

1 **Observation and a numerical study of gravity waves during**  
2 **tropical cyclone Ivan (2008).**

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4 **Fabrice Chane Ming<sup>1</sup>, Chouaibou Ibrahim<sup>1</sup>, Christelle Barthe<sup>1</sup>, Samuel Jolivet<sup>2</sup>,**  
5 **Philippe Keckhut<sup>3</sup>, Yuei-An Liou<sup>4</sup> and Yuriy Kuleshov<sup>5,6</sup>**

6 [1] {Université de la Réunion, Laboratoire de l'Atmosphère et des Cyclones, UMR 8105,  
7 UMR CNRS-Météo France-Université, La Réunion, France}

8 [2] {Singapore Delft Water Alliance, National University of Singapore, Singapore,  
9 Singapore}

10 [3] {Laboratoire Atmosphères, Milieux, Observations Spatiales, UMR 8190, Institut Pierre-  
11 Simon Laplace, Université Versailles-Saint Quentin, Guyancourt, France}

12 [4] {Center for Space and Remote Sensing Research National Central University, Chung-Li  
13 3200, Taiwan}

14 [5] {National Climate Centre, Bureau of Meteorology, Melbourne, Australia}

15 [6] {School of Mathematical and Geospatial Sciences, Royal Melbourne Institute of  
16 Technology (RMIT) University, Melbourne, Australia}

17 Correspondence to: F. Chane Ming (fchane@univ-reunion.fr)

18

19 **Abstract**

20 Gravity waves (GWs) with horizontal wavelengths of 32-2000 km are investigated during TC  
21 Ivan (2008) in the south-west Indian ocean in the upper troposphere (UT) and lower  
22 stratosphere (LS) using observational datasets, radiosonde and GPS radio occultation data,  
23 and numerical modelling, ECMWF analyses and simulations of French numerical model  
24 Meso-NH with vertical resolution of  $\sim 150$  m near the surface and 500 m in the UT/LS.  
25 Observation reveal dominant low-frequency GWs with short vertical wavelengths of 0.7-3  
26 km, horizontal wavelengths of 80-400 km, periods of 4.6-13 h in the UT/LS. Continuous  
27 wavelet transform and image processing tools highlight a wide spectrum of GWs with  
28 horizontal wavelengths of 40-1800 km, short vertical wavelengths of 0.6-3.3 km and periods

1 of 20 min-2 days from modelling analyses. Both ECMWF and Meso-NH analyses are  
2 consistent with radiosonde and GPS radio occultation data showing evidence of a dominant  
3 TC-related quasi-inertia GW propagating eastward east of TC Ivan with horizontal and  
4 vertical wavelengths of 400-800 km and 2-3 km respectively in the LS, more intense during  
5 TC intensification. In addition, MesoNH model produces realistic detailed description of TC  
6 dynamics, some high-frequency GWs near the TC eye, variability of the tropospheric and  
7 stratospheric background wind and TC rainband characteristics at different stages of TC Ivan.  
8 A wavenumber-1 vortex Rossby wave is suggested as a source of dominant inertia GW with  
9 horizontal wavelengths of 400-800 km while shorter scale modes (100-200 km) located at  
10 north-east and south-east of the TC could be attributed to strong localized convection in spiral  
11 bands resulting from wavenumber-2 vortex Rossby waves. Meso-NH simulations also reveal  
12 GWs-related clouds east of TC Ivan.

13

14

## 15 **1 Introduction**

16 Mesoscale organized convective systems such as tropical cyclones (TCs) have been known as  
17 intense sources of low-frequency convective gravity waves (GWs). Observations reveal that  
18 such GWs have horizontal wavelengths of 10-2000 km, vertical wavelengths of 1-6 km and  
19 periods of 1 hour-2.5 days in the upper troposphere (UT) and lower stratosphere (LS) above  
20 TC basins (Pfister et al., 1993; Sato et al., 1993; Chane Ming et al., 2002, 2010; Dhaka et al.,  
21 2003; Niranjana Kumar et al., 2011; Das et al., 2012). Recently, using radiosonde data, Chane  
22 Ming et al. (2010) also demonstrated a possible correlation between daily maximum surface  
23 wind speed and total energy density of inertia GWs produced by intense TCs Dina and Faxai  
24 in the UT/LS. Ibrahim et al. (2010) extended this study analysing a climatology of 10 TC  
25 seasons (1997/1998–2006/2007) and radiosonde data obtained at Tromelin Island (15.53° S,  
26 54.31° E) located in the south-west Indian ocean (SWIO). Results suggest a possible linear  
27 relationship between weekly GW total energy density in the LS and cyclone-days of intense  
28 TCs in the SWIO.

29 Non-orographic GWs triggered by deep convection play an important role in tropical  
30 dynamics (Piani et al., 2000; Lane and Reeder, 2001), in particular in the quasi-biennial  
31 oscillation (Baldwin et al., 2001) and the mesopause semi-annual oscillation (Dunkerton,  
32 1982) in the equatorial region. As various source mechanisms of such intermittent small-scale

1 waves are not clearly understood, observations as well as high-resolution mesoscale  
2 numerical modelling are needed to improve parameterizations of such unresolved processes in  
3 weather forecasting and climate models (Kim et al., 2003; Alexander et al., 2010). In  
4 particular, GW drag parameterizations fail to represent correctly non-orographic GWs  
5 produced by convection in general circulation models because of wide spectrum of GW  
6 frequencies, phase speeds, and spatial scales depending on properties of convection and the  
7 environment (Richter et al., 2010). Thus GW drag parameterizations require a set of  
8 observations of source properties covering a wide spectral range to constrain tunable  
9 parameters for realistic global behavior of both orographic and non-orographic GWs through  
10 GW momentum fluxes (Alexander, 2003; Fritts and Alexander, 2003). Therefore  
11 implementation of GW momentum flux parameterizations dedicated to specific convective  
12 source processes in Global Climate Models (GCMs) is a current research topic (Ern and  
13 Preusse, 2012). For example, Kim and Chun (2005) suggested a computationally efficient  
14 non-orographic GW parameterization scheme producing reasonably accurate variation of  
15 the momentum flux generated by convective heat sources for global atmospheric  
16 prediction models in the middle atmosphere.

17 Presently, prediction of TC intensification is limited by our understanding of TC structure and  
18 multi-scale interaction inside and with the environment. Wave processes, especially in the  
19 inner core dynamics, and their relationship with spiral rainbands are not fully understood.  
20 Recent numerical studies suggest that weakening of simulated TCs is closely associated with  
21 environmentally induced asymmetries that develop in the vicinity of the TC eyewall (Wu and  
22 Braun, 2004). Movement of storm through the surrounding atmosphere and the wind shear are  
23 major causes of an asymmetric distribution of rainband structures (Reasor et al. 2000; Houze,  
24 2010). In a low shear environment, rainfall is mainly ahead of a storm, especially in the outer  
25 rainband regions otherwise it is located downshear left (right) in the northern (southern)  
26 hemisphere (Wu and Braun, 2004). When TC intensity increases, the asymmetry maximum  
27 shifts upwind to the left in the northern hemisphere.

28 Indeed, sources of GWs and effects on TC structure still remain an open debate (Chow and  
29 Chan, 2003; Schubert et al., 2007; Schechter, 2008; Hendricks et al., 2008). Current  
30 sophisticated mesoscale numerical models showed evidence of GWs in the inner core and  
31 rainbands in high resolution simulations (Liu et al., 1999; Zhang et al., 2000, 2002; Lin et al.,  
32 2011). In resolving explicitly convection, mesoscale numerical models such as MM5 (Fifth-

1 Generation NCAR/Penn State Mesoscale Model PSU/NCAR Mesoscale Model) and AR-  
2 WRF (Advanced Research-Weather Research and Forecasting) proved to be useful  
3 numerical tools to explore the wide spectrum of TC-generated GWs as well as source  
4 mechanisms, propagation and effects on the atmosphere in relation with evolution of the TC  
5 dynamics (Kuester et al., 2008; Kim and Chun, 2010). Simulation of TC Saomai (2006)  
6 suggested significant momentum deposition in the UT/LS by GWs with short dominant  
7 horizontal wavelengths (20–100 km) and frequencies (0.3–2 h) and possible impact on the TC  
8 development through the modification of the tropospheric vertical wind shear (Kim and Chun,  
9 2011). At now, three major mechanisms, i.e. mechanical oscillator effect (Fovell et al. 1992),  
10 obstacle effect (Clark et al., 1986), and thermal heating effect (Salby and Garcia, 1987) are  
11 proposed to explain generation of convective GWs.

12 The present study aims at exploring GWs within a wide range of horizontal scales (32-2000  
13 km) during TC Ivan (2008) in the SWIO using French mesoscale numerical model Méso-NH  
14 with a large single horizontal domain, an horizontal grid size of 4 km and explicit deep  
15 convection. Characteristics of dominant GWs and their evolution are analyzed depending on  
16 TC stages using observational datasets (radiosondes, GPS radio occultation data), ECMWF  
17 analyses and Méso-NH simulations. In particular, TC-related GWs and processes generated  
18 the waves are investigated during TC intensification. In regards with TC-related GWs, the  
19 evolution and role of spiral rainbands are also briefly addressed.

20

## 21 **2 Overview of tropical cyclone Ivan (2008)**

22 Developing from a disturbed area of convection with a sustained monsoon flux in the lower  
23 layers, the system became well-organized northeast of Madagascar on 6 February 2008. Due  
24 to a rapid intensification favored by the passage of a tropopause anomaly above, it reached a  
25 stage of moderate tropical storm on 7 February. Moving south-eastward, the system oscillated  
26 between stages of moderate tropical storm and strong tropical storm on 11 and 12 February. It  
27 reversed course from 9 to 12 February, making a complete loop and turning to the west-south-  
28 west after 14 February. Encountering new favorable conditions after 14 February, the system  
29 re-intensified to a TC stage as it passed over Tromelin Island on 15 February. Then TC Ivan  
30 continued moving towards the west-southwest at an average speed of 8 knots ( $4.1 \text{ ms}^{-1}$ ),  
31 becoming a threat to the northeast coast of Madagascar. TRMM PR captured tall convective  
32 activity with high values of reflectivity (30 dBz) at 10-11 km heights on 16 February at 06:21

1 UTC. Tall towers, elevated up to about 13 km height, were observed in the concentric inner  
2 eyewall and in TC spiral rainbands at the beginning of its intensification. Figure 1a shows  
3 satellite observation of TC Ivan at the beginning of the intense stage of development on 16  
4 February at 00:00 UTC. Minimum central pressure of 920 hPa and 10-minute averaged  
5 maximum sustained winds of 105 knots ( $54 \text{ ms}^{-1}$ ) were reported on 16 February at 06:00 UTC  
6 (Fig. 1b). Figures 1c and 1d show evidence of a wavenumber-1 asymmetry characterized by  
7 an increase (a decrease) of convection close to the eyewall in the north-eastern (south-  
8 western) quadrant of the TC on 16 February at 16:30 UTC and 17 February at 00:00 UTC  
9 respectively. Eyewall asymmetries are common feature for TCs and are now considered to be  
10 crucial for understanding internal dynamics and variability of TC intensity (Hendricks et al.,  
11 2012). Using airborne Doppler radar, Marks et al. (1992) investigated the nature of the  
12 altitude-varying wind asymmetry of TC Norbert (1984). The asymmetry perturbations were  
13 characterized as a source-sink field at 1 km heights and a vortex couplet above 3 km heights  
14 (Marks et al., 1992; Liu et al., 1999). Indeed, most of this asymmetry of TC Olivia (1994)  
15 could be explained by the azimuthal variance of wavenumber-1 above 3 km height (Reasor et  
16 al., 2000).

17 On 17 February at 04:00 UTC, TC Ivan passed over Sainte Marie Island and then it made a  
18 landfall in the north of Madagascar at 06:00 UTC with maximum sustained winds of 95 knots  
19 ( $48.9 \text{ ms}^{-1}$ ) and a minimum central pressure of 935 hPa (Fig. 1d). It rapidly weakened into a  
20 remnant low pressure area as it crossed Madagascar. It regenerated over the Mozambique  
21 Channel into a tropical depression from 19 February before dissipation on 22 February. Best  
22 track data of TC Ivan from 13 February until its landfall in Madagascar are presented in  
23 Figure 2.

24

### 25 **3 Data and methodology**

26 Characteristics of GWs are derived using upper air data obtained by GPS radiosondes  
27 launched at meteorological stations of Gillot ( $20.9^{\circ}\text{S}$ ,  $55.5^{\circ}\text{E}$ ) at La Reunion Island and Ivato  
28 ( $18.9^{\circ}\text{S}$ ,  $47.8^{\circ}\text{E}$ ) at Antananarivo in Madagascar, FORMOSAT-3/COSMIC GPS RO dataset  
29 within the area encompassed by longitudes between  $48^{\circ}\text{E}$  and  $68^{\circ}\text{E}$  and latitudes between  
30  $10^{\circ}\text{S}$  and  $22^{\circ}\text{S}$ , and ECMWF analyses during TC Ivan in February 2008 (Fig. 2). From 5  
31 February to 27 February, 23 GPS radiosondes were launched daily at 11:00 UTC at the airport  
32 of Gillot (21 m altitude). Vertical profiles of temperature and horizontal wind with 100 m

1 resolution reached the mean altitude of 23 km. Radiosonde data quality and accuracy are  
2 described in Chane Ming et al. (2002, 2007, 2010) and Ibrahim (2010) which used similar  
3 vertical profiles to characterize GWs in the UT/LS. At Ivato airport (389 m altitude), 40 GPS  
4 radiosonde profiles were obtained twice a day at 00:00 and/or 09:00 and/or 12:00 UTC with a  
5 vertical resolution of 300 m and a mean maximum altitude of 23 km.

6 The FORMOSAT-3/COSMIC (Formosa Satellite Mission-3/Constellation Observing System  
7 for Meteorology, Ionosphere, and Climate) dataset from the COSMIC Data Analysis and  
8 Archive Center (CDAAC) consists of 70 daily soundings of temperature between 2 and 40 km  
9 altitude over the SWIO between 13 and 18 February 2008. Vertical profiles have high  
10 accuracy for temperature ( $< 1$  K from 5 km to 25 km) and spatial resolution varying from 100  
11 m at the surface to 1.5 km at 35 km altitude (1 km at the tropopause) (Pirscher et al., 2010;  
12 Anthes, 2011). Collocation mismatch affects the comparison: standard deviation errors are  $<$   
13 0.5 K for temperature in both the troposphere (850–200 hPa) and stratosphere, and for relative  
14 humidity are  $< 3.5\%$  for 3 h temporal buffer and 100 km spatial buffer (Sun et al., 2010;  
15 Zhang et al., 2011). GPS RO data observed by low-earth-orbit satellites have been used  
16 previously for GWs observations in the LS (Tsuda et al., 2000; Liou et al., 2003; 2006). A  
17 comprehensive introduction to the RO method for remote sensing of the atmosphere and  
18 ionosphere is presented by Liou et al. (2010). COSMIC GPS RO profiles recently have been  
19 analyzed to describe monthly global stratospheric GW energy densities (Alexander et al.,  
20 2008; Xiao and Hu, 2010).

21 In the present study, vertical velocities are extracted from 6 hourly ECMWF ERA-40  
22 operational analyses of T150  $1.125^\circ \times 1.125^\circ$  spectral resolution for the analysis of GWs in  
23 the UT/LS. Mountain and jet-stream-forced GWs have been previously derived from  
24 ECMWF data (Plougonven and Teitelbaum, 2003; Schroeder et al., 2009). Indeed current  
25 operational numerical weather prediction models (NWP) are likely to resolve explicitly a  
26 large fraction of the observed stratospheric inertia-gravity wave spectrum with horizontal  
27 wavelengths of 100–1000 km and probably even longer in the tropics (Shutts and Vosper,  
28 2011). Nevertheless, vertical resolution still remains insufficient to capture quasi-inertia wave  
29 energy with vertical wavelengths  $< 2$  km. In addition, high-quality temperature information in  
30 ECMWF data are provided in the UT/LS, more particularly in the southern hemisphere, ever  
31 since the assimilation of GPS RO bending angles beginning in late December 2006 (Healy

1 and Thepaut, 2006; Healy, 2007). Thus several studies proved that TC simulations are also  
2 improved in NWP models (Huang et al., 2010; Kunii et al., 2012; Liu et al., 2012).

3 Second- and third-order polynomial fits are applied to GPS radiosonde vertical profiles of  
4 temperature and wind respectively, using a cubic spline interpolation, and subtracted from the  
5 100-m resampled vertical profiles to derive temperature and wind perturbations induced by  
6 GWs. Conventional methods described in Chane-Ming et al. (2010) are applied to vertical  
7 profiles of temperature and wind perturbations to extract GW parameters such as energy  
8 densities and spectral characteristics. Radiosonde and GPS RO profiles explore low-  
9 frequency GWs with short vertical wavelengths limited by vertical height ranges in the  
10 UT/LS (Alexander and Barnet, 2007; Chane Ming et al., 2010). In addition the observational  
11 filter of GPS RO measurements sets the lower limit of periods at 2 h (Preusse et al., 2008).

12 One- and two-dimensional Fast Fourier Transforms (FFT) and Morlet continuous wavelet  
13 transform (CWT) together with other image processing tools are used to visualize dominant  
14 GWs and to extract spectral characteristics of GWs from GPS RO vertical perturbation  
15 profiles, ECMWF analyses and Meso-NH outputs. Second-order spectral parameters are  
16 derived from the linear relation of GW dispersion.

17

## 18 **4 Numerical experiment**

### 19 **4.1 Model description**

20 The non-hydrostatic Mesoscale model Meso-NH (Lafore et al., 1998) is used in this study to  
21 simulate development of TC Ivan from 13 to 18 February. The research model has been  
22 jointly developed by the Centre National de Recherches Météorologiques (Centre National de  
23 la Recherche Scientifique/Météo-France) and Laboratoire d'Aérodynamique (Centre National de la  
24 Recherche Scientifique/Université Paul Sabatier). In previous studies, the model proved to be  
25 useful for the simulation of cyclone development. Nuissier et al. (2006) studied a mature stage  
26 of category 4 TC Bret (1999) in the North Atlantic basin with the Meso-NH non-hydrostatic,  
27 two-way interactive, quadruple-nested grid mesoscale model initialized with airborne Doppler  
28 radar and dropsonde data. Leclaire De Bellevue et al. (2007) focused on tropospheric ozone  
29 enhancement at the periphery of TC Marlene in the SWIO. Recently orographic influence of  
30 La Réunion Island on the structure and evolution of TC Dina (2002), described in Roux et al.  
31 (2004), was numerically examined in Jolivet et al. (2013). Particularly, PV estimates revealed

1 that buoyancy waves were generated on the lee side of the island's peak (3070 m), when  
2 peripheral cyclonic flow of the TC hits the island.

3 The present model configuration consists of a single domain with 360 x 600 horizontal grid  
4 points (4 km resolution) in order to study GWs with horizontal wavelengths between 32 km  
5 ( $8\Delta x$ ) (Lane and Knievel, 2005) and 1200-2400 km. The chosen horizontal resolution is in the  
6 grey-zone regarding the representation of convection (Yu and Lee, 2010). But it is a good  
7 compromise for explicit convection to reproduce detailed structures of mesoscale convective  
8 systems in TCs (Klemp, 2006). Liu et al. (1999) and Lac et al. (2002) simulated convective  
9 GWs with short horizontal wavelengths of 15-80 km with MM5 and Meso-NH models with  
10 grid sizes of 6 km and 5 km respectively.

11 Fifty-five vertical levels are used from the surface to 29 km altitude with a damping layer at  
12 25 km. Vertical resolution is higher at the surface (60 m) for surface flux processes. It  
13 becomes gradually coarser in the middle troposphere about 1 km at heights of 6-7 km in the  
14 middle troposphere and ~ 500 m at heights between 10 and 24 km in the UT/LS.

15 The simulation started at 0000 UTC on 13 February 2008 with a time step of 15 s, when TC  
16 Ivan began moving to the southwest in the direction of Tromelin and Madagascar and ended  
17 at 2100 UTC on 18 February 2008 after its landfall in Madagascar. Thus, the intensification,  
18 mature stage and dissipation of TC Ivan are reproduced in the simulation.

19 Aladin-Réunion analyses were used to initialize Meso-NH and to feed the lateral boundary  
20 conditions which were updated every 6 hours. Aladin-Réunion is a limited area model used  
21 by Météo-France for TC forecasting in the SWIO at 9.6-km horizontal resolution since 2006  
22 (Montroty et al., 2008). Then, it better represents TC structure in comparison with global  
23 models so that no bogus is used in this model. Physics of the model includes a mixed-phase  
24 microphysics scheme (Pinty and Jabouille, 1998), and a 1D turbulence scheme (Cuxart et al.,  
25 2000). Shallow convection is parameterized with the scheme of Kain and Fritsch (1990)  
26 adapted by Bechtold et al. (2001). The same scheme is used for simulation of deep convection  
27 to the resolution of 5 km. At this resolution and below, deep convection is explicitly resolved  
28 by the model. The radiative scheme is the one used at ECMWF (Gregory et al., 2000).

29



## 1 **4.2 Validation of simulated TC Ivan track**

2 A simulated track is compared with best track data prepared by Météo-France Regional  
3 Specialized Meteorological Centre (RSMC) La Réunion (Fig. 2). TC categories used for  
4 classification of TC intensity by the RSMC La Reunion are based on 10-minute average  
5 maximum sustained winds. After a 24 hour spin-up, a track of TC Ivan is well represented in  
6 the model. At the beginning of the simulation, the system moved to the northwest before  
7 heading toward Madagascar. This simulated track becomes more consistent with the observed  
8 track from the TC intensification stage to its landfall in Madagascar. A position error of less  
9 than 50 km is observed during the intense phase of TC Ivan (from 16 February at 0000 UTC  
10 to 17 February at 2100 UTC) compared with best track data. A simulated landfall on Sainte  
11 Marie Island occurred with a delay of 3 hours. A TC tracker algorithm is based on detecting  
12 minimum pressure with a location uncertainty of about 10 km. Evolution of the maximum  
13 sustained windspeed and minimum central pressure is illustrated in Figure 3. In the model  
14 simulation, the TC intensity is slightly underestimated during the cyclone's mature stage. The  
15 minimum central pressure (maximum sustained winds speed) decreases (increases) to a  
16 minimum (maximum) of 940 hPa ( $53 \text{ m s}^{-1}$ ) until 16 February. The simulated parameters are  
17 in good agreement with the observations after the spin-up phase.

18 Synthetic brightness temperatures corresponding to the Meteosat Second Generation (MSG)  
19 observations in the infrared channels were computed from MesoNH outputs using the  
20 Radiative Transfer for Tiros Operational Vertical Sounder (RTTOV) code version 8.7  
21 (Saunders et al., 2005), and compared with observations (Chaboureau et al., 2000). Brightness  
22 temperatures observed with Meteosat-7 and computed from Meso-NH outputs on 16 February  
23 2008 at 0000 UTC for the intense stage of TC Ivan are presented in Figure 4. Meso-NH  
24 reproduces a TC eye characterized by a zone of high brightness temperature in the centre of  
25 TC Ivan (218 K for Meteosat-7 and 214 K for Meso-NH). An asymmetry of the system is  
26 well represented with an area of more intense convection in the northeastern quadrant  
27 characterized by low values of brightness temperature (192 K and 190 K for observations and  
28 Meso-NH, respectively). This area is more extended for the Meso-NH simulation at this time.

29 Simulated temperature and wind fields on 15 and 16 February at 00:00 UTC in the outer  
30 region of the storm are also examined. Both radiosonde and GPS RO vertical profiles of  
31 temperature are quite consistent with simulated fields of the environment in the troposphere at  
32 altitudes between 1 km and 25 km with relative mean errors  $<1.5\%$  at distance of 650 and 825

1 km from the centre of TC Ivan, respectively (Fig. 5a). A general behavior of temperatures is  
2 correctly simulated in the outer region of the storm in the troposphere (Fig 5a, 5b).  
3 Differences observed in mean temperature above 20 km at distance of 650 km do not affect  
4 GWs on profiles of temperature perturbations below 20 km altitudes (Fig. 5a). In addition,  
5 variations of mean simulated horizontal winds (Fig. 5c, d) are observed to be in good  
6 agreement with observed wind fields (mean relative error of about 5%) at altitudes between 5  
7 km and 25 km. Vertical behavior of mean horizontal wind affects vertical propagation of  
8 GWs in the UT/LS through critical level filtering.

9 Consequently, track, intensity and structure as well as the outer environment of TC Ivan are  
10 well-simulated by Meso-NH for a realistic study of GWs.

11

## 12 **5 Characteristics of GWs**

### 13 **5.1 Radiosonde and GPS Radio Occultation (RO) data**

14 Spectral characteristics of GWs with short vertical wavelengths (0.6-4 km) are first derived in  
15 the UT (10-15 km) and LS (18-22 km) from radiosonde dataset during TC stage of Ivan from  
16 15 to 18 February using conventional methods (Table 1). Altitude range of radiosonde data in  
17 the LS above Ivato limits the study to the UT. Low-frequency GWs are observed with shorter  
18 periods in the UT (4 h, 6-8 h) than in the LS (13 h). GWs have short dominant vertical  
19 wavelengths of 1-2.6 km and horizontal wavelengths of 70-210 km in the UT. Horizontal  
20 wavelengths are <400 km in the LS above Gillot. Rotary spectral analyses provide dominant  
21 eastward horizontal direction of GW propagation ( $40^{\circ}$ - $70^{\circ}$  from North) in the UT and LS  
22 from 16 to 18 February above Gillot. Horizontal phase speeds of  $3.58 \text{ ms}^{-1}$  and  $10.75 \text{ ms}^{-1}$  are  
23 estimated for horizontal wavelengths of 130 and 390 km respectively in the LS from 16 to 18  
24 February. A maximum upward energy of 70% in both the UT and the LS suggests that  
25 dominant sources of observed GWs are mostly located below 10 km. Upward energy peaks at  
26 58-70% in the UT during landfall after the passage of the TC above Ivato. Thus, different  
27 processes might be involved in the generation of GWs above the two meteorological stations  
28 before and after landfall (Chane Ming et al., 2002, 2010).

29 Daily dominant vertical wavelengths < 5 km with periods > 2 h are computed from 70 profiles  
30 of GPS RO data from 13 to 18 February in the UT (10-15 km) and the LS (18-24 km). A  
31 dominant vertical wavelength of 3 km is observed during the whole period in the UT and LS

1 above the SWIO basin, especially east of TC Ivan (Fig. 6). In the LS, energy intensity of the  
2 3-km vertical mode is larger from the intensification to landfall of TC Ivan (from 15 to 18  
3 February) and maximal during TC intensification on 16 February. The opposite is observed in  
4 the UT. The contrast between UT and LS is consistent with climatological observations of  
5 GW activity during TC seasons (Ibrahim et al., 2010).

6 Vertical wavelengths of collocated profiles of GPS RO temperature fluctuations and  
7 radiosonde data (distance <100 km and time <3 h) on 15 and 16 February at Gillot and Ivato  
8 are examined. A dominant mode of 3-km vertical wavelength is observed in radiosonde and  
9 GPS RO profiles in the UT/LS on 15 February above Gillot (Fig. 7). Better vertical resolution  
10 of radiosonde data at Gillot enables observation of smaller vertical wavelengths of ~700 m in  
11 the LS. A dominant mode with a vertical wavelength of 1.6 km in the LS is also present on  
12 FFT spectra above Ivato. GWs have a broader spectrum of vertical wavelengths > 1km above  
13 Ivato located in an orographic region. In addition, FFT energy is more intense both in the UT  
14 and the LS above Gillot in contrast to that above Ivato located ahead of TC Ivan, especially in  
15 the UT.

16 In conclusion, radiosonde and GPS RO profiles show evidence of consistent observations of  
17 low-frequency GWs. Dominant GWs with vertical wavelengths of 0.7-1.6 km and 2-3 km are  
18 observed in the UT/LS above Gillot and Ivato during TC Ivan. In addition they reveal the  
19 presence of an inertia GW with vertical wavelength of 2-3 km, horizontal wavelength of ~  
20 400 km, period of 13 h east of TC Ivan in the LS. It propagates eastward in the LS. Its  
21 intensity is larger east of the TC and peaks during TC intensification.

22

## 23 **5. 2 ECMWF analyses**

24 A spatial high-pass bi-directional 2D-filter, a separable eight-neighbor Laplacian (Pratt,  
25 2001), is applied on vertical velocity derived from ECMWF analyses for edge detection of  
26 wavelike patterns. Filtered vertical velocity shows evidence of semi-circular waves with a  
27 dominant horizontal wavelength of about 600 km east of TC Ivan which are visualized within  
28 a distance as far as four times the horizontal wavelength (2500 km) at 21 km altitude in the  
29 LS on 16 February 2008 (Fig. 8a). More intense and concentric similar patterns in the UT at  
30 13-km altitude during the intensification of TC Ivan are indicative of background wind  
31 filtering above 13 km (cf. wind reversal in Fig. 5c) for westward propagating modes with  
32 horizontal wavelengths of about 600 km and the location of GW sources in the UT. The

1 centre of concentric patterns is located in the northwestern side at a distance of 350 km from  
2 the TC centre (16.5°S, 53°E).

3 In Figure 8b, a FFT analysis of vertical velocity at latitudes of the TC centre (16.5°S) and  
4 observed GWs (9-21°S) also reveals presence of other wavelike structures with horizontal  
5 wavelengths of 460 km, 860 km, 1100 km and 1700 km, for which spectral peaks are  
6 maximum at latitudes close to TC centre. The horizontal wavelength-latitude diagram clearly  
7 indicates that most of energy distribution is located at latitudes between 7°S and 21°S (Fig.  
8 8c). A line of symmetry is at latitudes of about 14-16°S. Waves with long horizontal  
9 wavelengths of 1400-1700 km are observed only at latitudes of 15-16.5°S where as those with  
10 horizontal wavelengths of about 600 km are dominant at a distance of about 300 km from the  
11 TC eye.

12 CWT is applied to the vertical velocity at the latitude of the TC eye to locate observed  
13 horizontal modes (Chane-Ming et al., 1999). Longitude-horizontal wavelength distribution  
14 derived from CWT modulus shows evidence of modes with 350-1000 km horizontal  
15 wavelengths peaking at ~ 550 km at latitude of 61°S east of TC Ivan (Fig. 8d). A dominant  
16 mode of about 800 km horizontal wavelength is present ahead of the TC eye. In addition  
17 CWT diagram reveals the possible presence of a longer mode with 1700 km horizontal  
18 wavelength ahead of TC Ivan.

19 The observed phase relations between perturbation zonal, meridional, and vertical winds and  
20 temperature at latitude of 16.5°S agree with linear gravity wave theory for the dominant  
21 observed GWs (Gill, 1982). The ratio between CWT modulus of horizontal wind  
22 perturbations is computed for the continuous spectrum of GWs with horizontal wavelengths  
23 between 350 km and 1000 km to determine the intrinsic period from equation 1 in Chane  
24 Ming et al. (2002). Mean periods of 14 h and 12.8 h are obtained for the whole area and east  
25 of TC eye respectively. The ratio between CWT modulus of zonal and vertical wind  
26 perturbations provides vertical wavelengths of 1-2 km for the dominant mode of 600 km  
27 horizontal wavelength and 12.8 h period. Mean horizontal and vertical observed phase speeds  
28 are estimated of about  $13 \text{ ms}^{-1}$  and  $-0.04 \text{ ms}^{-1}$  respectively. A mean period of 1-1.8 days is  
29 obtained for GWs with horizontal wavelengths between 1400 km and 1700 km with a  
30 dispersive vertical wavelength of 4-10 km. Such periods correspond to inertial periods for  
31 latitudes between 5°S and 15°S. Mean horizontal and vertical phase speeds vary between 10  
32  $\text{ms}^{-1}$  and  $20 \text{ ms}^{-1}$  and between  $-0.03$  and  $-0.08 \text{ ms}^{-1}$  respectively.

1 Both FFT and CWT distribution suggest that winds have a directional filtering effect on  
2 propagation of TC-induced GWs from the UT to the LS.

3 Finally, observations of circular patterns are consistent with previous studies on GWs  
4 triggered by convective turrets (Dewan et al. 1998; Piani et al., 2000; Lane and Reeder, 2001;  
5 Horinouchi et al., 2002). ECMWF analyses also support that TC-related convection produces  
6 a large spectrum of low-frequency GWs in the UT/LS. In particular a dominant mode of  
7 horizontal and vertical wavelengths of 600 and 1-2 km respectively and 12.8 h period is  
8 observed east of the TC with an eastward propagation of about  $13 \text{ ms}^{-1}$  favored by the  
9 westward background wind above the tropopause. Estimated vertical wavelength of 1-2 km  
10 might be biased because it is probably not resolved by the ECMWF. Thus, the model  
11 describes mostly the low-frequency part of GW spectrum with horizontal wavelengths of 350-  
12 2000 km in agreement with Shutts and Vosper (2011).

13

### 14 **5.3 Simulated GWs**

15 Vertical profiles of meridional wind perturbations are extracted from the simulation every 10  
16 min to examine small-scale vertical wave activity from 13 February at 00:00 UTC to 18  
17 February at 12:00 UTC above Tromelin Island which is located on the track of TC Ivan (Fig.  
18 9a). A third-order polynomial fit is used to derive vertical profiles of perturbations. Wave  
19 activity with a vertical wavelength of about 2.5-3 km is clearly observed in the UT up to 25  
20 km altitude during the development stage of TC Ivan from 14 to 15 February. The downward  
21 phase progression estimated at about  $-0.08 \text{ ms}^{-1}$  reveals an upward energy propagation of  
22 convective GWs. It suggests that GW sources are located below the UT during the stage of  
23 tropical storm. GW activity increases in the UT at altitudes of 13-15 km and in the lowermost  
24 stratosphere after the passage of TC Ivan over Tromelin Island during TC intensification. A  
25 downward phase progression between  $-0.02$  and  $-0.06 \text{ ms}^{-1}$  is visualized from 16 February.  
26 Amplitudes of simulated horizontal wind perturbations ( $\sim 3\text{-}4 \text{ ms}^{-1}$ ) agree with observation.  
27 The activity weakens during the mature stage and increases in the UT again during landfall on  
28 17 February. Wavelike structures with longer vertical wavelengths of about 3-4 km and a  
29 clear upward phase progression ( $0.06 \text{ ms}^{-1}$ ) are also visualized in the middle troposphere at  
30 altitudes of 5-10 km on late 16 February during the mature stage of the TC. They are more  
31 intense in the afternoon of 17 February during landfall of TC Ivan and on 18 February. Large  
32 GW energy density was observed previously in the UT/LS during intensification of TC Dina

1 (Chane Ming et al., 2010) and landfalls of TC Hudah (2000) over Madagascar and  
2 Mozambique (Chane Ming et al., 2002). Time series of vertical GW momentum flux are  
3 computed with 10-min simulated vertical profiles of horizontal and vertical perturbations and  
4 averaged over height ranges in the UT (12-19 km) and LS (19-25 km) (Sato et al., 1993; Kim  
5 and Chun, 2010). They provide mean values of 0.01 and  $5-6 \times 10^{-4} \text{ N ms}^{-2}$  in the UT and LS  
6 respectively above Tromelin and La Réunion islands. Sato (1993) mentioned a maximum  
7 momentum flux of  $0.04 \text{ N m}^{-2}$  at 20 km during TC Kelly (1987) and Kuester et al. (2008)  
8 estimated an integrated average value of  $8.1 \times 10^{-4} \text{ N m}^{-2}$  in the LS during TC lifetime.

9 Simulated vertical profiles of mean zonal wind at Gillot display strong westward winds above  
10 the surface from 16 February until TC landfall (Fig. 9b). They are accompanied with stronger  
11 eastward zonal wind below the tropopause during TC intensification and landfall where  
12 strong GW activity occurs. Westward wind at 4 km altitude increases during intensification.  
13 Strong westward winds are also visualized above 25 km in the LS during TC intensification  
14 and at 23-25 km altitudes during landfall. Eastward zonal wind, appearing initially in a  
15 shallow layer in the UT, increases in strength during cyclone passage to the north, then  
16 deepens into the middle troposphere after landfall. Figure 9c shows zonal winds at 300 km off  
17 the TC centre increasing from  $0 \text{ m}^{-1}$  to about  $-25 \text{ ms}^{-1}$  and meridional winds varying between -  
18  $5 \text{ ms}^{-1}$  and  $5 \text{ ms}^{-1}$  at altitudes between 16-25 km on 16 February at 0600 UTC. In addition  
19 eastward winds are observed east of the TC centre in the UT where GWs with phase speeds  
20 within the interval of values taken by the wind speed will likely dissipate at critical layers.

21 Indeed, time series of vertical profiles of zonal wind from radiosonde data at Mahe ( $4.66^\circ\text{S}$ ,  
22  $55.53^\circ\text{E}$ ) show the downward propagation of westward QBO winds ( $0.8 \text{ km/month}$ ) from  
23 January to late May 2008 located between 20-22 km altitudes during TC Ivan and the  
24 occurrence of eastward QBO winds above 22 km altitude in agreement with quasi-biennial  
25 oscillation (QBO) index at 30 mb calculated by NOAA/ESRL. Thus GWs with westward  
26 horizontal propagation might be filtered by the westward QBO wind in the LS whereas GWs  
27 with eastward horizontal propagation propagating upward are likely to contribute to the  
28 eastward QBO wind in the LS above 22 km altitude. Using radiosonde observations, Vincent  
29 and Alexander (2000) previously observed energy density maxima during QBO westward  
30 phase for convective GWs with intrinsic periods of 20-25 h, horizontal wavelengths of 200-  
31 2000 km (mean value of 100 km) and horizontal phase speed of about  $10 \text{ ms}^{-1}$  in the LS above  
32 Coco Island ( $12^\circ\text{S}$ ,  $97^\circ\text{E}$ ). Recently, the analysis of SABER/TIMED data supports that QBO

1 winds act as a significant filter in GW propagation depending on the QBO phases (Zhang et  
2 al., 2012). Kawatani et al. (2010) also demonstrated that small-scale GWs play an important  
3 role during the QBO westward phase in the LS.

4 Figure 10 shows the vertical cross section of the vertical velocity at 16°S of TC Ivan on 16  
5 February at 1200 UTC. The eyewall is characterized by strong updrafts with vertical velocity  
6 equal to 5-10 ms<sup>-1</sup> from 1 km altitude up to 15 km altitude. Perturbations with short horizontal  
7 wavelengths < 50 km are embedded on the iso-theta contours close to the area of strong  
8 updrafts on the east side of the TC in the UT. Downdrafts are well-observed in the TC eye,  
9 along the inner eyewall and on the east side of TC Ivan at altitudes of 8-12 km. The shape of  
10 the boundary of cloud also reveals strong convection on the east side of the TC.

11 FFT is applied to 10-min time series of simulated vertical wind perturbations above the three  
12 meteorological stations (Gillot, Ivato, Tromelin) to analyze GW characteristics in the UT (12-  
13 16 km) and the LS (18-25 km) during the three stages of the TC:

- 14 - from 14 February to 15 February during the development stage of the system  
15 (hereafter called P1);
- 16 - from 15 February to 17 February during intensification (hereafter called P2);
- 17 - from 17 February to 18 February at 1200 UTC during the landfall (hereafter called  
18 P3);

19 During P1, periods vary between 20 min to 4 h in the UT/LS above the three sites with  
20 dominant high frequencies of about 20-30 min. During P2, similar periods are observed above  
21 Tromelin and Gillot. Secondary periods of 4-12h are also present in the UT/LS above Ivato.  
22 In contrast, FFT spectra reveal dominant periods between 1h and 12h during P3. Observations  
23 above Tromelin and Gillot are consistent during P1 and P2 because of their location at the  
24 same latitude.

25 During the intense stage of TC Ivan on 16 February 2008, vertical momentum flux increases  
26 in the UT above Tromelin (0.06 Nm<sup>-2</sup>) and Reunion Island (0.08 Nm<sup>-2</sup>).

27 Longitudinal series of horizontal pressure perturbations are filtered by a numeric  
28 monodimensional Butterworth filter to extract dominant GW modes with short (<200 km) and  
29 medium (200-800 km) horizontal wavelengths on 16 February at 1200 UTC at 20 km altitude  
30 (Fig. 11a and 11b). Figure 11a suggests an eastward phase propagation of the mode with 400-  
31 600 km horizontal wavelengths from the area of intense convection located north of the TC

1 eye. Two-dimensional FFT is applied on grayscale image of pressure perturbations at the TC  
2 area (Pratt, 2001). The bi-dimensional wavenumber space enables a multiscale analysis of the  
3 grayscale image and improves filtering from low to high frequencies. The FFT inverse  
4 provides reconstructed grayscale images for dominant modes. Contrast of filtered grayscale  
5 image is enhanced using contrast-limited adaptive histogram equalization (Zuiderveld, 1994).  
6 Figures 11c shows evidence of semi-circular patterns for medium modes. Black pixels in the  
7 upper left corner are attributed to processing side effects. Dominant modes of horizontal  
8 wavelengths of about 100-200 km are present in the south-east and north-east areas  
9 respectively (Fig. 11d). They are produced by strong convection in eastward propagating  
10 convective bands resulting from wavenumber-2 vortex Rossby waves located at northeast and  
11 southwest of the TC eye. FFT spectrum of vertical velocity provides a wide range of  
12 horizontal wavelengths between 20 and 2000 km with peaks at 60 km, 200 km, 500 and 1250  
13 km at the latitude of TC eye in the LS. Mean values at latitudes of 9-21°S reveal that most  
14 energy of observed modes is located at the latitude of TC eye (Fig. 12a). Large FFT  
15 amplitudes are displayed for short-scale waves (20-80 km) at the latitude of TC eye and  
16 longer scale waves (>150 km) above TC area (9-21°S). Waves with 400-500 km horizontal  
17 wavelength are dominant above the TC basin during TC intensification. Figure 12b supports  
18 findings that observed modes are mainly located near the latitudes of TC eye. Long-scale  
19 modes have large latitudinal extension. Figure 12c provides longitude-horizontal wavelength  
20 distribution derived from CWT of vertical velocity at the latitude of TC eye. It also supports  
21 the presence of modes with horizontal wavelengths <2000 km associated with TC Ivan.  
22 Energy of modes with 20-80 km horizontal wavelengths is confined at longitudes of 50-55°E  
23 near the TC eye and locally dominant. It peaks at 64 km horizontal wavelength at the location  
24 of the TC eye. Indeed, high-frequency GWs with horizontal wavelengths 15-50 km and  
25 periods of about 15-20 min, observed during P1 and P2, are expected in the vicinity of strong  
26 convection (Dewan et al., 1998; Lane and Reeder, 2001).

27 Energy of medium-scale modes (100-800 km) with peaks at 150 km and 500 km horizontal  
28 wavelengths are secondary dominant. It is mainly observed east of the TC while energy of  
29 longer modes (1250 km) has an horizontal extension west of the TC. Globally a longitudinal  
30 extension east of the TC is displayed for observed modes. Thus this last figure complements  
31 that of ECMWF outputs especially for modes with horizontal wavelengths of 32-350 km.



1 Similar modes are also observed in the horizontal wind, potential temperature and pressure.  
2 On 16 February at 1200UTC, horizontal wavelengths of GWs range between 40 and 60 km  
3 and between 300 km and 500 km with dominant periods of 12 h and 12-58 h (frequencies of  
4  $1.4 \times 10^{-3} \text{ s}^{-1}$  and  $1.39 \times 10^{-4} \text{ s}^{-1}$ - $3.5 \times 10^{-5} \text{ s}^{-1}$ ). The linear GW dispersion relationship provides  
5 vertical wavelengths of about 1.5 km and 3.3 km respectively.

6 Vertical profiles of zonal and meridional wind perturbations are examined at the location  
7 where GWs are observed on 16 February at 1200UTC (Fig. 11c and 11d). They show  
8 evidence of a simulated vertical wavelength of 2.5-3 km for modes of horizontal wavelengths  
9 of 300-600 km, previously observed on Figure 9a. In addition perturbations only suggest that  
10 modes of 40-60 km horizontal wavelengths have vertical wavelengths  $< 2\text{km}$  because of the  
11 500 m vertical resolution in the LS. Simulated wavelengths are in agreement with estimated  
12 vertical wavelengths.

13 Figure 13 displays a Hovmöller diagram of longitudinal pressure perturbations for modes with  
14 horizontal wavelengths between 200 and 800 km from 16 February at 12UTC to 17 February  
15 at 18UTC at latitude of  $16^\circ\text{S}$ . It reveals an eastward propagation of about  $8\text{-}11 \text{ ms}^{-1}$  for  
16 medium modes in the LS.

17 Finally, Meso-NH provides a realistic detailed description of low-frequency GWs in terms of  
18 perturbation amplitudes and phase relations.

19

## 20 **6 Characteristics of TC rainbands**

21 Spiral rainbands may produce severe rainfall outside the eyewall and play an important role in  
22 changing dynamic structure of TC structure, especially in the formation of concentric  
23 eyewalls (Wang and Wu, 2004; Hence and Houze, 2012). They can be triggered both by  
24 inertia-GWs (Willoughby, 1978) and vortex Rossby waves (Montgomery and Kallenbach  
25 1997). Mechanisms of spontaneous emission of spiral IG waves and impacts on the angular  
26 momentum of TCs through outward spiral rainbands are discussed in Chow et al. (2002),  
27 Chow and Chan (2003) and Schecter (2008). Thus, recent studies demonstrate that wave-  
28 induced spiral rainbands affect TC intensity.

29 Characteristics of simulated TC rainbands are here analyzed from 15 February at 2100 UTC  
30 to 17 February at 2100 UTC. On 15 February at 2100 UTC, a symmetry in TC rainbands is  
31 observed between east and west sides of the TC. The east-west (E-W) intensity ratio of

1 maximum precipitation (IRMP) is about 0.7 (Fig.14a). The eye size is observed to be 132 km  
2 large. On 16 February at 0300 UTC, intensification of the eyewall of TC Ivan is accompanied  
3 with an intensification of precipitation at east side of the system. E-W IRMP and eye size are  
4 estimated about 2.8 and 100 km respectively (Fig.14b). On 16 February at 0600 UTC an  
5 asymmetry in TC rainbands is observed (Fig.14c). The E-W IRMP decreases to about 1.4.  
6 Short rainbands of about 16 km wavelength appear at the eastern side of the TC.

7 Figure 14d shows a symmetry again on 16 February at 1200 UTC with an IRMP of 1.1. A  
8 strong symmetry in TC rainbands is visualized on 16 February at 1800 UTC with a TC eye  
9 size of 88 km (Fig.14e). In addition many oscillations are visualized in precipitation. After  
10 the landfall of TC Ivan, a clear eye contraction is observed (eye size of 80 km) on 17 February  
11 at 1200 UTC (Fig.14f). When the west side of Ivan is above land, TC rainbands on west side  
12 are spread and less intense than those on east side above ocean. This is consistent with surface  
13 friction and latent heat release during landfall. Thus TC intensification is characterized by  
14 intense precipitation on the eastside. In addition E-W IRMP balance supports that TC  
15 rainbands play a role in TC energy dissipation. Tropical Rainfall Measuring Mission  
16 Precipitation near surface rate estimates at altitudes  $<3$  km visualized an asymmetry of TC  
17 eyewall in the eastern quadrant with the heaviest precipitation ( $>10$  mmh<sup>-1</sup>) located north-east  
18 of the TC during intensification on 16 February at 0600 UT (Fig. 15). Large values are  
19 observed where wavenumber-1 vortex Rossby wave is located at north of TC eye. Figure 16  
20 also shows evidence of a natural continuous and symmetrical eye contraction cycle during  
21 intensification and landfall stages. Mean size of TC eye is around 96 km. The rainbands have  
22 widths varying between 15 km and 60 km. Distance between TC rainbands ranges between 24  
23 km and 76 km. TC rainbands propagate outward at speed between 0.5 ms<sup>-1</sup> and 3 ms<sup>-1</sup>. Thus  
24 the order of magnitude of the spacing and size of the rain bands are close to horizontal  
25 wavelengths of observed high-frequency GWs. Nevertheless, we should be cautious on the  
26 connection between GW horizontal wavelengths and radial spacing of rainbands. Figure 10  
27 shows the presence of wavelike structures on clouds at altitudes of 4-8 km with horizontal  
28 wavelengths of about 30-40 km at longitudes of 54-55°E. Wind perturbations verify GW  
29 polarization relation. Modes with similar spectral characteristics are also observed in the LS  
30 (Fig. 12c).

31

32

## 1 **7 Summary and conclusions**

2 Characteristics of GWs were examined in the UT/LS during the evolution of TC Ivan (2008)  
3 in the SWIO. Dominant low-frequency GWs (periods of 4.6-13 h) with horizontal and vertical  
4 wavelengths of 80-400 km and 0.7-3 km respectively were retrieved from radiosonde and  
5 GPS RO measurements. In particular, an inertia GW with vertical wavelength of 2-3 km,  
6 horizontal wavelength of ~ 400 km and period of 13 h is observed to be dominant and more  
7 intense east of TC Ivan in the LS over the SWIO during TC intensification. It propagates  
8 eastward in the LS. Because observational filtering and height ranges, the analysis focused on  
9 modes with short vertical wavelengths < 4-5 km and periods >2 h.

10 ECMWF analyses gave insight into spectrum of low-frequency convective GWs with  
11 horizontal wavelengths between 350 and 2000 km and vertical wavelengths > 2 km in the LS.  
12 They revealed that some waves are closely linked to TC Ivan. In particular, a large continuous  
13 spectrum of GWs with horizontal wavelengths between 350 km and 1000 km is observed east  
14 of TC eye. East of the TC, a dominant mode of horizontal wavelength of 600 km and 12.8 h  
15 period propagated eastward favored by the westward background wind in the LS. ECMWF  
16 analyses also indicated the presence of GWs with long horizontal wavelengths of 1400-1700  
17 km west of the TC with estimated periods of 1-2 days.

18 Meso-NH simulations provided detailed information about the activity and characteristics of  
19 TC-related GWs during the development stage, intensification and landfall. Model outputs  
20 revealed a larger spectrum with high and low-frequency GWs (periods of 20 min-2 days),  
21 horizontal wavelengths ranged between 32-2000 km and short vertical wavelengths of 1.5-3.3  
22 km. High-frequency modes produced by localized strong convection are dominant near the  
23 TC eye during TC intensification. In addition the model highlights intensity and spatial  
24 extension of other dominant mesoscale GWs. In particular, Meso-NH provided a good  
25 detailed description of dominant inertia GW with 300-600 km horizontal wavelengths and 3  
26 km vertical wavelength during TC intensification. Strong convection resulting from  
27 wavenumber-1 and wavenumber-2 vortex Rossby waves was suggested as sources of GWs  
28 with dominant horizontal wavelengths of 300-600 km and 100-200 km respectively.

29 Thus, observation and model outputs supported the presence of a dominant quasi-inertia GW  
30 with horizontal and vertical wavelengths of 400-800 km and 1.5-3.5 km, propagating  
31 eastward east of TC Ivan. It was closely linked to TC intensity with largest amplitudes during  
32 TC intensification.

1 Results are consistent with previous observational studies on characteristics of TC-related  
2 GWs (Chane Ming et al. 2002, 2010) and link between GW energy density and TC activity in  
3 the UT/LS (Ibrahim et al., 2010). Chane Ming et al. (2010) also detected dominant eastward  
4 propagating modes with a horizontal wavelength of about 500 km in the UT/LS during  
5 intense TC Dina (2002) in the SWIO and TC Faxai (2001) in north-west Pacific Ocean with  
6 prevailing westward wind between altitudes of 10-22 km and eastward QBO above. An  
7 increase in total energy density of about 30% of the climatological energy density in austral  
8 summer was estimated in the LS above Tromelin during TC Dina. From numerical  
9 simulations with an horizontal grid size of 27 km, Kim et al. (2005, 2009) analyzed low-  
10 frequency GWs with medium horizontal wavelengths of 300–600 km, a vertical wavelength  
11 of 3–11 km, and a period of 6–11 h during category 4 TCs Rusa (2002) and Ewiniar (2006) in  
12 the LS. Convection in the TC-generated cloud bands was suggested to be a major source of  
13 GWs during TC Rusa. Dominant eastward propagating stratospheric waves were observed  
14 during the mature stage of TC Ewiniar. In contrast, Kuester et al. (2008) simulated high  
15 frequency GWs with horizontal wavelengths of 15–300 km, vertical wavelengths of 4–8 km,  
16 and intrinsic periods of 20-100 min above a category 2 TC Humberto (2001) with nested  
17 horizontal grids of 27 km, 9 km and 3 km. With similar grids, Kim and Chun (2010)  
18 examined eastward propagating GWs with horizontal wavelengths of 10-100km and periods  
19 less than 2 h produced by a category 5 TC Saomai (2006). Waves with horizontal  
20 wavelengths > 80 km and periods > 1 h are found to be the dominant contribution to the  
21 momentum flux. More recently, using a large domain with a 27 km horizontal resolution,  
22 Chen et al. (2012) numerically investigated eastward propagating GWs with long horizontal  
23 scales of about 1000 km generated by TC Matsa (2005) in the LS. Vertical resolution of  
24 previous simulations was about 500 m in the UT/LS.

25 Results also supported that some GWs-related to TC could be filtered out by the background  
26 wind and contribute locally to the QBO forcing in the LS. A strong activity of GWs was also  
27 observed during landfall accompanied with the enhancement of eastward wind in the middle  
28 troposphere. In addition characteristics of TC rainbands revealed intensification of TC  
29 eyewall with strong precipitation at east side of TC Ivan during intensification. Meso-NH  
30 simulation also revealed high-frequency GWs-related TC-clouds in the troposphere on  
31 February 16 and a symmetrical eye contraction cycle during TC intensification and landfall.

1 Previously, asymmetries in surface friction caused by vortex translation were suggested to  
2 produce a wavenumber-1 asymmetry in convergence (Shapiro, 1983). Asymmetric forcing  
3 has also been studied as a possibly important intensification mechanism. Eyewall convection  
4 can be enhanced and shifted inward on one side by inflow associated with the vortex Rossby  
5 waves in the lower troposphere, while it is suppressed and shifted outward on the other side  
6 by outflow (Wang, 2002a). Asymmetries can transport energy to the outside of the eyewall  
7 due to their nature of the vortex Rossby waves (Montgomery and Kalenbach, 1997). Eyewall  
8 asymmetries interact with the mean vortex through eddy momentum fluxes and partially  
9 extract their kinetic energy from the mean vortex, leading to weakening of the mean  
10 tangential and radial winds (Houze et al., 2006). If TC asymmetries become sufficiently  
11 strong, then air with high values of potential vorticity and equivalent potential temperature are  
12 mixed outward and cause the weakening of the warm core aloft and the increase of central  
13 pressure (Frank and Ritchie, 2001). Radial maximum wind can also be accelerated during  
14 intensification stage and produce an eyewall contraction (Houze et al., 2006) which was  
15 observed in the present simulation. The environmental shear induced by land-sea contrast was  
16 also revealed to produce highly structures in landfalling TC, responsible of the distribution of  
17 the strongest wind and the heaviest rainfall (Chen and Yau, 2003). An asymmetry first occurs  
18 at the top of the vortex and propagates to the surface. Rainfall is generally observed to have a  
19 maximum ahead of the TC centre which indicates importance of surface friction induced by  
20 low-level convergence. Thus observations and numerical simulations have suggested vortex  
21 Rossby waves to be related to changes in the structure and intensity of TCs (Wang, 2002b). In  
22 addition, outward propagation of wavenumber-1 Rossby waves is believed to initiate inner  
23 spiral rainbands. During storm intensity change, shearing deformation can stretch vorticity  
24 into filaments that spiral toward the centre of the TC (Houze et al., 2006). In addition, Chow  
25 et al (2002) show that fluctuation of the PV distribution in the TC core region can act as a  
26 source, generating gravity waves that produce banded structures and the moving spiral  
27 rainbands. Chen et al. (2006) showed that during austral summer when TC s are active in the  
28 southern hemisphere, vertical wind shear is mostly weak and moderate ( $<15 \text{ ms}^{-1}$ ) and that  
29 TCs display the largest asymmetries. In our study the contrast wind shear enhanced by land-  
30 sea contrast is suggested to be responsible of the observed wavenumber-1 asymmetry during  
31 intensification stage just before landfall of TC Ivan.

32 In conclusion, the French research model Meso-NH proved to be a useful numerical tool to  
33 explore the large continuous spectrum of TC-related GWs in the UT/LS in relation with a

1 realistic TC dynamics. Further studies should include detailed description of GW sources,  
2 GW anisotropic propagation and GW effects on the rainband characteristics and the  
3 background wind.

4

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10

## 1 **References**

- 2 Alexander, M.J.: Parameterization of Physical Processes: Gravity wave momentum fluxes,  
3 Encyclopedia of the Atmospheric Sciences, Academic/Elsevier, London, 1699-1705, 2003.
- 4 Alexander, M. J. and Barnet, C.: Using satellite observations to constrain parameterizations of  
5 gravity wave effects for global models, *J. Atmos. Sci.*, 64, 1652–1665, 2007.
- 6 Alexander, M. J., Geller, M., McLandress, C., Polavarapu, S., Preusse, P., Sassi, F., Sato, K.,  
7 Eckermann, S., Ern, M., Hertzog, A., Kawatani, Y., Pulido, M., Shaw, T., Sigmond, M.,  
8 Vincent, R., and Watanabe, S.: Recent developments in gravity wave effects in climate  
9 models, and the global distribution of gravity wave momentum flux from observations and  
10 models, *Q. J. Roy. Meteorol. Soc.*, 136, 1103-1124, 2010.
- 11 Alexander, S. P., Tsuda, T., Kawatani, Y., and Takahashi, M.: Global distribution of  
12 atmospheric waves in the equatorial upper troposphere and lower stratosphere: COSMIC  
13 observations of wave mean flow interactions, *J. Geophys. Res.*, 113, D24115, doi:  
14 10.1029/2008JD010039, 2008.
- 15 Anthes, R. A.: Exploring Earth’s atmosphere with radio occultation: contributions to weather,  
16 climate and space weather, *Atmos. Meas. Tech.*, 4, 1077-1103, doi:10.5194/amt-4-1077-2011,  
17 2011.
- 18 Baldwin, M. P., Gray, L. J., Dunkerton, T. J., Hamilton, K., Haynes, P. H., Randel, W. J.,  
19 Holton, J. R., Alexander, M. J., Hirota, I., Horinouchi, T., Jones, D. B. A., Kinnnersley, J. S.,  
20 Marquardt, C., Sato, K., and Takahashi, M.: The Quasi-Biennial Oscillation, *Rev. Geophys.*,  
21 39, 179–229, doi:10.1029/1999RG000073, 2001.
- 22 Bechtold, P., Bazile, E., Guichard, F., Mascart, P., and Richard, E.: A mass flux convection  
23 scheme for regional and global models, *Q. J. Roy. Meteorol. Soc.*, 127, 869–886, 2001.
- 24 Chaboureaud, J.-P., Cammas, J.-P., Mascart, P., Pinty, J.-P., Claud, C., Roca, R., and  
25 Morcrette, J.-J.: Evaluation of a cloud system life-cycle simulated by Meso-NH during  
26 FASTEX using METEOSAT radiances and TOVS-3I cloud retrievals, *Q. J. Roy. Meteorol.*  
27 *Soc.*, 126, 1735–1750, 2000.
- 28 Chane Ming, F., Molinaro, F., and Leveau, J.: Wavelet techniques applied to lidar signal in  
29 the analysis of the middle atmosphere dynamics, *Appl. Sig. Process.*, 6, 95–106, 1999.

1 Chane-Ming, F., Roff, G., Robert, L., and Leveau, J.: Gravity waves characteristic over  
2 Tromelin Island during the passage of cyclone Hudah, *Geophys. Res. Lett.*, 29, 18-1–18-4,  
3 doi :10.1029/2003JD003489, 2002.

4 Chane-Ming, F., Faduilhe, D., and Leveau, J.: Latitudinal and seasonal variability of  
5 gravity energy in the South-West Indian Ocean, *Ann. Geophys.*, 25, 2479–2485,  
6 doi:10.5194/angeo-25-2479-2007, 2007.

7 Chane-Ming, F., Chen, Z., and Roux, F.: Analysis of gravity-waves produced by intense  
8 tropical cyclones, *Ann. Geophys.*, 28, 531–547, doi:10.5194/angeo-28-531-2010, 2010.

9 Chen, D., Chen, Z. Y., and Lü, D. R.: Simulation of the stratospheric gravity waves generated  
10 by the Typhoon Matsa in 2005, *Sci China Earth Sci.*, 55: 602–610, doi: 10.1007/s11430-011-  
11 4303-1, 2012.

12 Chen, S., Knaff, J. A., and Marks, F. D.: Effects of vertical wind shear and storm motion on  
13 tropical cyclone rainfall asymmetries deduced from TRMM, *Mon. Wea. Rev.*, 134, 3190–  
14 3208, 2006.

15 Chen, Y., and Yau, M. K.: Asymmetric structures in a simulated landfall hurricane, *J. Atmos.*  
16 *Phys.*, 60, 2294-2312, 2003.

17 Chow, K. C. and Chan, K. L.: Angular momentum transports by moving spiral waves, *J.*  
18 *Atmos. Sci.*, 60, 2004–2009, 2003. 30

19 Chow, K. C., Chan, K. L., and Lau, A. K. H.: Generation of moving spiral bands in tropical  
20 cyclones, *J. Atmos. Sci.*, 59, 2930–2950, 2002.

21 Clark, T. L., Hauf, T., and Kuettner, J. P.: Convectively forced internal gravity waves: Results  
22 from two-dimensional numerical experiments, *Q. J. Roy. Meteorol. Soc.*, 112: 899–925, 1986.

23 Cuxart, J., Bougeault, P., and Redelsperger, J.-L.: A turbulence scheme for mesoscale and  
24 large-eddy simulations, *Q. J. Roy. Meteorol. Soc.*, 126, 1–30, 2000.

25 Das, S. S., Uma, K. N., and Das, S. K.: MST radar observations of short-period gravity wave  
26 during overhead tropical cyclone, *Radio Sci.*, 47, RS2019, doi:10.1029/2011RS004840, 2012.

27 Dhaka, S. K., Takahashi, M., Shibagaki, Y., Yamanaka, M. D., and Fukao, S.: Gravity wave  
28 generation in the lower stratosphere due to passage of the Typhoon 9426 (Orchid) observed



1 by the MU radar at Shigaraki (34.85 N, 136.10 E), *J. Geophys. Res.*, 108, 4595,  
2 doi:10.1029/2003JD003489, 2003.

3 Dewan, E. M., Picard, R. H., O'Neil, R. R., Gardiner, H. A., Gibson, J., Mill, J. D., Richards,  
4 E., Kendra, M., and Gallery, W. O.: MSX satellite observations of thunderstorm-generated  
5 gravity waves in mid-wave infrared images of the upper stratosphere, *Geophys. Res. Lett.*, 25,  
6 939–942, 1998.

7 Dunkerton, T. J.: Theory of the mesopause semiannual oscillation, *J. Atmos. Sci.*, 39, 2681–  
8 2690, 1982.

9 Ern, M. and Preusse, P.: Gravity wave momentum flux spectra observed from satellite in the  
10 summertime subtropics: Implications for global modeling, *Geophys. Res. Lett.*, 39, L15810,  
11 doi:10.1029/2012GL052659, 2012.

12 Fovell, R., Durran, D., and Holton, J. R.: Numerical simulations of convectively generated  
13 stratospheric gravity waves, *J. Atmos. Sci.*, 49, 1427–1442, 1992.

14 Frank, W. M. and Ritchie, E. A.: Effects of vertical wind shear on the intensity and structure  
15 of numerically simulated hurricanes, *Mon. Wea. Rev.*, 129, 2249–2269, 2001.

16 Fritts, D. C. and Alexander, M. J.: Gravity wave dynamics and effects in the middle  
17 atmosphere, *Rev. Geophys.*, 41, 1003, doi:10.1029/2001RG000106, 2003.

18 Gill, A. E.: *Atmosphere-Ocean Dynamics*, Academic Press, Inc., New York, USA, 662 pp.,  
19 1982.

20 Gregory, D., Morcrette, J.-J., Jakob, C., Beljaars, A. C. M., and Stockdale, T.: Revision of  
21 convection, radiation and cloud schemes in the ECMWF Integrated Forecasting System, *Q. J.*  
22 *Roy. Meteorol. Soc.*, 126, 1685-1710, 2000.

23 Healy, S. B.: Operational assimilation of GPS radio occultation measurements at ECMWF,  
24 available online at: <http://www.ecmwf.int/publications/newsletters/pdf/111.pdf>, *ECMWF*  
25 *Newsletter*, 111, 6–11, 2007.

26 Healy, S. B. and Thepaut, J. N.: Assimilation experiments with CHAMP GPS radio  
27 occultation measurements, *Q. J. Roy. Meteorol. Soc.*, 132, 605–623, doi:10.1256/qj.04.182,  
28 2006.

1 Hence, D. A. and Houze, R. A.: Vertical structure of tropical cyclone rainbands as seen by the  
2 TRMM precipitation radar, *J. Atmos. Sci.*, 69, 2644–2661, 2012.

3 Hendricks, E. A., Schubert, W. H., Fulton, S. R., and McNoldy, B. D.: Spontaneous-  
4 adjustment emission of inertia-gravity waves by unsteady vortical motion in the hurricane  
5 core, *Q. J. Roy. Meteor. Soc.*, 136, 537–548, 2008.

6 Hendricks, E. A., McNoldy, B. D., and Schubert, W. H.: Observed inner core structural  
7 variability in hurricane Dolly (2008), *Mon. Weather Rev.*, 140, 4066–4077, 2012.

8 Horinouchi, T., Nakamura, T., and Kosaka, J.: Convectively generated mesoscale gravity  
9 waves simulated throughout the middle atmosphere, *Geophys. Res. Lett.*, 29, 2007,  
10 doi:10.1029/2002GL016069, 2002.

11 Houze, R. A.: Clouds in tropical cyclones, *Mon. Wea. Rev.*, 138, 293–344, 2010.

12 Houze, R. A., Cetrone, J., Brodzik, S. R., Chen, S. S., Zhao, W., Lee, W.-C., Moore, J. A.,  
13 Stossmeister, G. J., Bell, M. M., and Rogers, F. F.: The hurricane rainband and intensity  
14 change experiment: Observations and modeling of hurricanes Katrina, Ophelia, and Rita,  
15 *Bull. Amer. Meteor. Soc.*, 87, 1503–1521, 2006.

16 Huang, C.-Y., Kuo, Y.-H., Chen, S.-Y., Terng, C.-T., Chien, F.-C., Lin, P.-L., Kueh, M.-T.,  
17 Chen, S.-H., Yang, M.-J., Wang, C.-J., and Rao, A. S. K. A. P.: Impact of GPS radio  
18 occultation data assimilation on regional weather predictions, *GPS Solutions*, 14, 35-49,  
19 doi:10.1007/s10291-009-0144-1, 2010.

20 Ibrahim, C., Chane Ming, F., Barthe, C., and Kuleshov, Y: Diagnosis of tropical cyclone  
21 activity through gravity wave energy density in the South West Indian Ocean, *Geophys. Res.*  
22 *Lett.*, 37, L09807, doi:10.1029/2010GL042938, 2010.

23 Jolivet S., Chane Ming, F., Barbary, D., and Roux, F.: A numerical study of orographic  
24 forcing on TC Dina (2002) in South West Indian Ocean, *Ann. Geophys.*, 31, 107-125,  
25 doi:10.5194/angeo-31-107-2013, 2013.

26 Kain, J. S. and Fritsch, J. M.: A One-dimensional entraining/detraining plume model and its  
27 application in convective parameterization, *J. Atmos. Sci.*, 47, 2784–2802, 1990.

28 Kawatani, Y., Watanabe, S., Sato, K., Dunkerton, T. J., Miyahara, S., and Takahashi, M.: The  
29 roles of equatorial trapped waves and internal inertia-gravity waves in driving the Quasi-

1 Biennial oscillation. Part I: Zonal mean wave forcing, *J. Atmos. Sci.*, 67, 963–980,  
2 doi:10.1175/2009JAS3222.1, 2010.

3 Kim, S.-Y. and Chun, H.-Y.: Stratospheric gravity waves generated by Typhoon Saomai  
4 (2006): numerical modeling in a moving frame following the typhoon, *J. Atmos. Sci.*, 67,  
5 3617–3636, doi:10.1175/2010JAS3374.1, 2010.

6 Kim, S.-Y. and Chun, H.-Y.: Impact of typhoon-generated gravity waves in the typhoon  
7 development, *Geophys. Res. Lett.*, 38, L01806, doi:10.1029/2010GL045719, 719, 2011.

8 Kim, S.-Y., Chun, H.-Y., and Baik, J.-J.: A numerical study of gravity waves induced  
9 by convection associated with Typhoon Rusa, *Geophys. Res. Lett.*, 32, L24816,  
10 doi:10.1029/2005GL024662, 2005.

11 Kim, S.-Y., Chun, H.-Y., and Wu, D. L.: A study on stratospheric gravity waves generated by  
12 Typhoon Ewiniar: numerical simulations and satellite observations, *J. Geophys. Res.*, 114,  
13 D22104, doi:10.1029/2009JD011971, 2009.

14 Kim, Y.-J. and Chun, H.-Y.: A computationally efficient non stationary convective gravity-  
15 wave drag parameterization for global atmospheric prediction systems, *Geophys. Res. Lett.*,  
16 32, L22805, doi:10.1029/2005GL024572, 2005.

17 Kim, Y.-J., Eckermann, S. E., and Chun, H.-Y.: An overview of the past, present and future of  
18 gravity-wave drag parameterization for numerical climate and weather prediction models,  
19 *Atmos. Ocean*, 41, 65–98, 2003.

20 Klemp, J. B.: Advances in the WRF model for convection resolving forecasting, *Adv.*  
21 *Geosci.*, 7, 25–29, 2006.

22 Kuester, M. A., Alexander, M. J., and Ray, E. A.: A model study of gravity waves over  
23 Hurricane Humberto (2001), *J. Atmos. Sci.*, 65, 3231–3246, 2008.

24 Kunii M., Seko, H., Ueno, M., Shoji, Y., and Tsuda, T.: Impact of Assimilation of GPS radio  
25 occultation refractivity on the forecast of Typhoon Usagi in 2007, *J. Met. Soc. Jap.*, 90, 255–  
26 273, doi:10.2151/jmsj.2012-207, 2012.

27 Lac, C., Lafore, J.-P., Redelsperger, J.-L.: Role of gravity waves in triggering deep convection  
28 during TOGA COARE, *J. Atmos. Sci.*, 59, 1293–1316, 2002.

1 Lafore, J. P., Stein, J., Asencio, N., Bougeault, P., Ducrocq, V., Duron, J., Fischer, C., Hereil,  
2 P., Mascart, P., Pinty, J.-P., Redelsperger, J.-L., Richard, E., and Vila-Guerau de Arellano, J.:  
3 The Meso-NH atmospheric simulation system. Part I: Adiabatic formulation and control  
4 simulations, *Ann. Geophys.*, 16, 90-109, doi:10.1007/s00585-997-0090-6, 1998.

5 Lane, T. P. and Knievel, J. C.: Some effects of model resolution on simulated gravity waves  
6 generated by deep, mesoscale convection, *J. Atmos. Sci.*, 62, 3408–3419, doi :10.1175/JAS,  
7 2005.

8 Lane, T.P. and Reeder, M.J.: Modelling the generation of gravity waves by a maritime  
9 continent thunderstorm, *Q. J. Roy. Met. Soc.*, 127, 2705–2724, 2001.

10 Leclaire De Bellevue, J., Baray, J. L., Baldy, S., Ancellet, G., Diab, R., and Ravetta, F.:  
11 Simulations of stratospheric to tropospheric transport during the tropical cyclone Marlene  
12 event, *Atmos. Env.*, 41, 6510, doi:10.1016/j.atmosenv.2007.04.040, 2007.

13 Lin, C. Y., Hsu, H. M., Sheng, Y. F., Kuo, C. H., and Liou, Y. A.: Mesoscale processes for  
14 super heavy rainfall of Typhoon Morakot (2009) over southern Taiwan, *Atmos. Chem. Phys.*  
15 11, 345-361, doi:10.5194/acp-11-345-2011, 2011.

16 Liou, Y.-A., Pavelyev, A. G., Huang, C.-Y., Igarashi, K., Hocke, K., and Yan, S.-K.: Analytic  
17 method for observation of the gravity waves using radio occultation data, *Geophys. Res. Lett.*,  
18 30, 2021, doi:10.1029/2003GL017818, 2003.

19 Liou, Y.-A., Pavelyev, A. G., Wicker, J., Liu, S. F., Pavelyev, A. A., Schmidt, T., and  
20 Igarashi, K.: Application of GPS radio occultation method for observation of the internal  
21 waves in the atmosphere, *J. Geophys. Res.*, 111, D06104, doi:10.1029/2005JD005823, 2006.

22 Liou, Y.-A., Pavelyev, A. G., Matyugov, S. S., Yakovlev, O. I., and Wickert, J.: Radio  
23 Occultation Method for Remote Sensing of the Atmosphere and Ionosphere, INTECH,  
24 Vukovar, Croatia, 170 pp., 2010.

25 Liu, H., Anderson, J., and Kuo, Y.-H.: Improved analyses and forecasts of Hurricane Ernesto's  
26 genesis using radio occultation data in an ensemble filter assimilation system, *Mon. Wea.*  
27 *Rev.*, 140, 151–166, doi:10.1175/MWR-D-11-00024.1, 2012.

28 Liu, Y., Zhang, D. –L., and Yau, M. K.: A Multiscale Numerical Study of Hurricane Andrew  
29 (1992). Part II: Kinematics and Inner-Core Structures, *Mon. Wea. Rev.*, 127, 2597–2616,  
30 1999.

1 Marks, F. D., Houze, R. A., and Gamache, J. F.: Dual-Aircraft Investigation of the inner core  
2 of Hurricane Norbert. Part I: Kinematic structure, *J. Atmos. Sci.*, 49, 919–942, 1992.

3 Montgomery, M. T., and Kallenbach, R. J.: A theory for vortex Rossby-waves and its  
4 application to spiral bands and intensity changes in hurricanes, *Q. J. Roy. Met. Soc.*, 123,  
5 435–465, 1997.

6 Montroty, R., Rabier, F., Westrelin, S., Faure, G., and Viltard, N.: Impact of wind bogus and  
7 cloud and rain affected SSM/I data on tropical cyclones analyses and forecasts, *Q. J. Roy.  
8 Met. .Soc.*, 134, 1673–1699, 2008.

9 Niranjana Kumar, K., Ramkumar, T. K., and Krishnaiah, M.: MST Radar observation of  
10 inertia-gravity waves generated from tropical cyclones, *J. Atmos. Sol. Terr. Phys.*, 73, 1890-  
11 1906, 2011.

12 Nuissier, O., Rogers, R. F., and Roux, F.: A numerical simulation of Hurricane Bret on 22–23  
13 August 1999 initialized with airborne Doppler radar and dropsonde data, *Q. J. Roy. Meteorol.  
14 Soc.*, 131, 155–194, doi: 10.1256/qj.02.233, 2005.

15 Pfister, L., Chan, K. R., Bui, T. P., Bowen, S., Legg, M., Gary, B., Kelly, K., Proffitt, M., and  
16 Starr, W.: Gravity waves generated by a tropical cyclone during the step tropical field  
17 programm: A case study, *J. Geophys. Res.*, 98, 8611-8638, 1993.

18 Piani, C., Durran, D., Alexander, M. J., and Holton, J. R.: A numerical study of three-  
19 dimensional gravity waves triggered by deep tropical convection and their role in the  
20 dynamics of the QBO, *J. Atmos. Sci.*, 57, 3689–3702, 2000.

21 Pinty, J.-P., and Jabouille, P.: A mixed-phase cloud parameterization for use in mesoscale  
22 non-hydrostatic model: simulations of a squall line and of orographic precipitations, *Proc.  
23 Conf. of Cloud Physics*, Everett, WA, USA, Amer. Meteor. Soc., 217- 220, 1999.

24 Pirscher, B., Foelsche, U., Borsche, M., Kirchengast, G., and Kuo, Y.-H.: Analysis of  
25 migrating diurnal tides detected in FORMOSAT-3/COSMIC temperature data, *J. Geophys.  
26 Res.*, 115, D14108, doi:10.1029/2009JD013008, 2010.

27 Plougonven, R. and Teitelbaum, P. H.: Comparison of a large-scale inertia gravity wave as  
28 seen in the ECMWF analyses and from radio-sondes, *Geophys. Res. Lett.*, 30, 1954, doi  
29 :10.1029/2003GL017716, 2003.

1 Pratt, W. K.: *Digital Image Processing: PIKS Inside*, Third Edition, John Wiley & Sons, Inc.,  
2 New York, USA, 735 pp., 2001.

3 Preusse, P., Eckermann, S. D., and Ern, M.: Transparency of the atmosphere to short  
4 horizontal wavelength gravity waves, *J. Geophys. Res.*, 113, D24104,  
5 doi:10.1029/2007JD009682, 2008

6 Reasor, P.D., Montgomery, M. T., Marks, F. D., and Gamache, J. F.: Low-wavenumber  
7 structure and evolution of the hurricane inner core observed by airborne dual-Doppler radar,  
8 *Mon. Wea. Rev.*, 128, 1653-1680, 2000.

9 Richter, J. H., Sassi, F., and Garcia, R. R.: Toward a physically based gravity wave source  
10 parameterization in a general circulation model, *J. Atmos. Sci.*, 67, 136–156, 2010.

11 Roux, F., Chane-Ming, F., Lasserre-Bigorrry, A., and Nuissier, O.: Structure and evolution of  
12 intense tropical cyclone Dina near La Réunion on 22 January 2002: GB-EVTD analysis of  
13 single Doppler radar observations, *J. Atmos. Oceanic. Technol.*, 21, 1501–1518, 2004.

14 Salby, M. L. and Garcia, R. R.: Transient response to localized episodic heating in the  
15 tropics. Part I: Excitation and short-time near-field behavior, *J. Atmos. Sci.*, 44, 458–498,  
16 1987.

17 Sato, K.: Small-scale wind disturbances observed by the MU radar during the passage of  
18 Typhoon Kelly, *J. Atmos. Sci.*, 50, 518-537, 1993.

19 Saunders, R., Matricardi, M., Brunel, P., English, S., Bauer, P., O’Keeffe, U., Francis, P., and  
20 Rayer, P.: RTTOV-8 science and validation report, NWP SAF report, Met Office, Exeter, UK,  
21 41 pp., 2005.

22 Schechter, D. A.: The spontaneous imbalance of an atmospheric vortex at high Rossby number,  
23 *J. Atmos. Sci.*, 65, 2498–2521, 2008.

24 Schroeder, S., Preusse, P., Ern, M., and Riese, M.: Gravity waves resolved in ECMWF and  
25 measured by SABER, *Geophys. Res. Lett.*, 36, L10805, doi :10.1029/2008GL037054, 2009.

26 Schubert, W. H., Rozoff, C. M., Vigh, J. L., McNoldy, B. D., and Kossin, J. P.: On the  
27 distribution of subsidence in the hurricane eye, *Q. J. Roy. Meteorol. Soc.*, 133, 595-605, 2007.

28 Shapiro, L. J.: The asymmetric boundary layer flow under a translating hurricane, *J. Atmos.*  
29 *Sci.*, 40, 1984–1998, 1983.

1 Shutts, G. J., and Vosper, S. B.: Stratospheric gravity waves revealed in NWP model  
2 forecasts, *Q. J. Roy. Meteorol. Soc.*, 137, 303–317, doi :10.1002/qj.7, 2011.

3 Sun, B., Reale, A., Seidel, D. J., and Hunt, D. C.: Comparing radiosonde and COSMIC  
4 atmospheric profile data to quantify differences among radiosonde types and the effects of  
5 imperfect collocation on comparison statistics, *J. Geophys. Res.*, 115, D23104,  
6 doi:10.1029/2010JD014457, 2010.

7 Tsuda, T., Nishida, M., Rocken, C., and Ware, R. H.: A global morphology of gravity wave  
8 activity in the stratosphere revealed by the GPS occultation data (GPS/MET), *J. Geophys.*  
9 *Res.*, 105, 7257-7273, 2000.

10 Vincent, R. A., and Alexander, M. J.: Gravity waves in the tropical lower stratosphere: An  
11 observational study of seasonal and interannual variability, *J. Geophys. Res.*, 105, 17971–  
12 17982, doi:10.1029/2000JD900196, 2000.

13 Wang, Y.: Vortex Rossby waves in a numerically simulated tropical cyclone. Part I: Overall  
14 structure, potential vorticity and kinetic energy budgets, *J. Atmos. Sci.*, 59, 1213–1238,  
15 2002a.

16 Wang, Y.: Vortex Rossby waves in a numerically simulated tropical cyclone. Part II: The role  
17 in tropical cyclone structure and intensity changes, *J. Atmos. Sci.*, 59, 1239–1262, 2002b.

18 Wang, Y., and Wu, C.-C.: Current understanding of tropical cyclone structure and intensity  
19 changes - a review, *Meteor. Atmos. Phys.*, 87, 257 – 278, 2004.

20 Willoughby, H. E.: A possible mechanism for the formation of hurricane rainbands, *J. Atmos.*  
21 *Sci.*, 35, 838–848, 1978.

22 Xiao, C. Y. and Hu, X.: Analysis on the global morphology of stratospheric gravity wave  
23 activity deduced from the COSMIC GPS occultation profiles, *GPS Solutions*, 14, 65-74, doi:  
24 10.1007/s10291-009-0146-z, 2010.

25 Yu, Xing and Lee, Tae-Young: Role of convective parameterization in simulations of a  
26 convection band at grey-zone resolutions, *Tellus*, 62, 617–632, doi: 10.1111/j.1600-  
27 0870.2010.00470.x, 2010.

28 Zhang, D.-L., Liu, Y. B., and Yau, M. K.: A multiscale numerical study of Hurricane Andrew  
29 (1992), Part III: Dynamically induced vertical motion, *Mon. Weather Rev.*, 128, 3772–3788,

- 1 2000.
- 2 Zhang, D.-L., Liu, Y. B., and Yau, M. K.: A multiscale numerical study of hurricane Andrew  
3 (1992), Part IV: Inner-core thermodynamics, *Mon. Weather Rev.*, 130, 2745–2763, 2002.
- 4 Zhang, K., Fu, E., Silcock, D., Wang, Y., and Kuleshov, Y.: An investigation of atmospheric  
5 temperature profiles in the Australian region using collocated GPS radio occultation and  
6 radiosonde data, *Atmos. Meas. Tech.*, 4, 2087–2092, doi:10.5194/amt-4-2087-2011, 2011.
- 7 Zhang, Y., Xiong, J., Liu, L., and Wan, W.: A global morphology of gravity wave activity in  
8 the stratosphere revealed by the 8-yr SABER/TIMED data, *J. Geophys. Res.*, 117, D21101,  
9 doi:10.1029/2012JD017676, 2012.
- 10 Zuiderveld, K.: Contrast limited adaptive histogram equalization, in: *Graphics Gems IV*,  
11 edited by: Heckbert, P., Academic Press, ISBN 0-12-336155-9, Academic Press Professional,  
12 San Diego, USA, 474–485, 1994.
- 13



1 Table 1. Spectral characteristics of GWs above radiosonde stations of Gillot and Ivato from  
 2 15 to 18 February 2008 ( $\lambda_h$  and  $\lambda_v$ : horizontal and vertical wavelengths).  
 3

Station (altitude)	Number of profiles	Intrinsic period (h)	$\lambda_h$ (km)	$\lambda_v$ (km)
Gillot (10-15km)	4	7.6, 4	84, 210	1, 2.6
Gillot (18-22km)	3	13	130, 390	0.68, 2.1
Ivato (10-15km)	6	4, 6	66, 130	1.7, 2.6

## Figure captions

1

2 Figure 1. METEOSAT7 visible images of TC Ivan with **(a)** F-16 SSMI/S brightness  
3 temperatures on 16 February 2008 at 0000 UTC **(b)** TRMM TMI brightness temperatures at  
4 85 H on 16 February 2008 at 0600 UTC **(c)** F-16 SSMI/S brightness temperatures on 16  
5 February 2008 at 1630 UTC **(d)** F-16 SSMI/S brightness temperatures on 17 February 2008 at  
6 0000 UTC (from [http://www.nrlmry.navy.mil/tc\\_pages](http://www.nrlmry.navy.mil/tc_pages)).

7 Figure 2. TC Ivan best track data (RSMC La Reunion, solid line) and cyclone track data  
8 obtained by simulation (Meso-NH, dashed line). Crosses indicate locations of GPS RO  
9 soundings and black circles correspond to locations of meteorological stations (G: Gillot, I:  
10 Ivato, T: Tromelin). Colours of crosses and segments of tracks indicate the day (13 Feb –  
11 navy blue; 14 Feb – black; 15 Feb – green; 16 Feb – yellow; 17 Feb – light blue and 18 Feb –  
12 magenta).

13 Figure 3. Time series of **(a)** the minimum central pressure (hPa) and **(b)** the 10-min average  
14 maximum sustained winds speed ( $\text{ms}^{-1}$ ) from best track data (blue line) and model simulation  
15 (red line).

16 Figure 4. Brightness temperature (K) from **(a)** IR channel of Meteosat-7 and **(b)** Meso-NH  
17 outputs on 16 February 2008 at 0000 UTC.

18 Figure 5. Observed (black - radiosonde, blue - GPS) and simulated (red) vertical profiles of:  
19 **(a)** temperature from GPS RO at (19°S, 59°E) on 15 February at 0026 UTC (0000 UTC), **(b)**  
20 temperature of radiosonde at Gillot on 16 February at 1112 UTC (1200 UTC), and **(c)** and **(d)**  
21 radiosonde zonal wind and meridional wind at Gillot on 16 February 2008 at 1112 UTC.

22 Figure 6. Fast Fourier transform spectra of 70 GPS RO temperature perturbations from 13  
23 February to 18 February 2008 in **(a)** the UT and **(b)** the LS ( $\lambda_v=100\text{m}/\text{normalized frequency}$ ).

24 Figure 7. Fast Fourier transform of collocated GPS RO temperature perturbations on 15  
25 February 2008 in **(a)** the UT and **(b)** the LS above Gillot. **(c)** and **(d)** same as (a) and (b) but  
26 on 16 February 2008 above Ivato ( $\lambda_v=100\text{m}/\text{normalized frequency}$ ).

1 Figure 8. **(a)** Vertical velocity ( $\text{ms}^{-1}$ , color) at 50 hPa derived from ECMWF analyses on 16  
2 February 2008 (00 UTC). The black (white) cross locates the centre of semi-circular waves  
3 (TC Ivan). Fast Fourier Transform of vertical velocity **(b)** at latitudes of  $16.5^{\circ}\text{S}$  and  $9\text{-}21^{\circ}\text{S}$   
4 and **(c)** as a function of latitude. **(d)** Morlet continuous wavelet transform of vertical velocity  
5 at  $16.5^{\circ}\text{S}$ .

6 Figure 9. **(a)** 10-min time series of vertical profile of meridional wind perturbations ( $\text{ms}^{-1}$ ) at  
7 Tromelin ( $15.53^{\circ}\text{S}$ ,  $54.31^{\circ}\text{E}$ ) and **(b)** mean zonal wind ( $\text{ms}^{-1}$ ) at Gillot ( $20.9^{\circ}\text{S}$ ,  $55.5^{\circ}\text{E}$ ) from  
8 13 February (0000UTC) to 18 February 2008 (1200UTC). The bold broken line shows the  
9 tropopause height. **(c)** Vertical profiles of zonal and meridional winds at 300 km (north, east,  
10 south and west) and east at ( $56^{\circ}\text{E}$ ,  $16^{\circ}\text{S}$ ) off the TC centre on 16 February at 0600 UTC.

11 Figure 10. Vertical cross section of vertical wind velocity ( $\text{ms}^{-1}$ ) across the storm centre at  
12  $16.1^{\circ}\text{S}$  on 16 February 2008 at 1200 UTC. The black and brown solid lines respectively  
13 indicate iso-theta contours and the boundary of cloud, which is defined by the region where  
14 the sum of mixing ratios is  $> 0.1 \text{ g kg}$ .

15 Figure 11. Horizontal field of pressure perturbations at 20 km altitude on 16 February 2008 at  
16 1200 UTC for horizontal wavelengths between **(a)** 200 km and 800 km, **(b)**  $< 200 \text{ km}$ . A  
17 yellow dot indicates the location of TC eye. Grayscale filtered images using bidimensional  
18 FFT applied on left square regions of images **(a)** and **(b)** for modes with horizontal  
19 wavelengths of **(c)** 400-600 km and **(d)**  $< 200 \text{ km}$  respectively. Yellow dotted circles show the  
20 presence of GW modes in the south-east and north-east areas.

21 Figure 12. Fast Fourier Transform of vertical velocity ( $\text{ms}^{-1}$ ) **(a)** at latitudes of  $16.5^{\circ}\text{S}$  and  $9\text{-}$   
22  $21^{\circ}\text{S}$  and **(b)** as a function of latitude at the altitude of 20 km on 16 February 2008 at 1200  
23 UTC. **(c)** Morlet continuous wavelet transform of vertical velocity at  $16.5^{\circ}\text{S}$ .

24 Figure 13. Hovmoller diagram of longitudinal pressure perturbation at  $16^{\circ}\text{S}$  from 16 February  
25 2008 at 1200 UTC to 17 February at 1800 UTC at 20 km.

26 Figure 14. Longitudinal precipitation (mm/h) cross section at a centre of TC Ivan on 15  
27 February 2008 at 2100UTC (a), 16 February at 0300UTC (b), at 0600UTC (c), at 1200UTC  
28 (d), at 1800UTC (e), and 17 February at 1200 UTC (f).

29 Figure 15. TRMM Precipitation radar near surface precipitation rate from 2008/02/16  
30 06:05:43 to 2008/02/16 07:38:06 UTC.

1 Figure 16. Time evolution of smoothed meridional precipitation at latitude of TC centre from  
2 15 February at 2100 UTC to 17 February at 2100 UTC. TC centre is used as origin for  
3 distance. Dotted broken lines indicate eye contraction.