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# The effects of turbulent collision-coalescence on precipitation formation and precipitation-dynamical feedbacks in simulations of stratocumulus and shallow cumulus convection

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### Abstract

A double moment warm rain scheme that includes the effects of turbulence on droplet collision rates has been implemented in a large-eddy model to investigate the impact of turbulence effects on clouds and precipitation. Simulations of shallow cumulus and stratocumulus show that different precipitation-dynamical feedbacks occur in these regimes when the effects of turbulence are included in the microphysical processes. In both cases, inclusion of turbulent microphysics increases precipitation due to a more rapid conversion of cloud water to rain. In the shallow convection case, the greater water loading and latent heating in the upper cloud levels reduces the buoyancy pro-10 duction of turbulent kinetic energy and the entrainment. The stratocumulus case on the other hand shows a positive precipitation feedback, with enhanced rainwater producing greater evaporation, stronger circulations and more turbulence. Sensitivity studies where the cloud droplet number was varied show that greater number concentrations

suppress the stratocumulus precipitation leading to larger liquid water paths. This positive second indirect aerosol effect was produced in all of the simulations except for the case using the turbulent microphysics with the highest droplet number, which suggests a limit on the amount of liquid water that can be produced. While the sign of the second indirect effect is negative in the shallow convection case whether the effects of turbulence are considered or not, the magnitude of the effect is doubled when the turbulent microphysics are used.

#### 1 Introduction

Cloud microphysical parameterisations are required in atmospheric models of all scales from large-eddy simulation models through to climate models. Correctly representing microphysical processes in models is challenging yet imperative for quantitative precipitation forecasting and climate studies. To enable greater confidence in

titative precipitation forecasting and climate studies. To enable greater confidence in climate projections one of the processes that requires a quantitative analysis is the



second aerosol indirect effect, which is the effect from enhanced aerosol concentrations in clouds suppressing drizzle and prolonging cloud lifetimes (Albrect, 1989). To be able to quantify this effect with any real certainty, the cloud microphysical processes must be accurately represented in global climate models (GCMs), in particular the autoconversion process, which describes the collision and coalescence of small droplets to form larger rain drops.

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In clouds where the temperature does not reach freezing, it is the process of collision and coalescence that allows drops to grow to a size large enough to fall out of a cloud as rain. Observations of droplet growth tend to show a faster evolution and broader drop size distribution compared to the theoretically calculated drop spectra, where the

- drop size distribution compared to the theoretically calculated drop spectra, where the equations are applied to a randomly distributed population of drops whose motion is governed by gravitational forcing (see review by Grabowski and Wang, 2013). Several physical effects have been suggested to play an important role in the reduction of the growth times, including entrainment and mixing of dry air, turbulence and the role of
- giant cloud condensation nuclei (e.g. Beard and Ochs, 1993). Turbulence increases the collision rate of droplets in at least three ways: by changing the droplet velocities and the spatial distribution of the droplets (e.g. Franklin et al., 2005), and by changing the collision and coalescence efficiencies between droplets. Although the effect of turbulence on cloud droplet collision-coalescence rates is yet to be quantified by obser-
- vations, modelling studies have shown that turbulence can increase the collision rates of droplets by several times the purely gravitational rate (Franklin et al., 2005, 2007; Wang et al., 2005; Pinsky et al., 2006).

Franklin et al. (2007) performed direct numerical simulations (DNS) of droplets within turbulent flow fields and developed empirically derived equations that describe the tur-

<sup>25</sup> bulent collision kernel for droplet pairs, where the larger droplet is within the radius range of 10–30  $\mu$ m and the eddy dissipation rate of turbulent kinetic energy (TKE) is between 100 and 1500 cm<sup>2</sup> s<sup>-3</sup>. These turbulent collision kernels were used in solutions of the stochastic collection equation (SCE) by Franklin (2008) to develop empirical double-moment parameterisations of the effect of autoconversion, accretion and



self-collection on the rain and cloud water mixing ratios and the rain and cloud drop number concentrations. Parameterisations using both turbulent and non-turbulent collision kernels were developed. The SCE was solved for liquid water contents in the range of 0.01–2 gkg<sup>-1</sup>, cloud droplet number concentrations up to 500 drops cm<sup>-3</sup>
and relative dispersion coefficients of the initial drop size distribution between 0.25 and 0.4. The initial drop size distribution was a Gamma function and the separation radius that determined the point at which a cloud droplet becomes a raindrop was 40 µm. Using the SCE results for such a broad range of drop size distributions gives the resulting parameterisations greater statistical meaning and applicability. The two suites of warm rain parameterisations, turbulent and non-turbulent, allow the investigation of the effect of turbulence on the microphysical processes and the resulting feedbacks in atmospheric models. These effects are explored in this work for stratocumulus and shallow cumulus convection cases. Section 2 describes the model and the two cases

to be examined. Section 3 presents the results for the simulated cloud and dynamical structures and Sect. 4 shows the sensitivity of the results to changes in cloud droplet number concentrations. This is followed by a summary of the findings in Sect. 5.

### 2 Experiment design

The double-moment warm rain microphysics parameterisations of Franklin (2008) have been implemented in the University of California Los Angeles Large Eddy Simulation
 (UCLA-LES) model. The anelastic LES code is described in Stevens et al. (2005) and solves prognostic equations for the three velocity components, the total water mixing ratio, the liquid water equivalent potential temperature and the mass and number concentration of rain. Time integration of the momentum equations uses a leapfrog scheme and scalars are advanced using a forward-in-time method. Advection of the velocity components is solved using fourth-order centred differences and scalars are advected using a higher order upwind scheme with slope limiting using a montone centred method. Subgrid fluxes are modelled using the Smagorinksy–Lilly model. The



mass of cloud water is defined implicitly due to the dependence of the liquid water potential temperature on the total condensate, and the cloud droplet number concentration is a fixed parameter. The numerical solution of the cloud processes, including droplet sedimentation, is described in Savic-Jovcic and Stevens (2008) and assumes a constant cloud droplet number concentration (CDNC).

The default bulk microphysics scheme in the UCLA-LES is that of Seifert and Beheng (2001). In this study the autoconversion and accretion parameterisations of Franklin (2008) are the main subject of investigation, however, results from the default scheme and that of Khairoutdinov and Kogan (2000) are also used to give some indication of the range of results from different microphysics schemes. The turbulent autoconversion equation of Franklin (2008) has been modified to the following form, which gives a better representation of the DNS data at higher cloud water contents,

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$$\frac{\partial q_{\rm r}}{\partial t} \bigg|_{\rm auto} = 2.0026 \times 10^{3} \tan \left( -5.2 \times 10^{-2} R_{\lambda} + 15.78 \right) \cdot q_{\rm c}^{97.45(-8.4 \times 10^{-1})^{R^{\lambda}} + 2.5} N_{\rm c}^{1/\left(-9.0 \times 10^{-1} + 1.28 \times 10^{-2} R_{\lambda} - 2.3 \times 10^{-4} R_{\lambda}^{2}\right)}$$

- <sup>15</sup> where  $q_r$  and  $q_c$  are the rain and cloud water contents (kg m<sup>-3</sup>),  $N_c$  is the cloud droplet concentration (cm<sup>-3</sup>) and  $R_{\lambda}$  is the Taylor microscale Reynolds number of the flow field. This expression will underestimate the effects of turbulence on droplet collisioncoalescence due to the use of gravitational collision efficiencies and Taylor microscale Reynolds numbers that correspond to the DNS  $R_{\lambda}$ . Limited data are available for the effects of turbulence on collision efficiencies (Wang et al., 2008) and, therefore, we choose not to include this effect in the bulk microphysics scheme at this time. A significant limitation of DNS is the limited range of scales that can be simulated, with typical  $R_{\lambda}$  orders of magnitude smaller than those of atmospheric turbulence. The turbulent collision kernel parameterisations (Franklin et al., 2007) used to derive (1) are based
- on the  $R_{\lambda}$  of the DNS flow properties and any estimated effects of  $R_{\lambda}$  and flow intermittency are not included. However, the DNS simulations used as the basis for this



(1)

work did cover a wide range of dissipation rates from 100 up to  $1535 \text{ cm}^2 \text{ s}^{-3}$ . As is the approach in Seifert et al. (2010), in the LES implementation of the microphysics scheme  $R_1$  is calculated from the gridbox mean dissipation rate of TKE. Wyszogrodzki et al. (2013) showed that neglecting LES subgrid scale effects on the turbulent enhancement of the gravitational kernel is a reasonable approximation given the cur-5 rent state of knowledge. The autoconversion parameterisation (1) and the implementation described was used by Wang et al. (2013), where this equation and method was shown to produce cloud droplet and rain drop number concentrations and mixing ratios that were in better agreement with observations compared to other autoconversion schemes.

#### 2.1 Description of the shallow convection case – RICO

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The initial and boundary conditions and large scale forcings are taken from the Global Energy and Water Experiment (GEWEX) Cloud Systems Study (GCSS) Boundary Layer Cloud Working Group (BLCWG) intercomparison case described by vanZanten et al. (2011). This is a composite case based on observations taken during an undisturbed period of the Rain in Cumulus over the Ocean (RICO) field study (Rauber et al., 2007), which sampled precipitating trade wind cumulus. The domain size of these experiments is 13.2 km square and 5 km deep, with grid spacing of 100 m in the horizontal and 40 m in the vertical. The time step is variable and is chosen as to keep the Courant number between 0.65 and 0.85. The average observed cloud droplet num-20 ber concentration during RICO was 70 cm<sup>-3</sup>, and that number has been used for the

- control simulations. The length of the simulations for this case are 24 h and the profile statistics are taken as averages over the last 4 h. After the initial spin up, the model produces numerous shallow precipitating convective clouds as shown in Fig. 1a. The
- clouds typically extend up to 2400 m, have cloud bases at around 600 m and tend to 25 be 1-2 km in horizontal extent (Fig. 1b).



#### 2.2 Description of the stratocumulus case – RF02 of DYCOMS II

This case is based on the aircraft measurements taken during the second research flight (RF02) of the second Dynamics and Chemistry of Marine Stratocumulus (DY-COMS II) field campaign (vanZanten and Stevens, 2005). The initial conditions and large-scale forcings are taken from the GCSS BLCWG intercomparison study documented by Ackerman et al. (2009). RF02 penetrated nocturnal stratocumulus under a dry inversion consisting of heavy drizzling open cellular convection, as well as lightly drizzling closed cells. The initial conditions are an average over the two cloud populations sampled, except for the cloud droplet number concentration which is the average over the open cells only and set to 55 cm<sup>-3</sup>. The horizontal domain and grid spacing for this case study are 6.6 km<sup>2</sup> and 50 m respectively, while the vertical domain is 2 km and the grid spacing varies from 5 m at the surface and the inversion to 80 m at the model top. The model is run for 6 h and the profile statistics are calculated over the final 4 h. Typical liquid and rain water cross sections are shown in Fig. 2. Maximum liquid water

<sup>15</sup> contents occur at cloud top and precipitation reaches the surface.

#### 3 Simulated cloud and dynamical structure

### 3.1 Shallow cumulus convection – RICO

The turbulent microphysics parameterisations are applied in the regions of the clouds where the dissipation rates of TKE are between 100 and 1500 cm<sup>2</sup> s<sup>-3</sup>, with the higher dissipation rates associated with faster conversion rates from cloud to rain water (Franklin, 2008). In the RICO case the range of dissipation rates for which the turbulent microphysics scheme is valid is encountered in extensive regions of the clouds, with the highest dissipation rates occurring near the cloud tops (see Fig. 1b). These increased autoconversion, accretion and self-collection rates increase the rain water mixing ratio of the clouds as compared to the simulation where the non-turbulent pa-



rameterisation is used as shown in Fig. 3. The results using the well known Seifert and Beheng (2001) scheme are included as a measure of confidence for the more recent schemes of Franklin (2008). However, due to the different nature of the schemes a comparison is beyond the scope of this work and rather the focus is on the differ-<sup>5</sup> ences between the turbulent and non-turbulent microphysics schemes that have been derived using the same framework.

The rain water mixing ratios are significantly increased when the turbulent microphysics effects are included, with the largest difference occurring at the surface where the turbulent case produces almost 5 times more rain. The surface area experiencing rainfall increases by a factor of 3, and the rain fraction is also larger throughout the cloud layer in the turbulent microphysics case. The profiles of liquid water potential

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- cloud layer in the turbulent microphysics case. The profiles of liquid water potential temperature and total water mixing ratio show that the largest difference between the cases occurs near the height of the inversion, with the turbulent microphysics simulation being 0.2 K warmer than the case with the non-turbulent microphysics (Fig. 3).
- <sup>15</sup> The largest difference in cloud fraction occurs in the levels above 1000 m, where more cloud water in the turbulent case generates greater cloud fractions. The simulation using the turbulent microphysics parameterisation has on average greater cloud water throughout the cloud, however, the percentage increase in the amount of rain water produced in this simulation compared to the case using the non-turbulent microphysics
- is far more than the increase in the cloud liquid water contents. Quantitatively these results are in agreement with the RICO LES simulations of Seifert et al. (2010) who used a different turbulent collision kernel based on the results of Ayala et al. (2008) and Wang et al. (2008). Wyszogrodzki et al. (2013) used the Ayala et al. (2008) kernel in a bin microphysics scheme to simulate a shallow convection case from the Barba-
- dos Oceanographic and Meteorological Experiment (BOMEX). Their LES results show increases of accumulated surface precipitation of between 4 and 12 times depending on the cloud condensation nuclei concentration. Together with the results of this study, all these cases have demonstrated that including the effects of turbulence on the droplet collision rates makes a significant difference to the amount of rain that shallow



convective clouds produce. As discussed in both of the aforementioned publications, the resolution of these simulations is not fine enough to resolve the structure of these clouds. Seifert et al. (2010) tested the sensitivity of their results to a doubling in horizontal resolution and found a substantial reduction in the surface rain rate; however, the turbulence case still produced significantly greater rain.

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Time series of the evolution of the liquid water path, rain water path and cloud fractions are shown in Fig. 4. There is a spike during the first hour as the initial cloud field develops, and after about 2 h the cloud cover reaches 12%. The simulation with the turbulent microphysics shows a greater rain water path than the simulation with the non-turbulent microphysics at almost all times of the 24 h simulations, with a few significant peaks occurring during the last 4 h. The precipitation intermittency is due to the

icant peaks occurring during the last 4 h. The precipitation intermittency is due to the limited domain size that will only allow for one large rain event at a time (Seifert and Heus, 2013). All simulations show similar variability in the cloud fraction, however the average liquid water path variance over the last 4 h is almost double in the turbulent microphysics simulation.

Figure 5 shows that the evaporation of rain water is greatly enhanced in the turbulent microphysics simulation and this is due to an increase in both rain water and rain drop number concentration. The average TKE from the simulation using the turbulent microphysics is less than that of the non-turbulent case in the cloud levels above 2 km,

- however, in the lower levels including below cloud base, the TKE from the turbulent case is greater than the non-turbulent case. The increased TKE in the subcloud layer of the simulation that includes the turbulence effects on droplet collisions reflects the greater horizontal variability associated with the enhanced evaporation of precipitation destabilising the levels below the cloud (Fig. 5d). In the turbulent microphysics simu-
- <sup>25</sup> lation the reduced TKE in the upper regions of the cloud is caused by a reduction in the buoyancy production of TKE (Fig. 5c). In this case there is an increase in latent heating and water loading associated with the increased cloud and rain, particularly in these upper levels. This increase in water loading reduces the buoyancy production of TKE (Fig. 5c) and reduces the amount of TKE that is transported to the inversion layer



that is required for entrainment (Jiang and Cotton, 2000). Diagnosing the fractional entrainment rates using Eq. (16) of Stevens et al. (2001) and the total moisture mixing ratio, shows a larger entrainment rate throughout the vertical in the simulation with the non-turbulent microphysics parameterisations (not shown), in agreement with the analysis of the TKE budget and the larger water contents in the turbulent microphysics simulation.

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The reduced buoyancy production of TKE in the upper levels of the cloud in the turbulent case is associated with a reduction in the variance of the vertical motion (Fig. 5e). The updrafts within the clouds in the turbulent case are stronger in the upper levels due

- to the increased latent heating associated with the larger generation of cloud liquid water. This is also reflected in the more positive values of the third moment of vertical velocity in the turbulent microphysics case, indicating smaller, more intense updrafts and larger weaker downdrafts (not shown). These stronger in-cloud vertical velocities occur above the height of the maximum theta gradient (2321 m in the non-turbulent case).
- and 2328 m in the turbulent microphysics case) and reflect the stronger overshooting convection in the turbulent case. Wyszogrodzki et al. (2013) argued that the use of turbulent collision kernels produces a dynamical enhancement to the amount of precipitation generated due to the off-loading of condensed water, which in turn increases buoyancy and cloud top heights. In our case the water loading reduces the buoyancy
- in the upper levels of the cloud but increases the buoyancy below about 1800 m. Jiang and Cotton (2000) examined the differences between drizzling and non-drizzling shallow convective clouds and also found a reduction in buoyancy and turbulence in their case with larger precipitation. The effect of the dynamical feedback in the RICO case presented here is a negative feedback on the turbulent enhancement of rain water gen-
- eration. The reduced buoyancy production of TKE in the upper cloud levels where most of the liquid water is located (Figs. 1 and 3), reduces the TKE and dissipation rate of TKE compared to the simulation with the non-turbulent microphysics. Given that the turbulent enhancement is a function of the dissipation rate of TKE, the use of the turbulent microphysics parameterisations acts to reduce the dissipation rate in the cloud



levels where the liquid water contents are largest and hence produces a negative feedback. It should be recognised that there is still a significant enhancement compared to the non-turbulent case and the increased cloud depths discussed by Wyszogrodzki et al. (2013) are present in our simulations. Maximum cloud top heights are larger in the turbulent microphysics simulation compared to the non-turbulent; on average the highest cloud top is 2656 m compared to 2620 m. However, in this case the impact of the enhanced cloud and rain water acts to reduce the TKE rather than promote larger

buoyancy production of TKE.
The effect of this negative feedback can be seen in Fig. 6 where the dissipation
rates of TKE are shown for the control simulations and sensitivity tests where the cloud droplet number concentration was reduced from 70 to 40 cm<sup>-3</sup>. In the simulations with the reduced number concentration the amount of rain water is increased from the control, with the average rain water path in the non-turbulent microphysics simulations increasing from 1.9 to 4.3 gm<sup>-2</sup>, and 7.9 to 10.6 gm<sup>-2</sup> for the turbulent microphysics simulations. Figure 6 shows the reason why the percentage increase in rain water path is larger for the non-turbulent microphysics case, and this is due to a reduction in the dissipation rate of TKE in the turbulent microphysics simulations due to the negative feedback from the buoyancy generation of TKE, which limits the enhancement from the turbulent microphysics as the rain and cloud water increase.

#### 20 3.2 Stratocumulus – RF02 of DYCOMS II

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Similar to the shallow convection case, the dissipation rates of TKE that affect the microphysics are maximal in the upper levels of the stratocumulus cloud layer; however, for this case the dissipation rates are much weaker (Fig. 2). There are only small regions at the top of the cloud where the dissipation rate reaches  $100 \text{ cm}^2 \text{ s}^{-3}$  and, there-

fore, where the conversion rates between cloud and rain water will be accelerated by turbulence effects in the simulation that uses the turbulent microphysics. These small regions though do make a difference to the precipitation flux and the rain drop number concentration in the cloud and subcloud layers, while the cloud fractions remain



relatively unchanged (Fig. 7). The average rainwater path increases by 17% when the turbulent microphysics parameterisations are used. For this case the microphysics scheme of Khairoutdinov and Kogan (2000) has been used in the figures as a comparison for the new schemes, however, the results from the Khairoutdinov and Kogan scheme will not be discussed in this paper as the focus is on the turbulence effects.

For this lightly drizzling case the precipitation flux is maximum at cloud top (Fig. 7). The increased rain water in the turbulent microphysics simulation is associated with a greater number of rain drops and larger evaporation rates of rain water, particularly just below cloud base (Fig. 7a). In this case, the increased evaporation leads to greater variability and higher TKE in the turbulent microphysics simulation throughout both the cloud and subcloud layers. The enhanced rain water in the turbulent microphysics sim-

- ulation has a positive feedback, with more rain producing more evaporation of drizzle drops at cloud base, which destabilizes the subcloud layer and leads to stronger circulations and TKE (Feingold et al., 1996). The observations for this case showed that the vertical windo were possible along the showed instabilized base. (Ackarman et al., 2000)
- vertical winds were negatively skewed just above cloud base (Ackerman et al., 2009) and the simulation with the turbulent microphysics produces a closer match with nearly equal strength between updrafts and downdrafts at this height (Fig. 8f).

#### 4 Sensitivity to cloud droplet number concentrations

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Four simulations of the stratocumulus and shallow convection cases were performed
 with each of the non-turbulent and turbulent microphysics parameterisations. The simulations differ in the prescribed CDNC and reveal how the cloud properties change with changes in aerosol loading as manifested in changes of cloud droplet number. These simulations are not designed to reflect the complete aerosol-cloud interactions but rather to provide some insights into whether the effects of turbulence on cloud
 droplet interactions negate some of the reduction in precipitation that tends to occur with increasing cloud droplet number concentrations and the associated decrease in precipitation efficiency.



Figure 9 shows the average cloud properties over the last 4 h of the RF02 simulations of DYCOMS II. The cloud fraction increases monotonically for both the non-turbulent and turbulent cases as the CDNC increases from 25 to  $220 \text{ cm}^{-3}$ . There is a strong relationship between increasing cloud fraction and decreasing rain water path

- as the CDNC is increased. This result for a drizzling stratocumulus cloud agrees with the conceptual model that greater aerosol loading and associated CDNC suppresses precipitation formation and leads to larger cloud fractions (Albrecht, 1989). For the CDNC values explored here, the non-turbulent microphysics simulations demonstrate that stratocumulus clouds typical of this case study increase the amount of cloud water
- and reduce the rain water content when there is an increase in cloud droplet number, therefore, they show a positive second aerosol indirect effect (Fig. 9b; Stevens et al., 1998). While this is also true for the lowest three CDNC used in this study for the turbulent microphysics simulations, for the highest concentration of 220 droplets cm<sup>-3</sup> the turbulent microphysics simulation shows a reduction in both the rain and liquid wa-
- ter paths. The reduced rain water leading to a reduced liquid water path in the turbulent microphysics simulation with highest CDNC shows a negative second aerosol indirect effect. Other studies have also shown a non-monotonic increase in LWP with increasing aerosol concentrations and suggest that there is a limit to the degree of liquid water that can build up, with increasing efficiency of evaporation due to larger concentrations
   of smaller drops likely playing a role (Xue et al., 2008).

Figure 9c shows that there is an increase in the cloud base heights as cloud droplet numbers are increased and precipitation is decreased. This has been found before, for example by Savic-Jovcic and Stevens (2008), who showed that cloud base lowers in regions of precipitation due to the precipitation changes affecting the thermodynamic state of the subcloud layer. This can be seen through the tendency of the TKE to increase with CDNC in all simulations except for the turbulent case with highest CDNC (Fig. 9d). An important aspect for this work is that the TKE is greater for the turbulent

microphysics simulations compared to the corresponding non-turbulent simulation for each CDNC, except for the case with the largest CDNC where the behaviour changes



due to a reduction in liquid water path. These results reflect the positive feedback that the turbulent microphysics parameterisations have on increasing the TKE, which will then produce greater precipitation.

- Figure 10 shows the effects of increasing the CDNC in the RICO simulations. In this
  shallow cumulus convection case the liquid water path increases as the rain water path increases, which is the opposite of the stratocumulus case. Increased CDNC results in reduced rainwater in both cases, but in the RICO cases this also results in reduced liquid water paths. The increased CDNC will tend to slow the collision-coalescence process, enhance evaporation and reduce the drop fall speeds (Xue and Feingold, 2006). The result of this and the subsequent feedbacks in these small clouds is to reduce the liquid water path as well as the amount of precipitation. Therefore, for this case all simulations produce a negative second aerosol indirect effect, except for the highest CDNC using the non-turbulent microphysics scheme, which shows a small increase in liquid water path. The change in average cloud fraction for all simulations
- is small and generally less than 1 %. As shown in Xue et al. (2008) this may be due to the cancellation of changes in cloud size and cloud frequency.

The TKE response to increased CDNC in the shallow cumulus convection case is shown in Fig. 10b. Both sets of simulations tend to show an increase in vertically averaged TKE as CDNC increases, with the largest changes occurring for the smallest

- <sup>20</sup> CDNC in the turbulent microphysics set and the highest CDNC in the non-turbulent set. The simulation that produces the largest TKE is the non-turbulent microphysics scheme case with the highest CDNC. This is due to a significant increase in the vertical velocity variance and buoyancy production of TKE, which is responsible for the liquid water path being larger in this case than the simulation with CDNC of 100 cm<sup>-3</sup>. Examining
- the profiles of buoyancy production of TKE for the non-turbulent microphysics cases, shows that the reduction in vertically integrated TKE as CDNC reduces and rain water increases is due to the negative feedback that the enhanced precipitation has on the buoyancy production of TKE, as discussed previously. Figure 10 shows that the liquid water paths almost converge for the turbulent and non-turbulent simulations with the



largest CDNC due to the similar smaller rain water paths and the reduced effect of the turbulence enhanced autoconversion and accretion rates.

#### 5 Summary

Use of the bulk warm rain microphysics parameterisations of Franklin (2008) in the <sup>5</sup> UCLA-LES has allowed an investigation into the effects of turbulence on droplet collision-coalescence in stratocumulus and shallow convective clouds. The microphysics parameterisations that include the effects of turbulence on droplet collision rates had a greater impact on the simulated precipitation rates in the shallow convection case, where the larger dissipation rates of TKE produced a more rapid conversion

- of cloud water to rain water. The amount of rain water reaching the surface was almost 5 times larger in the simulation with the turbulent microphysics scheme. The much weaker dissipation rates in the stratocumulus case, however, also showed a change in the simulated precipitation when the effects of turbulence on microphysical processes were included in the model, with rain water paths increasing by 17%.
- <sup>15</sup> Both cases using the turbulent microphysics scheme produced greater evaporation rates of rain water, which caused a change in the thermodynamics of the subcloud layer, destabilizing the lower levels and enhancing the horizontal variability and TKE in this region. The difference in the precipitation-dynamical feedbacks between the two cases was in the upper levels of the clouds where the liquid water contents are largest.
- <sup>20</sup> In the shallow convection case the greater rain and cloud water loading and enhanced latent heating associated with the larger liquid water in the turbulent microphysics simulation, reduced the buoyancy production of TKE and the entrainment. Therefore, in this case a negative precipitation-dynamical feedback to the enhanced precipitation formation associated with turbulent microphysics effects was produced. In contrast,
- the stratocumulus case showed a positive feedback, with enhanced rainwater and rain water evaporation in the simulation with the turbulent microphysical parameterisations producing greater TKE in both the subcloud layer and in the upper cloud region.



Sensitivity studies where the CDNC was varied showed agreement with the conceptual model for lightly drizzling stratocumulus clouds, that greater CDNC suppresses precipitation formation leading to larger cloud fraction and liquid water paths (Albrecht, 1989). This can be interpreted as a positive second indirect aerosol effect, and was produced in all of the DYCOMS II simulations except for the case using the turbulent microphysics with the highest CDNC. This suggests that there may be a limit to the amount of liquid water that can build up in this atrategumulus gase, as here here

- the amount of liquid water that can build up in this stratocumulus case, as has been shown in other cases (e.g. Xue et al., 2008). The RICO shallow convection case produced a negative second indirect aerosol effect in all but one simulation. The increased
- <sup>10</sup> CDNC in the small convective clouds reduced the production of rainwater, enhanced the evaporation and led to a reduction in the liquid water path. While the sign of the second indirect effect is negative in the shallow convection case whether the effects of turbulence on cloud droplet collisions are considered or not, the magnitude of the effect is doubled when the turbulent microphysics are used. Liquid water paths reduce 15 from 19.1 to 16.1 gm<sup>-2</sup> for the non-turbulent microphysics simulations as CDNC in-
- creases from 40 to  $200 \text{ cm}^{-3}$ , whereas for the turbulent microphysics simulations the liquid water paths change from 24.2 to  $16.7 \text{ gm}^{-2}$ .

The results presented in this work are by no means a definitive or quantitative statement as to how the effects of turbulence on cloud droplet collision and coalescence impacts precipitation and cloud properties. Larger domains and higher resolution sim-

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- ulations need to be conducted in the future to test how robust the features are that have been described in this study. Seifert et al. (2010) performed a set of simulations at double the horizontal resolution of their control case and found a reduction in the rainfall increase due to turbulent enhancement. How this may change with fur-
- ther refinement of the computational grid remains to be seen. In addition, other case studies and thermodynamic profiles should be tested to investigate the sensitivity of the effects to changes in the large scale environment. Refinements and further developments to the turbulent collision kernels and collision efficiencies are also required to advance the knowledge regarding the effects of turbulence on cloud microphysics,





the formation of precipitation and the precipitation-dynamical feedbacks. Wyszogrodzki et al. (2013) describe their aims of developing an integrated multiscale computational approach that combines LES and direct numerical simulations approaches. This would provide a unique way to simulate the wide range of scales involved with precipitation formation from kilometres to millimetres.

As discussed by Savic-Jovcic and Stevens (2008), often LES require lower CDNC than observed to initiate precipitation, and this includes both bulk and bin models. Including the effects of turbulence in the microphysics parameterisations minimizes this need to artificially reduce CDNC in order to simulate observed precipitation rates. How much of this effect may be due to a better physical representation of the collision process or to numerical limitations is an open question. Use of observations to try to

cess or to numerical limitations is an open question. Use of observations to try to answer this would be a worthwhile endeavour; however, as noted by Xue and Feingold (2006), the variability of the cloud fields in shallow convection simulations where the impact of the turbulence enhancement is largest might make this somewhat chal-

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- <sup>15</sup> lenging. For example, the changes to liquid water paths due to the effects of turbulent microphysics are much smaller than the standard deviations of the liquid water path of any given simulation by about an order of magnitude. In this study the analysis of the turbulent enhancement and the precipitation-dynamical feedbacks has been on a scale larger than that of an individual cloud. Future work will investigate individual eloud properties and life evolues to examine the effects that the microphysics
- <sup>20</sup> cloud properties and life cycles to examine the effects that the microphysics parameterisations that include the effects of turbulence may have on the cloud scale.

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**Fig. 2.** Cross sections of the **(a)** liquid and **(b)** rain water mixing ratios  $(gkg^{-1})$  for the DYCOMS II case. Contour lines of the turbulent kinetic energy dissipation rate in **(a)** are  $100 \text{ cm}^2 \text{ s}^{-3}$ .





Fig. 3. RICO cloud properties for the simulations that use the turbulent (blue) and non-turbulent (red) microphysics parameterisations of Franklin (2008) and the microphysics scheme of Seifert and Beheng (2001; green). The initial conditions are given by the black dashed lines. (a) Liquid water potential temperature (K), (b) total water mixing ratio  $(gkg^{-1})$ , (c) liquid water mixing ratio  $(gkg^{-1})$ , (d) rain water mixing ratio  $(gkg^{-1})$ , (e) cloud fraction and (f) rain fraction.



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**Fig. 4.** Time series of RICO (a) liquid (cloud and rain) water path  $(gm^{-2})$ , (b) rain water path  $(gm^{-2})$  and (c) cloud fraction for the simulations that use the turbulent (blue) and non-turbulent (red) microphysics parameterisations of Franklin (2008) and the microphysics scheme of Seifert and Beheng (2001; green).





Fig. 5. As in Fig. 3 except for, (a) rain water evaporation (gkg<sup>-1</sup>s<sup>-1</sup>), (b) turbulent kinetic energy  $(m^2 s^{-2})$ , (c) buoyancy production of turbulent kinetic energy  $(10^{-4} m^2 s^{-3})$ , (d) variance of u component of horizontal wind  $(m^2 s^{-2})$ , (e) variance of vertical velocity  $(m^2 s^{-2})$  and (f) conditional average of vertical velocity inside clouds ( $ms^{-1}$ ).





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simulations for the control ( $N_c = 70$ ) and a reduced cloud droplet number concentration of  $N_{\rm c} = 40 \, {\rm cm}^{-3}$ .

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**Fig. 7.** DYCOMS II cloud and dynamical properties for the simulations that use the turbulent (blue) and non-turbulent (red) microphysics parameterisations of Franklin (2008) and the microphysics scheme of Khairoutdinov and Kogan (2000; green). The initial conditions are represented by the black dashed line. (a) Liquid water potential temperature (K), (b) total water mixing ratio  $(gkg^{-1})$ , (c) liquid water mixing ratio  $(gkg^{-1})$ , (d) precipitation flux  $(Wm^{-2})$ , (e) cloud fraction and (f) rain drop number concentration  $(m^{-3})$ .



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**Fig. 8.** As in Fig. 6 expect for, **(a)** rain water evaporation  $(gkg^{-1}s^{-1})$ , **(b)** turbulent kinetic energy  $(m^2 s^{-2})$ , **(c)** variance of liquid water  $(g^2 kg^{-2})$ , **(d)** variance of horizontal velocity  $(m^2 s^{-2})$ , **(e)** variance of vertical velocity  $(m^2 s^{-2})$  and **(f)** third moment of vertical velocity  $(m^3 s^{-3})$ .



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**Fig. 9.** Average DYCOMS II cloud and dynamical properties for specified CDNC. Rain water path  $(gm^{-2})$  and **(a)** cloud fraction and **(c)** cloud base height (m). Liquid water path  $(gm^{-2})$  and **(b)** rain water path  $(gm^{-2})$  and **(d)** vertically integrated turbulent kinetic energy  $(kgs^{-2})$ .







