

Supplementary Information

Technical Note: New methodology for measuring viscosities in small volumes characteristic of environmental chamber particle samples

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Viscosity vs. RH relationships for glycerol-water solutions at 20 °C.

Viscosity vs. concentration data was taken from Sheely (1931) and Segur and Oberstar (1951) where the viscosities reported by Segur and Oberstar were corrected to the viscosity of water at 20 °C (1.002×10^{-3} Pa s) (Kestin et al., 1978; Swindells et al., 1952). The concentrations used in these experiments were converted to relative humidity using the parameterization shown in Table S1. The resulting viscosity vs. RH data was then fit to a 3rd degree polynomial. The results of the fit are shown in Table S2.

Viscosity vs. RH relationships for Glycerol-water solutions at 0 °C.

Viscosity vs. concentration data was taken from Trejo González et al. (2011). Concentrations used in these experiments were converted to RH using the parameterizations shown in Table S1. The resulting viscosity vs. RH data was then fit to a 3rd degree polynomial (see Table S2).

Viscosity vs. RH relationships for sucrose-water solutions at 20 °C.

Viscosities measured at different concentration was taken from Swindells et al. (1958), Quintas et al. (2006) and Perry and Green (2008). The concentrations used in these references were converted to RH using the parameterization of Zobrist et al. (2011). The resulting viscosity vs. RH data was fit to a 3rd degree polynomial (see Table S2).

Viscosity of olive oil samples at 20 C.

A Haake RotoVisco 550 viscometer (sensor MV-1P) was used to determine the viscosity of the same olive oil sample used in the bead mobility experiments. The resulting shear stress vs. shear rate data are shown in Fig. S2. From the slope of the line in Fig. S2, the viscosity of the solution was determined to be $0.097 (\pm 0.006)$ Pa s.

Surface tension values for glycerol-water mixtures.

For glycerol-water solutions, the concentration of glycerol at a given RH was determined using the parameterization in Table S2 and the corresponding surface tension was determined from a 3rd degree polynomial fit to the data of Ernst et al. (1936) (see Table S3).

1 **Surface tension values for other organic and organic-water mixtures.**

2 Other surface tension values used to construct Figure 7c (main text) are given Table S4. Both 25
3 °C and 20 °C surface tension data from the literature were used to construct Fig. 7c. It is assumed
4 that the surface tension does not depend strongly on temperature over 20-25 °C, a good
5 assumption for the types of compounds used herein. For example, the surface tension of pure
6 glycerol is 63.3-63.5 mN/m at 20 °C (Jańczuk et al., 1993;Panzer, 1973), and 62.5 mN/m at
7 25°C. (Ernst et al., 1936)

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1 **Table S1:** Best fit parameters for concentration vs. relative humidity data for glycerol-water
 2 mixtures. $RH = 100 + Ax + Bx^2 + Cx^3 + Dx^4 + Ex^5$ where x = mass fraction glycerol. Data used
 3 to generate this equation taken from Marcolli and Peter (2005), Ninni et al. (2000), and Chenlo et
 4 al. (2004). The corresponding R^2 from the best fit function shows the quality of the fit.

A	B	C	D	E	R^2
-15.08	-30.62	-21.12	7.406	-36.17	0.9996

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1 **Table S2:** Best fit parameters for viscosity vs. relative humidity data where $\log(\text{viscosity}) = A +$
 2 $B(\text{RH}) + C(\text{RH})^2 + D(\text{RH})^3$ and the corresponding R^2 from the best fit function shows the quality
 3 of the fit.

Aqueous solution	A	B	C	D	R^2
Glycerol, 20°C	3.407×10^{-1}	-3.778×10^{-2}	1.914×10^{-4}	-1.409×10^{-6}	0.9997
Glycerol, 0°C	1.276	-4.352×10^{-2}	1.746×10^{-4}	-1.350×10^{-6}	0.9999
Sucrose, 20°C	44.33	-1.400	1.566×10^{-2}	-6.387×10^{-5}	0.9988

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1 **Table S3:** Best fit parameters for surface tension vs. mass fraction of glycerol. The data of Ernst
 2 et al. (1936) was fit to a 3rd degree polynomial where surface tension (mN/m) = $A - Bx + Cx^2 + Dx^3$
 3 where x= mass fraction of glycerol and the corresponding R^2 from the best fit function shows the
 4 quality of the fit.

Aqueous solution	A	B	C	D	R^2
Glycerol	71.97	-15.05	12.16	16.32	0.9997

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1 **Table S4:** Surface tensions from the literature used to construct Fig. 7c in the main text.

Droplet material	Range of concentrations studied (wt% organic)	Molecular formula of the organic	Surface tension (mN/m)	References
Glycerol + Water	35 - ~100	C ₃ H ₈ O ₃	62.5-68.2	(Ernst et al., 1936)
1,2,6-hexanetriol	~100	C ₆ H ₁₄ O ₃	50	(Aldrich Chemical Company, 1996)
Tetraethylene glycol	~100	C ₈ H ₁₅ O ₅	46	(Dow Chemical Company, 2007; Moumen et al., 2006)
Oleic Acid	~100	C ₁₈ H ₃₄ O ₂	32.79	(Chumpitaz et al., 1999)
PEG-300	~100	H(OCH ₂ CH ₂) _n OH, n=6-7	34.3	(Mazandarani et al., 2007)
Sucrose	55	C ₁₂ H ₂₂ O ₁₁	76	(Docoslis et al., 2000; MacDonald et al., 1996)
PEG-400	~100	H(OCH ₂ CH ₂) _n OH, n=8-9	44.5	(Ciobanu et al., 2009; Marcolli and Krieger, 2006)
Tergitol TM NP-7	~100	C ₂₉ H ₅₂ O ₈	32 ^a	(Dow Chemical Company, 2004)

2 ^a Upper limit on the surface tension of pure Tergitol NP-7 because literature value is for 1 wt%
3 TergitolTM NP-7 in water. The critical micelle concentration is < 1 wt% (Dow Chemical
4 Company, 2004). Surface tension vs. concentration data for structurally similar TergitolTM NP-
5 10 shows a minimal decrease in surface tension at concentrations greater than the critical micelle
6 concentration (Park and Bielefeldt, 2003) so surface tension of ~100 wt% TergitolTM NP-7 used
7 herein is likely close to the value reported here.

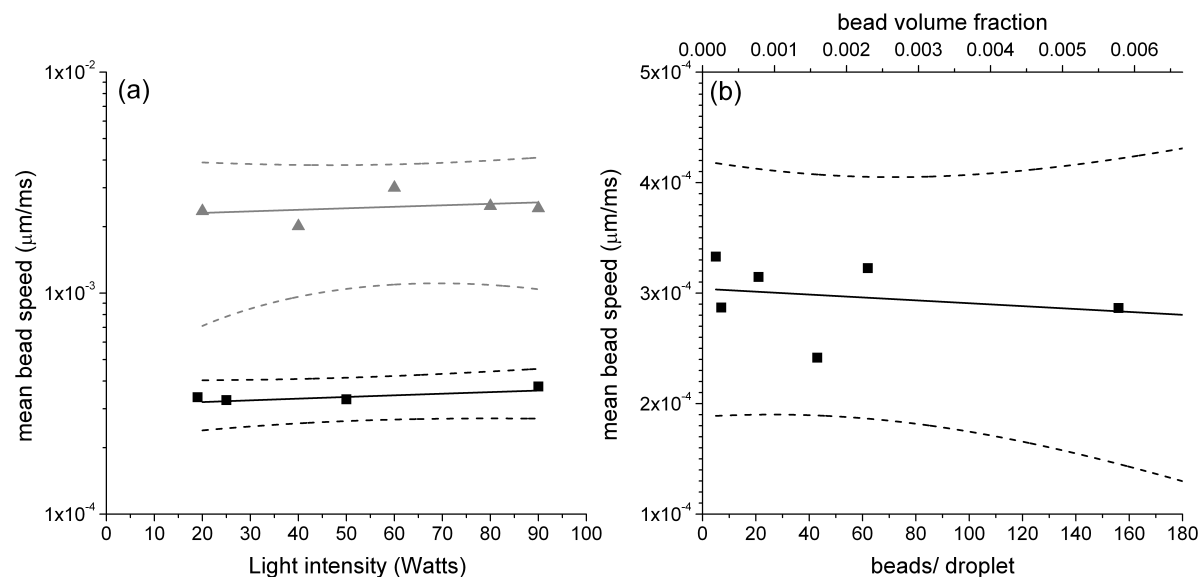


Figure S1: a) Mean melamine bead speed vs. light intensity of halogen light source on microscope in droplets composed of ~100 wt% glycerol (black squares) and ~100 wt% olive oil (grey triangles) at room temperature, b) Mean melamine bead speed vs. number of beads/droplet or bead volume fraction in droplets composed of ~100 wt% glycerol. In (a) and (b), the solid lines represent the best fit functions and the dashed lines represent the upper and lower 95% prediction intervals.

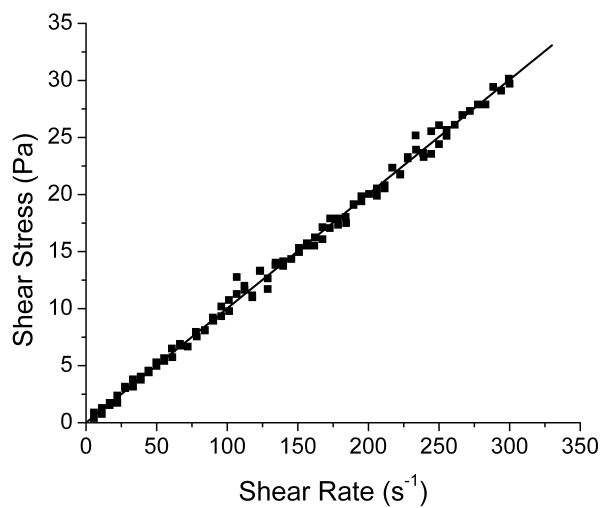


Figure S2. Shear stress v. shear rate data obtained with the Haake RotoVisco 550 viscometer using the virgin olive oil that was used in the bead mobility experiments. The slope of the best fit line (0.097 ± 0.006 Pa s) gives the measured viscosity.

1 **Movies**

2 **Movie S1:** Sample movie showing beads moving through a droplet matrix. The droplet shown
3 here is an aqueous glycerol droplet at 85% RH. The first three frames correspond to Figs. 3 a-c
4 in the main text. Frame rate = 5 frames/second and frame interval = 200 ms. (real time). The
5 white rings around the perimeter of the droplet are due to light diffraction and are an
6 experimental artifact.

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1 **References**

- 2 Aldrich Chemical Company: 1,2,6-hexanetriol technical bulletin AL-128, Available at:
3 [http://www.sigmaaldrich.com/etc/medialib/docs/Aldrich/Bulletin/al_techbull_al128.Par.0001.File.tmp/](http://www.sigmaaldrich.com/etc/medialib/docs/Aldrich/Bulletin/al_techbull_al128.Par.0001.File.tmp/al_techbull_al0128.pdf)
4 [al_techbull_al0128.pdf](http://www.sigmaaldrich.com/etc/medialib/docs/Aldrich/Bulletin/al_techbull_al128.Par.0001.File.tmp/al_techbull_al0128.pdf), 1996.
- 5 Chenlo, F., Moreira, R., Pereira, G., and Bello, B.: Kinematic viscosity and water activity of
6 aqueous solutions of glycerol and sodium chloride, *Eur. Food Res. Technol.*, 219, 403-408,
7 10.1007/s00217-004-0974-6, 2004.
- 8 Chumpitaz, L. D. A., Coutinho, L. F., and Meirelles, A. J. A.: Surface Tension of Fatty Acids
9 and Triglycerides, *J. Am. Oil Chem. Soc.*, 76, 379-382, 10.1007/BF02898125, 1999.
- 10 Ciobanu, V. G., Marcolli, C., Krieger, U. K., Weers, U., and Peter, T.: Liquid-liquid phase
11 separation in mixed organic/inorganic aerosol particles., *J. Phys. Chem. A*, 113, 10966-10978,
12 10.1021/jp905054d, 2009.
- 13 Docoslis, A., Giese, R. F., and Van Oss, C. J.: Influence of the water-air interface on the
14 apparent surface tension of aqueous solutions of hydrophilic solutes, *Colloids Surf., B*, 19, 147-
15 162, 10.1016/S0927-7765(00)00137-5, 2000.
- 16 Dow Chemical Company: Tergitol NP-7 Surfactant Technical Data Sheet, Available at:
17 [http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_00ae/0901b803800ae803909.pdf?filepath=](http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_00ae/0901b803800ae803909.pdf?filepath=surfactants/pdfs/noreg/803119-801915.pdf&fromPage=GetDoc)
18 [th=surfactants/pdfs/noreg/803119-801915.pdf&fromPage=GetDoc](http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_00ae/0901b803800ae803909.pdf?filepath=surfactants/pdfs/noreg/803119-801915.pdf&fromPage=GetDoc) 2004.
- 19 Dow Chemical Company: Tetraethylene Glycol Application Note, Available at:
20 [http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_007e/0901b8038007e8038005a803800](http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_007e/0901b8038007e8038005a8038005.pdf?filepath=ethyleneglycol/pdfs/noreg/8038612-8000005.pdf&fromPage=GetDoc)
21 [5.pdf?filepath=ethyleneglycol/pdfs/noreg/8038612-8000005.pdf&fromPage=GetDoc](http://msdssearch.dow.com/PublishedLiteratureDOWCOM/dh_007e/0901b8038007e8038005a8038005.pdf?filepath=ethyleneglycol/pdfs/noreg/8038612-8000005.pdf&fromPage=GetDoc), 2007.
- 22 Ernst, R. C., Watkins, C. H., and Ruwe, H. H.: The physical properties of the ternary system
23 ethyl-alcohol-glycerin-water, *J. Phys. Chem.*, 40, 627-635, 10.1021/j150374a008, 1936.
- 24 Jańczuk, B., Wójcik, W., and Zdziennicka, A.: Determination of the components of the surface
25 tension of some liquids from interfacial liquid-liquid tension measurements, *J. Colloid Interface*
26 *Sci.*, 157, 384, 10.1006/jcis.1993.1200, 1993.
- 27 Kestin, J., Sokolov, M., and Wakeham, W. A.: Viscosity of liquid water in the range -8°C to
28 150°C , *J. Phys. Chem. Ref. Data*, 7, 941-949, 10.1063/1.555581 1978.
- 29 MacDonald, G. A., Lanier, T. C., Swaisgood, H. E., and Hamann, D. D.: Mechanism for
30 Stabilization of Fish Actomyosin by Sodium Lactate, *J. Agric. Food. Chem.*, 44, 106-112,
31 10.1021/jf940698y, 1996.
- 32 Marcolli, C., and Peter, T.: Water activity in polyol/water systems: new UNIFAC
33 parameterization, *Atmos. Chem. Phys. Discuss.*, 5, 1501-1527, 10.5194/acpd-5-1501-2005,
34 2005.

- 1 Marcolli, C., and Krieger, U. K.: Phase changes during hygroscopic cycles of mixed
2 organic/inorganic model systems of tropospheric aerosols., J. Phys. Chem. A, 110, 1881-1893,
3 10.1021/jp0556759, 2006.
- 4 Mazandarani, M. T., Eliassi, A., and Fazlollahnejad, M.: Experimental data and correlation of
5 surface tension of binary polymer solutions at different temperatures and atmospheric pressure,
6 European Congress of Chemical Engineering, Copenhagen, 2007,
- 7 Moumen, N., Subramanian, R. S., and McLaughlin, J. B.: Experiments on the motion of drops on
8 a horizontal solid surface due to a wettability gradient, Langmuir, 22, 2682-2690,
9 10.1021/la053060x, 2006.
- 10 Ninni, L., Camargo, M., and Meirelles, A. J. A.: Water activity in polyol systems, J. Chem. Eng.
11 Data, 45, 654-660, 10.1021/je990303c, 2000.
- 12 Panzer, J.: Components of solid surface free energy from wetting measurements, J. Colloid
13 Interface Sci., 44, 142-161, 10.1006/jcis.1993.1344, 1973.
- 14 Park, S.-K., and Bielefeldt, A. R.: Equilibrium partitioning of a non-ionic surfactant and
15 pentachlorophenol between water and a non-aqueous phase liquid, Water Res., 37, 3412-3420,
16 10.1016/S0043-1354(03)00237-9, 2003.
- 17 Perry, R. H., and Green, D. W.: Perry's Chemical Engineers' Handbook, McGrawHill, 2400,
18 10.1036/0071511334, 2008.
- 19 Quintas, M., Brandão, T. R. S., Silva, C. L. M., and Cunha, R. L.: Rheology of supersaturated
20 sucrose solutions, J. Food Eng., 77, 844-852, 10.1016/j.jfoodeng.2005.08.011, 2006.
- 21 Segur, J. B., and Oberstar, H. E.: Viscosity of glycerol and its aqueous solutions, Ind. Eng.
22 Chem., 43, 2117-2120, 10.1021/ie50501a040, 1951.
- 23 Sheely, M. L.: Glycerol Viscosity Tables, Ind. Eng. Chem., 24, 1060-1064,
24 10.1021/ie50273a022, 1931.
- 25 Swindells, J. F., Coe Jr, J. R., and Godfrey, T. B.: Absolute Viscosity of Water at 20° C, J. Res.
26 Nat. Bur. Stand., 48, 1-31, 1952.
- 27 Swindells, J. F., Snyder, C. F., Hardy, R. C., and Golden, P. E.: Viscosities of Sucrose Solutions
28 at Various Temperatures: Tables of Recalculated Values- Supplement to National Bureau of
29 Standards Circular 440, Supplement to National Bureau of Standards Circular 440, United States
30 Department of Commerce and National Bureau of Standards, Washington, DC, 1958.
- 31 Trejo González, J. A., Longinotti, M. P., and Corti, H. R.: The Viscosity of Glycerol-Water
32 Mixtures Including the Supercooled Region, J. Chem. Eng. Data, 56, 1397-1406,
33 10.1021/je101164q, 2011.

1 Zobrist, B., Soonsin, V., Luo, B. P., Krieger, U. K., Marcolli, C., Peter, T., and Koop, T.: Ultra-
2 slow water diffusion in aqueous sucrose glasses., *Phys. Chem. Chem. Phys.*, 13, 3514-3526,
3 10.1039/c0cp01273d, 2011.

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