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Measurements of the timescales for the mass transfer of water in glassy aerosol at low relative humidity and ambient temperature

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Abstract

The influence of glassy states and highly viscous solution phases on the timescale of aerosol particle equilibration with water vapour is examined. In particular, the kinetics of mass transfer of water between the condensed and gas phases has been studied for sucrose solution droplets under conditions above and below the glass transition relative humidity (RH). At RHs above the glass transition, sucrose droplets are shown to equilibrate on a timescale comparable to the change in environmental conditions. Below the glass transition, the timescale for mass transfer is shown to be extremely slow, with particles remaining in a state of disequilibrium even after timescales of more than 10 000 s. A phenomenological approach for quantifying the time response of particle airs is used to illustrate the influence of the glassy transition at the kinetics.

- ticle size is used to illustrate the influence of the glassy aerosol state on the kinetics of mass transfer of water: the time is estimated for the droplet to reach the halfway point from an initial state towards a disequilibrium state at which the rate of size change decreases below 1 nm every 10 000 s. This half-time increases above 1000 s once the
- particle can be assumed to have formed a glass. The measurements are shown to be consistent with kinetic simulations of the slow diffusion of water within the particle bulk. Similar behaviour is observed for binary aqueous raffinose solution droplets consistent with the influence of a glass transition on mass transfer. Mixed component droplets of sucrose/sodium chloride/water also show slow equilibration at low RH, illustrating the importance of understanding the role of the bulk colution viscosity on the rate of measurements.
- ²⁰ importance of understanding the role of the bulk solution viscosity on the rate of mass transfer with the gas phase, even under conditions that may not lead to the formation of a glass.

1 Introduction

Aerosol particles affect the climate directly by absorbing and scattering radiation (Haywood and Boucher 2000; Yu et al., 2006) and indirectly by acting as cloud condensation nuclei (CCN) or ice nuclei (IN) (Lohmann and Feichter, 2005; Pósfai and Buseck,



2010). They also influence the chemical composition of the atmosphere by acting as sites for heterogeneous chemical reactions (Ravishankara et al., 1997; De Haan et al., 1999). Understanding the dynamic response of aerosols to changes in environmental conditions, such as temperature and relative humidity (RH), is crucial for interpreting

the physical and chemical properties of aerosols, including particle phase, hygroscopicity and the partitioning of semi-volatile organic components between the gas and condensed phase (Martin, 2000; Zobrist et al., 2008; Huffman et al., 2009; Pope et al., 2010a, b), and for predicting optical properties (Zieger et al., 2010).

The prompt dissolution of crystalline aerosol into the solution phase at the deliquescence RH (DRH) is well-characterised for the dominant inorganic aerosol components found in the atmosphere (Henzler et al., 1993; Tang and Munkelwitz, 1993; Shindo et al., 1997; Dai and Salmeron, 1997; Martin, 2000; Wise et al., 2008). The hysteresis behaviour observed in the mass of condensed phase water on reduction of RH below the deliquescence point is also well established, with a metastable supersat-

- ¹⁵ urated solution droplet existing until the efflorescence RH is reached (Martin, 2000; McGraw and Lewis, 2009; Pósfai and Buseck, 2010). With the organic mass fraction of aerosol often representing more than 50% of the aerosol mass (Reinhardt et al., 2007), the thermodynamic properties of mixed component inorganic/organic aerosol have become a focus for research. The phase behaviour of mixed component aerosol can be
- highly complex, with changes in the DRH of the inorganic component (Badger et al., 2006; Cruz and Pandis, 2000), the phase separation of hydrophobic and hydrophilic domains (Ciobanu et al., 2009), the RH dependent restructuring of particle morphology (Kwamena et al., 2010), and the influence of porosity on the DRH (Mikhailov et al., 2009).
- Recently, it has become evident that identifying the formation of metastable amorphous states rather than crystalline phases is crucial for interpreting many measurements of aerosol properties and processes (Virtanen et al., 2010). The formation of glasses, gels, rubbers or highly viscous liquids on drying or cooling is expected to lead to amorphous aerosol (i.e. with no long range molecular order) which may show kinetic



limitations when responding to changes in environmental conditions. Numerous inorganic aerosol components (Hoffman et al., 2004; Liu et al., 2008; Zhang et al., 2004; Wang et al., 2005; Tang and Fung, 1997) have been observed to form amorphous phases that do not exhibit prompt deliquescence or efflorescence, and many organic

- ⁵ aerosol components are observed to take up or lose water continuously with change in RH, without exhibiting discrete phase transitions (Chan et al., 2005; Prenni et al., 2001; Peng et al., 2001; Mikhailov et al., 2009; Zardini et al., 2008; Lightstone et al., 2000). The low diffusivity of water within an amorphous phase may lead to non-ergodic behaviour, influencing the rate of hygroscopic growth and the activation of CCN or IN, with
- the equilibration in size or composition of the aerosol particle occurring on a timescale that is longer than the timescale for the change in environmental conditions. The suppression of ice nucleation in ultra viscous emulsified micron size droplets (Zobrist et al., 2008; Murray et al., 2008) and the slow response to changes in RH for aqueous citric acid-ammonium sulphate droplets (Bodsworth et al., 2010) at low temperature are examples of non-ergodic behaviour. Further, it has been suggested that the high vis-
- cosity of amorphous aerosol may inhibit the progress of heterogeneous reactive aging (Mikhailov et al., 2009).

Glasses have found widespread application in numerous areas, including food preservation (Le Meste et al., 2002), drug delivery (Rabinowitz et al., 2006) and the materials industry (Binder and Kob, 2005). A glass is a disordered amorphous solid, lacking long range order. Glasses are normally derived by cooling the liquids to below

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a certain temperature (glass transition temperature, T_g) or by drying an aqueous solution without crystallization taking place (glass transition relative humidity RH_g) (Angell, 1995; Debenedetti and Stillinger, 2001). As the liquid approaches the glass transition,

the increase in viscosity leads to a reduced rate of molecular diffusion and an arrested non-equilibrium structure is formed, inhibiting nucleation and the formation of a crystalline solid. The system is restricted in the range of molecular configurations that can be sampled, reducing the likelihood that the system explores a configuration consistent with the thermodynamically stable crystalline state, described as non-ergodic



behaviour. The dynamic viscosity of the glass can be in excess of 10^{10} Pa s, equivalent to that of a typical solid phase (Mikhailov et al., 2009). The glass transition temperature and glass transition relative humidity are dependent on the rate of change of temperature or solute concentration. For example, rapid rates of cooling can lead to a higher value of T_g than slower cooling rates (Debenedetti and Stillinger, 2001; Zobrist et al., 2008). For aerosol particles, the timescale for change in environmental conditions can be expected to be an extremely important factor in influencing the formation of an arrested structure; rapid dehydration may lead to a compositional gradient within a particle and the formation of a highly viscous shell that slows the communication between the particle bulk and surrounding gas phase. Burnett et al. (2004) have reported an increase in RH_g from 30 to 40% when spray drying lactose particles at a higher drying rate.

The sensitivity of glass formation and crystallisation to changes in environmental conditions and the dependence on the timescale of coupling between the gas and ¹⁵ condensed phases highlights the importance of investigating the properties of glassy aerosol directly (Zobrist et al., 2008; Murray et al., 2008; Bodsworth et al., 2010), rather than relying on bulk solution measurements. In this publication, coarse mode ultra-viscous and glassy aerosol are formed by drying sucrose, raffinose and sucrose-sodium chloride solutions below the glass transition relative humidity. Carbohydrates

- ²⁰ have been identified in aerosol particles in different continents (Graham et al., 2002; Carvalho et al., 2003; Yttri et al., 2007; Wang et al., 2009). Although the thermodynamic properties and glass transition behaviour of small carbohydrates in solution have been studied extensively (MacKenzie et al., 1977; Orford et al., 1990; Roos, 1991, 2010; Champion et al., 1997; Hsu et al., 2003; Frank, 2007), only one study has examined directly the formation of glassy particles through debudration using an
- amined directly the formation of glassy aerosol particles through dehydration using an electrodynamic balance (EDB) (Zobrist et al., 2011). In the present work, we compare independent measurements of the formation of glassy sucrose aerosol using aerosol optical tweezers with the previous EDB measurements, confirming the previously reported non-ergodic behaviour accompanying the mass transfer of water between the



gas and condensed phases. In addition, we extend this previous work to a further system (raffinose) which exhibits behaviour that is again consistent with the formation of glassy aerosol. Finally, we examine the dependence of the glass formation on the mass fraction of an inorganic solute (sodium chloride).

5 2 Experimental method

2.1 Optical tweezers

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A detailed introduction to aerosol optical tweezers and the experimental approach has been described elsewhere (Mitchem and Reid, 2008; Wills et al., 2009) and will be only briefly summarized here. A dispersed aerosol mist is generated using a medical nebulizer and introduced into a custom fabricated cell (~8 cm³ in volume). The optical 10 tweezers are arranged in an inverted microscope configuration with an oil immersion microscope objective (numerical aperture of 1.25, 100 x magnification) used to focus the green light generated by a Nd:YVO₄ (532 nm) laser into the trapping cell, forming a single beam gradient force optical trap. As an aerosol droplet passes close to the laser focus, the gradient force draws the particle into the focus, the region with the 15 largest gradient in light intensity. The gradient force dominates the gravitational and scattering forces by at least two orders of magnitude, providing a strong restoring force that effectively immobilises the particle. A single droplet (1~8 µm in radius) is captured and held near the beam focus at a height of $\sim 40 \,\mu m$ above a thin glass coverslip mounted above the microscope objective. Typical laser powers required are in the 20 range 5 to 15 mW.

By adjusting the balance between flows of dry nitrogen gas and humidified nitrogen gas using needle valves, the RH in the cell can be regulated. The mass flow rate of each gas is measured by mass flow meters (Bronkhurst, UK). Two capacitance probes are used to monitor the RH in the gas flow before (probe 1) and after (probe 2) the cell. Once a droplet (sucrose-water, raffinose-water or sucrose-sodium chloride-water)



is trapped, the RH in the cell is held at the same value, typically $60 \pm 0.5\%$, for a couple of hours to allow the droplet and cell to equilibrate to the gas flow. The total gas flow rate is $\sim 0.1 \,\text{Lmin}^{-1}$ and the fluctuation of the temperature for each experiment is $\pm 1 \,\text{K}$. A blue LED (455 nm) provides illumination for microscopy. Brightfield images are ⁵ used to observe the morphology of the trapped droplet and the glassy particles that are eventually deposited on the coverslip simply by removing the trapping laser beam. The back scattered Raman light from the droplet is collected using a spectrograph equipped with a 1200 grooves/mm grating and imaged onto a CCD array of 1024 × 256 pixels. The changing spectra of the droplet are monitored in real time with a time-resolution of 1s. The spontaneous Raman spectrum provides a signature of the composition of 10 the droplet. The stimulated Raman spectrum, occurring at wavelengths commensurate with whispering gallery modes (WGMs), is used to characterize the size of the droplet (Mitchem and Reid, 2008; Wills et al., 2009). The wavelengths of the WGMs are dependent on the size of the droplet and by comparing these wavelengths with predictions from the Mie scattering theory, the droplet size can be determined with 15 nanometer accuracy.

2.2 The refractive index and density of aqueous sugar solutions

The refractive indices of sucrose, raffinose and mixed component (sucrose with sodium chloride) solutions with different concentrations were measured at $\lambda = 589$ nm using a Palm Abbe PA203 digital refractometer (MISCO, USA) at a constant temperature of 298 ± 1 K. Each refractive index value is determined from an average of 3 individual measurements. The measured refractive indices as a function of solute molarity are shown in Fig. 1 for the aqueous sucrose and raffinose binary solutions. Measurements for the sucrose solution agree well with published data (International Organization of Legal Metrology, 1993) and fall close to values estimated from a volume weighted mixing rule. To estimate the volume weighted values the average of the refractive index

ing rule. To estimate the volume weighted values, the average of the refractive index for the fast and slow axes for birefringent crystalline sucrose (1.558) is taken as the crystalline value (Halbout, 1982). A polynomial fit to the experimental data is used to



estimate the refractive index at intermediate molarities. Above the highest measured concentration (a refractive index of 1.504 at \sim 3.7 M), there is uncertainty in the refractive index value. As discussed in Sect. 3.1 this leads to uncertainty in the refractive index at RHs below 40%. However, even at the highest of solution concentrations when

- approaching a mass fraction of solute of 1, the value estimated from the polynomial fit lies below the crystalline value by only 0.0093 or 0.6%, equivalent to an uncertainty in the size estimate which remains less than 20 nm for all of the measurements reported here at RHs below 40%. Indeed, as we shall see later, the time dependence of size below this RH becomes the important parameter for investigation rather than the absolute value of the size, and the kinetic measurements of size change are not compromised
 - by inaccuracies in the refractive index treatment.

The polynomial fit is used to estimate the variation in refractive index with solute molarity and, thus, droplet size from knowledge of the droplet composition and size at the initial RH at which the droplet size is allowed to equilibrate (Wills et al., 2009). This

- enables Mie predictions of the WGM wavelengths with variation in trial particle size and the retrieval of the droplet size from each unique recorded fingerprint of WGM wavelengths. Although this is based on measurements at 589 nm and the WGM fingerprints are centred around 650 nm, the variation with wavelength over this range is considerably less than the variation with solute concentration. Thus, correctly representing the
 variation in refractive index with droplet size/solute concentration is crucial for estimat-
- ing the particle size from the WGM fingerprint. Neglecting dispersion introduces an error to the size of < 10 nm (Hanford et al., 2008).

The densities of sucrose solutions of different concentrations can be estimated from the assumption of the volume additivity of pure component densities (VAD), allowing

the density to be estimated from the densities of water, ρ_w (taken as 1000 kg/m⁻³), and sucrose, ρ_s (taken as 1580.5 kg/cm⁻³, Haynes, 2011), and the mass fraction of solute (MFS):

$$\frac{1}{\rho} = \frac{1 - \text{MFS}}{\rho_{\text{w}}} + \frac{\text{MFS}}{\rho_{\text{s}}}$$

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This treatment yields values that compare well with published data (Haynes, 2011) over the range up to an MFS of 0.9, as shown in Fig. 1b.

3 Predictions of the equilibrium and time-dependent size of glassy sucrose particles

5 3.1 Sucrose droplets at equilibrium

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The prediction of the equilibrium size or mass of an aqueous aerosol particle at a particular RH containing an involatile organic, such as sucrose, requires knowledge of the composition of the solution at thermodynamic equilibrium with the gas phase, the density of the solution at the equilibrium composition (ρ_w), and the mass of solute (m_{Dry}) or diameter of the equivalent dry solute particle (D_{Dry}). The dependence of the wet droplet diameter (D_w) on RH can be conveniently expressed as a diameter growth factor (GF_{dia} (RH)),

$$GF_{dia} (RH) = \frac{D_{w}}{D_{Dry}} = \left(\frac{m_{w}\rho_{Dry}}{m_{Dry}\rho_{w}}\right)^{1/3} = GF_{mass} (RH)^{1/3} \left(\frac{\rho_{Dry}}{\rho_{w}}\right)^{1/3}$$
(2)

where m_w is the mass of the solution droplet, ρ_{Dry} is the density of the pure dry solute and GF_{mass} (RH) is the mass growth factor. The mass growth factor can be estimated from a thermodynamic parameterisation of the equilibrium mass fraction of solute in the solution droplet at a specific water activity, such as those presented in Fig. 2a. The diameter growth factor can then be calculated and compared directly with the optical tweezers measurements, in which the varying droplet size with RH is measured.

Numerous experimental studies have measured the dependence of the water activity of aqueous sucrose solutions on the weight percentage of solute in solution, commonly referred to as the mass fraction of solute, MFS. These measurements are shown in Fig. 2a and are compared with four parameterisations (Norrish, 1966; Starzak and



Peacock, 1997; Zobrist et al., 2008). The dependence of the glass transition temperature on the MFS in solution reported in previous publications is shown in Fig. 2b, indicating that a glass transition should occur as the MFS increases above 0.95 at room temperature.

⁵ Norrish (1966) suggested a relationship of the water activity, a_w , of nonelectrolyte solutions to the mole fractions of water and solute, x_w and x_s , respectively:

 $a_{\rm w} = x_{\rm w} \exp(k x_{\rm s}^2)$

k is an empirical constant estimated to be -6.47 for sucrose (Labuza, 1984). The applicability of this value has been confirmed to extend to high solute concentrations by recent measurements (Baeza et al., 2010).

Starzak and Peacock (1997) provided a comprehensive fit to the experimental data using the Margules equation for the water activity coefficient, γ_w , with

$$\ln \gamma_{\rm w} = \frac{Q}{RT} \left(x_{\rm s}^0 \right)^2 \left[1 + b_1 x_{\rm s}^0 + b_2 \left(x_{\rm s}^0 \right)^2 \right] \tag{4}$$

where x_s^0 is the nominal mole fraction of sucrose, and $Q = -17538 \text{ J mol}^{-1}$, $b_1 = -1.0038$ and $b_2 = -0.24653$. From the activity coefficient estimate from Eq. (4) at a specific mole fraction of solute, the water activity can be estimated, and is shown in Fig. 2a.

A further parameterisation of experimental data has been described by Zobrist et al. (2011). The water activity is expressed as a function of the MFS in the form

$$a_{w} = \frac{1 + a \cdot \text{MFS}}{1 + b \cdot \text{MFS} + c \cdot \text{MFS}^{2}} + (T - T^{\Theta})(d \cdot \text{MFS} + e \cdot \text{MFS}^{2} + f \cdot \text{MFS}^{3} + g \cdot \text{MFS}^{4})$$
(5)

where a = -1, b = -0.99721, c = 0.13599, d = 0.001688, e = -0.005151, f = 0.009607and g = -0.006142, and T^{Θ} is the reference temperature 298.15 K. This expression is valid over the temperature range 160 to 313 K and the entire concentration range.

In previous optical tweezers measurements we have compared the change in equilibrium droplet size with RH for mixed inorganic/organic aerosol with the Aerosol Diameter



(3)

Dependent Equilibrium Model, ADDEM (Topping et al., 2005; Hargreaves et al., 2010; Hanford et al., 2008). The treatment of organic components in this model is based on the widely used group contribution method UNIFAC. The variation in water activity with solute concentration calculated from this treatment is also presented in Fig. 2a.

- ⁵ For the binary water-sucrose system, it is clear that the water activity is underestimated by ADDEM at a sucrose MFS greater than 0.35 when compared with the experimental data. The Norrish parameterisation represents the experimental data most accurately over the whole RH range. The Starzak and Peacock and Zobrist treatments deviate from the experimental data at water activities below 0.5. The latter treatment
- has been shown to accurately describe the change in equilibrium properties of aqueous sucrose droplets examined in EDB measurements (Zobrist et al., 2011) and is the treatment used for the kinetic simulations described below.

The mass growth factor can be estimated, with variation in water activity, from the expression:

15 GF_{mass} (RH) =
$$\frac{m_{\rm w}}{m_{\rm Dry}} = \frac{1}{\rm MFS}$$

The variations in the mass growth factors estimated from the four treatments are shown in Fig. 3a. From the VAD treatment of density and the mass growth factors reported in Fig. 3a, the RH dependence of the diameter growth factor can be estimated from Eq. (2), and the predictions are presented in Fig. 3b. The differences between growth factor predictions from the Norrish, Zobrist and ADDEM treatments reflect the differences in the water activity/MFS relationships discussed above. Only the Norrish and Zobrist treatments will be compared with the experimental data presented below as these provide the most accurate representation of the existing bulk phase sucrose data.



(6)

3.2 The time-dependent size of glassy sucrose droplets

Previously we have shown that the water uptake kinetics in sucrose droplets far from thermodynamic equilibrium can modelled by solving the spherical diffusion equation (Zobrist et al., 2011). The crucial point is that the diffusivity of water inside the particle ⁵ becomes a function of the water concentration itself, which renders the diffusion equation non-linear and difficult so solve. A numerical spherical shell diffusion model has been developed, which shows that the diffusion profiles of water into a highly viscous sucrose particle leads to steep diffusion "fronts" instead of the widely known creeping diffusion tails (Marshak, 1985). The temperature dependence of D_{H_2O} is parameterized according to a Vogel-Fulcher-Tammann (VFT) approach (Debenedetti and Stillinger, 2001) and thus D_{H_2O} is parameterized as:

$$\log_{10} \left[D_{H_2O}(T, a_w) \right] = - \left(A(a_w) + \frac{B(a_w)}{T - T_0(a_w)} \right)$$

A, *B* and T_0 are fit functions that all depend on the water activity of the aqueous sucrose solution, which in itself is also a function of the temperature and concentration. The fit equations for the three parameters, *A*, *B*, and T_0 are given in Zobrist et al. (2011). The relationship between the MFS and the water activity is provided by the Zobrist parameterisation described in Sect. 3.1.

4 Formation and hygroscopicity of single glassy sucrose particles at room temperature

Either rapid cooling or drying at a constant temperature enhances the likelihood of glass formation over nucleation and crystallisation (Angell, 1995; Debenedetti and Stillinger, 2001). In the measurements presented here, we have chosen to rapidly dry a trapped aerosol droplet by switching between a humidified gas flow at an RH above



(7)

60% to a completely dry flow of nitrogen gas with an RH approaching 0% at constant temperature. An example of the recorded change in RH and droplet size is presented in Fig. 4a for a sucrose-water droplet (initially with a MFS of ~ 0.3). After a period of ~ 2 h held at an RH of 66 % to allow the wet aerosol to equilibrate to a size of 4300 nm,

- the humidified wet N₂ flow was switched to a full dry N₂ flow to rapidly dry the droplet, reducing the RH in the cell to < 10% in less than 25 seconds. Notably, the release of water from the droplet persisted for more than 5 h. After 20 h, the RH was varied in increasing or decreasing steps while restricting it to below the glass transition relative humidity, expected to occur at ~ 24% at 298 K (Fig. 2b). Once again, the droplet radius
 responded very slowly to the changes in RH over a period of 2 to 3 h and size changes of less than < 10 pm were recorded for each 5% change in RH with the droplet never
- of less than < 10 nm were recorded for each 5% change in RH with the droplet never achieving an equilibrium size.

The variations in equilibrium size of the sucrose droplet with RH predicted by the Norrish and Zobrist parameterisations are shown in Fig. 4a for comparison. The observed

- ¹⁵ droplet radius is offset from the Norrish and Zobrist predictions by ~4 and ~15 nm, respectively, at the lowest RH (< 1.5%) after 20 h, well within the expected limits set by the uncertainties in the refractive index and RH. Agreement with the ADDEM predictions is worse with the offset > 180 nm, as anticipated from Fig. 2. These results suggest strongly that the droplet has passed through a glass transition on drying and that a diagonilibrium is anticipated between the droplet and the sugregulation of the suggest strongly that the droplet has passed through a glass transition on drying and that a diagonilibrium is anticipated between the droplet and the sugregulation.
- ²⁰ that a disequilibrium is established between the droplet and the surrounding vapour phase which persists for more than 5 h and is only very slowly approached.

After 41 h, the laser trap was removed allowing the particle to deposit onto the glass coverslip. Images were obtained by gradually raising the focal depth of the image plane for the brightfield image and laser focus from below to above the droplet, Fig. 4b. The

Raman spectra corresponding to each image are also shown in the region of the OH stretching vibration of water (Mitchem and Reid, 2008; Wills et al., 2009). Although the laser beam was reintroduced prior to recording the images and Raman spectra, it was not possible to remove the particle optically from the coverslip. Not only does the particle appear to retain a spherical morphology on sedimentation to the coverslip from



the brightfield image, but the presence of strong WGM enhanced Raman scattering in spectra 3, 4 and 5 confirms that the particle remains spherical (Mitchem and Reid, 2008; Wills et al., 2009). Release of a solution droplet to the coverslip always results in spreading and the loss of sphericity. These observations strongly suggest that the
⁵ particle has formed an amorphous solid or glass. The OH Raman stretching signature confirms that considerable water is retained within the particle even though the RH is considerably less than 10%.

Although Fig. 4 provides strong evidence for the formation of a glassy sucrose aerosol particle and a kinetically imposed limit on size, finer steps in RH are required to determine the glass transition RH and to compare the accuracy of the thermodynamic models for representing the size above and below the glass transition. An example of a sucrose droplet subjected to smaller transitions in RH is presented in Fig. 5a. For com-

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parison with the model predictions, the droplet is assumed to be in equilibrium at the highest water activity/RH. Predictions from the Norrish equilibrium treatment and the ki-

netic model based on the Zobrist water activity parameterisation are shown. The kinetic simulations are based on the diffusion constants for water in glassy sucrose particles measured in EDB studies (Zobrist et al., 2011). Although qualitatively in agreement, the shallow slope of the growth factor at intermediate RHs from the Norrish parameterisation (Fig. 3b) leads to an overestimate of the measured size by up to 25 nm.
 This cannot be accounted for by the uncertainty associated with the RH measurement,

 $\pm 2\%$. At RHs above the glass transition, the agreement between the kinetic model and measurements is excellent, both in absolute size and temporal dependence. For each transition in RH, the droplet approaches an equilibrium size at long times that is con-

sistent with that predicted from the Zobrist parameterisation to within 8 nm. Below the glass transition, the discrepancy in size becomes larger, but remains less than 20 nm at all RHs and times. This is well within the uncertainty expected from the uncertainty in composition and, thus, refractive index at low water activity, as discussed in Sect. 2.2.



A comparison of the temporal dependencies of size measured and predicted from the kinetic model is presented in Fig. 5b for four of the transitions in RH shown in Fig. 5a: 43 to 36.7%, 26 to 16.3%, 6.6 to 0% and 45.6 to 1.6%. The discontinuous appearance of the measured droplet size is simply a consequence of the choice to ⁵ perform the fitting of the WGM fingerprint with a trial size step of 1 nm. While the linear time scale shown in the inset demonstrates the clear slowing in the rate of mass transfer as the glass transition is approached and then passed, the log scale in the main figure more clearly highlights the exceptional degree of agreement between the kinetic model and measurements. The kinetic model reproduces the observed change ¹⁰ in timescale of more than 2 orders in magnitude for RH transitions above and below the glass transition. Notably even though the glass transition is not surpassed for the

- the glass transition. Notably, even though the glass transition is not surpassed for the first RH change, the droplet still takes up to 1000s to fully equilibrate, reflecting that even at this relatively high RH, the viscosity of the droplet and diffusion within the bulk of the particle still limit mass transfer. We shall return to a discussion of the correlation
- with viscosity in Sect. 5. For the largest change in RH considered in Fig. 5b, 45.6 to 1.6%, the temporal dependence of size is considerably different from that observed for small changes in RH. In fact, the size change takes longer to initiate and this may be a consequence of a very rapid dehydration of the droplet surface, dropping the water activity below the glass transition, and forming a relatively impermeable shell around
 the droplet surface. This is a clear indication of the effect of different conditions and
- drying rate on particle size.

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Estimating a timescale for droplets to adapt to change in environmental conditions above and below the glass transition would be extremely helpful for qualitatively assessing the change in rate of mass transfer as a droplet approaches a glassy state. However, care must be taken in assessing the time response of the glassy aerosol: it

is not clear that equilibrium is reached even on a timescale longer than 20000 s. In Fig. 6 we compare the apparent diameter growth factor measured after 5000 s to the Zobrist and Norrish equilibrium state predictions. While it is clear that the Zobrist parameterisation more accurately reflects the equilibrium state at RHs above 25%, it is



clear that there is increasing divergence as the RH is lowered, strongly suggesting that equilibrium is not achieved on a timescale of 5000 s, as shown in the error plot in the lower panel. This does, however, amount to an offset of < 0.01 in GF from the Zobrist parameterisation, or < 1% in size.

- From Figs. 4 and 5, a comparatively fast initial decrease (or increase) in size after an RH change is followed by extremely slow evaporation (or growth) and size changes of less than 1 nm over 10 000 s. We use this rate as a criterion for defining an effective plateau in the particle size. Then, the time for the droplet size to decrease to the halfway point in its progress to this plateau can be used to compare the response time
- of the droplet to changes in RH above and below the glass transition. Even if the measurements were prolonged for a further 50 000 s, this would lead to a further decrease in size that was less than 10% of the overall size change, with little impact on the reported timescale for the droplet to progress to the halfway point. In many applications, the behaviour on extremely long timescales (> 20 000 s) is much less relevant than the
 behaviour over the 100 to 1000 s timescale. The *half-time* provides a phenomenolog-
- ical guide as to the time-response of the droplet size, clearly signalling the onset of glassy behaviour.

The variations in the half-time recorded for the change in the RH reading from the probes before (probe 1) and after (probe 2) the cell are shown in Fig. 7a and b, respectively. The time-response of probe 2 provides a control measurement of the time

- 20 spectively. The time-response of probe 2 provides a control measurement of the time lag for the whole flow system to reach the conditions set by the input gas flow and recorded by probe 1. It is noticeable that although the response of the pre-cell probe 1 is limited by the slow time-response of the capacitance RH probe, some changes in RH do take longer to achieve for the whole flow system. Despite this, it is clear that
- the timescale for the aerosol size-response, made for numerous droplets, is systematically and significantly slower than the response of the RH probes once the final RH is below the glass transition at ~ 24% RH (Fig. 7c). All measurements were made at a temperature of $298 \pm 2 \text{ K}$. The marked slowing of the size change when conditions take the aerosol below the glass transition highlights the significant retardation in mass



transfer between the particle bulk and vapour phase once the glass is formed. No sudden loss of water is observed that would signify crystallisation; instead the aerosol vitrifies and becomes glassy and the mobility of water molecules is inhibited although not suppressed entirely.

- The half-times recorded during the humidifying process are shown in Fig. 7d. Again, particles existing in a glassy state show resistance to water transport and equilibration. The water adsorption remains controlled by bulk diffusion and the rate of permeation of water into the bulk of the glassy aerosol. Once the final RH with which the particle is equilibrating increases above the glass transition RH, the water adsorption and dis-
- solution of the glass becomes more rapid, although the rate noticeably remains higher than would be expected based on the timescale of the RH change. It is clear from Fig. 5a and b that increasing the RH above the glass transition returns the droplet to equilibrium with the gas phase on a timescale of 10's to 100's of seconds, considerably shorter than changes that maintain a glassy state.
- The solute mass fractions at which the tweezers measurements suggest the glass transition occurs (at 298±2K) are indicated in Fig. 2b, with the Norrish treatment of water activity yielding a solute mass fraction of 0.93 and the Stazark and Peacock treatment a value of 0.95. The values are in excellent agreement with previous measurements, confirming once again that the aerosol behaviour is consistent with the formation of a glassy particle. Using the model prediction by He et al. (2006), the viscosities
- of sucrose-water solutions with sucrose mass fractions of 0.93 and 0.95 are $\sim 10^9$ and $\sim 10^{13}$ Pa s, respectively. This suggests that the Stazark and Peacock (1997) thermodynamic treatment is better able to predict the glass transition of sucrose aerosol rather than the Norrish treatment; 10^{12} Pa s is a typically accepted viscosity value for a glass transition (Debenedetti and Stillinger, 2001).

Based on the diffusion constant prediction curve by He et al. (2006), the water diffusion coefficient is $\sim 10^{-19} \text{ m}^2 \text{ s}^{-1}$ in the 95% sucrose mass fraction solution at 20 °C. Fig. 5b suggests that the diffusion constant reported by Zobrist et al. (2011) and used in the kinetic simulation, $\sim 8 \times 10^{-16} \text{ m}^2 \text{ s}^{-1}$ at this temperature and composition, may



be too large; the experimental size changes more slowly than predicted for all three of the small steps in RH. Using the diffusion constant of He et al. (2006), a water molecule would require more than 2.8 years to diffuse to the surface from within a 3 micron radius droplet below the glass transition. Thus, a fully equilibrated sucrose droplet below the glass transition would be expected to be unobservable on the timescale of our experimental measurements.

5 Formation of glassy raffinose particles and mixed component sucrose/sodium chloride particles at room temperature

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To provide further evidence of the influence of a glass transition on the timescale for mass transfer between the condensed and gas phases, the time-response of droplets containing a higher molecular weight carbohydrate, raffinose (C₁₈H₃₂O₁₆), has been investigated. After equilibrating at ~ 89% RH for more than two hours, the RH in the cell was suddenly decreased to fully dry conditions (< 5% RH), Fig. 8, by switching instantaneously from a humidified nitrogen to dry nitrogen flow. Water desorption from the raffinose-water droplet persisted even after 6 h. As for the sucrose measurements, the concentration of raffinose in the droplet at the starting RH was estimated from the water activity parameterisation provided by Zobrist et al. (2008), allowing the refractive index to be estimated for determination of the starting size. According to Zobrist et at the starting size. According to Zobrist et al.

- al. (2008), raffinose passes through the glass transition at an RH of ~ 53% at room
 temperature. Thus, the influence of a glassy state on the mass transfer reported in Fig. 8 is expected and crystallization is inhibited. After 6 h, the particle was deposited on the coverslip. A brightfield image and Raman spectrum of the particle is shown in the inset to Fig. 8. As for sucrose, the particle retains a spherical shape when deposited on the coverslip, which is apparent from the persistence of WGMs on the OH water Raman
- ²⁵ band; this also indicates that water is retained within the particle. Notably, raising the RH above the glass transition RH led to the dissolution of the deposited particle.



To consider the significance of the length of the equilibration timescale for atmospheric aerosol, it is important to consider the influence of internally mixed inorganic components such as sodium chloride on the time response of the aerosol to change in environmental conditions. As a typical soluble organic chemical with many hy-

- ⁵ droxyl groups, sucrose is able to form strong hydrogen bonds with water. The addition of sodium chloride, recognised as a structure breaking solute in aqueous solution (Mitchem et al., 2006) can be expected to have a significant impact on the hydrogen bonding network in the aqueous sucrose droplets, hence influencing physical properties such as viscosity and the glass transition temperature.
- Measurements of the half-time for the equilibration of mixed component sucrose/sodium chloride were performed with a varying mole fraction of sodium chloride, balance sucrose. In each measurement, the droplet was first conditioned at an RH of 78% for 2–3 h, the RH was then abruptly decreased to below 2% RH and the response of the particle size was recorded. The ratio of the half-time for the droplet size change
- to the change in the RH measured by probe 1 is presented in Fig. 9a with variation in composition. Uncertainties in these ratios of half-times are based on measurements from numerous droplets with the same composition. The ratio was observed to decrease from ~ 150 to ~ 45 when the mole fraction of sodium chloride increased from 0 to 0.2. This indicates that the addition of NaCl significantly decreases the timescale for mass transfer with the surrounding vapour, enhancing the release of water, although
- the rate remains slow.

To interpret the compositional measurements for equilibration timescales shown in Fig. 9a, it is necessary to consider the change in viscosity with change in mole fractions of the two solutes. Chenlo et al. (2002) examined the dependence on composition ²⁵ of the kinematic viscosity and density of aqueous mixtures of sucrose and sodium chloride over the molality range 0 to 4.5 mol kg^{-1} for both solutes and at temperatures between 293 and 323 K. They also reported parameterisations based on solute molality and temperature that yielded the measured densities and kinematic viscosities for the ternary solutions within ±0.5% and ±3%, respectively. The dynamic viscosity (Pa s)



can be estimated from the density $(kg m^{-3})$ and kinematic viscosity $(m^2 s^{-1})$. For a sucrose solution with a MFS of 0.94, the dynamic viscosity can be estimated to be 6×10^{12} Pa s from the treatment of Chenlo et al. (2002), which compares well with the values estimated from the treatment of He et al. (2006), even though the molality at this MFS (38.8 mol kg⁻¹) is considerably above the highest concentration measurement on which the parameterisation is based. Given that the sucrose component dominates the determination of the viscosity for the mixture, this gives some confidence in the use of the Chenlo et al. (2002) parameterisations at higher solute molalities than 4.5 mol kg⁻¹. Ignoring the non-ideal effects that are likely to play a role at low RH, the water content of the ternary solution can be estimated by applying the Zdanovski-Stokes-Robinson mixing rule and the compositions of binary solutions. Specifically, the total water content *W* (kg), can be written as

$$W = \frac{M_{\text{NaCl}}}{m_{\text{NaCl},0}(a_{\text{w}})} + \frac{M_{\text{Sucrose}}}{m_{\text{Sucrose},0}(a_{\text{w}})}$$

where M_i is the number of moles of solute *i* and $m_{i,0}(a_w)$ is the molality of the binary solution at the water activity a_w . Experimental data for sodium chloride solutions extends down to a water activity of 0.4 (Clegg, 1997), and the composition of sucrose solutions below this water activity is also uncertain (Fig. 2). Given this, we have chosen this water activity (RH) at which to estimate the solution composition and the dynamic viscosity, shown in Fig. 9a. At this water activity, the molalities of sodium chloride and sucrose in the binary component solutions are 15.9 and 23.6 mol kg⁻¹. Although not

- fully reflecting the dynamic viscosity under the conditions at which the glassy aerosol is likely to form, it is clear that the change in equilibration half-time and bulk viscosity show similar behaviour (Fig. 9b). The water activity is likely to be inhomogeneous within an evaporating ternary droplet and it is not surprising that considering the vis-
- cosity at one water activity alone (in the middle of the RH range during the RH drop being studied) fails to capture effectively the microscopic nature of the dynamics. However, the increasing timescale for equilibration with decreasing RH and increasing bulk

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viscosity is consistent with the gradual change in equilibration timescale as the glass transition is approached and surpassed in the single component sucrose aerosol measurements. Further studies of the dependence of the timescale for mass transfer on particle composition are essential.

5 6 Conclusions

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We have described observations of the influence of a glass transition on the kinetics of mass transfer in the equilibration of water between the condensed and gas phases of aqueous sucrose, raffinose and sodium chloride/sucrose aerosol. Once the aerosol particle has formed a glass, the particle may remain at disequilibrium for timescales far longer than 5000 s reflecting the extremely low diffusivity of water within the glass. The 10 measured time-dependence of particle size compares well with kinetic predictions from the ETH model (Zobrist et al., 2011), providing independent verification of the impact of a glass transition on the water evaporation or condensation rate. When deposited on a glass coverslip, the particle retains a spherical shape, confirmed by the persistence of WGMs on the OH Raman band signature. Not only should the kinetic limitations 15 imposed on mass transfer by the glassy state be considered for organic aerosol, but a delay in mass transfer is observed for mixed component aerosol containing sodium chloride. Although there remains considerable uncertainty in the kinetic limitations imposed on condensation or evaporation by the surface accommodation coefficient (Miles

et al., 2010), this work suggests that the role of bulk accommodation in controlling mass transfer and aerosol equilibration must also be considered.

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Fig. 1. (a) Refractive index as a function of the solute molarity and mass fraction of solute (MFS) for aqueous sucrose solutions: black squares, these measurements; open circles, literature data; red line, polynomial fit; dashed blue line, volume fraction mixing rule; dotted blue line, mass fraction mixing rule; hexagon, value taken as crystalline refractive index from Halbout and Tang (1982). A parameterised fit to the measured values for aqueous raffinose solution are shown by the green line. **(b)** Dependence of sucrose solution density on solute molarity: black line, literature data (Haynes, 2011); red line, volume additivity model.





Fig. 2. (a) Water activity as a function of the mass fraction of solute (MFS) from the ADDEM model (dotted dashed black line), and the parameteriations of Norrish (1966, dotted red line), Zobrist et al. (2008, light blue line) and Starzak and Peacock (1997, dashed blue line). Experimental data is shown by the symbols: crosses, Scatchard et al. (1938); stars, Robinson and Stokes (1965); squares, Chuang et al. (1976); down triangles, Rüegg and Blanc (1981); diamonds, Lerici et al. (1983); filled circles, Bressan and Mathlouthi (1994); asterisks, Bubnik et al. (1995); and open circles, Mogenson et al. (2009). The inset shows an expanded range above a water activity of 0.8. (b) The glass transition temperature as a function of MFS from previous publications and the present data (Norrish, 1966; water activity, black star; Starzak and Peacock, 1997; black triangle). Literature values: open black circles, Koster (1991); red circles, Ablett et al. (1992); green triangles, Roos (1993); brown asterisks, Blanshard et al. (1991); blue triangles, Franks (1993); purple triangles, Sun et al. (1996); light blue line, Hsu et al. (2003).





Fig. 3. (a) Mass growth factors as a function of relative humidity based on the water activity data parameterisations of Norrish (dotted red line), ADDEM (dash dot black line) and Zobrist (light blue line). **(b)** Diameter growth factors for the same treatments (same colours) as (a) using the volume additivity treatment of density.





Fig. 4. (a) Time-dependence of the size of a sucrose droplet (green) with change in RH (grey line, right axis). The sizes predicted at equilibrium using the Norrish (red line), Zobrist (light blue line) and ADDEM (black line) thermodynamic models are shown for comparison. The inset shows an expanded view of the time dependence around 100 000 s. (b) Final images and Raman spectra of the glassy sucrose particle when deposited on the coverslip and with varying image height. From top to bottom: laser focus below the coverslip, at the bottom surface of the particle, at the middle of the particle, at the top surface of the particle and above the particle.





Fig. 5. (a) Time-dependence of the size of a sucrose droplet (green) with change in RH (grey line, right axis). The predicted equilibrium size using the Norrish (red line) model is shown for comparison along with the kinetic model of ETH (light blue) which uses the Zobrist parameterisation for water activity. The grey shaded envelope surrounding the Norrish predictions reports the uncertainty in the model based on the uncertainty in the experimentally determined RH of $\pm 2\%$. (b) Comparison of the time-response of droplet size for four of the RH changes reported in part (a): red, 43 to 36.7%; blue, 26 to 16.3%; green, 6.6 to 0%; black, 45.6 to 1.6%. The experimental data is shown by the symbols and the results of the kinetics simulations by the lines.





Fig. 6. A comparison of the measured RH variation in diameter growth factor after ~ 5000 s of equilibration with the Zobrist (solid line) and Norrish (dashed line) model predictions of the equilibrium state. Measurements made on different droplets (6 in total) are shown by different sybols. Although the Zobrist parameterisation is quantitatively more consistent with the measured data at high RH, the systematic departure from equilibrium behaviour after ~ 5000 s of equilibration with decreasing RH is apparent. The lower panel shows $\Delta(GF) = |GF(measured) - GF(Zobrist)|$. Uncertainties in the RH measurements are shown at the ±2% level for one experiment.





Fig. 7. The recorded half-time for the RH decrease before **(a)** and after **(b)** the trapping cell. The filled triangles denote the initial RH and the open circles the final RH with different colours corresponding to measurements on different droplets. **(c)** The half-time estimated for the change in sucrose droplet radius for a series of dehumidifying measurements on different droplets (different colours). The inset is an example of a typical size measurement. After 10 000 s, the rate of decrease in size becomes less than 1 nm in 10 000 s, as illustrated by the red dotted line. The time for the droplet to reach the half way point in progressing to this slowly evolving size provides a measure of the change in the rate of mass transfer below the glass transition. **(d)** The half-time for increase in radius of sucrose droplets during a humidifying cycle.





Fig. 8. The time dependence of the size of a raffinose droplet (green line) and the relative humidity of the gas flow entering the trapping cell (grey line, right axis). The inset shows the image of the particle and a Raman spectrum when deposited on the coverslip after 25 000 s.





Fig. 9. (a) The composition dependence of the ratio of the half-times for the radius to the RH changes (black circles) for aqueous sodium chloride/sucrose droplets. The composition dependence of the dynamic viscosity at a solution composition with water activity of 0.4 is also shown (red circles, right axis). **(b)** Dependence of the half-time ratio shown in (a) on solution viscosity.

