster algorithm."

One final comment. Since the asymmetry parameter g was quite small for the smallest clusters (Fig. 5c, bottom row), perhaps it would be better in Fig. 7c to plot the absolute error in g instead of the relative error. The actual deviation here appears to be relatively small.

We agree, and this has been done.

We agree with Smith and Graingers conclusion that light-scattering by BCFAs cannot be accurately modelled as equivalent spheres in general, but we wonder whether this conclusion could be reversed under certain conditions: could the errors in an equivalent-sphere treatment in an atmospherically-relevant parameter space ($D_f > 1.8$ and $n_s < 500$) be small enough to be acceptable in at least some modelling applications?

As we mentioned above, in order to keep errors in $\ln \sigma$ below 5 % and errors in g below 0.10, we would have to impose limits of $D_f \geq 1.8$ and $n_s < 100$ which seems unacceptable for most modelling applications.

Response to the short comment by M. Kahnert

1. Comment on the results presented in Sect. 3.3: Similar work has been done and discussed in Kahnert, M.: Numerically exact computations of the optical properties of light absorbing carbon aggregates for wavelength of 200 nm - 12.2 um, Atmos. Chem. Phys. 10, 8319-8329, 2010. The fitting ansatz used there (Sect. 3.2) was slightly different from that proposed here and did not lend itself equally easily to analytically performing size integrations. In this regard the fitting approach proposed here by the authors is more useful. In the ACP paper by Kahnert the fitting approach was eventually dismissed and the computational results obtained for the black carbon aggregates were put into a look-up table and directly coupled to a chemical transport model and to a radiative transfer model. The rationale was that there really is no more need for parameterisations if one can perform aerosol optics calculations for all relevant sizes and wavelengths. That this is indeed possible has been demonstrated in that paper, and it has been confirmed by the work presented here by Smith and Grainger.

Agreed. In the methods section, we have added a passage commenting on the differences between our methods: "Similar work by (Kahnert (2010b) used fewer different sizes of BCFA, but attempted to find a "typical" geometry that was a good optical representation of BCFA at that size, by this method obtaining smoothly varying fields. In this study, only a single representation of each n_s and D_f particle was generated, and so one would expect occaisional outliers in the output optical properties. Since the aim of this work was to find a mapping of complex shapes to simple spherical equivalents it was thought that a parameterisation of the conversion would smooth out these issues."

In the results section, discussing the fitting, we have similiary compared our fitting strategies: "In the work of Kahnert (2010b), attempts to parameterise the optical properties σ_{abs} with a cubic polynomial in the radius of equal volume, r_v, were successful, but fits of σ_{sca}, $g \times \sigma_{\mathrm{sca}}$, and the backscatter cross-section were unsuccessful. Instead, fits to the logarithm of these quantities were obtained which made analytic integration over r_v to develop optical properties of size distibutions of BCFA unfeasible. As such, a look-up table of pre-computed BCFA optical properties was used instead. In this work, that problem is not encountered since we are dealing with parameters of the properties we desire to integrate directly."

2. Comment on comparison between modelling results and measurements: In the manuscript the authors mention that their modelled single-scattering albedo at visible wavelengths agrees well with observations as reviewed by Bond and Bergstrom (2006). However, Bond and Bergstrom also review measurements of the mass absorption cross section (MAC). The ACP paper by Kahnert (2010) cited above briefly mentions that existing computations for black carbon aggregates do not fully agree with available measurements. This problem is discussed in more detail by Kahnert M.: On the discrepancy between modeled and mea-

sured mass absorption cross sections of light absorbing carbon aerosols, Aerosol Sci. Technol. 44, 453-460, 2010. It would be interesting if the authors could convert their absorption cross section at 550 nm to MAC and compare to the measured values reviewed by Bond and Bergstrom, as well as to the computed values reported by Kahnert.

A very good idea. This has been done and a figure added to the paper showing MAC at 550 nm. We also include it here as Fig. R4. We find values of $5.8 < \mathrm{MAC} < 6.3$ for $\lambda = 550$ nm, $D_f = 1.8$ which is in agreement with your paper. Discussion of this has been added to the results section and reads: "The mass absorption cross-section (MAC) is another common parameter used to describe black carbon aerosols. Values of MAC at $\lambda = 550\,\mathrm{nm}$ obtained by these calculations are shown in Fig. 4 and are consistent with similar calculations in the literature (Bond and Bergstrom, 2006; Kahnert, 2010a) which found calculated MAC values of around $6\,\mathrm{m}^2/\mathrm{g}$. There is a discrepancy between this and measured values of MAC which are around $7.5\,\mathrm{m}^2/\mathrm{g}$. Results also agree with the work of Scarnato et al. (2013) who found that 'lacy' aggregates had a higher MAC and lower SSA than more compact aggregates."

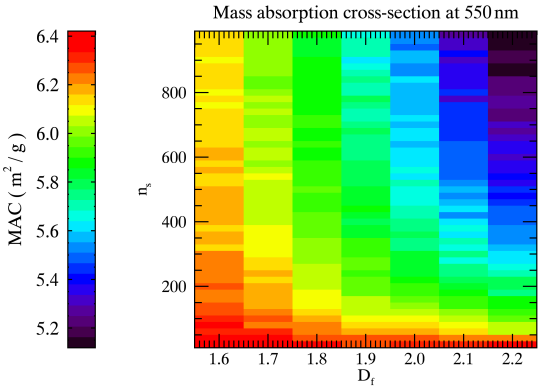

Figure R4: The mass absorption cross section at $\lambda = 550\,\mathrm{nm}$ for BCFAs. For these calculations, a density of $1.8\,\mathrm{g\,m^{-2}}$ was assumed. This figure has been added to the manuscript.

One more very minor thing: please correct the citation of Gustav Mies seminal paper: "Beiträgge" should be "Beiträge".

Done. Thank you for spotting this!