

# 1 **Standard climate models radiation codes underestimate** 2 **black carbon radiative forcing**

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8

## 9 **Abstract**

10 Radiative forcing (RF) of black carbon (BC) in the atmosphere is estimated using radiative  
11 transfer codes of various complexities. Here we show that the 2-stream radiative transfer  
12 codes used most in climate models give too strong forward scattering, leading to enhanced  
13 absorption at the surface and too weak absorption by BC in the atmosphere. Such calculations  
14 are found to underestimate the positive RF of BC by 10% for global mean, all sky conditions,  
15 relative to the more sophisticated multi-stream models. The underestimation occurs primarily  
16 for low surface albedo, even though BC is more efficient for absorption of solar radiation over  
17 high surface albedo.

18

## 19 **1 Introduction**

20 Black carbon (BC) in the atmosphere has been investigated over many decades (Novakov and  
21 Rosen, 2013). The first estimate of radiative forcing of BC on a global scale was provided  
22 already two decades ago (Haywood and Shine, 1995). However, the diversity in existing  
23 estimates of the climate effect of BC is large (Bond et al., 2013; Boucher et al., 2013; Myhre  
24 et al., 2013). The causes for the diversity in estimates are many, from emissions (Amann et  
25 al., 2013; Cohen and Wang, 2014; Lam et al., 2012; Stohl et al., 2013; Wang et al., 2014b),  
26 lifetime and abundance (Hodnebrog et al., 2014; Samset et al., 2014; Wang et al., 2014a) to  
27 radiative efficiency (Samset et al., 2013; Zarzycki and Bond, 2010).

28 When estimating BC RF, the radiative transfer code is a crucial component. Accurate results  
29 can be achieved by using multi-stream line-by-line codes. However, these calculations are

1 computationally demanding and are usually not applied for global scale simulations. In  
2 present climate models, simplified radiation schemes of various complexity are therefore  
3 used, and compared against line-by-line results, and each other, as consistency checks.

4 Several radiation intercomparison exercises have been taken place (Boucher et al., 1998;  
5 Collins et al., 2006; Ellingson et al., 1991; Forster et al., 2011; Forster et al., 2005; Myhre et  
6 al., 2009b; Randles et al., 2013), yielding important suggestions for improvement to the  
7 radiative transfer codes. Randles et al. (2013) found that many of the presently used radiative  
8 transfer codes underestimate the radiative effect of absorbing aerosols, relative to benchmark  
9 multi-stream line-by-line codes. Further, one of the radiative transfer codes was run both as a  
10 multi-stream code resembling the benchmark codes, as well as run as a 2-stream code  
11 resembling the simpler codes used in climate models. These two codes were denoted as  
12 number 3 and 4, respectively in Randles et al. (2013) and used in the current work. The results  
13 indicated that the number of streams in the radiative transfer calculation, i.e. the number of  
14 angles through which radiation is allowed to scatter, is crucial for the differences found  
15 between the radiation codes. On average, the simpler codes underestimated the radiative  
16 effect of BC of the order of 10-15% relative to the benchmark line-by-line codes. In the  
17 present study we further investigate this potential underestimation of BC RF in many of the  
18 global climate models, and develop a physical understanding for why it occurs.

19

## 20 **2 Models and methods**

21 Simulations in the present paper were performed with a radiative transfer code using the  
22 discrete ordinate method (Stamnes et al., 1988). This model has previously been run in  
23 idealized experiments with prescribed vertical profiles of aerosol extinction (Randles et al.,  
24 2013) and used for global climate simulations (Myhre et al., 2009a). The radiative transfer  
25 code was run either in a multi-stream mode (8-streams) or with 2-streams and the Delta-M  
26 method (Wiscombe, 1977). In the global simulations we used meteorological data from  
27 ECMWF, and specified aerosol optical properties (Myhre et al., 2009a) and aerosol  
28 distribution from the OsloCTM2 chemical transport model (Skeie et al., 2011). To study the  
29 impact of the radiation code on global mean RF of BC, input fields and results from  
30 OsloCTM2 part of AeroCom Phase II for several aerosol components were used. Here,  
31 aerosol BC abundances were specified for 1850 and 2000, and anthropogenic RF defined as

1 the difference between outgoing top-of-atmosphere shortwave radiative flux between these  
2 two years (Myhre et al., 2013).

3

## 4 **3 Results**

### 5 **3.1 Global distribution of underestimated BC RF in models**

6 Figure 1a shows the global mean, clear sky direct effect RF by BC, for a 2-stream simulation  
7 relative to a simulation with 8-streams. As in Randles et al. (2013) we find that the 2-stream  
8 calculation tends to give lower RF than the 8-stream one. The underestimation in the 2-stream  
9 simulation is shown here to be largest over ocean, with low surface albedo, whereas over  
10 regions with high surface albedo the 2-stream more closely reproduces the 8-stream  
11 simulation. Under clear sky conditions, the global, annual mean underestimation is 15%  
12 (0.158 versus 0.187 W m<sup>-2</sup>) in the 2-stream relative to 8-stream simulation (RF (2-stream)  
13 divided by RF (8-stream)).

14 The albedo of clouds is also affected by the number of streams adopted in the radiative  
15 transfer simulations. This makes the top-of-atmosphere reflected solar radiation increase in 2-  
16 stream calculations, relative to 8-stream simulations. For all-sky conditions, the global mean  
17 underestimation of RF in the 2-stream simulation amounts to 7%. However, modifying the  
18 scattering by clouds to get similar top-of-atmosphere solar flux as in the 8-stream simulation  
19 and close to measured fluxes leads to a 10% underestimation in the 2-stream simulation  
20 relative to the 8-stream simulation (0.254 versus 0.283 W m<sup>-2</sup>). The largest underestimation is  
21 over ocean, and over regions with small cloud cover, as shown in Figure 1b.

### 22 **3.2 Underestimation of BC RF as a function of altitude**

23 Global mean RF of BC, as a function of BC located at various altitudes, is shown in Figure 2.  
24 The figure shows results for both 2-stream and 8-stream simulations. A similar curve has  
25 previously been presented in Samset and Myhre (2011) for 8-stream simulations. The present  
26 curve is slightly modified, due to updated ozone and cloud fields. The same approach as in  
27 section 3.1, to keep cloud scattering and therefore top-of-atmosphere radiative flux for the 2-  
28 stream simulation equal to the 8-stream simulation, has been applied.

1 Figure 2a clearly shows the increasing normalized RF (RF exerted per unit aerosol burden) by  
2 BC as a function of altitude, due to enhanced effect of absorbing material above scattering  
3 components. The underestimation in the 2-stream simulation is similar in magnitude for clear  
4 sky and all sky conditions, but is in relative terms larger for clear sky due to smaller absolute  
5 values (Figure 2b).

6 For the all sky simulation the underestimation by the 2-stream versus 8-stream simulation is  
7 close to 10% for BC at all altitudes, except below 900 hPa. BC above scattering components  
8 such as clouds increases the absorption by BC, as do the presence of scattering aerosol types,  
9 and Rayleigh scattering. Absorption by gases such as ozone and water vapour, as well as  
10 absorption by other aerosol types, reduces the absorption by BC. For all sky conditions,  
11 Figure 2 shows a large degree of compensation by scattering and absorption by gases, and  
12 other aerosol types than BC. In a model simulation with only BC in the atmosphere, the  
13 normalized RF of BC was found to be 1% higher in 2-stream simulations than in 8-stream  
14 simulations, showing the importance of the other atmospheric components for the correct  
15 determination of BC RF.

16

### 17 **3.3 Physical description of the underestimation of BC RF**

18 The radiative forcing due to aerosols is known to be a strong function of surface albedo  
19 (Haywood and Shine, 1997). This is illustrated in Figure 3a, where the radiative effect of  
20 aerosols with different single scattering albedo has been calculated as a function of surface  
21 albedo. We reproduce the well-known characteristics of largest impact of absorbing aerosols  
22 over bright surfaces, and of scattering aerosols over dark surfaces.

23 Figure 3b shows the difference between 2-stream and 8-stream calculations, as a function of  
24 surface albedo, and for a range of aerosol single scattering albedos. 2-stream and 8-stream  
25 results deviate substantially between surface albedos of 0.05 and 0.2. These are surface albedo  
26 values where absorbing aerosols have a relatively weak radiative effect. An increasing single  
27 scattering albedo gives increasing underestimations of 2-stream results (Figure 3b) and at the  
28 same time a decreasing radiative effect (Figure 3a).

29 Our interpretation of the cause for the underestimation of 2-stream results relative to multi-  
30 stream results is lack of sufficient multiple scattering in connection to forward scattering and  
31 low surface albedo. Under such conditions the scattering is too strong in the forward direction

1 in 2-stream approaches. In addition the low surface albedo, and thus strong surface  
2 absorption, hinders further multiple scattering. Multiple scattering in general enhances the  
3 radiative effect of absorbing aerosols.

4 To illustrate the importance of multiple scattering for the abovementioned underestimation,  
5 additional simulations show that purely absorbing aerosols in a non-scattering atmosphere  
6 have differences between 2-stream and multi-stream results within only a few percent (less  
7 than 2%), which is the typical deviation as shown in Figure 3b, except for at low surface  
8 albedo. The agreement between 8-stream and even higher number of streams such as 16-  
9 stream simulations is generally within 1%, except for very small absolute RF values.  
10 Simulations with 4-streams are generally close to 8-stream simulations. For pure scattering  
11 aerosols 2-stream simulations varies with solar zenith angle (see Randles et al. (2013)) and  
12 surface albedo compared to 8-stream simulations, but on a global mean 5% stronger negative  
13 RF for anthropogenic sulphate aerosols. The results shown in Figure 3 are for a solar zenith  
14 angle of 30 degrees, but are generally applicable for other solar zenith angles. However, note  
15 that the critical single scattering albedo for transitioning from positive to negative radiative  
16 effect decreases with increasing solar zenith angle. The underestimation shown in Randles et  
17 al. (2013) can also be seen in Figure 3b for single scattering 0.75 (close to 0.8 used in the  
18 paper) and for surface albedo of 0.2 of around 10%.

19

## 20 **4 Conclusions**

21 Two-stream approximations using the Delta-M method, as employed by a majority of present  
22 climate models, are found to be relatively accurate for absorbing aerosols. The exception is  
23 over areas with low surface albedo. Here, the enhanced forward scattering hinders sufficient  
24 multiple scattering, causing an underestimation of the radiative effect of BC. Low albedo  
25 occurs in regions with low cloud cover, and low surface albedo such as ocean and snow free  
26 forest. In such cases the underestimation relative to more advanced radiation schemes can be  
27 of the order of 20-25%. The underestimation for BC is largest in the presence of scattering  
28 components. This also applies to gases with solar absorption. However, under clear sky  
29 condition, underestimation of a similar magnitude to BC will only be caused by gases with  
30 solar absorption in UV and visible region where Rayleigh scattering is strong. Thus ozone in  
31 the lower troposphere is the only gas that is substantially influenced by the number of streams  
32 in the radiative transfer simulations. For a global increase in water vapour by 20% in the

1 lowest 1-2 km of the atmosphere, the difference between 2-stream and 8-stream simulations is  
2 found to be less than 1%.

3 On a global scale we simulate a 10% underestimation for RF of BC for all-sky conditions, and  
4 15% for clear sky, for 2-stream relative to 8-streams. The clear sky results for selected  
5 profiles and solar zenith angles in Randles et al. (2013) showed an average model  
6 underestimation between 12 and 15% compared to benchmark model simulations. The  
7 implication of the underestimation is that recent estimates of global mean RF due to BC, e.g.  
8 in Myhre et al. (2013) and Bond et al. (2013), where the latter is based on radiative transfer  
9 calculations in Schulz et al. (2006), could be up to 10% too weak, as they are primarily based  
10 on models with radiative transfer codes with 2-stream simulations. It must however be noted  
11 that other issues related to radiative transfer codes may lead to compensation of this  
12 underestimation, or additional underestimation. In addition, uncertainties in the abundance of  
13 BC, and in its optical properties, are much larger than 10%. Burden of BC and the normalized  
14 RF has a standard deviation of the order of 50% relative to mean values for the 15 global  
15 aerosol models in AeroCom Phase 2 (Myhre et al., 2013). Even so, considerations for  
16 improvements of radiation schemes in global climate models should be made to provide more  
17 accurate calculations of present and future radiative forcing due to BC.

18

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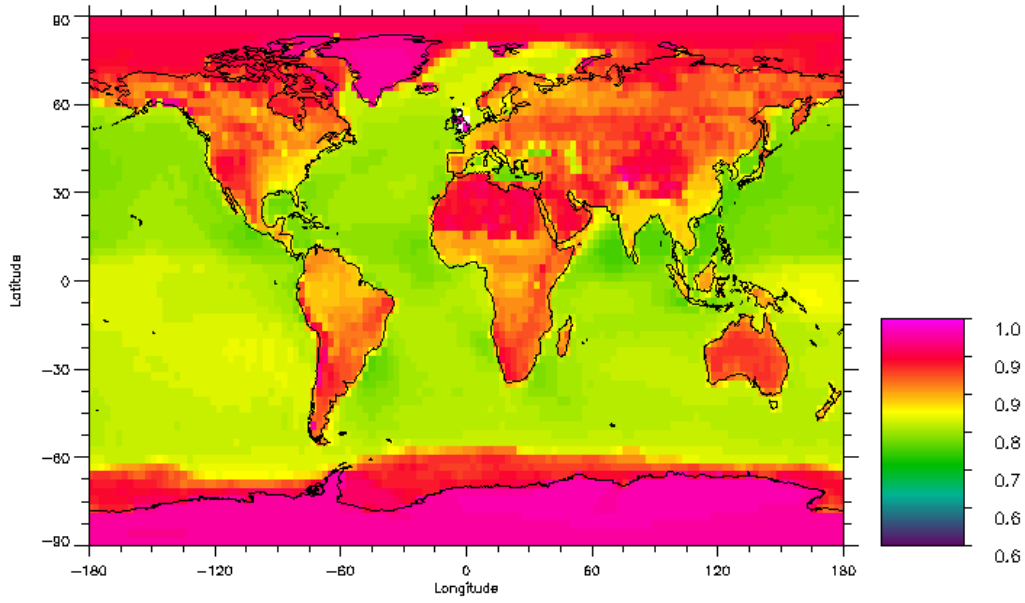
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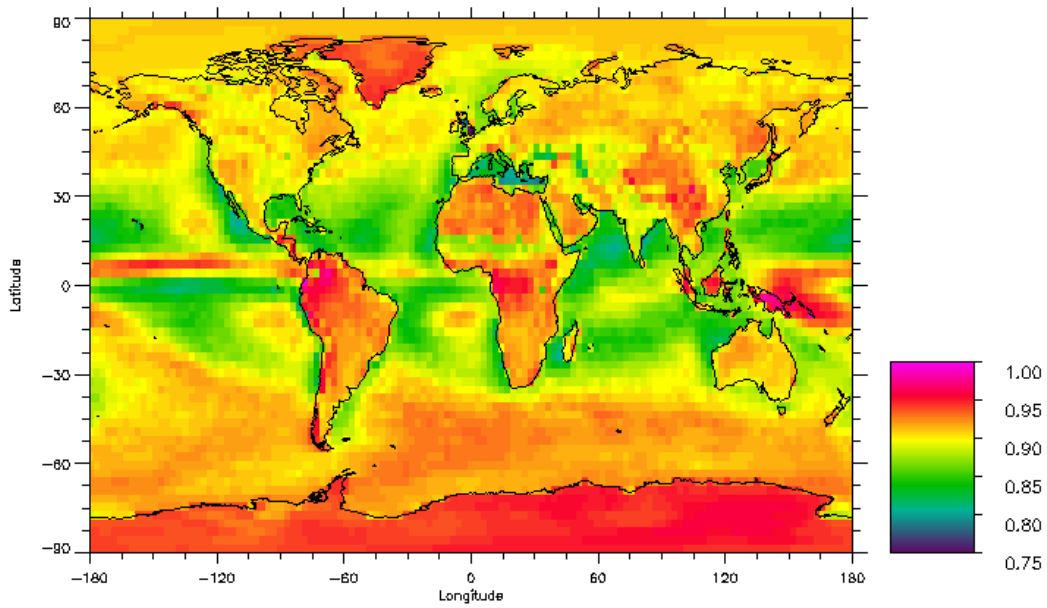
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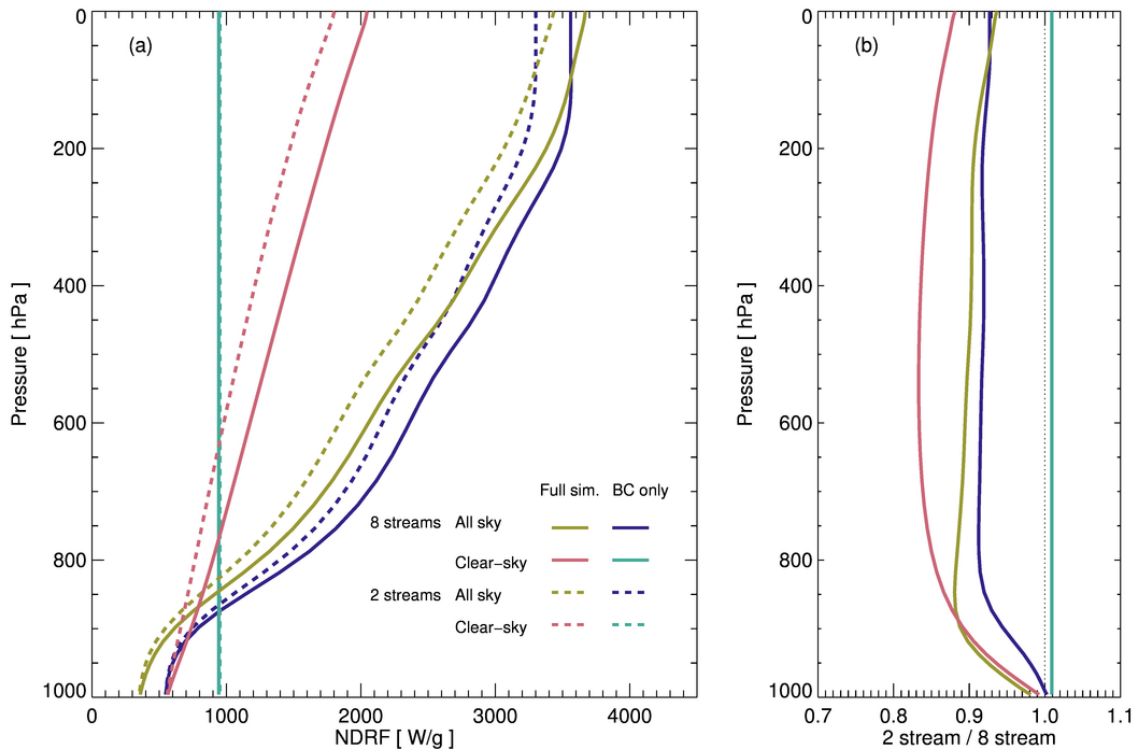


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6 **Figure 1: Geographical distribution of ratio between annual mean RF of BC**  
7 **from 2-stream simulation relative to 8-stream simulation for clear sky (upper)**  
8 **and all sky (lower).**

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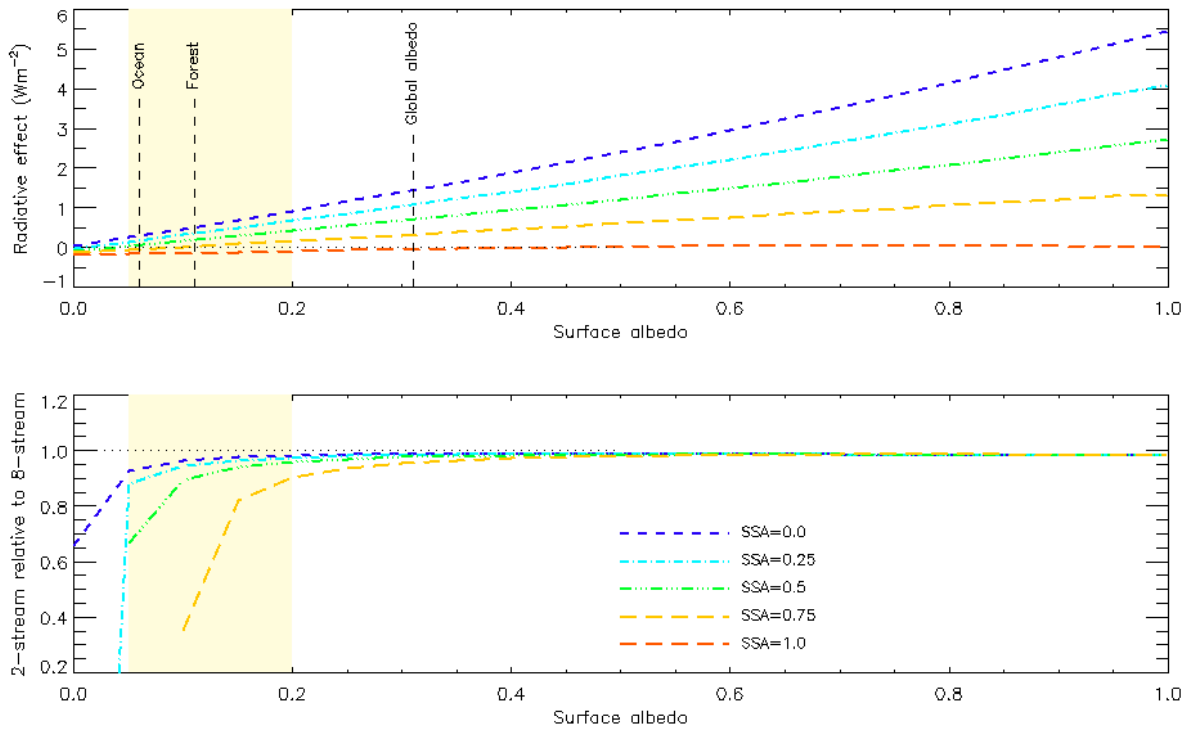


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2 **Figure 2: (a) BC RF normalized by abundance, as a function of altitude. Solid**  
 3 **lines: 8-stream simulations. Dashed lines: 2-stream simulations. Colors**  
 4 **represent all sky and clear sky conditions, and whether a full atmospheric**  
 5 **simulation including Rayleigh scattering, water vapour and background**  
 6 **aerosols was performed (“Full sim.”), or if BC was the only radiatively active**  
 7 **agent (“BC only”). (b) Ratio of 2-stream to 8-stream simulation results, for the**  
 8 **four cases shown in panel (a).**

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2 **Figure 3: RF as a function of surface albedo for various single scattering**  
 3 **albedo (upper), and relative differences between 2-stream and multi-stream**  
 4 **simulations (lower). In cases where the sign of 2-stream and multi-stream**  
 5 **simulations for a particular single-scattering albedo differs the results are left**  
 6 **out of the lower panel.**

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