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# On the relationship between responses in cloud water and precipitation to changes in aerosol

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# Abstract

Climate models continue to exhibit strong sensitivity to the representation of aerosol effects on cloud reflectance and cloud amount. This paper evaluates proposed efforts to constrain modeled cloud liquid water path (LWP) adjustments in response to changes in aerosol concentration  $N_a$  using observations of precipitation susceptibility. Recent climate modeling has suggested a linear relationship between relative LWP responses to relative changes in  $N_a$  (i.e., dln LWP/dln  $N_a$ ) and the precipitation frequency susceptibility  $S_{pop}$ , defined as the relative change in the probability of precipitation for a relative change in  $N_{\rm a}$ . A satellite-based measurement of  $S_{\rm pop}$  combined with this model-based relationship provide a constraint on  $dlnLWP/dlnN_a$ . Through a review of the existing 10 literature and a suite of large eddy simulations of stratocumulus and trade-wind cumulus clouds, we show that the climate model-based relationship is not unique and sometimes even has an opposite slope to those from fine-scale studies. Therefore, we propose a more careful examination of the scale and regime dependence of this relationship. 15

### 1 Introduction

Like its predecessors, the IPCC Fifth Assessment Report (AR5; IPCC 2013) continues to point to aerosol effects on clouds as a major source of uncertainty in our predictive climate modeling capability. Recognizing that cloud systems constantly ad-

- just to aerosol perturbations, AR5 chose to combine both cloud albedo and LWP responses to aerosol changes into one term, i.e., the effective radiative forcing associated with aerosol-cloud interactions (ERFaci). The representation of the underlying microphysical processes associated with cloud formation and albedo and precipitation modification must be improved to better quantify ERFaci. Attempts to constrain ER-
- <sup>25</sup> Faci with observations is an important part of this quantification. Early efforts (e.g., Quaas et al., 2006, 2009) used satellite-based measurements of drop concentration



(or size) responses to changes in aerosol (Bréon et al., 2002) to constrain the albedo effect (Twomey, 1977). More detailed analysis using surface-based remote sensing and proxy data from cloud resolving models pointed to the scale dependence of these relationships (McComiskey and Feingold, 2008, 2012) and called for a clear distinction
 <sup>5</sup> between the cloud process scale and the satellite data aggregation scale before such observational constraints are applied.

In this paper, we shift attention to observational constraints on aerosol effects on cloud amount or the "lifetime effect" (Albrecht, 1989) via precipitation modifications. Precipitation susceptibility, i.e.,  $S_o = -d \ln R/d \ln N_d$ , where *R* is the precipitation rate and  $N_d$  is the droplet number concentration (Feingold and Siebert, 2009; Sorooshian et al., 2009) was previously introduced as a means of quantifying this effect. An alternative definition, i.e., the susceptibility of the probability of precipitation (POP) to changes in aerosol  $S_{pop}$  has been proposed:  $S_{pop} = -d \ln POP/d \ln N_a$  (e.g., Wang et al., 2012; Terai et al., 2012) because POP is more amenable to measurement and because of the

- <sup>15</sup> high spatial variability in *R*. Several studies have attempted to quantify  $S_{pop}$  or  $S_o$  using satellite remote sensing (e.g., Sorooshian et al., 2009; L'Ecuyer et al., 2009), surface remote sensing (Mann et al., 2014), and in-situ aircraft observations (Terai et al., 2012). The values vary considerably depending on several factors, e.g., the definition of precipitation susceptibility, averaging scale (Duong et al., 2011), phase of cloud lifecycle
- <sup>20</sup> (Duong et al., 2011; Feingold et al., 2013), and aerosol loading (Feingold et al., 2013). There is disagreement in the literature not only on the values of  $S_{pop}$  and  $S_o$  but also on how they depend on important controlling parameters, such as cloud depth and LWP. While quantifying the precipitation susceptibility is not the focus of this paper, we refer to two values as guidance. The first,  $S_{pop} = 0.12$  (Wang et al., 2012), was derived from satellite remote sensing data. The second,  $S_o \approx 1$  (Mann et al., 2014) was calculated from surface-based remote sensing observations in the northeastern Atlantic Ocean and continental Europe.

Wang et al. (2012) proposed using measurements of  $S_{pop}$  as a means of constraining LWP responses to aerosol changes in a climate model. The authors used a series



of climate model simulations with the NCAR Community Atmosphere Model version 5 (CAM5) and the ECHAM5-HAM2 to derive an approximate linear relationship between  $\lambda = d\ln LWP/d\ln N_a$  and  $S_{pop}$  with an intercept at approximately (0,0). Interestingly, the model output from the Multiscale Modeling Framework (MMF) version of CAM5, which 5 resolves clouds and precipitation more reliably than the standard CAM5, also conforms to this linear relationship. The constraint on  $\lambda$  proceeds as follows. The output from a series of GCM simulations is used to define  $\lambda = f(S_{pop})$ ; then, a measurement of  $S_{pop}$  combined with the model-derived  $f(S_{pop})$  yields an observational constraint on  $\lambda$ . Wang et al. (2012) showed that because  $f(S_{pop})$  has an intercept at nearly (0,0) and the measured  $S_{pop}$  is small, it follows that  $\lambda$ , which is the cloud LWP adjustment portion 10 of of ERFaci, is also small. However, the authors did concede that more work must be performed to test these relationships in higher resolution models. The current work directly addresses this point. Specifically, this study addresses the generality and scale dependence of the  $\lambda - S_{pop}$  relationship. The  $\lambda - S_{pop}$  relationship is examined at the cloud scale based on previously published work and more rigorously via an analysis of 15 large eddy simulation (LES) results for warm (liquid phase only) cloud systems. Observations of  $S_{\text{pop}}$  and  $S_{\text{o}}$  are then used to provide LES constraints on  $\lambda$ ; the implications for albedo susceptibility (Platnick and Twomey, 1994) are also explored.

The remainder of the paper is organized as follows. Section 2 introduces the methods used to evaluate  $\lambda$  based on both extant literature and LES. The primary results are presented and discussed in Sect. 3. Finally, the important conclusions of this work are enumerated in Sect. 4.

### 2 Methods

# 2.1 Analysis of extant literature

<sup>25</sup> If indeed the relationship between  $\lambda$  and  $S_{pop}$  (or  $S_o$ ) is robust, one might expect this to emerge in extant literature. We therefore conducted a survey of published results from



a wide range of studies that simulated cases based on various field campaigns. The details of these studies are listed in Table 1. The choice of  $S_o$  vs.  $S_{pop}$  in the review of the existing literature was based on the lack of information regarding the rain fraction (or POP) in previously published studies. The potential effect of this substitution is discussed later.

### 2.2 LES simulations

Two different cloud regimes were explored: (i) stratocumulus, based on the Second Dynamics and Chemistry of Marine Stratocumulus (DYCOMS-II) Research Flight 2 (RF02) and (ii) trade-wind cumulus, based on the Rain in Cumulus over the Ocean (RICO) field experiment. The two different warm cloud regimes provide the opportunity to explore the robustness of both the  $\lambda - S_{pop}$  and  $\lambda - S_{o}$  relationships.

# 2.2.1 Stratocumulus clouds: DYCOMS-II, RF02

A suite of 25 simulations is performed with the Weather Research and Forecasting (WRF) model to explicitly examine the relationships between  $\lambda$  and  $S_{pop}$  and between  $\lambda$  and  $S_{o}$ . For the purposes of this study, WRF is coupled with a two-moment, binemulating microphysical model that has been widely used to examine aerosol-cloud interactions (Feingold et al., 1998; Wang and Feingold, 2009a). The simulations comprise 5 different initial aerosol number concentrations (i.e.,  $N_a = 25$ , 50, 75, 100, and  $125 \text{ mg}^{-1}$ ). Note that  $N_a$  is used interchangeably in this paper to denote both the aerosol number concentration (units of cm<sup>-3</sup>) and mixing ratio (units of mg<sup>-1</sup>) because the simulations use different initialization routines. However, because the air density is approximately 1 kg m<sup>-3</sup> for the considered domains, 1 mg<sup>-1</sup>  $\approx$  1 cm<sup>-3</sup>. While the aerosol concentration is a prognostic variable, the shape of the distribution is invariant with time and assumed to be lognormal with a median radius of 0.2 µm and a geometric standard deviation of 1.5. The aerosol is assumed to be composed of ammonium sulfate. Super-

<sup>25</sup> deviation of 1.5. The aerosol is assumed to be composed of ammonium sulfate. Supersaturation is calculated and prognostically treated in the model; droplets are formed on



the aerosol particles with radii above the critical supersaturation required for activation following Köhler theory. The activated aerosol particles are removed from the aerosol population. Particles are regenerated upon evaporation of droplets assuming that one drop regenerates one aerosol particle (Mitra et al., 1992). Thus, collision-coalescence
 and surface rain effectively reduce the aerosol concentration.

For each N<sub>a</sub>, a control simulation is performed based on DYCOMS-II RF02, which readily produced drizzle (Stevens et al., 2003). The WRF-LES setup described by Ya-maguchi and Feingold (2012) is used. Four additional simulations are performed to explore the sensitivity to environmental conditions and microphysical process rates, i.e.,
 <sup>10</sup> increased surface latent heat flux (140 W m<sup>-2</sup>, Hi-LHF), decrease surface latent heat flux (46.5 W m<sup>-2</sup>, Lo-LHF), increased collision-coalescence rate (110 % of the predicted rate, Hi-CC), and decreased collision-coalescence rate (80 % of the predicted rate, Lo-CC).

All simulations are performed with a horizontal grid spacing of 50 m and a vertical grid spacing of 12 m. The domain is 6.4 km by 6.4 km in the horizontal and 1.5 km in the vertical direction. A time step of 0.2 s is used to ensure numerical stability and convergence (see Yamaguchi and Feingold, 2012). The total simulation time is 6 h; however, the initial 1 h of all simulations is discarded to allow sufficient time for turbulence to develop. The rapid radiative transfer model (RRTM) is used to calculate the longwave

<sup>20</sup> radiative fluxes. The simulations are assumed to be nocturnal, i.e., shortwave radiative fluxes were not included. The necessary model information is recorded at 1 min intervals, yielding nearly 5 million *x*, *y* pairs for each simulation. Although the decorrelation time for cloud fields has been shown to be much longer than 1 min (e.g.,  $\approx$  15 min according to McComiskey et al., 2009), the 1 min resolution is necessary to ensure that the rare, high precipitation rate events are captured in the model output.

### 2.2.2 Trade-wind cumulus: RICO

The RICO simulations used in this study are adopted from Jiang et al. (2010). These simulations were performed using the Regional Atmospheric Modeling System



(RAMS) version 6.0 with an explicit bin-resolving microphysics scheme (Feingold et al., 1996; Stevens et al., 1996). The aerosol treatment in these simulations is very similar to that of the stratocumulus simulations (see Sect. 2.2.1). The domain size is  $25.6 \text{ km} \times 25.6 \text{ km} \times 6 \text{ km}$  with a horizontal grid spacing of 100 m and vertical grid spac-

- <sup>5</sup> ing of 40 m. The Global Energy and Water Cycle Experiment Cloud System (GCSS) boundary layer working group initial sounding is modified to initiate heavier rainfall by increasing the ambient water vapor mixing ratio and decreasing the potential temperature above 1 km. The model top is also extended in Jiang et al. (2010) to 6 km to allow for deeper convection. The simulations are performed for 8 h with 5 different aerosol
- <sup>10</sup> loadings, namely, 100, 200, 300, 400, and 500 cm<sup>-3</sup>. It is important to note that even with these modifications, the sounding used still resembles the observed sounding on 19 January 2005, during the RICO campaign. As in the case of the stratocumulus simulations, model output at 1 min intervals is used. For additional information on these simulations, the reader is referred to Jiang et al. (2010).

### 15 2.3 $\lambda$ calculation

The LWP was first calculated for every column and for every output time by including only cloud water, which is consistent with the method used in Wang et al. (2012). Here,  $\lambda$  is approximated as follows:

$$\lambda = \frac{d\ln LWP}{d\ln N_{a}} \approx \frac{\Delta \ln LWP}{\Delta \ln N_{a}} = \left\langle \frac{\ln \overline{LWP^{(2)}} - \ln \overline{LWP^{(1)}}}{\ln N_{a}^{(2)} - \ln N_{a}^{(1)}} \right\rangle, \tag{1}$$

20

25

where the overbars represent spatial (horizontal) means and the brackets represent temporal means. The superscripts correspond to low (1) and high (2) aerosol loading scenarios. The results were found to be qualitatively (and nearly quantitatively) insensitive to the order in which the calculations were performed, i.e., taking the temporal average of the relative differences (as in Eq. 1) or taking the relative difference of the temporal averages.



### 2.4 $S_{pop}$ calculation

To calculate  $S_{pop}$ , we first determined if it was raining at the surface in a given grid cell and assigned the grid cell a probability of P = 1 if it was raining and P = 0 otherwise – namely, the precipitation probability P(t) as a function of time t is conditional on <sup>5</sup> a threshold rain rate  $T_h$ :

$$P_{i,j}^{(k)}(t) = \begin{cases} 1 & \text{if } R_{i,j}^{(k)}(t) \ge T_{h} \\ 0 & \text{if } R_{i,j}^{(k)}(t) < T_{h} \end{cases}$$

where  $T_h$  represents a predefined threshold in mm day<sup>-1</sup> and the superscript *k* corresponds to the specific simulation. The surface rain rate was used for the calculations herein. Then,  $S_{pop}$  was calculated similar to  $\lambda$ , i.e.,

$$S_{\text{pop}} = -\frac{d\ln\text{POP}}{d\ln N_{\text{a}}} \approx -\frac{\Delta\ln\text{POP}}{\Delta\ln N_{\text{a}}} = -\left\langle \frac{\ln\overline{P^{(2)}} - \ln\overline{P^{(1)}}}{\ln N_{\text{a}}^{(2)} - \ln N_{\text{a}}^{(1)}} \right\rangle.$$
(3)

For calculating P, 10 thresholds were applied to R, ranging from  $10^{-6}$  to 20 mm day<sup>-1</sup>. Only a representative subset of these calculations is presented in this paper.

### 15 2.5 So calculation

Here,  $S_o$  was computed by conditionally averaging the rain rate over the aforementioned rain rate thresholds. However, in keeping with Feingold and Siebert (2009), the denominator is  $d \ln N_d$  instead of  $d \ln N_a$ ; therefore, we have

$$S_{\rm o} = -\frac{\mathrm{d}\ln R}{\mathrm{d}\ln N_{\rm d}} \approx -\frac{\Delta \ln R}{\Delta \ln N_{\rm d}} = -\left\langle \frac{\ln \overline{R^{(2)}} - \ln \overline{R^{(1)}}}{\ln \overline{N_{\rm d}^{(2)}} - \ln \overline{N_{\rm d}^{(1)}}} \right\rangle,\tag{4}$$

20

where all of the variables and symbols are defined above.



(2)

# 2.6 S<sub>o, mod</sub> and S<sub>pop, mod</sub> calculations

Two additional parameters were computed, i.e.,  $S_{o, mod}$  and  $S_{pop, mod}$ ;  $S_{o, mod}$  is the same as in Eq. (4) except that  $N_a$  replaces  $N_d$  in the denominator. Similarly,  $S_{pop, mod}$  replaces  $N_a$  with  $N_d$  in the denominator of Eq. (3). These modified parameters are use-

<sup>5</sup> ful for analyzing the sensitivity of the results to the use of  $N_a$  or  $N_d$ , in which the latter evolves with time and the former is used to represent the response in the system to an initial change in aerosol loading, which is similar to the approach used in global climate simulations. The simulations also help to examine the robustness of results to multiple representations of precipitation susceptibility.

### 10 2.7 A<sub>f</sub> calculations

While values of  $\lambda$  constrained by  $f(S_{pop})$  and/or  $f(S_{o, mod})$  are far from certain, the estimates provided herein for the different cloud regimes can be used to estimate the potential effects of changes in aerosol loading on albedo susceptibility  $A'_{o}$ . We begin with the definition of  $A'_{o}$  from Feingold and Siebert (2009):

$$_{15} \quad A'_{o} = A_{o} \left[ 1 + \frac{5}{2} \frac{d \ln LWP}{d \ln N_{d}} + \dots \right],$$
 (5)

where  $A_0$  represents the albedo susceptibility under constant LWP conditions, i.e.,

$$A_{\rm o} = \left. \frac{\mathrm{d} \ln A}{\mathrm{d} \ln N_{\rm d}} \right|_{\rm LWP} = \frac{1 - A}{3},\tag{6}$$

and all other terms have been previously defined. The ellipsis on the right hand side of Eq. (5) represents additional terms that have been excluded in this study. These terms can include such effects as changes in the breadth of the drop size distribution (Feingold and Siebert, 2009). However, Eq. (5) is provided in terms of incremental changes in  $N_d$ , whereas, the LWP susceptibility, i.e.,  $\lambda$ , is defined relative to incremental



changes in  $N_{\rm a}$ . Therefore, we make use of a power law relationship between  $N_{\rm d}$  and  $N_{\rm a}$ :

 $N_{\rm d} \propto N_{\rm a}^c$ ,

<sup>5</sup> where *c* is theoretically ≤ 1. Previous studies have provided a broad range of values for *c*. For example, Shao and Liu (2009) suggested a range of 0.25 to 0.85 based on direct measurements of both polluted and clean clouds. Other studies have shown that *c* is likely on the higher end of this range in relatively clean conditions, i.e., N<sub>a</sub> < 500 cm<sup>-3</sup> (e.g. Conant et al., 2004; Twohy et al., 2005). Therefore, we chose a characteristic
 <sup>10</sup> value of 0.75 (or 3/4) for *c* in this study. As a result, the relationship presented in Eq. (7) can be rewritten as

$$\frac{\mathrm{d}\ln N_{\mathrm{d}}}{\mathrm{d}\ln N_{\mathrm{a}}} = c = \frac{3}{4}.$$

Then, by rewriting Eq. (5) as

<sup>15</sup> 
$$A'_{o} = A_{o} \left[ 1 + \frac{5}{2} \frac{\mathrm{d} \ln \mathrm{LWP}}{\mathrm{d} \ln N_{a}} \frac{\mathrm{d} \ln N_{a}}{\mathrm{d} \ln N_{d}} + \dots \right],$$

and incorporating Eq. (8), we get

$$A'_{\rm o} = A_{\rm o} \left[ 1 + \frac{10}{3} \lambda + \dots \right]. \tag{10}$$

<sup>20</sup> Because we are not necessarily concerned here with the specific values of either  $A'_{o}$  or  $A_{o}$ , we define the albedo susceptibility enrichment factor  $A_{f}$  as follows:

$$A_{\rm f} = \frac{A_{\rm o}'}{A_{\rm o}} = \left[1 + \frac{10}{3}\lambda + \dots\right].$$
 (11)



(7)

(8)

(9)

Thus  $\lambda = 0.3$  corresponds to a doubling of the albedo susceptibility relative to the value under constant LWP conditions. Calculations of  $A_f$  using Eq. (1) will be shown alongside those of  $\lambda$  for the two cloud types. Previous studies have provided estimates of both  $S_{pop}$  (0.12, Wang et al., 2012) and  $S_{o, mod}$  (0.66, Mann et al., 2014) using satellite-based and ground-based observations, respectively. Mann et al. (2014) reported the precipitation susceptibility in terms of incremental changes in  $N_a$ , which corresponds to  $S_{o, mod}$  in this study. However, precipitation susceptibility has been previously defined in numerous studies relative to incremental changes in  $N_d$  (i.e.,  $S_o$ ). Therefore, using Eq. (8), one finds that  $S_o$  is nearly 1.

### 10 3 Results

# 3.1 Analysis of extant literature

An initial review of the literature revealed several interesting components relevant to understanding the relationship between  $\lambda$  and  $S_{pop}$  (or  $S_o$ ). First, the lack of detailed information regarding the rain fraction or POP made it impossible to determine accurate values of  $S_{pop}$  from previously published results. Therefore, we chose to use  $S_o$  in our analysis of the published literature. However, even with this assumption, several studies still lacked the necessary details to determine a relationship between  $\lambda$  and  $S_o$  due to either the lack of information regarding  $N_d$  (needed to calculate  $S_o$ ) or the lack of information regarding the initial aerosol number concentration (needed to calculate  $\lambda$ ).

- As a result, we show the findings from the published literature in Fig. 1 for  $\lambda'$  as a function of  $S'_{o}$ , where the "prime" denotes that the axes are not necessarily the same for *all* points. Specifically,  $S'_{o}$  is  $d \ln R/d \ln N_{a}$  in Jiang et al. (2010) and  $\lambda'$  is  $d \ln LWP/d \ln N_{d}$  in Berner et al. (2011). For all other references,  $\lambda' = \lambda$  and  $S'_{o} = S_{o}$ , as defined in Eqs. (1) and (4), respectively.
- Furthermore, because the model output was unavailable from many of these studies, every effort was made to carefully read off the relevant values of LWP, R and  $N_a$  (or



a similar aerosol measurement, such as the number concentration of cloud condensation nuclei  $N_{\rm CCN}$  or  $N_{\rm d}$ ) from the published figures. Although a consistent methodology was applied to calculate  $\lambda'$  and  $S'_0$ , we make no claims on the accuracy of these results. The main point is to see whether any trends in  $\lambda'$  vs.  $S'_{0}$  emanate from different mod-<sup>5</sup> els and for different environmental conditions. Figure 1 shows substantial variability in the  $\lambda' - S'_{0}$  relationship. Depending upon which subset of points are selected, one can find a negative slope (e.g., green squares Wang and Feingold, 2009a), nearly no slope (e.g., red closed circles, Berner et al., 2011), and a positive slope (e.g., blue crosses, Wang and Feingold, 2009a). Interestingly, Wang and Feingold (2009a) suggests either a positive or a negative slope, depending upon how the LWP and R are averaged over 10 the domain (i.e., averaging all of the grid points or conditionally averaging grid points that exceed some predefined threshold). Regardless, none of the slopes predicted by the individual studies exhibits an intercept near (0.0). Moreover, the slopes of these lines tend to be negative or nearly 0, unlike the coarser grained climate model results in Wang et al. (2012). A more in-depth analysis is clearly warranted. 15

# 3.2 Stratocumulus LES (DYCOMS-II)

# 3.2.1 Rain rates

The LES results are presented below in the context of three specific thresholds on *R*. These thresholds are utilized to mimic minimum detectable limits for *R* from current satellite-based retrievals (and potentially from future satellite platforms). The three values for  $T_h$  are 0.001, 0.5, and 5 mm day<sup>-1</sup>. For perspective, the minimum detectable radar reflectivity for CloudSat is -30 dBZ (e.g., Haynes et al., 2009), while the minimum for the Tropical Rainfall Measuring Mission (TRMM) is 17 dBZ. These reflectivities roughly correspond to precipitation rates of 0.5 and 5 mm day<sup>-1</sup>, respectively. While inherent uncertainties in the *Z*-*R* relationships (emanating from, e.g., assumed drop size distributions and attenuation) can contribute to small variations in the lowest



detectable rain rates. we use  $T_h$  of 0.5 and 5 mm day<sup>-1</sup> to represent of CloudSat and TRMM precipitation rate observations, respectively.

Before delving into the relative changes in LWP, *R*, and POP, it is necessary to first evaluate the absolute range of *R* produced in the simulations. Figure 2 depicts the mean (solid) and median (dashed) rain rates for  $T_h$  of 0.001 (gray), 0.5 (blue), and 5 (red) mm day<sup>-1</sup> for the DYCOMS-II simulations. The shaded area encompasses the 10th to the 90th percentiles. Figure 2a shows that the average *R* is approximately 1– 2 mm day<sup>-1</sup> for  $T_h$  of 0.001 and 0.5 mm day<sup>-1</sup> and  $N_a = 25 \text{ mg}^{-1}$ ; the 90th percentile approaches 10 mm day<sup>-1</sup>. The values decrease as  $N_a$  increases (Fig. 2b–d).

<sup>10</sup> In general, there is a small increase in the mean and median *R* as  $T_h$  increases from 0.001 to 0.5 mm day<sup>-1</sup>. However, the increase is much more substantial for a further increase in  $T_h$  to 5 mm day<sup>-1</sup>. At this high threshold, the mean *R* is nearly equivalent to the 90th percentile for  $T_h$  of 0.001 and 0.5 mm day<sup>-1</sup>; therefore, most of the lightly drizzling grid points are excluded by choosing such a high  $T_h$ . The importance of these thresholds on *R* will be discussed in more detail below with respect to incremental increases in  $N_a$ . Figure 2 excludes the model results for  $N_a = 125 \text{ mg}^{-1}$  because *R* was too small for all but the smallest  $T_h$  to be confident in the averaged values of POP and *R*.

# 3.2.2 $\lambda - S_{pop}$ Relationship and $A_f$

- <sup>20</sup> It is important to note that for ease in interpretation of the LES results, we present the analysis of the 25 DYCOMS-II simulations (and the 5 RICO simulations presented below) using  $S_{pop}$ , which is identical to  $S_{pop}$  in Wang et al. (2012) except that the aerosol index (AI; the product of the Ångstrom coefficient and the aerosol optical depth) is replaced with  $N_a$ , i.e., the initial aerosol concentration that was used in the simulations. <sup>25</sup> This change should have little if any effect on the qualitative nature of the findings
- presented here given the nearly linear relationship observed between the AI and  $N_a$  or  $N_{CCN}$  (e.g. Nakajima et al., 2001; Liu and Li, 2014).



Figure 4 suggests several important results. First, the relationship between  $\lambda$  and  $S_{pop}$  depends on the chosen *R* threshold (i.e.,  $T_h$ ). The  $\lambda$ – $S_{pop}$  slope tends to decrease as  $T_h$  increases, especially when only examining relatively small changes in  $N_a$  (i.e., black and red points). In fact, for  $T_h = 0.001 \text{ mm day}^{-1}$ ,  $S_{pop} \simeq 0$  for a change in  $N_a$  from

- <sup>5</sup>  $25 \text{ mg}^{-1}$  to  $50 \text{ mg}^{-1}$ . In those relatively clean conditions, with such a low  $T_h$ , nearly all grid points are precipitating; a small absolute change in  $N_a$  is not sufficient to decrease R such that R becomes less than  $T_h$  for a substantial subset of the domain; hence, little if any change is found in POP in response to increases in  $N_a$ . This finding suggests that for low  $T_h$ , POP may be largely insensitive to changes in  $N_a$  in relatively clean envi-
- <sup>10</sup> ronments, especially for these stratocumulus simulations. However, for higher  $T_h$ , even in relatively clean conditions, a doubling of  $N_a$  produces an increase in  $S_{pop}$  (Fig. 4c) because in these conditions, even a change in  $N_a$  from 25 mg<sup>-1</sup> to 50 mg<sup>-1</sup> is sufficient to reduce R such that R becomes less than  $T_h = 5$  mm day<sup>-1</sup> for a substantial subset of the domain.
- <sup>15</sup> Furthermore, Fig. 4a suggests that for marine stratocumulus  $\lambda$  likely does not increase indefinitely as  $S_{pop}$  increases. Instead, an asymptotic behavior is suggested whereby any further increase in  $S_{pop}$  produces a smaller or nearly no change in  $\lambda$ . It is at this point that the change in  $N_a$  is sufficiently large to permit aerosol-induced evaporation-entrainment or sedimentation-entrainment effects to play a role. In other
- <sup>20</sup> words, further suppression in POP does not lead to an additional increase in LWP because the much smaller droplets are more readily evaporated (e.g., Wang et al., 2003; Ackerman et al., 2004; Xue and Feingold, 2006) or because weaker sedimentation enhances both evaporation and cloud-top cooling, both of which increase entrainment (Bretherton et al., 2007). This asymptotic behavior is challenging to discern for
- <sup>25</sup> higher  $T_h$  due to an insufficient number of points for which *R* exceeds  $T_h$  in the presence of higher aerosol loadings. However, the inability for  $\lambda$  to increase indefinitely as POP is further reduced should be expected given previously published findings. For example, Ackerman et al. (2004) demonstrated that LWP first increases with increasing  $N_a$  ( $\lambda > 0$ ), however further increases in  $N_a$  result in  $\lambda = 0$ . Ultimately, for a strong



enough aerosol perturbation,  $\lambda$  becomes negative; however, under these conditions clouds are likely not precipitating and  $\lambda$  is dominated by processes other than collision-coalescence.

As mentioned above,  $T_{\rm h} = 0.5 \,\mathrm{mm}\,\mathrm{day}^{-1}$  corresponds roughly to the threshold that <sup>5</sup> is commonly used to determine precipitating locations in the CloudSAT dataset. However, the results presented in Fig. 4 suggest that such a threshold may not be capable of capturing the entire parameter space for the selected case. Furthermore, such a large threshold tends to suppress the LWP response to changes in  $N_{\rm a}$  (i.e.,  $\lambda$ ), i.e., the intercept approaches (0,0) as  $T_{\rm h} \longrightarrow 5 \,\mathrm{mm}\,\mathrm{day}^{-1}$  for these stratocumulus clouds. <sup>10</sup> Physically, an intercept of  $\approx 0$  seems unlikely. Hypothetically, if an increase in  $N_{\rm a}$  re-

- sults in no change in POP ( $S_{pop} = 0$ ), the LWP should increase as the cloud droplets become smaller and more numerous and rain formation becomes less efficient. Therefore, in readily precipitating clouds, one would expect that the LWP should increase in response to increasing  $N_a$  ( $\lambda > 0$ ), as suggested in Fig. 4a and b. Both observational
- <sup>15</sup> studies (Christensen and Stephens, 2011) and LES (e.g., Wang et al., 2003; Ackerman et al., 2004; Xue et al., 2008) have confirmed  $\lambda > 0$  for readily precipitating clouds. However,  $\lambda$  can become negative in the presence of high aerosol loadings and readily precipitating cloud (discussed below with regard to the RICO simulations). Regardless, the high-resolution LES results for stratocumulus clouds presented herein suggest that

for  $S_{pop} = 0.12$  (Wang et al., 2012),  $\lambda$  varies between nearly 0 for high  $T_h$  to approximately 0.5 for lower  $T_h$ .

Figure 4 also provides a useful estimate of  $A_f$  for marine stratocumulus by applying Eq. (11) to the simulated values of  $\lambda$ . The right axes of the plots in Fig. 4 demonstrate the range of possible  $A_f$ . For a value of  $S_{pop}$  of 0.12 or by simply choosing the results

for small changes in  $N_a$ , the DYCOMS-II RF02 simulations suggest that  $A_f$  is between 1.8 and 2.5, i.e., the albedo susceptibly may be 80% to 150% higher than expected under constant LWP conditions.



# 3.2.3 $\lambda - S_{pop, mod}$ relationship

Fig. 5 shows the relationship between  $\lambda$  and  $S_{pop, mod}$ , in which the denominators of the x and y axes are no longer identical. For low  $T_h$ , changing the denominator has little to no effect on the relationship between relative changes in LWP and POP (Fig. 5a).

<sup>5</sup> However, for higher  $T_h$ , i.e., values that better reflect the lower detection limits of satellite retrievals, the inconsistent denominator causes the relationship to become less linear and more chaotic, especially for  $T_h = 5 \text{ mm day}^{-1}$ . The reason for this discrepancy is related to the fact that the relative changes in LWP and POP due to changes in  $N_a$ reflect a response due to the prescribed aerosol perturbation, i.e., the changes are relative to only the initial aerosol loading, whereas relative changes in LWP and POP due to changes in  $N_d$  reflect the effects of numerous microphysical processes (e.g., activation, collision-coalescence, and scavenging). Because  $N_d$  is not constant in time, the relative change in  $N_d$  tends to vary as a function of time. This transient nature produces the chaotic behavior in Fig. 5b and c.

### 15 3.2.4 $\lambda - S_{o, mod}$ relationship and $A_{f}$

As discussed above,  $S_o$  is typically represented in terms of relative changes in  $N_d$ . However, the previous subsection demonstrated how inconsistencies in the denominator can cause the relationship between  $\lambda$  and  $S_{pop}$  to become chaotic and no longer exhibit a clear trend. Therefore, we show the relationship between  $\lambda$  and  $S_{o, mod}$ , i.e., where the denominators in the *x* and *y* axes are both a function of the relative change in  $N_a$  (Fig. 6). As mentioned in Sect. 3.2.2, small changes in  $N_a$  exhibit little to no effect on POP when a low threshold on *R* is applied to determine raining and non-raining locations. However, the same does not hold true for *R*, i.e., even at low thresholds, *R* still changes due to increases in aerosol loading, even for small absolute changes. Therefore, the stratocumulus clouds continue to precipitate throughout most of domain for imposed increases in  $N_a$ , yet the average *R* is slightly reduced. This effect is



demonstrated in Fig. 6a, where we see that  $S_{o, mod}$  is greater than 0 (unlike the case for  $S_{pop}$ , Fig. 4a).

A comparison between Figs. 4 and 6 suggests that the relationships are qualitatively the same (i.e.,  $\lambda$  tends to increase as either  $S_{pop}$  or  $S_{o, mod}$  increases), although the slopes can be quite different. The difference in slopes is related to the aforementioned point about how changes in  $N_a$  act differently on R and POP. In the case of  $S_{o, mod}$ , small changes in  $N_a$  do little to affect the average R in the heavily drizzling regions, i.e., the high threshold is inclusive enough to maintain a relatively constant average Rfor all aerosol perturbations. On the other hand, for low  $T_h$ , nearly the entire domain is considered to be drizzling and a small change in  $N_a$  reduces R. However, because this reduction is not sufficient to convert many drizzling locations into non-drizzling points,  $S_o$  increases (Fig. 6a) while  $S_{pop}$  (Fig. 4a) remains nearly constant for small changes

in N<sub>a</sub>.

Using the  $S_{o, mod} = 0.66$  observational constraint from Mann et al. (2014) (note that  $S_o \approx 1$  for realistic values of *c*) for this scenario, one arrives at values of  $\lambda$  ranging from 0.4 to 1.0 for  $T_h = 0.001 \text{ mm day}^{-1}$  and  $T_h = 0.5 \text{ mm day}^{-1}$ , respectively. For  $T_h = 5 \text{ mm day}^{-1}$ , Fig. 6c suggests that  $\lambda$  would be substantially larger; however, the simulations do not extend to large enough  $N_a$  to quantify this effect. The right hand axes of Fig. 6 provide equivalent estimates of  $A_f$  derived from Eq. (11) and point to enhancements in the albedo susceptibility of 2.5 (4) for  $T_h = 0.001 \text{ mm day}^{-1}$  (0.5 mm day<sup>-1</sup>).

### 3.3 Trade-wind cumulus: RICO LES

### 3.3.1 Rain rates

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Figure 3a shows that the average *R* for  $N_a = 100 \text{ cm}^{-3}$  is approximately 10– 20 mm day<sup>-1</sup> for  $T_h$  of 0.001 and 0.5 mm day<sup>-1</sup> in the simulated trade-wind clouds (the domain average is naturally much less than this, however the threshold removes very small values of *R* such that the average *R* is higher). The average *R* for all thresholds



tends to decrease as  $N_a$  increases (Fig. 3b–e); the largest change occurs when  $N_a$  increases from 300 to 400 cm<sup>-3</sup> (Fig. 3c and d). The changes in *R* for increasing  $N_a$  are similar to those shown for the stratocumulus case (Fig. 2) except that *R* tends to change more rapidly in the trade-wind cumulus, especially for higher aerosol loadings. Moreover, Fig. 3 demonstrates that the clouds precipitate for all aerosol loading scenarios and under all threshold values in the RICO case; therefore, the analysis that follows incorporates all 5 RICO simulations.

# 3.3.2 $\lambda$ -S<sub>pop</sub>, S<sub>pop, mod</sub>, and S<sub>o, mod</sub> relationships and A<sub>f</sub>

The RICO simulations elicit an important finding that was alluded to earlier. Namely,  $\lambda$ is not necessarily positive. Figure 7 demonstrates that  $\lambda$  is negative for changes in  $N_a$ that are a factor of 3 or larger. Moreover, Fig. 7a suggests that in the case of these shallow trade-wind cumulus clouds,  $\lambda$  does not increase as  $S_{pop}$  increases; in fact, the opposite is true. This downward trend is related to the balance between aerosol perturbations acting to decrease R, and to increase entrainment and evaporation within the cloud. The former acts to increase  $S_{pop}$ , while the latter decreases  $\lambda$ . However, the simulations also suggest that  $\lambda$  saturates, which was suggested earlier in the case of stratocumulus clouds (Fig. 4). For larger and larger changes in  $N_a$ ,  $S_{pop}$  continues to increase while  $\lambda$  remains relatively constant. This asymptotic behavior is because the changes in droplet size for increases in aerosol loading beyond 400 cm<sup>-3</sup> are smaller relative to an increase in  $N_a$  from 100 to 200 mg<sup>-1</sup> and thus limit additional evaporationentrainment feedbacks on the cloud system. This is analogous to the findings of Xue

- and Feingold (2006) (Figs. 3 and 5 therein), who showed that several cloud characteristics (e.g., LWP and cloud fraction) asymptote for high aerosol number concentrations. This effect is largely related to the system converging on the saturation adjustment limit, which suppresses further decreases in  $\lambda$ . The results of the RICO simulations for
- small changes in  $N_a$  (i.e., from 100 to 200 cm<sup>-3</sup>) suggest that  $A_f$  may be similar for both marine stratocumulus and trade-wind cumulus (i.e., approximately 1.7 for the RICO simulations). However, whereas  $A_f$  was shown to increase for larger changes in  $N_a$  in



marine stratocumulus (Fig. 4),  $A_f$  tends to decrease in the case of trade-wind cumulus. In this case, the LWP response to an aerosol perturbation acts to *decrease* the albedo susceptibility ( $A_f$  is less than 1).

- The DYCOMS-II stratocumulus simulations demonstrated that the consistency in the denominator of the x- and y-axes was important for predicting an increase in  $\lambda$  as a function of  $S_{pop}$  or  $S_{o, mod}$ . However, in the trade-wind cumulus case, this effect is not seen (Figs. 7a and b are very similar). This follows because an increase in  $N_a$  results in an increase in  $N_d$  that does not vary much over the course of the 8 h simulations (Fig. 8a). This was not true in the case of drizzling stratocumulus clouds, where  $N_d$ decreased with time (Fig. 8b). Therefore, in the stratocumulus simulations, the relative droplet number concentration increases, especially when comparing the pristine simulation ( $N_a = 25 \text{ mg}^{-1}$ ) with the more polluted cases (i.e.,  $N_a = 100$  and  $125 \text{ mg}^{-1}$ ). We suggest that the difference is related to the different cloud systems. In the case of trade-wind cumulus, only a small fraction of the domain contains cloud water at any given time; therefore the time required to scavenge a large portion of the ambient aerosol is much longer than in the case of stratocumulus clouds where the cloud fraction is often nearly 1. This effect is demonstrated in Fig. 8, where the increase in
- the relative droplet number concentration (i.e.,  $N_d/N_{d,0}$ ) for the larger aerosol perturbations in the stratocumulus scenario corresponds to the rapid decrease in  $N_d$  in the low aerosol loading case as a result of the efficient removal of aerosol from the domain.

Furthermore, Fig. 7a and b suggest that  $\lambda$  decreases more rapidly with increased aerosol loading for lower  $T_{\rm h}$ . For  $T_{\rm h} = 0.001$  mm day<sup>-1</sup>,  $\lambda$  decreases from approximately 0.2 to -0.8 for an increase in  $S_{\rm pop}$  of only 0.8. However, for  $T_{\rm h} = 5$  mm day<sup>-1</sup>,  $\lambda$  decreases from approximately 0.2 to -0.8 for an increase in  $S_{\rm pop}$  of 2.5. This has important implications for constraining  $\lambda$  using observations of  $S_{\rm pop}$ . For example, if the former trend is true, then small values of  $S_{\rm pop}$  result in small values of  $\lambda$ , as suggested by Wang et al. (2012). However, if the latter trend is true, i.e.,  $\lambda$  decreases gradually with increasing  $N_{\rm a}$  (and increasing  $S_{\rm pop}$ ), then a small value of  $S_{\rm pop}$  implies a larger  $\lambda$ . For reference, if  $S_{\rm pop}$  is 0.12 (Wang et al., 2012), then  $\lambda$  is approximately 0 for



 $T_{\rm h} = 0.001 \text{ mm day}^{-1}$  (Fig. 7a, closed circles), while  $\lambda$  increases to approximately 0.3 for  $T_{\rm h} = 5 \text{ mm day}^{-1}$  (determined by extrapolating the points to smaller values of  $S_{\rm pop}$  in Fig. 7a, diamonds). Alternatively, if  $S_{\rm o, mod} = 0.66$  (Mann et al., 2014), then Fig. 7c indicates that  $\lambda$  ranges from 0.3 ( $T_{\rm h} = 0.001 \text{ mm day}^{-1}$ ) down to 0.05 ( $T_{\rm h} = 5 \text{ mm day}^{-1}$ ). Therefore, the equivalent range of  $A_{\rm f}$  range is an enhancement of 20% to 100% rel-

<sup>5</sup> Therefore, the equivalent range of  $A_{\rm f}$  range is an enhancement of 20% to 100% relative to constant LWP conditions. However, for even slightly higher  $S_{\rm o, mod}$ ,  $\lambda$  quickly becomes negative and  $A_{\rm f}$  becomes less than 1.

### 4 Conclusions

Wang et al. (2012) explored the relationship between the LWP response to an increase in aerosol loading  $\lambda$  and the precipitation frequency susceptibility  $S_{pop}$  in climate model simulations. If a robust relationship between  $\lambda$  and  $S_{pop}$  were to exist, observations of  $S_{pop}$  would provide a strong constraint on  $\lambda$  in climate studies. The current work examines this relationship at the large eddy scale.

First, a review of the literature suggests that the relationship between  $\lambda$  and  $S_{o}$  need <sup>15</sup> not be positive nor linear; however, these results exhibited little quantitive power given the paucity of the model output from the previous studies. To explore this relationship in more detail, a set of large eddy simulations of a drizzling stratocumulus case was performed, and a previously published set of trade-wind cumulus simulations was analyzed. In each of these sets, the simulations differ only in their initial aerosol con-<sup>20</sup> centration, allowing us to explore albedo susceptibility in an idealized framework.

The following important findings were drawn from this analysis. Although they are formulated with respect to  $S_{pop}$  for brevity, these conclusions apply more generally to  $S_{o, mod}$  as well.

1. The *y*-intercept of the  $\lambda - S_{pop}$  relationship is likely > 0, for both stratocumulus and trade-wind cloud systems. This differs from the climate-model derived intercept of 0 in Wang et al. (2012)



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2.  $\lambda$  does not necessarily increase linearly as a function of  $S_{pop}$ . Instead,  $\lambda$  exhibits an asymptotic behavior at sufficiently large  $S_{pop}$ . In the case of stratocumulus, aerosol-induced evaporation-entrainment and/or sedimentation-entrainment effects limit further increases in the LWP. This effect is schematically represented in Fig. 9 (red, stippled). For trade-wind cumulus clouds,  $\lambda$  is shown to *decrease* with increasing  $S_{pop}$  due to the effects of entrainment and evaporation (Fig. 9; blue, dotted). These different trends in  $\lambda$  are important if one wishes to diagnose  $\lambda$  from observations of  $S_{pop}$  or  $S_{o, mod}$ , especially for small aerosol perturbations, which are reflected by larger changes in  $\lambda$  and small changes in both  $S_{pop}$  (Fig. 9; crossed).

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- 3. At the  $S_{pop} = 0$  intercept,  $\lambda$  is approximately 0.2–0.3 in both the stratocumulus and trade-wind cumulus. However, the simulations suggest that  $\lambda$  may increase or decrease with increased aerosol loading (and increasing  $S_{pop}$ ) depending on the cloud type and dominant microphysical processes. Specifically, the results presented herein suggest that  $\lambda$  increases in marine stratocumulus and decreases in the case of trade-wind cumulus (Fig. 9).
- 4. To gauge the influence of these results on albedo susceptibility, we calculated  $A_{\rm f}$ , the fractional enhancement in the albedo susceptibility relative to constant LWP conditions. For the stratocumulus cloud case,  $A_{\rm f}$  ranges from enhancements of 80 % to 150 % if  $S_{\rm pop} = 0.12$  (Wang et al., 2012) is used as a constraint or approximately 150 % to 300 % if  $S_{\rm o,\ mod} = 0.66$  (Mann et al., 2014) is the constraint. Moreover, in the case of the trade-wind cumulus clouds, the  $A_{\rm f}$  ranges are 20–80 % for  $S_{\rm pop} = 0.12$  and 70 % for  $S_{\rm o,\ mod} = 0.66$ . However, for slightly higher  $S_{\rm pop}$  or  $S_{\rm o,\ mod}$ , the albedo susceptibility may actually decrease relative to constant LWP conditions due to the strong leverage of  $\lambda$  in Eq. (11).
- 5. The importance of using a consistent denominator in the  $\lambda$  and  $S_{pop}$  calculations was demonstrated by calculating  $S_{pop}$  (but not  $\lambda$ ) in terms of  $N_d$  rather than  $N_a$  (i.e.,  $S_{pop, mod}$ ). The introduced inconsistency is important in the case of stratocumulus



clouds in which  $N_{\rm d}$  decreases (quite rapidly in relatively clean conditions) as a function of time. This effect produces an ill-defined relationship between  $\lambda$  and  $S_{\text{pop, mod}}$ .

In general, while a measurement of  $S_{pop}$  is practical from a remote-sensing stand point and the use of a GCM allows for the analysis of the entire climate system, the  $\lambda - S_{pop}$ relationship is likely related to the resolution of convection, the scales at which the aerosol interacts with clouds, and the type of system (i.e., stratocumulus vs. trade-wind cumulus). Based on our earlier work (McComiskey and Feingold, 2012), we surmise that even if convection and aerosol-cloud processes are adequately resolved, the  $\lambda$ -

- $S_{\text{pop}}$  relationship will also be dependent on the scale at which data are aggregated. Determining POP is a binary option, i.e., it is either raining or it is not, which is dependent on some threshold for what is considered "raining". It has been shown here that the slope and intercept of the  $\lambda - S_{pop}$  is largely dependent upon the selected rain threshold. We therefore caution that these scale, threshold, and aerosol proxy sensi-
- tivities be carefully considered before  $\lambda S_{pop}$  relationships are universally applied. 15

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### Table 1. Data source description.

Campaign	Location	Reference	Cloud Type(s)	Model	Microphysics
ASTEX <sup>a</sup>	Northeastern Atlantic	Ackerman et al. (2004)	Nocturnal drizzling stratocumulus	Stevens et al. (2002), Ogura and Phillips (1962)	Ackerman et al. (1995)
DYCOMS-II <sup>b</sup>	Coastal Southern California	Ackerman et al. (2004)	Marine stratocumulus	Stevens et al. (2002), Ogura and Phillips (1962)	Ackerman et al. (1995)
FIRE-I <sup>c</sup>	Coastal Southern California	Ackerman et al. (2004)	Cloud field	Stevens et al. (2002), Ogura and Phillips (1962)	Ackerman et al. (1995)
RICO <sup>d</sup>	Antigua and Barbuda (Caribbean)	Lee et al. (2012)	Precipitating shallow cumulus	WRF <sup>1</sup> (Skamarock et al., 2008)	2-moment bulk (Feingold et al., 1998; Wang and Feingold, 2009a)
VOCALS-REx <sup>e</sup>	Southeast Pacific	Berner et al. (2011)	POCs	SAM <sup>2</sup> (Khairoutdinov and Randall, 2003)	2-moment bulk (Morrison and Gettelman, 2008)
DYCOMS-II <sup>b</sup>	Coastal Southern California	Wang and Feingold (2009a)	Marine stratocumulus	WRF <sup>1</sup> (Skamarock et al., 2008)	2-moment bulk (Feingold et al., 1998)
DYCOMS-II <sup>b</sup>	Coastal Southern California	Wang and Feingold (2009b)	Marine stratocumulus, ship tracks	WRF <sup>1</sup> (Skamarock et al., 2008)	2-moment bulk (Feingold et al., 1998)
RICO <sup>d</sup>	Antigua and Barbuda (Caribbean)	Jiang et al. (2010)	Precipitating shallow cumulus	RAMS <sup>3</sup> (Cotton et al., 2003)	bin (Feingold et al., 1996; Stevens et al., 1996)

<sup>a</sup> Atlantic Stratocumulus Transition Experiment

<sup>b</sup> second Dynamics and Chemistry of Marine Stratocumulus (Stevens et al., 2003, 2005)

<sup>c</sup> First ISCCP (International Satellite Cloud Climatology Project) Regional Experiment

<sup>d</sup> Rain in Cumulus over the Ocean

<sup>e</sup> VAMOS (Variability of the American Monsoon System) Ocean-Cloud-Atmosphere-Land Study - Regional Experiment

<sup>1</sup> Weather Research and Forecasting

<sup>2</sup> System for Atmospheric Modeling

<sup>3</sup> Regional Atmospheric Modeling System





**Figure 1.** Scatterplot of  $\lambda'$  vs.  $S'_{o}$  from previously published studies. The legend provides the reference that corresponds to each symbol. Note here that "prime" notation is used because not all these studies provide enough detail to determine  $\lambda$  and  $S_{o}$ . Specifically,  $S'_{o}$  is  $d\ln R/d\ln N_{a}$  in Jiang et al. (2010) and  $\lambda'$  is  $d\ln LWP/d\ln N_{d}$  in Berner et al. (2011). For all other references,  $\lambda' = \lambda$  and  $S'_{o} = S_{o}$ . The thin dashed line shows the linear relationship determine by Wang et al. (2012) for the  $\lambda - S_{pop}$  relationship.





**Figure 2.** Mean (solid) and median (dashed) rain rates for the 3 rain rate thresholds, i.e.,  $T_h$  of 0.001 (gray), 0.5 (blue), and 5 (red) mm day<sup>-1</sup> for four different aerosol loadings. The shaded region encompasses the 10th percentile to the 90th percentile. *R* is depicted as equal to to  $T_h$  for the first hour as a reference point for the minimum *R* that is possible under each  $T_h$  condition.





Figure 3. As in Fig. 2 except for the RICO case (the model output is from Jiang et al., 2010).





**Figure 4.** Scatterplot of  $\lambda$  (and  $A_{\rm f}$ , right axis) vs.  $S_{\rm pop}$  for thresholds  $T_{\rm h}$  of **(a)** 0.001, **(b)** 0.5, and **(c)** 5 mm day<sup>-1</sup>. These thresholds are representative of the set of 10 thresholds analyzed. Here, the following colors denote changes in  $N_{\rm a}$  from 25 mg<sup>-1</sup> to 50 mg<sup>-1</sup> (black), 75 mg<sup>-1</sup> (red), and 100 mg<sup>-1</sup> (blue) for the DYCOMS-II case. The symbols signify the control (solid circles), Hi-LHF (open circles), Lo-LHF (crosses), Lo-CC (open squares), and Hi-CC (open triangles) simulations. Note that not all symbols appear, especially for larger changes in  $N_{\rm a}$  and high threshold values because for those conditions no points met the criterion for calculating  $\lambda$  and/or  $S_{\rm pop}$ . The thin dashed line shows the linear relationship determined by Wang et al. (2012) for the  $\lambda$ - $S_{\rm pop}$ , i.e., 0.12 (Wang et al., 2012).











**Figure 6.** As in Fig. 4 except for  $\lambda$  vs.  $S_{o, mod}$ , i.e., where the denominators of the x- and y-axes are the same. The vertical dashed line corresponds to the surface remotely measured value of  $S_{o, mod}$ , i.e., 0.66 (Mann et al., 2014).





**Figure 7. (a)**  $\lambda$  (and  $A_{\rm f}$ ) vs.  $S_{\rm pop}$ , **(b)**  $\lambda$  vs.  $S_{\rm pop, \, mod}$ , and **(c)**  $\lambda$  vs.  $S_{\rm o, \, mod}$  for the RICO simulations from Jiang et al. (2010). The colors correspond to increasing  $N_{\rm a}$  from 100 mg<sup>-1</sup> to 200 (black), 300 (red), 400 (blue), and 500 (green) cm<sup>-3</sup>. The symbols denote the different thresholds used to conditionally average R and POP, i.e.,  $T_{\rm h} = 0.001$  (closed circle), 0.5 (downward pointing triangle, and 5 (diamond) mm day<sup>-1</sup>. In **(a)**, the thin dashed line shows the linear relationship determined by Wang et al. (2012) for the  $\lambda$ - $S_{\rm pop}$  relationship and the vertical dashed line corresponds to **(a)** the satellite-measured value of  $S_{\rm pop}$ , i.e., 0.12 (Wang et al., 2012) and **(c)** the surface-based estimate of  $S_{\rm o, \, mod}$ , i.e., 0.66 (Mann et al., 2014).





**Figure 8.**  $N_d$  relative to  $N_d$  for the lowest aerosol number concentration scenario (i.e.,  $N_{d,0}$ ) for both the **(a)** RICO and **(b)** DYCOMS-II RF02 simulations. Doubling (red), tripling (blue), quadrupling (green), and quintupling (orange)  $N_a$  are depicted for both sets of simulations. corresponding to  $N_a = 200$ , 300, 400, and 500 cm<sup>-3</sup> relative to 100 cm<sup>-3</sup>, respectively, for RICO and  $N_a = 50$ , 75, 100, and 125 mg<sup>-1</sup> relative to 25 mg<sup>-1</sup>, respectively, for DYCOMS-II RF02.





**Figure 9.** Schematic representation of the results presented herein. The red (blue) curve corresponds to the trajectory in the  $\lambda$ - $S_{pop}$  parameter space for increasing changes in  $N_a$  (i.e.,  $\Delta N_a$ ) in marine stratocumulus (trade-wind cumulus). The dotted region corresponds to the area of the parameter space where further increases in  $S_{pop}$  result in smaller changes in  $\lambda$  due to entrainment effects. The dashed region corresponds to the area in which the cloud microphysical characteristics asymptote to nearly constant values for larger  $\Delta N_a$ . The crossed area represents the region in which  $\lambda$  changes rapidly relative to small changes in  $S_{pop}$ .

