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Deliquescence, efflorescence, and phase miscibility of mixed particles of ammonium sulfate and isoprene-derived secondary organic material

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Abstract

The hygroscopic phase transitions of ammonium sulfate mixed with isoprene-derived secondary organic material were investigated in aerosol experiments. The organic material was produced by isoprene photo-oxidation at 40% relative humidity. The low volatility fraction of the photo-oxidation products condensed onto ammonium sulfate particles. The particle-phase organic material had oxygen-to-carbon ratios of 0.67 to 0.74 for mass concentrations of 20 to $30 \,\mu g \,m^{-3}$. The deliquescence, efflorescence, and phase miscibility of the mixed particles were investigated using a dual arm tandem differential mobility analyzer. The isoprene photo-oxidation products induced deviations in behavior relative to pure ammonium sulfate. Compared to an efflorescence relative humidity (ERH) of 30 to 35% for pure ammonium sulfate, efflorescence was eliminated for mixed aqueous particles having organic volume fractions ε of approximately 0.6 and greater. Compared to a deliquescence relative humidity (DRH) of 80% for pure ammonium sulfate, the DRH steadily decreased for increasing ε , approaching a DRH of 40%

- for ε of 0.9. Parameterizations of the DRH(ε) and ERH(ε) curves were as follows: DRH(ε) = $\Sigma_i c_{i,d} x^i$ valid for $0 \le \varepsilon \le 0.86$ and ERH(ε) = $\Sigma_i c_{i,e} x^i$ valid for $0 \le \varepsilon \le 0.55$ for the coefficients $c_{0,d}$ = 80.67, $c_{0,e}$ = 28.35, $c_{1,d}$ = -11.45, $c_{1,e}$ = -13.66, $c_{2,d}$ = 0, $c_{2,e}$ = 0, $c_{3,d}$ = 57.99, $c_{3,e}$ = -83.80, $c_{4,d}$ = -106.80, and $c_{4,d}$ = 0. The molecular description that is thermodynamically implied by these strongly sloped DRH(ε) and
- ²⁰ ERH(ε) curves is that the organic isoprene photo-oxidation products, the inorganic ammonium sulfate, and water form a miscible liquid phase even at low relative humidity. This phase miscibility is in contrast to the liquid-liquid separation that occurs for some other types of secondary organic material. These differences in liquid-liquid separation are consistent with a prediction recently presented in the literature that the bifur-
- cation between liquid-liquid phase separation versus mixing depends on the oxygento-carbon ratio of the organic material. The conclusions are that the influence of secondary organic material on the hygroscopic properties of ammonium sulfate varies with organic composition and that the degree of oxygenation of the organic material, which



is a measurable characteristic of complex organic materials, is an important variable influencing the hygroscopic properties of mixed organic-inorganic particles.

1 Introduction

The water content of atmospheric particles can influence heterogeneous chemistry, cloud activation, and radiative forcing, among other phenomena (Seinfeld and Pandis, 5 2006). The deliguescence and efflorescence transitions that switch particles between crystalline and aqueous phases, altering the equilibrium particle water content in the process, have been widely studied, typically either for inorganic and organic components separately or for two- or three-component mixtures of them (Tang and Munkelwitz, 1993; Virkkula et al., 1999; Hameri et al., 2000; Martin, 2000; Parsons et al., 2006; 10 Varutbangkul et al., 2006). In the past few years, an additional transition of liquid-liquid phase separation between single and multiple liquid phases at a critical relative humidity has been a topic of increasing research interest (Pankow, 2003; Marcolli and Krieger, 2006; Ciobanu et al., 2009; Zuend et al., 2010; Bertram et al., 2011; Smith et al., 2011; Song et al., 2012). The separation relative humidity depends both on 15 the identity and the relative concentrations of the organic and inorganic components (Pankow, 2003; Zuend et al., 2010; Bertram et al., 2011). The different morphologies of phase-separated particles, such as coating-core or other structures (Reid et al.,

2011), compared to single-phase homogeneous particles can influence the availabil ity of water for heterogeneous chemistry and cloud activation (Ravishankara, 1997), affect particle optical properties (Martin, 2000), and alter the deliquescence and efflorescence phase transition relative humidities (Parsons et al., 2006; Chan and Chan, 2007; Smith et al., 2011).

Laboratory particles of sulfate mixed with secondary organic material represent an ²⁵ important surrogate for a common class of atmospheric particles (Buzorius et al., 2002; Murphy et al., 2006; Pratt and Prather, 2010). These mixed organic-inorganic particles are believed to be produced in the atmosphere by two principal mechanisms. In the



first, low-volatility molecules formed by the atmospheric oxidation of volatile organic compounds (VOCs) condense as secondary organic material (SOM) onto preexisting inorganic particles (Hallquist et al., 2009). In the second, mixed residual particles remain after the evaporation of cloud droplets that contained dissolved inorganic and

- organic components and in which active scavenging of gas-phase species and subsequent secondary organic chemistry took place during the cloud's lifetime (Ervens et al., 2011). The chemical nature of the inorganic and organic components determines the extent of their interactions and hence the governing organic-inorganic-water phase diagram, including both stable and metastable aspects.
- To date, the effects of secondary organic material on the phase transitions of the inorganic components of particles such as ammonium sulfate have been characterized in only a few studies. These studies show that SOM produced by α -pinene, limonene, and β -caryophyllene ozonolysis exerts a minor influence on the deliquescence relative humidity (DRH) and the efflorescence relative humidity (ERH) of the ammonium sul-
- fate component of the mixed particles (Saathoff et al., 2003; Takahama et al., 2007; Bertram et al., 2011; Smith et al., 2011). The implication is a biphasic morphology for the aqueous inorganic and organic components of the particles, at least for the range of water activities associated with ERH and DRH. In the case of α -pinene ozonolysis, Smith et al. (2011) showed that DRH and ERH were altered by less than 4 % RH
- from the values of pure ammonium sulfate for organic volume fractions of up to 0.96. Although these studies suggest the immiscibility of SOM with an aqueous inorganic phase and thus a minimal influence of SOM on DRH and ERH of the inorganic phase, the dark ozonolysis products of these precursors represent only a narrow range of possible SOM types. Among other factors, the chemistry and properties of SOM can
- ²⁵ change with oxidation conditions (e.g., low compared to high NO_x) and VOC precursor chemistries (e.g., short chain compared to long chain species). For instance, in contrast with the aforementioned ozonolysis studies, Meyer et al. (2009) provided evidence that SOM produced by α -pinene photo-oxidation in the presence of NO_x can decrease the DRH of ammonium sulfate by more than 5 %, though the additional decrease was



not quantified. Bertram et al. (2011) likewise presented an initial data set for the effects of SOM produced by isoprene photo-oxidation on the phase transitions of ammonium sulfate, showing a decrease in DRH for organic volume fractions from 0 to 0.8 and a decrease in ERH for organic volume fractions from 0 to 0.6. Compared to the other SOM types studied, this isoprene derived SOM appeared to have a markedly different

⁵ SOM types studied, this isoprene-derived SOM appeared to have a markedly different effect on the phase transitions of ammonium sulfate.

In the present study, a comprehensive data set for the effects of SOM produced by isoprene photo-oxidation on the phase transitions of ammonium sulfate is collected for a broad range of organic volume fractions from 0.0 up to 0.86. The data set is more comprehensive and the experimental protocols and analysis are improved compared

- ¹⁰ comprehensive and the experimental protocols and analysis are improved compared to our earlier treatment in Bertram et al. (2011). These improvements allow a better assessment of phase miscibility, a more accurate parameterization of DRH(ε) and ERH(ε), and a new account of partial dissolution of ammonium sulfate for RH < DRH (i.e., initial deliquescence) for these mixed particles. The influence of different con-15 ditions of SOM production, including in the presence of agueous compared to solid
- ¹⁵ ditions of SOM production, including in the presence of aqueous compared to sulfate particles at relative humidities of 40 and 60 %, is also explored.

2 Experimental

2.1 Particle generation

Particles of ammonium sulfate having isoprene-derived SOM coatings were produced
 using the Harvard Environmental Chamber (HEC) (Shilling et al., 2008; King et al., 2009). The chamber was operated as a continuously mixed flow reactor (CMFR), with balanced inflows and outflows and a mean reactor residence time of 3.3 h. Ammonium sulfate particles (Fluka TraceSELECT, >99.9999% purity), gaseous isoprene (200 ppb; Scott Specialty Gases, 50 ppm in nitrogen), and gaseous hydrogen peroxide
 (ca. 10 ppm) were continuously injected. The hydrogen peroxide was evaporated from a solution (Sigma-Aldrich, 30 wt% solution) in a warmed bulb. The sulfate particles,



produced by atomization from an aqueous solution, were equilibrated unless stated otherwise to less than 30% relative humidity (RH) by passing the aerosol through a diffusion dryer. Aqueous ammonium sulfate particles in pure form effloresce between 30% and 35% RH to form solidified particles (Martin, 2000). Prior to entering the

- ⁵ CMFR, the sulfate particles were classified using a differential mobility analyzer (DMA) that was set to pass an electric-field mobility diameter $d_{m,+1}^{seed}$ (i.e., +1 charge-equivalent) of 68 to 72 nm (Knutson and Whitby, 1975). The resolution of the DMA for the operating conditions corresponded to singly charged particle diameters as small as 61 ± 2 nm and as large as 83 ± 2 nm. Doubly charged sulfate particles, characterized by a mode
- diameter between 99 and 103 nm and a total diameter range of 90 ± 2 to 120 ± 2 nm, were also transmitted through the DMA and entered the CMFR. The +1 and +2 solid particles were present in the CMFR inflow in an approximate ratio of 5:1. The seed number-diameter distribution was measured using a TSI Scanning Mobility Particle Sizer (SMPS) (Fig. S1) (Wang and Flagan, 1990).
- ¹⁵ Within the CMFR, photolysis of H_2O_2 by ultraviolet light produced OH radicals that initiated photo-oxidation of the isoprene (Kroll et al., 2006). The OH concentration was estimated as approximately 2×10^6 cm⁻³ based on the steady-state concentration of isoprene in the outflow from the CMFR. Except when noted otherwise, experiments were conducted at 40 % RH. Low-volatility gas-phase products of the isoprene oxi-
- ²⁰ dation condensed onto the surfaces of the particles present in the CMFR, increasing particle diameter. The particles had a range of individual residence times because Poisson statistics governed particle loss in the CMFR, both to the walls as well as in the outflow (Kuwata and Martin, 2012). At steady state, the number-diameter distribution of the particles in the CMFR outflow was controlled by three main factors: (1)
- the number concentration and diameters of the +1 and +2 particles in the CMFR inflow, (2) the rate of condensable product generation by isoprene photo-oxidation, and (3) the particle mean residence time in the CMFR. For the conditions of the experiments, the mode of the particle population in the CMFR outflow was between 151 and 172 nm, and the lower and upper quartile diameters were between 95 and 103 and



242 to 257 nm, respectively, as measured by the SMPS at 25 % RH (Fig. S1). The total number concentration in the CMFR outflow was typically $7 \pm 1 \times 10^3$ cm⁻³.

For a single seed diameter (i.e., either +1 or +2 seed particles), larger particles in the CMFR outflow corresponded to longer residence times and higher organic vol-

- ume fractions. The particle population in the CMFR outflow thus consisted of two sub-5 populations, meaning that for any outflow diameter equal to or greater than 90 nm (i.e., the lower limit of +2 seed particles) there was one sub-population of organic volume fractions associated with the +1 seed particles and another sub-population associated with the +2 seed particles.
- The steady-state organic particle mass concentration, which is a measure of the rate 10 of condensable product generation, ranged from 20 to $30 \,\mu g \,m^{-3}$. The concentration was measured using an Aerodyne Aerosol Mass Spectrometer (AMS) (DeCarlo et al., 2006; Aiken et al., 2007; Chen et al., 2011). The AMS also provided information on the oxygen-to-carbon elemental ratio of the particle-phase organic material, which varied from 0.67 to 0.74 for the experiments described herein. 15

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2.2 Particle hygroscopic analysis

The hygroscopic properties of the particle population in the CMFR outflow were analyzed using a dual-arm hygroscopic tandem differential mobility analyzer (TDMA) (Martin et al., 2008; Rosenoern et al., 2009; Smith et al., 2011). Figure 1 shows schematically the flow path of the aerosol from the generation system through the TDMA components, along with the typical RH of each component, to be discussed below. Two different types of experiments, described as transmission ratio and number-diameter distribution measurements, were carried out.

2.2.1 Transmission ratio experiments

The transmission ratio experiments directly measured the fraction of the particles in 25 the test population that underwent irreversible diameter changes as a result of RH



cycling, such as those associated with deliquescence and efflorescence phase transitions (Rosenoern et al., 2009; Smith et al., 2011). For this measurement, the incoming flow of the TDMA was conditioned to RH^{mono} by use of a Nafion tube (Perma Pure, PD50T-12SS). A first differential mobility analyzer (DMA^{mono}; TSI, 3081; 9.6:1 sheath:sample flow ratio; 25 °C) selected a fraction of the particle population having an electric-field mobility diameter $d_{m,+1}^{mono}$. The sheath flow RH was adjusted to RH^{mono} prior to entering the DMA. Following DMA^{mono}, the flow was split and directed into dual arms, labeled α and β . Each of these arms consisted of the following components in series:

a Nafion tube (Perma Pure, MD 110-96SS) set to a value $RH_{1,\alpha/\beta}$, a Nafion tube set to RH^{mono} , a differential mobility analyzer $DMA_{\alpha/\beta}^{filter}$ (TSI, 3081; ca. 9.6:1 sheath:sample flow ratio; 25 °C) set to pass the same electric-field mobility diameter as $d_{m,+1}^{mono}$ and maintained at RH^{mono} , and a condensation particle counter (CPC; TSI, 3010) to measure the number concentration $N_{\alpha/\beta}^{filter}$ of particles passing $DMA_{\alpha/\beta}^{filter}$. The experiment

consisted of measuring the transmission ratio ϕ (calculated as $\phi = N_{\beta}^{\text{filter}} / N_{\alpha}^{\text{filter}}$) while

¹⁵ holding RH^{nafion}_{1, α} fixed to the same value as RH^{mono} and scanning RH^{nafion}_{1, β}. The purpose of the α -arm was to provide a control for fluctuations in the number concentration of $d_{m,+1}^{mono}$ in the CMFR outflow by counting how many particles passed through the instrument in the absence of RH perturbations.

For experiments designed to identify deliquescence transitions (Fig. 1, row 1; ²⁰ Fig. 2a), RH^{nafion}_{1, β} was scanned upward from 60% to 90% during the course of an experiment while RH^{mono} was maintained at 60%. In this way, the particles in the β arm underwent an RH history described by the following:

$$60\% \to d_{m,+1}^{\text{mono}} \to 60\% + \delta \to 60\%$$
⁽¹⁾

for $0 < \delta < 30$ %. For experiments designed to identify efflorescence transitions (Fig. 1, row 2; Fig. 2c), the particle population in the CMFR outflow was deliquesced at 90 % RH prior to entering the TDMA instrument. The transmission ratio was recorded for a



downward scan of $\text{RH}_{1,\beta}^{\text{nafion}}$ from 50% to 15% while RH^{mono} was maintained at 50%. The RH history of the particles was thus as follows:

 $90\% \rightarrow 50\% \rightarrow d_{m,+1}^{mono} \rightarrow 50\% - \delta \rightarrow 50\%$

for $0 < \delta < 35$ %. The lower limit of 15 % emerged as a practical matter based on the time constant for Nafion material to equilibrate and transfer local relative humidity, which was longer at progressively lower RH, compared to the time constant desired for an experimental scan of approximately 1 % RH min⁻¹. A series of these deliquescence and efflorescence experiments was carried out in which stepwise changes were made to $d_{m,+1}^{mono}$ between experiments. In this way, a range of organic volume fractions was probed. The RH histories of Eqs. (1) and (2) are summarized in Table S1.

For the conducted experiments, the transmission ratio ϕ responded to the fraction of particles in the population for which an irreversible change in diameter occurred when exposed to the cycle of RH^{mono} \rightarrow RH^{nafion} \rightarrow RH^{mono} (Rosenoern et al., 2009; Smith et al., 2011). A direct interpretation of ϕ as the actual fraction of particles for which the diameters changed irreversibly (i.e., a linear response factor) was possible provided that the shift from one branch to the other of the hysteresis curve changed the particle diameter sufficiently to ensure negligible particle transmission through the DMA^{mono} – DMA^{filter} sequence. For the employed operating conditions, the minimum growth factor *g* required for full separation was 1.12 (cf. Eq. 2 of Rosenoern et al. (2009) and Figs. 5 and 6 of Smith et al., 2011).

A goal of our experiments was to probe a maximum range of organic volume fractions ε while ensuring g > 1.12. For this purpose there existed an optimal value of RH^{mono}. A requirement of the deliquescence mode experiments was that the particles must not yet be fully deliquesced at RH^{mono}. In this regard, a low value of RH^{mono} avoided full deliquescence to some high value of ε . A high value of RH^{mono}, however, favored compliance with the condition g > 1.12. The optimal value of RH^{mono} was the value that just satisfied g = 1.12 while maximizing ε (cf. Fig. S2). A priori to our collected data set, the optimal value of RH^{mono} could not be known, but the results of initial survey



(2)

experiments conducted by us suggested a good value for RH^{mono} would be 60% for the deliquescence mode experiments, and this value was used in collecting the detailed data set. Similarly, for the efflorescence mode experiments, initial survey experiments established that RH^{mono} of 50% was a good value, and this value was used to collect the detailed data sets. A posteriori to the collection of the data set, the optimal value could be established as 69.5% for both the deliquescence and efflorescence mode experiments, corresponding to a maximum range of $0 < \varepsilon < 0.66$ that could possibly be measured in a transmission ratio experiment (cf. Fig. S2).

2.2.2 Number-diameter distribution experiments

As described in the previous section, the transmission ratio experiments were restricted by the experimental protocols to particles that fully deliquesced above 60 % RH in the deliquescence mode experiments and particles that had efflorescence points greater than 15 % RH in the efflorescence mode experiments. The number-diameter distribution experiments, as described below, pushed these limits to as low as 48 % RH for deliquescence measurements and as low as 7 % RH for efflorescence measurements. The experimental design and data analysis, however, were more complicated.

A number-diameter distribution N(d) was collected in a single arm for some fixed value of $d_{m,+1}^{mono}$ and a constant RH^{mono} value of 7%, meaning particles classified by DMA^{mono} had minimal water content (Fig. 1, rows 3 and 4). To acquire N(d), we recorded the number concentration N^{filter} as $d_{m,+1}^{\text{filter}}$ was scanned. During a single scan of $d_{m,+1}^{\text{filter}}$, the values RH₁^{nafion} and RH₂^{nafion} of the two Nafion tubes remained constant. Between scans, these RH values were changed, and a data set N(d,RH) was thereby obtained for one $d_{m,+1}^{\text{mono}}$. The RH histories that were employed for RH₁^{nafion} and RH₂^{nafion} are presented in Sect. 3.2 because of their close coupling to the data interpretation. The value of $d_{m,+1}^{\text{mono}}$, fixed during the acquisition of a single data set N(d,RH), was adjusted between experiments to a small number of selected values (cf. Table S1)



ranging from 75 to 190 nm so that data sets of N(d, RH) for different regions of organic

volume fraction were obtained. The data sets N(d,RH) are reported as recorded without any corrections for the presence of multiply charged particles (Wang and Flagan, 1990). Instead, a forward-model was used that includes a treatment of the particle sub-populations in the outflow from the CMFR (cf. Sect. 3.1).

- In comparison to the transmission ratio experiments, the number-diameter distribution measurements could probe efflorescence to lower RH. In these experiments, RH^{mono} was set to a static value of 7 % RH, which could be achieved after sufficient equilibration time of the Nafion material. Furthermore, measurements of deliquescence were also extended to lower RH values by detailed interpretation of the data that con-
- ¹⁰ sidered the several particle types present in the population and the resulting contributions to N(d) (cf. Sect. 3.2) in the number-diameter distribution experiments. Compared to the theoretical lower limit of 40 % RH that is implied by the experimental RH inside the CMFR, there was a practical restriction to 48 % RH in these deliquescence experiments because of a coupling of factors, including the accuracy of sizing resolution by the instrumentation and the decreases in diameter by the restriction for increasing c
- the instrumentation and the decrease in diameter hysteresis for increasing ε .

2.2.3 Other number-diameter distribution experiments

To extend the range of efflorescence measurements to 7 % < RH < 15 %, we collected a few number-diameter distributions following the protocol of the transmission ratio efflorescence experiments. Aqueous particles of $d_{m,+1}^{\text{mono}}$ were selected at 50 % RH, and the RH cycling in the TDMA was identical to that defined by Eq. (2). The measured quantity, however, was N(d,50 %) instead of ϕ . The range $7 \% < \text{RH}_{1,\beta}^{\text{nafion}} < 15 \%$ was obtained by using 3 h equilibration times for each step of the Nafion conditioner. This protocol was also used in several control experiments to probe ERH between 15 % and 50 % to test for and ultimately rule out any possible bias introduced by scan time or alternate approaches to data analysis.



3 Results and discussion

3.1 Particle population and sub-populations

The particle population in the outflow of the CMFR is statistically described by first and third quartile diameters of approximately 100 and 250 nm, respectively, at 25 %

RH. Individual particles are composed of sulfate and organic components. The sulfate component represents a mass-equivalent diameter of either 61–83 nm or 90–120 nm, corresponding to initial seed particles of +1 or +2 charge. The water content at 25 % RH is small by volume compared to the sulfate and organic components: the mixed particles on the lower branch of the hysteresis curve had a hygroscopic diameter growth factor of less than 1.02 at 25 % RH.

The particle population exiting the CMFR is re-charged by a radiation source as it enters the TDMA (Fig. 1). Correspondingly, by number concentration there are four significant particle types that enter DMA^{mono}. In descending importance, these subpopulations include: (A) singly charged particles having 61–83 nm sulfate seeds, (B) doubly charged particles having 61–83 nm seeds, (C) singly charged particles having 90–120 nm seeds, and (D) doubly charged particles having a 90–120 nm seeds. The relative concentration of each particle type at the setpoint value $d_{m,+1}^{mono}$ determines the composition of the particle population that exits DMA^{mono}. Particles of type C have non-zero concentrations after DMA^{mono} only for $d_{m+1}^{mono} > 90$ nm.

- The sub-population probability density functions $p(\varepsilon;T)$ of organic volume fraction ε for the four particle types T (i.e., A, B, C, and D) in the outflow of DMA^{mono} are obtained by use of a model. Model inputs include the measured number-diameter distributions of the seed particles in the CMFR inflow and of the particle population in the CMFR outflow. Further information about the model is presented in the Appendix. Examples
- of the cumulative distribution function $P(\varepsilon)$ of the entire particle population are plotted in panels b and d of Fig. 2. Examples of the probability density functions $p(\varepsilon;T)$ of the



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four different sub-populations are represented by the colored lines in panels b and d of Fig. 3.

3.2 Deliquescence and efflorescence

3.2.1 Transmission ratios

- Solid ammonium sulfate particles in pure form deliquesce at 80 % RH to form purely liquid particles (Martin, 2000). When mixed with other components, ammonium sulfate and those components can form a mixed aqueous phase at a relative humidity less than 80 %, often called the initial deliquescence RH or eutonic RH. The mixed phase persists in equilibrium with pure ammonium sulfate (alternatively, in equilibrium with the other components depending on the relative initial mass of each) across a finite RH range prior to full dissolution into a mixed phase, often referred to as final deliquescence. Particles in the RH range of partial dissolution lie on the lower side of the hysteresis
- curve because the residual pure phase solid material typically grows and dissolves without an activation barrier, leading to reversible changes in particle diameter with 5 RH cycling. By comparison, full dissolution at final deliguescence shifts a particle from
- ¹⁵ RH cycling. By comparison, full dissolution at final deliquescence shifts a particle from the lower to the upper side of the hysteresis curve. Irreversible changes in particle diameter are associated with RH cycles that pass through full dissolution. The organic volume fraction at which final deliquescence occurs for a fixed RH value is denoted by $\varepsilon_{\rm D}(\rm RH)$. The Gibbs-Duhem thermodynamic relationship describes the curve $\varepsilon_{\rm D}(\rm RH)$
- for decreasing RH (Berry et al., 2000). The particles in the CMFR outflow having $\varepsilon < \varepsilon_{\rm D}(40\%)$ are on the lower side of the hysteresis branch because the seed particles in the CMFR inflow are injected as solid sulfate particles at 40% RH. This sub-population having $\varepsilon < \varepsilon_{\rm D}(40\%)$ can be probed for deliquescence transitions by cycling RH.

An example of a data set of transmission ratios used to identify deliquescence transitions is plotted in Fig. 2a. The data of Fig. 2a, plotted for $d_{m,+1}^{mono} = 90$ nm, show that 80 % of the particles in this population deliquesce and that their DRH values range from 73 % and 79 % RH. Particles deliquescing at the highest RH values, corresponding to

the green point of Fig. 2a, have the lowest organic volume fraction, corresponding to the green point of Fig. 2b. The pink point in Fig. 2a and b shows that particles of $\varepsilon = 0.6$ have a deliquescence point of 73 % RH. This result is written in shorthand as $\varepsilon_D(73\%) = 0.6$. The conclusion from Fig. 2a and b is that DRH drops from 80 % for pure ammonium sulfate to 73 % for ε of 0.6. The set of points $\varepsilon_D(RH)$ for 73 % < RH < 80 % of Fig. 2a and b represent a curve of $\varepsilon_D(RH)$ across the domain $0 < \varepsilon_D < 0.6$. Exchanging dependent and independent variables, the line DRH(ε) appears in Fig. 4. Examples of other data sets are shown in Fig. S3.

The pink point of Fig. 2a and b represents the beginning of a gap in the continuity of ε , separating particles of types A and D from those of type B. As a result, there are very few particles in the range $0.6 < \varepsilon < 0.7$. Fig. 2a and b show that the particles in the range of $\varepsilon = 0.7$ to 0.85 do not show an irreversible change in diameter upon RH cycling. The implication, given that the RH cycle is of $60 \% \rightarrow d_{m,+1}^{mono} \rightarrow 60 \% + \delta \rightarrow$ 60 % for $0 < \delta < 30 \%$, is that the mixed particles of ammonium sulfate and isoprene-¹⁵ derived SOM fully deliquesce at 60 % RH for some value of ε that lies between 0.6 and 0.85, meaning $0.6 < \varepsilon_{D}(60 \%) < 0.85$.

An example of a data set of transmission ratios used to identify efflorescence transitions is plotted in Fig. 2c. The cumulative distribution function $P(\varepsilon)$ of organic volume fraction for the particle population is plotted in Fig. 2d. In this population, all particles

- ²⁰ begin as aqueous because of exposure to 90 % RH prior to entering the TDMA. The data of Fig. 2c show that 82 % of the particles effloresce between 15 % and 30 % RH and that no particles effloresce above 30 % RH. The particles efflorescing at the highest RH values, corresponding to the pink point of Fig. 2c, have the lowest organic volume fractions, corresponding to the pink point of Fig. 2d. The green point in Fig. 2c and d
- ²⁵ shows that particles of ε = 0.43 effloresce at 15% RH. This result is written in shorthand as $\varepsilon_{\rm E}(15\%)$ = 0.43 and means that for an efflorescence relative humidity of 15% the organic volume fraction is 0.43. As for Fig. 2a and b, this analysis is extended to obtain a curve $\varepsilon_{\rm E}(\rm RH)$, and this curve is represented in Fig. 4.



Figure 2d shows that there are very few particles in the population having $0.43 < \varepsilon < 0.8$. For $\varepsilon > 0.8$, particles do not show an irreversible change in diameter upon RH cycling (Fig. 2c). Given that the RH cycle is $90\% \rightarrow 50\% \rightarrow d_{m,+1}^{mono} \rightarrow 50\% - \delta \rightarrow 50\%$ for $0 < \delta < 35\%$, possible explanations are (a) that these mixed particles of ammonium sulfate and isoprene-derived SOM are already fully effloresced at 50% RH, (b) that ERH is below 15% for particles of $\varepsilon > 0.8$, or (c) that the solubility of the ammonium sulfate within the organic material exceeds $(1 - \varepsilon)$ even below 15% RH. In other words, ammonium sulfate is not supersaturated even below 15% RH for aqueous solutions of $\varepsilon > 0.8$. Case *a* seems untenable because the ERH of the mixed material should not, under most circumstances, be greater than that of the pure material (30–35%), though cooperative nucleation cannot be ruled out beyond possibility. The more expected phenomenon is a mix of cases *b* and *c*, with case *b* holding true for $\varepsilon \rightarrow 0.8$ and case *c* for $\varepsilon \rightarrow 1$. Extrapolation of the DRH line of Fig. 4 to <15% RH suggests a crossover between cases *b* and *c* at an organic volume fraction close to 1.0.

15 3.2.2 Number-diameter distributions

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The number-diameter distribution measurements were used to probe the deliquescence transitions of the particle population for DRH < 60%, thereby extending the transmission ratio measurements. Data were also collected for DRH > 60% to test for confirmation of the results obtained by the transmission ratio measurements.

Figure 3a shows an example of N(d) at 52 % RH, meaning $\delta = 45$ %, $x_a = 52$ % (gray squares), $x_b = 90$ % (black squares), and y = 52 % in the following protocols:

$$40\% \to 7\% \to d_{m,+1}^{\text{mono}} \to x_a : 7\% + \delta \to y : 7\% + \delta \to N(d,y) \text{ (gray squares)}$$
(3a)

$$40\% \to 7\% \to d_{m+1}^{\text{mono}} \to x_b : 90\% \to y : 7\% + \delta \to N(d, y) \text{ (black squares)}$$
(3b)

for which $x_{a/b}$ represents RH^{nafion} and *y* represents RH^{nafion}. The size distribution represented by the gray squares (Eq. 3a) corresponds to a population in which the 9917



ammonium sulfate components of some fraction of the particles are fully deliguesced (i.e., those particles of $\varepsilon > \varepsilon_{\rm D}(52\%)$). The size distribution represented by the black squares (Eq. 3b) corresponds to a population in which the ammonium sulfate components of all particles are fully deliquesced because of exposure to 90% RH and the absence of efflorescence at 52 % RH. A series of experiments of the type represented by Fig. 3a was carried out by scanning δ from 33 % to 73 %, corresponding to 40 % < *y* < 80 %.

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For a single value of y, $\varepsilon_{D}(y)$ can be determined by scanning ε and observing $N_{3b}(d,y;\varepsilon)$ compared to $N_{3a}(d,y;\varepsilon)$. This statement is explained by the following line of reasoning. The RH histories of Eqs. (3a) and (3b) begin at 40%. Depending on the 10 overall composition ε of a particle, the ammonium sulfate component at 40 % RH in the CMFR outflow is, by definition, either partially solid for $\varepsilon < \varepsilon_{D}(40\%)$ or completely dissolved for $\varepsilon \geq \varepsilon_{D}(40\%)$. For a particle population characterized by a single organic volume fraction ε , a comparison of $N(d,y;\varepsilon)$ of Eq. (3a) to that of $N(d,y;\varepsilon)$ of Eq. (3b) has sixteen possible outcomes to consider based on whether the following conditions 15 are true or false: DRH(ε) > 40 %, ERH(ε) > 7 %, DRH(ε) > y, and ERH(ε) > y. Evaluation of these 16 cases, however, shows that there is redundancy among the cases, and a condensed statement can be written as follows (cf. Tables S2 and S3):

shifted right, for $(\varepsilon < \varepsilon_D (40\%) \text{ and } DRH(\varepsilon) \ge y)$ $N_{3b}(d, y; \varepsilon)$ compared to $N_{3a}(d, y; \varepsilon)$ is dentical, for $(\varepsilon < \varepsilon_D (40\%)$ and DRH $(\varepsilon) < y$) (4) identical, for $\varepsilon \geq \varepsilon_{\rm D}$ (40%)

Therefore, in the case that ε can be scanned at constant y from a low to a high 20 value (i.e., $0 < \varepsilon < \varepsilon_{D}(40\%)$), $\varepsilon_{D}(\gamma)$ and hence DRH(ε) are obtained by noting at what value of ε an abrupt change occurs in $N_{3a}(d,y;\varepsilon)$ such that $N_{3b}(d,y;\varepsilon)$ compared to $N_{3a}(d,y;\varepsilon)$ is changed from right-shifted to identical overlap.

The particle population of Fig. 3a is characterized by a broad distribution $p(\varepsilon;T)$ (i.e., Fig. 3b) and thus inherently represents a scan of low to high ε , including to values of 25 ε greater than $\varepsilon_{\rm D}(40\%)$. The black squares compared to the gray squares of Fig. 3a represent the comparison of $N_{3b}(d,y)$ to $N_{3a}(d,y)$. The dependency of relative shifts



between $N_{3a}(d,y;\varepsilon)$ and $N_{3b}(d,y;\varepsilon)$ on ε underlies any comparison between the two data sets of Fig. 3a. Even so, these shifts are not immediately discernible by the unaided eye because their effects are convoluted with the dispersity of $p(\varepsilon;T)$.

A forward hygroscopic model that incorporates $p(\varepsilon;T)$ of the four particle types is used to aid in the interpretation of data sets represented in Fig. 3a. The initial number-diameter distributions used as inputs represent particle types A through D (cf. Sect. 3.1). These initial distributions for each particle type are evolved in the model according to the RH exposures given either by Eq. (3a) or (3b), including phase transitions (cf. Fig. S4). The analysis optimizes the parameter $\varepsilon_D(y)$ to minimize the difference between model prediction and observed data. The optimized model predictions (dashed red line in Fig. 3a) compare well to the data (gray squares). The dashed red line is the sum result for the four particle types, and the individual results for the different particle types are shown by the four solid color lines. The result for $\varepsilon_D(52\%)$ is plotted as a data point of DRH(0.82) = 52 % in Fig. 4. The results of similar experiments carried out

at other values of y are represented as the data points of Fig. 4.

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The number-diameter distribution measurements were also used to extend the efflorescence measurements to lower RH values than probed by the transmission ratio measurements (i.e., to ERH values below 15%). Two different protocols were used (cf. Sects. 2.2.2 and 2.2.3). For the first protocol, the settings $x_{a/b}$:RH^{nafion} and y:RH^{nafion} were as follows:

$$40\% \to 90\% \to 7\% \to d_{m,+1}^{\text{mono}} \to x_a : 50\% \to y : 50\% \to N(d,y) \text{ (gray squares)}$$
(5a)

$$40\% \to 90\% \to 7\% \to d_{m,+1}^{\text{mono}} \to x_b : 90\% \to y : 50\% \to N(d,y) \text{ (black squares)} \quad (5b)$$

The RH histories of Eqs. (5a) and (5b) force full deliquescence of all ammonium sulfate components at 90 % RH. At 7 % RH in the next step of the RH sequence, the ammonium sulfate component at least partially crystallizes for particles of $\varepsilon \le \varepsilon_{\rm E}(7\%)$ but does not crystallize at all for particles of $\varepsilon > \varepsilon_{\rm E}(7\%)$. Discussion Paper ACPD 12, 9903–9943, 2012 Deliquescence, efflorescence, and phase miscibility **Discussion Paper** M. L. Smith et al. **Title Page** Introduction Abstract Conclusions References **Discussion** Paper **Tables Figures** Back **Discussion** Paper Full Screen / Esc **Printer-friendly Version** Interactive Discussion

Figure 3c shows an example of the number-diameter distributions obtained for the protocols of Eqs. (5a) and (5b). The black squares represent a population in which the ammonium sulfate components of all particles are fully deliquesced, and the gray squares represent a population that can have two categories of particles. These cate-

- ⁵ gories include: (1) particles of the high organic volume fraction that do not effloresce at 7 % RH and (2) those of low to intermediate ε that do effloresce at 7 % RH and are not fully deliquesced by 50 % RH. The DRH and ERH lines of Fig. 4 imply that an additional possible category of particles, those of intermediate ε that effloresce at 7 % RH but fully deliquesce by 50 % RH, does not exist for the tested particle populations. The rightward shift apparent in Fig. 3c for the black squares compared to the gray squares
- ¹⁰ rightward shift apparent in Fig. 3c for the black squares compared to the gray squares arises from the sub-population representing the second category. Particles of the first category have identical diameters for Eqs. (5a) and (5b).

For the hypothetical experiment of a particle population of monodisperse ε , for a series of measurements that scans from high to low ε , a comparison of $N_{3a}(d,y;\varepsilon)$ to

¹⁵ $N_{3b}(d,y;\varepsilon)$ shows identical distributions until $\varepsilon_{\rm E}(7\%)$. In the real experiment, the particle population represented in Fig. 3d is characterized by a broad distribution $p(\varepsilon;T)$ and thus inherently represents a scan from high to low ε . The forward hygroscopic model is employed to match the model output (dashed red line) to the data (gray squares) by optimization of the parameter $\varepsilon_{\rm E}(7\%)$. Figure 3a shows that the model distribu-²⁰ tion compares well to the data. The result for $\varepsilon_{\rm E}(7\%)$ is plotted as a data point of ERH(0.55) = 7\% in Fig. 4. The clustering of three data points at 7% RH represents three data sets that were independently collected and analyzed.

The second protocol used number-diameter distribution measurements to probe efforescence transitions for greater than 7% RH. This protocol followed the RH history of Eq. (2), i.e., $90\% \rightarrow 50\% \rightarrow d_{m,+1}^{mono} \rightarrow y$: $50\% - \delta \rightarrow 50\%$ (Fig. 1, β arm of row 2). In comparison to the transmission mode measurements, somewhat higher values of δ were achieved (41% compared to 35%) for number-diameter distribution measurements by allowing much longer equilibration times for the Nafion tube set to RH₁^{nafion}. From the collected data sets, values $\varepsilon_{F}(y)$ were again obtained by



optimization between the hygroscopic model and the measured data. The results of this protocol appear in Figs. 4 and 5 as the points for ERH > 7 %.

Figure 4 consolidates the data from the transmission ratio experiments as lines and from the number-diameter distribution experiments as points. The two sets of data and analysis methods show a consistent picture of the deliquescence and efflorescence phase transitions of ammonium sulfate mixed with isoprene-derived secondary organic material. Table 1 presents parameterization equations of the DRH(ε) and ERH(ε) data sets, and these equations are shown as the dashed lines in Fig. 4.

The experiments described thus far were all carried out at 40 % RH in the CMFR with solid ammonium sulfate seed particles. The full matrix of experiments, however, consisted of measurements at 40 % and 60 % RH and solid and aqueous seed particles, resulting in a total of four conditions. The gas-phase mechanism can be altered by changes in relative humidity (Jonsson et al., 2006). Heterogeneous particle-phase chemistry can be altered by particle-phase liquid water content (Jang et al., 2002;

- ¹⁵ Volkamer et al., 2009; Sareen et al., 2010). There can also be increased partitioning of gas phase products to the particle phase (Pankow and Chang, 2008; Barley et al., 2009; Romakkaniemi et al., 2011). Singly or combined, these differences can influence the composition and hence hygroscopic properties of secondary organic material. The results of the conducted experiments, however, show no detectable differences in the phase being of the conducted experiments.
- ²⁰ phase transitions of the ammonium sulfate for the investigated matrix of four experimental conditions (Fig. 5a). The explanation, with respect to the indifference of the phase transitions, may be tied to the consistent oxygen-to-carbon elemental ratio of the SOM that characterized these four experimental conditions (i.e., 0.67 to 0.74).

3.3 Comparison to other studies

The results of this study can be compared to other observations of the hygroscopic phase transitions of particles composed of ammonium sulfate and secondary organic material, particularly in relation to the miscibility of the aqueous phases at intermediate relative humidity (RH < DRH) and the effects thereof on the deliquescence and</p>



efflorescence phase transitions of ammonium sulfate. In contrast to the strong dependence of DRH and ERH on ε that is apparent in Fig. 4 for isoprene-derived SOM, both the DRH and ERH of ammonium sulfate were reduced by no more than 4 % RH when mixed with SOM produced by α -pinene dark ozonolysis products for 0.0 < ε < 0.96

- ⁵ (Takahama et al., 2007; Smith et al., 2011) (Fig. 5b). Similarly, β -caryophyllene ozonolysis SOM caused at most a 2% RH reduction in DRH and ERH for ε up to 0.96 (Bertram et al., 2011), and limonene ozonolysis SOM caused no statistically different change in the ERH of ammonium sulfate for ε up to 0.94 (Takahama et al., 2007). In these cases, the explanation for the absence of strong effects, as suggested by Smith
- et al. (2011), is that separation occurs between the organic-water and inorganic-water phases below some critical relative humidity (>80 % RH). The phase transitions of ammonium sulfate then proceed approximately as they would for the pure compound. By comparison, the implication of the results shown in Fig. 4 is that the SOM produced by photo-oxidation of isoprene is phase miscible with aqueous ammonium sulfate, even to low water activity.

The difference of phase miscibility in the case of SOM produced by the photooxidation of isoprene compared to phase separation for the ozonolyzed terpenes should be related to the different compositions of the SOMs and their relative interactions with water and dissolved ammonium sulfate. Although relating SOM physical ²⁰ properties to specific molecules is impractical given the multi-molecular composition, some generalizations may be possible by relating to bulk properties of the SOM. For example, the isoprene SOM presented herein had oxygen-to-carbon (O:C) ratios rang-

ing from 0.67–0.74 whereas the α -pinene and β -caryophyllene SOM had lower O:C ratios of 0.39–0.44 (Smith et al., 2011) and 0.35 (Bertram et al., 2011), respectively.

According to the classification system presented in Bertram et al. (2011), the observed phase miscibility and phase separation of ammonium sulfate with these different SOM types are consistent with the differing O:C ratios. The underlying physical phenomenon is the expectation that water-solubility increases for greater O:C ratios, all other factors being equal.



Bertram et al. (2011) present an equation to predict DRH and ERH based on the organic-to-sulfate mass ratio of the particle components and the O:C ratio of the organic material. The comparison of DRH and ERH observations of this study to the values predicted by the equation of Bertram et al. (2011) is shown in Fig. 5c. The predictions are shown as shaded regions that correspond to a measurement uncertainty

- ⁵ dictions are shown as shaded regions that correspond to a measurement uncertainty of ± 30 % for the O:C ratio measured by the AMS (Aiken et al., 2007). The predictive equation is highly nonlinear in its dependence on O:C, meaning that the sensitivity of the prediction to the negative side of the uncertainty is very small and that the shaded region in Fig. 5c represents nearly entirely the positive side of the uncertainty. Figure 5c
- shows that the DRH observations and predictions are in good agreement across the range of organic volume fractions for which the prediction is valid. Within the uncertainty of the O:C measurement, the ERH observations are also in good agreement with the predictions. The ERH data lie along the lower edge of the shaded region, corresponding to the +30 % uncertainty in O:C.

15 4 Conclusions and implications

The results of this study show that secondary organic material produced by isoprene photo-oxidation strongly influences the hygroscopic phase transitions of ammonium sulfate. The SOM was produced at 40 % and 60 % relative humidity, at mass loadings from 20 and 30 μ g m⁻³, with O:C ratios from 0.67 and 0.74, and with aqueous and solid sulfate seed particles. The results are presented in Fig. 4 within the framework of a phase diagram (Berry et al., 2000). The liquidus line is given by DRH(ε). This line divides the phase space into a miscible liquid region to the right of the DRH(ε) curve and a liquid-solid region to the left of the curve in which a liquid and a solid co-exist (i.e., phase separated). The solidus representing pure ammonium sulfate is a vertical line at $\varepsilon = 0$.

Compared to a deliquescence relative humidity of 80 % and an efflorescence relative humidity of 30–35 % for pure ammonium sulfate, efflorescence was eliminated for



mixed aqueous particles of high organic volume fractions of approximately 0.6, and the deliquescence relative humidity decreased to 40% for volume fractions approaching 0.9. These strong effects caused by isoprene-derived SOM stand in contrast to the minimal influence on ammonium sulfate phase transitions that have been reported for

- SOM produced by terpene ozonolysis. These different behaviors are rooted in the differing tendencies of the studied SOMs to either mix with or separate from an aqueous inorganic phase. A uniphasic morphology, as in the case of isoprene-derived SOM with aqueous sulfate, lowers both the DRH and ERH of the mixed particles for increasing organic volume fraction. The decrease in DRH is driven thermodynamically (i.e., the
- Gibbs-Duhem relation) whereas the decrease in ERH is driven both thermodynamically and kinetically (i.e., homogeneous nucleation theory). Comparison of this study's findings to the results reported in the literature for other types of SOM underscores that secondary organic material composition, which varies with VOC precursor and oxidation conditions, is an important factor governing phase separation and the efflorescence and deliguescence of mixed particles.

These results have several different important implications with respect to atmospheric processes. The hydrolysis of N₂O₅ on and in aerosol particles affects the rates of atmospheric ozone production. The availability of water is a key factor influencing the rate of this reaction (Chang et al., 2011). Anttila et al. (2006) observed that the up take probability of N₂O₅ on aqueous ammonium bisulfate particles coated by *α*-pinene ozonolysis products is inversely related to the thickness of the organic coating. The suggestion was that N₂O₅ must first dissolve into and then diffuse through the organic layer to reach the aqueous inorganic core and hydrolyze. By comparison, the present study's results show that aqueous ammonium sulfate and isoprene-derived SOM form

²⁵ a mixed phase, ruling out a thick organic coating. Water is expected to be readily available at the surface of the particle and to promote N_2O_5 hydrolysis, though this expectation remains to be tested in laboratory conditions. Furthermore, as a result of the decreased DRH and ERH of ammonium sulfate that is caused by the isoprenederived SOM, the relative humidity conditions for which the particles participate in



aqueous-phase reactions such as N_2O_5 hydrolysis are significantly extended compared to mixed particles composed of terpene-derived SOM. These differences with SOM type suggest that there are large differences in N_2O_5 and NO_3 concentrations in urban environments depending on the properties of the local atmospheric SOM (Riemer et al., 2009).

Another important atmospheric process that influences both the atmospheric oxidant cycle as well as the mass concentration of atmospheric particles is the partitioning of organic molecules between the gas and particle phases (Chang and Pankow, 2006; Zuend et al., 2010). Particle morphology can change both the thermodynamics and the kinetics of this partitioning. For aqueous ammonium sulfate and terpenederived SOM, partitioning occurs into a heterogeneous morphology of organic-rich and inorganic-rich components of the particles. By comparison, for aqueous ammonium sulfate and isoprene-derived SOM, partitioning occurs into a single homogeneous particle. The thermodynamics and kinetics related to these two morphologies can differ

- significantly. As an example, for the heterogeneous morphology, a slightly hygroscopic organic-rich phase absorbs some water in response to an increase in RH, leading to at least some increased partitioning of organic molecules from the gas phase. For homogeneously mixed particles, however, this phenomenon can be greatly enhanced by the additional water uptake associated with the much more hygroscopic dissolved in-
- ²⁰ organic salt (Zuend et al., 2010). Given the variability in atmospheric particles, such as organic composition, hygroscopicity, and the ratio of organic to inorganic material, systematic studies of how particle water content and morphology affect other atmospheric processes are an important area for future study.

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Appendix A

Probability density function $p(\varepsilon)$ of organic volume fraction ε

A1 CMFR outflow

The probability density function $p(\varepsilon;T)$ of organic volume fraction for the different particle types *T* is modeled using an approach similar to that described previously in Smith et al. (2011), with two updates in the present analysis: (1) the four particle types are individually modeled and (2) the transmission window around $d_{m,+1}^{mono}$ is taken into account. Sectional number-diameter bins are used to represent the particle population present in the inflow to the CMFR. One group of 23 bins spanning 61–83 nm physical diameter represents +1 charged particles, and another group of 31 bins spanning 90–120 nm physical diameter represents +2 charge particles. The number concentrations in these bins correspond to the SMPS measurements. The model grows each approximately monodisperse bin of the inflow into a polydisperse number-diameter distribution in the outflow using the growth equations originally presented in Seinfeld and Pankow (2003) and adapted in Smith et al. (2011). The growth rates are optimized such that the sum of the modeled distributions is in close agreement with the observed distributions in

the CMFR outflow (Smith et al., 2011). For each modeled outflow number-diameter distribution, the model also tracks the corresponding original inflow diameter d_{in} of that distribution. An organic volume fraction ε given by $1 - (d_{in}/d)^3$ can be calculated for any *d* of each outflow distribution, and the probability density function $p(\varepsilon;T)$ at any *d* is constructed by simultaneous consideration of the contributions by all distributions.

A2 DMA^{mono} outflow

The +1 and +2 particle groups are recharged as they enter the TDMA. There is correspondingly a doubling in the number of tracked number-diameter distributions: the +1 group splits into +1 and +2 subgroups as does the +2 group. These +1/+1, +1/+2,



+2/+1, and +2/+2 subgroups can be identified as the four particle types A, B, C, and D introduced in the main text. The model propagates the number-diameter distributions of the groups representing the four particles types through the transfer function of DMA^{mono} . A nondiffusing triangular transfer function is used (Knutson and Whitby,

- 5 1975). Each post-DMA distribution is still tracked to the original corresponding inflow diameter d_{in} so that the organic volume fraction ε is calculable at any d for each distribution. The number concentration n(ε;T) that is associated with any organic volume fraction is calculated for each particle type by taking the appropriate sum across all distributions. Based on n(ε;T) the probability density function p(ε;T) and the cumula 10 tive distribution function P(ε;T) are calculated for each particle type. Distributions p(ε)
- and $P(\varepsilon)$ for the entire particle population are calculated from the underlying $p(\varepsilon;T)$ and $P(\varepsilon;T)$ of the particle sub-populations by taking averages that are weighted by the subtotal concentrations.

A3 Water content

- ¹⁵ The foregoing analysis leading to $p(\varepsilon)$ and $P(\varepsilon)$ assumes that both d_{in} and d are composed only of sulfate and organic material. For the number-diameter distribution experiments of Eqs. (3a), (3b), (5a), and (5b), the size selection in DMA^{mono} takes place at 7 % RH, and an approximation of negligible water content is acceptably accurate for our data analysis under these conditions. For the transmission ratio experiments, size
- ²⁰ selection in DMA^{mono} takes place at approximately 50 to 60 % RH (i.e., Eqs. 1 and 2), and the water content is not negligible. The nominal diameter of the DMA setpoint is corrected by the water content to obtain the dry diameter *d* that is needed for $p(\varepsilon)$ and $P(\varepsilon)$. An iterative optimization approach is used for estimating the dry number-diameter distribution, as follows: (1) a dry number-diameter distribution is assumed, (2) a model
- of hygroscopic growth is applied to the dry distribution (described in next section), and (3) the modeled distribution is compared to the distribution that is implied by the transfer function of DMA^{mono}. These steps are repeated iteratively by refining the assumed dry number-diameter distribution until the modeled distribution converges to the implied



distribution. Figure S5 shows examples of the optimized dry and the DMA-implied distributions of each particle type in deliquescence-mode experiments.

A4 Hygroscopic growth

25

The volume growth factor *G* is defined as the particle volume $V(y;\varepsilon)$ at a relative humidity *y* because of water uptake divided by the particle volume V(0) in the absence of water. The hygroscopic model uses a fractional mixing rule of independent water uptake, as follows (Stokes and Robinson, 1966; Virkkula et al., 1999):

$$G(y;\varepsilon) = \frac{V(y;\varepsilon)}{V(0)} = \frac{(1-f)V_0 + f G_0(y) V_0 + G_1(y) V_1}{V_0 + V_1}$$

= $(1-\varepsilon)(1+f (G_0(y)-1)) + \varepsilon G_1(y)$ using $\varepsilon = V_1 / (V_0 + V_1)$

- for a particle having an ammonium sulfate component of volume V_0 in the absence of water and an organic component of volume V_1 in the absence of water. In the presence of water, the organic volume grows by a factor $G_1(y)$. The sulfate component grows to a volume $(1 - f)V_0 + fG_0(y)V_0$ for an aqueous sulfate growth factor $G_0(y)$. The factor f is the fraction of ammonium sulfate that is dissolved (see below). The conceptual model
- ¹⁵ implied by use of Eq. (A1) is that water is taken up independently by the organic and sulfate components even though these three components can occur mixed together in a single phase. This assumption is accurate for ammonium sulfate mixed with α -pinene dark ozonolysis SOM (Virkkula et al., 1999; Cocker et al., 2001; Smith et al., 2011) as well as for mixtures of ammonium sulfate and a variety of single organic compounds (Cruz and Pandis, 2000; Choi and Chan, 2002).

The diameter growth factor g, which is the theoretical quantity underlying the presentation of diameter changes in Fig. 3a and c, is defined as the particle diameter at a relative humidity y because of water uptake divided by the particle diameter in the absence of water (Swietlicki et al., 2008). The dependence on particle diameter (i.e., Kelvin effect) is assumed negligible for the diameters of the particles of this study.



Particles with and without water are taken as spherical. The equation is as follows:

$$g(y;\varepsilon) = \frac{d(y;\varepsilon)}{d(0)} = \left[\frac{V(y;\varepsilon)}{V(0)}\right]^{1/3}$$
$$= \left[(1-\varepsilon)\left(1+\left(g_0^3(y)-1\right)f\right)+\varepsilon g_1^3(y)\right]^{1/3}$$

The quantity $g_0(y)$ of ammonium sulfate is known (Biskos et al., 2006).

15

The growth factor g_1 of pure-phase isoprene-derived secondary organic material is calculated by inversion of Eq. (A2) for g_1 and using as inputs (1) the measured data sets for hygroscopic growth of mixed particles on the upper branch of the hysteresis curve (i.e., f = 1), (2) the known $g_0(y)$, and (3) the mode value of $p(\varepsilon)$ that is modeled for the data set. The results of the inversion analysis using data from $d_{m,+1}^{mono} = 95$, 145, 150, and 190 nm are parameterized as a continuous function $g_1(y)$ using a three-parameter fit. The curves of $g_0(y)$ and $g_1(y)$ are presented in Fig. S6.

The parameter *f*, representing the fraction of the ammonium sulfate that dissolves into aqueous form at relative humidity *y*, is used to treat partial deliquescence in the model. The solid phase has a volume $(1 - f)V_0$, and the liquid phase has a dry volume (i.e., excluding water) of $fV_0 + V_1$. For $\varepsilon \ge \varepsilon_D(y)$, particles are deliquesced and *f* is unity. For $\varepsilon < \varepsilon_D(y)$, the average composition must satisfy the relation: $\varepsilon = V_1/(V_0 + V_1)$, which re-arranges to $V_0 = V_1((1 - \varepsilon)/\varepsilon)$. The liquid phase must satisfy the liquidus relation: $\varepsilon_D = V_1/(fV_0 + V_1)$. Substitution of the result for V_0 into the equation for ε_D leads after re-arrangement to the following result:

$$f(y;\varepsilon) = \begin{cases} \frac{\varepsilon(1-\varepsilon_{\rm D})}{\varepsilon_{\rm D}(1-\varepsilon)}, & \text{for } \varepsilon < \varepsilon_{\rm D}(y) \\ 1, & \text{for } \varepsilon \ge \varepsilon_{\rm D}(y) \end{cases}$$
(A2)

The optimization between model and data sets, such as represented by the dashed red line constrained to the gray data points of Fig. 3a, relates fundamentally to optimizing $\varepsilon_{\rm D}$ of Eq. (A3). The optimized value minimizes the residual of the sum of the squares



(A1)

between the modeled and observed size distributions. Figure S7 presents a variational analysis in $\varepsilon_{\rm D}$ that demonstrates the optimization.

Supplementary material related to this article is available online at: http://www.atmos-chem-phys-discuss.net/12/9903/2012/

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Discussion Paper **ACPD** 12, 9903–9943, 2012 Deliquescence, efflorescence, and phase miscibility **Discussion** Paper M. L. Smith et al. **Title Page** Introduction Abstract Conclusions References **Discussion Paper Tables Figures** ►T. Back **Discussion** Paper Full Screen / Esc **Printer-friendly Version** Interactive Discussion

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Table 1. Parameterization of $DRH(\varepsilon)$ and $ERH(\varepsilon)$ data sets shown in Fig. 4. Coefficients ex-
press equations of the form $DRH(\varepsilon) = \sum_{i} c_{i,d} x^{i}$ valid for $0 \le \varepsilon \le 0.86$ and $ERH(\varepsilon) = \sum_{i} c_{i,e} x^{i}$
valid for $0 \le \varepsilon \le 0.55$. The parameterization of DRH(ε) is for full deliquescence. These equa-
tions for DRH(ε) and ERH(ε) appear as the dashed lines in Fig. 4. The parameterization is
accurate compared to the data within 1.5 % RH for DRH(ε) and 4 % for ERH(ε).

Coefficient	DRH	ERH
<i>c</i> ₀	80.67	28.35
C_1	-11.45	-13.66
C ₂	0	0
C3	57.99	-83.80
C ₄	-106.80	0





Fig. 1. Schematic diagram of the experimental setup for the transmission ratio and numberdiameter distribution measurements. Labeled components include the sulfate seed particle generation system (SGS), the Harvard Envrionmental Chamber (HEC), a polonium-210 charger (Po), relative humidity (RH) adjustments in Nafion tubes, differential mobility analyzers (DMA), and condensation particle counters (CPC). The background color shading of each component represents the local relative humidity (see color bar). Rainbow shading within a single component indicates that the relative humidity is scanned during the measurements. The gray dashed boxes enclose the components that comprise the TDMA.





Fig. 2. Examples of data sets and associated analysis for transmission ratio experiments. (a) Transmission ratio ϕ of the particle population as relative humidity is cycled with positive perturbations. These experiments are designed to identify deliquescence transitions. The ratio drops as the particles deliquesce. (b) Cumulative distribution function of organic volume fraction ε for this particle population. The colored circles of (a) and (b) show points of correspondence between the $\phi(RH)$ and $P(\varepsilon)$ curves. The corresponding points of each curve are the basis of the DRH(ε) curves shown in Fig. 4. Panels (c) and (d) are as described for (a) and (b) with the difference that relative humidity is cycled with negative perturbations in experiments designed to identify efflorescence transitions. The corresponding data points of (c) and (d) are the basis of the ERH(ε) curves shown in Fig. 4.





Fig. 3. Caption on next page.



Fig. 3. Examples of data sets and associated analysis for number-diameter distribution experiments. The black squares of (a) correspond to a population in which the ammonium sulfate components of all particles are fully deliguesced because of exposure to 90 % RH and the absence of efflorescence at 52 % RH. The gray squares correspond to a population in which the ammonium sulfate components of some fraction of the particles are fully deliquesced (i.e., those particles of $\varepsilon > \varepsilon_{\rm D}(52\%)$). That fraction, as well as $\varepsilon_{\rm D}(52\%)$, are unknown prior to measurement and analysis. The solid colored lines represent model results for the different particle sub-populations represented in (b). The dashed lines represent model results for the entire particle population, with the red lines as the sum of the other four colored lines, the shortdashed gray lines as a population in which the ammonium sulfate components of the particles are crystalline, and the long-dashed gray lines as a population in which the ammonium sulfate components of the particles are aqueous. A comparison between the data and the dashed lines is the basis of the DRH(ε) points shown in Fig. 4 (cf. main text for additional explanation). (b) Probability density functions $p(\varepsilon;T)$ for the different particle types that constitute the four particle sub-populations. Cartoons A through D represent these four particle types, for which organic material is in green and sulfate is in red. The background shading represents the dissolved fraction of ammonium sulfate, ranging from zero in white to unity in black (cf. Eq. A3). The ordinate of $p(\varepsilon;T)$ for each particle type is scaled to the fractional contribution to the total $p(\varepsilon)$ (i.e., to the number concentration of the particle sub-population). Panels (c) and (d) are as described for (a) and (b) but for efflorescence measurements. Other differences, especially as related to the gray squares, are described in the main text. For all panels, $d_{m+1}^{mono} = 90 \text{ nm}$.





Fig. 4. The deliquescence and efflorescence relative humidities of ammonium sulfate when mixed with isoprene-derived secondary organic material. The solid lines show the DRH(ε) and ERH(ε) as derived from data sets like panels (a)/(b) and (c)/(d) of Fig. 2. The lines represent the mean across all collected data sets, and the shading around the lines represents the minimum and maximum of the data sets. Squares show DRH(ε) and ERH(ε) values derived from the type of analysis represented by panels (a)/(b) and (c)/(d) of Fig. 3. Blue points correspond to isoprene-derived secondary organic material (this study). Black points correspond to pure ammonium sulfate. The dashed lines represent the parameterization equations for DRH(ε) and ERH(ε) that are given in Table 1.









Fig. 5. Additional results and comparison to the literature for the deliquescence and efflorescence relative humidities of ammonium sulfate when mixed with SOM. Blue lines and squares reproduce the data set of Fig. 4. **(a)** Additional results for SOM produced by isoprene photooxidation at 60 % RH with solid sulfate seed particles (magenta), at 40 % RH with aqueous sulfate seed particles (red), and at 60 % RH with aqueous sulfate seed particles (orange). **(b)** Literature results of DRH(ε) and ERH(ε) for ammonium sulfate mixed with ozonolysis products of α -pinene (green shading and lines, Smith et al., 2011; green points, Takahama et al., 2007), limonene (yellow points, Takahama et al., 2007), and β -caryophyllene (purple points, Bertram et al., 2011). **(c)** Comparison between the observations of this study and the predictions of Bertram et al. (2011) for DRH(ε) and ERH(ε) based on O:C ratio (gray shaded area). The upper limit of the gray areas corresponds to the prediction for an O:C of 0.7 and the lower limit is the prediction for O:C of 0.9. The solid lines show the prediction of Bertram et al. (2011) using O:C of 0.7. The light dashed lines show ± 10 % on this O:C ratio. The lines for the central value of 0.7 and for the perturbation of -10% nearly overlap, emphasizing the absence of sensitivity to O:C ratio for the predicted result in this range of O:C ratios.

