

1 **A Comprehensive Parameterization of Heterogeneous Ice Nucleation of Dust Surrogate:**  
2 **Laboratory Study with Hematite Particles and Its Application to Atmospheric Models**

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## 32 Abstract

33

34 A new heterogeneous ice nucleation parameterization that covers a wide temperature  
35 range (-36 to -78 °C) is presented. Developing and testing such an ice nucleation  
36 parameterization, which is constrained through identical experimental conditions, is important to  
37 accurately simulate the ice nucleation processes in cirrus clouds. The ice nucleation active  
38 surface-site density ( $n_s$ ) of hematite particles, used as a proxy for atmospheric dust particles,  
39 were derived from AIDA (Aerosol Interaction and Dynamics in the Atmosphere) cloud chamber  
40 measurements under water subsaturated conditions. These conditions were achieved by  
41 continuously changing the temperature ( $T$ ) and relative humidity with respect to ice ( $\text{RH}_{\text{ice}}$ ) in the  
42 chamber. Our measurements showed several different pathways to nucleate ice depending on  $T$   
43 and  $\text{RH}_{\text{ice}}$  conditions. For instance, almost  $T$ -independent freezing was observed at  $-60\text{ °C} < T < -$   
44  $50\text{ °C}$ , where  $\text{RH}_{\text{ice}}$  explicitly controlled ice nucleation efficiency, while both  $T$  and  $\text{RH}_{\text{ice}}$  played  
45 roles in other two  $T$  regimes:  $-78\text{ °C} < T < -60\text{ °C}$  and  $-50\text{ °C} < T < -36\text{ °C}$ . More specifically,  
46 observations at  $T$  lower than  $-60\text{ °C}$  revealed that higher  $\text{RH}_{\text{ice}}$  was necessary to maintain a  
47 constant  $n_s$ , whereas  $T$  may have played a significant role in ice nucleation at  $T$  higher than  $-50$   
48  $\text{°C}$ . We implemented the new hematite-derived  $n_s$  parameterization, which agrees well with  
49 previous AIDA measurements of desert dust, into two conceptual cloud models to investigate  
50 their sensitivity to the new parameterization in comparison to existing ice nucleation schemes for  
51 simulating cirrus cloud properties. Our results show that the new AIDA-based parameterization  
52 leads to an order of magnitude higher ice crystal concentrations and to an inhibition of  
53 homogeneous nucleation in lower temperature regions. Our cloud simulation results suggest that  
54 atmospheric dust particles that form ice nuclei at lower temperatures, below  $-36\text{ °C}$ , can  
55 potentially have a stronger influence on cloud properties, such as cloud longevity and initiation,  
56 compared to previous parameterizations.

## 57 1. Introduction

58

59 Ice clouds represent a significant source of uncertainty when predicting the Earth's  
60 climate change according to the recent Intergovernmental Panel on Climate Change report (i.e.,  
61 *Chapter 7 of IPCC, 2013; Boucher et al., 2013*). Rare airborne particles that can act as ice  
62 nucleating particles (INPs) at supercooled temperatures indirectly influence the Earth's forcing  
63 by changing microphysical properties of ice clouds, such as reflectivity, longevity and  
64 precipitation. However, understanding ice cloud formation over a wide range of atmospherically  
65 relevant temperatures and humidity is challenging (e.g., *DeMott et al., 2011; Murray et al.,*  
66 *2012*), and our knowledge of ice formation through various nucleation modes is still scarce and  
67 limited, such that the ice nucleation processes are currently very poorly represented in global  
68 climate models (e.g., *Hoose et al., 2010; Liu and Penner, 2005*). In particular, heterogeneous ice  
69 nucleation processes proceed through various modes including deposition nucleation,  
70 immersion-, condensation- and contact freezing (*Chapter 9 of Pruppacher and Klett, 1997; Vali,*  
71 *1985*). Briefly, deposition mode induces ice formation when water vapor is directly deposited  
72 onto the INP, immersion and condensation freezing can induce ice formation when freezing is  
73 initiated by the INP immersed within the supercooled droplet or solution droplet, and contact  
74 freezing can initiate at the moment when an INP comes into contact with a supercooled droplet.

75 A global model simulation of INPs in tropospheric clouds showed that more than 85% of  
76 heterogeneous ice nucleation results from freezing of supercooled cloud droplets, in which INPs  
77 are either immersed or condensed (*Hoose et al., 2010*). However, freezing mechanisms in cirrus  
78 clouds are still uncertain (e.g., *Sassen and Khvorostyanov, 2008*). It is understood that various  
79 INPs can nucleate ice at water subsaturation and a range of supercooled temperature conditions  
80 as comprehensively illustrated in Fig. 2 of *Hoose and Möhler (2012)*. The potential importance  
81 of ice nucleation under ice supersaturated conditions below the homogeneous freezing threshold  
82 line (i.e., Koop line; *Koop et al., 2000; Ren and MacKenzie, 2005*) has already been proved in  
83 earlier studies, suggesting the need for further investigations in the water subsaturated region.  
84 For example, *Christenson (2013)* experimentally showed that the capillary condensation of  
85 supercooled liquid on surface defects facilitated subsequent homogeneous nucleation and growth  
86 of ice below water saturation. *Marcilli (2014)* suggested that the inverse Kelvin effect below  
87 water saturation helps to form water in pores or cavities and hypothesized that this condensate

88 could freeze through the homogeneous- or immersion mode freezing. This freezing mechanism  
89 was referred to as pore condensation and freezing. Previous laboratory studies introduced the  
90 concept of a freezing mechanism of solutions on particles at below water saturation (*Zuberi et al.*,  
91 2002; *Hung et al.*, 2003; *Archuleta et al.*, 2005). More recently, *Welti et al.* (2014) explored the  
92 relevance of soluble components of mineral dust (i.e., Fluka kaolinite) to condensation freezing  
93 below water saturation in the context of classical nucleation theory (CNT). Further, recent  
94 aircraft-based field observations suggested that predominant heterogeneous ice formation at  
95 cirrus temperatures occurs under water subsaturated conditions, in particular when  $RH_{ice}$  is  
96 below 140% (*Cziczo et al.*, 2013). In addition, *Storelvmo and Herger* (2014) demonstrated that  
97 forward modeling simulation with 50% of the mineral dust particles acting as INPs was in good  
98 agreement with an observation reported by *Cziczo et al.* (2013). Another airborne observation  
99 during an Asian mineral dust event suggested that ice nucleation in cirrus clouds occurs under  
100 water subsaturation conditions below 130%  $RH_{ice}$  (*Sakai et al.*, 2014).

101 Previously, empirical descriptions given in *Meyers et al.* (1992, hereinafter referred to as  
102 M92) were derived from the limited field measurements of ice nuclei concentrations measured at  
103  $-23\text{ }^{\circ}\text{C} < T < -7\text{ }^{\circ}\text{C}$  and  $102\% < RH_{ice} < 125\%$ . Recently, *Phillips et al.* (2008, 2013) empirically  
104 parameterized the heterogeneous ice nucleation of various types of aerosols as a function of  
105 humidity ( $RH_{ice} > 100\%$ ) and temperature conditions (0 to  $-100\text{ }^{\circ}\text{C}$ ). Besides, CNT-based ice  
106 nucleation descriptions have also been widely used and implemented in cloud models (e.g.,  
107 *Barahona and Nenes*, 2009a and 2009b; *Kärcher and Lohmann*, 2003; *Khvorostyanov and Curry*,  
108 2004). These parameterizations can predict different cloud properties for identical environmental  
109 conditions. For example, *Barahona et al.* (2010) showed that the ice crystal number can vary by  
110 up to an order of magnitude in a global chemical transport model depending on the choice of the  
111 heterogeneous ice nucleation parameterization. The authors found the lowest global mean ice  
112 crystal concentration from the parameterization of *Phillips et al.* (2008). Moreover, sensitivity of  
113 ice cloud properties to the parameterization was observed by *Liu et al.* (2012). They showed that  
114 the heterogeneous INP number concentration obtained from a CNT-based parameterization is  
115 typically higher by several factors than that of Phillips's parameterization under identical test  
116 conditions. To gain insight on what triggers such deviation and to constrain model uncertainties,  
117 more and better in situ measurements are necessary (*Cziczo and Froyd*, 2014). In specific,  
118 identifying and quantifying sources, global spatio-temporal distribution and mixing-state of INPs

119 might support to reduce model assumptions. In parallel, systematic laboratory measurements are  
120 indeed needed to develop water subsaturated ice nucleation parameterizations for the range of  
121 atmospherically relevant  $T$ -RH<sub>ice</sub> conditions for a better representation of ice nucleation  
122 processes in cloud models and to support in situ measurements.

123         Recently, *Hoose and Möhler* (2012) compiled previously reported aerosol-specific  
124 heterogeneous freezing efficiencies from laboratory experiments based on a single-parameter,  $n_s$   
125 (e.g., *Niemand et al.*, 2012; *Connolly et al.*, 2009). In addition, the authors formulated ice  
126 nucleation efficiency by evaluating aerosol-specific “singular” freezing onsets when or after  
127 specific ambient conditions were met. Such time-independent and surface area-scaled  $n_s$   
128 formulations can be further adapted to comprehensively assess the ice nucleation in a wide range  
129 of atmospherically relevant  $T$ -RH<sub>ice</sub> conditions. Accordingly, the  $n_s$  concept was adapted to  
130 deposition nucleation at low temperatures (up to -80 °C).

131         Within the framework of Ice Nucleation research UnIT (INUIT), we comprehensively  
132 investigated the ice nucleation efficiency of pristine cubic hematite particles as a model proxy for  
133 atmospheric dust particles. Hematite is used as an example of atmospheric mineral dust particles,  
134 which can also be found in the form of cloud-borne particles in shallow stratocumulus clouds  
135 (*Matsuki et al.*, 2010). Natural hematite often exists in supermicron-sized silt particles and  
136 accounts for a few percent of the total dust particle mass (*Claquin et al.*, 1999). Ice nucleation  
137 efficiencies of cubic hematite particles were measured using the AIDA cloud chamber. We also  
138 re-examined the previously reported AIDA results of hematite ice nucleation (*Hiranuma et al.*,  
139 2014; *Skrotzki et al.*, 2013) and combined them with the results from this work in order to  
140 examine the ice nucleation efficiency of hematite particles in the temperature range between -36  
141 and -78 °C. In addition to developing the new dust parameterization from these AIDA  
142 measurements (Sects. 3.1-3.3), the fitted  $n_s$  parameterization was also applied to atmospheric  
143 modeling simulations (Sect. 3.4). We implemented the parameterization in the Single column  
144 version of the Community Atmospheric Model version 5 (SCAM5, *Neale et al.*, 2010) and the  
145 COnsortium for Small-scale Modeling (COSMO, *Baldauf et al.*, 2011; *Doms et al.*, 2011)  
146 models to assess the newly developed parameterization and compare them with existing  
147 parameterizations. It is important to note that the purpose of the current study is to perform a  
148 conceptual study with laboratory-synthesized hematite particles as a model aerosol for deposition

149 ice nucleation, over a wide range of  $T$  and  $RH_{ice}$ , but not to quantify how much hematite content  
150 contributes to ice formation in cirrus clouds.

151 **2. Method**

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153 **2.1. Description of hematite particles**

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155 Laboratory-generated cubic hematite particles that have homogeneous chemico-physical  
156 properties were used as a proxy for atmospheric dust particles. These particles had a uniform  
157 composition, morphology and well-defined surface area. Hence, they are suited well for  
158 investigating  $T$ - $\text{RH}_{\text{ice}}$ -dependent ice nucleation efficiency and relating it to the surface area  
159 (*Hiranuma et al.*, 2014). Detailed information on the manufacturing process of cubic hematite  
160 particles is available elsewhere (*Sugimoto and Sakata*, 1992). Three different sizes of quasi-  
161 monodispersed hematite particles (~200, ~500 and ~1000 nm diameter, respectively) were used  
162 in this work. The morphology and size of the hematite particles were characterized by scanning  
163 electron microscopy and determined based on an equivalent circle diameter derived from the  
164 observed 2D particle projection area (*Vragel*, 2009; *Hiranuma et al.*, 2014). A Small-Scale  
165 Powder Disperser (SSPD, TSI, Model 3433) was used to dry-disperse the quasi-monodispersed  
166 hematite particles into the AIDA vessel as demonstrated in *Skrotzki et al.* (2013).

167

168 **2.2. AIDA cooling expansion**

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170 The AIDA expansion freezing experiments were achieved by mechanical pumping  
171 (*Möhler et al.*, 2003). Mechanical pumps can be operated at different pumping speeds simulating  
172 atmospherically relevant adiabatic cooling of rising air parcels in the cylinder of 84 m<sup>3</sup> in volume  
173 (i.e., 7 m height x 4 m width thermally conductive aluminum vessel) installed inside the  
174 thermostatic housing. For this study, a cooling rate of 5 °C min<sup>-1</sup> was typically applied at the  
175 beginning. Then, the cooling rate decreased to <0.1 °C min<sup>-1</sup> within 400 s for each pumping  
176 expansion experiment, which was mainly due to an increasing heat flux from the chamber walls.  
177 Afterwards, an almost constant temperature was maintained by the stirred and well-mixed  
178 volume of the cold chamber. During the experiment, the pressure in the vessel decreased from  
179 1000 to 800 mb.

180 The mean gas temperature in the AIDA vessel was determined by five thermocouples  
181 installed at different vertical levels. The sensors of these thermocouples were located about 1 m

182 off the vessel wall and, thus, fully exposed to the chamber air. Stirring of the air by the  
183 mechanical ventilator prior to and during pumping ensured a homogeneous temperature  
184 distribution in the vessel of  $\pm 0.3$  °C (Möhler *et al.*, 2003). The relative humidities with respect  
185 to water ( $RH_{\text{water}}$ ) and  $RH_{\text{ice}}$  were determined with an accuracy of  $\pm 5\%$  using the mean gas  
186 temperature and the mean water vapor concentration. The water vapor concentrations were  
187 measured in situ by tunable diode laser (TDL) water vapor absorption spectroscopy throughout  
188 the expansion experiments. Since this direct long path absorption technique is described and  
189 evaluated in detail in other publications (Fahey *et al.*, 2014; Skrotzki *et al.*, 2013), no further  
190 information is given here.

191 Under atmospheric pressure, prior to each expansion experiment, a combination of a  
192 Scanning Mobility Particle Sizer (SMPS, TSI, Model 3080 DMA and Model 3010 condensation  
193 particle counter), an Aerosol Particle Sizer (APS, TSI, Model 3321) and a condensation particle  
194 counter (CPC, TSI, Model 3076) collectively measured the total number and size distribution of  
195 aerosols at the horizontally extended outlet of the AIDA chamber. Subsequently, the total aerosol  
196 surface area was estimated as presented in Hiranuma *et al.* (2014). During expansion, we  
197 quantified the ice nucleation of hematite particles with two different light scattering instruments:  
198 an optical particle counter welas (PALAS, Sensor series 2300 and 2500) (Benz *et al.*, 2005) and  
199 SIMONE (German acronym of Streulicht-intensitätsmessungen zum optischen Nachweis von  
200 Eispartikeln, which translates to the scattering intensity measurement for the optical detection of  
201 ice; Schnaiter *et al.*, 2012). More details on the application of this specific combination of two  
202 instruments for the AIDA ice nucleation experiments are given in Hiranuma *et al.* (2014).

203

### 204 **2.3. Ice nucleation parameterization and modeling**

205

206 The size-independent singular ice nucleation efficiency,  $n_s$ , was calculated by  
207 normalizing the observed AIDA ice crystal concentration ( $N_{\text{ice}}$ ) to the total surface area of  
208 aerosols, which can be calculated by multiplying the surface area of an individual particle ( $S_i$ ) by  
209 the total number concentration of aerosols ( $N_{\text{ae}}$ ) (e.g., Niemand *et al.*, 2012; Hoose and Möhler,  
210 2012). For size-selected hematite particles, this linear approximation (i.e.,  $n_s = (-\ln(1-\alpha))/S_i \sim$   
211  $\alpha/S_i$ ) was valid independent of the ice active number fraction ( $\alpha = N_{\text{ice}}/N_{\text{ae}}$ ). An overestimation of  
212 ice due to the use of linear approximation only amounted up to about a factor of three at  $n_s \leq 10^{12}$



213  $\text{m}^{-2}$ . Subsequently, the  $n_s$  values estimated for the wide range of experimental conditions ( $-36\text{ }^\circ\text{C}$   
214  $< T < -78\text{ }^\circ\text{C}$  and  $100\% < \text{RH}_{\text{ice}} < \text{water saturation}$ ) were used to depict and fit constant  $n_s$  contour  
215 lines. Here, these lines are referred to as the  $n_s$ -isolines or simply as the isolines.

216 The isoline-based parameterizations were derived (see section 3.3) and then implemented  
217 in two atmospheric models (a single-column version of a global scale model and a convection  
218 resolving model, see Sect 2.3.1. and 2.3.2. for model descriptions). The unique advantages of the  
219 use of both models in this study are (1) to demonstrate that our AIDA  $n_s$ -based parameterization  
220 can be directly applied on different scales of atmospheric models and (2) to estimate the number  
221 of ice crystals simulated in two different atmospheric scenarios that complement each other and  
222 cover a wide range of atmospheric temperature and saturation conditions (ice formation at higher  
223  $\text{RH}_{\text{ice}}$ , up to  $\sim 180\%$ , and lower  $T$ , down to  $\sim -70\text{ }^\circ\text{C}$ ). More specifically, the former represents a  
224 finely resolved parameterization-oriented model embedded in the global model while the latter is  
225 a more physically based high-resolution grid scale model, typically used to analyze small scale  
226 complex systems for a fundamental understanding of ice formation. Altogether, results from two  
227 independent models were examined for a detailed modeling of atmospheric ice formation on all  
228 scales.

229 The mean size and surface area of hematite particles were prescribed with an assumption  
230 that either these particles are spherical and have a mean particle diameter of 1000 nm or the size  
231 of these particles follows a lognormal distribution, with a mean volume-equivalent diameter of  
232  $\sim 1000\text{ nm}$  ( $\sigma_g = 1.05$ ), which is consistent with the AIDA experiments described earlier  
233 (*Hiranuma et al.*, 2014). The cloud microphysical sensitivity of these two size treatments was  
234 characterized. In addition, sensitivity simulations of two lower boundaries of  $\text{RH}_{\text{ice}}$  (i.e., 100 vs.  
235 105%) were also carried out. This sensitivity analysis was specifically useful to examine  
236 uncertainty involved in the TDL measurement ( $\text{RH}_{\text{ice}} \pm 5\%$ ) concerning the condensed  $n_s$  spacing  
237 (up to several orders of magnitude) in a narrow  $\text{RH}_{\text{ice}}$  range and a certain  $T$  region. In both  
238 models, hematite particle number concentrations are given to be  $200\text{ L}^{-1}$ , which is about the  
239 average dust concentration simulated by the SCAM5 model over the Southern Great Plain (SGP)  
240 site in springtime. Since the  $n_s$ -isoline parameterization tested in this study is applicable at  $T$   
241 below  $-36\text{ }^\circ\text{C}$ , an additional parameterization was used to simulate ice formation of background  
242 particles at  $T > -36\text{ }^\circ\text{C}$ , namely, the aerosol-independent M92 scheme. These parameterizations  
243 were combined to ensure more atmospherically relevant processes and conditions (e.g.,

244 distributions of water vapor) when compared to the application of the  $n_s$ -isoline parameterization  
245 alone.

246 To better understand to what an extent the AIDA  $n_s$ -based parameterization differs from  
247 other parameterizations commonly used in atmospheric models, the existing empirical  
248 parameterization of heterogeneous ice nucleation by *Phillips et al.* (2013, hereinafter denoted as  
249 P13) was implemented as well. The P13 scheme reflects the aerosol specific ice nucleation. In  
250 particular, the contribution of mineral dust with the background troposphere baseline surface  
251 area mixing ratio of ice-active mineral dust particles ( $=2.0 \times 10^{-6} \text{ m}^2\text{kg}^{-1}$ ) was considered in this  
252 study. Ice formation occurring below water saturation only was considered and, thus, Eqn. 1 in  
253 *Phillips et al.* (2008) was used for parameterizing ice nucleation.

254

### 255 2.3.1. SCAM5

256

257 Single column models are widely used to test physical parameterizations for use in the  
258 general circulation model (GCM). The model has 30 vertical levels, and the model time step is  
259 set to 10 min. The single column model resembles a single column of a GCM and can be derived  
260 from observations or model output. The complex feedbacks between the simulated column and  
261 other columns due to large-scale dynamics are not considered. Therefore, the single column  
262 model is an ideal tool for testing ice cloud parameterizations. The SCAM5 model was modified  
263 to incorporate the new parameterization developed in this study. The *Barahona and Nenes* (2008,  
264 2009a, b) scheme, which provides an analytical solution of the cloud parcel model equations  
265 (hereinafter called BN scheme), is used for calculating ice nucleation in cirrus clouds. The new  
266 AIDA  $n_s$ -isoline-based parameterizations as well as the P13 scheme were implemented in the  
267 model. The simulation was performed for one month (April 2010) at the United States  
268 Department of Energy's Atmospheric Radiation Measurement facility located at the SGP site  
269 (*Hiranuma et al.*, 2014).

270

### 271 2.3.2. COSMO

272

273 The non-hydrostatic weather forecast model, COSMO, was adapted to systematically  
274 investigate the impact of hematite particles under the simulated upper tropospheric conditions.

275 COSMO is the high-resolution limited-area model to assess clouds and convection at a  
276 horizontal spatial resolution of 2.8 km with 50 layers of stretched vertical grids. The time step is  
277 set to 20 seconds. In this study, we simulated a period of two days (July 23 to July 25, 2011) on a  
278 domain of 450 x 450 horizontal grid points centered over the German Alps (longitude: 0.1°E to  
279 18.7°E, latitude: 41.7°N to 53.2°N). The initial and boundary conditions were provided by the  
280 European Centre for Medium-Range Weather Forecasts. They are available at the  
281 Meteorological Archival and Retrieval System. In order to account for the spatio-temporal  
282 evolution of mass and number densities of six hydrometeor classes (i.e., cloud droplets,  
283 raindrops, cloud ice, snow, graupel and hail), the two-moment bulk microphysics scheme was  
284 incorporated in our COSMO model version following the method described by *Seifert and*  
285 *Beheng* (2006) and *Seifert et al.* (2012). Apart from the AIDA isoline-based freezing  
286 parameterization of hematite, two other ice nucleation modes, namely, M92 and homogeneous  
287 nucleation of cloud or solution droplets (*Kärcher et al.*, 2006; *Ren and MacKenzie*, 2005), were  
288 considered in our COSMO simulations. The latter was used to parameterize the competition of  
289 water vapor between homogeneous and heterogeneous freezing.

290

## 291 3. Results

292

### 293 3.1. AIDA ice nucleation experiments

294

295 A series of AIDA experiments was carried out during the INUIT01 and INUIT04  
296 campaigns to investigate the ice nucleation efficiency of well-characterized hematite particles  
297 under water subsaturated conditions at  $-47\text{ }^\circ\text{C} < T$ . In addition, we used the AIDA results  
298 reported by *Skrotzki et al.* (2013) and reconciled them with the  $n_s$  values in order to parameterize  
299 the overall ice nucleation efficiency of hematite particles up to  $-78\text{ }^\circ\text{C}$ . In total, 12 expansion  
300 experiments, 4 from the INUIT campaigns and 8 from *Skrotzki et al.* (2013), were studied.  
301 Detailed experimental conditions and aerosol properties for these expansion experiments are  
302 summarized in Table 1. The use of different sizes of hematite particles in different temperature  
303 regions was justified by calculating the size-independent  $n_s$  values of 200 and 1000 nm diameter  
304 particles at  $\sim -40\text{ }^\circ\text{C}$ . For instance, the evaluated  $n_s$  values ( $10^{10}\text{ m}^{-2}$ ) for these two sizes agreed  
305 very well within  $\pm 1\%$   $\text{RH}_{\text{ice}}$  and  $\pm 0.3\text{ }^\circ\text{C}$  of chamber conditions (see corresponding  $\text{RH}_{\text{ice}}$  and  $T$   
306 at Evaluated  $n_s$  in Table 1 for INUIT04\_08, 1000 nm, HALO06\_19, 200 nm, and HALO06\_20,  
307 200 nm). This agreement verified the reproducibility of the AIDA chamber experiments, ice  
308 nucleation efficiency of hematite particles and size-independence of the  $n_s$  calculations. The  
309 advantage of using 1000 nm diameter hematite particles was that, due to their comparatively  
310 larger surface area, they were efficient in forming ice in cooling expansion experiments at  $-40$   
311  $^\circ\text{C} < T < -36\text{ }^\circ\text{C}$  (*Hiranuma et al.*, 2014).

312 The temporal profiles of deposition nucleation experiments from HALO campaigns,  
313 including  $N_{\text{ice}}$ , gas  $T$ ,  $\text{RH}_{\text{ice}}$  and  $\text{RH}_{\text{water}}$  measured by the TDL as well as the polarized light  
314 scattering properties in near-backscattering direction measured by SIMONE, are shown in Figure  
315 1. The depolarization ratio, which is sensitive to ice particle nucleation and growth, can be  
316 deduced from the latter. During a typical expansion, the air mass in the vessel experiences  
317 continuous cooling (for up to 500 s) and an increase in relative humidity (for up to 200 s, Fig. 1  
318 panel i and ii). Figure 1 panel iii shows the temporal plot of the depolarization ratio. At the  
319 beginning of the expansion, the depolarization ratio increases because ice is nucleating on the  
320 hematite particles. Conversely, repartitioning of gas phase water to ice phase water due to  
321 growing ice crystals triggers the declines in both depolarization ratio (i.e., sizing effect,

322 *Schnaiter et al.*, 2012) and RH, usually after 100 s. The time-delay in our wet ice detection  
323 (typically 1  $\mu\text{m}$  is the minimum ice detection diameter for 200 and 500 nm diameter hematite  
324 particles) due to slower depositional growth after ice nucleation at lower  $T$  is accounted for in  
325 our error analyses (Figure 2). We evaluated only up to several hundred seconds of each  
326 expansion experiment as the ice nucleating period. Similar experimental profiles for INUIT  
327 campaigns are presented in Figure S1.

328 The initial  $n_s$ -isoline curves in the  $T$ -RH<sub>ice</sub> space are illustrated in Figure 2. Constant  $n_s$ -  
329 isoline curves are obtained by fitting second degree polynomial fit equations to the constant  $n_s$   
330 magnitudes calculated at various  $T$  and RH<sub>ice</sub> (see the supplement for more details). Previous  
331 AIDA results of two immersion freezing experiments (i.e., INUIT04\_13 and INUIT01\_28 from  
332 *Hiranuma et al.*, 2014) are also shown on the water saturation line and used to constrain the  
333 fitted curves because immersion freezing is considered part of isolines. Since the  $n_s$  values  
334 presented in Fig. 3 of *Hiranuma et al.* (2014) only extends up to  $\sim 10^9 \text{ m}^{-2}$ , the data points of  
335 higher  $n_s$  values were extrapolated based on the observed values from two measurements. Figure  
336 2 shows several important features of  $n_s$ -isoline curves. First, below  $-60 \text{ }^\circ\text{C}$ ,  $n_s$ -isolines showed  
337 an increase in RH<sub>ice</sub> required to maintain a constant  $n_s$  (i.e.,  $n_s > 2.5 \times 10^8 \text{ m}^{-2}$ ) with decreasing  $T$   
338 (i.e., RH<sub>ice</sub>-dependent ice nucleation regime). For example, at a RH<sub>ice</sub> = 120% and  $T = -75 \text{ }^\circ\text{C}$ ,  
339 cooling by 1  $^\circ\text{C}$  corresponds to a 10% decrease in  $n_s$ . This observation is interesting because the  
340 increase in RH<sub>ice</sub> required to maintain constant  $n_s$  values is consistent with the CNT for  
341 deposition nucleation (Eqn. A11 in *Hoose and Möhler*, 2012). Second, the highest sensitivity of  
342 RH<sub>ice</sub> is observed in a region where  $n_s$ -isolines are perpendicular to temperature-isolines ( $\sim -60 \text{ }^\circ\text{C}$   
343  $< T < \sim -50 \text{ }^\circ\text{C}$ ). Here,  $n_s$  is almost independent of  $T$ , and solely dependent on RH<sub>ice</sub>. Finally, we  
344 observed strong  $T$ -dependent nucleation near water saturation (i.e., while cooling along the water  
345 saturation line towards  $\sim -50 \text{ }^\circ\text{C}$ ). At a constant RH<sub>ice</sub> (e.g., 114%), for example, cooling by 1  $^\circ\text{C}$   
346 from  $-41$  to  $-42 \text{ }^\circ\text{C}$  corresponds to an increase in  $n_s$  of approximately half an order of magnitude  
347 (see inset of Fig. 2). This suggests that the  $n_s$  values depend on temperature. Interestingly, we  
348 observed a continuous increase in  $n_s$  during cooling even after the depletion of supersaturation  
349 below  $-40 \text{ }^\circ\text{C}$  (Figure S2). CNT does not explain this predominant  $T$  contribution near water  
350 saturation (Fig. A1 in *Hoose and Möhler*, 2012). Therefore, other microphysical processes at the  
351 particle surface and/or perhaps even within the bulk phase may be responsible for this  $T$ -  
352 dependent behavior and these results appear to support the existence of a pore or surface freezing

353 process, as discussed in recent literature (e.g., *Marcilli*, 2014). In particular, we suspect that  
354 water condensation on the particle surface plays an important role on subsequent freezing. To  
355 support this, the surfaces of our hematite particles are not perfectly smooth and contain some  
356 active sites (e.g., pores and steps, *Hiranuma et al.*, 2014). Moreover, water vapor may preferably  
357 fill the surface cavities due to the reduced saturation pressure in pores or at steps because of  
358 negative curvature Kelvin effects (*Marcilli*, 2014), thus leading to namely “surface condensation  
359 freezing (SCF)”. As described in previously published literatures (*Christenson*, 2013; *Marcilli*,  
360 2014), SCF may be of relevance to homogeneous nucleation (i.e., spontaneous ice nucleation in  
361 supercooled aerosol) at relevant  $T (< -36 \text{ }^\circ\text{C})$  and/or immersion mode freezing under water  
362 subsaturated conditions. Thus, SCF may arise from both homogeneous and heterogeneous  
363 nucleation.

364

### 365 **3.2. Comparison with previous studies**

366

367 The  $n_s$ -isolines of hematite particles were compared to previous measurements made  
368 using different aerosol species. This comparison was performed to (1) confirm that our  $n_s$  fit  
369 reproduces the overall trend shown by previous studies under certain  $T$ -RH<sub>ice</sub> conditions and (2)  
370 to demonstrate that the parameterization with laboratory-synthesized hematite particles  
371 quantitatively represents ice nucleation properties of atmospheric dust particles.

372 Comparison of the hematite  $n_s$ -isolines to previous deposition freezing observations are  
373 shown in Figure 3. More specifically, previous measurements were performed with natural  
374 Saharan desert dust (SD2, *Möhler et al.*, 2006), reference Arizona test dust (ATD, *Möhler et al.*,  
375 2006; *Welti et al.*, 2009), volcanic ash (*Steinke et al.*, 2011), soot (*Möhler et al.*, 2005), clay  
376 minerals (*Welti et al.*, 2009; *Koehler et al.*, 2010) and organics (*Shilling et al.*, 2006; *Wang and*  
377 *Knopf*, 2011). These previous experimental studies used various types of ice nucleation  
378 instruments, such as substrate-supported cold stages coupled with an optical microscope (*Shilling*  
379 *et al.*, 2006; *Wang and Knopf*, 2011), portable ice nuclei counters (*Koehler et al.*, 2010; *Welti et*  
380 *al.*, 2009) and the AIDA cloud simulation chamber (*Möhler et al.*, 2005; *Möhler et al.*, 2006;  
381 *Steinke et al.*, 2011). They revealed the importance of both RH<sub>ice</sub> and temperature onto  
382 deposition mode ice nucleation of specific particle compositions. In Fig. 3a, previous AIDA  
383 results for dusts, ash and soot, are presented. Specifically, we utilized the  $T$ -RH<sub>ice</sub> data at  $\alpha =$

384 0.08 of SD2 and ATD reported in the previous AIDA study (Möhler *et al.*, 2006) to define  
385 isolines. It is noteworthy that an  $\alpha$  of 0.08 corresponds to  $\sim 10^{11} \text{ m}^{-2}$  in  $n_s$  when assuming  
386 uniform distributions of spherical particles of 0.5  $\mu\text{m}$  diameter ( $n_s = (-\ln(1-\alpha))/(\pi(0.5 \times 10^{-6})^2)$ ),  
387 which is in good agreement with the  $10^{11} \text{ m}^{-2}$   $n_s$ -isoline of hematite particles. For volcanic ash,  
388 we adapted  $n_s$  values ( $10^9$ ,  $5 \times 10^9$  and  $10^{10} \text{ m}^{-2}$ ) originally reported in Steinke *et al.*, (2011).  
389 Möhler *et al.* (2005) found that the ice nucleation of soot starts at the initial increase in polarized  
390 light scattering intensity in near-backscattering direction at 488 nm ( $n_s$  values are inaccessible).  
391 Except for these AIDA studies, other isolines in Fig. 3b and c were defined based on the reported  
392 ice nucleation measurements. For instance, Koehler *et al.* (2010) studied the deposition mode  
393 nucleation of size-selected (i.e., 200 nm, 300 nm, 400 nm) natural dusts, and reported ice  
394 nucleation conditions ( $T$  and  $\text{RH}_{\text{ice}}$ ) of ATD at  $\alpha = 0.01$  and of Canary Island Dust and Saharan  
395 Dust at  $\alpha = 0.05$ . Welti *et al.* (2009) also studied the deposition nucleation abilities of size-  
396 segregated mineral dusts (i.e., 100 to 800 nm diameter of ATD, illite, kaolinite and  
397 montmorillonite) based on  $\alpha = 0.01$ . Shilling *et al.* (2006) reported the ice nucleation onsets of  
398 ammonium sulfate and maleic acid detected by the decreasing partial pressure of water with  
399 FTIR-reflection absorption spectroscopy (e.g., 1 in  $10^5$  nucleation at about  $-33 \text{ }^\circ\text{C}$  for a spherical  
400 particle size of 1 to 10  $\mu\text{m}$  diameter). Wang and Knopf. (2011) investigated deposition freezing  
401 of various mineral and organic particles including kaolinite, Suwannee River standard fulvic acid  
402 and Leonardite standard humic acid particles. The authors reported the mean size of particles and  
403 associated ice-activated fractions at the given  $T$ - $\text{RH}_{\text{ice}}$ .

404 As seen in Fig. 3, the results from previous studies suggest the necessity of increasing  
405  $\text{RH}_{\text{ice}}$  to maintain a constant  $n_s$  value below  $T \sim -55^\circ\text{C}$ . They also indicate that nucleation may be  
406 triggered by SCF in the region where data and isolines approach water saturation where  
407 temperature plays a significant role on ice nucleation. It can also be observed that the contour of  
408 our new  $n_s$ -isoline parameterization of cubic hematite particles in  $T$ - $\text{RH}_{\text{ice}}$  coordinates generally  
409 agrees with the onsets determined by previous studies of other atmospherically relevant aerosols.  
410 In particular, the  $n_s$ -isolines estimated from ATD and SD2 ( $\sim 10^{11} \text{ m}^{-2}$ , Fig. 3a), which reasonably  
411 agree with the hematite  $n_s$ -isoline, suggest that atmospheric dust may have similar deposition  
412 mode ice nucleation efficiency.

413

### 414 3.3. $n_s$ -isoline-based parameterizations

415

416 Next, the ice nucleation efficiency of hematite particles was parameterized over a wide  
417 range of  $T$ - $RH_{ice}$ . Three types of parametrical descriptions used in this study are shown in Figure  
418 4. First, based on the AIDA experimental results, a series of constant  $n_s$  curves was interpolated  
419 to produce isolines in the range of  $10^6 \text{ m}^{-2} < n_s < 10^{12} \text{ m}^{-2}$  (Fig. 4a). The lower bound of  $n_s$  value  
420 ( $10^6 \text{ m}^{-2}$ ) was set based on the minimum  $n_s$  observed during AIDA expansions. Since the certain  
421 regions of  $n_s$ -isolines (i.e.,  $n_s < 7.5 \times 10^{10} \text{ m}^{-2}$ ; blue lines in Fig. 2) can submerge below ice  
422 saturation, the correction was applied to shift them and maintain all isolines above 100%  $RH_{ice}$ .  
423 The procedure to constrain  $n_s$  to  $>100\% RH_{ice}$  is described in the supplement (Fig. S3). Above  
424 the upper bound of  $10^{12} \text{ m}^{-2}$ ,  $n_s$  presumably remains constant up to the water saturation line in  
425 the  $T$ - $RH_{ice}$  space (no experimental data is available in this range). This assumption is valid in  
426 the present study because this  $n_s$  upper limit was hardly reached in our modeling case. However,  
427 more cloud simulation chamber measurements and data points for  $n_s \gg 10^{12} \text{ m}^{-2}$  are required to  
428 correctly constrain the  $n_s$  upper limit. It also has to be noted that the modeled ice crystal number  
429 concentration ( $\text{L}^{-1}$ ) derived from ice nucleation of hematite in this study is approximated by  
430 multiplying  $n_s$  by a simulated total surface of hematite ( $6.3 \times 10^{-10} \text{ m}^2 \text{ L}^{-1}$ ).

431 In the second fit approach (Fig. 4b), the interpolated  $n_s$  values were used to formulate the  
432  $n_s$ -isoline with a third degree-polynomial fit as a function of  $T$  ( $^{\circ}\text{C}$ ) and  $RH_{ice}$  (%) as

433

$$\begin{aligned} n_s^{3d}(T, RH_{ice}) = & -3.777 \times 10^{13} - 7.818 \times 10^{11} \cdot T + 4.252 \times 10^{11} \cdot RH_{ice} - 4.598 \\ & \times 10^9 \cdot T^2 + 6.952 \times 10^9 \cdot T \cdot RH_{ice} - 1.111 \times 10^9 \cdot RH_{ice}^2 - 2.966 \times 10^6 \cdot T^3 \\ & + 2.135 \times 10^7 \cdot T^2 \cdot RH_{ice} - 1.729 \times 10^7 \cdot T \cdot RH_{ice}^2 - 9.438 \times 10^5 \cdot RH_{ice}^3 \\ & \text{for } -78 \text{ }^{\circ}\text{C} < T < -36 \text{ }^{\circ}\text{C} \text{ and } 100 \% < RH_{ice} < \text{water saturation} \end{aligned} \quad (1)$$

434

435

436 where  $n_s^{3d}(T, RH_{ice})$  is the  $n_s$  derived from the third degree fit. The resulting spatial plot of  
437 isolines for constant  $n_s$  is shown in Fig. 4b. Note that the upper temperature boundary of  $-36 \text{ }^{\circ}\text{C}$   
438 was assigned as the interface between immersion mode- and deposition mode ice nucleation  
439 (*Hiranuma et al.*, 2014), and the lower boundary of  $-78 \text{ }^{\circ}\text{C}$  is the limit introduced by  
440 interpolating the hematite-isoline curves. The third approach (Fig. 4c) consisted in applying the  
441 equivalent  $n_s$  for deposition nucleation of hematite particles parameterized using the method  
442 introduced by *Phillips et al.* (2008 and 2013). In detail, we characterized the nucleation activity



443 solely of mineral dust through the deposition mode by adapting the Equation (1) from *Phillips et*  
444 *al.* (2008), which accounts for nucleation under water subsaturated conditions, and excluded the  
445 contribution at water saturation, i.e., Equation (2) of *Phillips et al.* (2008). AIDA  $n_s$ -isoline-  
446 based parameterization suggests strong supersaturation dependence of  $n_s$  at low  $T$ . Observed  
447 diversity between a new parameterization (Figs. 4a and 4b) and P13 (Fig. 4c) may result in  
448 different ice crystal forming propensities and may predict different cloud properties. The  
449 potential consequence of observed diversity is demonstrated using conceptual models and  
450 discussed in the following section.

451

### 452 3.4. *Model simulations*

453

454 The SCAM5 results for monthly mean profiles of the simulated in-cloud  $N_{ice}$  ( $N_i \sim N_{ice}$ )  
455 over the ARM SGP site for five cases are shown in Figure 5. These include (Case 1) the pure  
456 homogeneous ice nucleation case, (Case 2-4) cases with contributions from both homogeneous  
457 and heterogeneous ice nucleation (hereinafter referred to as the combined case) described in Fig.  
458 4a-c (corresponding to Simulations A, B and C) and (Case 5) the simulation of the different  
459 lower boundaries of  $RH_{ice}$  ( $RH_i^*$ , Simulation D). In addition, the observed profile of ice crystal  
460 number concentrations is also shown in comparison to the simulations in Fig. 5. The  
461 observational data were collected over the SGP site on eight days of April 2010 during the Small  
462 PARTicles In Cirrus (SPARTICUS) campaign (*Zhang et al.*, 2013). The results of our  
463 simulations suggests that ice crystal formation due to heterogeneous ice nucleation processes  
464 inhibits homogeneous ice nucleation and significantly reduces the ice number concentrations for  
465 the AIDA parameterizations (Fig. 4a and b). In contrast, due to the much smaller ice crystal  
466 production from P13, as shown by the pure heterogeneous case in Figure 5, homogeneous ice  
467 nucleation in the P13 case (Fig. 4c) is less affected by heterogeneous nucleation. The observed  
468 mean profile of in-cloud ice crystal number concentrations is in agreement with the simulated  
469 ones. The differences between the three parameterizations derived from AIDA measurements,  
470 corresponding to Simulations A, B and D, are small for both the combined case and the pure  
471 heterogeneous ice nucleation case as presented in Fig. 6. This is because the BN scheme used in  
472 SCAM5 is based on parcel model theory and uses the predicted maximum ice supersaturation  
473 ( $S_{max}$ ) to calculate deposition ice nucleation rates.  $S_{max}$  is determined by assuming that the

474 supersaturation will reach its maximum where the depletion of water vapor compensates the  
475 supersaturation increase from cooling in a cloud parcel (i.e., BN scheme). The three  
476 parameterizations (i.e., Simulations A, B and D) have largest differences when  $RH_{ice}$  is below  
477 120% while  $S_{max}$  calculated in the model is often larger than 115%. This also explains the low  
478 sensitivity of  $N_{ice}$  to the lower bound of the onset  $RH_{ice}$  value (Figs. 5 and 6). We also  
479 investigated the impact of different particle size distributions on the calculation (not shown). The  
480 impact is small and negligible. The negligible sensitivity to the choice of AIDA  
481 parameterizations in SCAM5 simulations (Simulation A and B of Figs. 5 and 6) as well as the  
482 negligible sensitivity to the lower bound of the  $RH_{ice}$  value for ice nucleation,  $RH_i^*$  in Figs. 5 and  
483 6, reflect the limitation of SCAM5 as a large-scale model, which can't explicitly resolve the sub-  
484 grid (for the GCM grid box) variability of the supersaturation.

485         The results of the COSMO model for the vertical profiles of  $N_{ice}$  (presumably equivalent  
486 to the heterogeneous INP number concentration) are summarized in Figure 7. These results  
487 simulate the three different parameterization schemes (corresponding to Fig. 4a-c) in  
488 combination with homogeneous freezing.  $N_{ice}$  was spatially averaged over all areas of the model  
489 domain which in principle allow for deposition nucleation in our simulations, i.e. conditions  
490 below  $-36^\circ\text{C}$  and above 100%  $RH_{ice}$ . Because not always  $n_s$  is larger than zero (white areas of  
491 Fig. 2), also areas without ice formation are contained. It is also noteworthy that only purely  
492 heterogeneous ice formation is presented rather than the total ice occurring in the model. As  
493 shown in Fig. 7, the mean  $N_{ice}$  resulting from the parameterization based on P13 is smaller than  
494 that obtained from the AIDA  $n_s$ -isoline-based parameterization by more than two orders of  
495 magnitude. This large difference results predominantly from the inactivity of P13 at low  $RH_{ice}$ .  
496 Unlike the SCAM5 results, the COSMO results show the sensitivity to the different lower  
497 boundaries of  $RH_{ice}$  (i.e.,  $RH_i^* = 105\%$ , Simulation D). For instance, the mean  $N_{ice}$  below  $-36^\circ\text{C}$   
498 with a higher  $RH_{ice}$  boundary (105%) is reduced by 12%. This difference is perhaps due to the  
499 use of finely resolved grid-scale humidity in COSMO rather than parameterizing  $S_{max}$  as done in  
500 SCAM5 (Gettelman *et al.*, 2010). Figure 8 illustrates the differences between P13 and the AIDA  
501 results depending on  $T$  and  $RH_{ice}$ . Simulated  $N_{ice}$  values are segregated in fine  $T$  and  $RH_{ice}$   
502 spacing (1K and 2% bins, respectively) based on the thermodynamic conditions under which ice  
503 crystals were formed in COSMO and summed up over the time of simulation. This segregation  
504 allows for an estimation of the relative contribution of different thermodynamic conditions to the

505 simulated ice formation. Our results show diversity between P13 and the AIDA  $n_s$ -isoline-based  
506 parameterization. Ice crystal formation was less for P13 and more for the new parameterization.  
507 A possible explanation for the observed deviation may be due to the difference in  
508 parameterization based on lab- or field data. For instance, atmospheric aging and processing (i.e.,  
509 surface coating and associated heterogeneous surface reactions) may have altered ice-nucleating  
510 propensity and limited deposition nucleation of dust-derived INPs in the P13 parameterization  
511 for the field data-derived parameterization as discussed in *Phillips et al.* (2008).

512

#### 513 4. Discussions

514

515 As described in the previous section (Sect. 3.1), deposition mode freezing cannot solely  
516 explain the  $n_s$ -isoline observation below water saturation ( $-50\text{ °C} < T < -36\text{ °C}$  in Fig. 2).  
517 Although we presumed that SCF acts as a subset of immersion freezing and plays an important  
518 role in this region, further insight and evidence of SCF beyond cloud simulation chamber  
519 observations are required to correctly understand the contributions of both homogeneous and  
520 heterogeneous nucleation. High-resolution microscopic techniques with an integrated continuous  
521 cooling setup are needed to visualize the freezing process of a single particle and to fully  
522 understand the complex freezing processes involved in SCF on particle surfaces.

523 Comparison of the new parameterization to a previous empirical parameterization (P13)  
524 showed that the new AIDA  $n_s$ -isoline-based scheme predicts more ice (Figs. 4-8). In particular,  
525  $T$ -RH<sub>ice</sub> dependence of  $N_{ice}$  and  $n_s$  at low  $T$  that may coincide in the upper troposphere, and this  
526 highlights the need for further investigations. However, it should be noted that there is some  
527 evidence for the atmospheric relevance and applicability of the new parameterization. First of all  
528 we demonstrated that the new  $n_s$  parameterization based on the experiments with hematite  
529 particles agrees well with previous literature results for mineral dust aerosol (e.g., *Möhler et al.*,  
530 2006; *Welti et al.*, 2009; *Köhler et al.*, 2010). Second, *Niemand et al.* (2012) demonstrated that  
531 different dusts exhibit similar  $n_s$  in immersion mode freezing and perhaps such a similarity  
532 remains true for the deposition mode ice nucleation of desert dusts. Lastly, the comparison  
533 between the observed profile of ice crystal number concentrations and the simulated ones (Figs.  
534 5 and 6) also suggests the validity of the new parameterization. These premises must be further  
535 examined in comparing to atmospherically relevant substrates (fresh and aged ones) and their ice  
536 nucleation activities in laboratory settings. In situ INP measurements, such as the number  
537 concentration and the types of INPs, at the upper troposphere can also help to constrain the  
538 parameterization.

539 Finally, to further develop more atmospherically relevant parameterizations other than  
540 the fit-based parameterization with artificial test aerosol, the relationship between  $1/T$  and  $\ln S_{ice}$   
541 for a constant nucleation rate or  $n_s$  based on the CNT can be analyzed (i.e., Eqns. A10-A11 in  
542 *Hoose and Möhler*, 2012). In this way, the composition specific  $n_s(T-S_{ice})$  values, where the

543 transition from SCF to deposition nucleation (or vice versa) occurs, may be better defined and  
544 can be then be used as an inexpensive model friendly parameterization.

545

## 546 5. Conclusion

547

548 A new heterogeneous ice nucleation parameterization was developed using results  
549 obtained from AIDA cloud simulation chamber experiments. The new  $n_s$ -isoline-based  
550 parameterization is applicable to a wide temperature range from  $-36$  to  $-78$  °C and, hence, allows  
551 for the examination of ice nucleation spectra in a simple framework for modeling application.

552 Our experimental results provide a good basis for the  $T$  and  $\text{RH}_{\text{ice}}$  dependence of  
553 deposition nucleation, and the formulated hematite  $n_s$ -isolines are comparable to that of desert  
554 dust samples. Consequently, our results with synthesized hematite particles can also be relevant  
555 to cirrus applications despite their smaller atmospheric relevance compared to natural hematite.  
556 Our isoline formulation suggested three different ice nucleation pathways over the wide range of  
557 temperature. In specific, a  $\text{RH}_{\text{ice}}$ -dependent ice nucleation regime was observed at temperatures  
558 below  $\sim -60$  °C, where deposition mode is presumably responsible to trigger ice nucleation. At -  
559  $60$  °C  $< T < -50$  °C, ice nucleation efficiency was  $T$ -independent (i.e.,  $\text{RH}_{\text{ice}}$  dependent).  
560 Conversely, a predominant influence of  $T$  on ice nucleation was observed near the water  
561 saturation condition ( $T > \sim -50$  °C), which may be indicative of nucleation due to condensation of  
562 water at the particle surface followed by homogeneous freezing of the condensed water (i.e.,  
563 SCF). The observed active SCF near water saturation and physical processes at the transitions of  
564 nucleation modes still remain to be studied in detail for various types of atmospheric particles.

565 Our conceptual model examinations also considered the competition between  
566 heterogeneous freezing and homogeneous freezing of solution particles to evaluate the relative  
567 importance of the different freezing processes in two models (SCAM5 and COSMO). The  
568 inhibition of homogeneous nucleation due to heterogeneous freezing was commonly observed in  
569 both SCAM5 and COSMO simulations. Our new parameterization revealed a minimum  
570 deviation of  $N_{\text{ice}}$  values estimated by SCAM5 at minimum  $\text{RH}_{\text{ice}}$  values for ice formation (100 or  
571 105%) compared to COSMO. This deviation suggests different sensitivities of the model to the  
572 lower bound of the  $\text{RH}_{\text{ice}}$  value owing to the presence of the model-resolved supersaturation to  
573 calculate the ice nucleation rate. Overall, our new hematite-based parameterization strongly  
574 suggests the role of  $T$  and more ice nucleation when compared to the existing empirical  
575 parameterization, presumably allowing more ice activation under water subsaturated conditions.

576

577 **Author Contributions**

578

579 N. Hiranuma and O. Möhler designed and conceived the experiments. Parameterizations  
580 were implemented by N. Hiranuma, I. Steinke and M. Paukert. M. Paukert and K. Zhang carried  
581 out modeling studies with input from C. Hoose, N. Hiranuma and G. Kulkarni. M. Schnaiter  
582 analyzed SIMONE data. H. Saathiff contributed to TDL measurements and analysis. The  
583 manuscript was written by N. Hiranuma. All authors discussed the results and contributed ideas  
584 to the manuscript.

585

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587

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600



601 **References**

- 602
- 603 Archuleta, C. M., DeMott, P. J., and Kreidenweis, S. M.: Ice nucleation by surrogates for  
604 atmospheric mineral dust and mineral dust/sulfate particles at cirrus temperatures, *Atmos. Chem.*  
605 *Phys.*, 5, 2617–2634, doi:10.5194/acp-5-2617-2005, 2005.
- 606
- 607 Baldauf, M., Seifert, A., Förstner, J., Majewski, D., Raschendorfer, M., and Reinhardt, T.:  
608 Operational convective-scale numerical weather prediction with the COSMO model: Description  
609 and sensitivities, *Mon. Weather Rev.*, 139, 12, 3887–3905, doi: 10.1175/MWR-D-10-05013.1,  
610 2011.
- 611
- 612 Barahona, D. and Nenes, A.: Parameterization of cirrus cloud formation in large-scale models:  
613 Homogeneous nucleation, *J. Geophys. Res.*, 113, D11211, doi:10.1029/2007JD009355, 2008.
- 614
- 615 Barahona, D. and Nenes, A.: Parameterizing the competition between homogeneous and  
616 heterogeneous freezing in cirrus cloud formation – monodisperse ice nuclei, *Atmos. Chem. Phys.*,  
617 9, 369–381, doi:10.5194/acp-9-369-2009, 2009a.
- 618
- 619 Barahona, D. and Nenes, A.: Parameterizing the competition between homogeneous and  
620 heterogeneous freezing in ice cloud formation – polydisperse ice nuclei, *Atmos. Chem. Phys.*, 9,  
621 5933–5948, doi:10.5194/acp-9-5933-2009, 2009b.
- 622
- 623 Barahona, D., Rodriguez, J., and Nenes, A.: Sensitivity of the global distribution of cirrus ice  
624 crystal concentration to heterogeneous freezing, *J. Geophys. Res.*, 115, D23213,  
625 doi:10.1029/2010JD014273, 2010.
- 626
- 627 Benz, S., Megahed, K., Möhler, O., Saathoff, H., Wagner, R., and Schurath, U.: *T*-dependent rate  
628 measurements of homogeneous ice nucleation in cloud droplets using a large atmospheric  
629 simulation chamber, *J. Photoch. Photobio. A*, 176, 208–217,  
630 doi:10.1016/j.jphotochem.2005.08.026, 2005.
- 631
- 632 Boucher, O., Randall, D., Artaxo, P., Bretherton, C., Feingold, G., Forster, P., Kerminen, V.-M.,  
633 Kondo, Y., Liao, H., Lohmann, U., Rasch, P., Satheesh, S. K., Sherwood, S., Stevens, B., and  
634 Zhang, X. Y.: Clouds and Aerosols. In: *Climate Change 2013: The Physical Science Basis.*  
635 *Contribution of Working Group I to the Fifth Assessment Report of the Intergovernmental Panel*  
636 *on Climate Change* [Stocker, T. F., D. Qin, G.-K. Plattner, M. Tignor, S. K. Allen, J. Boschung,  
637 A. Nauels, Y. Xia, V. Bex, and P. M. Midgley (eds.)]. Cambridge University Press, Cambridge,  
638 United Kingdom and New York, NY, USA, 2013.
- 639
- 640 Christenson, H.: Two-step crystal nucleation via capillary condensation, *Cryst. Eng. Comm.*, 15,  
641 2030–2039, doi:10.1039/C3CE26887J, 2013.
- 642
- 643 Claquin, T., Schulz, M., and Balkanski, Y.: Modeling the mineralogy of atmospheric dust  
644 sources, *J. Geophys. Res.*, 104, 22243–22256, doi:10.1029/1999JD900416, 1999.
- 645

646 Connolly, P.J., Möhler, O., Field, P.R., Saathoff, H., Burgess, R., Choulaton, T., and Gallagher,  
647 M.: Studies of heterogeneous freezing by three different desert dust samples, *Atmos. Chem.*  
648 *Phys.*, 9, 2805–2824, doi:10.5194/acp-9-2805-2009, 2009.

649  
650 Cziczo, D. J., Froyd, K. D., Hoose, C., Jensen, E. J., Diao, M., Zondlo, M. A., Smith J. B.,  
651 Twohy, C. H., and Murphy, D. M.: Clarifying the dominant sources and mechanisms of cirrus  
652 cloud formation, *Science*, 340, 1320–1324, doi:10.1126/science.1234145, 2013.

653  
654 Cziczo, D. J. and Froyd, K. D.: Sampling the composition of cirrus ice residuals, *Atmospheric*  
655 *Research*, 142, 15–31, doi: 10.1016/j.atmosres.2013.06.012, 2014.

656  
657 DeMott, P. J., Möhler, O., Stetzer, O., Vali, G., Levin, Z., Petters, M. D., Murakami, M., Leisner,  
658 T., Bundke, U., Klein, H., Kanji, Z. A., Cotton, R., Jones, H., Benz, S., Brinkmann, M.,  
659 Rzesanke, D., Saathoff, H., Nicolet, M., Saito, A., Nillius, B., Bingemer, H., Abbatt, J., Ardon,  
660 K., Ganor, E., Georgakopoulos, D. G., and Saunders, C.: Resurgence in ice nuclei measurement  
661 research, *Bulletin of the Amer. Meteorol. Soc.*, 92, 1623–1625,  
662 doi:http://dx.doi.org/10.1175/2011BAMS3119.1, 2011.

663  
664 Doms, G., Förster, J., Heise, E., Herzog, H.-J., Mironov, D., Raschendorfer, M., Reinhardt, T.,  
665 Ritter, B., Schrodin, R., Schulz, J.-P., and Vogel, G.: A description of the nonhydrostatic  
666 regional COSMO Model. Part II: Physical parameterization, Technical Report. Deutscher  
667 Wetterdienst, 154 pp, 2011.

668  
669 Fahey, D. W., Gao, R.-S., Möhler, O., Saathoff, H., Schiller, C., Ebert, V., Krämer, M., Peter, T.,  
670 Amarouche, N., Avallone, L. M., Bauer, R., Bozóki, Z., Christensen, L. E., Davis, S. M.,  
671 Durr, G., Dyroff, C., Herman, R. L., Hunsmann, S., Khaykin, S. M., Mackrodt, P., Meyer, J.,  
672 Smith, J. B., Spelten, N., Troy, R. F., Vömel, H., Wagner, S., and Wienhold, F. G.: The  
673 AquaVIT-1 intercomparison of atmospheric water vapor measurement techniques, *Atmos. Meas.*  
674 *Tech. Discuss.*, 7, 3159–3251, doi:10.5194/amtd-7-3159-2014, 2014.

675  
676 Gettelman, A., Hegglin, M. I., Son, S.-W., Kim, J., Fujiwara, M., Birner, T., Kremser, S., Rex,  
677 M., Añel, J. A., Akiyoshi, H., Austin, J., Bekki, S., Braesike, P., Brühl, C., Butchart, N.,  
678 Chipperfield, M., Dameris, M., Dhomse, S., Garny, H., Hardiman, S. C., Jöckel, P., Kinnison, D.  
679 E., Lamarque, J. F., Mancini, E., Marchand, M., Michou, M., Morgenstern, O., Pawson, S., Pitari,  
680 G., Plummer, D., Pyle, J.A., Rozanov, E., Scinocca, J., Shepherd, T. G., Shibata, K., Smale, D.,  
681 Teyssèdre, H., and Tian, W.: Multimodel assessment of the upper troposphere and lower  
682 stratosphere: Tropics and global trends, *J. Geophys. Res.*, 115, D00M08,  
683 doi:10.1029/2009JD013638, 2010.

684  
685 Hiranuma, N., Hoffmann, N., Kiselev, A., Dreyer, A., Zhang, K., Kulkarni, G., Koop, T., and  
686 Möhler, O.: Influence of surface morphology on the immersion mode ice nucleation efficiency of  
687 hematite particles, *Atmos. Chem. Phys.*, 14, 2315–2324, doi:10.5194/acp-14-2315-2014, 2014.

688  
689 Hoose, C., Kristjánsson, J.E., Chen, J.-P., and Hazra, A.: A classical-theory-based  
690 parameterization of heterogeneous ice nucleation by mineral dust, soot and biological particles in

691 a global climate model, *J. Atmos. Sci.*, 67(8) 2483–2503,  
692 doi:<http://dx.doi.org/10.1175/2010JAS3425.1>, 2010.  
693  
694 Hoose, C and Möhler, O.: Heterogeneous ice nucleation on atmospheric aerosols: a review of  
695 results from laboratory experiments, *Atmos. Chem. Phys.*, 12, 9817–9854,  
696 doi:10.5194/acp-12-9817-2012, 2012.  
697  
698 Hung H.-M., Malinowski, A., and Martin, S. T.: Kinetics of heterogeneous ice nucleation on the  
699 surfaces of mineral dust cores inserted into aqueous ammonium sulfate particles, *J. Phys. Chem.*  
700 *A.*, 107, 1296–1306, doi: 10.1021/jp021593y, 2003.  
701  
702 Kärcher, B. and Lohmann, U.: A parameterization of cirrus cloud formation: Heterogeneous  
703 freezing, *J. Geophys. Res.*, 108, 4402, doi:10.1029/2002JD003220, 2003.  
704  
705 Kärcher, B., Hendricks, J., and Lohmann, U.: Physically based parameterization of cirrus cloud  
706 formation for use in global atmospheric models, *J. Geophys. Res.*, 111, D01, 205,  
707 doi:10.1029/2005JD006219, 2006.  
708  
709 Khvorostyanov, V. I. and Curry, J. A.: The theory of ice nucleation by heterogeneous freezing of  
710 deliquescent mixed CCN. Part I: Critical radius, energy, and nucleation rate, *J. Atmos. Sci.*, 61,  
711 2676–2691, doi:<http://dx.doi.org/10.1175/JAS3266.1>, 2004.  
712  
713 Koehler, K. A., Kreidenweis, S. M., DeMott, P. J., Petters, M. D., Prenni, A. J., and Möhler, O.:  
714 Laboratory investigations of the impact of mineral dust aerosol on cold cloud formation, *Atmos.*  
715 *Chem. Phys.*, 10, 11955–11968, doi:10.5194/acp-10-11955-2010, 2010.  
716  
717 Koop, T., Luo, B., Tsias, A., and Peter, T.: Water activity as the determinant for homogeneous  
718 ice nucleation in aqueous solutions, *Nature*, 406, 611–614, doi:10.1038/35020537, 2000.  
719  
720 Liu, X. and Penner, J. E.: Ice nucleation parameterization for global models, *Meteorol. Z.*, 14,  
721 499–514, doi:10.1127/0941-2948/2005/0059, 2005.  
722  
723 Liu, X., Shi, X., Zhang, K., Jensen, E. J., Gettelman, A., Barahona, D., Nenes, A., and Lawson,  
724 P.: Sensitivity studies of dust ice nuclei effect on cirrus clouds with the Community Atmosphere  
725 Model CAM5, *Atmos. Chem. Phys.*, 12, 12061–12079, doi:10.5194/acp-12-12061-2012, 2012.  
726  
727 Marcolli, C.: Deposition nucleation viewed as homogeneous or immersion freezing in pores and  
728 cavities, *Atmos. Chem. Phys.*, 14, 2071–2104, doi:10.5194/acp-14-2071-2014, 2014.  
729  
730 Matsuki, A., Schwarzenboeck, A., Venzac, H., Laj, P., Crumeyrolle, S., and Gomes, L.: Cloud  
731 processing of mineral dust: direct comparison of cloud residual and clear sky particles during  
732 AMMA aircraft campaign in summer 2006, *Atmos. Chem. Phys.*, 10, 1057–1069,  
733 doi:10.5194/acp-10-1057-2010, 2010.  
734

735 Meyers, M. P., DeMott, P. J., and Cotton, W. R.: New primary ice nucleation parameterizations  
736 in an explicit cloud model, *J. Appl. Meteorol.*, 31, 708–721, doi:[http://dx.doi.org/10.1175/1520-0450\(1992\)031<0708:NPINPI>2.0.CO;2](http://dx.doi.org/10.1175/1520-0450(1992)031<0708:NPINPI>2.0.CO;2), 1992.  
737  
738

739 Möhler, O., Stetzer, O., Schaefers, S., Linke, C., Schnaiter, M., Tiede, R., Saathoff, H., Krämer,  
740 M., Mangold, A., Budz, P., Zink, P., Schreiner, J., Mauersberger, K., Haag, W., Kärcher, B., and  
741 Schurath, U.: Experimental investigation of homogeneous freezing of sulphuric acid particles in  
742 the aerosol chamber AIDA, *Atmos. Chem. Phys.*, 3, 211–223, doi:10.5194/acp-3-211-2003,  
743 2003.  
744

745 Möhler, O., Linke, C., Saathoff, H., Schnaiter, M., Wagner, R., Mangold, A., Krämer, M., and  
746 Schurath, U.: Ice nucleation on flame soot aerosol of different organic carbon content, *Meteorol.  
747 Z.*, 14, 477–484, doi:10.1127/0941-2948/2005/0055, 2005.  
748

749 Möhler, O., Field, P. R., Connolly, P., Benz, S., Saathoff, H., Schnaiter, M., Wagner, R., Cotton,  
750 R., Krämer, M., Mangold, A., and Heymsfield, A. J.: Efficiency of the deposition mode ice  
751 nucleation on mineral dust particles, *Atmos. Chem. Phys.*, 6, 3007–3021, doi:10.5194/acp-6-  
752 3007-2006, 2006.  
753

754 Murray, B. J., O’Sullivan, D., Atkinson, J. D., and Webb, M. E.: Ice nucleation by particles  
755 immersed in supercooled cloud droplets, *Chem. Soc. Rev.*, 41, 6519–6554,  
756 doi:10.1039/c2cs35200a, 2012.  
757

758 Neale, R. B., Chen, C.-C., Gettelman, A., Lauritzen, P. H., Park, S., Williamson, D. L., Conley,  
759 A. J., Garcia, R., Kinnison, D., Lamarque, J.-F., Marsh, D., Mills, M., Smith, A. K., Tilmes, S.,  
760 Vitt, F., Morrison, H., Cameron-Smith, P., Collins, W. D., Iacono, M. J., Easter, R. C., Ghan, S.  
761 J., Liu, X., Rasch, P. J., and Taylor, M. A.: Description of the NCAR Community At- mosphere  
762 Model (CAM5.0), Tech. Rep. NCAR/TN-486-STR, NCAR, available at:  
763 <http://www.cesm.ucar.edu/models/cesm1.0/cam/> (last access: 8 January 2013), 2010.  
764

765 Niemand, M., Möhler, O., Vogel, B., Vogel, H., Hoose, C., Connolly, P., Klein, H., Bingemer,  
766 H., DeMott, P., Skrotzki, J., and Leisner, T.: A particle-surface-area-based parameterization of  
767 immersion freezing on mineral dust particles, *J. Atmos. Sci.*, 69, 3077–3092,  
768 doi:<http://dx.doi.org/10.1175/JAS-D-11-0249.1>, 2012.  
769

770 Phillips, V. T. J., DeMott, P. J., and Andronache, C.: An empirical parameterization of  
771 heterogeneous ice nucleation for multiple chemical species of aerosol, *J. Atmos. Sci.*, 65, 2757–  
772 2783, doi:<http://dx.doi.org/10.1175/2007JAS2546.1>, 2008.  
773

774 Phillips, V. T. J., DeMott, P. J., Andronache, C., Pratt, K. A., Prather, K. A., Subramanian, R.,  
775 and Twohy, C.: Improvements to an empirical parameterization of heterogeneous ice nucleation  
776 and its comparison with observations, *J. Atmos. Sci.*, 70, 378–409, doi:  
777 <http://dx.doi.org/10.1175/JAS-D-12-080.1>, 2013.  
778

779 Pruppacher, H. R. and Klett, J. D.: Microphysics of Clouds and Precipitation, Atmospheric and  
780 Oceanographic Sciences Library, Kluwer Academic Publishers, Dordrecht, The Netherlands,  
781 309–360, 1997.  
782  
783 Ren, C. and Mackenzie, A. R.: Cirrus parameterization and the role of ice nuclei, *Q. J. Roy.*  
784 *Meteorol. Soc.*, 131, 1585–1605, doi:10.1256/qj.04.126, 2005.  
785  
786 Sakai, T., Orikasa, N., Nagai, T., Murakami, M., Tajiri, T., Saito, A., Yamashita, K., and  
787 Hashimoto, A.: Balloon-borne and Raman lidar observations of Asian dust and cirrus cloud  
788 properties over Tsukuba, Japan, *J. Geophys. Res.*, 119, 3295–3308, doi:10.1002/2013JD020987,  
789 2014.  
790  
791 Sassen, K. and Khvorostyanov, V. I.: Cloud effects from boreal forest fire smoke: Evidence for  
792 ice nucleation from polarization lidar data and cloud model simulations, *Environ. Res. Lett.*, 3,  
793 025006, doi:10.1088/1748-9326/3/2/025006, 2008.  
794  
795 Schnaiter, M., Büttner, S., Möhler, O., Skrotzki, J., Vragel, M., and Wagner, R.: Influence of  
796 particle size and shape on the backscattering linear depolarisation ratio of small ice crystals –  
797 cloud chamber measurements in the context of contrail and cirrus microphysics, *Atmos. Chem.*  
798 *Phys.*, 12, 10465–10484, doi:10.5194/acp-12-10465-2012, 2012.  
799  
800 Seifert, A. and Beheng, K. D.: A two-moment cloud microphysics parameterization for mixed-  
801 phase clouds. Part I: Model description, *Meteorol. Atmos. Phys.*, 92, 45–66, doi:10.1007/s00703-  
802 005-0112-4, 2006.  
803  
804 Seifert, A., Köhler, C., and Beheng, K. D.: Aerosol-cloud-precipitation effects over Germany as  
805 simulated by a convective-scale numerical weather prediction model, *Atmos. Chem. Phys.*, 12  
806 (2), 709–725, doi:10.5194/acp-12-709-2012, 2012.  
807  
808 Shilling, J. E., Fortin, T. J., and Tolbert, M. A.: Depositional ice nucleation on crystalline organic  
809 and inorganic solids, *J. Geophys. Res.*, 111, D05207, doi:10.1029/2005JD006664, 2006.  
810  
811 Skrotzki, J., Connolly, P., Schnaiter, M., Saathoff, H., Möhler, O., Wagner, R., Niemand, M.,  
812 Ebert, V., and Leisner, T.: The accommodation coefficient of water molecules on ice – cirrus  
813 cloud studies at the AIDA simulation chamber, *Atmos. Chem. Phys.*, 13, 4451–4466,  
814 doi:10.5194/acp-13-4451-2013, 2013.  
815  
816 Steinke, I., Möhler, O., Kiselev, A., Niemand, M., Saathoff, H., Schnaiter, M., Skrotzki, J.,  
817 Hoose, C., and Leisner, T.: Ice nucleation properties of fine ash particles from the  
818 Eyjafjallajökull eruption in April 2010, *Atmos. Chem. Phys.*, 11, 12945–12958, doi:10.5194/acp-  
819 11-12945-2011, 2011.  
820  
821 Storelvmo, T. and Herger, N.: Cirrus cloud susceptibility to the injection of ice nuclei in the  
822 upper troposphere, *J. Geophys. Res.*, 119, 2375–2389, doi:10.1002/2013JD020816, 2014.  
823

824 Sugimoto, T. and Sakata, K.: Preparation of monodisperse pseudocubic  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> particles from  
825 condensed ferric hydroxide gel, *J. Colloid Interface Sci.*, 152, 2, 587–590, doi:10.1016/0021-  
826 9797(92)90062-Q, 1992.

827

828 Vali, G.: Nucleation terminology, *J. Aerosol Sci.*, 16, 575–576, doi:10.1016/0021-  
829 8502(85)90009-6, 1985.

830

831 Vragel, M.: Messung klimarelevanter optischer Eigenschaften von Mineralstaub im Labor,  
832 Faculty of Physics, Karlsruhe Institute of Technology, Karlsruhe, 162 pp., 2009.

833

834 Wang, B. and Knopf, D.: Heterogeneous ice nucleation on particles composed of humic-like  
835 substances impacted by O<sub>3</sub>, *J. Geophys. Res.*, 116, D03205, doi:10.1029/2010JD014964, 2011.

836

837 Welti, A., Lüönd, F., Stetzer, O., and Lohmann, U.: Influence of particle size on the ice  
838 nucleating ability of mineral dusts, *Atmos. Chem. Phys.*, 9, 6705–6715, doi:10.5194/acp-9-6705-  
839 2009, 2009.

840

841 Welti, A., Kanji, Z. A., Lüönd, F., Stetzer, O., and Lohmann, U.: Exploring the mechanisms of  
842 ice nucleation on kaolinite: from deposition nucleation to condensation freezing, *J. Atmos. Sci.*,  
843 71, 16–36, doi: 10.1175/JAS-D-12-0252.1, 2014.

844

845 Zhang, K., Liu, X., Wang, M., Comstock, J. M., Mitchell, D. L., Mishra, S., and Mace, G. G.:  
846 Evaluating and constraining ice cloud parameterizations in CAM5 using aircraft measurements  
847 from the SPARTICUS campaign, *Atmos. Chem. Phys.*, 13, 4963–4982, doi:10.5194/acp-13-  
848 4963-2013, 2013.

849

850 Zuberi, B., Bertram, A. K., Cassa, C. A., Molina, L. T., and Molina, M. J.: Heterogeneous  
851 nucleation of ice in (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub>–H<sub>2</sub>O particles with mineral dust immersions, *Geophys. Res.*  
852 *Let.*, 29, 1504, doi:10.1029/2001GL014289, 2002.

853

854 **Table and Figures of “A Comprehensive Parameterization of Heterogeneous Ice Nucleation**  
855 **of Dust Surrogate: Laboratory study with Hematite Particles and Its Application to**  
856 **Atmospheric Models”**  
857

858 **October 1, 2014**

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879 **Citation:**

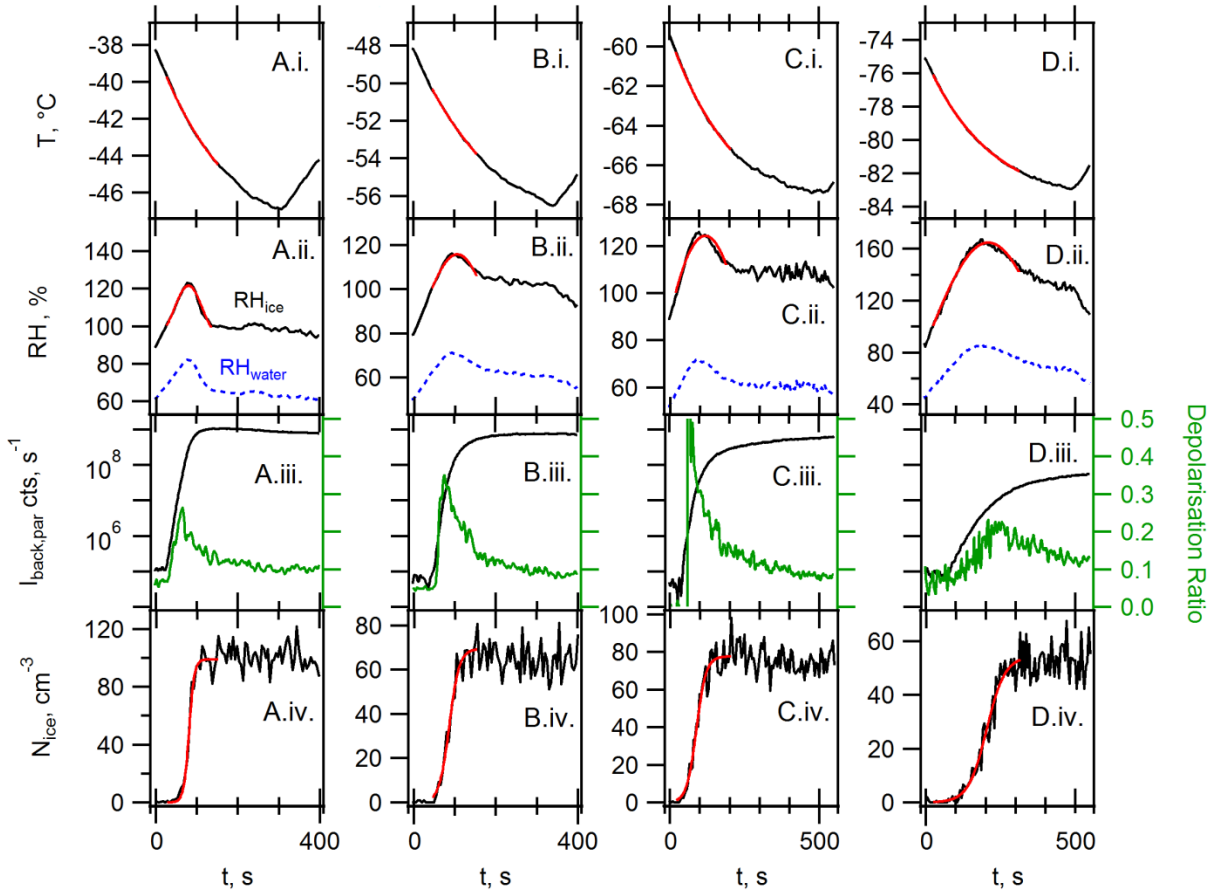
880 Hiranuma, N. et al. **A Comprehensive Parameterization of Heterogeneous Ice Nucleation of**  
881 **Dust Surrogate: Laboratory study with Hematite Particles and Its Application to**  
882 **Atmospheric Models**, for *Atmospheric Chemistry and Physics*

Table 1. Summary of aerosol measurements and AIDA ice nucleation experiments. All HALO experiments are from *Skrotzki et al.* (2013).

Experiment ID	Aerosol Measurements			Ice Nucleation Measurements				
	Hematite Diameter, nm	Total Number Conc., cm <sup>-3</sup>	Total Surface Conc., μm <sup>2</sup> cm <sup>-3</sup>	Examined <i>T</i> Range, °C	Examined RH <sub>ice</sub> Range, %	Evaluated <i>n<sub>s</sub></i> , m <sup>-2</sup>	<i>T</i> (Evaluated <i>n<sub>s</sub></i> ), °C	RH <sub>ice</sub> (Evaluated <i>n<sub>s</sub></i> ), %
HALO05_24	200	115.0	14.4	-76.1 to -81.9	100.6 to 164.8	10 <sup>11</sup>	-78.2	136.4
HALO04_09	500	112.5	26.9	-75.8 to -80.1	100.3 to 149.8	10 <sup>11</sup>	-77.5	128.3
HALO04_05	500	142.2	30.9	-61.8 to -65.5	100.2 to 135.6	10 <sup>11</sup>	-62.6	111.1
HALO05_18	200	161.9	21.8	-60.3 to -65.2	100.1 to 124.5	10 <sup>11</sup>	-60.8	106.0
HALO06_22	200	145.7	19.2	-50.2 to -53.9	100.3 to 123.4	10 <sup>11</sup>	-50.7	106.7
HALO06_21	200	245.0	32.9	-50.3 to -53.8	100.4 to 115.8	10 <sup>11</sup>	-50.5	102.2
INUIT01_26	1000	342.1	749.0	-41.0 to -47.1	100.2 to 103.9	10 <sup>10</sup>	-41.2	102.2
HALO06_20	200	168.7	22.4	-39.8 to -44.4	100.4 to 128.8	10 <sup>10</sup>	-40.7	111.3
HALO06_19	200	283.0	42.9	-39.7 to -44.5	100.2 to 121.6	10 <sup>10</sup>	-40.6	109.2
INUIT04_08	1000	193.0	647.0	-39.3 to -45.4	100.0 to 113.2	10 <sup>10</sup>	-40.4	110.1
INUIT04_10	1000	161.7	546.6	-37.5 to -43.7	100.0 to 124.1	10 <sup>10</sup>	-40.1	123.3
INUIT01_30	1000	414.5	889.7	-34.6 to -42.0	100.2 to 127.1	2.5 x 10 <sup>8</sup>	-37.0	122.8

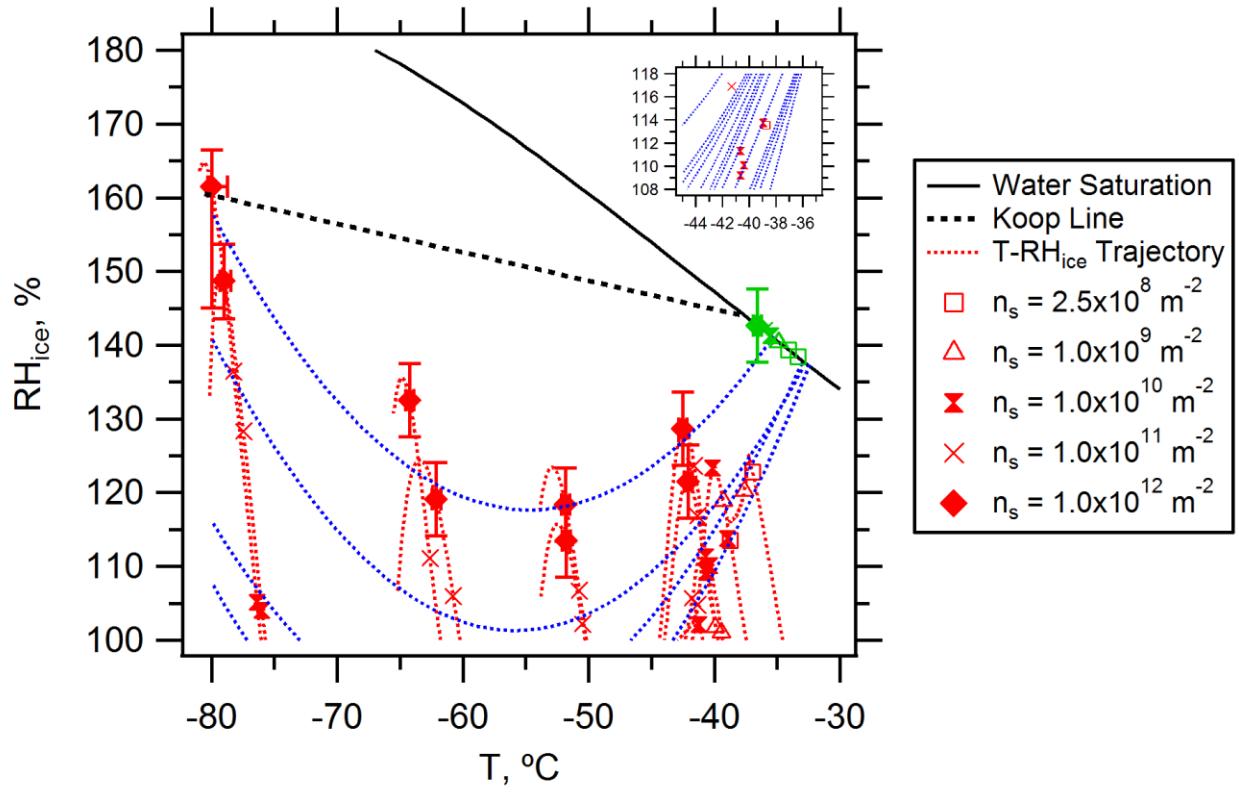
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Figure 1.



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Figure 2.

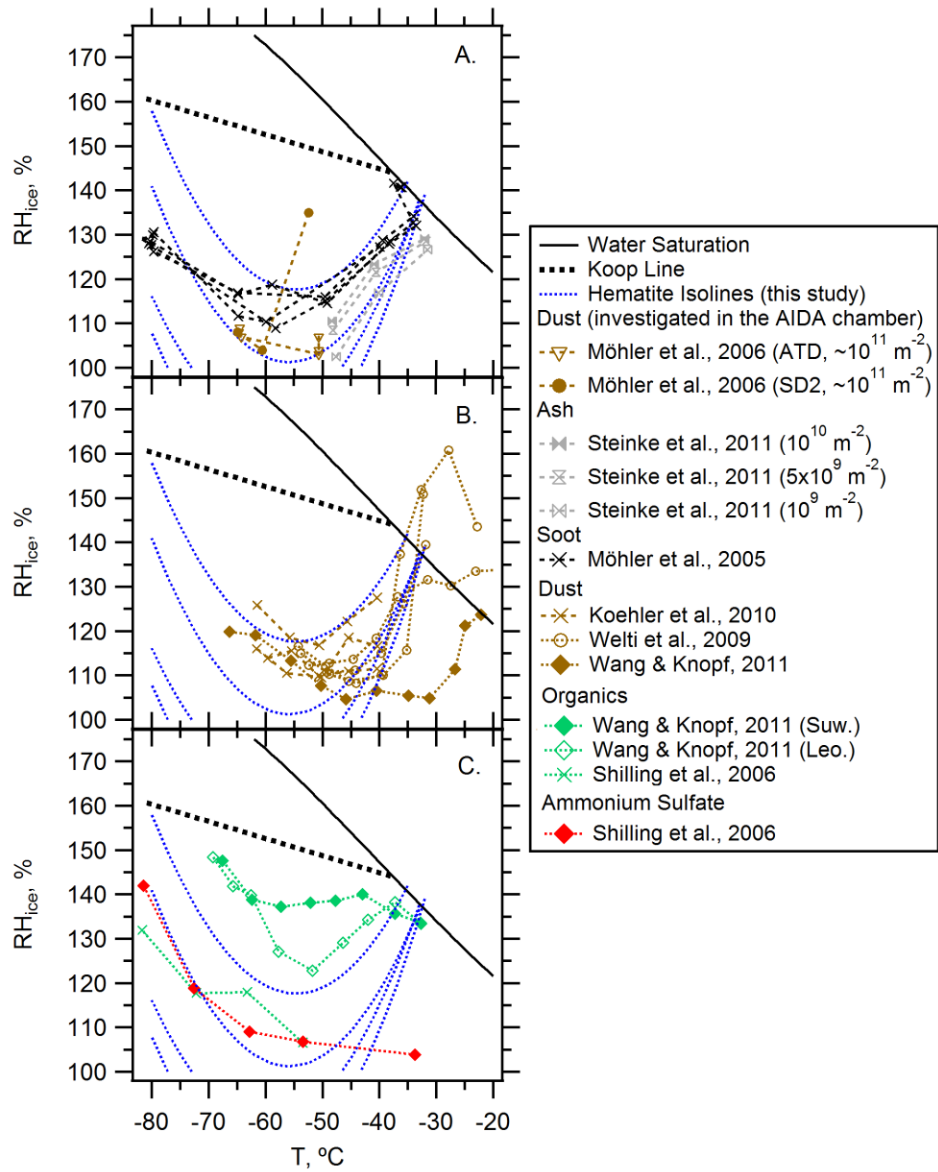
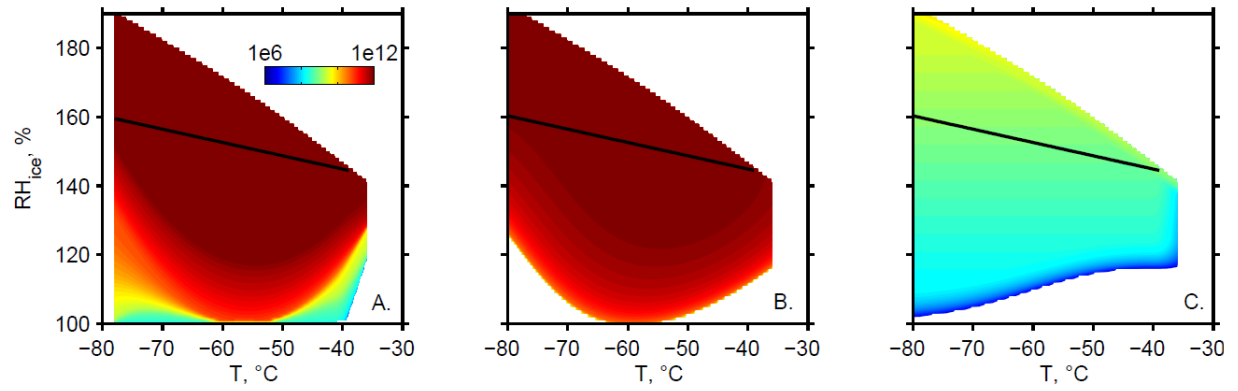


Figure 3.

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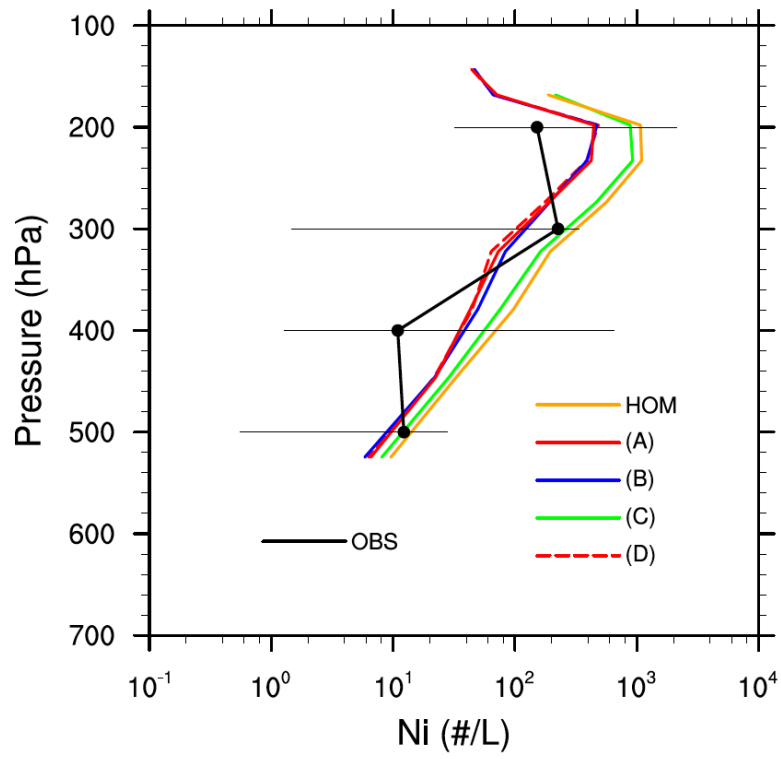
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Figure 4.

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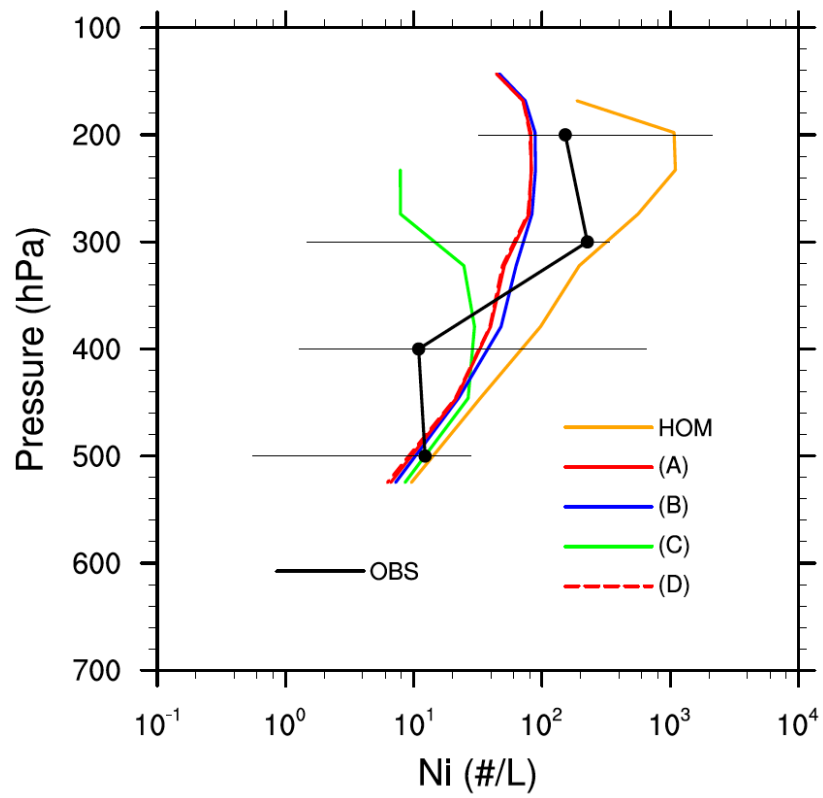


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Figure 5.

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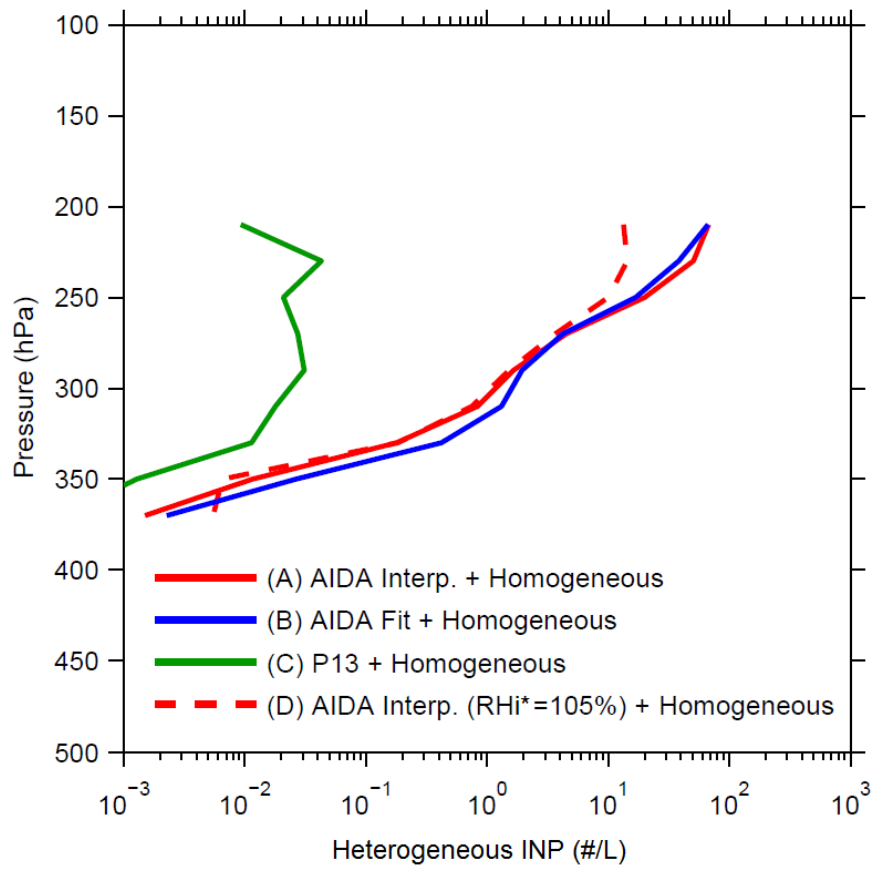


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Figure 6.

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Figure 7.

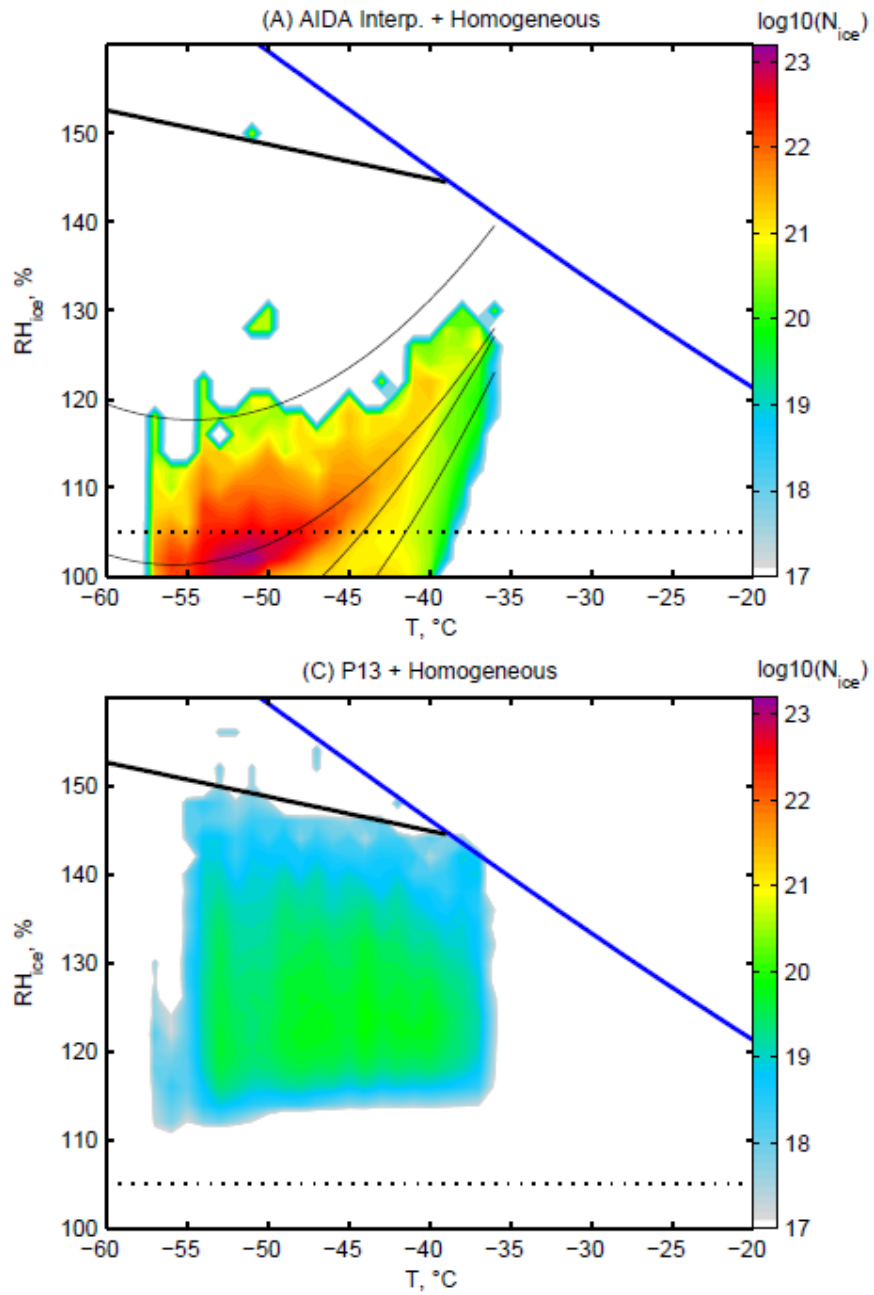


Figure 8.

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909 **Figure Captions**

910

911 Figure 1. Temporal plots of the representative AIDA deposition mode freezing experiments with  
912 various cooling ranges, including A. HALO06\_19, B. HALO06\_21, C. HALO05\_18 and D.  
913 HALO05\_24. Panels are arranged to show the measurements of i. AIDA mean gas temperature  
914 ( $T$ ), ii. TDL, iii. SIMONE and iv. ice crystal concentration ( $N_{ice}$ ). Note that the red lines represent  
915 interpolated data used for the  $n_s$ -isoline formulation. The  $I_{back,par}$  in Panel iv axis denotes the  
916 backscattered light scattering intensity parallel to the incident polarisation state (log-scaled). An  
917 increase in the depolarisation ratio indicates the formation and growth of ice crystals.

918

919 Figure 2. The constant  $n_s$  magnitudes are joined by lines (blue), representing “isolines” of  
920 hematite freezing profiles in the  $T$ - $RH_{ice}$  space. The interpolated isolines are equally spaced at  
921 every order of magnitude from  $10^{12} \text{ m}^{-2}$  (top) to  $10^9 \text{ m}^{-2}$  (bottom). Experimental trajectories of  
922 AIDA expansion-experiments with hematite particles are shown as red dotted lines. The data  
923 indicated by green color on the water saturation line represent the previously reported results of  
924 immersion freezing (*Hiranuma et al.*, 2014). The sub-panel shows a magnified section of  $T$  (-35  
925 °C to -45 °C) and  $RH_{ice}$  (110 to 120 %) space with equi-distant  $n_s$  spacing (every quarter  
926 magnitude). The error bars at  $n_s$  of  $10^{12} \text{ m}^{-2}$  are from *welas*.

927

928 Figure 3. Ice nucleation onset  $T$ - $RH_{ice}$  of previously published data (A. AIDA studies, B. dust,  
929 and C. ammonium sulfate and organics) shown together with the isolines of hematite particles  
930 from the present study ( $10^{12} \text{ m}^{-2}$ , top, to  $10^9 \text{ m}^{-2}$ , bottom).

931

932 Figure 4. Spatial plot of isolines for constant  $n_s$  derived from A. interpolating AIDA data, B.  
933 applying the third degree polynomial fit function to interpolated AIDA data and C. a previously  
934 published parameterization (*Phillips et al.*, 2013) for hematite particles. The color scale displays  
935 log-scaled  $n_s$  values in  $\text{m}^{-2}$ , applicable to all panels. The solid black lines indicate the  
936 homogeneous freezing threshold line (i.e., Koop line).

937

938 Figure 5. Monthly mean profiles of the simulated in-cloud ice crystal number concentrations ( $N_i$   
939  $\sim N_{ice}$ ) over the ARM SGP site. The four cases shown in the figure include the pure

940 homogeneous ice nucleation case (HOM) and four combined (heterogeneous + homogeneous)  
941 ice nucleation cases: (A) AIDA Interp. + Homogeneous; (B) AIDA Fit + Homogeneous; (C) P13  
942 + Homogeneous; and (D) AIDA Interp. ( $RH_i^* = 105\%$ ) + Homogeneous. Black dots show the  
943 observed mean profile of  $N_i$ . Left and right ends of the horizontal bars indicate the 10<sup>th</sup> and 90<sup>th</sup>  
944 percentiles of the observed  $N_i$  values at each pressure level.

945

946 Figure 6. Monthly mean profiles of the simulated in-cloud ice crystal number concentrations ( $N_i$   
947  $\sim N_{ice}$ ) over the ARM SGP site. The four cases shown in the figure include the pure  
948 homogeneous ice nucleation case (HOM) and four pure heterogeneous ice nucleation cases: (A)  
949 AIDA Interp.; (B) AIDA Fit; (C) P13; and (D) AIDA Interp. ( $RH_i^* = 105\%$ ). Black dots show the  
950 observed mean profile of  $N_i$ . Left and right ends of the horizontal bars indicate the 10<sup>th</sup> and 90<sup>th</sup>  
951 percentiles of the observed  $N_i$  values at each pressure level.

952

953 Figure 7. The mean heterogeneous INP number concentrations ( $\sim N_{ice}$ ) simulated in COSMO.  
954 The red dashed line represents the simulation with 105%  $RH_{ice}$  as the lower boundary of ice  
955 formation, while the others are based on with 100% for the minimum  $RH_{ice}$  value.

956

957 Figure 8. Accumulated ice crystal concentrations (color scale in total crystals per model domain)  
958 as a function of temperature (1°C bins) and  $RH_{ice}$  (2% bins). Heterogeneous nucleation simulated  
959 by AIDA parameterization (i.e., Figure 4A) and P13 parameterization (i.e., Figure 4C) was  
960 combined with homogeneous nucleation of cloud droplets.

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