**Atmospheric
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Evaluation of the accuracy of analysis tools for atmospheric new particle formation

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Evaluation of analysis tools for nucleation

H. Korhonen et al.

Title Page

Abstract	Introduction
Conclusions	References
Tables	Figures

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Abstract

Several mathematical tools have been developed in recent years to analyze new particle formation rates and to estimate nucleation rates and mechanisms at sub-3nm sizes from atmospheric aerosol data. Here we evaluate these analysis tools using 1239 numerical nucleation events for which the nucleation mechanism and formation rates were known exactly. The accuracy of the estimates of particle formation rate at 3 nm (J_3) showed significant sensitivity to the details of the analysis, i.e. form of equations used and assumptions made about the initial size of nucleating clusters, with the fraction of events within a factor-of-two accuracy ranging from 43–97%. In general, the estimates of the actual nucleation rate at 1.5 nm ($J_{1.5}$) were less accurate, and even the most accurate analysis set-up estimated only 59% of the events within a factor of two of the simulated mean nucleation rate. The $J_{1.5}$ estimates were deteriorated mainly by the size dependence of the cluster growth rate below 3 nm, which the analysis tools do not take into account, but also by possible erroneous assumptions about the initial cluster size. The poor estimates of $J_{1.5}$ can lead to large uncertainties in the nucleation prefactors (i.e. constant P in nucleation equation $J_{1.5} = P \times [H_2SO_4]^k$). Large uncertainties were found also in the procedures that are used to determine the nucleation mechanism. When applied to individual events, the analysis tools clearly overestimated the number of H_2SO_4 molecules in a critical cluster for most events, and thus associated them with a wrong nucleation mechanism. However, in some conditions the number of H_2SO_4 molecules in a critical cluster was underestimated. This indicates that analysis of field data that implies a maximum of 2 H_2SO_4 molecules in a cluster does not automatically rule out a higher number of molecules in the actual nucleating cluster. Our analysis also suggests that combining data from several new particle formation events to scatter plots of H_2SO_4 vs. formation rates ($J_{1.5}$ or J_3) and determining the slope of the regression line may not give reliable information about the nucleation mechanism.

1 Introduction

Recent ion cluster measurements have indicated that atmospheric new particle formation via nucleation initiates at a cluster size of ~1.5 nm in diameter (Manninen et al., 2009). However, the majority of instruments measuring the size distribution of neutrally charged atmospheric aerosol can currently detect only particles larger than 3 nm. This limitation severely complicates the analysis of the first steps of new particle formation since an accurate quantification of nucleation rates at the initial cluster size and their dependence on the nucleating compounds would be crucially important for identifying the atmospheric nucleation mechanism(s).

Motivated by this, previous studies have developed a set of analysis tools to estimate the actual nucleation rate ($J_{1.5}$) based on the measured size distribution and gas phase data. The foundation of these tools, originally presented in Fiedler et al. (2005) and Sihto et al. (2006), lies in the observation that the diurnal profiles of sulphuric acid (H_2SO_4) concentration and nucleation mode particle concentration follow each other closely with a typical time shift of 0–4 h (Sihto et al., 2006; Riipinen et al., 2007; Kuang et al., 2008). Since H_2SO_4 is currently thought to be the key nucleating vapour, this time delay has been assumed as the time it takes for a cluster formed at 1–1.5 nm to grow to the detectable size of 3 nm. This assumption makes it possible to estimate the cluster growth rate below 3 nm and, together with information about the coagulation scavenging of the clusters to background particles, it can be used to estimate the fraction of formed clusters that survive to the detectable sizes (Kerminen and Kulmala, 2002; Lehtinen et al., 2007). This information is in turn used to extrapolate the actual nucleation rate at 1.5 nm ($J_{1.5}$) from the measured particle formation rate at 3 nm (J_3) (Kerminen and Kulmala, 2002).

The $J_{1.5}$ estimate has been used to provide information about the atmospheric nucleation mechanism. Based to the nucleation theorem, the exponent k in the equation

$$J_{1.5} = P \times [C]^k \tag{1}$$

is often interpreted as the number of vapour C molecules in the nucleating cluster (Oxtoby and Kashchiev, 1994). In the analysis of field measurements, the exponent linking $J_{1.5}$ and $[H_2SO_4]$ is typically found to be between 1 and 2 (Weber et al., 1996; Sihto et al., 2006; Riipinen et al., 2007; Kuang et al., 2008).

In this study, we test the validity of these commonly used nucleation event analysis tools and their ability to identify the correct nucleation mechanism by applying them to output from aerosol microphysics model simulations. In these simulations the nucleation mechanism as well as nucleation and new particle formation rates ($J_{1.5}$ and J_3, respectively) are known, and thus the predictions of the analysis tools can be directly evaluated.

2 Methods

2.1 Aerosol microphysics model

We used an aerosol microphysics box model to simulate new particle formation in a variety of atmospheric conditions. A fully moving sectional grid described the evolution of the particle size distribution through nucleation, condensation and coagulation. The pre-existing particle population at the beginning of the simulation was described with 100 sections, and a new section was created for the newly nucleated particles of diameter 1.5 nm at every nucleation time step (60 s). Since the new particle formation rate deviated from zero for 8 h during each run, the number of size sections at the end of simulation was 580.

The microphysical subroutines for condensation and coagulation were based on those in previously published UHMA model (Korhonen et al., 2004), which has been successfully used in studies of new particle formation (Grini et al., 2005; Tunved et al., 2006; Komppula et al., 2006; Vuollekoski et al., 2009; Sihto et al., 2009). To capture the growth of sub-3 nm particles accurately, condensation and coagulation were solved with a time step of 10 s when particles smaller than 4 nm in diameter were present;

otherwise the microphysical time step was 60 s (same as nucleation time step). These comparatively long time steps were chosen to balance the accuracy and computation time of the model, the latter of which is in a box model framework determined mainly by the number of size sections and the length of the time step in the coagulation routine.

Comparison to sensitivity simulations that used shorter time steps (10 s for all aerosol processes; or a 30-s nucleation time step with a 5-s microphysics time step) indicated that the chosen time steps do not lead to significant inaccuracy and that the simulated J_3 values are very close to the accurate solution.

Table 1 presents the parameters that were varied in the model simulations. We simulated four sulphuric acid nucleation mechanisms, i.e.

$$J_{1.5} = A \times [H_2SO_4] \tag{2}$$

$$J_{1.5} = K \times [H_2SO_4]^2 \tag{3}$$

$$J_{1.5} = T \times [H_2SO_4]^3 \tag{4}$$

$$J_{1.5} = Q \times [H_2SO_4]^4 \tag{5}$$

where A, K, T and Q are constant prefactors called nucleation coefficients. All four mechanisms were simulated with five different nucleation coefficients whose values covered two orders of magnitude (Table 1). For the first two mechanisms, which are often called activation and kinetic nucleation, the chosen ranges of nucleation coefficients are consistent with the reported values from field measurements (Riipinen et al., 2007; Kuang et al., 2008).

The concentration profile of the nucleating vapour H_2SO_4 was a down-facing parabola peaking at noon and departing from zero from 08:00 a.m. to 04:00 p.m. Another condensing vapour, a non-specified organic compound, had either a constant concentration profile throughout the simulation, or showed parabolic time behaviour with the same constraints as described above for H_2SO_4. The peak concentrations of both of these vapours were varied over approximately one order of magnitude.

Whereas H_2SO_4 was assumed totally non-volatile in all simulations, the organic vapour was given a saturation pressure in some of the model runs. All the simulations were carried out for three pre-existing aerosol distributions.

Altogether, this resulted in 3240 simulations. However, to ensure that the simulated events were strong enough to form a distinct nucleation mode, events for which J_3 did not reach the value $1\,\mathrm{cm^{-3}\,s^{-1}}$ at any point of the model run were excluded from further analysis. Furthermore, we excluded all events for which J_3 exceeded $100\,\mathrm{cm^{-3}\,s^{-1}}$. This is because such high new particle formation rates have never been observed during regional nucleation episodes (Kulmala et al., 2004). After applying these two criteria, 1464 events were left for further analysis.

In each simulation, the nucleation rate ($J_{1.5}$) was obtained from one of Eq. (2–5). New particle formation rate (J_3) was calculated at each microphysics time step as the sum of rates at which particles grew over the 3 nm threshold diameter due to coagulation and condensation. Of these two processes, coagulation was solved first.

The modelled size distribution, vapour concentrations as well as $J_{1.5}$ and J_3 values (both instantaneous and 10 min averages) were outputted every 10 min. In order to evaluate the analysis tools in conditions that resemble as much as possible atmospheric size distribution measurements, the size distribution in the range of 2.8–556 nm was regridded to 32 channels corresponding to the Differential Mobility Particle Sizer (DMPS) instrument at Hyytiälä measurement station in Southern Finland. This re-gridded data is hereafter referred to as *DMPS-gridded distribution* and it is the size distribution data used as input in the analysis below.

2.2 Baseline analysis of modelled events

Each simulated new particle formation event was analysed with the procedure commonly used to quantify nucleation rates and mechanisms from atmospheric measurement data. The baseline analysis follows for the most parts the methods outlined in Sihto et al. (2006), in addition to which we performed several sensitivity tests detailed in Sect. 2.3. The baseline analysis consisted of the following 5 steps:

1. The *time delay* $\Delta t_{N_{3-6}}$ was determined from the time shift between the N_{3-6} (number concentration of particles in the diameter range 3–6 nm) and $[H_2SO_4]^b$ curves ($0.1 \leq b \leq 10$). It was obtained by a fit searching a combination of the time delay and exponent b that maximized the correlation coefficient between the curves N_{3-6} and $[H_2SO_4]^b$. In the baseline analysis, the fitting was done over the whole time period when N_{3-6} was clearly above zero. The obtained time delay is interpreted as the time it takes for the newly formed clusters to grow to the detectable size of 3 nm.

2. The *particle formation rate at 3 nm* (J_3) was calculated from the DMPS-gridded distribution using the balance equation

$$J_3 = \frac{dN_{3-6}}{dt} + \text{CoagS}_4 \times N_{3-6} + \frac{1}{3\,\text{nm}} \text{GR}_6 \times N_{3-6}. \tag{6}$$

Here Coag_4 is the coagulation sink of 4 nm particles and was calculated from the simulated particle size distribution. The time derivative of N_{3-6} was obtained by fitting a parabola to the simulated N_{3-6} and by differentiating the obtained parabolic function. This approach is beneficial especially in the case of noisy field measurement data as it smoothes fluctuations in the N_{3-6} data and thus leads to a more stable derivative. The growth rate of 6 nm particles, GR_6, was assumed to be the same as that of newly formed clusters in the 1.5 to 3 nm size range. This growth rate can be estimated using equation

$$\text{GR}_{1.5-3} = \frac{1.5\,\text{nm}}{\Delta t_{N_{3-6}}}, \tag{7}$$

where Δt_{N3-6} is the time delay determined in step 1.

Evaluation of analysis tools for nucleation

H. Korhonen et al.

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

|◄ | ►|

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

3. The *actual nucleation rate at 1.5 nm ($J_{1.5}$)* was estimated from the analytical formula (Kerminen and Kulmala, 2002)

$$J_{1.5}(t) = J_3(t + \Delta t_{N3-6}) \times \exp\left(\gamma \frac{CS'}{GR}\left(\frac{1}{1.5\,nm} - \frac{1}{3\,nm}\right)\right), \tag{8}$$

where CS' is the condensation sink (in units m^{-2}) and Y is a coefficient with value 0.23 m^2 nm^2 h^{-1}. Here GR was again calculated using Eq. (7).

Note that Sihto et al. (2006) assumed, in accordance with the theoretical understanding of the time, that nucleation initiates at 1 nm and thus calculated J_1 values. However, improvements in measurement techniques in recent years have indicated that the likely diameter of critical clusters is ~1.5 nm and therefore this value is used in the current study.

4. The *best fit exponent b* was calculated by determining the highest correlation coefficient between the modelled $[H_2SO_4]^b (0.1 \leq b \leq 10)$ and modelled N_{3-6} or analysed $J_{1.5}$ (from Eq. 8). Note that for N_{3-6} the best fit exponent was determined simultaneously with time delay Δt_{N3-6} (see step 1). Based on the nucleation theorem, this best fit exponent is often interpreted as the number of H_2SO_4 molecules in a critical cluster.

5. The *nucleation coefficients A and K* for activation and kinetic type nucleation (as shown in Eqs. 2 and 3), respectively, were determined by a least square fit between the analysed $J_{1.5}$ given by Eq. (8) and modelled H_2SO_4 concentration to the power of 1 or 2. To double-check the obtained results, the same fitting for nucleation coefficients was done also for J_3. Here the J_3 estimated from sulphuric acid concentration (using Eq. (8) in the reverse direction) was optimized against J_3 obtained from DMPS-gridded data (Eq. 6). The *A* and *K* coefficient estimates from these two fits were typically almost identical and their mean value was taken as the nucleation coefficient presented below.

Evaluation of analysis tools for nucleation

H. Korhonen et al.

Note that the coefficients *A* and *K* were both fitted for *all* events irrespective of the simulated nucleation mechanism. This is because such fitting has been previously done for atmospheric data (Sihto et al., 2006; Riipinen et al., 2007; Kuang et al., 2008) without exact information about the nucleation mechanism. We will investigate both (a) how accurately the analysis predicts the coefficients when the assumption about the nucleation mechanism is correct, and (b) whether the correctness of the nucleation mechanism assumption affects the range of *A* and *K* values obtained from the fitting.

2.3 Sensitivity tests

The analysis tools outlined in Sect. 2.2 follow the procedure presented in Sihto et al. (2006). However, some of the other previous analyses of atmospheric new particle formation events have used slightly modified versions of these tools, and therefore their results may not be directly comparable to each other. For example, Kuang et al. (2008) calculated the time delay used in Eq. (7) by fitting only over the duration of the nucleation event (i.e. the increasing part of N_{3-6} curve) and concluded that their results were very sensitive to the length of the fitting time interval. Furthermore, they used slightly different versions of Eqs. (6) and (8) to calculate the new particle formation rate and actual nucleation rate. Riipinen et al. (2007), on the other hand, obtained the growth rate of 6 nm particles (GR_6) from lognormal fits to the DMPS data in the size range of 3–7 nm, instead of using the growth rate of 1 to 3 nm particles.

To test the sensitivity of the results to the assumptions of the procedure, the modelled events were reanalysed using the following three set-ups:

1. *Set-up Δt_{short}* tests how much the length of the interval over which Δt_{N3-6} is fitted affects the analysed results. We recalculated Δt_{N3-6} using two other definitions of fitting periods, i.e. fitting from the start of the event until one hour ($\Delta t_{\text{short\_1 h}}$) or two hours ($\Delta t_{\text{short\_2 h}}$) after the maximum N_{3-6} concentration was reached. Apart from the fitting interval, this set-up followed the procedure described in Sect. 2.2.

2. *Set-up d_{crit}* tests how sensitive the analysis is to knowing the exact size of the nucleating cluster. Previous analyses of field data have often assumed a 1 nm diameter for the critical cluster, whereas the most recent atmospheric measurements suggest a roughly 1.5 nm size. An incorrect assumption of the initial size affects the cluster growth rate calculation (Eq. 7) as well as the exponent term in Eq. (8). The analysis was repeated for two assumptions of the cluster size: 1 nm (d_{crit} = *1 nm*) and 2 nm (d_{crit} = *2 nm*). Note that the analysed model events were the same as in all the other set-ups (i.e. nucleation initiated at 1.5 nm size) and that in all other respects the set-up followed the procedure outlined in Sect. 2.2.

3. *Set-up Kuang* tests how sensitive the analysis is to the exact formulation of equations predicting J_3 and $J_{1.5}$. In this set-up, we used the formulations suggested by Kuang et al. (2008) (instead of Eqs. 6 and 8), i.e.

$$J_3 = \frac{1}{3 \, nm} GR_6 \times N_{3-6} \qquad (9)$$

and

$$J_{1.5}(t) = J_3(t + \Delta t_{N3-6}) \times \exp\left(\frac{1}{2}\frac{A_{Fuchs}}{GR}\sqrt{\frac{48k_bT}{\pi^2\rho}}\left(\frac{1}{\sqrt{1.5 \, nm}} - \frac{1}{\sqrt{3 \, nm}}\right)\right). \qquad (10)$$

Here k_b is the Boltzmann constant, T temperature, ρ aerosol particle density and A_{Fuchs} is the Fuchs surface area calculated from

$$A_{Fuchs} = \frac{16\pi D \times CS'}{c}, \qquad (11)$$

where c is the monomer mean thermal speed and D the vapour diffusivity. In all other respects, including the calculation of time delay Δt_{N3-6}, this set-up followed the procedure described in Sect. 2.2. Therefore it is important to note that this

26288

set-up does not strictly follow that of Kuang et al. (2008) since we calculate the time delay Δt_{N3-6} over the whole peak of N_{3-6} whereas they calculated it only over the ascending part of N_{3-6}.

The performance of the set-ups was measured by calculating (1) the fraction of analysed events for which the estimated quantity is not within a factor of two of the accurate simulated value (approximate measure of the *relative* accuracy of the set-ups), (2) the normalised mean absolute error

$$\text{NMAE} = 100\% \times \frac{\sum |A_i - S_i|}{\sum S_i} \tag{12}$$

and (3) the normalised mean bias

$$\text{NMB} = 100\% \times \frac{\sum (A_i - S_i)}{\sum S_i}, \tag{13}$$

where A_i is the analysed value and S_i is the actual simulated value in case i. We use NMAE as a measure of the *absolute* accuracy of the set-ups and NMB as an indicator of low or high bias (i.e. overall under- or overestimation).

3   Results

3.1   Time delay Δt_{N3-6} and cluster growth rate

The cluster growth rate (Eq. 7) was calculated from the time delay between N_{3-6} and $[H_2SO_4]^b$ profiles. This approach assumes that N_{3-6} follows $[H_2SO_4]^b$ with a time shift Δt_{N3-6}, which is the case if the growth from initial nucleation size to 3 nm were dominated by condensation with a constant growth rate and if the coagulation sink of the clusters remained fairly constant for the duration of the event.

However, our aerosol model simulations indicate that the time delay approach can be problematic in the case of strong particle formation events that produce a high concentration of nucleation mode particles. This is because the nucleation mode (i.e.

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

◄ | ►

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

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first formed clusters that have grown to detectable sizes above 3 nm) can act as a significant additional coagulation sink for the small clusters that form later during the event and thus prevent their growth to 3 nm. As a result, the N_{3-6} peak can be skewed to earlier in the day than in a case of purely condensation controlled formation of N_{3-6}, and can in some cases occur at the same time or before the H_2SO_4 peak.

Figure 1 depicts one such case for activation nucleation. The H_2SO_4 concentration, and thus the nucleation rate $J_{1.5}$, peak at noon (red solid line). The initial increase in N_{3-6} (blue solid line) starts about 20 min after the increase in H_2SO_4; however, due to the additional coagulation sink from the growing nucleation mode, N_{3-6} peaks about 35 min before H_2SO_4. When fitting over the whole N_{3-6} peak (i.e. roughly 08:30 a.m. to 05:00 p.m.), an optimum fit between N_{3-6} and $[H_2SO_4]^b$ is now obtained with a *negative* time delay.

All in all, the analysis yielded a zero or negative time delay for 15.3% of the 1464 analysed events. For these events the growth rate of the clusters could not be es- timated using Eq. (7). For the case depicted in Fig. 1, we tried approximating the cluster growth rate with that of the nucleation mode in the detectable size region. This growth rate was obtained by fitting lognormal modes to the DMPS-gridded data in the size range of 3–7 nm (Riipinen et al., 2007). Figure 1 shows this approach was not able to predict the timing or the magnitude of J_3 and $J_{1.5}$ curves correctly (black and red dashed lines, respectively). This is because during strong particle formation events self-coagulation can significantly increase the growth rate of clusters smaller than 3 nm, while this effect is much weaker for larger nucleation mode particles. Therefore, using the growth rate of 3–7 nm particles underestimates the growth rate of sub-3 nm clus- ters, which can be seen from the later appearance of the $J_{1.5}$ estimate peak compared to the actual $J_{1.5}$. The underestimated cluster growth rate explains also the overestima- tion of the analysed $J_{1.5}$ peak value. The slower the clusters grow, the larger fraction of them is scavenged by coagulation before reaching the detectable size range. Thus when the growth rate is underestimated, Eq. (8) overcorrects for the coagulation loss and yields too high an estimate for $J_{1.5}$.

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

|◄ | ►|

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Since the cluster growth rate could not be reliably established for events for which the time delay Δt_{N3-6} was zero or negative, we excluded these events from further analysis. As a result, the final analysis below consists of 1239 simulated events, out of which 289 are based on the nucleation mechanism represented by Eq. (2) (activation nucleation), 362 on that by Eq. (3) (kinetic nucleation), 334 on that by Eq. (4), and 254 on that by Eq. (5). Note that this set of events may still include cases in which coagulation of the clusters to the growing nucleation mode skews the N_{3-6} curve as long as the time delay remains positive. In these cases the time delay is underestimated and the growth rate calculated from it is an overestimate of the simulated growth rate.

Following Sihto et al. (2006), we made the time delay fitting over the whole N_{3-6} peak. However, Kuang et al. (2008) found that their analysis of atmospheric new particle formation events was highly sensitive to the time period over which the time delay was fitted. Therefore, we repeated the fitting procedure for two other fitting periods: until one hour or two hours after the maximum N_{3-6} concentration (*set-ups* $\Delta t_{\text{short}-1\,\text{h}}$ and $\Delta t_{\text{short}-2\,\text{h}}$, respectively). The baseline analysis and set-up $\Delta t_{\text{short}-2\,\text{h}}$ gave the same time delay in 67.2% of the 1239 analysed cases. In all other cases apart from 18 events, the baseline analysis gave a longer time delay (maximum difference 30 min when using 10 min increments) and thus predicted a slower growth rate than the sensitivity set-up. On the other hand, out of the 18 events when the baseline line analysis gave a shorter time delay, the difference in the predicted time delays was over 30 min in 5 cases. Further shortening the fitting period to one hour after the maximum N_{3-6} concentration reduced the percentage of identical time delays to 34.4%. For the non-identical events, the baseline analysis gave again longer time delays apart from 25 cases. However, even now the absolute difference from the baseline analysis was ≤30 min in all but 39 cases (maximum difference 3 h 10 min).

It should be noted that even relatively small changes in time delay can lead to large changes in growth rate and thus deteriorate the predictions of $J_{1.5}$ and J_3. Unfortunately, it is impossible to give a general recommendation on the optimal length of the fitting period. A comparison of the actual simulated mean growth rates to those

from the time delay analysis in 67 activation nucleation cases revealed that any of the three fitting periods (baseline, $\Delta t_{\text{short}-1\,\text{h}}$ or $\Delta t_{\text{short}-2\,\text{h}}$) can give the most accurate, or alternatively a clearly inaccurate, growth rate estimate depending on the simulation conditions. Overall, however, the shortest fitting period ($\Delta t_{\text{short}-1\,\text{h}}$) gave worse growth rate estimates than the other two periods. Furthermore, the time delay between J_3 and H_2SO_4 curves (Δt_{J_3}) should not be used to estimate the cluster growth rate as it systematically overestimates the growth.

3.2 Nucleation and new particle formation rates, $J_{1.5}$ and J_3

Next, we tested how well Eqs. (6) and (8) capture the simulated event mean values of new particle formation (J_3) and nucleation rates ($J_{1.5}$), respectively. Figure 2a shows that the predictions of J_3 are fairly accurate with 81.8% of all events within a factor-of-two margin of the accurate value in the baseline analysis. There is, however, a tendency to overestimate the mean formation rate J_3, especially at the high end of the particle formation rates. Analysing one simulated event in detail, Vuollekoski et al. (2010) concluded that the single most significant factor deteriorating the prediction of J_3 is the poor approximation of the size distribution function at 6 nm in the last right-hand term of Eq. (6), i.e.

$$n_6 = \left.\frac{\partial N}{\partial d_p}\right|_{d_p = 6\,\text{nm}} \approx \frac{N_{3-6}}{3\,\text{nm}}. \tag{14}$$

Following the suggestion of Vuollekoski et al. (2010), we reanalysed the new particle formation rates replacing Eq. (14) with

$$n_6 \approx \frac{N_{5-7}}{2\,\text{nm}} \tag{15}$$

and thus using for the particle formation rate the equation

$$J_3 = \frac{dN_{3-6}}{dt} + \text{CoagS}_4 \times N_{3-6} + \frac{1}{2\,\text{nm}}\text{GR} \times N_{5-7} \tag{16}$$

where N_{5-7} is the number concentration of particles in the diameter range 5–7 nm. This formulation improves our predictions of mean J_3 significantly with only 2.8% of events not falling within a factor of 2 of accurate values (compared to 18.2% in the baseline analysis, Table 2). We therefore recommend using Eq. (16) over Eq. (6) in all future analyses of new particle formation; however, to be consistent with previous analyses of field data (Sihto et al., 2006; Riipinen et al., 2007), we continue to use Eq. (6) throughout the remainder of this study.

As could be expected, the mean nucleation rate ($J_{1.5}$) is predicted less accurately than J_3 (Fig. 2b) with 40.8% of the events falling outside a factor-of-two margin of the simulated rate in the baseline analysis. Furthermore, the nucleation rate is underestimated by over an order of magnitude in 77 cases (6.2% of all events). Note that the largest discrepancies in $J_{1.5}$ are underestimates, while the opposite is true for J_3. Therefore, improvements in the prediction of J_3 are likely to deteriorate the overall $J_{1.5}$ prediction using Eq. (8). For example, the use of Eq. (16), which improves the J_3 analysis, increases the fraction of $J_{1.5}$ values outside a factor of 2 range from 40.8% to 46.2% (Table 2).

The reason for the poorer prediction capability of $J_{1.5}$ lies in the built-in assumptions of Eq. (8). It is assumed that (1) intramodal coagulation in the nucleation mode is negligible, and (2) growth rate between 1.5 and 3 nm is constant. The former has been found a good assumption as long as $J_{1.5}/Q < 10^{-2}$, where Q is the formation rate of condensable vapours (Anttila et al., 2010). In our simulations this corresponds roughly to cases in which $J_{1.5}$ is less than $10^2 - 10^3$ cm^{-3} s^{-1}. Neglecting self-coagulation in Eq. (8) leads in theory to underestimation of $J_{1.5}$, which is consistent with the results in Fig. 2b at high nucleation rates when the effect should be the strongest. Note, however, that the majority of the very strong nucleation events were excluded from the analysis in Sect. 2.1 due to unrealistically high J_3 values and in Sect. 3.1 due to negative time delays.

On the other hand, the assumption of a constant growth rate in the size range 1.5–3 nm is never strictly true. For non-volatile vapours such as H_2SO_4, molecular effects

lead to an enhancement of condensation flux in the smallest particle sizes (Lehtinen and Kulmala, 2003; Sihto et al., 2009). For vapours whose saturation pressure deviates from zero (such as the organic vapour in most of our simulations), the Kelvin effect works in the opposite direction and decreases the growth rate of the smallest clusters. Furthermore, in our simulations the condensing vapour concentration is not constant, but H_2SO_4 has a parabolic time profile in all and the organic vapour in half of the simulations. These factors lead to a significant deviation from the constant growth rate assumption. Since the coagulation loss rate of the formed clusters is strongly dependent on their size, lowered growth rate right after their formation leads to faster scavenging and thus to a smaller fraction of clusters that survive to the detectable size, and vice versa.

Table 2 summarises the performance of the sensitivity tests. All but the *Kuang* set-up give fairly large positive normalized mean bias (NMB) values for J_3, i.e. generally overestimate the mean new particle formation rate. *Set-up Kuang* gives clearly lower normalised mean absolute error (NMAE) and NMB values (55.3% and –20.4%, respectively) compared to the baseline analysis (68.5% and 66.4%, respectively) but performs the worst out of all the set-ups in terms of events that are predicted within factor of 2 accuracy (56.7% of cases not meeting this criterion). This apparent discrepancy is due to the fact that the set-up underpredicts especially the lowest formation rates ($<2\,\mathrm{cm}^{-3}\,\mathrm{s}^{-1}$) for which the absolute difference in analysed and simulated values (which is used to calculate NMAE and NMB) is very small. Shortening the fitting time window (*set-ups* $\Delta t_{\text{short}-2\,\text{h}}$ and $\Delta t_{\text{short}-1\,\text{h}}$) deteriorates the accuracy of the results, especially in terms of absolute error and bias. On the other hand, the assumption of the critical cluster size has an even larger effect. Assuming a too small initial cluster size (*set-up d_{crit} = 1 nm*) clearly deteriorates and a too large cluster size (*set-up d_{crit} = 2 nm*) clearly improves the estimate. This is because the baseline set-up tends to overestimate J_3 and thus sensitivity set-ups, such as *set-up d_{crit} = 2 nm*, that underestimate the growth rate (and thus the last term of Eq. 6) lead to more accurate prediction, and vice versa.

The actual nucleation rate $J_{1.5}$ is captured most accurately in the baseline analysis and *set-up* $\Delta t_{short\_2\,h}$ (Table 2). Further shortening the fitting time window (set-up $\Delta t_{short\_1\,h}$) or using Eq. (16) instead of Eq. (6) to calculate J_3 slightly increase both the absolute and relative errors. On the other hand, the other set-ups perform clearly poorer especially in terms of events that are captured within a factor-of-2 accuracy. Note that the incorrect assumption that nucleation initiates at 1 nm size (*set-up d_{crit} = 1 nm*) leads generally to overestimation (i.e. positive NMB) of mean nucleation rate (in this sensitivity case assumed to be J_1 instead of $J_{1.5}$), while all the other set-ups tend to underestimate the actual nucleation rate. This is because *set-up d_{crit} = 1 nm* overestimates the size range that the cluster needs to grow to become detectable and thus overestimates the scavenging of sub-3nm particles. As a result, Eq. (8) overcorrects for the coagulation loss and thus leads to an overestimation of the nucleation rate.

3.3 Nucleation mechanism

Previous analyses of field data have used the method of least squares or calculated correlation coefficients between $N_{3-6} \sim [H_2SO_4]^b$ (Sihto et al., 2006; Riipinen et al., 2007) or $J_{1.5} \sim [H_2SO_4]^b$ (Kuang et al., 2008; Riipinen et al., 2007), and interpreted the exponent b giving the best fit as the number of sulphuric acid molecules in the critical cluster. Therefore, for example exponents falling close to 1 or 2 have been taken as evidence for activation and kinetic nucleation, respectively. Here we test the approach separately for the four simulated nucleation mechanisms.

Figure 3 shows the frequency distribution of the best fit exponents that were obtained in the baseline analysis by calculating the highest correlation coefficient between N_{3-6} and $[H_2SO_4]^b$ profiles ($0.1 \le b \le 10$). It is evident that for the majority of the events the analysis yields exponents that are clearly higher than the number of H_2SO_4 molecules in the critical cluster. Depending on the nucleation mechanism, only in 17.3–25.1% of the events the predicted exponent falls into the roughly correct range (defined here as $k \pm 0.5$, where k is the simulated nucleation exponent) (Table 3). On the other hand, in

58.7–82.7% of cases the exponent is overestimated. This result is consistent with the modelling study of Sihto et al. (2009) which found that the size dependence of the sub-3 nm particle growth rate often skews the best fit exponent for $N_{3-6} \sim [H_2SO_4]^b$ high. Shortening the period over which the time delay is calculated (*set-up* Δt_{short}) shifts the predicted exponents to even higher values and thus deteriorates the analysis results (Table 3).

Figure 4 shows the frequency distribution for the best exponent fit between analysed $J_{1.5}$ (from Eq. 8) and simulated $[H_2SO_4]^b$ profiles ($0.1 \leq b \leq 10$) in the baseline analysis. Again, the analysis tends to overestimate the nucleation exponent, and places only 19.1–33.2% of the events in the correct exponent range. Now, however, also the fraction of underestimated exponents is significant at 10.7–41.3% (Table 4). Overall, the results are not very sensitive to the length of the fitting period or the assumption of the initial cluster size (Table 4). However, using the analysis equations in *set-up Kuang* (i.e. Eqs. 9 and 10 instead of Eqs. 6 and 8) shifts the distribution of best fit exponents significantly to larger values. Using this set-up, 56.3–82.4% of the cases are overestimated and the fraction of events for which the exponent is predicted correctly either decreases or increases depending on the nucleation mechanism (Table 4). Note that our *set-up Kuang* differs from the baseline analysis only with respect to the equations used to calculate J_3 and $J_{1.5}$. Therefore, the higher nucleation exponents found in Kuang et al. (2008) compared to some other analyses (Sihto et al., 2006; Riipinen et al., 2007) are likely to be partly due to the different analysis equations used and not only the chosen fitting period.

Several points are worth noting: first, fitting $J_{1.5} \sim [H_2SO_4]^b$ gives overall more accurate results than $N_{3-6} \sim [H_2SO_4]^b$ despite the fact that $J_{1.5}$ is estimated using Eq. (8), which has several potential error sources, whereas N_{3-6} is obtained directly from measurement data. Second, some previous studies have classified events based on the correlation coefficients of $N_{3-6} \sim [H_2SO_4]$ and $N_{3-6} \sim [H_2SO_4]^2$ (or $J_{1.5} \sim [H_2SO_4]$ and $J_{1.5} \sim [H_2SO_4]^2$) so that larger coefficient for the former is interpreted as activation nucleation and for the latter kinetic nucleation (Sihto et al., 2006; Riipinen et al., 2007).

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If this classification were applied to the events analysed here using N_{3-6}, 82.7% of the activation events would be classified kinetic. Using $J_{1.5}$, on the other hand, would classify 56.1% of activation events as kinetic and 19.1% of kinetic events as activation. Third, Tables 3 and 4 show that under some conditions the best fit correlation exponent gives too low a number of molecules in the critical cluster. Therefore, field data that typically shows correlation exponents in the range 1–2 do not automatically rule out more than two sulphuric acid molecules in a critical cluster.

In this study, we followed the procedure of Sihto et al. (2006) and determined the best fit exponents b based on the highest correlation coefficient. In some of the analysed cases several exponent values gave very similar correlation coefficients, thus complicating the determination of the best fit. In their modelling study, Sihto et al. (2009) attributed this to the smoothness of the simulated curves. Figure 5, which illustrates three nucleation events each simulated using nucleation mechanism $J_{1.5} = Q \times [\text{H}_2\text{SO}_4]^4$ (Eq. 5), shows however that the flat peak of a correlation coefficient curve is typically a problem only in cases for which the best fit exponent is significantly overestimated (blue line), whereas in cases that are classified correctly (red line) or underestimated (black line) the curve has a distinct peak. Furthermore, even in the case of the flat curve (blue line) the correct exponent, i.e. $b = 4$, has a clearly lower correlation coefficient than the curve maximum.

Since the correlation method does not actually minimise the difference between the curves being fitted, we recalculated the time shift Δt_{N3-6} and best fit exponents applying the method of least-squares. With this method, we minimised the difference between the N_{3-6} and $[\text{H}_2\text{SO}_4]^b$ curves with respect to the exponent b and time delay Δt_{N3-6}, and between the $J_{1.5}$ and $[\text{H}_2\text{SO}_4]^b$ curves with respect to the exponent b. The results obtained for the best fit exponents were very similar to those using the correlation method (not shown), and therefore we do not expect the chosen fitting method to affect the conclusions of this study.

In addition to examining individual new particle formation events, previous studies have searched for indications of the nucleation mechanism by plotting several events

in a logarithmic plot of H_2SO_4 versus $J_{1.5}$ or of H_2SO_4 versus J_3 (Sihto et al., 2006; Riipinen et al., 2007; Kuang et al., 2008). The slope of the regression line drawn to such plot has been thought to give the number of H_2SO_4 molecules in the critical cluster.

For the modelled data, we find that the obtained slope is very sensitive to the subset of events plotted. However, typical features for consistently selected subsets from the four nucleation mechanisms are that (1) the slope increases with the number of H_2SO_4 molecules in the simulated critical cluster, and (2) the slope may correspond quite closely to the simulated cluster molecule number for one or two of the mechanisms, but not for all four. As an example, Fig. 6 shows the H_2SO_4 versus $J_{1.5}$ plots separately for the four nucleation mechanisms but only for events that were simulated using the middle value of the five nucleation coefficients (Table 1) and assuming a non-volatile organic compound. While the obtained slope represents well the number of H_2SO_4 molecules in the critical cluster in the case of activation nucleation (slope 1.1 versus 1 simulated molecule), for all the other nucleation mechanisms the slope clearly under-estimates the critical cluster size (slope 1.6 versus 2 simulated molecules, 2.1 versus 3, and 2.6 versus 4). On the other hand, taking into account only events with the same nucleation coefficient but assuming that the organic saturation pressure is $10^5 \, cm^{-3}$, gives slopes 2.9, 3.4, 3.6 and 4.1 for the four mechanisms, respectively. Furthermore, calculating the slope for all events of a certain nucleation type gives slopes 1.4, 1.9, 2.2 and 2.6, respectively.

It is possible that the slope analysis using measured field data is not as sensitive to the selection of the subset of events as the analysis of modelled data. This is because at a given location it is likely that many of the environmental conditions, such as the condensing organic vapour properties (e.g., saturation pressure) and approximate level of background condensation sink, are relatively constant during nucleation event days. Furthermore, the fact that the modelled sulphuric acid concentration follows one of three prescribed parabolas limits the scatter of H_2SO_4 in model-based plots such as Fig. 6 (resulting in vertical stripes), which may affect the slope from the modelled

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

◄◄ | ►►

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

data. Despite these differences between the field and modelled data, our analysis suggests that the slopes from H_2SO_4 versus $J_{1.5}$ or of H_2SO_4 versus J_3 plots should be interpreted with caution also in the case of field data.

3.4 Nucleation coefficients A and K

Finally, Fig. 7 compares the simulated nucleation coefficients A and K for activation and kinetic type nucleation (Eqs. 2 and 3) to the coefficients obtained by determining the best fit between analysed $J_{1.5}$ and simulated $[H_2SO_4]$ or $[H_2SO_4]^2$ concentration profiles. In this figure the events are classified to activation and kinetic types according to the simulated (i.e. known) nucleation mechanism and *not* based on the classification given by the analysis (see Sect. 3.3).

For activation nucleation (Fig. 7a), the analysis estimates the coefficient A within a factor of 2 from the correct simulated value in 72.3% of the cases. Coefficient K for kinetic nucleation is analysed less accurately with only 55.5% of the events within a factor of 2 (Fig. 7b). On the other hand, the coefficients are off by more than an order of magnitude in 4.8% of activation and 8.0% of kinetic events. The largest discrepancies are seen for the highest nucleation coefficients. As expected, these results follow closely those of analysed $J_{1.5}$ (Sect. 3.2) that they were calculated from. The most accurate results are given by the baseline analysis and *set-up* Δt_{short}, although the NMAE and NMB values for *set-up* $\Delta t_{short-1\,h}$ are deteriorated by 6 events whose absolute A value is greatly overestimated (Table 5). The other three set-ups give clearly poorer estimates, especially in terms of relative error, i.e. events outside a factor of 2 from the actual simulated nucleation coefficient. Apart from estimation of A coefficient with *set-up* $\Delta t_{short-1\,h}$, *set-up* d_{crit} = *1 nm* is the only one that generally leads to overestimation of coefficients (positive NMB). The reason for this behaviour is given in Sect. 3.2.

Note that in the atmosphere the actual nucleation mechanism is *not* known during the new particle formation analysis. However, A and K coefficients have still been calculated from the atmospheric data. Our results indicate that the range of nucleation coefficients obtained from the analysis is not highly dependent on the correctness of the

nucleation mechanism assumption. The range of analysed A coefficients for *all* events (regardless of the simulated mechanism) was 8.4×10^{-8}–7.0×10^{-5} s^{-1}, whereas for the subset of activation type events following Eq. (2) it was 8.4×10^{-8}–1.3×10^{-5} s^{-1} (actual simulated range 10^{-7}–10^{-5} s^{-1}). Similarly, the range of analysed K coefficients for *all* events was 5.7×10^{-15}–1.4×10^{-11} cm^3 s^{-1}, whereas for the subset of kinetic type events following Eq. (3) it was 1.9×10^{-14}–1.0×10^{-11} cm^3 s^{-1} (actual simulated range 10^{-13}–10^{-11} s^{-1}).

4 Conclusions

We have evaluated the accuracy of the mathematical tools commonly used to anal-yse atmospheric new particle formation events in 1239 cases in which the nucleation mechanism and rate as well as the particle formation rate at 3 nm were known. The simulated particle size distributions in the range 2.8–556 nm were gridded to a typical size and time resolution of DMPS instruments (i.e. 32 size channels and 10 min in-tervals) in order to mimic the analysis of atmospheric nucleation events as closely as possible.

We find that calculating the growth rate of sub-3 nm clusters from the time delay between H$_2$SO$_4$ and N_{3-6} curves can lead to overestimation of the growth rate during strong particle formation events. This is because coagulation scavenging of the formed clusters to the growing nucleation mode can skew the N_{3-6} peak to earlier in the day. In extreme cases this can lead to apparent negative time delays; however, more prob-lematic for the analysis are the cases in which the time delay remains positive but is shortened compared to time delay corresponding to the actual growth rate. It is there-fore recommended to exclude from the analysis events during which the coagulation sink caused by the nucleation mode is not negligible compared to the background sink.

The time delay obtained from the analysis was in many cases sensitive to the period over which it was fitted. While the differences in the estimates from the three fitting intervals in this study (over whole N_{3-6} peak, or from event start until 1 or 2 h after the N_{3-6} maximum concentration) were ≤30 min in all but 24 cases, the corresponding

differences in growth rates were as high as 7.5 nm/h. While it is impossible to make a general recommendation on the optimal length of the fitting period, our overall results indicate that the fitting period should be extended to well at least two hours after the N_{3-6} peak. On the other hand, the time delay between J_3 and H_2SO_4 curves (Δt_{J_3}) should not be used to estimate the cluster growth rate as it systematically overestimates the growth.

The new particle formation rate at 3 nm (J_3) was estimated most accurately in terms of both relative and absolute error with the formulation of Vuollekoski et al. (2010). We recommend this formulation to be used in all future analyses of new particle formation, with the reservation that improving J_3 estimates tends to deteriorate the analysis of actual nucleation rates ($J_{1.5}$). In our study, the accuracy of the $J_{1.5}$ analysis was only satisfactory with 37–59% of events within a factor-of-two of the simulated value. The main factors deteriorating the estimates were the assumption of a constant cluster growth rate (currently made in all formulations) and possible erroneous assumptions concerning the initial size at which nucleation occurs. It is worth noting that several previous analyses of field measurements have assumed nucleation to initiate at 1 nm size, whereas recent ion instrument data suggests a size ∼1.5 nm. In our analysis, this erroneous assumption in initial cluster size increased the normalised mean absolute error (NMAE) from 65% to 135% and biased the nucleation rate values high (whereas a correct assumption about the size biased the rates low). It is therefore possible that the nucleation coefficients A and K derived in previous analyses of field data (Sihto et al., 2006; Riipinen et al., 2007; Kuang et al., 2008) overestimate the atmospheric values. On the other hand, all the analysis set-ups tested in this study resulted to an order-of-magnitude accuracy for at least 93% of the A coefficients and 89% of K coefficients. This can be considered a reasonable accuracy since the coefficients derived from atmospheric data typically exhibit a variation of 1–3 orders of magnitude (Riipinen et al., 2007). Thus, it is likely that this high variation of observed A and K coefficients is not a consequence of inaccuracies in the analysis methods, but a real phenomenon caused by (so far unknown) environmental factors.

Large uncertainties were found when the analysis tools were used to determine the nucleation mechanism in terms of the number of H_2SO_4 molecules in a critical cluster. When applied to individual events, the best fit exponents from both $N_{3-6} \sim [H_2SO_4]^b$ and $J_{1.5} \sim [H_2SO_4]^b$ fittings were generally clearly higher than the actual number of H_2SO_4 molecules in the simulated critical cluster in the majority of the cases. Out of the two fitting approaches, the exponents from the N_{3-6} fit were higher and thus typically more biased. Decreasing the length of the fitting period or using the analysis equations of Kuang et al. (2008) led to further overestimation of the nucleation exponent. This indicates that the higher exponents found in Kuang et al. (2008) compared to some other analyses (Sihto et al., 2006; Riipinen et al., 2007) may in part be due to different analysis equations, and not only to the chosen fitting period. Although our results suggest that in general the analysis tools tend to overestimate the number of H_2SO_4 molecules in the critical cluster, also significant underestimation was found in up to 41% of the cases. This indicates that one cannot automatically rule out more than 2 sulphuric acid molecules in a critical cluster even if field data shows nucleation exponents in the range 1–2.

Despite the general overestimation of nucleation exponents for individual events, the regression lines drawn to logarithmic plots of $J_{1.5}$ versus H_2SO_4 of several events tend to underestimate the number of molecules in the critical cluster. However, we found the accuracy of the regression line analysis to be highly sensitive to the analysed subset of simulated events. It is not currently known how well this sensitivity of the modelled data reflects the situation with the field data. Overall, however, we conclude that interpretation of nucleation mechanism from $J_{1.5} \sim [H_2SO_4]^b$, $N_{3-6} \sim [H_2SO_4]^b$ and regression line analyses contain many potential sources of error and should be done with great caution also for field measurements.

Finally, it should be noted that this study investigated only the errors resulting from the mathematical analysis tools and used smooth simulation data as an input. In typical atmospheric measurements, on the other hand, variations in atmospheric conditions and in air mass directions as well as the measurement instruments themselves result

in significant noise in the data. This noise is likely to cause further uncertainty in the analysis of atmospheric new particle formation events.

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Evaluation of analysis tools for nucleation

H. Korhonen et al.

Title Page

Abstract	Introduction
Conclusions	References
Tables	Figures

|◄ | ►|

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

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Evaluation of analysis tools for nucleation

H. Korhonen et al.

Title Page

Abstract	Introduction
Conclusions	References
Tables	Figures

|◄ | ►|

◄ | ►

| Back | Close |

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Table 1. Parameters used in the model simulations.

H_2SO_4 concentration at noon (cm^{-3})		4×10^6	8×10^6	1.6×10^7	
Organic vapour					
concentration profile		constant	parabola		
concentration at noon (cm^{-3})		2×10^6	10^7	5×10^7	
saturation pressure (cm^{-3})		0	10^5	10^6	
Pre-existing condensation sink (s^{-1})		1.8×10^{-3}	5.4×10^{-3}	1.1×10^{-2}	
Nucleation exponent (k)*	1	2	3	4	
Prefactor (P)*					
A (s^{-1})	10^{-7}	5×10^{-7}	10^{-6}	5×10^{-6}	10^{-5}
K (cm^3 s^{-1})	10^{-13}	5×10^{-13}	10^{-12}	5×10^{-12}	10^{-11}
T (cm^6 s^{-1})	10^{-20}	5×10^{-20}	10^{-19}	5×10^{-19}	10^{-18}
Q (cm^9 s^{-1})	10^{-26}	5×10^{-26}	10^{-25}	5×10^{-25}	10^{-24}

* Nucleation rate is expressed as $J_{1.5} = P \times [H_2SO_4]^k$. In Eq. (2), P corresponds to A and $k = 1$. In Eq. (3), P corresponds to K in and $k = 2$. In Eq. (3), P corresponds to T in and $k = 3$. In Eq. (3), P corresponds to Q in and $k = 4$.

Table 2. Performance metrics for the different analysis set-ups when estimating the mean new particle formation (J_3) and actual nucleation rates (J_{nuc}). The columns show the percentage of analysed events for which the estimate is not within a factor of two of the simulated rate (> factor 2), the normalised mean absolute error (NMAE) and the normalised mean bias (NMB). Note that in sensitivity *set-ups d_{crit} = 1 nm* and *d_{crit} = 2 nm* the analysis tool calculates J_1 and J_2, respectively, and these values are compared to the simulated $J_{1.5}$.

	J_3			$J_{1.5}$		
	> factor 2 (%)	NMAE (%)	NMB (%)	> factor 2 (%)	NMAE (%)	NMB (%)
baseline	18.2	68.5	66.4	40.8	65.5	−60.0
Eq. (6) → 16	2.8	31.3	17.8	46.2	71.4	−68.9
Δt_{short_2h}	21.5	80.6	78.6	41.5	66.3	−62.2
Δt_{short_1h}	26.0	96.6	94.3	45.1	78.8	−58.3
d_{crit} = 1 nm	25.3	92.7	91.8	63.2	134.5	84.1
d_{crit} = 2 nm	9.9	46.1	41.1	60.5	80.5	−80.4
Kuang	56.7	55.3	−20.4	55.1	76.8	−76.1

Table 3. Accuracy of best fit exponent b calculations when correlating $N_{3-6} \sim [H_2SO_4]^b$. The accuracy is given as percentage (%) of analysed events in each of the following three classes: events for which the analysis predicts roughly the correct nucleation mechanism ($k - 0.5 \leq b \leq k + 0.5$, where k is the nucleation exponent in the simulation and b is the best fit exponent from the analysis); events for which the exponent is clearly underestimated ($b < k - 0.5$); and events for which the exponent is clearly overestimated ($b > k + 0.5$).

	roughly correct $(k - 0.5 < b < k + 0.5)$	underestimated $(b < k - 0.5)$	overestimated $(b > k + 0.5)$
baseline			
$k = 1$	17.3	0.0	82.7
$k = 2$	24.3	0.0	75.7
$k = 3$	25.1	11.1	63.8
$k = 4$	23.2	18.1	58.7
$\Delta t_{\text{short\_2h}}$			
$k = 1$	9.0	1.7	89.3
$k = 2$	14.6	0.0	85.4
$k = 3$	24.0	4.8	71.3
$k = 4$	18.9	15.0	66.1
$\Delta t_{\text{short\_1h}}$			
$k = 1$	5.5	6.6	87.9
$k = 2$	7.7	1.1	91.2
$k = 3$	18.9	1.2	79.9
$k = 4$	13.8	5.1	81.1

Table 4. Accuracy of best fit exponent b calculations when correlating $J_{1.5} \sim [H_2SO_4]^b$. The accuracy is given as percentage (%) of analysed events in the same three classes as in Table 3.

	roughly correct $(k - 0.5 < b < k + 0.5)$	underestimated $(b < k - 0.5)$	overestimated $(b > k + 0.5)$
baseline			
$k = 1$	33.2	10.7	56.1
$k = 2$	19.1	19.1	61.9
$k = 3$	31.1	29.0	39.8
$k = 4$	20.1	41.3	38.6
$\Delta t_{\text{short\_1 h}}$			
$k = 1$	24.2	5.5	70.2
$k = 2$	19.9	10.8	69.3
$k = 3$	28.4	21.3	50.3
$k = 4$	24.4	31.5	44.1
$d_{\text{crit}} = 1$ nm			
$k = 1$	35.6	6.6	57.8
$k = 2$	19.1	17.1	63.8
$k = 3$	30.5	25.7	43.7
$k = 4$	19.3	39.4	41.3
$d_{\text{crit}} = 2$ nm			
$k = 1$	31.1	13.5	55.4
$k = 2$	21.5	20.2	58.3
$k = 3$	30.5	31.7	37.7
$k = 4$	19.3	43.7	37.0
Kuang			
$k = 1$	17.6	0.0	82.4
$k = 2$	26.0	0.0	74.0
$k = 3$	26.9	11.4	61.7
$k = 4$	24.4	19.3	56.3

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

|◄ | ►|

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Table 5. Performance metrics for the different analysis set-ups when estimating the nucleation factor A for activation events and factor K for kinetic events. The columns show the percentage of analysed events for which the estimate is not within a factor of two of the simulated rate (> factor 2), the normalised mean absolute error (NMAE) and the normalised mean bias (NMB).

	A			K		
	> factor 2 (%)	NMAE (%)	NMB (%)	> factor 2 (%)	NMAE (%)	NMB (%)
baseline	27.7	45.8	−40.0	44.5	64.0	−61.1
$\Delta t_{\text{short\_2h}}$	29.8	47.3	−41.8	47.5	65.1	−62.8
$\Delta t_{\text{short\_1h}}$	37.0	249.2	151.4	49.7	67.8	−66.2
$d_{\text{crit}=1\,\text{nm}}$	51.2	96.5	73.8	61.6	85.8	25.0
$d_{crit=2\,nm}$	46.4	64.1	−64.1	65.5	78.6	−78.6
Kuang	57.4	67.1	−67.1	70.2	79.4	−79.3

Full Screen / Esc
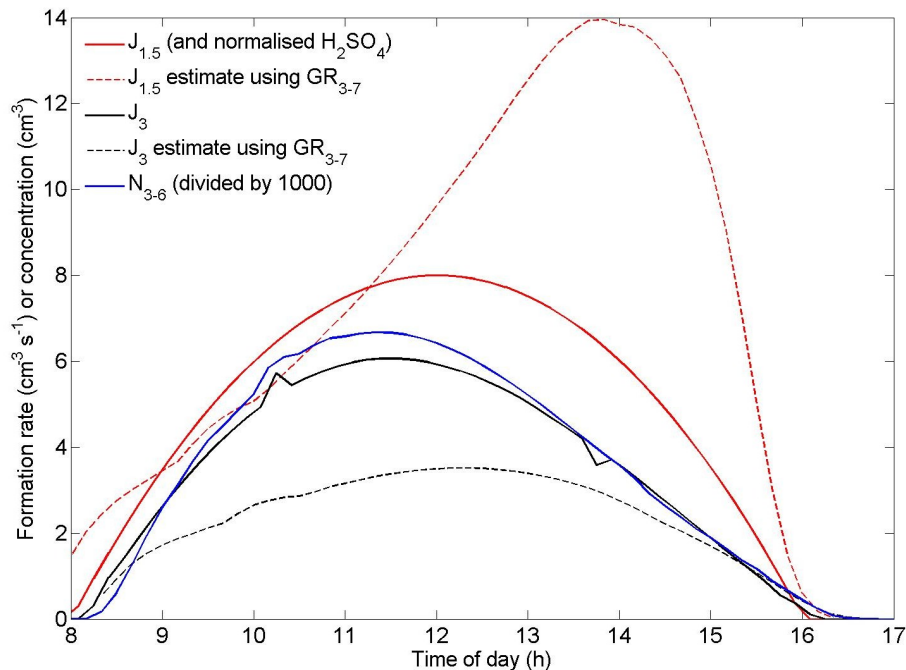
Fig. 1. An example of a simulated activation nucleation event in which N_{3-6} peaks earlier in the day than H_2SO_4 and thus the analysis yields a negative time delay Δt_{N3-6}. Also shown are the simulated nucleation and new particle formation rates ($J_{1.5}$ and J_3 solid lines) as well as the estimates obtained using a cluster growth rate from lognormal fits to the 3–7 nm size range (dashed lines).

Full Screen / Esc

Printer-friendly Version

Interactive Discussion
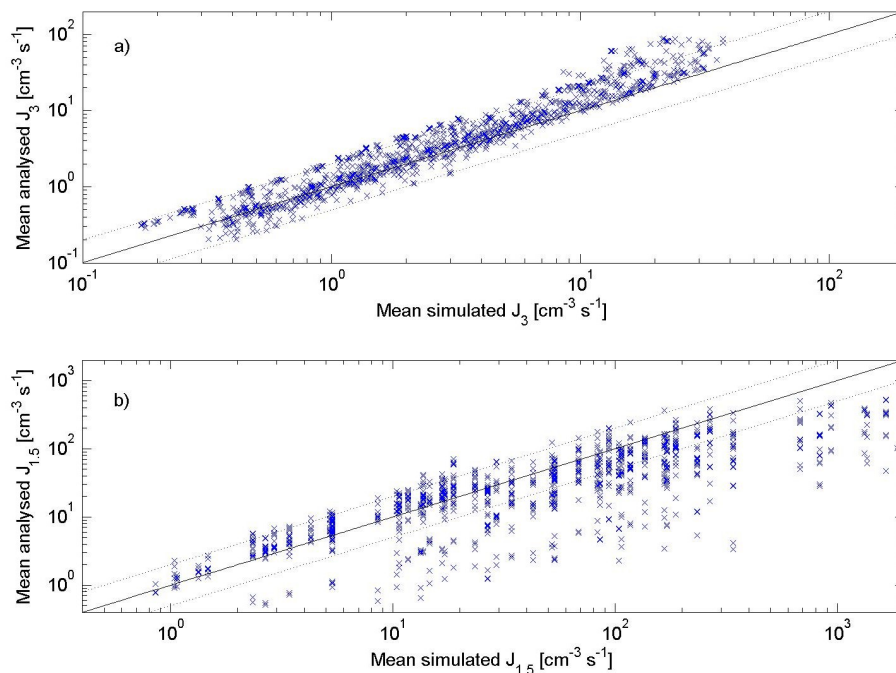
Fig. 2. Comparison of baseline analysis predictions of mean **(a)** new particle formation rates (J_3), and **(b)** nucleation rates ($J_{1.5}$) to the simulated values. All four nucleation mechanisms are included. Shown are also 1:1 line (solid) as well as 1:2 and 2:1 lines (dotted).
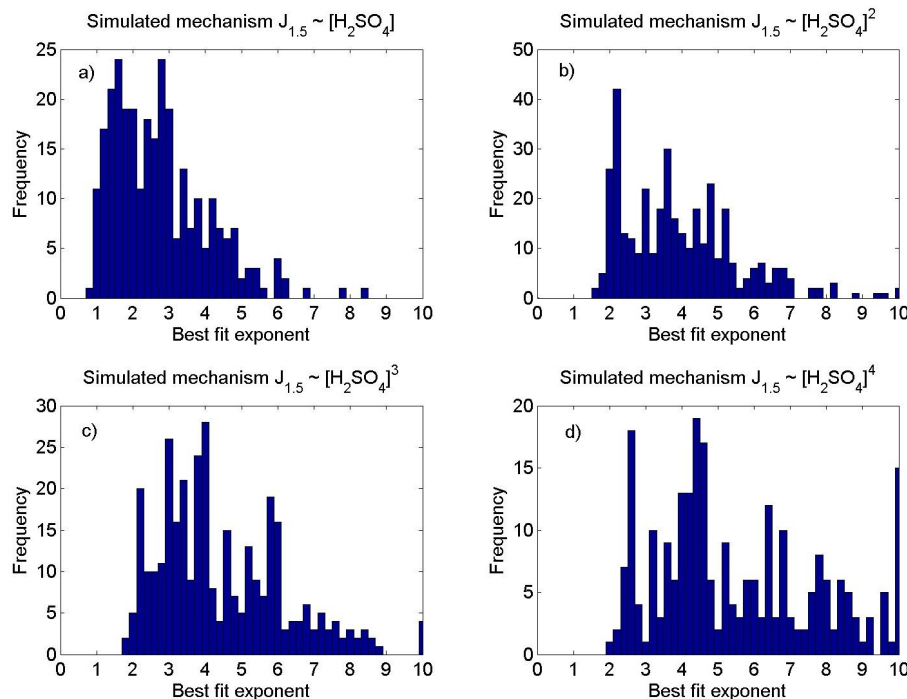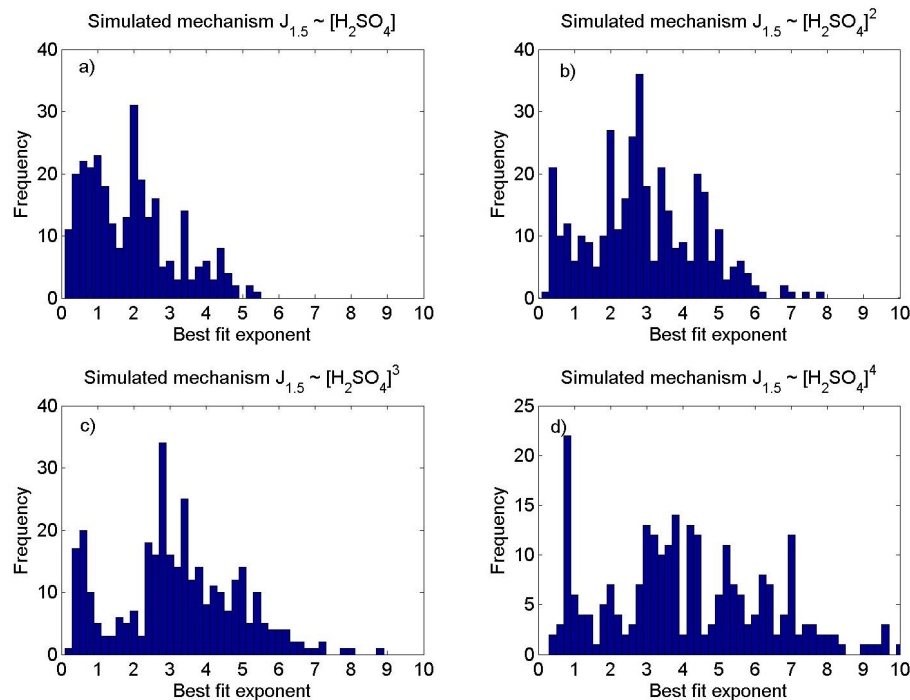
Fig. 3. The frequency distribution of best fit exponents for $N_{3-6} \sim [H_2SO_4]^b$ for the four nucleation mechanisms: **(a)** $J_{1.5} \sim [H_2SO_4]$ (activation nucleation), **(b)** $J_{1.5} \sim [H_2SO_4]^2$ (kinetic nucleation), **(c)** $J_{1.5} \sim [H_2SO_4]^3$, and **(d)** $J_{1.5} \sim [H_2SO_4]^4$. Note that the peaks at exponent 10 are due to the fact that only $b = [0.1, 10]$ was allowed.

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

|◄ | ►|

◄ | ►

Back | Close

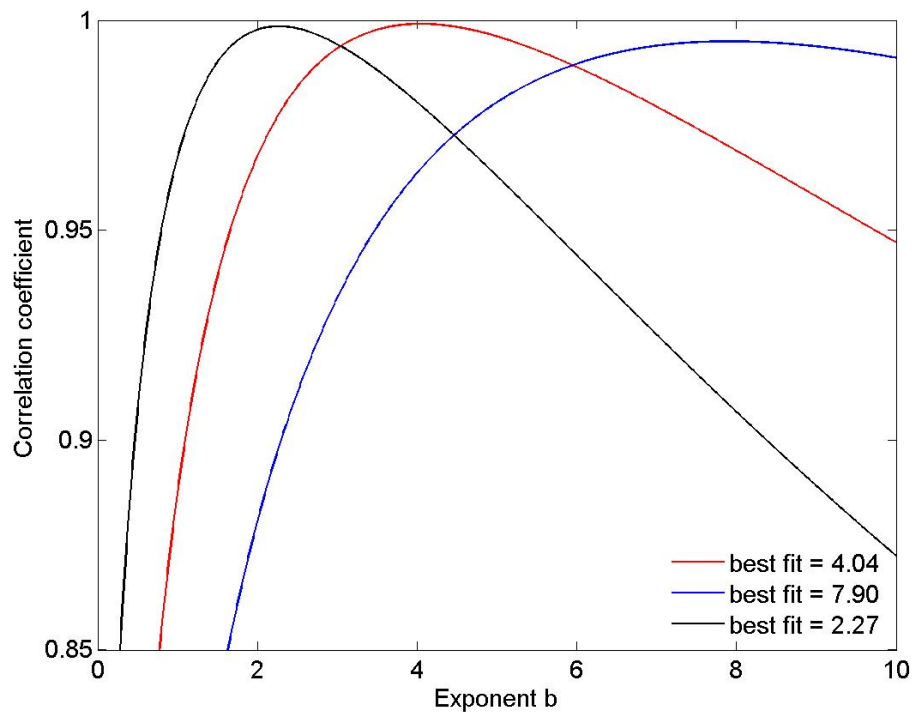Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Fig. 4. The frequency distribution of best fit exponents for $J_{1.5} \sim [H_2SO_4]^b$ for the four nucleation mechanisms: **(a)** $J_{1.5} \sim [H_2SO_4]$ (activation nucleation), **(b)** $J_{1.5} \sim [H_2SO_4]^2$ (kinetic nucleation), **(c)** $J_{1.5} \sim [H_2SO_4]^3$, and **(d)** $J_{1.5} \sim [H_2SO_4]^4$. Note that only $b = [0.1, 10]$ was allowed.

Fig. 5. Correlation coefficient as a function of exponent b when fitting $N_3 \sim [H_2SO_4]^b$ for three example cases each simulated using nucleation mechanism $J_{1.5} = Q \times [H_2SO_4]^4$. The legend indicates the best fit exponent, i.e. value of b that has the highest correlation coefficient, in each case.
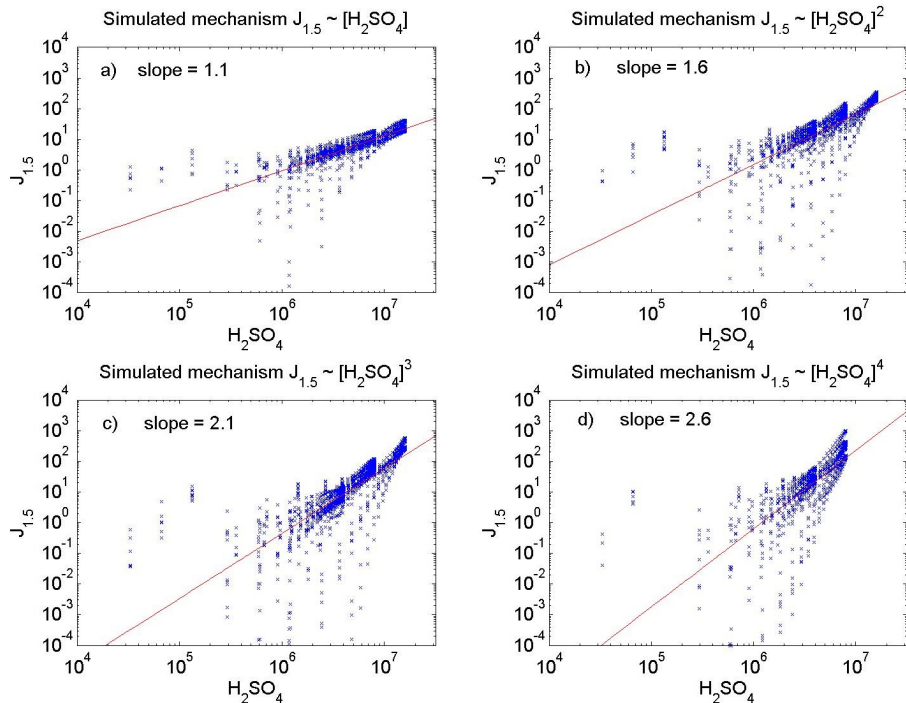
Fig. 6. The analysed nucleation rates $J_{1.5}$ versus simulated sulphuric acid concentrations for the four nucleation mechanisms: **(a)** $J_{1.5} \sim [H_2SO_4]$ (activation nucleation), **(b)** $J_{1.5} \sim [H_2SO_4]^2$ (kinetic nucleation), **(c)** $J_{1.5} \sim [H_2SO_4]^3$, and **(d)** $J_{1.5} \sim [H_2SO_4]^4$. Only events which were simulated using the middle value for the nucleation coefficient (Table 1) and assuming a non-volatile organic compound are shown. The number of events plotted is (a) 29, (b) 30, (c) 34, and (d) 21. The regression line is shown in red.

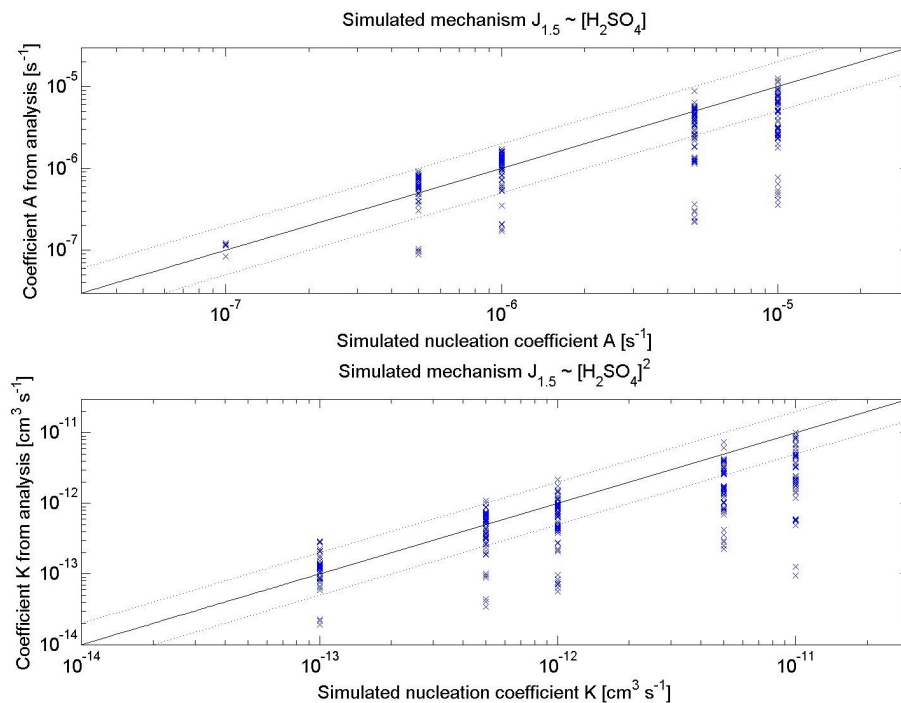**Evaluation of analysis tools for nucleation**

H. Korhonen et al.

Title Page

Abstract | Introduction

Conclusions | References

Tables | Figures

|◄ | ►|

◄ | ►

Back | Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion

Fig. 7. Comparison of predicted and simulated nucleation coefficients for **(a)** activation nucleation events only and **(b)** kinetic nucleation events only. Shown are also 1:1 line (solid) as well as 1:2 and 2:1 lines (dotted).