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*Supplement of*

## **A comprehensive parameterization of heterogeneous ice nucleation of dust surrogate: laboratory study with hematite particles and its application to atmospheric models**

**N. Hiranuma et al.**

*Correspondence to:* N. Hiranuma (seong.moon@kit.edu)

916 This supplementary information provides additional details for 1) temporal plots of the  
 917 AIDA experiments during INUIT campaigns, 2) the  $n_s$  interpolation to draw initial  $n_s$ -isolines in  
 918 the T-RH<sub>ice</sub> space, 3) an indication of continuous increase in  $n_s$  after depletion of superaturation,  
 919 and 4) the method used to constrain  $n_s$  to >100% RH<sub>ice</sub>.

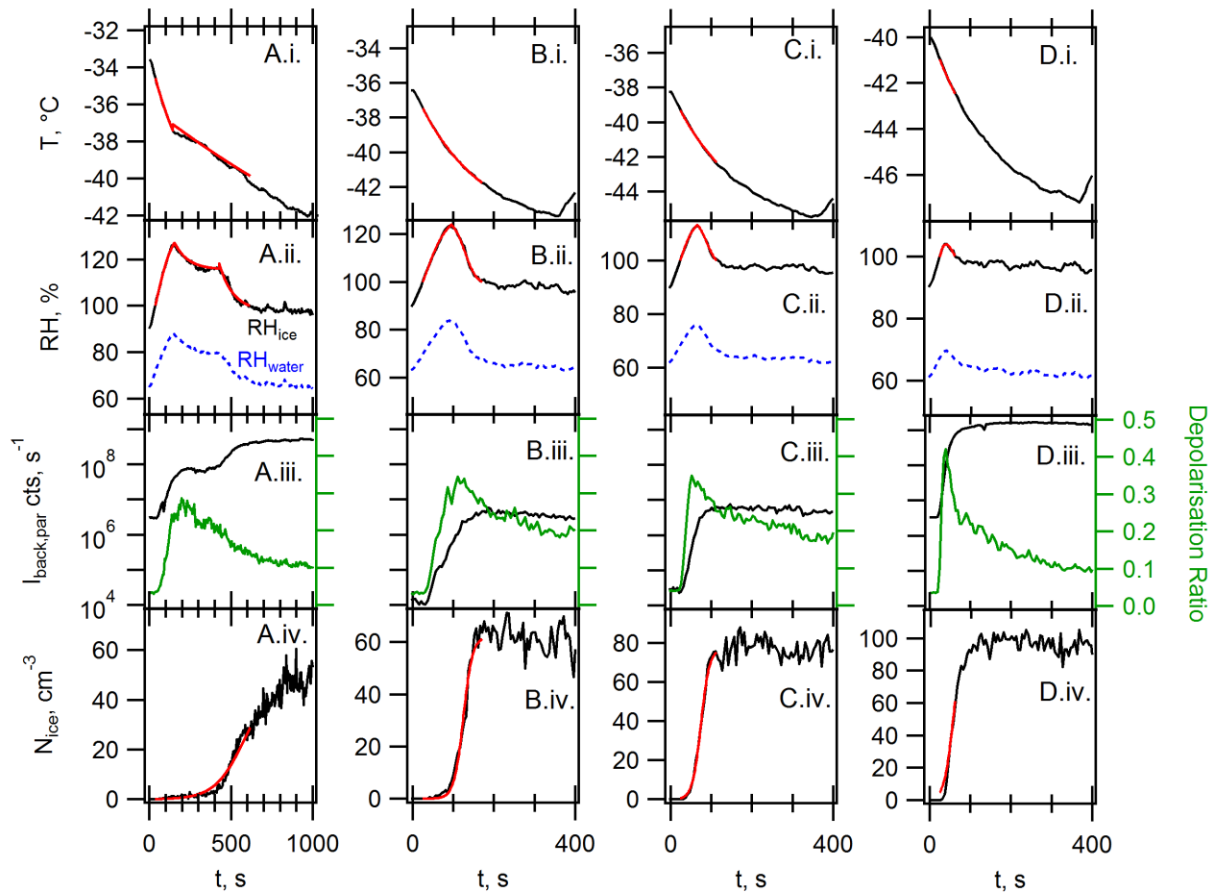
920

921 **AIDA experimental profiles for INUIT campaigns**

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923 Figure S1 shows the temporal profiles of AIDA experiments during INUIT campaigns,  
 924 including mean gas T, RH measured by TDL, depolarisation measured by SIMONE and  $N_{ice}$   
 925 measured by welas. The temporal  $n_s$  profiles were formulated based on these data.

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928 **Figure S1.** Temporal plots of the AIDA experiments of INUIT campaigns including A. INUIT01\_30, B.  
 929 INUIT04\_10, C. INUIT04\_08 and D. INUIT01\_26. Panel-arrangements are identical to Fig. 1.

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932 **Fitting procedure to generate initial  $n_s$ -isolines**

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934 In order to connect discrete constant  $n_s$  values derived from AIDA experiments plotted in  
935 the T-RH<sub>ice</sub> space (Fig. 2), isolines were initially fitted by assuming RH<sub>ice, (ns)</sub> to be a function of  
936 T. A bundle of  $n_s$ -isolines ( $2.5 \times 10^8 \text{ m}^{-2} < n_s < 1.0 \times 10^{12} \text{ m}^{-2}$ ) was derived from the following  
937 second degree polynomial fit equations:

938

939  $RH_{ice, (n_s)} = f(T)$   
940  $RH_{ice, (n_s = 1.0 \times 10^{12})} = 305.62 + (6.8767 \times T) + (0.062894 \times T^2)$   
941  $RH_{ice, (n_s = 1.0 \times 10^{11})} = 312.94 + (7.5808 \times T) + (0.067883 \times T^2)$   
942  $RH_{ice, (n_s = 1.0 \times 10^{10})} = 334.74 + (8.2497 \times T) + (0.06897 \times T^2)$   
943  $RH_{ice, (n_s = 5.0 \times 10^9)} = 334.17 + (8.2704 \times T) + (0.068525 \times T^2)$   
944  $RH_{ice, (n_s = 1.0 \times 10^9)} = 355.52 + (9.2094 \times T) + (0.07642 \times T^2)$   
945  $RH_{ice, (n_s = 5.0 \times 10^8)} = 383.61 + (10.414 \times T) + (0.087181 \times T^2)$   
946  $RH_{ice, (n_s = 2.5 \times 10^8)} = 434.61 + (12.552 \times T) + (0.10605 \times T^2)$  (S1)

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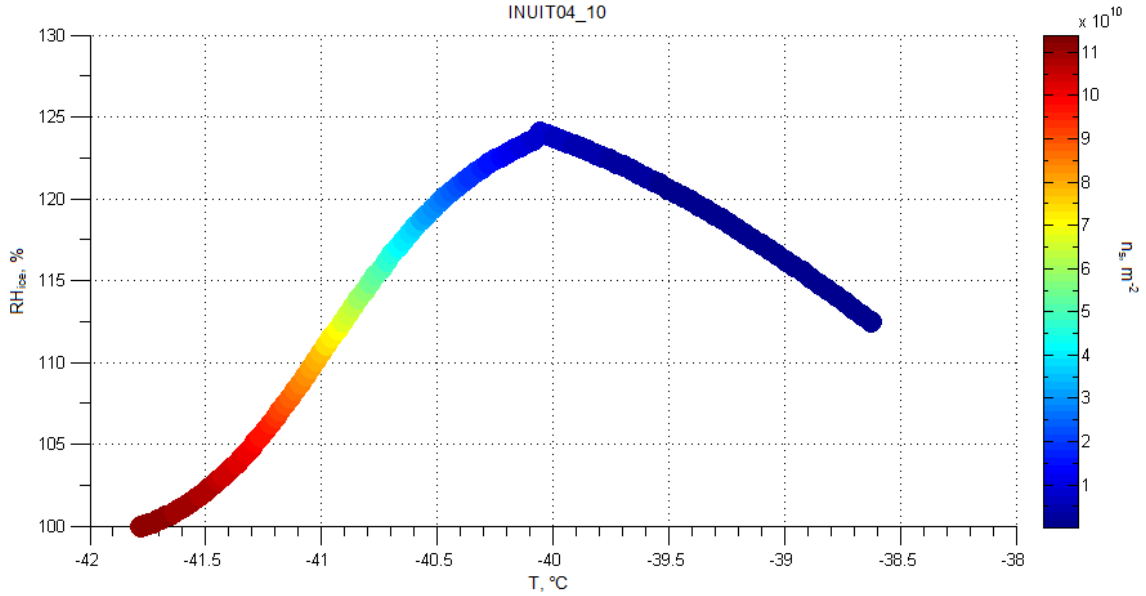
948 Note that the number in RH<sub>ice</sub>-bracket represents  $n_s$  values in  $\text{m}^{-2}$ .

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950 **Evidence of  $n_s$  increase after saturation depletion due to further cooling**

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952 Figure S2 shows an example of continuous increase in  $n_s$  after depletion of superaturation  
953 and resulting max  $n_s$  after the peak RH<sub>ice</sub> while continuous cooling at  $T > -50 \text{ }^\circ\text{C}$ , which is  
954 indicative of a predominant T influence. As opposed to the strong influence of RH<sub>ice</sub> at  $T < -60$   
955  $^\circ\text{C}$ , observed strong temperature-dependency was routinely observed for other experiments for T  
956  $> -50 \text{ }^\circ\text{C}$  (not shown).



957

958 **Figure S2.**  $n_s$  for hematite particles as a function of temperature under water subsaturated conditions from  
 959 INUIT04\_10. While continuous cooling (from right to left) proceeds, concurrent increase in  $n_s$  after depletion of  
 960 supersaturation at  $RH_{ice} = 123\%$  is observed. Color scale represents  $n_s$  in  $m^{-2}$ .

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### 962 Constraining $n_s$ to $>100\% RH_{ice}$

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964 The  $n_s$ -isolines governed by Eqn. S1 are not analogous to observed ice nucleation data  
 965 because the fit is blind to the presence of ice saturation conditions and therefore prone to an  
 966 artifact (i.e., nucleation under ice subsaturation conditions). Without any corrections, modelling  
 967 studies can be biased and mislead by concealed  $n_s$  values. Hence, we invariably confine the  $n_s$ -  
 968 isolines ( $2.5 \times 10^8 m^{-2} < n_s < 7.5 \times 10^{10} m^{-2}$ ) to  $RH_{ice} > 100\%$  (Fig. 4A) and corrected  $RH_{ice}$  by the  
 969 following procedures. First, an upper bound of the  $n_s$  ( $= 7.5 \times 10^{10} m^{-2}$ ) is assigned as the  
 970 reference isoline hovering above  $100\% RH_{ice}$  at any T between  $-36\text{ }^\circ\text{C}$  and  $-78\text{ }^\circ\text{C}$ . Next, to  
 971 relocate concealed isolines to  $RH_{ice} > 100\%$ , we introduced the constant, c, as:

972

$$973 \quad c = \frac{RH_{ice}(n_s=7.5 \times 10^{10}) - 100}{100 - RH_{ice}(n_s=2.5 \times 10^8)} \equiv \frac{a}{b} \quad (S2)$$

974

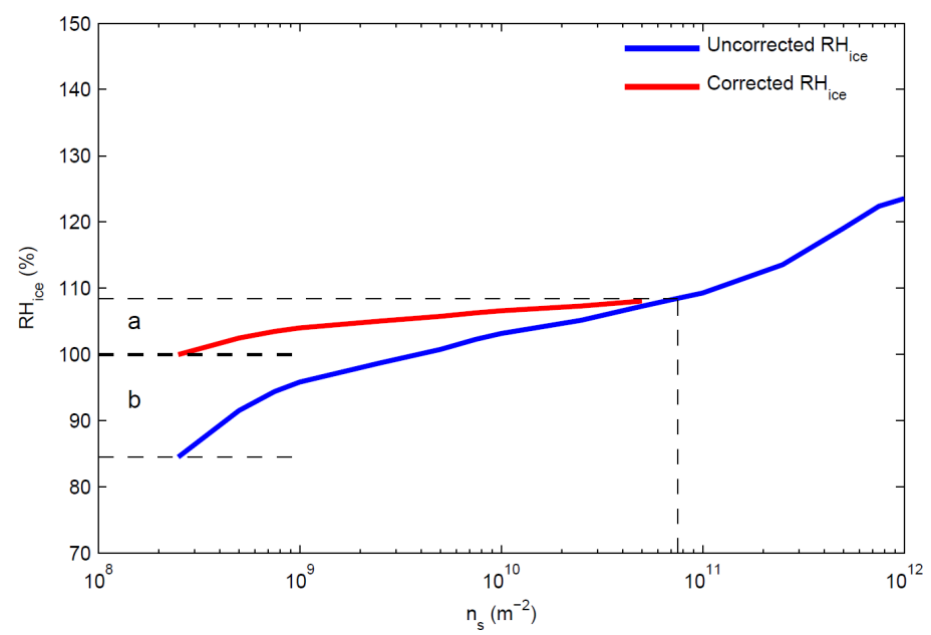
975 in which, a/b is evaluated at each temperature step (every  $0.1\text{ }^\circ\text{C}$  for  $-36\text{ }^\circ\text{C}$  to  $-78\text{ }^\circ\text{C}$ ).

976 Accordingly, the scaled  $RH_{ice}$  for a given  $n_s$ ,  $RH_{ice}(n_s)$ , is estimated as:

977

978 
$$RH_{ice,(n_s)} = \frac{RH_{ice,(n_s=7.5 \times 10^{10})} + c \cdot RH_{ice,(n_s)}}{c+1} \quad (S3)$$

979  
 980 As can be seen in Figure S3, the ratio of a and b (at -45 °C as an example) is set to be a constant  
 981 in order to scale the  $RH_{ice,(n_s)}$ . An ensemble of  $RH_{ice,(n_s)}$ -T is represented in Figure 4A.



982  
 983 **Figure S3.** An example of visualizing the relationship between uncorrected- and corrected  $RH_{ice}$  as a function of  $n_s$   
 984 at -45 °C.