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Probabilistic description of ice-supersaturated layers in low resolution profiles of relative humidity

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Abstract

The global observation, assimilation and prediction in numerical models of ice supersaturated (ISS) regions (ISSR) are crucial if the climate impact of aircraft condensations trails (contrails) is to be fully understood, and if, for example, contrail formation is

- to be avoided through aircraft operational measures. A robust assessment of the global distribution of ISSR will further this debate, and ISS event occurrence, frequency and spatial scales have recently attracted significant attention. The mean horizontal path length through ISSR as observed by MOZAIC aircraft is 150 km (±250 km). The average vertical thickness of ISS layers is 600–800 m (±575 m) but layers ranging from 25 m to 3000 m have been observed, with up to one third of ISS layers thought to be
- less than 100 m deep. Given their small scales compared to typical atmospheric model grid sizes, statistical representations of the spatial scales of ISSR are required, in both horizontal and vertical dimensions, if global occurrence of ISSR is to be adequately represented in climate models.
- ¹⁵ This paper uses radiosonde launches made by the UK Meteorological Office, from the British Isles, Gibraltar, St. Helena and the Falkland Islands between January 2002 and December 2006, to investigate the probabilistic occurrence of ISSR. Specifically each radiosonde profile is divided into 50- and 100-hPa pressure layers, to emulate the coarse vertical resolution of some atmospheric models. Then the high resolution ob-
- 20 servations contained within each thick pressure layer are used to calculate an average relative humidity and an ISS fraction for each individual thick pressure layer. These relative humidity pressure layer descriptions are then linked through a probability function to produce an s-shaped curve describing the ISS fraction in any average relative humidity pressure layer. An empirical investigation has shown that this one curve is
- statistically valid for mid-latitude locations, irrespective of season and altitude, however, pressure layer depth is an important variable. Using this empirical understanding of the s-shaped relationship a mathematical model was developed to represent the ISS fraction within any arbitrary thick pressure layer. Here the statistical distributions of

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actual high resolution RHi observations in any thick pressure layer, along with an error function, are used to mathematically describe the s-shape. Two models were developed to represent both 50- and 100-hPa pressure layers with each reconstructing their respective s-shapes within 8–10% of the empirical curves. These new models can be used, to represent the small scale structures of ISS events, in modelled data where only low vertical resolution is available. This will be useful in understanding and im-

only low vertical resolution is available. This will be useful in understanding, and improving the global distribution, both observed and forecasted, of ice super-saturation.

1 Introduction

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The global observation, assimilation and prediction in numerical models of ice super saturated (ISS) regions (ISSR) are crucial if the climate impact of aircraft condensation trails (contrails) is to be fully understood, and if, for example, contrail formation is to be avoided through aircraft operational measures. A robust assessment of the global distribution of ISSR will further this debate, and ISS event occurrence, frequency and spatial scales have recently attracted significant attention (Spichtinger et al., 2003b;
 Gierens et al., 2004; Vaughan et al., 2005; Gettelman et al., 2006b; Rädel and Shine,

- 2007; Lamquin et al., 2004, Vadghan et al., 2009, Getterman et al., 2009, Hader and Onine, 2007; Lamquin et al., 2009). The mean horizontal path length through ISSR, observed by MOZAIC aircraft, is 150 km (\pm 250 km) (Gierens and Spichtinger, 2000). The average vertical thickness of ISS layers is 600–800 m (\pm 575 m) but layers ranging from 25 m to 3000 m have been observed, with up to one third of ISS layers thought to be
- ²⁰ less than 100-m deep (Spichtinger et al., 2003a; Treffeisen et al., 2007). Given their small scales compared to typical model grid sizes, statistical representations of the spatial scales of ISSR are required, in both horizontal and vertical dimensions, if global occurrence of ISSR is to be adequately represented in climate models. Lamquin et al. (2009) showed the influence of model vertical resolution on the predicted occurrence of
- ²⁵ ISSR using the European Centre for Medium Range Weather Forecasts (ECMWF) Integrated Forecast System (IFS) on both standard and high vertical resolution pressure levels, and also using radiosonde observations from a launch station in Lindenberg,





Germany. Lamquin et al. (2009) linked the probability of at least one ISS event occurring within a thick pressure layer to the average relative humidity over the same layer. An s-shaped probability relationship was then suggested to describe the occurrence of ISS events in low vertical resolution pressure layers.

- ⁵ This paper aims to extend the research of Lamquin et al. to now link the ISS fractional occurrence within a given thick pressure layer (herein known as the ISS fraction) to the average relative humidity over that layer. This relationship is investigated for 50-hPa and 100-hPa thick pressure layers using high resolution vertical profiles of the atmosphere, specifically, radiosonde launches made by the UK Meteorological Office
- (UK Met Office) from the British Isles, Gibraltar, St. Helena and the Falkland Islands between January 2002 and December 2006. The ultimate aims of this research are to define both an empirical and mathematical description linking ISS fraction to average relative humidity within thick pressure layers. Both the empirical and mathematical descriptions presented here could be used to improve the prediction and representation
 of ISSR in climate models.

2 Radiosonde data

2.1 Selection of launch stations

The UK Met Office global radiosonde dataset consists of vertical profiles of pressure, temperature, relative humidity, specific humidity, wind speed and wind direction from
the surface to a pressure level of approximately 10 hPa from approximately 900 launch stations (UK Meteorological Office). These data are typically recorded at standard pressure levels of 1000, 925, 850, 700, 500, 400, 300, 250, 200, 150, 100, 70, 50, 30, 20, and 10 hPa. Within this dataset a sub-set of ten radiosonde stations, sited predominantly around the UK but with three non-UK stations (Gibraltar, St. Helena and La Falkland Islands), have recorded vertical profiles at a higher vertical resolution, i.e. every two seconds. These profiles have been available from the 1990s onwards. In





this paper, the high resolution radiosonde profiles for a five year period, from 1 January 2002 to 31 December 2006, from nine UK Met Office radiosonde launch stations as shown in Table 1, were used to study the vertical extent of ISS layers. Only nine of the ten available high resolution stations were used because the Aberporth sub-set is

sparsely populated, with some months recording as few as six launches. Otherwise, for the nine stations used, launches were typically twice daily at local times of 1200 h and 2400 h, although there were occasional variations in launch time by ±2 h. The only exception to this was St. Helena, which recorded approximately one launch per day, with approximately 20–25 launches per month.

10 2.2 Relative humidity correction

Vaisala Radiosonde instruments, particularly the RS80-H type, have been used globally for over 20 years and therefore a significant body of literature exists on the accuracy and limitations of these observations (Wang et al., 2002; Miloshevich et al., 2004; Vömel et al., 2007). The Vaisala RS80-H radiosonde was in service with UK Met Office
¹⁵ launch stations until approximately mid-2005, when the RS92 type radiosonde entered service. The exact changeover date was launch station dependent, but from the beginning of 2006 all observations used here were made with the RS92 radiosonde. Both RS80 and RS92 are subject to different systematic errors and as such these instruments have different correction algorithms. The RS80-H has specific issues over tem-

- ²⁰ perature dependency, chemical contamination, sensor ageing and measurement time lag, leading to a dry bias. To account for the resulting bias in observations, the correction presented by Wang et al. (2002) was used. RS92 observations are also subject to a dry bias, in this case due to the lack of a radiation shield, leading to solar heating of the humidity sensor (Vömel et al., 2007). There is less information regarding RS92
- accuracy and only a few correction methods are available, however, a study by (Vömel et al., 2007) was applied here to correct for the observation dry bias. Figure 1 shows uncorrected and corrected profiles for four arbitrarily chosen profiles using RS80-H radiosondes launched from the Watnall station (1.25° W, 53.005° N) during January 2004.





It is worthy of note, that in three of the four profiles, ISS events would not be observed if it were not for application of the correction algorithms (see also Rädel and Shine, 2007).

Whilst the example radiosonde ascents, shown in Fig. 1, provide an indication of the correction magnitude for individual ascents, the percentage corrections to the relative humidity are shown as functions of temperature for the RS80-H and RS92 radiosondes in Fig. 2. The average correction for the RS80-H is up to ~20% at 212 K and for the RS92, during the daytime, the correction is between ~15% at 273 K and ~40% at 212 K. This large correction for the RS92 is due to solar heating of the humidity sensor but for night-time observations, when there is no solar heating generated dry bias, the RS92 is corrected by up to 10% at 238 K.

An additional problem is that the RS80-H radiosondes are known to experience instrument sensor icing during some operations (Miloshevich et al., 2004). This could occur if the radiosonde passed through either super–cooled liquid water (T < 0°C) or

- an ice cloud. If this happened then ice formed on the sensor could remain even after the icing event, and as a result ice super-saturation could be measured for the remainder of the profile, even into the stratosphere(Miloshevich et al., 2004). To detect such erroneous events, all RS80-H radiosonde profiles which had RH> 90% above the tropopause were excluded from the analysis. In mid-latitudes, the tropopause is ex-
- ²⁰ pected to be at pressures between 225 and 300 hPa, depending on season (Hoinka, 1998b), although three-sigma standard deviations from this mean suggested that the tropopause could be at pressures as low as 100 hPa. To ensure that only anomalous data were excluded, the sensor icing criterion was only applied for the parts of all radiosonde profiles below a pressure threshold of 100 hPa. In the tropics the tropopause
- ²⁵ can be at pressures below 100 hPa (Hoinka, 1998b), so that actual tropospheric ISS events below 100 hPa are feasible. Therefore, to mitigate the risk of removing genuine ISS events, the sensor icing criterion was not applied to any of the St. Helena radiosonde profiles. The RS92 radiosonde, in addition to improved calibration accuracy and faster sensor response time, eliminates sensor icing through alternately heated

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dual humidity sensors, which allows one sensor to be heated while the other makes the observation (Paukkunen, 1995). Therefore, for the RS92, the application of a sensor icing criterion to observed profiles is unnecessary.

3 Analysis of radiosonde data

⁵ Relative humidity with respect to ice (RHi), defined here as U, was calculated from the corrected relative humidity with respect to water (RH) observations (U_w) using known water ($e_w(T)$) and ice ($e_i(T)$) saturation relationships (e.g. Goff and Gratch, 1946):

$$U = \frac{e_{\rm w}(T)}{e_{\rm i}(T)} \cdot U_{\rm w}.$$
(1)

This gave high resolution profiles of RHi, which were divided either into five 50 hPa (400–150 hPa) or two 100 hPa pressure layers (400–200 hPa). An example high resolution profile, referenced to a 50 hPa pressure layer discretization, is shown in Fig. 3. Radiosonde observations of relative humidity have larger corrections around the tropopause and lower stratosphere, and the residual errors increase with altitude (Vömel et al., 2007). Therefore, to reduce uncertainties in the analysis, pressure layers
which included the tropopause and higher were omitted. This was achieved by including only those pressure layers which maintained a negative lapse rate throughout that entire layer. As a result, the final analysis was based on 30 462 radiosonde profiles which gave totals of 152 310 50-hPa and 60 924 100-hPa pressure layers.

4 Probability of ice super-saturation occurrence

Each pressure layer, whether 50 hPa or 100 hPa, contained a high resolution RHi profile where each observation U_i^k in a profile was defined by the RHi observed at point *j* in ACPD 10, 2357–2395, 2010 Ice-supersaturated layers in low resolution profiles N. C. Dickson et al.





pressure layer k. Here, as in Lamquin et al. (2009), a pressure layer average RHi (U^k) was calculated as

$$U^k = \frac{\sum_j U_j^k}{N^k},$$

where N^k is the number of profile RH measurements in that pressure layer.

Of course, the average RHi over an entire pressure layer is not expected to define the ISS fraction within that layer. To overcome this Lamquin et al. (2009) investigated whether ice super-saturation was observed at all (at least once) in a pressure layer. For example, let us use a simple binary indicator (*I*), where for each observation $I_j^k = 1$ if $U_j^k \ge 100\%$ and is zero otherwise. Then by letting $I^k = \max_j I_j^k$ means that I^k will equal 1 when there is at least one ISS observation in a pressure layer (*k*) and zero otherwise. This approach meant that while an ISS event in a pressure layer would be captured, the ISS fraction in that layer would not. In contrast, here a count of high resolution ISS events, where $I_j^k = 1$, was made and an ISS fraction (S^k) within a pressure layer was derived using the total number of observations in a pressure layer (N^k), as:

$$S^{k} = \frac{\sum_{j} I_{j}^{k}}{N^{k}}.$$
(3)

For each pressure layer the ISS fraction (S^k) was determined together with a layer average relative humidity (U^k). Figure 4 shows the relationship between S^k and U^k for all 50-hPa pressure layers within the British Isles dataset, where each data point represents an individual pressure layer.

To define a probability relationship each pressure level data point, i.e. (U^k, S^k) , was binned by average relative humidity (U^k) . To accomplish this, the pressure layer data were divided into 28 average relative humidity bins $(0\% < U^k < 140\%)$, in steps Δu of 5% RHi), where *u* represents the average relative humidity bin and Δu is the bin size. Then by taking the mean of S^k in each average relative humidity bin, the probability,

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(2)

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 $P(u \pm \Delta u/2)$, of an ISS event occurring in any pressure layer with an average relative humidity bin, $u - \Delta u/2$ to $u + \Delta u/2$, was defined, that is:

$$P\left(u \pm \Delta u/2\right) = \frac{\sum_{k} S^{k}(u)}{n^{k}(u)},\tag{4}$$

where $n^{k}(u)$ is the number of pressure layers with U^{k} within the average relative humidity bin $u \pm \Delta u/2$. $P(u \pm \Delta u/2)$ is now the average of the ISS event indicator function count in any pressure layer and describes the ISS fraction within the average relative humidity bins between u = 0% and u = 140%.

 $P(u \pm \Delta u/2)$ is equal to zero at u = 0% and equates to 1 when all observations in a pressure layer are ISS. This will occur at a minimum of u = 100% but layers with subsaturated fractions can occur at u > 100%. The relationship defined by Lamquin et al. (2009) is equal to zero at u = 0% but when u = 100%, where there must be at least one ISS event, the relationship always equates to 1 (unity). Therefore, the Lamquin et al. (2009) relationship cannot represent sub-saturated events in layers which are ISS on average, and this limitation was the focus of the research here. By applying $P(u \pm \Delta u/2)$ to the high resolution UK Met office radiosonde data an empirical descrip-

- tion of the probability relationship between U^k and S^k was obtained. This probability relationship is described for the entire British Isles data–set by the s-shaped relationship shown in Fig. 5a, and at this stage the relationship does not account for variations in pressure level, geographical location, pressure layer depth or season. Empirically,
- the first occurrence of ice supersaturation is at an average RHi of ~20%, and therefore when the average RHi is below 20% the entire pressure layer is expected to be sub-saturated. Conversely, a 50-hPa pressure layer can have an average RHi as low as 20% and contain a non-zero ice supersaturation fractional occurrence. The probability of ISS events within a pressure layer increases towards an average RHi of 100%,
- and at this point on the s-shaped curve the pressure layers are shown to contain an ISS fraction of approximately 0.5. From here the probability of more ISS observations within a pressure layer increases rapidly until the average RHi is greater than 130%

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where the pressure layer is entirely ISS. The standard deviation, of the British Isles dataset, from this s-shaped mean is shown in Fig. 5b. The standard deviation is low in the lower and higher average RHi bins, and highest in the middle bins, at around 90–95% average RHi, where the standard deviation is up to an ISS fraction of ± 0.18 within the bin. The s-shaped curve and standard deviation form the basis of an empirical and mathematical investigation.

5 Empirical study of the s-shaped relationship

5.1 Interannual and geographical variation

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Differences in the s-shaped relationship, resulting from selecting sub-sets from the
 overall radiosonde dataset used here (e.g. by pressure level and location etc.), were investigated. Each s-shaped curve shown represents a specific data sub-set, and for ease of comparison the ISS fraction difference between the sub-set in question and the British Isles mean is also shown. Each time this ISS fraction difference will be compared to the standard deviation from British Isles s-shaped curve (shown in Fig. 5b)
 to demonstrate the statistical significance of the variables. Figure 6 shows all the data from the six British Isles launch stations, within 50-hPa (250–300 hPa) pressure layers, for each individual calendar year. For each station and calendar year there is a clear

s-shaped relationship, and while there is some variation between calendar years, the difference between the different curves and the British Isles mean is up to ±0.06 ISS fraction of a pressure layer, with maximum variability around 70–90% average RHi.

The largest deviation from the British Isles average, which is observed consistently at all the stations, is for the 2006 sub-set and this is discussed further below.

To investigate the differences between geographic location further, and in the first instance just within the British Isles sub-set, for the pressure layer 250–300 hPa, the five calendar years of data per launch station were considered. Figure 7a shows the

²⁵ five calendar years of data per launch station were considered. Figure 7a shows the s-shaped relationship and Fig. 7b shows the difference in ISS fraction for each average 10, 2357–2395, 2010

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RHi bin between the British Isles mean s-shaped curve and each launch station. Overall, a similar s-shaped relationship between the six stations is shown and this is likely to be due to the broadly consistent meteorological and topographical features between these stations. Global ISS event frequency and magnitude are expected to vary significantly between geographical locations (Gettelman et al., 2006a), and this would be expected to influence the s-shaped curve. However, within this British Isles dataset the selection of launch site only changes the curves shape by up to ± 0.03 ISS fraction of a pressure layer, with the largest differences around 90–110% average RHi (see panel b).

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- ¹⁰ Data from the same pressure layer was used to analyse the inter-annual variability between the calendar years 2002–2006, utilising all six British Isles launch stations, as shown in Fig. 8. The ISS fraction differences between the curves for each calendar year and the British Isles average are up to ± 0.05 ISS fraction within a pressure layer and there are consistent s-shaped relationships, with similar absolute differences for the
- years 2002–2005. Interestingly, the 2006 curve shows smaller ISS fraction differences (±0.03) than the other calendar years but the curve has a different shape. In particular, average layers which are sub-saturated contain a higher fractional occurrence of ice super-saturation, and conversely, super-saturated layers show a lower fractional occurrence of ISS events. This difference could be due to the change in radiosonde in-
- strument, from the RS80-H to the RS92, during mid-2005. While the exact changeover date is station dependent, the RS92 was definitely in operation with all British Isles launch stations after 1 January 2006 (UK Meteorological Office). In comparison with the RS80-H, the RS92 offers improved calibration accuracy, faster response time and does not suffer from sensor icing (Paukkunen, 1995). A faster response time could
- ²⁵ lead to a more precise definition of an ISS layer when compared to the RS80-H, as the RS92 sensor can respond more quickly to changes between super-saturated and subsaturated environments (Miloshevich et al., 2004). Therefore, using the RS92 could lead to the change in s-shaped curve demonstrated during the 2006 calendar year, but this uncertain.

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So far the analysis has focussed on 50-hPa pressure layers from the British Isles dataset, and has considered the impact of inter-annual variability and geographical location on the form of the s-shaped curve. The largest differences in the s-shaped curve, of up to ± 0.06 ISS fraction within a pressure layer, are observed between the average

- RHi bins of 70% and 110%. Importantly, within this same set of average RHi bins the standard deviation from the British Isles dataset is between ±0.08 and ±0.18, respectively. Therefore, given that the maximum s-shaped curve deviation from the British Isles mean is smaller than the standard deviation for the dataset, the single s-shaped curve, shown earlier in Fig. 5a, is likely to be representative of this region, irrespective of geographical and inter-annual variability. Given this, for all further analysis the British
- Isles mean s-shaped curve will be used as the datum for comparison.

5.2 Altitude variation and vertical resolution

The next stage was to conduct a comparison between different pressure levels (150–400 hPa) and layer depths (50 and 100 hPa), and these are shown in Fig. 9. For 50-hPa
pressure layers the variation in pressure level change, in the first instance between 200 and 400 hPa, means that the s-shaped curve changes by up to ±0.02 ISS fraction. At the lower pressure level of 150–200 hPa the curve changes shape (Fig. 9a) and differences in ISS fraction of up to ±0.07 ISS fraction are observed (Fig. 9c). The proximity of this pressure layer (150–200 hPa) to the tropopause could influence the shape of the curve, as the atmosphere in this region is typically colder and drier than at higher pressure levels (e.g. Houghton, 2002). While the impact of including the tropopause within any given pressure layer is removed, as discussed earlier, the lower occurrence of fully super-saturated layers shown by the s-shaped curve (Fig. 9a) at this

pressure level is likely to be related to the higher prevalence of drier air masses near the tropopause. Specifically, Hoinka (1998a) presented a 15-year (1979–1993) relative humidity global mean for the tropopause, where relative humidity is approximately 10% in mid-latitudes. When pressure layer depth is varied, between 50 and 100 hPa, a more significant change in the s-shape is observed. Figure 9b shows that, as the pressure





layer depth is increased, the probability of capturing more ISS events in on average sub-saturated layer increases and consequently the probability reduces in on average super-saturated layers. Furthermore, Fig. 9d shows that the ISS fraction differences for 100-hPa s-shaped curves are larger for average sub-saturated layers (up to ± 0.1) when

- ⁵ compared to average super-saturated layers (up to ± 0.06). Overall, the difference between 100-hPa s-shaped relationships and the British Isles mean is up to ± 0.1 ISS fraction of a pressure layer. Therefore, vertical resolution is an important variable when applying any s-shaped function to vertical thick pressure layers, and will be considered in all further analysis.
- ¹⁰ An s-shaped relationship is applicable to both 50-hPa and 100-hPa thick pressure layers at all pressure levels between 400 hPa and 150 hPa. Specifically, for 50-hPa pressure layers at levels up to 200 hPa the British Isles mean s-shaped curve is representative. The changing shape of the curve between 150–200 hPa (up to ± 0.06 ISS fraction) also can be represented by the dataset mean because the difference between
- ISS fraction in all average RHi bins is within the standard deviation of the British Isles dataset. The ISS fraction difference between the British Isles mean and both 100-hPa layers (200–300 hPa and 300–400 hPa) is also consistently within the standard deviation of the dataset. Therefore, when representing 100-hPa pressure layers the British Isles mean (for 50-hPa pressure layers) is arguably still applicable. However, the 100-
- ²⁰ hPa layer curve is shallower than the 50-hPa curve and the deviation from the British Isle mean is significantly larger than the deviation shown by other variables analysed. The pressure layer depth is also the variable of most interest particularly if any mathematical model based on these s-shaped curves is to be applied to data of different pressure layer depths. Therefore the conclusion here is that a different s-shape is re-
- quired for different pressure layer depths. The variation in the s-shape demonstrated between 50-hPa and 100-hPa layers will be considered further during the development of a mathematical model later in this paper.

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5.3 Seasonal variation

The occurrence frequency of ice super-saturation shows a seasonal signal. During the winter 15–25% of radiosonde observations are ISS and in the summer 5–15% are ice super-saturated (Rädel and Shine, 2007). Therefore, it is expected that the s-shaped curve will be influenced by season. Again the British Isles dataset was used,

but this time only 50 hPa pressure layers between 200–400 hPa were considered, so any uncertainties over pressure layer depth and level were removed. Figure 10 shows that the largest ISS fraction differences are between the summer and winter curves, and this reflects the higher occurrence of ISS events observed during winter months
 when compared to the summer. The ISS fraction differences are within ±0.04–0.05 of the British Isles average, with the largest variation in average RHi bins between 85 and 100% during winter months.

5.4 Gibraltar, St. Helena and Falkland Islands

This paper has so far concentrated on launch stations within the British Isles, and therefore the next the step is to include those Met Office launch stations, at different latitudes, from Gibraltar, St. Helena and the Falkland Islands. Figure 11 shows the s-shaped relationship for Gibraltar and the Falkland Islands which show ISS fraction differences of up to ±0.02 from the British Isles mean. These two stations have shown similar frequencies of ISS event occurrence to the British Isles during winter and sum-

- ²⁰ mer months, i.e. more ISS events during the winter (10–25%) and less during the summer (5–15%). Therefore, the s-shaped curves are similar to the British Isles mean and the ISS fraction differences are well within the standard deviation of the British Isles dataset. Given this, the single British Isles s-shape curve could be used to represent both these mid-latitude locations.
- ²⁵ The data from St. Helena is shown in a different manner, in Fig. 12, because the occurrence of ISS events is much lower than for the other eight launch stations. In fact, using the same five years (2002–2006), St. Helena dataset showed that ISS events

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are only observed on average $\sim 2.1\%$ of the time, compared to 5–25% for mid-latitude locations. This means that the number of pressure layers containing any amount of ice super-saturation is too small to generate a coherent curve. This is the only station within this sub-set which is located in the tropics and, as discussed earlier, because

- the tropopause is typically at a lower pressure, this launch station data sub-set has two more 50 hPa pressure layers between 150 hPa and 50 hPa compared to all other stations. Even with this larger pressure range, the fractional occurrence of ice supersaturation observed at mid-latitude locations (5–25%) is not observed at St. Helena. Therefore, there is a lower occurrence of ISS events at St. Helena and satellite studies
- of global ice supersaturation distribution do support the lower occurrence of ISS events in the tropics (~10%), particularly when compared to the frequency of ISS events in the extra-tropics (up to ~40%) (Gettelman et al., 2006a). This does not mean that an s-shaped curve is not applicable to St. Helena, or for that matter the tropics (30° N– 30° S), but that this St. Helena dataset does not demonstrate the curve. Furthermore, approximately 98% of the St. Helena pressure layers are within the standard deviation of the British Isles dataset (up to ±0.18 ISS fraction difference in a pressure layer),
- and therefore the s-shape for the British Isles dataset could be representative of the St. Helena station.

To conclude, empirically the s-shaped curve, for 50-hPa pressure layers between
150 and 400 hPa, appears to be representative of ISS events within thick pressure layers in the British Isles. This curve is also valid for the other mid-latitude locations of Gibraltar and the Falkland Islands. The tropical station of St. Helena has a low occurrence of ice super-saturation (~2.1%) and therefore constructing an s-shape, even with five years of data, was not possible. However, similar trends to the British Isles
dataset are evident wherever ISS events occur in pressure layers, and specifically most of the St. Helena pressure layers are within the standard deviation of the British Isles dataset. This means that the s-shaped curve could be representative of the St. Helena station, and the tropics, but a specific study, with a larger more geographically

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varied dataset, is recommended. Other variables such as, pressure level, inter annual

variation and seasonality do influence the s-shape curve but, as presented, variations from the British Isles mean are within the standard deviation of the dataset. Therefore, for these variables a single s-shaped curve is representative. The only variable of importance to the formation of the s-shape, as described earlier, because of its statistical significance and importance in application to low resolution data, is pressure layer depth. Therefore this variable will be considered during the next stage, which is to develop a mathematical model of the s-shape.

6 Mathematical model of the s-shaped relationship

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In this section a simple mathematical model to represent the s-shaped curve is presented. The findings from the empirical investigation showed that a single s-shape, i.e. the s-shape from the British Isles, is valid for 50-hPa pressure layers between 150–400 hPa, for stations outside the British Isles (Gibraltar, the Falkland Islands and St. Helena) and for both summer and winter seasons. Moreover, given that the only statistically significant variable, as found earlier, is the pressure layer depth, then this modelling exercise is focussed upon developing a mathematical relationship for the British Isles dataset and for both 50- and 100-hPa pressure layer depths.

In Sect. 4 it was stated that each pressure layer contained a high resolution RHi profile, where each observation, U_j^k , in a profile was defined by the RHi observed at point *j* in pressure layer *k*. Earlier using this definition the ISS fraction (S^k) in a thick pressure layer and the average relative humidity (U^k) over the same layer were calculated. Here the mathematical modelling exercise begins by again calculating U^k for each pressure layer for the full British Isles dataset. However, this time, instead of calculating S^k , the cumulative probability distribution of all U_j^k observations in thick pressure layers, grouped by U^k into bins of $u - \Delta u/2$ to $u + \Delta u/2$, was calculated. Again *u* represented the average relative humidity bin, Δu is the bin size, and the pressure layer data were divided into 28 average relative humidity bins ($0\% < U^k < 140\%$, in steps



 Δu of 5% RHi). If the cumulative distribution of each bin grouping is $F_u(x)$, i.e. this represents the probability of finding a particular RHi value (*U*) which is less than *x* in any of the layers *k* that had U^k within $u \pm \Delta u/2$. Therefore, the probability of finding an ISS event in any thick pressure layer, i.e. when *x* = 100, is

$$5 \quad 1 - F_u(100) := \overline{F_u}(100) \equiv P\left(u \pm \Delta u/2\right)$$

which is equivalent to the probability of haveing a certain ISS fraction in layers with average RHi in the interval $u \pm \Delta u/2$.

To construct a mathematical model in this way the distributions of U_j^k in each average relative humidity bin needs to be quantified. Therefore, by way of example, three average relative humidity bins are chosen 15–20% (low-bin), 55–60% (mid-bin), 115– 120% (high-bin) and Fig. 13 shows the distribution of U_j^k in each bin. The probability distributions of U_j^k in each average relative humidity bin are mono-modal, right skewed in the low-bin, left skewed in the high-bin and approximately symmetrical (normal) in the mid-bin. These distributions are similar to those derived from airborne data in the upper troposphere (Gierens et al., 2007).

A Gaussian distribution is certainly applicable for the mid-bin (15–20%) and this is representative of bins between 40% and 80% average relative humidity. For the low-bin (representative of bins < 40% average RHi) and upper bins (representative of bins > 80% average RHi), including those which are ice super-saturated on average, the

- ²⁰ Gaussian distribution is not fully representative, and in particular does not account for the skewness or the tails to high and low RHi. However, the mono-modal characteristic, of both the high and low average relative humidity bin distributions, is captured and for the purposes of mathematical modelling here a Gaussian distribution is used to represent all average relative humidity bins. Each bin therefore is assumed to have a
- ²⁵ Gaussian distribution, with a mean RHi (which is the same as the *u* for that bin) and a corresponding standard deviation (σ_u). Using these data for each average relative humidity bin, a further mathematical formulation of (as defined in Eq. 5), or the probability of finding an ISS event in any arbitrary average relative humidity thick pressure layer,

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(5)



can be constructed. Equation (6) shows how $\overline{F_u}(100)$ is modelled using the integral of a Gaussian distribution, or an error function:

$$\overline{F_u}(100) \approx \frac{1}{2} - \frac{1}{2} \operatorname{erf}\left[\frac{100 - u}{\sqrt{2}\sigma_u}\right].$$
(6)

To utilise this error function based formulation of $F_u(100)$ an understanding of the standard deviation for each average relative humidity bin, $u \pm \Delta u/2$, is required. As stated earlier this mathematical model focuses on the representation of the British Isle sshaped curves for both 100-hPa and 50-hPa pressure layers. The standard deviation in each of the 28 bins is shown in Fig. 14 for pressure layers 200–300 hPa, 300–400 hPa, 200–250 hPa, and 250–300 hPa. The four standard deviation datasets show similar trends with the largest σ_u in the mid-bins and lower σ_u in high- and low-bins. The σ_u in any 50-hPa layer is smaller than that of any 100-hPa layer. This is due to the thicker 100-hPa layer having a larger U_j^k variance, because approximately twice as much data is captured compared to the 50-hPa layer, and therefore the probability of a larger variance, and so σ_u , increases.

¹⁵ The British Isles data is now represented by average relative humidity bins, $u \pm \Delta u/2$, and in each bin, a standard deviation of RHi observations, σ_u . These data, (u, σ_u) , from the four thick pressure layers considered here, are used with the mathematical error function model and an s-shaped description of ISS events, for thick pressure layers, represented by average relative humidity, is constructed, as shown in Fig. 15a. The

- ²⁰ differences in ISS fraction between the modelled s-shape curves and the curves generated from observations (shown earlier in Fig. 9) is shown in Fig. 15b. The differences here are between -0.05 and 0.08 ISS fraction. If the same rationale is employed here as in Sect. 5, in that the ISS fraction differences are compared to the British Isles dataset ISS fraction standard deviation (±0.18 ISS fraction) shown earlier in Fig. 5b,
- then the differences between observation generated s-shaped curves and modelled s-shapes are within acceptable limits. Of course the modelled shaped curves rely on σ_u and these data are produced from observations. However, it is proposed that the

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 (u, σ_u) dataset for the British Isles, for both 50-hPa and 100-hPa pressure layers, can be used with the error function model for other geographical locations, pressure levels (400–150 hPa), seasons and years. Finally, this model can be used, to represent ISS events, in modelled data where only low vertical resolution is available. This will be useful in understanding the global distribution of ice super-saturation and modelling persistence of contrails.

7 Concluding remarks

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Five years, from January 2002 to December 2006, of corrected high resolution radiosonde profiles, from nine UK Met Office launch stations, were used to investigate
the fractional occurrence of ice super-saturation within 50-hPa and 100-hPa thick vertical pressure layers. The nine launch stations consisted of six within the British Isles and one from each of the Falkland Islands, Gibraltar and St. Helena. The analysis was based on 30 462 radiosonde profiles which gave totals of 152,310 50-hPa and 60 924 100-hPa pressure layers. Within each pressure layer the average RHi and ISS fraction of the same pressure layer were derived and this allowed for the development of an empirical s-shaped relationship which linked the ISS fraction to the average RHi in any 50-hPa or 100-hPa pressure layer. The analysis was extended to identify the statistical significance of variations between s-shaped curves for geographical location of launch station, seasonality, pressure level and pressure layer depth. In each case the British

Isles average s-shaped curve (i.e. 5 years, 50-hPa layers and six launch stations) was used as a datum to assess the influence of each variable on the s-shaped curve.

Within the British Isles, launch stations displayed similar s-shaped relationships and were within ± 0.03 ISS fraction difference in a pressure layer of one another. Seasonality in mid-latitudes also impacts the s-shaped relationship, by between 0.04 and 0.05 ISS fraction from the British Isles mean, and with higher occurrences of de-

rived ISS fractions during the winter compared to the summer. Increasing the pressure layer depth from 50 hPa to 100 hPa also shows deviations from the mean British





Isles s-shaped relationship but by up to ± 0.1 ISS fraction. Pressure level changes (150–400 hPa) show $\pm 0.03-0.07$ ISS fraction differences within a pressure layer for 50-hPa pressure layers. Inter-annual variability, for calendar years between 2002 and 2006, showed deviation from the mean of up to ± 0.06 ISS fraction. Stations out-

- side the British Isles, and in the first instance, Gibraltar and Falkland Islands stations, both representative of mid-latitudes, show ISS fraction differences of ±0.02 from the British Isles mean s-shape curve. Interestingly, at the tropical station of St. Helena, an s-shaped curve was not formed and this was due to the lower occurrence of ISS events observed at this station (~2.1% of observations were ISS). This lower occurrence of
- ¹⁰ ISS events in the tropics is supported by satellite observation (Gettelman et al., 2006a). This does not mean that an s-shaped curve is not applicable to St. Helena, or for that matter the Tropics (30° N– 30° S), but that this St. Helena dataset does not demonstrate the curve. Furthermore, approximately 98% of the St Helena pressure layers are within the standard deviation of the British Isles dataset (up to ±0.18 ISS fraction difference
- ¹⁵ in a pressure layer), and therefore the s-shape for the British Isles dataset could be representative of the St. Helena station. The empirical form of the s-shaped function has been demonstrated for mid-latitude locations and has shown sensitivity to changes in geographical location, season, pressure level and pressure layer depth of up to ± 0.1 ISS fraction difference in any thick pressure layer. However, given that the standard
- ²⁰ deviation of the British Isles dataset (the analysis datum) is up to ±0.18 ISS fraction difference in a pressure layer then all variables accounted for here are within this. Moving forward the authors postulated that pressure level, geographical location (including St. Helena) and season were all within the British Isles dataset standard deviation and can be accounted for by one single s-shape. The variable which, while still within the
- standard deviation, showed the largest ISS fraction difference (up to ± 0.1) from the mean was the pressure layer depth (50 and 100 hPa). Pressure layer depth is also likely to be the most important variable when using any mathematical model on different vertical resolution datasets. Therefore, for each pressure layer depth, different s-shapes were considered in the mathematical modelling exercise that followed.

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The mathematical model presented used the distributions of the actual radiosonde observations in each average relative humidity bin. A standard deviation for each bin was calculated and it was assumed that within each bin the RHi observations followed a Gaussian distribution. Using these data an error function, based on the integral of the Gaussian distribution, was used to form a mathematical representation of the ISS fraction within any arbitrary thick pressure layer. More specifically the model used two standard deviation data-sub-sets, for both pressure layers (50 and 100 hPa). The

model appears to represent the s-shaped function to within ± 0.08 ISS fraction within a

- pressure layer when compared to the observation derived s-shapes for both thick pressure layers. This is within acceptable limits given the standard deviation of the British Isles dataset used. The modelled s-shaped curves rely on σ_u and these data are produced from observations. However, it is proposed that the (u, σ_u) dataset for the British Isles, for both 50- and 100-hPa pressure layers, can be used with the error function model for other geographical locations, pressure levels (400–150 hPa), seasons and years. This model can be used, to represent ISS events, in modelled data where only low vertical resolution is available. This will be useful in understanding, and improving
- low vertical resolution is available. This will be useful in understanding, and improving the global distribution, both observed and forecasted, of ice super-saturation.

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 their support and many useful comments. The study contributes to German projects UFO and CATS and to the European Network of Excellence ECATS. All three projects aim at environmentally compatible aviation, and the present study contributes especially to improved forecast of ice super-saturated regions which is a requirement for operational contrail avoidance measures.

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Table 1. A summary of UK Met Office high resolution radiosonde observations (1 January 2002–31 December 2006) used in this study. Observations were generally performed using the Vaisala RS80 up to mid-2005 with the RS92 instrument used thereafter (UK Meteorological Office).

Station	Location		Launches (2002–2006)	Radiosonde type
Albemarle	1.88° W	55.02° N	3546	RS80/RS92
Camborne	5.329° W	50.218° N	3981	RS80/RS92
Castor Bay	6.503° W	54.503° N	3234	RS80/RS92
Herstmonceux	0.319° W	50.89° N	3771	RS80/RS92
Lerwick	1.183° W	60.139° N	3957	RS80/RS92
Watnall	1.25° W	53.005° N	3804	RS80/RS92
Gibraltar	5.35° W	36.15° N	3429	RS80
St Helena	5.667° W	15.933° S	1189	RS80
Falkland Islands	58.45° W	51.817° S	3551	RS80

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Fig. 2. The average correction made to the RS80-H and RS92 radiosonde relative humidity observations. In this case observations were corrected using Wang et al. (2002) for the RS80-H and Vömel et al. (2007) for the RS92.

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Fig. 3. A schematic diagram showing a high resolution RHi profile and how radiosonde RHi profiles were divided into 50-hPa of 100-hPa pressure layers. Each pressure layer could contain up to 100 high resolution RHi radiosonde observations.



Average RHi% (*Ui^{*}*)

Fig. 4. Relationship between the average RHi (U^k in %) and ISS fraction (S^k in %) within 50-hPa layers (400–150 hPa). These data are derived from five years of UK Met Office high resolution radiosonde launches from Camborne, Castor Bay, Herstmonceux, Albemarle, Lerwick and Watnall launch stations (January 2002–December 2006).

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Fig. 5. (a) Probability relationship between the average RHi and the ISS fraction, $P(u \pm \Delta u/2)$, for 50-hPa layers (400–150 hPa). **(b)** Standard deviation for the British Isles dataset from the s-shaped mean (in each relative humidity bin). The analysis was performed from five years of high resolution radiosonde launches from Camborne, Castor Bay, Herstmonceux, Albemarle, Lerwick and Watnall (January 2002–December 2006).





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Fig. 7. The relationship between average RHi and the ISS fraction for the 250–300-hPa pressure layer is shown. Panel **(a)** shows the s-shaped relationships for each station and panel **(b)** shows the difference between curves from each station and the British Isles average s-shaped relationship. These data are from six high resolution radiosonde launch stations within the British Isles (January 2002–December 2006).

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Fig. 8. The relationship between average RHi and the ISS fraction for the 250–300 hPa pressure layer is shown. Panel **(a)** shows the s-shaped relationships and panel **(b)** shows the difference between each calender year curve and the British Isles mean. These data are from six high resolution radiosonde launch stations within the British Isles (January 2002–December 2006).

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Fig. 9. The relationship between average RHi and the ISS fraction within individual 50 hPa pressure layers is shown (panel **(a)**. The differences between them are shown in panel **(c)**. Panel **(b)** displays a comparison between s-shaped curves for 50- vs. 100-hPa layers, and their differences are shown in panel **(d)**. These data are derived from six high resolution radiosonde launch stations within the British Isles (January2002–December 2006).



Fig. 10. The relationship between average RHi and the ISS fraction within 50-hPa pressure layers, comparing individual seasons is shown in panel **(a)**. The differences between them and the British Isles average curve are shown in panel **(b)**. These data are derived from six high resolution radiosonde launch stations within the British Isles (January 2002–December 2006).

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Fig. 11. The relationship between average RHi and the ISS fraction within 50-hPa pressure layers, comparing Gibraltar and the Falkland Islands to the Bristish Isles mean is shown in panel **(a)**. The differences between them and the British Isles average curve are shown in panel **(b)**. These data are derived from six high resolution radiosonde launch stations within the British Isles and one from both Gibraltar and the Falkland Islands (January 2002–December 2006).

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Fig. 13. Probability densitiy functions of RHi distributions in thick pressure levels and three average relative humidity bins. A low bin (average RHi 15–20%, orange line), mid-bin (55–60%, green line), and a high bin (115–120%, turquoise line). The distributions are derived from the British Isles dataset (January 2002–December 2006).

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Fig. 14. Standard deviations (σ_u) versus average RHi (bin-wise) in 50- and 100-hPa pressure layers. The data are derived from the British Isles dataset (January 2002–December 2006).

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