## Modeling polarized solar radiation from ocean-atmosphere system for CLARREO inter-calibration applications

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Abstract
Conclusions
Tables

14
4

Back
Introduction
References
Figures

Full Screen / Esc

Printer-friendly Version


## Abstract

Reflected solar radiance from the Earth-atmosphere system is polarized. Radiance measurements can be affected by the reflected light's state of polarization if the radiometric sensor is sensitive to the polarization of observed light. To enable the Climate Absolute Radiance and Refractivity Observatory (CLARREO) mission for intercalibration of the polarization-sensitive imagers, such as the MODIS, the polarization state of the reflected solar light must be known with sufficient accuracy. For this purpose, the polarized solar radiation from the ocean-atmosphere system is studied with an adding-doubling radiative transfer model (ADRTM). The Cox-and-Munk ocean wave slope distribution model is used in calculation of the reflection matrix of a wind-ruffled ocean surface. An empirical foam spectral reflectance model and an empirical spectral reflectance model for water volume below the surface are integrated in the ocean surface model. Solar reflectance from the ADRTM is compared with that from the discrete-ordinate radiative transfer (DISORT) model. Sensitivity studies for reflected solar radiation are conducted for various ocean-surface and atmospheric conditions for the stratification of polarization distribution models (PDMs), which are to be used in the inter-calibration of the polarization-sensitive imager measurements with the CLARREO data. This modeling provides a reliable approach for making the spectral CLARREO PDMs over the broad solar spectra, which cannot be achieved by empirical PDMs

## 1 Introduction

Reflected solar radiance from the Earth-atmosphere system can be significantly polarized by the Earth's surface and by atmospheric components such as air molecules and aerosols. Radiance measurements can be seriously affected by the state of polarization of the observed light if the radiometric sensor is sensitive to polarization. To use the highly accurate data from the Climate Absolute Radiance and Refrac-

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


tivity Observatory (CLARREO) mission (Wielicki et al., 2013, currently available online http://journals.ametsoc.org/doi/pdf/10.1175/BAMS-D-12-00149.) to calibrate the polarization-sensitive solar imagers like MODIS (King et al., 1992; Sun and Xiong, 2007) or its follow-on instrument VIIRS and geostationary imagers, the state of po5 larization of the reflected solar light must be known with sufficient accuracy, e.g. better than $15 \%$ in RMS. Empirical Polarization Distribution Models (PDMs) (Nadal and Breon, 1999; Maignan et al., 2009) based on the PARASOL data can be used to correct radiometric bias in imager's measurements (Lukashin et al., 2013). However, the incidence and viewing geometries of pertinent scene types of these empirical PDMs 10 are limited by the specific sensors and their satellites' orbits and equator-crossing times, etc., which may not always be applicable to other imagers on different satellites. For example, currently PARASOL is the only polarimetric sensor in-orbit that is suitable for empirical PDM development. However, since PARASOL is in the A-train sun-synchronous orbit, small solar zenith angle (SZA) is not available. Although this may not be a problem for VIIRS since it is also in the A-train sun-synchronous orbit with an equator-crossing time of 1.30 p.m., for imagers not in the A-train orbit, such as the geostationary ones, the empirical PDMs based on the PARASOL polarimetric data will be insufficient to cover all viewing and solar geometries.Also, CLARREO is designed to measure solar spectra, with spectral coverage from 320 to 2300 nm and spectral sampling of 4 nm , which has potential to inter-calibrate spaceborne sensors at nearly all of the solar wavelengths. Thus, the PDMs for the inter-calibration applications should be made over the broad solar spectra, and this cannot be achieved by using only available polarimetric measurement. Furthermore, polarization sensitivity studies are necessary in stratification of the PDMs for different surface scene types and atmospheric conditions, as well as incidence and viewing geometries, etc. These polarization sensitivity studies require comprehensive modeling of the polarized solar radiation's sensitivity to the surface and atmospheric optical properties in order to optimize stratification of the PDMs. Therefore, numerical modeling of the polarized solar radiation from the Earthatmosphere system is critical for making accurate and efficient PDMs.

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion


Sensitivity to polarization of imaging radiometers such as MODIS and VIIRS, is obtained during instrument characterization before launch, and expressed in polarization factor. These factors are corrections of the baseline (not-polarized) gain, and depend on the instrument band, scan angle, and angle of polarization (Sun and Xiong, 2007). Taking into account of this framework, the PDM should be developed in a consistent manner, providing information on the degree of polarization (DOP), and the angle of linear polarization (AOLP) of the reflected solar radiation at the top-of-atmosphere (TOA). As demonstrated in a previous study by Lukashin et al. (2013), the DOP strongly depends on the scene type (clear sky and clouds, etc.), and both DOP and AOLP strongly depend on solar and viewing geometry. Before describing our approach to numerical modeling of the PDMs, we would like to briefly review the fundamentals relevant to polarization of reflected light.

Following Mischenko and Travis (1997), we set a right-handed Cartesian coordinate system as shown in Fig. 1, with the z-axis directed vertically to the upper boundary of the atmosphere and $x o z$ being the principal plane. The direction of the scattered light from the ocean-atmosphere system is specified by the unit vector $\boldsymbol{R}$. In the local righthanded orthonormal coordinate system formed by the unit vectors $R, \theta$, and $\phi$, we have $\boldsymbol{R}=\theta \times \phi$, where $\theta$ lies in the meridian plane of the scattered light beam. The AOLP of the reflected radiance in the direction of $R$ is the angle between the local meridian line and the electric vector of the linearly polarized light, counted anticlockwise when viewing in the reverse direction of the reflected radiance. Also, in the local right-handed orthonormal coordinate system formed by the unit vectors $R, \theta$, and $\phi$, the common intensity and the polarization state of any quasi-monochromatic light can be completely specified by the Stokes parameters $I, Q, U$, and $V$. Following the definition in Hansen

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion

and Travis (1974), we have
$I=\left\langle E_{\theta} E_{\theta}^{*}+E_{\phi} E_{\phi}^{*}\right\rangle$,
$U=\left\langle E_{\theta} E_{\phi}^{*}+E_{\phi} E_{\theta}^{*}\right\rangle$,
where $E_{\theta}$ and $E_{\phi}$ are the $\theta$ and $\phi$ components of the electric field in the local right-handed orthonormal coordinate system, respectively. The asterisk denotes the complex-conjugate value, and angular brackets denote averaging in time. Any arbitrarily polarized incoherent radiation denoted by Stokes parameters $I, Q, U$, and $V$ can be represented by a sum of an unpolarized part and a $100 \%$ polarized part as
$\left[\begin{array}{l}I \\ Q \\ U \\ V\end{array}\right]=\left[\begin{array}{c}I-\sqrt{Q^{2}+U^{2}+V^{2}} \\ 0 \\ 0 \\ 0\end{array}\right]+\left[\begin{array}{c}\sqrt{Q^{2}+U^{2}+V^{2}} \\ Q \\ U \\ V\end{array}\right]$.
For a sensor with polarization dependence, the measurement of the polarized portion of light $\left[\sqrt{Q^{2}+U^{2}+V^{2}}, Q, U, V\right]$ is a function of the polarization angle. As an extreme example, a linearly polarized lens can transmit a linearly polarized light $\left[\sqrt{Q^{2}+U^{2}}, Q\right.$, $U$, 0 ] from 0 to $100 \%$, depending on the AOLP relative to the polarization direction of the lens.

Since the circularly polarized radiance from the ocean-atmosphere system is negligible ( $V \approx 0$ ) (Coulson, 1988), only the common intensity / and linearly polarized radiance $Q$ and $U$ need to be calculated in this study. Without considering the circularly polarized radiance ( $V \approx 0$ ) at TOA, the DOP and AOLP are defined in terms of Stokes

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

## Abstract

Conclusions
Tables


4

Back
Introduction
References

Figures

- 1
- 

Close

Full Screen / Esc

parameters, respectively, as
$\mathrm{DOP}=\frac{\sqrt{Q^{2}+U^{2}}}{l}$
ACPD
13, 17585-17642, 2013
and
AOLP $=\frac{1}{2} \tan ^{-1}\left(\frac{U}{Q}\right)+\alpha_{0}$
5 where $\alpha_{0}=0$ if $Q>0$ and $U \geq 0 ; \alpha_{0}=\pi$ if $Q>0$ and $U<0 ; \alpha_{0}=\frac{\pi}{2}$ if $Q \leq 0$. The physical meaning of AOLP is illustrated in Fig. 1. Note that the definition of the AOLP in this work is not the same as in PARASOL data. In the local coordinate system, when both DOP and AOLP of the radiance are known, the sensor-measured intensity counts of light can be expressed as
$C_{m}=G_{0} \cdot(1-\mathrm{DOP}) \cdot /+G_{\mathrm{p}}(\mathrm{AOLP}) \cdot \mathrm{DOP} \cdot /$
where I denotes the true intensity, $G_{0}$ and $G_{\mathrm{p}}$ (AOLP) are sensor's gain factors for unpolarized radiation and linearly polarized radiation, respectively, which are the ratios of the sensor-measured intensity counts to the incidence intensity. $G_{0}$ can be obtained in calibration with natural solar light as incidence source. $G_{p}$ (AOLP) can be measured with a linearly polarized light as incidence source, which can be obtained by placing a linear polarizer in front of the sensor under natural solar radiation. From Eq. (5), the true radiance can be derived from the measured value as

$$
\begin{equation*}
I=\frac{C_{\mathrm{m}} / G_{0}}{1+\left[\frac{G_{\mathrm{p}}(\mathrm{AOLP})-G_{0}}{G_{0}}\right] \cdot \mathrm{DOP}}, \tag{6}
\end{equation*}
$$

where $C_{\mathrm{m}} / G_{0}$ is simply the measured intensity without polarization correction, and $\left[\frac{G_{p}(A O L P)-G_{0}}{G_{0}}\right]$, as a function of AOLP, is the imager's sensitivity-to-polarization coefficient, obtained during the prelaunch calibration of the instrument. Note here that 17590

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

Abstract

Conclusions

Tables

$\checkmark$

Back
Full Screen / Esc

for a well-depolarized imager, $m(A O L P)=\left[\frac{G_{\mathrm{p}}(\mathrm{AOLP})-G_{0}}{G_{0}}\right]$ should be a quantity with $|m(\mathrm{AOLP})| \ll 1$. Therefore, using $\frac{1}{1+x} \approx 1-x$ for small $x$, Eq. (6) can be expressed as
$I \approx\left(C_{\mathrm{m}} / G_{0}\right) \cdot[1-m(\mathrm{AOLP}) \cdot \mathrm{DOP}]$.
5 The relative error (RE) of the measured intensity due to polarization can then be calculated as

In deriving Eq. (8), we neglected the second-order small value [m(AOLP).DOP] ${ }^{2}$. Thus, e.g., for a sensor with a sensitivity-to-polarization coefficient of only $1 \%$, its measurethe polarization.

Equation (6) gives the way of using the DOP and AOLP in correction of measured radiance errors caused by the polarization of the reflected light and the polarization dependence of the radiation sensor. The polarization correction could be more complicated for an imager with scan mirror optical system (Sun and Xiong, 2007; Lukashin et al., 2013).

In summary, Eq. (6) shows that if the DOP and AOLP of the reflected solar light at TOA are known, the correction of errors caused by the polarization of light in the ocean-atmosphere-reflected radiance measured by polarization-dependent remote sensors, can be accurately done.

In this study, we will couple an atmospheric radiative transfer model with a rough-ocean-surface light reflection matrix, to do the modeling of solar radiation through the ocean-atmosphere system, focusing on the DOP and AOLP of the reflected solar light at TOA, while also addressing the common intensity of the reflected light.

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page
Abstract
Conclusions
Tables


Full Screen / Esc


## 2 Atmospheric radiative transfer model

A variety of techniques have been developed for computing the radiative transfer including multiple-scattering light through the atmosphere. The most frequently used algorithms that can calculate not only common intensity but also the polarization state of 5 light include the invariant imbedding method (Ambartsumian, 1958; Adams and Kattawar, 1970; Hansen and Travis, 1974; Mishchenko and Travis, 1997), the method of successive order scattering (van de Hulst, 1948; Dave, 1964; Irvine, 1965; Hovenier, 1971; Hansen and Travis, 1974; Min and Duan, 2004; Lenoble et al., 2007; Zhai et al., 2010; Duan et al., 2010), the Monte Carlo method (Hammersley and Handscomb, 1964; Plass and Kattawar, 1968; Kattawar et al., 1973; Hansen and Travis, 1974; Mayer, 2009; Cornet et al., 2010), the discrete ordinate method (Chandrasekhar, 1950; Hansen and Travis, 1974; Stamnes et al., 1988; Schulz et al., 1999; Rozanov and Kokhanovsky, 2006; Ota et al., 2010), and the adding-doubling method (Stokes, 1862; Peebles and Plesset, 1951; van de Hulst, 1963; Twomey et al., 1966; Hansen and 5 Hovenier, 1971; Hansen and Travis, 1974; de Haan et al., 1987; Evans and Stephens, 1991). Some of these methods were already applied to the study of ocean-atmosphere system, e.g., the Monte Carlo method was applied to study the effect of ocean refractive index on the polarization of light over a calm ocean (Kattawar and Adams, 1989); the method of successive order scattering was applied to study the water color of a planar ocean (Chami et al., 2001, 2007); the adding-doubling method was used in the study of the polarized reflection from a wind-ruffled ocean (Takashima and Masuda, 1985), the study of the polarized light at the $\mathrm{O}_{2} \mathrm{~A}$ band from a Lambertian ocean (Stam et al., 1999), and in the study of ocean polarized reflectance including water-leaving radiation for precise aerosol retrieval (Chowdhary et al., 2005, 2006). In this study, we employ the adding-doubling method, and couple it with a rough-ocean-surface light reflection matrix, to do the modeling of solar radiation through the ocean-atmosphere system, focusing on deriving the DOP and AOLP of the reflected light at TOA, within the scope

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion

of using these parameters for correcting measurements from polarization-sensitive instruments in orbit.

In the adding-doubling algorithm, the medium in which the light propagates is separated into many optically thin sub-layers. The optical thickness of each sub-layer is 5 set to be so small that the optical properties of the sub-layer can be represented simply by single-scattering ones. If reflection and transmission are known for each of the two adjacent sub-layers, the reflection and transmission from the combined layer can be obtained by computing the successive reflections back and forth between the two sub-layers. If the optical properties of the two sub-layers are identical, the results for adding-doubling programming, Fourier decomposition is made for the Stokes vector and also for the scattering phase matrix. The numerical solution is obtained for each and also for the scattering phase matrix. The numerical solution is obtained for each Fourier component, and the Stokes vector of the transferred light is calculated with these Fourier components (de Haan et al., 1987; Evans and Stephens, 1991).

Due to its simple essence, the adding-doubling method is a standard radiative transfer algorithm that has a long history of applications and documentations and does not need to be further introduced here. In this study, the adding-doubling model follows the latest program development in this method (Evans and Stephens, 1991), which can be applied to calculate all Stokes parameters of the radiation through a plane-parallel atmosphere composed of absorbing gas, scattering molecules, scattering particulates including various aerosols, water cloud droplets, and ice cloud particles.

In this study, the atmosphere is assumed to be plane-parallel and separated into 32 layers with the ocean surface as the reflecting boundary layer. The atmospheric profiles, which give the pressure, temperature, water vapor, and ozone as functions of altitude, are from the tables of tropical, midlatitude summer, midlatitude winter, subarctic summer, and subarctic winter atmospheric profiles (McClatchey et al., 1972). We use gas absorption coefficients from the $k$-distribution treatment (Kato et al., 1999) of the spectral data from the line-by-line radiative transfer model (LBLRTM) (Clough et al., 1992, 1995) using the MODTRAN 3 dataset (Kneizys et al., 1988). Ozone absorption

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


coefficients are also taken from the ozone cross-section table provided by the World Meteorological Organization (1985) for wavelengths smaller than $0.7 \mu \mathrm{~m}$. Molecular scattering optical thickness above any pressure level, $P$, is from (Hansen and Travis, 1974)
${ }_{5} \tau=0.008569 \lambda^{-4}\left(1+0.0113 \lambda^{-2}+0.00013 \lambda^{-4}\right)\left(\frac{P}{P_{0}}\right)$,
where $\lambda$ is the wavelength of light in $\mu \mathrm{m}, P$ is the pressure in mb , and $P_{0}=1013.25 \mathrm{mb}$ is the standard surface pressure. The scattering phase matrix elements of molecular atmosphere are based on Rayleigh scattering solution with a depolarization factor of 0.03 (Hansen and Travis, 1974). Single-scattering properties of aerosol and cloud particles are calculated differently. For spherical droplets including liquid aerosols and water cloud particles, Mie solution (Mie, 1908; Fu and Sun, 2001) is applied. For solid or mixed phase aerosols or small ice crystals, which are usually nonspherical particles, the finite-difference time domain (FDTD) method (Sun et al., 1999, 2002) and the discrete dipole approximation (DDA) (Zubko et al., 2006, 2009) will be used. For large ice crystals, we will use the data from geometric optics approximation (GOA) (Macke, 1993; Yang and Liou, 1996). The C1 size distribution (Deirmendjian, 1969) is used for water cloud droplets. The 28 measured ice-crystal size distributions used in Fu (1996) and the two other size distributions in Mitchell et al. (1996) will be used to calculate the volume single-scattering properties of ice clouds. Two-mode lognormal size distributions (Davies, 1974; Whitby, 1978; Reist, 1984; Ott, 1990; Porter and Clarke, 1997) are applied for aerosols.

Traditional radiative transfer modeling generally assumes independent radiation process for molecules and aerosol or cloud particles, which means that molecular radiation process and particulate process are assumed at different layers of atmosphere to avoid the convolution of the light scattering phase functions of molecules and particulates in the radiative transfer calculations. This may involve errors due to unphysical single-scattering properties in each layer. In this study, for layers with more than one

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion
type of scattering atmospheric components, such as layers with both air molecules and aerosols, and layers composed of air molecules, aerosols, and cloud particles, the mixed single-scattering properties, including absorption and scattering coefficients and phase matrix elements, are calculated, as the mixed optical property of the layer.

In the radiative transfer calculations, the phase matrix elements of particulate atmospheric components are input to the radiative transfer model as Legendre polynomial series (e.g. Evans and Stephens, 1991). If the phase matrix elements of the scattering particles have strong forward-scattering peaks (what happens on large cloud particles), it needs many Legendre high-order terms to approach the original phase matrix elements, which will heavily increase the computation time and memory of the radiative transfer calculation due to the large increment in the Legendre terms and stream number in the modeling. To avoid this problem, we conduct a delta adjustment (e.g. Gu and Liou, 2001) to the layer's mixed single-scattering properties prior to the Legendre series expansion of the scattering phase matrix elements. This means a truncation of the forward-scattering peak in the phase matrix elements for particulate atmospheric components. In this study, this is done in a modified way as shown in Fig. 2, exemplified by the conventional phase function $\left(P_{11}\right)$ of a water cloud. The scattering peak between the scattering angle of $\theta_{0}$ and the forward-scattering direction is truncated and replaced by values from a linear extrapolation algorithm
$\frac{\log _{10} P_{11}(\theta)-\log _{10} P_{11}\left(\theta_{1}\right)}{\left(\theta-\theta_{1}\right)}=\frac{\log _{10} P_{11}\left(\theta_{0}\right)-\log _{10} P_{11}\left(\theta_{1}\right)}{\left(\theta_{0}-\theta_{1}\right)}$
where $\theta_{0}$ and $\theta_{1}$ are two neighboring scattering angles and $\theta_{1}>\theta_{0}$, and $\theta$ is any scattering angle between 0 and $\theta_{0}$. The truncated phase function is integrated over the scattering angle to obtain the energy loss fraction $f$ due to the truncation of the forwardscattering peak, which is the difference between the integral of original phase function and the integral of truncated phase function over scattering angles. After the energy loss fraction $f$ is obtained, the scattering optical thickness ( $\tau_{\mathrm{s}}^{\prime}$ ), total optical thickness

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

$\left(\tau^{\prime}\right)$, and single-scattering albedo ( $\alpha^{\prime}$ ) of the adjusted cloud are
$\tau_{\mathrm{s}}^{\prime}=(1-f) \tau_{\mathrm{s}}$,
$\tau=\tau_{\mathrm{a}}+\tau_{\mathrm{s}}$,
and
$\alpha^{\prime}=\tau_{\mathrm{s}}^{\prime} / \tau^{\prime}$,
where $\tau_{\mathrm{s}}$ and $\tau_{\mathrm{a}}$ are the scattering and absorption optical thickness of the original clouds, respectively. Other elements of phase matrix are also adjusted by conserving their ratio values to the conventional phase function $\left(P_{11}\right)$ (e.g. $P_{12} / P_{11}$ does not change after the adjustment). The adjusted phase matrix elements are renormalized by ( $1-f$ ).

The delta-adjustment treatment may cause some numerical errors in calculation of the total reflectance from the clouds due to the strong forward-scattering peak in their phase-matrix elements. However, since radiation from clouds has a very low degree of polarization, which we show later, the delta-adjustment approximation should not cause any significant errors in the correction of radiance measurement caused by polarization state of light in remote-sensing inter-calibration applications.

## 3 Surface reflection model

The major expansion to the adding-doubling method in this study is the coupling of the rough-ocean-surface light reflection matrix with the atmospheric layers. The ocean 20 surface light reflection matrix is based on an empirical foam spectral reflectance model (Koepke, 1984), an empirical spectral reflectance model for water volume below the surface (Morel, 1988), and the standard Kirchhoff approach under the stationary phase approximation (Mishchenko and Travis, 1997) for foam-free waves with slope distribution as given in Cox and Munk (1954, 1956). To examine the dependence of the

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page
Abstract
Conclusions
Tables
References
Figures


Full Screen / Esc
reflected light's polarization on the direction of wind over ocean, the wave slope distribution models with the Gram-Charlier series expansion (Cox and Munk, 1954), and without the Gram-Charlier series expansion (Cox and Munk, 1956), are both integrated in the adding-doubling radiative transfer model. The surface reflection matrix with $4 \times 4$ elements is calculated as

$$
\begin{equation*}
\boldsymbol{R}_{0}\left(\theta_{\mathrm{s}}, \theta_{\mathrm{v}}, \phi\right)=f \mathbf{R}_{\mathrm{WC}}+(1-f) \mathbf{R}_{\mathrm{WL}}+(1-f) \frac{\pi \mathbf{M}\left(\theta_{\mathrm{s}}, \theta_{\mathrm{v}}, \phi\right)}{4 \cos ^{4} \beta \cos \theta_{\mathrm{s}} \cos \theta_{\mathrm{v}}} P\left(Z_{x}, Z_{y}\right), \tag{14}
\end{equation*}
$$

where $\theta_{\mathrm{s}}, \theta_{\mathrm{v}}$, and $\phi$ denote solar zenith angle, viewing zenith angle, and relative azimuth angle of the reflected light, respectively. The fraction of whitecap (WC) is denoted as $f$. The fraction of whitecaps has a large uncertainty, which not only depends on the wind speed but also on the fetch and on the factors altering the mean lifetime of the whitecaps, such as water temperature and thermal stability of the lower atmosphere (Koepke, 1984). In this study, we use the expression by Monahan and O'Muircheartaigh (1980)
$f=2.95 \times 10^{-6} W^{3.52}$,
where the wind speed $W$ is in the units of $\mathrm{ms}^{-1}$. In Eq. (14), $\mathbf{R}_{\mathrm{wc}}$ is the whitecap reflection matrix. Since foam is generally assumed to be a Lambertian reflector, the only nonzero element of $\mathbf{R}_{\text {WC }}$ is the reflectance, which is from an empirical foam spectral reflectance model (Koepke, 1984) in this study. The water-leaving (WL) reflection is also assumed to be Lambertian. Similar to $\mathbf{R}_{\mathrm{Wc}}, \mathbf{R}_{\mathrm{WL}}$ has only one nonzero element, the reflectance of water volume below the surface, which is obtained from an empirical spectral reflectance model (Morel, 1988) with an ocean water pigment concentration of $0.01 \mathrm{mg} \mathrm{m}^{3}$. The $4 \times 4$ elements of $\mathbf{M}\left(\theta_{s}, \theta_{v}, \phi\right)$ for each wave facet orientation are calculated in the same way as in Mishchenko and Travis (1997) based on the Fresnel Laws. As given in Cox and Munk (1954, 1956), $P\left(Z_{x}, Z_{y}\right)$ is the wave slope probability

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page
Abstract
Conclusions
Tables
References
Figures


Full Screen / Esc

distribution as a function of the two components of the surface slope
$Z_{x}=\frac{\partial Z}{\partial x}=\frac{\sin \theta_{\mathrm{v}} \cos \phi-\sin \theta_{\mathrm{s}}}{\cos \theta_{\mathrm{v}}+\cos \theta_{\mathrm{s}}}$,
and
$z_{y}=\frac{\partial z}{\partial y}=\frac{\sin \theta_{\mathrm{v}} \sin \phi}{\cos \theta_{\mathrm{v}}+\cos \theta_{\mathrm{s}}}$,
${ }_{5}$ where $Z$ denotes the height of the surface. In Eq. (14), $\beta$ is the tilting angle of wave facet, thus
$\tan \beta=\sqrt{Z_{x}^{2}+Z_{y}^{2}}$.
If wind direction is not accounted for, Cox and Munk (1956) gives $P\left(Z_{x}, Z_{y}\right)$ as a function of wind speed in a form
$P\left(Z_{x}, Z_{y}\right)=\frac{1}{\pi \sigma^{2}} \exp \left(-\frac{Z_{x}^{2}+Z_{y}^{2}}{\sigma^{2}}\right)$,
where $\sigma^{2}$ is linearly related to wind speed $W\left(\mathrm{~ms}^{-1}\right)$ in an empirical form
$\sigma^{2}=0.003+5.12 \times 10^{-3} W$,
Furthermore, to study the sensitivity of reflected light's polarization state to wind direction over the ocean, we also integrate in the model a form of the wave slope probability

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

Abstract
Conclusions
Tables


14
$\checkmark$
Back
Introduction
References
Figures
$\rightarrow 1$
-
Close

Full Screen / Esc
$P\left(Z_{\mathrm{c}}, Z_{\mathrm{u}}\right)=\frac{1}{2 \pi \sigma_{\mathrm{c}} \sigma_{\mathrm{u}}} \exp \left(-\frac{\xi^{2}+\eta^{2}}{2}\right)\left[1-\frac{c_{21}}{2}\left(\xi^{2}-1\right) \eta-\frac{c_{03}}{6}\left(\eta^{3}-3 \eta\right)+\right.$,

where $\xi=\frac{z_{\mathrm{c}}}{\sigma_{\mathrm{c}}}$ and $\eta=\frac{z_{\mathrm{u}}}{\sigma_{\mathrm{u}}}$, with $Z_{\mathrm{c}}$ and $Z_{\mathrm{u}}$ denoting the two components of the surface slope crosswind and upwind, $\sigma_{\mathrm{c}}$ and $\sigma_{\mathrm{u}}$ denoting the rms values of $Z_{\mathrm{c}}$ and $Z_{\mathrm{u}}$, respectively. $\sigma_{\mathrm{c}}^{2}, \sigma_{\mathrm{u}}^{2}$, and the coefficients $c_{21}, c_{03}, c_{40}, c_{04}$, and $c_{22}$ are all empirical linear functions of wind speed as given in Cox and Munk (1954). The geometry for the definition of wind direction is illustrated in Fig. 3.

The ocean surface is treated as the bottom (1st) layer in the adding-doubling calculation in this study. The cosine azimuth modes and sine azimuth modes of the ocean reflection matrix elements are integrated into the adding-doubling process as the bottom layer optical properties functioning as boundary conditions. In this study, the $4 \times 4$ ocean reflection matrix elements calculated in Eq. (14) are transformed into cosine azimuth modes or sine azimuth modes by discrete Fourier transform (DFT) over azimuth angles with a numerical Gauss integration.

## 4 Numerical results

The objective of this study is to enable and to demonstrate numerical methods for building efficient PDMs to correct satellite-measured solar radiance, which has bias errors caused by the polarization of reflected light. The numerical results reported here will optimize the input parameters of the radiative transfer model. However, the emphasis of our numerical calculation is to study the sensitivity of the polarization state of the reflected light to the solar wavelength, incidence and viewing geometries, and components of Earth-atmosphere system. This includes solar zenith angle (SZA), viewing zenith angle (VZA), relative azimuth angle (RAZ), reflection surface conditions, atmospheric gas absorption, and molecular and particulate scattering to the light. With these sensitivity studies, we aim to identify the incidence, surface, or atmospheric parameters to which the DOP and AOLP are not sensitive. These parameters are given certain val-

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Introduction
References
Figures


Full Screen / Esc

tables. With this approach, we can make PDMs as functions of only necessary input parameters for quick accesses during polarization correction in practice.

In the ADRTM, the adding-doubling scheme is actually conducted on the coefficients of the Fourier series expansion of the Stokes parameters over azimuth angle (de Haan et al., 1987; Evans and Stephens, 1991). After the adding-doubling calculations, the cosine modes and sine modes (Evans and Stephens, 1991) of the Stokes parameters are transformed back into the Stokes parameters. Therefore, the number of the cosine modes and sine modes in the Fourier series expansion of the Stokes parameters affects the accuracy of the radiative transfer calculation. A bigger number is required for accurate calculation of radiation with stronger anisotropy. Sensitivity of modeled Stokes parameters to mode number shows that a mode number of 18 is adequate for modeling all atmospheric and ocean conditions.

Also, in adding-doubling schemes, the calculation for transferred light's sine and cosine modes of the Stokes parameters is conducted only on streams over discrete viewing zenith angles. Using more streams means higher resolution in the zenith angles and better accuracy in the results, but also means requiring more computational resources. To keep the computing time reasonable, we limited the number of streams to 18. In this study, the streams follow a set of discrete Gaussian quadrature angles. Integration of radiance over limited discrete viewing zenith angles at Gaussian quadrature points can result in more accurate flux than over uniformly distributed discrete angles. However, this treatment will output Stokes parameters at Gaussian quadrature points, which is not the easiest way for storing and accessing the parameters during applications. To obtain the calculated Stokes parameters and the DOP and AOLP derived from these parameters over high-resolution uniform discrete viewing zenith angles, the Stokes parameters at only the Gaussian quadrature points are extrapolated and interpolated to the uniform grid points of viewing zenith angle. With this approach, using only 18 streams can produce accurate Stokes parameters of reflected light at all viewing angles and over nearly all atmospheric and ocean conditions.

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


Printer-friendly Version
Interactive Discussion


Figure 4 shows the comparison of the total reflectance at the wavelength of 670 nm on the principal plane from the ADRTM and from the widely-validated DISORT. The atmosphere is in the mid-latitude summer (MLS) pristine profile with only molecular scattering (Rayleigh scattering) and gas absorption. The empirical ocean foam and
5 water-leaving reflectance models and the wave slope probability distribution model with a Gram-Charlier series expansion (Cox and Munk, 1954), which is described in Sect. 3, are used. The wind speed is $7.5 \mathrm{~ms}^{-1}$ and wind direction is assumed in the reverse direction of $x$-axis as illustrated in Fig. 1 (i.e. wind direction is $0^{\circ}$ ). The solar zenith angle (SZA) is $23.4^{\circ}$ and $43.16^{\circ}$, respectively. In the numerical simulations, we 10 use 36 streams in the DISORT and 18 streams in the ADRTM. In the ADRTM calculation, the number of Fourier expansion modes is set to 18. We can see that the total reflectance from the ADRTM is very close to that from the DISORT, with significant differences only at VZA $>\sim 80^{\circ}$, when the atmospheric path optical thickness is large. For VZA $<\sim 80^{\circ}$, the largest relative difference in reflectance from the ADRTM and the DISORT is smaller than $\sim 4 \%$ at the VZA where reflectance is minimum. Since most in-orbit sensors do not report observations for VZA larger than $\sim 70^{\circ}$, the focus for the modeling quality is really in the VZA range from $0^{\circ}$ to $70^{\circ}$. As a scalar approximation to a vector radiative transfer problem, DISORT may involve errors due to the negligence of polarization (Adams and Kattawar, 1970; Lacis et al., 1998). At small VZA, since the path optical thickness is small at the near-IR wavelength, the errors in the DISORT caused by the polarization of scattered light are also small, so the DISORT result is very close to the ADRTM data. At a larger SZA of $43.16^{\circ}$, we can see that the agreement of the DISORT and ADRTM results are even better. For VZA < $\sim 80^{\circ}$, the largest relative difference in reflectance from the ADRTM and the DISORT is smaller than
$25 \sim 2 \%$ at VZA where reflectance reaches its minimum value. From these case studies, we can conclude that the ADRTM with 18 streams and 18 Fourier expansion modes can produce reflectance consistent with other radiative transfer model at solar spectra.

Figure 5 shows the DOP on the principal plane from the ADRTM for the cases in Fig. 4. We can see that for both of the solar incidence geometries, the DOPs reach

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion
their maxima at the VZA of $\sim 60^{\circ}$ in the forward scattering direction and reach their minima at about the backscattering angles (i.e. $23.44^{\circ}$ and $43.16^{\circ}$, respectively). The DOPs also strongly depend on solar zenith angles. Larger solar zenith angles result in larger DOPs at nadir direction. Based on the definition of AOLP and the geometry over the RAZ range of $0^{\circ}$ to 180 are displayed in Fig. 6. We can see that on the principal plane, the AOLPs are $\sim 90^{\circ}$ at nearly all of the VZAs. Solar zenith angle significantly affects AOLP's distribution pattern in VZA and RAZ. Therefore, SZA, VZA, and RAZ are three critical parameters to determine DOP and AOLP in the PDMs.

To build a comprehensive set of PDMs, we also need to check the dependence of DOP and AOLP on the background atmospheric profiles. Actually, the only significant effect of different atmospheric profiles on reflected solar radiance spectra is the gas absorption to the light. Therefore, the sensitivity of solar light's polarization to atmospheric profiles can be examined by studying the dependence of the DOP and AOLP on the gas absorption coefficients. Figure 7 shows the total reflectance, DOP, and AOLP at wavelength 670 nm at TOA, which is calculated with the ADRTM at a solar zenith angle of $43.16^{\circ}$ over a pristine clear sky ocean with a wind speed of $7.5 \mathrm{~m} \mathrm{~s}^{-1}$. The total reflectance and DOP with the mid-latitude summer gas absorption (solid curves) and those with 4 -times the mid-latitude summer gas absorption (black dots) are shown. Also shown are the AOLP with the mid-latitude summer gas absorption (Fig. 7e) and those with 4 -times the mid-latitude summer gas absorption (Fig. 7f). From these figures, we can see that gas absorption can significantly affect the total reflectance, but has little effect on both DOP and AOLP. This is consistent with the results for single scattering by particles (Sun et al., 2002). Therefore, gas absorption in different atmospheric pro- AOLP. A standard atmospheric profile should be sufficient for accurate modeling of the DOP and AOLP of the reflected solar light from the ocean-atmosphere system.

It is well known that wind-caused ocean surface roughness can significantly affect the reflectance of solar light. However, it is not yet known how much wind speed and direc-

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


tion can affect the polarization state of reflected solar light at TOA. Figure 8 shows the total reflectance and DOP on the principal plane, which is calculated with the ADRTM at wavelength 670 nm . Pristine clear atmosphere with the mid-latitude summer atmospheric profile is assumed. The SZA is $33.30^{\circ}$. Wind direction is assumed to be at $0^{\circ}$. 5 Wind speeds are given as $5.0 \mathrm{~ms}^{-1}, 7.5 \mathrm{~m} \mathrm{~s}^{-1}, 10.0 \mathrm{~ms}^{-1}$, and $15.0 \mathrm{~ms}^{-1}$, respectively. We can see that wind speed significantly affects the total reflectance at RAZ $=0^{\circ}$, but has only a small effect on the total reflectance at RAZ $=180^{\circ}$. Wind speed effect on the DOP is also insignificant. The AOLPs of these cases are shown in Fig. 9. We should note that the AOLP values of $\sim 0^{\circ}$ and $\sim 180^{\circ}$ mean the same polarization plane of the linear polarization and have no difference to the measurement instrument. Thus the deep blue and deep red angular regions in Fig. 9 actually represent similar AOLPs and the same polarization direction. From Fig. 9, we can see that the wind speed effect on the AOLP is also small. In the PDM development and applications we will be able to use wind speed assimilated from GMAO weather data products. Our modeling results show that the uncertainty of wind speed data will only have a small impact on the DOP and AOLP.

Wind direction and ocean wave slope probability distribution models like the one with wind direction dependence (Cox and Munk, 1954) and the one without wind-direction dependence (Cox and Munk, 1956), could also affect the calculated reflectance and polarization state of the reflected light at TOA. Figure 10 shows the total reflectance and DOP on the principal plane, which is calculated with the ADRTM at wavelength 670 nm . Pristine clear atmosphere with the mid-latitude summer atmospheric profile is used. The SZA is $33.30^{\circ}$. Wind speed is $7.5 \mathrm{~m} \mathrm{~s}^{-1}$. Both the ocean wave slope probability distribution model with wind direction dependence (Cox and Munk, 1954) and the one without wind-direction dependence (Cox and Munk, 1956) are used in the calculation. In the ocean wave slope probability distribution model with wind direction dependence, wind direction is set at $0^{\circ}, 90^{\circ}$, and $180^{\circ}$, respectively. We can see that varying wind direction or using different ocean wave slope probability distribution models can significantly change the total reflectance at $R A Z=0^{\circ}$, but has little impact on the

total reflectance at RAZ $=180^{\circ}$. Varying wind direction, or using different ocean wave slope probability distribution models, has nearly no effect on the DOP at RAZ $=180^{\circ}$, and only causes small changes in the DOP at RAZ $=0^{\circ}$ when VZA $>60^{\circ}$. The AOLPs for the cases in Fig. 10 are shown in Fig. 11. The AOLPs from the ocean surface models with different wind directions and different wave slope probability distributions show very similar patterns, with only small differences when AOLPs are close to $0^{\circ}$ and $180^{\circ}$. Since wind direction may not be reliably obtained over ocean, and wind direction and wave slope distribution models have little effect on the polarization state of reflected light at TOA, we will use the Cox-and-Munk ocean wave slope probability distribution model without wind direction dependence (Cox and Munk, 1956) in all of the following studies and in the future modeling for operational PDMs. Using the Cox-and-Munk ocean wave slope probability distribution model without wind direction dependence can make the reflection field symmetric to the principal plane. Therefore, we only need to calculate and store the reflectance, DOP, and AOLP over the RAZ of $0^{\circ}$ to $180^{\circ}$ in practice. These quantities will easily be obtained by symmetry for the RAZ of $180^{\circ}$ to $360^{\circ}$. However, it is worth noting that among the Stokes parameters / and $Q$ are symmetric to the principal plane, but $U$ and $V$ are oddly symmetric to the principal plane, i.e.
$I\left(\mathrm{VZA}, 360^{\circ}-\mathrm{RAZ}\right)=I(\mathrm{VZA}, \mathrm{RAZ})$,
$Q\left(\mathrm{VZA}, 360^{\circ}-\mathrm{RAZ}\right)=Q(\mathrm{VZA}, \mathrm{RAZ})$,
$U\left(V Z A, 360^{\circ}-R A Z\right)=-U(V Z A, R A Z)$,
$V\left(V Z A, 360^{\circ}-R A Z\right)=-V(V Z A, R A Z)$.
From Eqs. (3), (4), and (22a-c), we can further derive out
$\operatorname{DOP}\left(V Z A, 360^{\circ}-R A Z\right)=\operatorname{DOP}(V Z A, R A Z)$,
AOLP $\left(V Z A, 360^{\circ}-R A Z\right)=180^{\circ}-$ AOLP $(V Z A, R A Z)$.
In study of the polarization state of the reflected solar light from the ocean-atmosphere system, there is also a concern that the shadows of ocean waves may affect the DOP

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc
and AOLP of the reflected light. In this work, the effect of shadowing by surface waves on reflected light is examined by multiplying the ocean reflection matrix by a bidirectional shadowing function (Tsang et al., 1985; Mishchenko and Travis, 1997)

13, 17585-17642, 2013

$$
\begin{equation*}
S\left(\theta_{\mathrm{s}}, \theta_{\mathrm{v}}\right)=\frac{1}{1+\Lambda\left(\theta_{\mathrm{s}}\right)+\Lambda\left(\theta_{\mathrm{v}}\right)}, \tag{24}
\end{equation*}
$$

5 where

$$
\begin{equation*}
\Lambda(\theta)=\frac{1}{2}\left\{\frac{\sigma}{\cos \theta}\left[\frac{\left(1-\cos ^{2} \theta\right)}{\pi}\right]^{1 / 2} \exp \left[-\frac{\cos ^{2} \theta}{\sigma^{2}\left(1-\cos ^{2} \theta\right)}\right]-\operatorname{erfc}\left[\frac{\cos \theta}{\sigma \sqrt{1-\cos ^{2} \theta}}\right]\right\} \tag{25}
\end{equation*}
$$

and $\sigma$ is calculated with Eq. (20) and $\operatorname{erfc}(x)$ is the complementary error function. Figure 12 shows the total reflectance and DOP on the principal plane at the wavelength of 550 nm from the mid-latitude summer pristine atmosphere over the ocean with and without wave shadows. The wind speed is $7.5 \mathrm{~ms}^{-1}$. The SZA is $33.30^{\circ}$. We can see that ocean wave shadowing can significantly reduce the total reflectance at VZA $>\sim 60^{\circ}$, but its effect on reflectance at smaller VZA and on DOP is not big. Shown in Fig. 13 are the AOLPs of the cases in Fig. 12. It can be seen that the ocean wave shadows also do not significantly affect the AOLPs of the reflected solar light.

To derive PDMs that are adequate for application over broad solar spectral range, we need to investigate the sensitivity of the polarization state of reflected light to the wavelength. Figure 14 shows the total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelengths of 470 nm and 865 nm , respectively. Pristine clear atmosphere with the mid-latitude summer atmospheric profile is used. The SZA is $33.30^{\circ}$. Wind speed is $7.5 \mathrm{~ms}^{-1}$. We can see that changing the wavelength can affect the total reflectance very much. Although changing solar wavelength also significantly affects the DOP especially when VZA $>\sim 45^{\circ}$, the DOP's sensitivity to wavelength is not as significant as the total reflectance's. Though not shown here,
we also find that increasing the solar zenith angle can largely increase the difference between the DOPs of different wavelengths at all viewing zenith angles. The AOLPs for the cases in Fig. 14 are displayed in Fig. 15. AOLP's dependence on wavelength is relatively more significant than DOP's. Therefore, the PDMs must be made a strong 5 function of solar wavelengths, but may not require high spectral resolution.

One of the most uncertain components in the atmosphere is aerosols. Effect of aerosols on solar reflectance has been widely studied. Aerosols' effect on polarization of light also attracts many efforts (Chowdhary et al., 2002; Mishchenko et al., 2007, 2013; Sun et al., 2013). In this study, to calculate the effect of aerosols on the polarization state of reflected light at TOA, we chose an example of a mid-latitude summer atmosphere with sea-salt aerosols. The calculation is conducted at the visible wavelength of 550 nm , where the refractive index of sea-salt is given as $1.5+i 10^{-8}$ (Chamaillard et al., 2003). The sea-salt aerosol particle shapes are assumed being the agglomerated debris as shown in Fig. 16, and their single-scattering properties are from the DDA calculations (Zubko et al., 2006, 2009, 2013). A two-mode lognormal size distribution (Porter and Clarke, 1997) is applied for the sea-salt aerosols in a form
$\mathrm{d} N / \mathrm{d} \log D=\bmod e_{1}+\operatorname{mode}{ }_{2}$,
$\operatorname{mode}_{i}=\frac{M}{D \log \sigma_{\mathrm{g}} \sqrt{2 \pi}} \exp \left[\frac{-\left(\log D-\log D_{\mathrm{g}}\right)^{2}}{2 \log ^{2} \sigma_{\mathrm{g}}}\right]$ where $i=1,2$.
In Eqs. (26a) and (26b), $D$ is the aerosol diameter in $\mu \mathrm{m}, M$ is a multiplier, $\sigma_{\mathrm{g}}$ is the geometric standard deviation, and $D_{\mathrm{g}}$ is the geometric mean diameter in $\mu \mathrm{m}$. In this study, we chose a sea-salt aerosol case for wind speed between 5.5 to $7.9 \mathrm{~ms}^{-1}$ from Porter and Clarke (1997) with all the parameters for fine and coarse mode and size distribution curves shown in Fig. 17. The optical thickness of the aerosol layer is given

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc as 0.1 . Figure 18 shows a comparison of the total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelengths of 550 nm from the pristine mid-latitude summer ocean-atmosphere system and those from the mid17606
latitude summer ocean-atmosphere system with sea-salt aerosols. The ocean wind speed is $7.5 \mathrm{~m} \mathrm{~s}^{-1}$. The SZA is $33.30^{\circ}$. We can see that aerosols can increase the total reflectance and decrease the DOP significantly. The AOLPs for the cases in Fig. 18 are given in Fig. 19. We can see that aerosols also noticeably change the AOLP. These re5 sults tell us that aerosols are an important component in the atmosphere that can alter the polarization state of the reflected light at TOA. Thus, in building the PDMs aerosol should be carefully accounted for.

The multiple scattering processes in water clouds can largely depolarize the reflection and thus result in significantly smaller DOP of reflected solar light at TOA than clear sky ocean. However, the spherical droplets in water clouds have some distinct light scattering features, such as the maxima (rainbow) at scattering angles of $\sim 130^{\circ}-$ $160^{\circ}$ (Deirmendjian, 1964), where the polarization state of scattered light could be very different. A modified gamma (MG) particle size distribution (PSD) is assumed in this study for water cloud droplets
${ }_{5} \mathrm{~d} N / \mathrm{d} R=N_{0} R^{v} \exp \left(-v \frac{R}{R_{0}}\right)$,
where $R$ denotes the droplet radius, $R_{0}$ is the modal radius, $v$ defines the shape of the distribution, and
$N_{0}=\frac{v^{v+1}}{\Gamma(v+1) R_{0}^{v+1}} N_{\text {tot }}$
is a constant with $\Gamma(v+1)$ being the gamma function and $N_{\text {tot }}$ being the total number of particles per unit volume (Petty and Huang, 2011). The commonly used C1 size distribution (Deirmendjian, 1969), which is defined by Eq. (27) with $R_{0}=4 \mu \mathrm{~m}$ and $v=6$, is applied in this study. Figure 20 shows the total reflectance and DOP on the principal plane, which calculated with the ADRTM at the wavelengths of 550 nm from the ocean-atmosphere system with water clouds of optical thickness 5.0 and 10.0, respectively. The water cloud layer is assumed at 2 to 3 km over the ocean. The wind speed is

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Introduction
References
Figures
Tables

-I


Back


Close
Full Screen / Esc
$7.5 \mathrm{~ms}^{-1}$. The SZA is $33.30^{\circ}$. It can be seen that the reflectance of the water cloud with optical thickness of 10.0 is nearly two times that of the water cloud with optical thickness of 5.0. However, the reflectance maxima at $\mathrm{VZA}=2^{\circ}$ and $\mathrm{RAZ}=0^{\circ}, \mathrm{VZA}=35^{\circ}$ and $R A Z=180^{\circ}$ (rainbow), and VZA $=73^{\circ}$ and $R A Z=180^{\circ}$, exists for both optical thicknesses. Also, at these reflectance maxima angles, the DOP is very sensitive to the optical thickness. Larger optical thickness of the water cloud significantly decreases the DOP at these reflectance maxima angles and at other VZAs at RAZ $=0^{\circ}$. However, the DOPs of water clouds are generally relatively small, not larger than $\sim 20 \%$, for most of the viewing angles in this case. Moreover, the AOLPs of these water clouds in Fig. 21 show that varying optical thickness of water clouds has nearly no effect on the polarization angle.

To study the polarized reflection from ice clouds, we tested the in-situ-measured 28 ice cloud particle size distributions used in Fu (1996) and various ice cloud particle shapes including solid and hollow columns, plates, smooth and rough surface bullet rosettes of four and six branches, and smooth and rough surface column aggregates. The single-scattering properties of these nonspherical ice crystals are from the geometric ray-tracing approximation (Yang and Liou, 1996). Our tests show that applying different size distributions has a negligible effect on the DOP and AOLP of thin ice clouds, and varying particle shapes can only cause as big as $\sim 10 \%$ change in the DOP of thin ice clouds, but that the AOLPs are minimally affected by the particle shapes. Figure 22 gives an example of the size distribution for ice clouds. Also shown in this figure is the assumed ice crystal aggregate particle shape. Figure 23 shows the total reflectance and DOP on the principal plane, which is calculated with the ADRTM at wavelengths 865 nm from the mid-latitude summer ocean-atmosphere system composed of an ice cloud layer. The ice cloud layer has an optical thickness 5.0 at wavelength 865 nm . The particle size distribution and the particle shape of the ice cloud are shown in Fig. 22. The ice cloud layer is set between 7 and 8 km over the ocean with a wind speed of $7.5 \mathrm{~ms}^{-1}$. The SZA is $33.30^{\circ}$. We can see that the total reflectance from the thick ice cloud does not have the maxima as shown in Fig. 20

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


Printer-friendly Version
Interactive Discussion
for water clouds. Also, since we assumed randomly-oriented ice crystal aggregates in the calculation, there is no specular reflection peak from horizontally-oriented ice columns or plates either. The DOPs of the thick ice clouds in Fig. 23 at most of the viewing angles are smaller than $\sim 4 \%$, so the polarization of solar reflection from thick 5 ice clouds may not be an issue for measurements. Due to the insignificant DOP of thick ice clouds, the AOLPs of these clouds are not shown here. However, when ice clouds are so thin that they are transparent to the solar radiation, it becomes a big problem for the polarization state of the reflected light at TOA. Figure 24 shows the same as in Fig. 23, but for an ice cloud optical thickness of 0.3 at 865 nm . Also shown in Fig. 24

## 5 Summary and conclusion

In this study, the polarized solar radiation reflected from the ocean-atmosphere system is studied with an adding-doubling radiative transfer model (ADRTM). The Cox-and-Munk ocean wave slope distribution model is used in calculation of the reflection matrix of a wind-ruffled ocean surface. An empirical foam spectral reflectance model and an empirical spectral reflectance model for water volume below the surface are integrated in the ocean surface model. Solar reflectance from the ADRTM is in excellent agreement with that from the discrete-ordinate radiative transfer (DISORT) model is the total reflectance and DOP from the pristine atmosphere for comparison. We can see that the thin cirrus could significantly increase the total reflectance and decrease the DOP of the reflected light from the surface. When VZA is large, as shown in Fig. 25 the AOLPs are also noticeably changed by the thin cirrus. Since thin cirrus clouds are widely distributed around the globe, their effects on the polarization state of reflected solar light from the Earth-atmosphere system must be carefully studied (Sun et al., at the near-IR wavelength for VZA $<\sim 80^{\circ}$. The sensitivity studies for the polarized so- lar radiation are conducted for various ocean-surface and atmospheric conditions for understanding the dependencies and optimizing the stratification o polarization distri-

bution models (PDMs), which are to be used in the inter-calibration of the polarizationsensitive imager measurements with CLARREO data. We found that the total solar reflectance from the ocean-atmosphere system is very sensitive to wavelength, solar and viewing angles, cloud and aerosols, surface wind speed and direction, and atmo5 spheric gas absorption. However, the degree of polarization (DOP) and angle of linear polarization (AOLP) of the reflected light are less sensitive to wind speed and direction and virtually not sensitive to atmospheric gas absorption. Water clouds generally have small DOPs but at some specific viewing angles, such as the rainbow angle, their DOPs are still significant. Thick ice clouds have the minimum DOPs, which will not cause significant errors due to polarization in the measurement even by a satellite imager with strong polarization dependence. The major issues related to solar radiation polarization are aerosols and thin ice clouds. The two atmospheric components must be carefully accounted for in making the CLARREO PDMs. The major problem with thin cirrus clouds and aerosols related to the polarization of reflected solar light from the ocean-atmosphere system is their optical thickness. However, although thin cirrus clouds and aerosols could significantly affect DOP, their effect on AOLP is not significant. Also, applying different size distributions has negligible effects on the DOP and AOLP of light from thin ice clouds, and the effect of different particle shapes of thin cirrus on the polarization state of the reflected light is also moderate.

This work demonstrates a radiative transfer methodology for building and optimizing the PDMs as functions of ocean surface conditions, aerosol and clouds types, and atmospheric components. Our results provide a reliable approach for building the spectral CLARREO PDMs over the broad solar spectra, which cannot be achieved by empirical PDMs based on the analysis of available data from current polarimetric sensors in orbit. Further studies are needed for comparing the modeling results with PARASOL data and for modeling different scene types over land surfaces.

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## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Printer-friendly Version
Interactive Discussion

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## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


Printer-friendly Version
Interactive Discussion

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## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin


Printer-friendly Version
Interactive Discussion


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13, 17585-17642, 2013

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Printer-friendly Version
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ACPD
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Title Page


Full Screen / Esc


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ACPD
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W. Sun and C. Lukashin


Printer-friendly Version
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## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

> Printer-friendly Version

Interactive Discussion


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ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page
Abstract
Introduction
Conclusions
References

Figures
Tables

14
$\rightarrow 1$
-

Back
Close

Full Screen / Esc

Printer-friendly Version
Interactive Discussion


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

Tables

14
Figures
$\checkmark$

Back
Close

Full Screen / Esc

Printer-friendly Version


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

Abstract

Conclusions

Tables

14
Introduction

References

Figures
$\checkmark$

Back

Full Screen / Esc


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

Abstract

Conclusions

Tables

14
Introduction

References

Figures

4

Back
Close

Full Screen / Esc

Printer-friendly Version


Fig. 4. Comparison of the total reflectance at the wavelength of 670 nm on the principal plane from the ADRTM (black dots) and that from the DISORT (solid curve). The atmosphere is of the mid-latitude summer profile with only Rayleigh scattering and gas absorption. The wind speed is $7.5 \mathrm{~m} \mathrm{~s}^{-1}$ and wind direction is $0^{\circ}$. The solar zenith angle for (a) and (b) is $23.4^{\circ}$ and

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Conclusions

Tables
Figures


Full Screen / Esc

Printer-friendly Version
Interactive Discussion


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version

Fig. 6. Same as in Fig. 5, but for the AOLP from the ADRTM. The solar zenith angle for (a) is $23.4^{\circ}$ and for (b) is $43.16^{\circ}$.



Fig. 7. The total reflectance, DOP, and AOLP at a wavelength of 670 nm at TOA, which is calculated with the ADRTM at a solar zenith angle of $43.16^{\circ}$ over a pristine clear sky ocean with a wind speed of $7.5 \mathrm{~ms}^{-1}$ and a wind direction of $0^{\circ}$. Solid curves denote the total reflectance and DOP with the mid-latitude summer gas absorption, respectively. Black dots denote the total reflectance and DOP with 4-times the mid-latitude summer gas absorption, respectively. Panel (e) shows the AOLP with mid-latitude summer gas absorption and (f) shows the AOLP with 4-times the mid-latitude summer gas absorption.

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion


ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Conclusions

Tables
Figures


4

Back
Introduction
References

14
$-1$
-
Close

Full Screen / Esc

Printer-friendly Version
Interactive Discussion


13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
(b) $7.5 \mathrm{~ms}^{-1}$, (c) $10.0 \mathrm{~ms}^{-1}$, and (d) $15.0 \mathrm{~ms}^{-1}$, respectively.


13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion


Fig. 11. Same as in Fig. 10, but for the AOLPs from the ocean wave slope probability distribution model with wind direction (a) $0^{\circ}$, (b) $90^{\circ}$, and (c) $180^{\circ}$, and for (d) the ocean wave slope probability distribution model without wind direction dependence.

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion


Fig. 12. The total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelength of 550 nm from the mid-latitude summer pristine atmosphere over the ocean without wave shadow (solid curve) and with wave shadow (dashed curve). The wind speed is $7.5 \mathrm{~m} \mathrm{~s}^{-1}$. The SZA is $33.30^{\circ}$.

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc


Printer-friendly Version
Interactive Discussion


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion

Fig. 13. Same as in Fig. 12, but for AOLPs from the mid-latitude summer pristine atmosphere over the ocean (a) without wave shadow and (b) with wave shadow.


ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Fig. 14. The total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelengths of 470 nm (dashed curve) and 865 nm (solid curve), respectively. Pristine atmosphere with the mid-latitude summer atmospheric profile is used. The solar zenith



## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion

Fig. 15. Same as in Fig. 14, but for AOLPs at the wavelengths of (a) 470 nm and (b) 865 nm .



Fig. 16. The agglomerated debris particle shapes of sea-salt aerosols.

## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

## Abstract

Conclusions
Introduction
References
Tables
Figures


Full Screen / Esc

## Printer-friendly Version




Fig. 17. A two-mode sea-salt aerosol size distribution from Porter and Clarke (1997) for ocean wind speed between 5.5 to $7.9 \mathrm{~m} \mathrm{~s}^{-1}$. The dotted curve denotes fine-mode size distribution; the dashed curve denotes coarse-mode size distribution. The combined size distribution is denoted by the solid curve.

ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page

## Abstract

Conclusions
References

Figures
Tables

14
$>1$
$\checkmark$
Back


Close
Full Screen / Esc

Printer-friendly Version
Interactive Discussion


ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Fig. 18. The total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelengths of 550 nm from the pristine mid-latitude summer oceanatmosphere system (solid curve) and those from the mid-latitude summer ocean-atmosphere system with sea-salt aerosols (dashed curve) of optical thickness 0.1 . The ocean wind speed



## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version

Fig. 19. Same as in Fig. 18, but for AOLPs of the ocean-atmosphere system (a) without aerosols and (b) with sea-salt aerosols, respectively.


ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Fig. 20. The total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelength of 550 nm from the mid-latitude summer ocean-atmosphere system with water clouds of optical thickness 5.0 (dashed curve) and 10.0 (solid curve), respectively.



## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion

Fig. 21. Same as in Fig. 20, but for AOLPs of the ocean-atmosphere system with water clouds of optical thickness (a) 5.0 and (b) 10.0, respectively.



ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc
Fig. 22. The ice cloud particle size distribution of HP (1984): $T=-20^{\circ}$ to $-25^{\circ}$ (Fu, 1996). Also shown is the assumed ice crystal aggregate particle shape.


ACPD
13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Fig. 23. The total reflectance and DOP on the principal plane, which is calculated with the ADRTM at the wavelength of 865 nm from the mid-latitude summer ocean-atmosphere system with an ice cloud layer of optical thickness 5.0 at 865 nm . The ice cloud layer is between 7 km and 8 km over the ocean with a wind speed of $7.5 \mathrm{~m} \mathrm{~s}^{-1}$. The SZA is $33.30^{\circ}$.


## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version
Interactive Discussion



## ACPD

13, 17585-17642, 2013

Modeling polarized radiation
W. Sun and C. Lukashin

Title Page


Full Screen / Esc

Printer-friendly Version

Fig. 25. Same as in Fig. 24, but for AOLPs of the ocean-atmosphere system (a) without ice cloud and (b) with an ice cloud of optical thickness 0.3 at 865 nm , respectively.


