

This discussion paper is/has been under review for the journal Atmospheric Chemistry and Physics (ACP). Please refer to the corresponding final paper in ACP if available.

On the representation of immersion and condensation freezing in cloud models using different nucleation schemes

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Received: 22 February 2012 – Accepted: 2 March 2012 – Published: 9 March 2012

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Published by Copernicus Publications on behalf of the European Geosciences Union.

ACPD

12, 7167–7209, 2012

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Abstract

Ice nucleation in clouds is often observed at temperatures >235 K, pointing to heterogeneous freezing as a predominant mechanism. Many models deterministically predict the number concentration of ice particles as a function of temperature and/or supersaturation. Laboratory experiments at constant temperature and/or supersaturation often report heterogeneous freezing as a stochastic, time-dependent process that follows classical nucleation theory which might appear to contradict singular freezing behavior.

We explore the extent to which the choice of nucleation scheme (deterministic/stochastic, single/multiple contact angles θ) affects the prediction of the frozen ice nuclei (IN) fraction and cloud evolution. A box model with constant temperature and supersaturation is used to mimic published laboratory experiments of immersion freezing of kaolinite (~ 243 K), and the fitness of different nucleation schemes. Sensitivity studies show that agreement of all five schemes is restricted to the narrow parameter range (time, temperature, IN diameter) in the original laboratory studies.

The schemes are implemented in an adiabatic parcel model that includes feedbacks of the formation and growth of drops and ice particles on supersaturation during the ascent of an air parcel. Model results show that feedbacks of droplets and ice on supersaturation limit ice nucleation events, often leading to smaller differences in number concentration of ice particles and ice water content (IWC) between stochastic and deterministic approaches than expected from the box model studies. However, the different parameterizations of θ distributions and time-dependencies are highly sensitive to IN size and can lead to great differences in predicted ice number concentrations and IWC between the different schemes. Finally, since the choice of nucleation scheme determines the temperature range over which nucleation occurs, at habit-prone temperatures (~ 253 K) different onset temperatures of freezing create variability in the initial inherent growth ratio of ice particles, which can lead to amplification or reduction in differences in predicted IWC.

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1 Introduction

The interactions of aerosol particles and clouds represent the largest uncertainty in current estimates of radiative forcing (Solomon et al., 2007). The uncertainty is particularly acute in mixed-phase clouds, which play an important role in modulating climate.

5 For example, mixed-phase clouds are often observed in the Arctic and significantly influence radiation and energy budgets (e.g., Curry, 1995; Fridlind et al., 2007; Morrison et al., 2012). Efficient ice formation at temperatures $235\text{ K} < T < 273\text{ K}$ suggests the existence of ice nuclei (IN) that heterogeneously nucleate ice. Observations of mixed-phase clouds have shown that ice forms over relatively long time scales and in
10 the presence of a liquid phase prior to ice formation (e.g., Hobbs and Rangno, 1985; Crawford et al., 2011; Crosier et al., 2011). These observations might imply that ice nucleation occurs by freezing of droplets (immersion freezing) (de Boer et al., 2010; Lance et al., 2011).

To avoid undue complexity in the representation of poorly constrained freezing processes, models often apply parameterizations that are based on observed relationships between the number concentration of ice particles (N_{ice}) and temperature and/or ambient supersaturation with respect to ice (S_{ice}) (e.g., Fletcher, 1969; Meyers et al., 1992; Cotton and Field, 2002; Morrison et al., 2008; Phillips et al., 2008; Eidhammer et al., 2009; de Boer et al., 2010; DeMott et al., 2010). Such empirical expressions have
20 been developed based on observed freezing events and reflect the instantaneous conditions of the ice phase in the corresponding temperature and/or S_{ice} range. They imply singular, time-independent freezing that is initiated at various stages of cloud evolution.

Singular freezing behavior is in contradiction to many laboratory measurements that report continuous ice formation during experiments at constant temperature and/or S_{ice} . Such experimental results are in agreement with the classical nucleation theory (CNT) that describes ice nucleation as a stochastic, time-dependent process (Fukuta and Schaller, 1982; Khvorostyanov and Curry, 2000; Curry and Khvorostyanov, 2012). Several studies attempt to reconcile these discrepancies between the empirical,
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singular approaches that imply that active sites on IN are unambiguously associated with their freezing conditions and CNT-based stochastic approaches. While the two descriptions of heterogeneous freezing appear to be fundamentally different, stochastic freezing might exhibit no (or very little) time dependence if freezing occurs rapidly (Vali, 1971, 2008). In practice, they also might not be clearly distinguishable because of the temporal and temperature-dependent aspects of ice formation (stochasticity) (Vali and Stansbury, 1966; Vali, 1994; Field et al., 2011). A recently developed theoretical framework shows how the deterministic and stochastic descriptions converge as the number of nucleation sites increases (Niedermeier et al., 2011).

CNT for condensation and immersion freezing includes physicochemical parameters that characterize particle properties that affect water uptake by haze particles, droplet activation prior to freezing, and ice nucleation on insoluble cores within the deliquesced particles or drops. θ is defined here as the effective contact angle of ice with the IN surface. While the compatibility of the ice crystal with the solid IN surface cannot be directly measured, θ provides a convenient way to parameterize these interactions by means of a macroscopic quantity.

In many studies, θ has been derived from experimentally-determined nucleation rates J for different IN, assuming that θ is the only unknown parameter in the CNT (e.g., Archuleta et al., 2005; Chen et al., 2008; Wang and Knopf, 2011). Recent laboratory studies suggest that a single θ for one type of IN of identical bulk composition is inadequate to characterize the freezing behavior of individual particles and/or aerosol populations (Marcolli et al., 2007; Welti et al., 2009; Lüönd et al., 2010; Niedermeier et al., 2010; Murray et al., 2011; Broadley et al., 2012; Wheeler and Bertram, 2012). Fits to the observed temperature-dependence of the frozen fraction F_{fr} of the IN number concentration N_{IN} ($F_{fr} = N_{ice}/N_{IN}$) in these experiments provide parameters for different θ distributions and deterministic expressions that all reproduce the observed F_{fr} over the range of experimental conditions. A recent model study shows that cloud properties might differ greatly if different parameter sets are applied. The authors ascribed these

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differences to the variation in temperature and supersaturation of the onset of freezing due to the width of the θ distribution (Kulkarni et al., 2012).

The goal of this study is to analyze in detail the microphysical processes and their feedbacks that are the primary controls on predicted cloud properties (N_{ice} , ice water content (IWC), ice distributions) resulting from different nucleation schemes. We do so by using a variety of nucleation schemes, all of which are able to mimic laboratory nucleation events over a limited period of time. Using a series of models of increasing complexity, we shed light on the similarities and differences in these nucleation schemes for a variety of conditions, and their potential consequences for cloud evolution.

2 Model description

2.1 Ice nucleation schemes

A number of stochastic and deterministic nucleation schemes have been put forth to explain observed freezing behavior in the laboratory (L  nd et al., 2010; Niedermeier et al., 2011) and field (Fletcher, 1969; Meyers et al., 1992; DeMott et al., 2010) (Fig. 1). Their differences are explained in the following.

2.1.1 1θ scheme

CNT implies that the surface of particles of identical bulk composition can be characterized by a single θ as the dominant physicochemical property that determines their IN ability. The nucleation rate J is a function of the IN diameter (D_{IN}), the activation energy at the solution–ice interface ΔF_{act} , and the critical energy of ice germ formation ΔF_{cr}

$$J \propto D_{\text{IN}}^2 \exp \left[-\frac{\Delta F_{\text{act}} - \Delta F_{\text{cr}}}{kT} \right] \quad (1)$$

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with k = Boltzmann constant [$1.3806504 \times 10^{-16}$ erg K⁻¹], and T = temperature [K].

The formation energy of an ice germ is a function of the cosine of the contact angle ($\cos(\theta) = m$)

$$\Delta F_{\text{cr}} = 4/3\pi\sigma_{\text{i,s}} \cdot r_{\text{germ}}^2 \cdot f(m, x) \quad (2)$$

- 5 with $\sigma_{\text{i,s}}$ = surface tension of ice/solution [dynes cm⁻¹], r_{germ} = ice germ radius [cm], $f(m, x)$ = geometric factor, and $x = r_{\text{germ}}/(D_{\text{IN}}/2)$.

Thus, the probability P that a particle freezes within a given time t is influenced by θ in the exponential term ΔF_{cr} in Eq. (1)

$$P_{1\theta} = 1 - \exp(-Jt). \quad (3)$$

10 2.1.2 θ PDF scheme

Since the freezing ability of IN is a function of *surface* properties ($\sigma_{\text{i,s}}$ and θ , in Eq. 2), identical *bulk* composition of IN might not translate into the same freezing behavior of particles within an IN population. It has been suggested that IN populations are externally mixed with respect to their surface properties (Fig. 1b) since observed differences in freezing behavior of equally-sized particles cannot be fully explained by stochastic processes of identical surfaces (Marcolli et al., 2007). The overall freezing probability of such a population of N particles is the weighted sum of the probabilities for each individual particle i .

$$P_{\text{PDF}} = \frac{1}{N} \sum_i^N P_i. \quad (4)$$

- 20 Such an external mixture of particles implies that particles with the smallest θ are the most likely to freeze. Data from immersion and deposition freezing experiments have shown that the probability density function (PDF) of θ over the particle population can be described by lognormal distributions (L   nd et al., 2010; Kulkarni et al., 2012; Wheeler and Bertram, 2012).

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2.1.3 Internally-mixed soccer ball scheme (soccer (int))

While both the 1θ and the θ PDF scheme describe the surface of each particle by a single θ , images of IN show surfaces that are not smooth and uniform but exhibit numerous possible nucleating sites (cracks, imperfections, crystal structure, etc.; e.g., Kumai, 1951; Bryant et al., 1959; Fukuta, 1966; Kulkarni and Dobbie, 2009). This diversity suggests that each IN might comprise a distribution of contact angles.

Niedermeier et al. (2011) introduced the term “soccer balls” for particles with multiple nucleation sites, to reflect the patches that make up the surface of a soccer ball. The simplest soccer ball scheme assumes that all particles within a population have the same distribution of contact angles throughout their surfaces; thus, particles are identical and appear to be *internally mixed* (“int”) with respect to the surface characteristics that determine ice nucleation (Fig. 1c). The overall freezing probability of a particle with n nucleation sites is the product of the individual freezing probabilities of each nucleation site j , weighted by the fraction S_j a single nucleation site covers on the total particle surface

$$P_{\text{socint}} = 1 - \prod_j^n [\exp(-J_j S_j t)] \quad (5)$$

As J depends exponentially on ΔF_{cr} , which includes θ in the geometric factor, the relative impact of a nucleation site j with a small θ_j on J_j in the exponential term in Eq. (5) will tend to be greater than the weighting factor S_j . Thus, a single nucleation site can dominate the overall freezing probability P_{socint} if θ_j (and/or S_j) are sufficiently low.

2.1.4 Externally-mixed soccer ball scheme (soccer (ext))

Both the θ PDF and the soccer (int) scheme are idealized representations of θ distributions throughout IN populations. A more realistic description represents the combination of these two schemes as it is likely that statistical θ distributions extend over

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the total surface area of an aerosol population rather than being confined to a single particle. Thus, particles are *externally mixed* (“ext”) soccer balls with respect to their θ distributions (Fig. 1d).

The freezing probability of a population of N different particles that each have n nucleation sites can be described by combination of Eqs. (4) and (5). L    nd et al. (2010) have shown that the surface density of nucleation sites can be fit to an exponential expression with very few relatively low contact angles and a nearly uniform θ distribution towards higher values (bottom panel of Fig. 1d). A surface-density dependent θ distribution over the surface of an IN population could explain higher IN efficiency for larger particles as they likely have a greater number of nucleation sites and a statistically higher probability of freezing, exceeding the increase in P that is predicted due to IN size based on CNT (Eq. 1) (Welti et al., 2009). Niedermeier et al. (2011) have shown that the increase in n on a single particle can explain the transition from stochastic to apparently singular freezing behavior since statistically the abundance of efficient nucleation sites increases. These findings are in qualitative agreement with those by Fletcher (1958) who showed a strong size-dependence of freezing ability of particles smaller than ~ 100 nm whereas this dependence is significantly reduced at larger sizes.

2.1.5 Deterministic scheme

Deterministic schemes as used in many models describe N_{ice} as a function of temperature and/or supersaturation (Fletcher, 1969; Cotton et al., 1986; Meyers et al., 1992). Some parameterizations also take the bulk chemical composition and size of IN into account (Phillips et al., 2008; DeMott et al., 2010; Eidhammer et al., 2010). These parameterizations do not include any constraint on the total N_{ice} , i.e., they are not limited by the number of potential IN that exist in the aerosol population. In ice chamber experiments, N_{IN} is constrained by the experimental conditions and thus N_{ice} is capped by an upper limit of N_{IN} . Therefore, rather than considering N_{ice} , experimentally determined frozen fractions F_{fr} have been fitted as a function of temperature and IN surface area

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S_{IN} , such as

$$F_{\text{fr}} = 1 - \exp[-S_{\text{IN}}A_1(T + A_2)^2] \quad (6)$$

below a temperature threshold $-A_2$ [°C], and $F_{\text{fr}} = 0$ at higher temperatures (Lüönd et al., 2010; Niedermeier et al., 2010).

2.2 Description of the box model

Lüönd et al. (2010) performed experiments of immersion freezing of kaolinite in an ice chamber where particles had a residence time of ~ 14 s at constant temperature and supersaturation. They presented F_{fr} as a function of temperature for experiments in a range of $237.5 \text{ K} < T < 241.0 \text{ K}$. In order to parameterize the observed freezing behavior, they fitted different nucleation schemes (Fig. 1a, b, c, e) to the experimental results and demonstrated that with the derived fit parameters all schemes predict F_{fr} very similar to each other and to the experimental data.

In order to anchor our simulations in the realism of laboratory experiments, we perform box model studies that closely mimic the simulations by Lüönd et al. (2010) using different nucleation schemes (Fig. 1). The box model describes in detail the activation of monodisperse aerosol particles to droplets using Köhler theory over a range of relative humidity with respect to water, $99 \% < \text{RH}_w < 100.2 \%$. After an initialization period (1 s), RH_w is kept constant at supersaturated conditions (supersaturation with respect to water, $S_w = 0.2 \%$) in order to prevent droplets from evaporating and to allow formation of ice particles through immersion freezing. Simulations are performed at 12 temperatures, constant over the simulation time, in the same range as the laboratory experiments by Lüönd et al. (2010). The temperature together with the constant S_w determines S_{ice} in each simulation. For the θ PDF and both soccer ball schemes, a random selection of contact angles is sampled from the distributions shown in the bottom panel of Fig. 1. The number of selected contact angles varies for the different schemes but each selection reasonably represents the overall distribution (Table 1).

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Limitations of the experimental setups do not allow continuing laboratory experiments for times much beyond the initial nucleation events owing to the rapid decline of S_{ice} by efficient water vapor deposition on the newly formed ice particles (L  nd et al., 2010; Wheeler and Bertram, 2012). However, the box model allows us to explore numerically the temporal evolution of predicted F_{fr} beyond the initial freezing events using the various nucleation schemes described in Sect. 2.1.

2.3 Description of the adiabatic parcel model

In contrast to the box model simulations where temperature, S_w , and S_{ice} are constant, the cloud parcel model simulates the dynamical feedbacks on the supersaturation field as a result of the source due to the cooling rate (\propto constant updraft velocity w), and sinks by the water vapor condensation onto aerosol particles, droplets and deposition on ice particles:

$$\frac{dS_{\text{ice}}}{dt} \propto \frac{dS_w}{dt} = \underbrace{C \cdot w}_{\text{Cooling}} - \underbrace{\phi_1 \frac{d\text{LWC}}{dt}}_{\text{Condensation}} - \underbrace{\phi_2 \frac{d\text{IWC}}{dt}}_{\text{Deposition}}, \quad (7)$$

where C , ϕ_1 , ϕ_2 are well-known functions of temperature, pressure and ambient supersaturation, and LWC and IWC represent the liquid (i.e. water on droplets and aerosol particles) and ice water contents [g kg^{-1}], respectively.

The model using the 1θ scheme has been previously described in detail (Ervens et al., 2011). In brief, particles are treated on a moving size grid with the initial size determined by the discrete aerosol particle mass at that grid point. Cloud droplets form on a population of cloud condensation nuclei (CCN), composed of ammonium sulfate and insoluble material (kaolinite), in 11 size classes with a lognormal size distribution ($\sigma_g = 1.4$, $r_g = 0.04 \mu\text{m}$) over a size range of $0.02 \mu\text{m} < D_{\text{CCN}} < 2 \mu\text{m}$ with a total concentration of $N_{\text{CCN}} = 100 \text{ cm}^{-3}$. The same random selection of contact angles is sampled from the PDFs of the soccer ball and θ PDF schemes as used in the box model

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studies (Fig. 1; Table 1). Since the freezing probability generated by any scheme would lead to an unmanageable number of ice classes during the course of the simulation, a more computationally efficient method is to establish a new ice size class when a discrete percentage (e.g., 1 % or 2.5 % for the simulations in this study) of a particle class, characterized by size and contact angle, is predicted to freeze. The choice of the relatively broad probability bin width can on occasion generate stepwise results at small time scales but the overall results are unchanged. The description of the growth of ice particle includes the temperature-dependent evolution of their primary habits (Chen and Lamb, 1994; Sulia and Harrington, 2011). The parcel model simulations are initialized at $T = 241$ K and $RH_w = 99$ % and chosen in a way that the parcel reaches the conditions as in the box model (Sect. 3.1) shortly after initialization.

In a first set of parcel model simulations, it is assumed that only a fraction of a single CCN size class ($D_{CCN} = 800$ nm) act as ice nuclei with a concentration of $N_{IN} = 4$ l⁻¹; freezing of droplets formed on other particle sizes and ice nucleation by contact or deposition freezing are not considered. The freezing of IN that are immersed in a droplet or haze particle follows the description by Khvorostyanov and Curry (2004) and includes both immersion and condensation (deliquescence) freezing. This approach allows ice nucleation under both subsaturated and supersaturated conditions with respect to water.

Simulations of monodisperse IN allow us to compare the parcel model results (Sect. 4.1) to the laboratory-based box model studies (Sect. 3). In a second set of simulations, a polydisperse IN distribution is assumed, where a fraction of all CCN size classes can act as IN, yielding the same total IN number concentration (Sect. 4.2). Building on our previous study where we explored systematically the effects of various parameters (N_{IN} , N_{CCN} , w , ice particle habits) on the ice/liquid partitioning in mixed-phase clouds (Ervens et al., 2011), we restrict our analysis here to some selected conditions in order to highlight the sensitivities of N_{ice} and IWC to the different nucleation schemes.

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3 Box model results

3.1 Agreement of nucleation schemes with laboratory studies

We reproduced the simulations by Lüönd et al. (2010) using one of their selected particle sizes ($D_{\text{IN}} = 800 \text{ nm}$), albeit with slightly different parameters to describe the θ distributions by the stochastic models. These parameters, together with the assumed number of different θ in the θ PDF scheme and nucleation sites in the soccer ball schemes are summarized in Table 1. A slight shift in freezing temperature and F_{fr} can be easily achieved by different random selections of contact angles even if the overall θ distribution is described by the same fit parameters. We note that the exact match between our parameters and those by Lüönd et al. (2010) for the different nucleation schemes is not of critical importance for the following analysis, but our discussion will instead build on the fact that all schemes predict similar F_{fr} over a temperature range of $237.5 \text{ K} < T < 241.0 \text{ K}$ (Fig. 2). Each point marks a single simulation of 14 s duration.

The conditions under which all schemes predict identical F_{fr} (50 % at $T = 240 \text{ K}$ and $S_{\text{ice}} = 38.1 \%$) are used as initial conditions for additional box model simulations to explore the temporal evolution of F_{fr} ($t \leq 200 \text{ s}$). Even though after 14 s all five schemes show $F_{\text{fr}} = 50 \%$ for $D_{\text{IN}} = 800 \text{ nm}$ (solid lines in Fig. 3), the slopes of the individual lines are different, affecting the evolution of F_{fr} at longer time scales. By definition, the deterministic scheme does not show any time dependence and appears as a horizontal line. The 1θ and the soccer (int) schemes show nearly identical F_{fr} . This behavior can be explained if

$$P_{1\theta} \sim P_{\text{socint}} \quad (8)$$

i.e., if the overall nucleation rates in Eqs. (3) and (5) are approximately equal:

$$J_{1\theta} t \sim \sum_i^n (J_i S_i t) \quad (9)$$

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The distribution in the soccer (int) scheme exhibits a few small θ that are lower ($\theta_{\text{socint,min}} = 75^\circ$) than the single value in the 1θ scheme ($\theta_{1\theta} = 88.8^\circ$); the majority of the contact angles is larger than this single value. Large θ do not contribute significantly to P_{socint} and, thus, the sum of $(J_j S_j t)$ is mostly dominated by contributions by the smallest contact angles. It is obvious that the agreement between the two schemes might not occur for different θ distributions and/or selections in the soccer (int) scheme.

3.2 Impact of IN diameter D_{IN} on frozen fraction F_{fr}

According to Eq. (1), J is directly proportional to the IN surface area (D_{IN}^2) and a complex function of D_{IN} in the ΔF_{cr} term. Thus, varying the IN size while all else is equal leads to different freezing probabilities. For simplicity, we assume here that the number of nucleation sites is the same on small and large particles. This approach implies that the size of the nucleation sites increases with IN size. While there is no physical basis for this assumption, and it might be more reasonable to scale the number of nucleation sites with particle surface, such a treatment would add more complexity to our conceptual model analysis since the IN ability of larger particles would increase not only due to size but also due to a statistically larger variety of nucleation sites.

For $D_{\text{IN}} = 1600 \text{ nm}$, the 1θ , and both soccer ball schemes predict $F_{\text{fr}} \sim 100\%$ after a few seconds (dashed lines in Fig. 3a). In this case, the evolution of F_{fr} appears to be (nearly) time-independent since J increases in response to a doubling of D_{IN} (Eqs. 1 and 2). The very high F_{fr} for large D_{IN} results in very small absolute and relative differences between the schemes. For smaller D_{IN} (400 nm), all five schemes lead to smaller F_{fr} (dotted lines in Fig. 3a). As a result, the relative spread in F_{fr} for $D_{\text{IN}} = 400 \text{ nm}$ amongst the five schemes is larger, and F_{fr} differs by more than a factor of four after 200 s, from $F_{\text{fr}} \sim 18\%$ (deterministic) to $F_{\text{fr}} \sim 80\%$ (1θ and soccer (int) schemes).

3.3 Variation of temperature and S_{ice}

A reduction in temperature leads to higher supersaturation (S_{ice}) if $S_w = \text{const} = 0.2\%$, and J increases exponentially with decreasing temperature (Eq. 1). Model results for the narrow range of $238.8\text{ K} < T < 240\text{ K}$ and $39.7\% > S_{ice} > 38.1\%$ ($D_{IN} = 800\text{ nm}$) exhibit very similar trends (Fig. 3b) as compared to those achieved by varying D_{IN} .

The results in Fig. 3 show that only for the specific conditions near the cross-over point in Fig. 2, do the different freezing schemes predict identical F_{fr} . Thus, we caution against extrapolating the general agreement of all five schemes at prescribed laboratory conditions to a wider range of conditions. These simple box model simulations for well-constrained conditions, i.e. time-invariant temperature, S_{ice} and S_w , suggest a potentially significant sensitivity of F_{fr} to nucleation scheme in a continuously cooling air parcel experiencing temporal evolution of temperature and supersaturation. The extent to which this is true is investigated in Sect. 4.

4 Parcel model results

4.1 Monodisperse IN

4.1.1 Variation of updraft velocity

The relative strength and time-dependence of cooling and condensation/deposition terms in Eq. (7) determine the vertical (or equivalently temporal) profile of S_w and S_{ice} . While condensation freezing can occur at subsaturated conditions ($RH_w < 100\%$), immersion freezing requires the formation of droplets prior to ice nucleation, i.e., S_w has to exceed the critical supersaturation $S_{w,crit}$ for a CCN with a given size and composition, and has to remain sufficiently high throughout the cloud in order to prevent droplets from evaporating. For the single aerosol particle size class that act as CCN and IN in the model, this threshold is $S_{w,crit} \sim 0.15\%$ (Pruppacher and Klett, 2003); however

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larger CCN will form droplets at lower S_w . Since the model includes both condensation and immersion freezing, ice nucleation can continue if droplets evaporate as the remaining haze particles can form ice by condensation freezing if the size of the ice germ exceeds the required threshold value (Khvorostyanov and Curry, 2000).

Figure 4a shows the vertical evolution of N_{ice} as predicted by the five nucleation schemes for a cloud of 300 m depth in an air parcel rising with $w = 50 \text{ cm s}^{-1}$. Similar to the box model results, the θ PDF model leads to smaller N_{ice} than the other stochastic models since only IN with sufficiently low θ form ice; the probability that such low θ are abundant on IN with multiple nucleation sites is much greater and thus F_{fr} is nearly 100 % ($N_{ice} = 4 \text{ l}^{-1}$) for the 1θ and the soccer ball schemes. In fact, closer inspection of results shows that the source of these ice particles can be partially ascribed to condensation freezing below the critical supersaturation of CCN. All stochastic schemes predict very rapid nucleation of a large N_{IN} fraction near cloud base since the supersaturation is sufficiently high to activate IN with relatively low θ . As already suggested by the box model studies, the range of N_{ice} predicted by stochastic schemes is bounded by the θ PDF scheme for the smallest values and the 1θ and the soccer (int) scheme that predict the fastest and most efficient ice formation. The soccer (ext) scheme, which is likely the most realistic representation of IN surface properties, shows N_{ice} in between these two limits. N_{ice} predicted based on the deterministic scheme reflects the continuous cooling rate of the air parcel during its ascent. The evolution of IWC for the same simulation (Fig. 4b) can be explained by the trends in N_{ice} : ice particles that nucleate near cloud base have the longest growth times. The gradual increase in N_{ice} predicted by the deterministic scheme leads to the smallest IWC since relatively few ice particles start growing near cloud base. The ice size distribution in the θ PDF scheme comprises about 0.5 l^{-1} large particles that formed near cloud base; even though the final N_{ice} is smaller in the θ PDF scheme, these early-nucleated particles lead to a similar IWC as compared to the 1θ and the soccer (int) schemes; in the latter cases the ice nucleation events occurred more gradually between $\sim 20 \text{ m}$ and 50 m resulting in similar growth

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time scales, and ice particle sizes. Thus, the agreement in IWC amongst the stochastic schemes is related to a combination of N_{ice} and the duration of growth.

The amount of liquid water greatly dominates the total condensate, and the condensation term presents the most significant sink for supersaturation (Eq. 7). The IWC ($\sim 0.003 \text{ g kg}^{-1}$ at $h = 300 \text{ m}$) in all simulations represents less than $\sim 6\%$ of the total condensate, (IWC + LWC) $\sim 0.05 \text{ g kg}^{-1}$. Under such conditions, the LWC is not affected by the ice phase and the water vapor supply allows both droplets and ice particles to grow independently of one other (Ervens et al., 2011).

At smaller updraft velocities ($w = 10 \text{ cm s}^{-1}$), the cooling term is smaller causing a lower maximum supersaturation near cloud base ($S_{w,max} = 0.8\%$; $S_{ice,max} = 38\%$ at $h = 25 \text{ m}$; as opposed to $S_{w,max} = 2.3\%$, $S_{ice,max} = 40.3\%$ at $h = 60 \text{ m}$ for $w = 50 \text{ cm s}^{-1}$). With a weaker supersaturation source term, the condensation sink to droplets plays a commensurately larger role in regulating S_w and S_{ice} (Eq. 7). In general, the trend in the divergence of N_{ice} between the different schemes is similar to the box model results (Fig. 3) that show a greater divergence and time-dependence for the stochastic schemes at low S_{ice} . All IWCs are greater for low w and more similar to each other than for high w at a given height (Fig. 4b and d) because the lower updraft velocity implies longer growth time scales for particles, considering an equivalent cloud depth. The similar trends of N_{ice} and IWC between the schemes suggest that ice growth rates might be comparable and thus average particle sizes are similar.

The differences in vertical temperature profiles are small because w dominates the cooling rate and differences in latent heating associated with condensation/deposition are small. Thus the evolution of N_{ice} in Fig. 4a and c are almost identical for the deterministic scheme, which does not take into account any feedbacks of supersaturation on N_{ice} (Eq. 6). Unlike the box model studies, the deterministic scheme in the parcel model predicts similar N_{ice} to the stochastic schemes (at cloud top) because of continuously decreasing temperature. This behavior suggests that in constantly cooling clouds N_{ice} might be predicted by appropriate deterministic parameterizations of ice nucleation spectra (Vali, 1994). The evolution of N_{ice} predicted is determined by

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the temperature range in the case of the deterministic scheme, and the supersaturation field that determines the occurrence of further nucleation events in the stochastic schemes.

Note that we have presented all model results at the same cloud thickness; however, ambient observations show that thinner clouds are usually observed in low-updraft regimes. If one considers similar growth *times*, IWC is significantly smaller at the low w (e.g., compare IWC at 300 m for $w = 50 \text{ cm s}^{-1}$ to IWC at 60 m for $w = 10 \text{ cm s}^{-1}$) because of the lower N_{ice} .

4.1.2 Initiation of the Bergeron-Findeisen-Process

It has been discussed previously that low updrafts provide conditions in mixed-phase clouds that weaken the stability of the liquid phase as S_w is not sufficiently high to maintain continuous droplet growth (Korolev and Isaac, 2003; Ervens et al., 2011). Ice particles will grow at the expense of the droplets (Bergeron-Findeisen process) resulting in fully glaciated clouds.

The 1θ and the soccer ball schemes predict $N_{\text{ice}} \sim 3 \text{ l}^{-1}$ above $h \sim 150 \text{ m}$ at very low updraft velocity ($w = 2 \text{ cm s}^{-1}$) (Fig. 4e). In contrast to conditions of higher supersaturation (higher w), at low w far fewer CCN are activated into droplets, resulting in a smaller condensation term and thus a relatively larger impact of vapor deposition on S . The θ PDF scheme initiates ice nucleation near cloud base ($N_{\text{ice}} \sim 0.6 \text{ l}^{-1}$); these ice particles limit the maximum supersaturation and thus N_{ice} , S_{ice} and S_w reach lower maximum values and peak higher in the cloud as compared to the other schemes (Fig. 5a with zoom of the region near cloud base in Fig. 5b). Ice nucleation requires the formation of an ice germ above a threshold size; this critical germ size increases with decreasing supersaturation which causes less efficient nucleation (Khvorostyanov and Curry, 2000, 2004; Curry and Khvorostyanov, 2012). The decrease in supersaturation prevents additional freezing events by increasing the required size threshold for ice germs and thus N_{ice} remains constant as soon as the supersaturation decreases (vertical lines in Fig. 4e above 100 m). The decrease in S_{ice} (Fig. 5c and d) is not as

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significant as that for S_w and the cloud always remains supersaturated with respect to ice. The evaporating droplets decrease the LWC and provide an additional source of water vapor for the further growth of ice particles, which explains the continuous increase in IWC (Fig. 4f).

5 N_{ice} and S_w from the deterministic and θ PDF schemes are similar to each other near cloud base; their early onset of freezing results in particles that have a distinct impact on S . Since the deterministic scheme does not take into account any feedbacks of the supersaturation on ice nucleation, N_{ice} and IWC continue to increase, with commensurate influence on LWC loss (Fig. 4f, inset). In contrast, N_{ice} asymptotes at about 100 m
10 in the θ PDF scheme. For the other stochastic schemes, nucleation is delayed relative to the θ PDF scheme. This leads to shorter growth time and smaller ice particles, which allows supersaturation to reach larger values higher in the cloud, and the liquid phase to persist longer (Fig. 4f, inset).

The initiation of the Bergeron-Findeisen-Process is closely linked to the stability and
15 lifetime of mixed-phase clouds. Even though the parcel model is limited in its ability to simulate cloud stability and lifetime effects in detail due to its simplistic treatment of dynamic processes, it can be concluded that under conditions where the ice and liquid phases significantly impact supersaturation (and vice versa), detailed knowledge of the duration of ice nucleation events over a given temperature range is required to correctly
20 predict mixed-phase cloud properties.

The updraft regimes explored here represent three different scenarios in terms of impacts on cloud evolution. (i) The high supersaturation at $w = 50 \text{ cm s}^{-1}$ exceeds a threshold supersaturation that is required to nucleate ice on nearly all IN on very short time scales. Thus, under such conditions detailed knowledge of contact angle distributions is likely less critical. (ii) The supersaturation profile at $w = 10 \text{ cm s}^{-1}$ covers
25 the range of the onset supersaturations for the θ ranges throughout the IN population. Thus, subtle differences in θ (distributions) on IN translate into different N_{ice} . Under those conditions, different nucleation schemes will lead to different ice nucleation spectra ($N_{ice} = f(S, T)$) (Barahona, 2011). (iii) While in the latter two regimes there is very

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little impact of IWC on S , at very low updraft ($w = 2 \text{ cm s}^{-1}$), the differences in N_{ice} associated with the different temperature ranges over which nucleation occurs can impact cloud phase distribution due to significant feedback of IWC on S .

4.1.3 Considerations on the temperature range of nucleation events

5 Temperature dependence of ice habit formation

The nucleation schemes predict different temperature ranges over which nucleation events occur. While many nucleation events are predicted almost synchronously by the stochastic models over a narrow temperature range ($w = 50 \text{ cm s}^{-1}$, $h < 50 \text{ m}$, $240.5 \text{ K} < T < 241.0 \text{ K}$; and $w = 2 \text{ cm s}^{-1}$, $h < 150 \text{ m}$, $239.5 \text{ K} < T < 241.0 \text{ K}$), the deterministic scheme predicts nucleation throughout the depth of the cloud for all w ($237.7 \text{ K} < T < 241.0 \text{ K}$).

In general, the temperature at which ice nucleation occurs determines the initial ice particle shape which is described by the inherent growth Γ ratio of the ice particle and is equal to the ratio of the water vapor condensation coefficients along the basal (c) and prism (a) axes (Hallett and Mason, 1958; Chen and Lamb, 1994; Lamb and Verlinde, 2011). At the temperature range relevant for immersion/condensation freezing of kaolinite ($T \sim 243 \text{ K}$), Γ is near unity, i.e. ice particles are approximately spherical (Fig. 6). At higher temperatures, Γ might differ significantly from unity and strongly impact the evolution of the aspect ratio ($\varphi g = c/a$) of an ice particle that develops from the initial geometry, prescribed by Γ , towards a geometry as predicted at a given temperature. Such more extreme habits result in highly nonlinear growth rates of ice particles in different temperature regimes since non-spherical particles grow faster than spheres of the same mass (Mason, 1953; Takahashi et al., 1991). Atmospheric observations reveal that ice is sometimes formed at habit-prone temperatures and model studies have shown the need of the detailed description of ice growth rates as they significantly affect the phase partitioning in mixed-phase clouds (Avramov and Harrington, 2010; Sulia and Harrington, 2011). Ice nucleation at such temperatures implies the presence

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of more efficient IN than kaolinite, such as biological particles (Schnell and Vali, 1976; Christner et al., 2008) or other types of dust (Roberts and Hallett, 1968; DeMott et al., 2003; Möhler et al., 2006).

Model studies at higher temperatures (T1 and T2)

5 Notwithstanding the lack of comprehensive parameter sets from laboratory experiments for all nucleation schemes for IN that nucleate ice at $\sim 253 \text{ K} < T < \sim 263 \text{ K}$, in the following, we explore effects of nonlinear growth rates on N_{ice} and IWC of ice particles nucleated at these temperatures ranges. These simulations demonstrate effects in a more conceptual way and add other potential aspects that could lead to convergence
10 or divergence in predicted cloud properties due to different temperature ranges of ice nucleation. We have chosen two temperature ranges (T1 and T2) in such a way that with decreasing temperature, Γ approaches unity in the former, and shows the opposite trend in the latter (Fig. 6). We limit this analysis to the 1 θ and deterministic schemes and adjust the two parameter sets (θ , A_1 , A_2 , Table 1) for the temperature regimes
15 T1 and T2, respectively, in order to predict first nucleation events at the same height in the cloud as for the results discussed for kaolinite. The appropriate selection of parameters results in a similar temporal (vertical) evolution of N_{ice} to that obtained by the model studies at the lower temperature (Fig. 4). Model conditions are chosen such that the Bergeron-Findeisen-Process does not occur ($N_{\text{IN}} = 1 \text{ l}^{-1}$, $w = 10 \text{ cm s}^{-1}$) in order
20 to exclude nonlinear increases in IWC due to rapid changes in phase partitioning.

Similar to the findings in Fig. 4, in T1 most nucleation events predicted by the 1 θ scheme occur near cloud base whereas continuous ice nucleation is predicted over the depth of the cloud for the deterministic scheme (Fig. 7a). The resulting IWCs differ by a factor of ~ 4 ($h = 300 \text{ m}$) between the two schemes (Fig. 7b). The evolution of N_{ice}
25 in the temperature regime T2 is very similar to that in T1 (Fig. 7c), as pre-determined by the parameter sets θ and A_2 for the respective temperature range (Table 1). However, the resulting IWC from the two schemes are much more similar in T2 and only differ by a factor of two (Fig. 7d). The reason lies in the behavior of Γ in the two different

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temperature regimes and the different temperature *ranges* over which freezing occurs. For the warmer T2, the 1θ scheme predicts freezing occurring over a very narrow temperature range with an initial inherent growth ratio $\Gamma \sim 0.7$ (blue shading in Fig. 6). For the deterministic model freezing occurs over a much larger temperature range (green shading) with Γ becoming progressively *smaller* than 0.7. Such particles with smaller initial Γ are less spherical and grow faster than the high number of particles that are predicted by the 1θ scheme to freeze near cloud base ($T \sim 263$ K; $\Gamma \sim 0.7$), resulting in small IWC differences. In T1, ice particles predicted by the 1θ scheme near cloud base benefit from smaller Γ (~ 0.3) and, thus, have higher growth rates throughout the cloud since they are more plate-like due to their initial geometry than particles that nucleate at lower temperature. For the deterministic model, progressively colder temperatures result in an *increase* in Γ , leading to more spherical particles with smaller growth rates. Thus, the many non-spherical particles predicted by the 1θ scheme not only have longer growth times but also higher growth rates, which results in a larger differential in IWC between the two nucleation schemes.

The tendency for IWC to often scale with N_{ice} (Figs. 4 and 7) suggests that ice particle sizes are relatively uniform amongst the different schemes. Indeed, additional analysis of the results in Fig. 4 shows that particle sizes for all five schemes cover a similar size range of ~ 10 μm and 250 μm (at 200 m, not shown). This relatively broad range is due to the large spread in onset temperatures of freezing for the monodisperse IN which implies different growth time scales for ice particles nucleated at different times and thus reflects the stochastic and temperature-dependent nature of the freezing process. A more thorough analysis of the size distributions from these simulations is not particularly meaningful since ambient IN distributions are unlikely to be monodisperse. Nevertheless, the assumption of monodisperse IN has allowed us to separate effects of different nucleation schemes on N_{ice} without having to deal with potential effects due to different IN sizes.

4.2 Parcel model studies: polydisperse IN

4.2.1 Ice/liquid distribution

Since the box model results in Sect. 3 suggested a great sensitivity of F_{fr} to IN size if D_{IN} is varied by a factor of two, we performed additional simulations ($w = 10 \text{ cm s}^{-1}$) where we assume that a fraction of *each* of the 11 CCN size classes ($0.02 \mu\text{m} < D_{CCN} < 2 \mu\text{m}$) can form ice; the total IN number is the same as in the simulations discussed in Sect. 4.1 ($N_{IN} = 4 \text{ l}^{-1}$ at $T \sim 243 \text{ K}$ (kaolinite); $N_{IN} = 1 \text{ l}^{-1}$ at T1 and T2). These simulations yield a more realistic picture of ice size distributions and tie in with our previous analysis where we showed that the temporal (vertical) change of LWC as a function of the ratio of the integral ice capacitance to the integral droplet radius can be considered a measure of the stability of a mixed-phase cloud (Ervens et al., 2011).

Predicted N_{ice} show a much greater discrepancy between the five schemes than the results for monodisperse IN (Fig. 8a). Since most IN are smaller than 800 nm, all schemes predict much lower N_{ice} . While in the simulations of monodisperse IN, the 1 θ and the soccer (int) schemes showed nearly identical N_{ice} for all updraft velocities, the difference in N_{ice} resulting from different IN size classes is significant for these two schemes. As explained above, for a given size the predicted freezing probabilities might be equal if Eq. (9) holds true. However, since J is a complex function of D_{IN} (Eqs. 1 and 2), $P_{1\theta}$ and P_{socint} do not scale proportionally with D_{IN} so that one no longer expects agreement. The strong size dependence of F_{fr} in the deterministic approach (Eq. 6) results in very small N_{ice} for the selected initial size distribution. The trend in N_{ice} is reflected in IWC with the exception of the θ PDF scheme higher in the cloud owing to high N_{ice} near cloud base.

The evolution of LWC shows that under these model initial conditions the choice of the nucleation scheme might have bearing on the stability of the cloud (Fig. 8b). The soccer (int) scheme predicts the largest N_{ice} and IWC and thus LWC is clearly affected, as evidenced by a deceleration of growth with increasing height. This sensitivity to the different nucleation schemes is more clearly depicted by the ratio IWC/LWC (Fig. 8c):

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in situations where $IWC \sim 0.5$ LWC there is noticeable evidence of cloud droplets evaporating due to the Bergeron-Findeisen process.

The adiabatic conditions in the parcel model determine the total amount of condensate ($IWC + LWC$) which is smaller at lower temperatures. This is clearly seen in the significantly smaller $IWC + LWC$ for the colder regime compared to the warmer regimes (T_1 and T_2) (cf. Fig. 8b and e). Ratios of IWC/LWC are notably smaller than at the colder temperature (cf. Fig. 8c and f). The similar evolution of N_{ice} at T_1 and T_2 is due to the parameter choices for these simulations. (Recall that $\theta_{1\theta}$ and A_2 , Table 1, were adjusted in order to produce similar vertical N_{ice} profiles as compared to the corresponding schemes at $T \sim 243$ K.) The differences in N_{ice} between the nucleation schemes are much greater as compared to results in Fig. 7a and c due to the different dependencies of F_{fr} on IN size.

4.3 Size distribution of ice particles

Ice size distributions from the above simulations for polydisperse IN at $h = 200$ m are shown in Fig. 9a (lower temperatures) and 9b (higher temperatures, T_1 and T_2). The equivalent diameter of a (non-spherical) ice particle is used to represent the diameter of a sphere with the same mass. Since the number of ice size classes in the model is huge (several thousand classes for the externally-mixed θ PDF and soccer (ext) schemes) but each ice class only contains a very small number of particles, size distributions are created by sorting into ten equally-spaced size bins. The size range of nearly spherical ice particles that grew at cold temperatures is very similar for all nucleation schemes (Fig. 9a), which is consistent with the trend of N_{ice} and IWC to scale (Fig. 8a). The higher IWC in the soccer (int) scheme (Fig. 8b) is consistent with the high number of ice particles that nucleated near cloud base. Even though these particles slightly reduce the supersaturation, the growth rates of ice particles are not significantly affected as compared to those predicted in the other schemes, resulting in similar particle sizes. In general, the change in supersaturation (Eq. 7) is mostly controlled by the numerous small droplets (LWC) and to a smaller extent by the much fewer

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ice particles if both phases grow independently of one other. Only under conditions of the Bergeron-Findeisen process (e.g., near cloud top in the soccer (int) scheme), when LWC and thus the impact of the condensation term on S decreases, does efficient deposition of water vapor on ice particles represent a major sink for supersaturation.

Under those conditions, the ice particles benefit from the evaporation of droplets as an additional source of water vapor. The consistency in size range between the 1 θ and deterministic scheme is also evident in the simulations at T1 and T2 (Fig. 9b). At the same temperature, the size range is similar for the two nucleation schemes. On the other hand, the size range differs between the T1 and T2 regimes because in T1 particles grow more efficiently owing to their more extreme habits in T1 (Sect. 4.1.3).

The capacitance C of a spherical particle equals particle radius; for non-spherical particles capacitance is determined by the curvature of the particle (e.g., McDonald, 1963). The integral capacitance is the number-weighted capacitance in each size class i , $\Sigma_i(N_{ice,i} \cdot C_i)$. Many different combinations of individual $(N_{ice,i} \cdot C_i)$ can yield the same integrated value and thus affect the evolution of IWC and its impact on LWC to similar extents (Ervens et al., 2011). Figure 9c and d display N_{ice} as a function of the mean capacitance C_{mean} (average value over all C_i [μm] within the ice particle population). The contours show lines of equal integral capacitance [$\mu\text{m l}^{-1}$]. The distributions of (nearly) spherical particles show a very similar C_{mean} for all schemes over the depth of the cloud (color-coding indicates height) (Fig. 9c). Both the size distributions and the mean capacitances show that the particle sizes do not differ much between the different schemes. This consistency is similar to that found in our previous study where we showed that different N_{ice} result in similar equivalent diameters for the same growth time scales (Ervens et al., 2011). It was concluded that the vapor supply is sufficient in order to allow independent particle growth without competition for water vapor. The integral capacitance differs by a factor of seven between the soccer (int) [3] and the deterministic [5] scheme due to the different $N_{ice}(C_{mean, soccer(int)} \sim 700 \mu\text{m l}^{-1}; C_{mean, determ} \sim 100 \mu\text{m l}^{-1})$. At the higher temperatures (T1 and T2) the vertical evolution of the mean capacitance is not as consistent as for

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the more uniform spherical particles at the lower temperatures since the different initial particle shapes and resulting growth rates lead to different capacitances throughout the ice population. However, the differences in C_{mean} between the two different nucleation schemes ($C_{\text{mean},1\theta}/C_{\text{mean,determ}} \sim 160/20$) are very similar to those at $T \sim 243$ K.

This analysis suggests that the choice of the nucleation scheme does not affect resulting particle growth rates and sizes to a significant extent but that the differences in resulting integral capacitance are mostly ascribed to differences in N_{ice} . Thus, the choice of the nucleation scheme has the most significant impact on N_{ice} by determining the timing of nucleation events, subsequent duration of ice growth, and the temperature regime over which ice growth occurs. For a given temperature regime, the nucleation scheme has little influence on growth rates of ice particles as long as the cloud is supersaturated with respect to ice.

5 Conclusions

Model simulations have been performed to explore the sensitivity of cloud properties to different nucleation schemes for immersion and condensation freezing of kaolinite in mixed-phase clouds. The five nucleation schemes cover time-dependent (stochastic) freezing of particle populations of (i) identical surface properties with a single contact angle (1θ), (ii) an external mixture of surface properties (θPDF); a distribution of contact angles of particle surfaces of (iii) internally mixed (soccer (int)) and (iv) externally mixed particles (soccer (ext)) and (v) a time-independent, singular freezing behavior (deterministic scheme).

A box model was applied in order to mimic laboratory experiments that were previously used to derive parameters for the different nucleation schemes (L    nd et al., 2010). This provides realism to the parameter choices for the subsequent modeling exercises. Sensitivity studies show that the frozen IN fractions from the different schemes that are very similar over short time scales diverge significantly for extended time

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scales, as well as for different conditions such as IN diameter, supersaturation and temperature.

The schemes were implemented into a parcel model that takes into account detailed microphysical feedbacks of droplet and ice particle growth on supersaturation. During the early stages of cloud evolution, frozen particles are formed by condensation freezing at (water) subsaturated conditions. When the supersaturation in the cloud exceeds the critical value for droplet formation, freezing occurs through the immersion mode. At high updraft velocities, the high supersaturation allows nearly all IN to nucleate ice, with only weak dependence on their θ distributions. In updraft regimes where the maximum supersaturation reaches values near the onset supersaturation and temperatures of freezing for individual particles, the choice of the nucleation scheme leads to the greatest differences in predicted N_{ice} . The deterministic approach only depends on temperature and is independent of supersaturation and thus N_{ice} is not regulated by feedbacks of N_{ice} and LWC on supersaturation leading to the highest N_{ice} in supersaturation-limited scenarios. The sensitive relationship between ice and supersaturation tends to initiate the Bergeron-Findeisen-Process in low updraft regimes. Depending on the choice of the nucleation scheme, the demise of the liquid phase will be initiated at different times/heights in a cloud since nucleation events occur over different temperature ranges.

At higher temperatures, differences in the temperature range of nucleation events not only translate into different temporal N_{ice} profiles but also into different initial particle shapes (inherent growth ratios). Exploratory simulations show that such differences in initial particle geometry as predicted by the 1θ or deterministic scheme, respectively, can translate into different growth rates that can lead to either amplification or reduction in predicted differences in IWC.

Finally, parcel model simulations that consider a polydisperse IN population show that the different parameterizations of θ distributions and time-dependencies are highly sensitive to IN size and lead to great differences in predicted ice number concentrations between the different schemes. The analysis of parameters that characterize the ice

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size distributions, i.e. the mean and integral capacitances, show that the differences in the latter are mostly determined by differences in ice number concentration and less by the spread in ice particle sizes in the resulting size distributions. The IWC tends to scale with N_{ice} , so that ice particle sizes are very similar from one scheme to the other. As long as the water phase exists, condensation is the primary loss term for supersaturation. Under these conditions, and at the low ambient N_{ice} , ice particles grow by diffusion without competition from other particles.

The absence of a dynamical framework, collection, and sedimentation in the current study makes it difficult to assess just how much impact these schemes would have on cloud ice. Some insight can be obtained from Kulkarni et al. (2012), who used a two-dimensional, cloud-resolving model to show that differences in N_{ice} as predicted from the 1θ and the θ PDF scheme result in significant differences in IWC, depending on the choice of parameters. It is therefore likely that the additional schemes tested here will have significant influence.

In summary, the large differences in predicted ice number concentrations and related parameters from the five nucleation schemes reveal that the consistency in predicted frozen IN fraction suggested by recent laboratory experiments is restricted to a very narrow range of conditions. The extrapolation of these schemes to a wide range of atmospherically-relevant conditions can lead to great discrepancies in predicted cloud-relevant parameters if the cloud covers conditions where ice nucleation is sensitive to surface properties (contact angle distributions). Our sensitivity studies show the urgent need for better constraints of the physicochemical properties that determine the freezing behavior of IN. Laboratory experiments should be designed to refine the appropriateness of different nucleation schemes for various aerosol types and conditions.

Acknowledgements. The authors acknowledge support from NOAA's Climate Goal.

References

- Archuleta, C. M., DeMott, P. J., and Kreidenweis, S. M.: Ice nucleation by surrogates for atmospheric mineral dust and mineral dust/sulfate particles at cirrus temperatures, *Atmos. Chem. Phys.*, 5, 2617–2634, doi:10.5194/acp-5-2617-2005, 2005.
- 5 Avramov, A. and Harrington, J. Y.: Influence of parameterized ice habit on simulated mixed phase Arctic clouds, *J. Geophys. Res.*, 115, D03205, doi:10.1029/2009jd012108, 2010.
- Barahona, D.: On the ice nucleation spectrum, *Atmos. Chem. Phys. Discuss.*, 11, 29601–29646, doi:10.5194/acpd-11-29601-2011, 2011.
- Broadley, S. L., Murray, B. J., Herbert, R. J., Atkinson, J. D., Dobbie, S., Malkin, T. L.,
10 Condliffe, E., and Neve, L.: Immersion mode heterogeneous ice nucleation by an illite rich powder representative of atmospheric mineral dust, *Atmos. Chem. Phys.*, 12, 287–307, doi:10.5194/acp-12-287-2012, 2012.
- Bryant, G. W., Hallett, J., and Mason, B. J.: The epitaxial growth of ice on single-crystalline substrates, *J. Phys. Chem. Solids*, 12, 189–195, 1959.
- 15 Chen, J.-P. and Lamb, D.: The theoretical basis for the parameterization of ice crystal habits: Growth by vapor deposition, *J. Atmos. Sci.*, 51, 1206–1221, 1994.
- Chen, J.-P., Hazra, A., and Levin, Z.: Parameterizing ice nucleation rates using contact angle and activation energy derived from laboratory data, *Atmos. Chem. Phys.*, 8, 7431–7449, doi:10.5194/acp-8-7431-2008, 2008.
- 20 Christner, B. C., Morris, C. E., Foreman, C. M., Cai, R., and Sandis, D. C.: Ubiquity of biological ice nucleators in snowfall, *Science*, 319, 1214, doi:10.1126/science.1149757, 2008.
- Cotton, R. J. and Field, P. R.: Ice nucleation characteristics of an isolated wave cloud, *Q. J. Roy. Meteorol. Soc.*, 128, 2417–2437, 2002.
- Cotton, W. R., Tripoli, G. J., Rauber, R. M., and Mulvihill, E. A.: Numerical Simulation
25 of the Effects of Varying Ice Crystal Nucleation Rates and Aggregation Processes on Orographic Snowfall, *J. Clim. Appl. Meteorol.*, 25, 11, 1658–1680, doi:10.1175/1520-0450(1986)025<1658:NSOTEO>2.0.CO;2, 1986.
- Crawford, I., Bower, K. N., Choularton, T. W., Dearden, C., Crosier, J., Westbrook, C., Capes, G., Coe, H., Connolly, P., Dorsey, J. R., Gallagher, M. W., Williams, P., Trembath, J., Cui, Z., and
30 Blyth, A.: Ice formation and development in aged, wintertime cumulus over the UK: observations and modelling, *Atmos. Chem. Phys. Discuss.*, 11, 30797–30851, doi:10.5194/acpd-11-30797-2011, 2011.

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Crosier, J., Bower, K. N., Choularton, T. W., Westbrook, C. D., Connolly, P. J., Cui, Z. Q., Crawford, I. P., Capes, G. L., Coe, H., Dorsey, J. R., Williams, P. I., Illingworth, A. J., Gallagher, M. W., and Blyth, A. M.: Observations of ice multiplication in a weakly convective cell embedded in supercooled mid-level stratus, *Atmos. Chem. Phys.*, 11, 257–273, doi:10.5194/acp-11-257-2011, 2011.

Curry, J.: Interactions among aerosols, clouds, and climate of the Arctic Ocean, *Sci. Total Environ.*, 160/161, 777–791, 1995.

Curry, J. A. and Khvorostyanov, V. I.: Assessment of some parameterizations of heterogeneous ice nucleation in cloud and climate models, *Atmos. Chem. Phys.*, 12, 1151–1172, doi:10.5194/acp-12-1151-2012, 2012.

de Boer, G., Hashino, T., and Tripoli, G. J.: Ice nucleation through immersion freezing in mixed-phase stratiform clouds: Theory and numerical simulations, *Atmos. Res.*, 96, 315–324, 2010.

DeMott, P. J., Prenni, A. J., Liu, X., Kreidenweis, S. M., Petters, M. D., Twohy, C. H., Richardson, M. S., Eidhammer, T., and Rogers, D. C.: Predicting global atmospheric ice nuclei distributions and their impacts on climate, *P. Natl. Acad. Sci.*, 107, 11217–11222, doi:10.1073/pnas.0910818107, 2010.

DeMott, P. J., Sassen, K., Poellot, M. R., Baumgardner, D., Rogers, D. C., Brooks, S. D., Prenni, A. J., and Kreidenweis, S. M.: African dust aerosols as atmospheric ice nuclei, *Geophys. Res. Lett.*, 30, 1732, doi:10.1029/2003GL017410, 2003.

Eidhammer, T., DeMott, P. J., and Kreidenweis, S. M.: A comparison of heterogeneous ice nucleation parameterizations using a parcel model framework, *J. Geophys. Res.*, 114, D06202, doi:10.1029/2008JD011095, 2009.

Eidhammer, T., DeMott, P. J., Prenni, A. J., Petters, M. D., Twohy, C. H., Rogers, D. C., Stith, J., Heymsfield, A., Wang, Z., Pratt, K. A., Prather, K. A., Murphy, S. M., Seinfeld, J. H., Subramanian, R., and Kreidenweis, S. M.: Ice Initiation by Aerosol Particles: Measured and Predicted Ice Nuclei Concentrations versus Measured Ice Crystal Concentrations in an Orographic Wave Cloud, *J. Atmos. Sci.*, 67, 2417–2436, doi:10.1175/2010JAS3266.1, 2010.

Ervens, B., Feingold, G., Sulia, K., and Harrington, J.: The impact of microphysical parameters, ice nucleation mode, and habit growth on the ice/liquid partitioning in mixed-phase Arctic clouds, *J. Geophys. Res.*, 116, D17205, doi:10.1029/2011jd015729, 2011.

Field, P. R., Heymsfield, A. J., Shipway, B. J., DeMott, P. J., Pratt, K. A., Rogers, D. C., Stith, J., and Prather, K. A.: Ice in Clouds Experiment – Layer Clouds. Part 2: Testing character-

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- istics of heterogeneous ice formation in lee wave clouds, *J. Atmos. Sci.*, 69, 1066–1079, doi:10.1175/jas-d-11-026.1, 2011.
- Fletcher, N. H.: Size effects in heterogeneous nucleation, *J. Chem. Phys.*, 29, 572–576, 1958.
- Fletcher, N. H.: Active sites and ice nucleation, *J. Atmos. Sci.*, 26, 1266–1271, 1969.
- 5 Fridlind, A. M., Ackermann, A. S., McFarquhar, G., Zhang, G., Poellot, M. R., DeMott, P. J., Prenni, A. J., and Heymsfield, A. J.: Ice properties of single-layer stratocumulus clouds during the Mixed-Phase Arctic Cloud Experiment: 2. Model results, *J. Geophys. Res.*, 112, D24202, doi:10.1029/2007JD008646, 2007.
- Fukuta, N.: Experimental studies of organic ice nuclei, *J. Atmos. Sci.*, 23, 191–196, 1966.
- 10 Fukuta, N. and Schaller, R. C.: Ice Nucleation by Aerosol Particles. Theory of Condensation-Freezing Nucleation, *J. Atmos. Sci.*, 39, 648–655, doi:10.1175/1520-0469(1982)039<0648:inbapt>2.0.co;2, 1982.
- Hallett, J. and Mason, B. J.: The Influence of Temperature and Supersaturation on the Habit of Ice Crystals Grown from the Vapour, *Proceedings of the Royal Society of London. Series A, Mathematical and Physical Sciences*, 247, 1251, 440–453, 1958.
- 15 Hobbs, P. V. and Rangno, A. L.: Ice Particle Concentrations in Clouds, *J. Atmos. Sci.*, 42, 2523–2549, doi:10.1175/1520-0469(1985)042<2523:ipcic>2.0.co;2, 1985.
- Khvorostyanov, V. I. and Curry, J. A.: A new theory of heterogeneous ice nucleation for application on cloud and climate models, *Geophys. Res. Lett.*, 27, 4081–4084, 2000.
- 20 Khvorostyanov, V. I. and Curry, J. A.: The theory of ice nucleation by heterogeneous freezing of deliquescent mixed CCN: Part I: Critical radius, energy, and nucleation rate, *J. Atmos. Sci.*, 61, 2676–2691, 2004.
- Korolev, A. and Isaac, G.: Phase transformation in mixed phase clouds, *Q. J. Roy. Meteorol. Soc.*, 129, 19–38, 2003.
- 25 Kulkarni, G. and Dobbie, S.: Ice nucleation properties of mineral dust particles: determination of onset RH_i, IN active fraction, nucleation time-lag, and the effect of active sites on contact angles, *Atmos. Chem. Phys.*, 10, 95–105, doi:10.5194/acp-10-95-2010, 2010.
- Kulkarni, G., Fan, J., Comstock, J. M., Liu, X., and Ovchinnikov, M.: Laboratory measurements and model sensitivity studies of dust deposition ice nucleation, *Atmos. Chem. Phys. Discuss.*, 12, 2483–2516, doi:10.5194/acpd-12-2483-2012, 2012.
- 30 Kumai, M.: Electron microscope study of snow-crystal nuclei, *Journal of Meteorology*, 8, 151–156, doi:10.1175/1520-0469(1951)008<0151:emsosc>2.0.co;2, 1951.

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- Lamb, D. and Verlinde, H.: Physics and Chemistry of Clouds, 1st ed., University Press, Cambridge, 584 pp., 2011.
- Lance, S., Shupe, M. D., Feingold, G., Brock, C. A., Cozic, J., Holloway, J. S., Moore, R. H., Nenes, A., Schwarz, J. P., Spackman, J. R., Froyd, K. D., Murphy, D. M., Brioude, J., Cooper, O. R., Stohl, A., and Burkhardt, J. F.: Cloud condensation nuclei as a modulator of ice processes in Arctic mixed-phase clouds, *Atmos. Chem. Phys.*, 11, 8003–8015, doi:10.5194/acp-11-8003-2011, 2011.
- Lüönd, F., Stetzer, O., Welti, A., and Lohmann, U.: Experimental study on the ice nucleation ability of size-selected kaolinite particles in the immersion mode, *J. Geophys. Res.*, 115, D14201, doi:10.1029/2009jd012959, 2010.
- Marcolli, C., Gedamke, S., Peter, T., and Zobrist, B.: Efficiency of immersion mode ice nucleation on surrogates of mineral dust, *Atmos. Chem. Phys.*, 7, 5081–5091, doi:10.5194/acp-7-5081-2007, 2007.
- Mason, B. J.: The growth of ice crystals in a supercooled water cloud, *Q. J. Roy. Meteorol. Soc.*, 79, 441–441, doi:10.1002/qj.49707934121, 1953.
- McDonald, J. E.: Use of the electrostatic analogy in studies of ice crystal growth, *Z. Angew. Math. Phys.*, 14, 610–619, 1963.
- Meyers, M., DeMott, P. J., and Cotton, W. R.: New primary ice-nucleation parameterizations in an explicit cloud model, *J. Appl. Meteorol.*, 31, 708–720, 1992.
- Möhler, O., Field, P. R., Connolly, P., Benz, S., Saathoff, H., Schnaiter, M., Wagner, R., Cotton, R., Krämer, M., Mangold, A., and Heymsfield, A. J.: Efficiency of the deposition mode ice nucleation on mineral dust particles, *Atmos. Chem. Phys.*, 6, 3007–3021, doi:10.5194/acp-6-3007-2006, 2006.
- Morrison, H., de Boer, G., Feingold, G., Harrington, J., Shupe, M. D., and Sulia, K.: Resilience of persistent Arctic mixed-phase clouds, *Nature Geosci.*, 5, 11–17, 2012.
- Morrison, H., Pinto, J. O., Curry, J. A., and McFarquhar, G. M.: Sensitivity of modeled Arctic mixed-phase stratocumulus to cloud condensation and ice nuclei over regionally varying surface conditions, *J. Geophys. Res.*, 113, D05203, doi:10.1029/2007JD008729, 2008.
- Murray, B. J., Broadley, S. L., Wilson, T. W., Atkinson, J. D., and Wills, R. H.: Heterogeneous freezing of water droplets containing kaolinite particles, *Atmos. Chem. Phys.*, 11, 4191–4207, doi:10.5194/acp-11-4191-2011, 2011.
- Niedermeier, D., Hartmann, S., Shaw, R. A., Covert, D., Mentel, T. F., Schneider, J., Poulain, L., Reitz, P., Spindler, C., Clauss, T., Kiselev, A., Hallbauer, E., Wex, H., Mildenerger,

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- K., and Stratmann, F.: Heterogeneous freezing of droplets with immersed mineral dust particles – measurements and parameterization, *Atmos. Chem. Phys.*, 10, 3601–3614, doi:10.5194/acp-10-3601-2010, 2010.
- 5 Niedermeier, D., Shaw, R. A., Hartmann, S., Wex, H., Clauss, T., Voigtländer, J., and Stratmann, F.: Heterogeneous ice nucleation: exploring the transition from stochastic to singular freezing behavior, *Atmos. Chem. Phys.*, 11, 8767–8775, doi:10.5194/acp-11-8767-2011, 2011.
- Phillips, V. T. J., DeMott, P. J., and Andronache, C.: An empirical parameterization of heterogeneous ice nucleation for multiple chemical species of aerosol, *J. Atmos. Sci.*, 65, 2757–2783, 2008.
- 10 Pruppacher, H. R. and Klett, J. D.: *Microphysics of clouds and precipitation*, 2nd revised and enlarged ed., Atmospheric and oceanographic science library, Kluwer Academics Publisher, Dordrecht (NL), 954 pp., 2003.
- Roberts, P. and Hallett, J.: A laboratory study of the ice nucleating properties of some mineral particulates, *Q. J. Roy. Meteorol. Soc.*, 94, 25–34, doi:10.1002/qj.49709439904, 1968.
- 15 Schnell, R. C. and Vali, G.: Biogenic ice nuclei: Part I. Terrestrial and marine sources, *J. Atmos. Sci.*, 33, 1554–1564, 1976.
- Solomon, S., Qin, D., Manning, M., Chen, Z., Marquis, M., Averyt, K. B., Tignor, M., and Miller, H. L.: *Climate Change 2007 – The Physical Science Basis*, Contribution of Working Group I to the Fourth Assessment Report of the IPCC, Intergovernmental Panel on Climate Change, Cambridge, United Kingdom and New York, NY, USA, 2007.
- 20 Sulia, K. J. and Harrington, J. Y.: Ice aspect ratio influences on mixed-phase clouds: Impacts on phase partitioning in parcel models, *J. Geophys. Res.*, 116, D21309, doi:10.1029/2011jd016298, 2011.
- Takahashi, T., Endoh, T., Wakahama, G., and Fukuta, N.: Vapor diffusional growth of freefalling snow crystals between -3 and -23°C , *J. Meteorol. Soc. Japan*, 69, 15–30, 1991.
- 25 Vali, G.: Quantitative Evaluation of Experimental Results on the Heterogeneous Freezing Nucleation of Supercooled Liquids, *J. Atmos. Sci.*, 28, 402–409, doi:10.1175/1520-0469(1971)028<0402:QEOERA>2.0.CO;2, 1971.
- Vali, G.: Freezing rate due to heterogeneous nucleation, *J. Atmos. Sci.*, 51, 1843–1856, 1994.
- 30 Vali, G.: Repeatability and randomness in heterogeneous freezing nucleation, *Atmos. Chem. Phys.*, 8, 5017–5031, doi:10.5194/acp-8-5017-2008, 2008.
- Vali, G. and Stansbury, E. J.: Time-dependent characteristics of the heterogeneous nucleation of ice, *Can. J. Phys.*, 44, 477–502, 1966.

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Wang, B. and Knopf, D. A.: Heterogeneous ice nucleation on particles composed of humic-like substances impacted by O₃, J. Geophys. Res., 116, D03205, doi:10.1029/2010jd014964, 2011.

5 Welti, A., Lüönd, F., Stetzer, O., and Lohmann, U.: Influence of particle size on the ice nucleating ability of mineral dusts, Atmos. Chem. Phys., 9, 6705–6715, doi:10.5194/acp-9-6705-2009, 2009.

Wheeler, M. J. and Bertram, A. K.: Deposition nucleation on mineral dust particles: a case against classical nucleation theory with the assumption of a single contact angle, Atmos. Chem. Phys., 12, 1189–1201, doi:10.5194/acp-12-1189-2012, 2012.

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Table 1. Parameters to describe contact angle distributions for the different nucleation schemes as used in the box and parcel models. Note for both the box and the parcel models the same selections of contact angles were used.

Model	Number of nucleation sites/particle (n)	Number of different particles (N)	Mean θ	Standard deviation of PDF σ	$f(\theta) = b \cdot \exp\left(\frac{-b-1}{\theta-b_2}\right)^2$	$F_{fr} = f(A_1, A_2, T)$ Eq. (6)
Kaolinite ¹						
1 θ	1	1	88.8°	–	–	–
θ PDF	–	20	92°	0.089	–	–
Soccer (int)	80	1	–	–	$b = 0.010455$	–
Soccer (ext)	50	20	–	–	$b_1 = -9.647$ $b_2 = 0.0922$	–
Deterministic	1	1	–	–	–	$A_1 = 2.405 \times 10^7 \text{ cm}^{-2}$ $A_2 = 31.58^\circ\text{C}$
T1: 256.5 K > T > 253.4 K						
1 θ	1	1	52.5°	–	–	–
Deterministic	1	1	–	–	–	$A_1 = 3 \times 10^7 \text{ cm}^{-2}$ $A_2 = 16.5^\circ\text{C}$
T2: 262.5 K > T > 260.25 K						
1 θ	1	1	40°	–	–	–
Deterministic	1	1	–	–	–	$A_1 = 3 \times 10^7 \text{ cm}^{-2}$ $A_2 = 10.5^\circ\text{C}$

¹ Based on Lüönd et al. (2010). Small deviations of the listed parameters as compared to the original once were introduced in order to predict a frozen fraction of 50 % at 240 K.

² Unlike Lüönd et al. (2010), who fitted the surface density of nucleation sites [m^{-2}], our parameters directly give the probability of a contact angle θ in the θ distribution on a particle surface for both soccer ball schemes.

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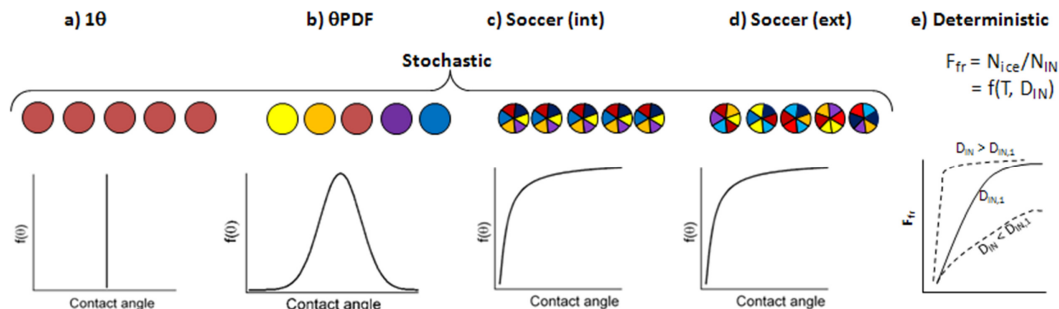


Fig. 1. Nucleation schemes that have been developed to describe freezing of kaolinite (Lüönd et al., 2010). Parameters to describe the θ distributions and temperature dependence of F_{fr} are summarized in Table 1.

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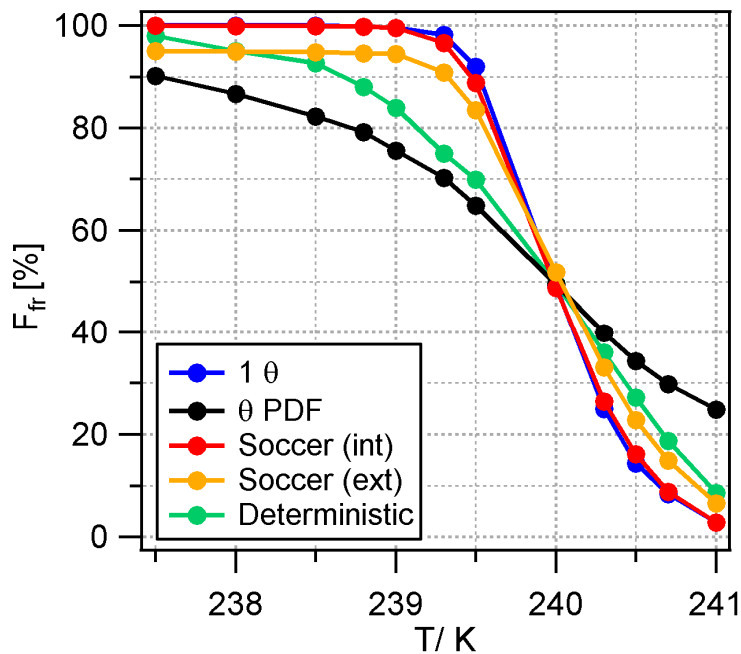


Fig. 2. Predicted frozen fraction F_{fr} as a function of temperature from box model calculations after 14 s simulation time and at $S_w = 0.2\%$.

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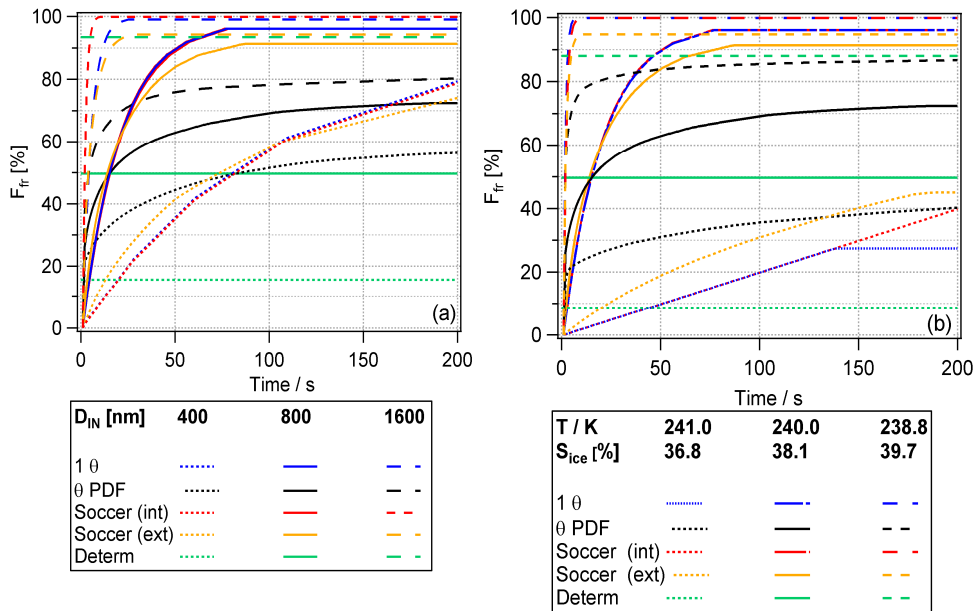


Fig. 3. Box model results for constant temperature and supersaturation. **(a)** Variation of the ice nuclei diameter D_{IN} ($T = 240$ K, $S_{ice} = 38.1$ %; $S_w = 0.2$ %); **(b)** variation of temperature and S_{ice} ($D_{IN} = 800$ nm, $S_w = 0.2$ %).

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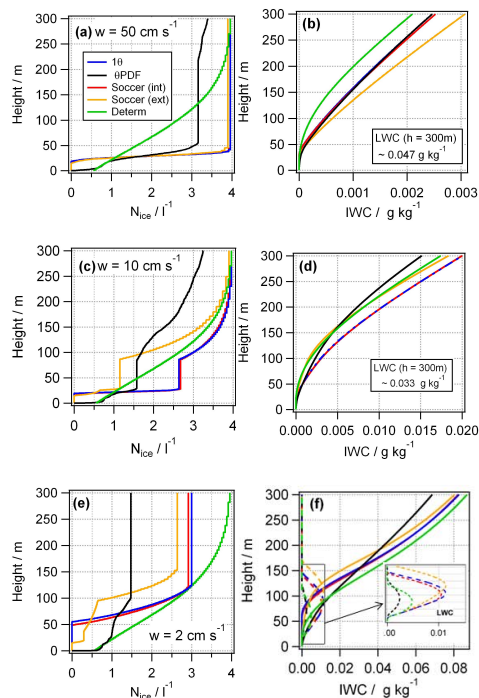


Fig. 4. Parcel model results using the five schemes as described in Fig. 1 and Table 1. **(a, c, e)** Predicted ice particle number concentration N_{ice} for three different updraft velocities ($w = 50 \text{ cm s}^{-1}$, 10 cm s^{-1} , 2 cm s^{-1}) and a cloud depth of 300 m ($238.2 \text{ K} < T < 241 \text{ K}$). **(b, d, f)** Ice water content IWC for the five nucleation schemes. The LWC in **(b, d)** is approximately the same for all schemes since the liquid phase is not significantly impacted by the ice phase. The dashed lines in **(f)** denote the liquid water content (LWC). The onset shows a zoom of the grey box.

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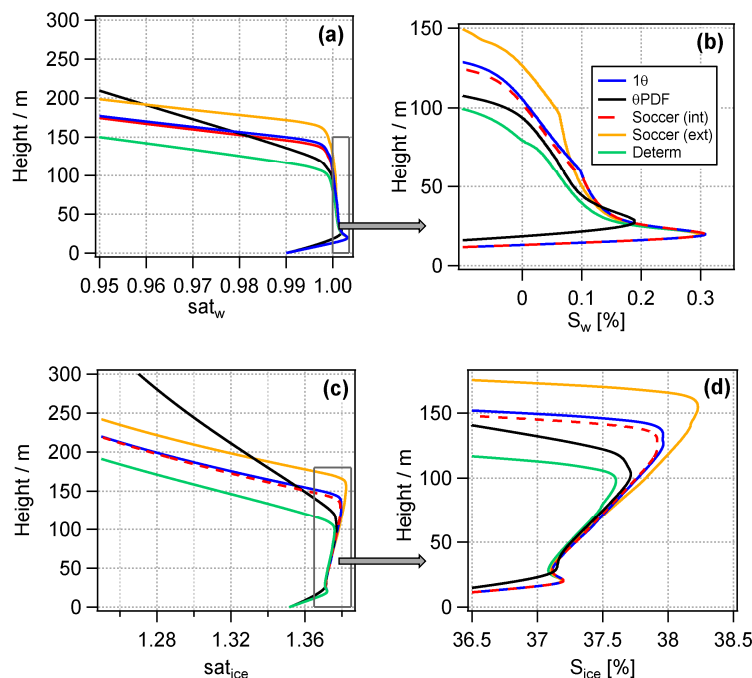


Fig. 5. Saturation sat and supersaturation S [%] with respect to (a, b) water and (c, d) ice for the simulations in Fig. 4e, f ($w = 2 \text{ cm s}^{-1}$). The grey boxes in (a, c) are enlarged in (b) and (d), respectively, in order to show details of the maximum supersaturation near cloud base where initial ice nucleation occurs.

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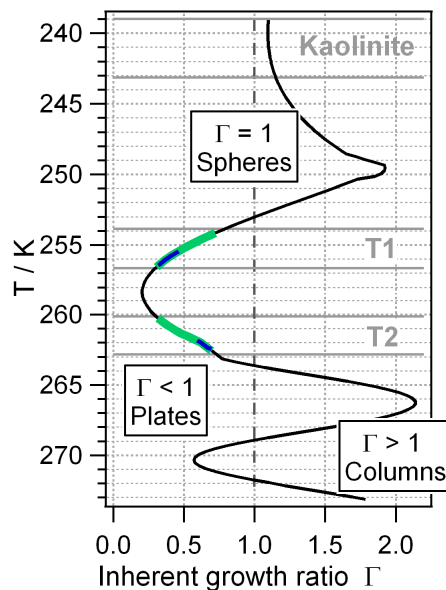
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Fig. 6. Inherent growth ratio Γ as a function of temperature (adapted from Chen and Lamb, 1994). The notation “columns, spheres, plates” refers to the shape the particle would attain if it were nucleated and grown primarily within that temperature range. The grey horizontal lines show temperature regimes for simulations where (i) IN composed of kaolinite nucleate ice and (ii) other IN are expected to nucleate ice (T1, T2). The blue and green shading within T1 and T2 marks the range where nucleation occurs if the 1θ or the deterministic schemes, is applied, respectively.

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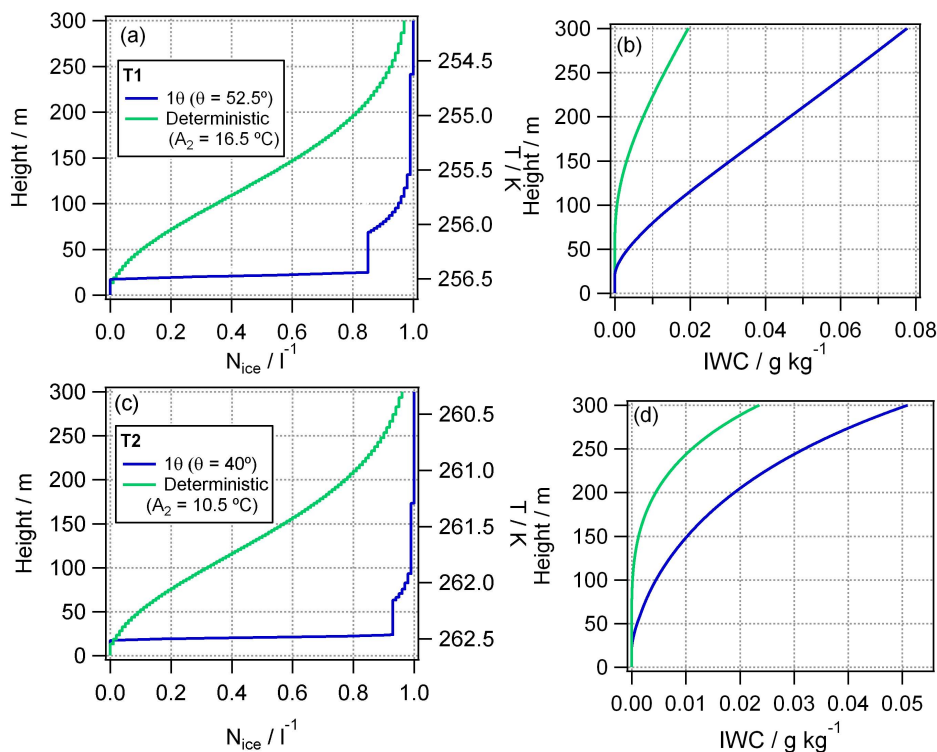


Fig. 7. Predicted number concentration of ice particles N_{ice} and ice water content IWC for heterogeneous freezing in temperature regime T1 (a, b) and T2 (c, d) as marked in Fig. 6. For the two temperature regimes, different parameter sets (θ , A_1 , A_2) were applied (Table 1).

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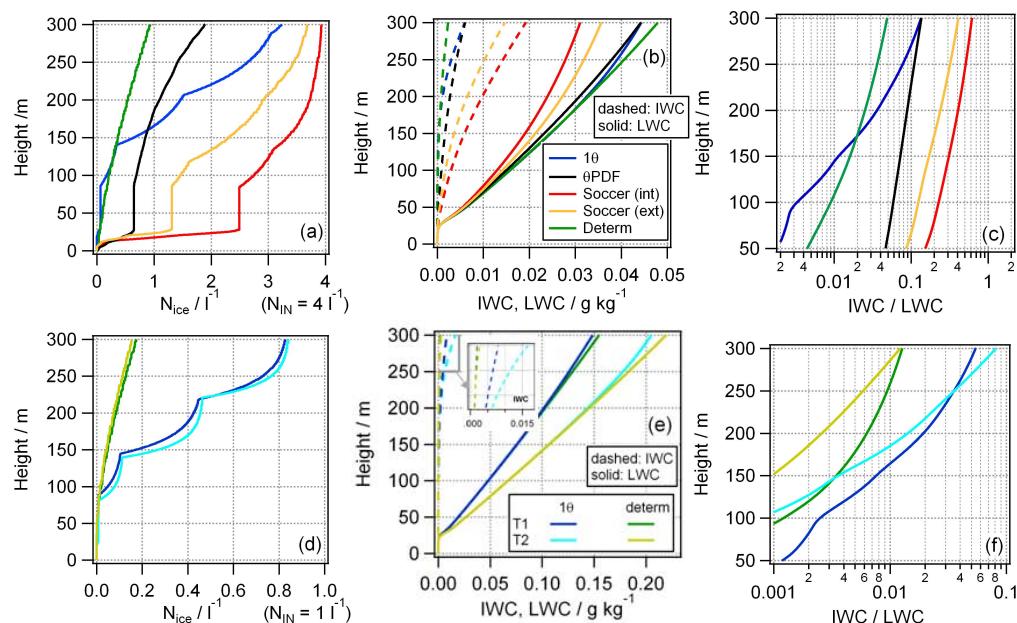


Fig. 8. Parcel model results of (a, d) N_{ice} , (b, e) IWC, LWC, and (c, f) IWC/LWC assuming a polydisperse IN size distribution. The upper panel corresponds to immersion/condensation freezing of kaolinite; the bottom panel includes results for simulations at temperature regimes T1 and T2.

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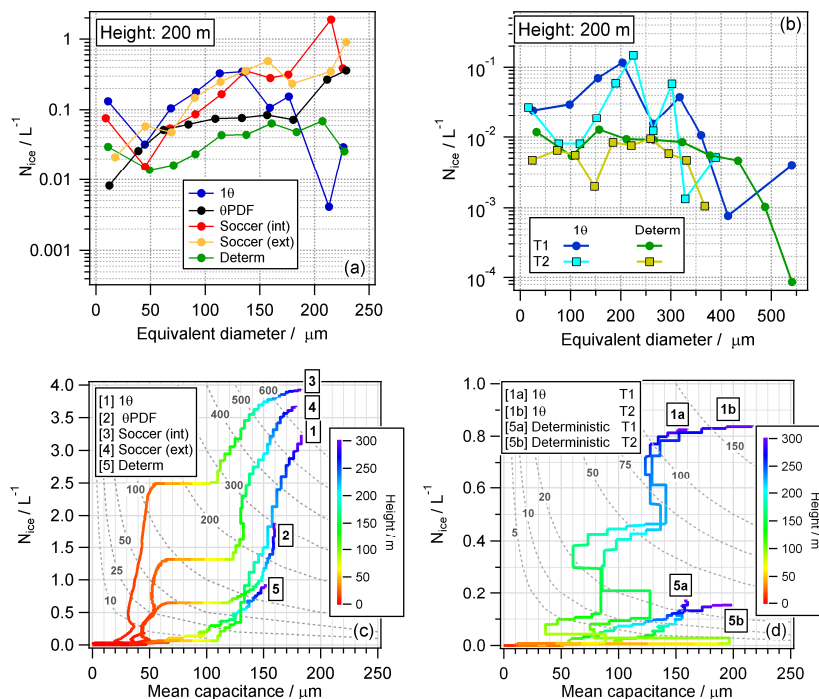
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Fig. 9. Parcel model results for polydisperse IN distributions: **(a, b)** ice size distributions ($h = 200$ m) and **(c, d)** details on mean and integral ice capacitance. Grey contours show lines of equal capacitance; numbers on the contours denote integral capacitance $N_i C_i$ [$\mu m l^{-1}$]. **(a, c)** $T \sim 243$ K (kaolinite). **(b, d)** Temperature ranges T1 and T2.

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