

Experiments at FORD: Model including deuterated species

Model run using upper limit on CH3ONO impurity in CH2DONO of 0.00016, and updated rates from NIST, IUPAC, JPL.

General description and conditions

Model of photochemistry of CH2DO + O₂ forming CH₂O vs CHDO

Experiments with CH2DONO precursor in the FORD photochemical reactor

Modeling series starting 02-21-18

```
> restart;
> ppm := 1e-6: ppb := 1e-9: ppt := 1e-12:
> T:= 273 + 23:
Ptot := 700:
> P:= 101300*Ptot/760:
```

Chemical equations

- 1a. CH₃ONO + hν --> CH₃O + NO
- 1b. CH₂DONO + hν --> CH₂DO + NO
- 2a. CH₃O + O₂ --> CH₂O + HO₂
- 2b. CH₂DO + O₂ --> CH₂O + DO₂
- 2c. CH₂DO + O₂ --> CHDO + HO₂
- 3a. HO₂ + NO --> OH + NO₂
- 3b. DO₂ + NO --> OD + NO₂
- 4a. OH + cC₆H₁₂ --> H₂O + RO₂
- 4b. OD + cC₆H₁₂ --> HDO + RO₂
5. RO₂ + NO --> RO + NO₂
6. NO₂ + hν --> NO + O
7. O + O₂ + M --> O₃ + M
- 8a. CH₂O + hν --> CO + H₂
- 8b. CHDO + hν --> CO + HD
- 9a. CH₂O + hν --> CO + 2*HO₂
- 9b. CHDO + hν --> CO + HO₂ + DO₂
- 10a. HO₂ + NO₂ + M --> PNA + M
- 10b. DO₂ + NO₂ + M --> PNAD + M
- 11a. HO₂ + CH₂O --> HOCH₂O₂
- 11b. DO₂ + CH₂O --> DOCH₂O₂
- 11c. HO₂ + CHDO --> HOCHDO₂
- 11d. DO₂ + CHDO --> DOCHDO₂
- 12a. HOCH₂O₂ + RO₂ --> HCOOH + RO + HO₂
- 12b. DOCH₂O₂ + RO₂ --> HCOOD + RO + HO₂
- 12c. HOCHDO₂ + RO₂ --> DCOOH + RO + HO₂
- 12d. DOCHDO₂ + RO₂ --> DCOOD + RO + HO₂
- 13a. CH₃O + NO + M --> CH₃ONO + M
- 13b. CH₂DO + NO + M --> CH₂DONO + M
- 14a. CH₃O + NO₂ + M --> CH₃ONO₂ + M

- 14b. $\text{CH}_2\text{DO} + \text{NO}_2 + \text{M} \rightarrow \text{CH}_2\text{DONO}_2 + \text{M}$
 15a. $\text{OH} + \text{CH}_3\text{ONO} \rightarrow \text{CH}_2\text{O} + \text{NO} + \text{H}_2\text{O}$
 15b. $\text{OH} + \text{CH}_2\text{DONO} \rightarrow \text{CHDO} + \text{NO} + \text{H}_2\text{O}$
 15c. $\text{OH} + \text{CH}_2\text{DONO} \rightarrow \text{CH}_2\text{O} + \text{NO} + \text{HDO}$
 15d. $\text{OD} + \text{CH}_2\text{DONO} \rightarrow \text{CH}_2\text{O} + \text{NO} + \text{D}_2\text{O}$
 15e. $\text{OD} + \text{CH}_2\text{DONO} \rightarrow \text{CHDO} + \text{NO} + \text{HDO}$
 15f. $\text{OD} + \text{CH}_3\text{ONO} \rightarrow \text{CH}_2\text{O} + \text{NO} + \text{HDO}$
 16a. $\text{CH}_2\text{O} + \text{OH} \rightarrow \text{H}_2\text{O} + \text{CO} + \text{HO}_2$
 16b. $\text{CHDO} + \text{OH} \rightarrow \text{H}_2\text{O} + \text{CO} + \text{DO}_2$
 16c. $\text{CHDO} + \text{OH} \rightarrow \text{HDO} + \text{CO} + \text{HO}_2$
 16d. $\text{CHDO} + \text{OD} \rightarrow \text{D}_2\text{O} + \text{CO} + \text{HO}_2$
 16e. $\text{CHDO} + \text{OD} \rightarrow \text{HDO} + \text{CO} + \text{DO}_2$
 16f. $\text{CH}_2\text{O} + \text{OD} \rightarrow \text{HDO} + \text{CO} + \text{HO}_2$
 17a. $\text{HO}_2 + \text{HO}_2 \rightarrow \text{H}_2\text{O}_2$
 17b. $\text{HO}_2 + \text{DO}_2 \rightarrow \text{HDO}_2$
 17c. $\text{DO}_2 + \text{DO}_2 \rightarrow \text{D}_2\text{O}_2$
 18a. $\text{H}_2\text{O}_2 + h\nu \rightarrow 2\text{OH}$
 18b. $\text{HDO}_2 + h\nu \rightarrow \text{OH} + \text{OD}$
 18c. $\text{D}_2\text{O}_2 + h\nu \rightarrow 2\text{OD}$
 19a. $\text{CH}_3\text{O} + \text{NO}_2 \rightarrow \text{CH}_2\text{O} + \text{HONO}$
 19b. $\text{CH}_2\text{DO} + \text{NO}_2 \rightarrow \text{CHDO} + \text{HONO}$
 19c. $\text{CH}_2\text{DO} + \text{NO}_2 \rightarrow \text{CH}_2\text{O} + \text{DONO}$
 20a. $\text{HOCH}_2\text{O}_2 + \text{HOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 2\text{HCOOH} + 2\text{HO}_2$
 20b. $\text{HOCH}_2\text{O}_2 + \text{HOCHDO}_2 + \text{O}_2 \rightarrow 1.5\text{HCOOH} + 0.5\text{DCOOH} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20c. $\text{HOCH}_2\text{O}_2 + \text{DOCH}_2\text{O}_2 + \text{O}_2 \rightarrow \text{HCOOH} + \text{HCOOD} + 2\text{HO}_2$
 20d. $\text{HOCH}_2\text{O}_2 + \text{DOCHDO}_2 + \text{O}_2 \rightarrow \text{HCOOH} + 0.5\text{HCOOD} + 0.5\text{DCOOD} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20e. $\text{HOCHDO}_2 + \text{HOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOH} + 1.5\text{HCOOH} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20f. $\text{HOCHDO}_2 + \text{HOCHDO}_2 + \text{O}_2 \rightarrow \text{DCOOH} + \text{HCOOH} + \text{HO}_2 + \text{DO}_2$
 20g. $\text{HOCHDO}_2 + \text{DOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOH} + \text{HCOOD} + 0.5\text{HCOOH} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20h. $\text{HOCHDO}_2 + \text{DOCHDO}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOH} + 0.5\text{HCOOH} + 0.5\text{HCOOD} + 0.5\text{DCOOD} + \text{HO}_2 + \text{DO}_2$
 20i. $\text{DOCH}_2\text{O}_2 + \text{HOCH}_2\text{O}_2 + \text{O}_2 \rightarrow \text{HCOOD} + \text{HCOOH} + 2\text{HO}_2$
 20j. $\text{DOCH}_2\text{O}_2 + \text{HOCHDO}_2 + \text{O}_2 \rightarrow \text{HCOOD} + 0.5\text{HCOOH} + 0.5\text{DCOOH} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20k. $\text{DOCH}_2\text{O}_2 + \text{DOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 2\text{HCOOD} + 2\text{HO}_2$
 20l. $\text{DOCH}_2\text{O}_2 + \text{DOCHDO}_2 + \text{O}_2 \rightarrow 1.5\text{HCOOD} + 0.5\text{DCOOD} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20m. $\text{DOCHDO}_2 + \text{HOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOD} + 0.5\text{HCOOD} + \text{HCOOH} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20n. $\text{DOCHDO}_2 + \text{HOCHDO}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOD} + 0.5\text{HCOOD} + 0.5\text{HCOOH} + 0.5\text{DCOOH} + \text{HO}_2 + \text{DO}_2$
 20o. $\text{DOCHDO}_2 + \text{DOCH}_2\text{O}_2 + \text{O}_2 \rightarrow 0.5\text{DCOOD} + 1.5\text{HCOOD} + 1.5\text{HO}_2 + 0.5\text{DO}_2$
 20p. $\text{DOCHDO}_2 + \text{DOCHDO}_2 + \text{O}_2 \rightarrow \text{DCOOD} + \text{HCOOD} + \text{HO}_2 + \text{DO}_2$
 21a. $\text{CH}_3\text{OH} + \text{OH} \rightarrow \text{CH}_2\text{OH} + \text{H}_2\text{O}$
 21b. $\text{CH}_2\text{DOH} + \text{OH} \rightarrow \text{CH}_2\text{OH} + \text{HDO}$

- 21c. CH₂DOH + OH --> CHDOH + H₂O
 21d. CH₃OH + OD --> CH₂OH + HDO
 21e. CH₂DOH + OD --> CHDOH + HDO
 21f. CH₂DOH + OD --> CH₂OH + D₂O
 22a. CH₂OH + O₂ --> CH₂O + HO₂
 22b. CHDOH + O₂ --> CHDO + HO₂
 23. O₃ + NO --> NO₂
 24a. CO + OH --> CO₂ + HO₂
 24b. CO + OD --> CO₂ + DO₂
 25a. H₂ + OH --> H₂O + HO₂
 25b. HD + OH --> H₂O + DO₂
 25c. HD + OH --> HDO + HO₂
 25d. H₂ + OD --> HDO + HO₂
 25e. HD + OD --> HDO + DO₂
 25f. HD + OD --> D₂O + HO₂
 26. RO₂ + RO₂ --> 2RO
 27. RO₂ + RO₂ --> RO + cC₆H₁₂
 28a. RO₂ + HO₂ --> cC₆H₁₂ (recycle)
 28b. RO₂ + DO₂ --> cC₆H₁₂
 29. RO + O₂ --> cC₆H₁₂ + HO₂
 30aa. HOCH₂O₂ + HO₂ --> HOCH₂OOH + O₂
 30ab. HOCH₂O₂ + DO₂ --> HOCH₂OOD + O₂
 30ac. DOCH₂O₂ + HO₂ --> DOCH₂OOH + O₂
 30ad. DOCH₂O₂ + DO₂ --> DOCH₂OOD + O₂
 30ae. HOCHDO₂ + HO₂ --> HOCHDOOH + O₂
 30af. HOCHDO₂ + DO₂ --> HOCHDOOD + O₂
 30ag. DOCHDO₂ + HO₂ --> HOCHDOOH + O₂
 30ah. DOCHDO₂ + DO₂ --> HOCHDOOD + O₂
 30ba. HOCH₂O₂ + HO₂ --> HCOOH + H₂O + O₂
 30bb. HOCH₂O₂ + DO₂ --> HCOOH + HDO + O₂
 30bc. DOCH₂O₂ + HO₂ --> HCOOD + H₂O + O₂
 30bd. DOCH₂O₂ + DO₂ --> HCOOD + HDO + O₂
 30be. HOCHDO₂ + HO₂ --> DCOOH + H₂O + O₂
 30bf. HOCHDO₂ + DO₂ --> DCOOH + HDO + O₂
 30bg. DOCHDO₂ + HO₂ --> DCOOD + H₂O + O₂
 30bh. DOCHDO₂ + DO₂ --> DCOOD + HDO + O₂
 30ca. HOCH₂O₂ + HO₂ --> HOCH₂O + OH + O₂
 30cb. HOCH₂O₂ + DO₂ --> HOCH₂O + OD + O₂
 30cc. DOCH₂O₂ + HO₂ --> DOCH₂O + OH + O₂
 30cd. DOCH₂O₂ + DO₂ --> DOCH₂O + OD + O₂
 30ce. HOCHDO₂ + HO₂ --> HOCHDO + OH + O₂
 30cf. HOCHDO₂ + DO₂ --> HOCHDO + OD + O₂
 30cg. DOCHDO₂ + HO₂ --> HOCHDO + OH + O₂
 30ch. DOCHDO₂ + DO₂ --> DOCHDO + OD + O₂
 31a. NO₂ + OH + M --> HNO₃
 31b. NO₂ + OD + M --> DNO₃

- 32a. $\text{CH}_3\text{ONO}_2 + \text{OH} \rightarrow \text{CH}_2\text{O} + \text{H}_2\text{O} + \text{NO}_2$
 32b. $\text{CH}_2\text{DONO}_2 + \text{OH} \rightarrow \text{CH}_2\text{O} + \text{HDO} + \text{NO}_2$
 32c. $\text{CH}_2\text{DONO}_2 + \text{OH} \rightarrow \text{CHDO} + \text{H}_2\text{O} + \text{NO}_2$
 32d. $\text{CH}_3\text{ONO}_2 + \text{OD} \rightarrow \text{CH}_2\text{O} + \text{HDO} + \text{NO}_2$
 32e. $\text{CH}_2\text{DONO}_2 + \text{OD} \rightarrow \text{CH}_2\text{O} + \text{D}_2\text{O} + \text{NO}_2$
 32f. $\text{CH}_2\text{DONO}_2 + \text{OD} \rightarrow \text{CHDO} + \text{HDO} + \text{NO}_2$
 33a. $\text{HOCH}_2\text{O}_2 \rightarrow \text{HO}_2 + \text{CH}_2\text{O}$
 33b. $\text{DOCH}_2\text{O}_2 \rightarrow \text{DO}_2 + \text{CH}_2\text{O}$
 33c. $\text{HOCHDO}_2 \rightarrow \text{HO}_2 + \text{CHDO}$
 33d. $\text{DOCHDO}_2 \rightarrow \text{DO}_2 + \text{CHDO}$

Parameters

Time unit in the calculations

> `time_unit := second;`

Number of time steps in the calculations

> `nrt := 300;`

> `time_tot := time_unit*nrt;`

Fundamental constants

Physical constants are present in Maple after the call:

`with(ScientificConstants) :`

Avogadros number

> `Na := evalf(Constant(N[A])) ;`

The gas constant

> `R := evalf(Constant(R)) ;`

Fixed concentrations and Rate constants

Concentrations

Number of molecules per cm³ is calculated from temperature and pressure

$$M_i := \frac{P_i 10^{-6} Na}{R T_i}$$

Torr is defined in units of molecules per cc.

> `M := 1/1000000 * P Na / (R T); 1; 1; 1; Torr := 1/760 M; 1; 1`

$$M := 2.283066164 \cdot 10^{19}$$

1

1

$$Torr := 3.004034426 \cdot 10^{16}$$

1

1

Fixed concentrations

```
> O2:= 100*Torr:  
N2 := 600*Torr:  
> iso_impurity:=0.00016:#upper limit on CH3 contamination  
in CH2DONO/CH2DOH from IR spectra.
```

Initial concentrations of time-varying species, modeling series starting 02-21-18

```
> CH3ONO_zero := iso_impurity*36.8*Torr/1000:  
> CH2DONO_zero := (1-iso_impurity)*36.8*Torr/1000:  
> CH3OH_zero := iso_impurity*1.48*Torr/1000:  
> CH2DOH_zero := (1-iso_impurity)*1.48*Torr/1000:  
> C6H12_zero := 75.3*Torr/1000:  
> NO2_zero := 0:  
> startconc := 0:
```

The rate constants:

1a. $\text{CH}_3\text{ONO} + h\nu \rightarrow \text{CH}_3\text{O} + \text{NO}$

```
> j1a:=1.44e-3: R1a:=j1a*CH3ONO(t):
```

1b. $\text{CH}_2\text{DONO} + h\nu \rightarrow \text{CH}_2\text{DO} + \text{NO}$

```
> j1b:=1.44e-3: R1b:=j1b*CH2DONO(t):
```

The rates $j1a$ and $j1b$ are set to be equal since deuteration has little effect on the chromophore.

2a. $\text{CH}_3\text{O} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{HO}_2$

```
> k2a:= 1.9e-15: R2a:=k2a*CH3O(t)*O2:
```

2b. $\text{CH}_2\text{DO} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{DO}_2$

```
> k2b:= (1/7.593)*(2/3)*1.9e-15: R2b:=k2b*CH2DO(t)*O2:
```

2c. $\text{CH}_2\text{DO} + \text{O}_2 \rightarrow \text{CHDO} + \text{HO}_2$

```
> k2c := (2/3)*1.9e-15: R2c:=k2c*CH2DO(t)*O2:
```

The rate k_2c is 2/3 that of k_2a because there are two hydrogen atoms, not three. The rate k_2b is $(1/7.593)*(2/3)$ to match the first-order experimental result.

3a. HO₂ + NO --> OH + NO₂

```
> k3a := 8.1e-12: R3a:=k3a*HO2(t)*NO(t):
```

3b. DO₂ + NO --> OD + NO₂

```
> k3b := 8.1e-12: R3b:=k3b*DO2(t)*NO(t):
```

4a. OH + cC₆H₁₂ --> H₂O + RO₂

```
> k4a := 6.37e-12: R4a:=k4a*OH(t)*C6H12(t):
```

4b. OD + cC₆H₁₂ --> HDO + RO₂

```
> k4b := k4a: R4b:=k4b*OD(t)*C6H12(t):
```

5. RO₂ + NO --> RO + NO₂

```
> k5 := 6.7e-12: R5:=k5*RO2(t)*NO(t):
```

6. NO₂ + hv --> NO + O

```
> j6 := 2*j1a: R6:=j6*NO2(t):
```

7. O + O₂ + M --> O₃ + M

```
> k7 := 6.1e-34: R7:=k7*O_atom(t)*O2*M:
```

8. Formaldehyde photolysis with the Ford chamber lamps is about 0.05 % as fast as that of methyl nitrite. It will be divided 1:3 between radical and molecular channels. The relative photolysis rates for the deuterated formaldehydes, channel specific, are taken from Feilberg et al., 2007: molecular jhcho/jhcdo = 1.82; radical jhcho/jhcdo = 1.10

8a. CH₂O + hv --> CO + H₂

```
> j8a := 0.05*0.75*j1a: R8a:=j8a*CH2O(t):
```

8b. CHDO + hv --> CO + HD

```
> j8b := j8a/1.82: R8b:=j8b*CHDO(t):
```

9a. CH₂O + hv --> CO + 2*HO₂

```
> j9a := 0.05*0.25*j1a: R9a:=j9a*CH2O(t):
```

9b. CHDO + hv --> CO + HO₂ + DO₂

```
> j9b := j9a/1.10: R9b:=j9b*CHDO(t):
```

10a. HO₂ + NO₂ + M --> PNA + M

```
> k10a := 1.8e-31: R10a:=k10a*HO2(t)*NO2(t)*M:
```

10b. DO₂ + NO₂ + M --> PNAD + M

```
> k10b := 1.8e-31: R10b:=k10b*DO2(t)*NO2(t)*M:
```

11a. HO₂ + CH₂O --> HOCH₂O₂

```
> k11a := 8.01e-14: R11a:=k11a*HO2(t)*CH2O(t):
```

11b. DO₂ + CH₂O --> DOCH₂O₂

```
> k11b := 8.01e-14: R11b:=k11b*DO2(t)*CH2O(t):
```

11c. HO₂ + CHDO --> HOCHDO₂

```
> k11c := 8.01e-14: R11c:=k11c*HO2(t)*CHDO(t):
```

11d. DO₂ + CHDO --> DOCHDO₂

```
> k11d := 8.01e-14: R11d:=k11d*DO2(t)*CHDO(t):
```

12a. HOCH₂O₂ + RO₂ --> HCOOH + RO + HO₂

```
> k12a := 5e-14: R12a:=k12a*HOCH2O2(t)*RO2(t):
```

12b. DOCH₂O₂ + RO₂ --> HCOOD + RO + HO₂

```
> k12b := 5e-14: R12b:=k12b*DOCH2O2(t)*RO2(t):
```

12c. HOCHDO₂ + RO₂ --> DCOOH + RO + HO₂

```
> k12c := 5e-14: R12c:=k12c*HOCHDO2(t)*RO2(t):
```

12d. DOCHDO2 + RO2 --> DCOOD + RO + HO2
 > k12d := 5e-14: R12d:=k12d*DOCHDO2(t) *RO2(t) :
 13a. CH3O + NO + M --> CH3ONO + M
 > k13a := 2.34e-26: R13a:=k13a*CH3O(t) *NO(t) *M:
 13b. CH2DO + NO + M --> CH2DONO + M
 > k13b := 2.34e-26: R13b:=k13b*CH2DO(t) *NO(t) *M:
 14a. CH3O + NO2 + M --> CH3ONO2 + M
 > k14a := 5.46e-26: R14a:=k14a*CH3O(t) *NO2(t) *M:
 14b. CH2DO + NO2 + M --> CH2DONO2 + M
 > k14b := 5.46e-26: R14b:=k14b*CH2DO(t) *NO2(t) *M:
 15a. OH + CH3ONO --> CH2O + NO + H2O
 > k15a := 3.0e-13: R15a:=k15a*OH(t) *CH3ONO(t) :
 15b. OH + CH2DONO --> CHDO + NO + H2O
 > k15b := (2/3)*k15a: R15b:=k15b*OH(t) *CH2DONO(t) :
 15c. OH + CH2DONO --> CH2O + NO + HDO, factor of 1/8 based on relative reactivity of CD in methane.
 > k15c := (1/3)*(1/8)*k15a: R15c:=k15c*OH(t) *CH2DONO(t) :
 15d. OD + CH2DONO --> CH2O + NO + D2O
 > k15d := (1/3)*(1/8)*k15a: R15d:=k15d*OD(t) *CH2DONO(t) :
 15e. OD + CH2DONO --> CHDO + NO + HDO
 > k15e := (2/3)*k15a: R15e:=k15e*OD(t) *CH2DONO(t) :
 15f. OD + CH3ONO --> CH2O + NO + HDO
 > k15f := k15a: R15f:=k15f*OD(t) *CH3ONO(t) :
 16a. CH2O + OH --> H2O + CO + HO2
 > k16a := 8.5e-12: R16a:=k16a*CH2O(t) *OH(t) :
 16b. CHDO + OH --> H2O + CO + DO2, from Feilberg 2004, k(OH+HCHO/kOH+HCDO) 1.28
 > k16b := (8/9)*k16a/1.28: R16b:=k16b*CHDO(t) *OH(t) :
 16c. CHDO + OH --> HDO + CO + HO2
 > k16c := (1/9)*k16a/1.28: R16c:=k16c*CHDO(t) *OH(t) :
 16d. CHDO + OD --> D2O + CO + HO2
 > k16d := (1/9)*k16a/1.28: R16d:=k16d*CHDO(t) *OD(t) :
 16e. CHDO + OD --> HDO + CO + DO2
 > k16e := (8/9)*k16a/1.28: R16e:=k16e*CHDO(t) *OD(t) :
 16f. CH2O + OD --> HDO + CO + HO2
 > k16f := k16a: R16f:=k16f*CH2O(t) *OD(t) :
 17a. HO2 + HO2 --> H2O2
 > k17a := 2.3e-12: R17a:=k17a*HO2(t) *HO2(t) :
 17b. HO2 + DO2 --> HDO2
 > k17b := 8.6e-13: R17b:=k17b*HO2(t) *DO2(t) :
 17c. DO2 + DO2 --> D2O2
 > k17c := 2.0e-14: R17c:=k17c*DO2(t) *DO2(t) :
 18a. H2O2 + hv --> 2OH, the photolysis rates are 0.0038 that of methyl nitrite
 > j18a:=0.0038*j1a: R18a:=j18a*H2O2(t) :
 18b. HDO2 + hv --> OH + OD
 > j18b:=0.0038*j1a: R18b:=j18b*HDO2(t) :
 18c. D2O2 + hv --> 2OD

```

> j18c:=0.0038*j1a: R18c:=j18c*D2O2(t) :
19a. CH3O + NO2 --> CH2O + HONO
> k19a := 2.0e-13: R19a:=k19a*CH3O(t)*NO2(t) :
19b. CH2DO + NO2 --> CHDO + HONO
> k19b := (2/3)*k19a: R19b:=k19b*CH2DO(t)*NO2(t) :
19c. CH2DO + NO2 --> CH2O + DONO
> k19c := (1/8)*(1/3)*k19a: R19c:=k19c*CH2DO(t)*NO2(t) :
20a. HOCH2O2 + HOCH2O2 + O2 --> 2HCOOH + 2HO2
> k20a := 5.5e-12: R20a:=k20a*HOCH2O2(t)*HOCH2O2(t)*O2(t) :
20b. HOCH2O2 + HOCHDO2 + O2 --> 1.5HCOOH + 0.5DCOOH + 1.5HO2 + 0.5DO2
> k20b := 5.5e-12: R20b:=k20b*HOCH2O2(t)*HOCHDO2(t)*O2(t) :
20c. HOCH2O2 + DOCH2O2 + O2 --> HCOOH + HCOOD + 2HO2
> k20c := 5.5e-12: R20c:=k20c*HOCH2O2(t)*DOCH2O2(t)*O2(t) :
20d. HOCH2O2 + DOCHDO2 + O2 --> HCOOH + 0.5HCOOD + 0.5DCOOD +
1.5HO2 + 0.5DO2
> k20d := 5.5e-12: R20d:=k20d*HOCH2O2(t)*DOCHDO2(t)*O2(t) :
20e. HOCHDO2 + HOCH2O2 + O2 --> 0.5DCOOH + 1.5HCOOH + 1.5HO2 + 0.5DO2
> k20e := 5.5e-12: R20e:=k20e*HOCHDO2(t)*HOCH2O2(t)*O2(t) :
20f. HOCHDO2 + HOCHDO2 + O2 --> DCOOH + HCOOH + HO2 + DO2
> k20f := 5.5e-12: R20f:=k20f*HOCHDO2(t)*HOCHDO2(t)*O2(t) :
20g. HOCHDO2 + DOCH2O2 + O2 --> 0.5DCOOH + HCOOD + 0.5HCOOH +
1.5HO2 + 0.5DO2
> k20g := 5.5e-12: R20g:=k20g*HOCHDO2(t)*DOCH2O2(t)*O2(t) :
20h. HOCHDO2 + DOCHDO2 + O2 --> 0.5DCOOH + 0.5HCOOH + 0.5HCOOD +
0.5DCOOD + HO2 + DO2
> k20h := 5.5e-12: R20h:=k20h*HOCHDO2(t)*DOCHDO2(t)*O2(t) :
20i. DOCH2O2 + HOCH2O2 + O2 --> HCOOD + HCOOH + 2HO2
> k20i := 5.5e-12: R20i:=k20i*DOCH2O2(t)*HOCH2O2(t)*O2(t) :
20j. DOCH2O2 + HOCHDO2 + O2 --> HCOOD + 0.5HCOOH + 0.5DCOOH + 1.5HO2 +
0.5DO2
> k20j := 5.5e-12: R20j:=k20j*DOCH2O2(t)*HOCHDO2(t)*O2(t) :
20k. DOCH2O2 + DOCH2O2 + O2 --> 2HCOOD + 2HO2
> k20k := 5.5e-12: R20k:=k20k*DOCH2O2(t)*DOCH2O2(t)*O2(t) :
20l. DOCH2O2 + DOCHDO2 + O2 --> 1.5HCOOD + 0.5DCOOD + 1.5HO2 + 0.5DO2
> k20l := 5.5e-12: R20l:=k20l*DOCH2O2(t)*DOCHDO2(t)*O2(t) :
20m. DOCHDO2 + HOCH2O2 + O2 --> 0.5DCOOD + 0.5HCOOD + HCOOH +
1.5HO2 + 0.5DO2
> k20m := 5.5e-12: R20m:=k20m*DOCHDO2(t)*HOCH2O2(t)*O2(t) :
20n. DOCHDO2 + HOCHDO2 + O2 --> 0.5DCOOD + 0.5HCOOD + 0.5HCOOH +
0.5DCOOH + HO2 + DO2
> k20n := 5.5e-12: R20n:=k20n*DOCHDO2(t)*HOCHDO2(t)*O2(t) :
20o. DOCHDO2 + DOCH2O2 + O2 --> 0.5DCOOD + 1.5HCOOD + 1.5HO2 + 0.5DO2
> k20o := 5.5e-12: R20o:=k20o*DOCHDO2(t)*DOCH2O2(t)*O2(t) :
20p. DOCHDO2 + DOCHDO2 + O2 --> DCOOD + HCOOD + HO2 + DO2
> k20p := 5.5e-12: R20p:=k20p*DOCHDO2(t)*DOCHDO2(t)*O2(t) :
21a. CH3OH + OH --> CH2OH + H2O
k21a := 8.8e-13: R21a:=k21a*CH3OH(t)*OH(t) :

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21b. CH₂DOH + OH --> CH₂OH + HDO
 > k21b := (1/3) * (1/8) * k21a: R21b:=k21b*CH₂DOH(t)*OH(t) :
 21c. CH₂DOH + OH --> CHDOH + H₂O
 > k21c := (2/3) * k21a: R21c:=k21c*CH₂DOH(t)*OH(t) :
 21d. CH₃OH + OD --> CH₂OH + HDO
 > k21d := k21a: R21d:=k21d*CH₃OH(t)*OD(t) :
 21e. CH₂DOH + OD --> CHDOH + HDO
 > k21e := (2/3) * k21a: R21e:=k21e*CH₂DOH(t)*OD(t) :
 21f. CH₂DOH + OD --> CH₂OH + D₂O
 > k21f := (1/3) * (1/8) * k21a: R21f:=k21f*CH₂DOH(t)*OD(t) :
 22a. CH₂OH + O₂ --> CH₂O + HO₂
 > k22a := 9.6e-12: R22a:=k22a*CH₂OH(t)*O₂ :
 22b. CHDOH + O₂ --> CHDO + HO₂
 > k22b := 9.6e-12: R22b:=k22b*CHDOH(t)*O₂ :
 23. O₃ + NO --> NO₂
 > k23 := 1.9e-14: R23:=k23*O₃(t)*NO(t) :
 24a. CO + OH --> CO₂ + HO₂
 > k24a := 2.3e-13: R24a:=k24a*CO(t)*OH(t) :
 24b. CO + OD --> CO₂ + DO₂
 > k24b := 5.0e-14: R24b:=k24b*CO(t)*OD(t) :
 25a. H₂ + OH --> H₂O + HO₂
 > k25a := 6.7e-15: R25a:=k25a*H₂(t)*OH(t) :
 25b. HD + OH --> H₂O + DO₂
 > k25b := 2.5e-15: R25b:=k25b*HD(t)*OH(t) :
 25c. HD + OH --> HDO + HO₂
 > k25c := 6.7e-16: R25c:=k25c*HD(t)*OH(t) :
 25d. H₂ + OD --> HDO + HO₂
 > k25d := 7.4e-15: R25d:=k25d*H₂(t)*OD(t) :
 25e. HD + OD --> HDO + DO₂
 > k25e := 0.9*k25b: R25e:=k25e*HD(t)*OD(t) :
 25f. HD + OD --> D₂O + HO₂
 > k25f := 0.9*k25c: R25f:=k25f*HD(t)*OD(t) :
 26. RO₂ + RO₂ --> 2RO
 > k26 := 1.3e-14: R26:=k26*RO2(t)*RO2(t) :
 27. RO₂ + RO₂ --> RO + cC₆H₁₂
 > k27 := 7.7e-14: R27:=k27*RO2(t)*RO2(t) :
 28a. RO₂ + HO₂ --> cC₆H₁₂
 > k28a := 17.1e-12: R28a:=k28a*RO2(t)*HO2(t) :
 28b. RO₂ + DO₂ --> cC₆H₁₂
 > k28b := k28a: R28b:=k28b*RO2(t)*DO2(t) :
 29. RO + O₂ --> cC₆H₁₂ + HO₂
 > k29 := 2.0e-17: R29:=k29*RO(t)*O2:
 30aa. HOCH₂O₂ + HO₂ --> HOCH₂OOH + O₂
 > k30aa := 6.0e-12: R30aa:=k30aa*HOCH2O2(t)*HO2(t) :
 30ab. HOCH₂O₂ + DO₂ --> HOCH₂OOD + O₂
 > k30ab := k30aa: R30ab:=k30ab*HOCH2O2(t)*DO2(t) :
 30ac. DOCH₂O₂ + HO₂ --> DOCH₂OOH + O₂

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> k30ac := k30aa: R30ac:=k30ac*DOCH2O2 (t) *HO2 (t) :
30ad. DOCH2O2 + DO2 --> DOCH2OOD + O2
> k30ad := k30aa: R30ad:=k30ad*DOCH2O2 (t) *DO2 (t) :
30ae. HOCHDO2 + HO2 --> HOCHDOOH + O2
> k30ae := k30aa: R30ae:=k30ae*HOCHDO2 (t) *HO2 (t) :
30af. HOCHDO2 + DO2 --> HOCHDOOD + O2
> k30af := k30aa: R30af:=k30af*HOCHDO2 (t) *DO2 (t) :
30ag. DOCHDO2 + HO2 --> HOCHDOOH + O2
> k30ag := k30aa: R30ag:=k30ag*DOCHDO2 (t) *HO2 (t) :
30ah. DOCHDO2 + DO2 --> HOCHDOOD + O2
> k30ah := k30aa: R30ah:=k30ah*DOCHDO2 (t) *DO2 (t) :
30ba. HOCH2O2 + HO2 --> HCOOH + H2O + O2
> k30ba := 3.6e-12: R30ba:=k30ba*HOCH2O2 (t) *HO2 (t) :
30bb. HOCH2O2 + DO2 --> HCOOH + HDO + O2
> k30bb := k30ba: R30bb:=k30bb*HOCH2O2 (t) *DO2 (t) :
30bc. DOCH2O2 + HO2 --> HCOOD + H2O + O2
> k30bc := k30ba: R30bc:=k30bc*DOCH2O2 (t) *HO2 (t) :
30bd. DOCH2O2 + DO2 --> HCOOD + HDO + O2
> k30bd := k30ba: R30bd:=k30bd*DOCH2O2 (t) *DO2 (t) :
30be. HOCHDO2 + HO2 --> DCOOH + H2O + O2
> k30be := k30ba: R30be:=k30be*HOCHDO2 (t) *HO2 (t) :
30bf. HOCHDO2 + DO2 --> DCOOH + HDO + O2
> k30bf := k30ba: R30bf:=k30bf*HOCHDO2 (t) *DO2 (t) :
30bg. DOCHDO2 + HO2 --> DCOOD + H2O + O2
> k30bg := k30ba: R30bg:=k30bg*DOCHDO2 (t) *HO2 (t) :
30bh. DOCHDO2 + DO2 --> DCOOD + HDO + O2
> k30bh := k30ba: R30bh:=k30bh*DOCHDO2 (t) *DO2 (t) :
30ca. HOCH2O2 + HO2 --> HOCH2O + OH + O2
> k30ca := 2.4e-12: R30ca:=k30ca*HOCH2O2 (t) *HO2 (t) :
30cb. HOCH2O2 + DO2 --> HOCH2O + OD + O2
> k30cb := k30ca: R30cb:=k30cb*HOCH2O2 (t) *DO2 (t) :
30cc. DOCH2O2 + HO2 --> DOCH2O + OH + O2
> k30cc := k30ca: R30cc:=k30cc*DOCH2O2 (t) *HO2 (t) :
30cd. DOCH2O2 + DO2 --> DOCH2O + OD + O2
> k30cd := k30ca: R30cd:=k30cd*DOCH2O2 (t) *DO2 (t) :
30ce. HOCHDO2 + HO2 --> HOCHDO + OH + O2
> k30ce := k30ca: R30ce:=k30ce*HOCHDO2 (t) *HO2 (t) :
30cf. HOCHDO2 + DO2 --> HOCHDO + OD + O2
> k30cf := k30ca: R30cf:=k30cf*HOCHDO2 (t) *DO2 (t) :
30cg. DOCHDO2 + HO2 --> HOCHDO + OH + O2
> k30cg := k30ca: R30cg:=k30cg*DOCHDO2 (t) *HO2 (t) :
30ch. DOCHDO2 + DO2 --> DOCHDO + OD + O2
> k30ch := k30ca: R30ch:=k30ch*DOCHDO2 (t) *DO2 (t) :
31a. NO2 + OH + M --> HNO3
> k31a := 4.1E-11: R31a := k31a*NO2 (t) *OH (t) : #M is included
in rate, cf JPL
31b. NO2 + OD + M --> DNO3

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> k31b := 9.3E-11:R31b := k31b*NO2(t)*OD(t):
32a. CH3ONO2 + OH --> CH2O + H2O + NO2
> k32a := 3.0e-13: R32a:=k32a*OH(t)*CH3ONO2(t):
32b. CH2DONO2 + OH --> CH2O + HDO + NO2
> k32b := (1/3)*(1/8)*k32a: R32b:=k32b*OH(t)*CH2DONO2(t):
32c. CH2DONO2 + OH --> CHDO + H2O + NO2
> k32c := (2/3)*k32a: R32c:=k32c*OH(t)*CH2DONO2(t):
32d. CH3ONO2 + OD --> CH2O + HDO + NO2
> k32d := k32a: R32d:=k32d*OD(t)*CH3ONO2(t):
32e. CH2DONO2 + OD --> CH2O + D2O + NO2
> k32e := (1/3)*(1/8)*k32a: R32e:=k32e*OD(t)*CH2DONO2(t):
32f. CH2DONO2 + OD --> CHDO + HDO + NO2
> k32f := (2/3)*k32a: R32f:=k32f*OD(t)*CH2DONO2(t):
33a. HOCH2O2 --> HO2 + CH2O
> k33a := 150:R33a := k33a*HOCH2O2(t):
33b. DOCH2O2 --> DO2 + CH2O
> k33b := 150:R33b := k33b*DOCH2O2(t):
33c. HOCHDO2 --> HO2 + CHDO
> k33c := 150:R33c := k33c*HOCHDO2(t):
33d. DOCHDO2 --> DO2 + CHDO
> k33d := 150:R33d := k33d*DOCHDO2(t):
>
34a. PNA --> HO2 + NO2
> k34a := 10:R34a := k34a*PNA(t):

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REFERENCES: Photolysis rate for CH3ONO is derived from experimental data, other photolysis rates calculated using estimated lamp flux curve and JPL cross section to derive a photolysis rate relative to methyl nitrite. Reaction rates are from JPL or NIST.

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Definition of differential equations with initial conditions

For example the equation $d(CH3ONO)/dt = -R1a+R13a-R15a-R15f$ is written:

```

> D_CH3ONO:= diff(CH3ONO(t),t) = -R1a+R13a-R15a-R15f,
CH3ONO(0)=CH3ONO_zero:
> D_CH3O:= diff(CH3O(t),t) = R1a - R2a - R13a - R14a -
R19a, CH3O(0)=startconc:
> D_NO:= diff(NO(t),t) = R1a+R1b-R3a-R3b-R5+R6-R13a-
R13b+R15a+R15b+R15c+R15d+R15e+R15f-R23, NO(0) = startconc:
> D_CH2DONO:= diff(CH2DONO(t),t) = -R1b+R13b-R15b-R15c-
R15d-R15e, CH2DONO(0)=CH2DONO_zero:
> D_CH2DO:= diff(CH2DO(t),t) = R1b-R2b-R2c-R13b-R14b-R19b-
R19c, CH2DO(0)=startconc:
```

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> D_CH2O:= diff(CH2O(t),t) = R2a+R2b-R8a-R9a-R11a-
R11b+R15a+R15c+R15d+R15f-R16a-
R16f+R19a+R19c+R22a+R32a+R32b+R32d+R32e+R33a+R33b,
CH2O(0)=startconc:
> D_HO2:= diff(HO2(t),t) = R2a+R2c-R3a+2*R9a+R9b-R10a-R11a-
R11c+R12a+R12b+R12c+R12d+R16a+R16c+R16d+R16f-2*R17a-
R17b+2*R20a+1.5*R20b+2*R20c+1.5*R20d+1.5*R20e+R20f+1.5*R20g
+R20h+2*R20i+2*R20j+2*R20k+1.5*R20l+1.5*R20m+R20n+1.5*R20o+
R20p+R22a+R22b+R24a+R25a+R25c+R25d+R25f-R28a+R29-R30aa-
R30ac-R30ae-R30ag-R30ba-R30bc-R30be-R30bg-R30ca-R30cc-
R30ce-R30cg+R33a+R33c, HO2(0)=startconc:
> D_DO2:=diff(DO2(t),t) = R2b-R3b+R9b-R10b-R11b-
R11d+R16b+R16e-R17b-
2*R17c+0.5*R20b+0.5*R20d+0.5*R20e+0.5*R20f+0.5*R20g+0.5*R20
h+0.5*R20j+0.5*R20l+0.5*R20m+0.5*R20n+0.5*R20o+R20p+R24b+R2
5b+R25e-R28b-R30ab-R30ad-R30af-R30ah-R30bb-R30bd-R30bf-
R30bh-R30cb-R30cd-R30cf-R30ch+R33b+R33d, DO2(0)=startconc:
> D_CHDO:=diff(CHDO(t),t) = R2c-R8b-R9b-R11c-
R11d+R15b+R15e-R16b-R16c-R16d-
R16e+R19b+R22b+R32c+R32f+R33c+R33d, CHDO(0)=startconc:
> D_OH:=diff(OH(t),t) = R3a-R4a-R15a-R15b-R15c-R16a-R16b-
R16c+2*R18a+R18b-R21a-R21b-R21c-R24a-R25a-R25b-
R25c+R30ca+R30cc+R30ce+R30cg-R31a-R32a-R32b-R32c,
OH(0)=startconc:
> D_NO2:=diff(NO2(t),t) = R3a+R3b+R5-R6-R10a-R10b-R14a-
R14b-R19a-R19b-R19c+R23-R31a-
R31b+R32a+R32b+R32c+R32d+R32e+R32f, NO2(0)=NO2_zero:
> D_OD:=diff(OD(t),t) = R3b-R4b-R15d-R15e-R15f-R16d-R16e-
R16f+R18b+2*R18c-R21d-R21e-R21f-R24b-R25d-R25e-
R25f+R30cb+R30cd+R30cf+R30ch-R31b-R32d-R32e-R32f,
OD(0)=startconc:
> D_C6H12:=diff(C6H12(t),t) = -R4a-R4b+R27+R28a+R28b+R29,
C6H12(0)=C6H12_zero:
> D_H2O:=diff(H2O(t),t) =
R4a+R15a+R15b+R16a+R16b+R21a+R21c+R25a+R25b+R30ba+R30bc+R30
be+R30bg+R32a+R32c, H2O(0)=startconc:
> D_RO2:=diff(RO2(t),t) = R4a+R4b-R5-R12a-R12b-R12c-R12d-
2*R26-2*R27-R28a-R28b, RO2(0)=startconc:
> D_HDO:=diff(HDO(t),t) =
R4b+R15c+R15e+R15f+R16c+R16e+R16f+R21b+R21d+R21e+R25c+R25d+
R25e+R30bb+R30bd+R30bf+R30bh+R32b+R32d+R32f,
HDO(0)=startconc:
> D_RO:=diff(RO(t),t) = R5+R12a+R12b+R12c+R12d+2*R26+R27-
R29, RO(0)=startconc:
> D_O_atom:=diff(O_atom(t),t) = R6-R7, O_atom(0)=startconc:
> D_O3:=diff(O3(t),t) = R7-R23, O3(0)=startconc:
> D_CO:=diff(CO(t),t) =

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R8a+R8b+R9a+R9b+R16a+R16b+R16c+R16d+R16e+R16f-R24a-R24b,
CO(0)=startconc:
> D_H2:=diff(H2(t),t) = R8a-R25a-R25d, H2(0)=startconc:
> D_HD:=diff(HD(t),t) = R8b-R25b-R25c-R25f-R25e,
HD(0)=startconc:
> D_PNA:=diff(PNA(t),t) = R10a-R34a, PNA(0)=startconc:
> D_PNAD:=diff(PNAD(t),t) = R10b, PNAD(0)=startconc:
> D_HOCH2O2:=diff(HOCH2O2(t),t) = R11a-R12a-R20d-R20e-R20i-
R20m-R30aa-R30ab-R30ba-R30bb-R30ca-R30cb-R33a,
HOCH2O2(0)=startconc:
> D_DOCH2O2:=diff(DOCH2O2(t),t) = R11b-R12b-R20c-R20g-R20i-
R20j-2*R20k-R20l-R20o-R30ac-R30ad-R30bc-R30bd-R30cc-R30cd-
R33b, DOCH2O2(0)=startconc:
> D_HOCHDO2:=diff(HOCHDO2(t),t) = R11c-R12c-R20b-R20e-
2*R20f-R20g-R20h-R20j-R20n-R30ae-R30af-R30be-R30bf-R30ce-
R30cf-R33c, HOCHDO2(0)=startconc:
> D_DOCHDO2:=diff(DOCHDO2(t),t) = R11d-R12d-R20d-R20h-R20l-
R20m-R20n-R20o-2*R20p-R30ag-R30ah-R30bg-R30bh-R30cg-R30ch-
R33d, DOCHDO2(0)=startconc:
> D_HCOOH:=diff(HCOOH(t),t) =
R12a+2*R20a+1.5*R20b+R20c+R20d+1.5*R20e+R20f+0.5*R20g+0.5*R
20h+R20i+0.5*R20j+R20m+0.5*R20n+R30ba+R30bb,
HCOOH(0)=startconc:
> D_HCOOD:=diff(HCOOD(t),t) =
R12b+R20c+0.5*R20d+R20g+0.5*R20h+R20i+R20j+2*R20k+1.5*R20l+
0.5*R20m+0.5*R20n+1.5*R20o+R20p+R30bc+R30bd,
HCOOD(0)=startconc:
> D_DCOOH:=diff(DCOOH(t),t) =
R12c+0.5*R20b+0.5*R20e+R20f+0.5*R20g+0.5*R20h+0.5*R20j+0.5*
R20n+R30be+R30bf, DCOOH(0)=startconc:
> D_DCOOD:=diff(DCOOD(t),t) =
R12d+0.5*R20d+0.5*R20h+0.5*R20l+0.5*R20m+0.5*R20n+0.5*R20o+
R20p+R30bg+R30bh, DCOOD(0)=startconc:
> D_CH3ONO2:=diff(CH3ONO2(t),t) = R14a-R32a-R32d,
CH3ONO2(0)=startconc:
> D_CH2DONO2:=diff(CH2DONO2(t),t) = R14b-R32b-R32c-R32e-
R32f, CH2DONO2(0)=startconc:
> D_D2O:=diff(D2O(t),t) = R15d+R16d+R21f+R25f+R32e,
D2O(0)=startconc:
> D_H2O2:=diff(H2O2(t),t) = R17a-R18a, H2O2(0)=startconc:
> D_HDO2:=diff(HDO2(t),t) = R17b-R18b, HDO2(0)=startconc:
> D_D2O2:=diff(D2O2(t),t) = R17c-R18c, D2O2(0)=startconc:
> D_HONO:=diff(HONO(t),t) = R19a+R19b, HONO(0)=startconc:
> D_DONO:=diff(DONO(t),t) = R19c, DONO(0)=startconc:
> D_CH2OHOH:=diff(CH2OHOH(t),t) = R20a+R20e+R20i+R20m,
CH2OHOH(0)=startconc:
> D_CHDOHOH:=diff(CHDOHOH(t),t) = R20b+R20f+R20j+R20n,

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CHDOHOH(0)=startconc:
> D_CH2OHOD:=diff(CH2OHOD(t),t) = R20c+R20g+R20k+R20o,
CH2OHOD(0)=startconc:
> D_CHDOHOD:=diff(CHDOHOD(t),t) = R20d+R20h+R20l+R20p,
CHDOHOD(0)=startconc:
> D_CH3OH:=diff(CH3OH(t),t) = -R21a-R21d,
CH3OH(0)=CH3OH_zero:
> D_CH2OH:=diff(CH2OH(t),t) = R21a+R21b+R21d+R21f-R22a,
CH2OH(0)=startconc:
> D_CH2DOH:=diff(CH2DOH(t),t) = R21b-R21c-R21e-R21f,
CH2DOH(0)=CH2DOH_zero:
> D_CHDOH:=diff(CHDOH(t),t) = R21c+R21e-R22b,
CHDOH(0)=startconc:
> D_CO2:=diff(CO2(t),t) = R24a+R24b, CO2(0)=startconc:
> D_HOCH2OOH:=diff(HOCH2OOH(t),t) = R30aa+R30ab,
HOCH2OOH(0)=startconc:
> D_DOCH2OOH:=diff(DOCH2OOH(t),t) = R30ac,
DOCH2OOH(0)=startconc:
> D_HOCHDOOH:=diff(HOCHDOOH(t),t) = R30ae+R30ag,
HOCHDOOH(0)=startconc:
> D_HOCHDOOD:=diff(HOCHDOOD(t),t) = R30af+R30ah,
HOCHDOOD(0)=startconc:
> D_DOCH2OOD:=diff(DOCH2OOD(t),t) = R30ad,
DOCH2OOD(0)=startconc:
> D_HOCH2O:=diff(HOCH2O(t),t) = R30ca+R30cb,
HOCH2O(0)=startconc:
> D_DOCH2O:=diff(DOCH2O(t),t) = R30cc+R30cd,
DOCH2O(0)=startconc:
> D_HOCHDO:=diff(HOCHDO(t),t) = R30ce+R30cf,
HOCHDO(0)=startconc:
> D_DOCHDO:=diff(DOCHDO(t),t) = R30cg+R30ch,
DOCHDO(0)=startconc:
> D_HNO3:=diff(HNO3(t),t) = R31a, HNO3(0)=startconc:
> D_DNO3:=diff(DNO3(t),t) = R31b, DNO3(0)=startconc:

```

The following are markers used in making budgets for species components.

```

> D_mR02a:=diff(mR02a(t),t) = R2a, mR02a(0) = startconc:
> D_mR02b:=diff(mR02b(t),t) = R2b, mR02b(0) = startconc:
> D_mR02c:=diff(mR02c(t),t) = R2c, mR02c(0) = startconc:
> D_mR03a:=diff(mR03a(t),t) = R3a, mR03a(0) = startconc:
> D_mR04a:=diff(mR04a(t),t) = R4a, mR04a(0) = startconc:
> D_mR08a:=diff(mR08a(t),t) = R8a, mR08a(0) = startconc:
> D_mR08b:=diff(mR08b(t),t) = R8b, mR08b(0) = startconc:
> D_mR09a:=diff(mR09a(t),t) = R9a, mR09a(0) = startconc:
> D_mR09b:=diff(mR09b(t),t) = R9b, mR09b(0) = startconc:
> D_mR10a:=diff(mR10a(t),t) = R10a, mR10a(0) = startconc:
> D_mR10b:=diff(mR10b(t),t) = R10b, mR10b(0) = startconc:

```

```

> D_mR11a:=diff(mR11a(t),t) = R11a, mR11a(0) = startconc;
> D_mR11b:=diff(mR11b(t),t) = R11b, mR11b(0) = startconc;
> D_mR11c:=diff(mR11c(t),t) = R11c, mR11c(0) = startconc;
> D_mR11d:=diff(mR11d(t),t) = R11d, mR11d(0) = startconc;
> D_mR12a:=diff(mR12a(t),t) = R12a, mR12a(0) = startconc;
> D_mR12b:=diff(mR12b(t),t) = R12b, mR12b(0) = startconc;
> D_mR12c:=diff(mR12c(t),t) = R12c, mR12c(0) = startconc;
> D_mR12d:=diff(mR12d(t),t) = R12d, mR12d(0) = startconc;
> D_mR15a:=diff(mR15a(t),t) = R15a, mR15a(0) = startconc;
> D_mR15b:=diff(mR15b(t),t) = R15b, mR15b(0) = startconc;
> D_mR15c:=diff(mR15c(t),t) = R15c, mR15c(0) = startconc;
> D_mR15d:=diff(mR15d(t),t) = R15d, mR15d(0) = startconc;
> D_mR15e:=diff(mR15e(t),t) = R15e, mR15e(0) = startconc;
> D_mR15f:=diff(mR15f(t),t) = R15f, mR15f(0) = startconc;
> D_mR16a:=diff(mR16a(t),t) = R16a, mR16a(0) = startconc;
> D_mR16b:=diff(mR16b(t),t) = R16b, mR16b(0) = startconc;
> D_mR16c:=diff(mR16c(t),t) = R16c, mR16c(0) = startconc;
> D_mR16d:=diff(mR16d(t),t) = R16d, mR16d(0) = startconc;
> D_mR16e:=diff(mR16e(t),t) = R16e, mR16e(0) = startconc;
> D_mR16f:=diff(mR16f(t),t) = R16f, mR16f(0) = startconc;
> D_mR17a:=diff(mR17a(t),t) = R17a, mR17a(0) = startconc;
> D_mR17b:=diff(mR17b(t),t) = R17b, mR17b(0) = startconc;
> D_mR17c:=diff(mR17c(t),t) = R17c, mR17c(0) = startconc;
> D_mR18a:=diff(mR18a(t),t) = R18a, mR18a(0) = startconc;
> D_mR18b:=diff(mR18b(t),t) = R18b, mR18b(0) = startconc;
> D_mR19a:=diff(mR19a(t),t) = R19a, mR19a(0) = startconc;
> D_mR19b:=diff(mR19b(t),t) = R19b, mR19b(0) = startconc;
> D_mR19c:=diff(mR19c(t),t) = R19c, mR19c(0) = startconc;
> D_mR20a:=diff(mR20a(t),t) = R20a, mR20a(0) = startconc;
> D_mR20b:=diff(mR20b(t),t) = R20b, mR20b(0) = startconc;
> D_mR20c:=diff(mR20c(t),t) = R20c, mR20c(0) = startconc;
> D_mR20d:=diff(mR20d(t),t) = R20d, mR20d(0) = startconc;
> D_mR20e:=diff(mR20e(t),t) = R20e, mR20e(0) = startconc;
> D_mR20f:=diff(mR20f(t),t) = R20f, mR20f(0) = startconc;
> D_mR20g:=diff(mR20g(t),t) = R20g, mR20g(0) = startconc;
> D_mR20h:=diff(mR20h(t),t) = R20h, mR20h(0) = startconc;
> D_mR20i:=diff(mR20i(t),t) = R20i, mR20i(0) = startconc;
> D_mR20j:=diff(mR20j(t),t) = R20j, mR20j(0) = startconc;
> D_mR20k:=diff(mR20k(t),t) = R20k, mR20k(0) = startconc;
> D_mR20l:=diff(mR20l(t),t) = R20l, mR20l(0) = startconc;
> D_mR20m:=diff(mR20m(t),t) = R20m, mR20m(0) = startconc;
> D_mR20n:=diff(mR20n(t),t) = R20n, mR20n(0) = startconc;
> D_mR20o:=diff(mR20o(t),t) = R20o, mR20o(0) = startconc;
> D_mR20p:=diff(mR20p(t),t) = R20p, mR20p(0) = startconc;
> D_mR21a:=diff(mR21a(t),t) = R21a, mR21a(0) = startconc;
> D_mR21b:=diff(mR21b(t),t) = R21b, mR21b(0) = startconc;
> D_mR21c:=diff(mR21c(t),t) = R21c, mR21c(0) = startconc;

```

```

> D_mR22a:=diff(mR22a(t),t) = R22a, mR22a(0) = startconc;
> D_mR22b:=diff(mR22b(t),t) = R22b, mR22b(0) = startconc;
> D_mR24a:=diff(mR24a(t),t) = R24a, mR24a(0) = startconc;
> D_mR25a:=diff(mR25a(t),t) = R25a, mR25a(0) = startconc;
> D_mR25b:=diff(mR25b(t),t) = R25b, mR25b(0) = startconc;
> D_mR25c:=diff(mR25c(t),t) = R25c, mR25c(0) = startconc;
> D_mR25d:=diff(mR25d(t),t) = R25d, mR25d(0) = startconc;
> D_mR25e:=diff(mR25e(t),t) = R25e, mR25e(0) = startconc;
> D_mR25f:=diff(mR25f(t),t) = R25f, mR25f(0) = startconc;
> D_mR28a:=diff(mR28a(t),t) = R28a, mR28a(0) = startconc;
> D_mR28b:=diff(mR28b(t),t) = R28b, mR28b(0) = startconc;
> D_mR29:=diff(mR29(t),t) = R29, mR29(0) = startconc;
> D_mR30aa:=diff(mR30aa(t),t) = R30aa, mR30aa(0) =
startconc;
> D_mR30ab:=diff(mR30ab(t),t) = R30ab, mR30ab(0) =
startconc;
> D_mR30ac:=diff(mR30ac(t),t) = R30ac, mR30ac(0) =
startconc;
> D_mR30ad:=diff(mR30ad(t),t) = R30ad, mR30ad(0) =
startconc;
> D_mR30ae:=diff(mR30ae(t),t) = R30ae, mR30ae(0) =
startconc;
> D_mR30af:=diff(mR30af(t),t) = R30af, mR30af(0) =
startconc;
> D_mR30ag:=diff(mR30ag(t),t) = R30ag, mR30ag(0) =
startconc;
> D_mR30ah:=diff(mR30ah(t),t) = R30ah, mR30ah(0) =
startconc;
> D_mR30ba:=diff(mR30ba(t),t) = R30ba, mR30ba(0) =
startconc;
> D_mR30bb:=diff(mR30bb(t),t) = R30bb, mR30bb(0) =
startconc;
> D_mR30bc:=diff(mR30bc(t),t) = R30bc, mR30bc(0) =
startconc;
> D_mR30bd:=diff(mR30bd(t),t) = R30bd, mR30bd(0) =
startconc;
> D_mR30be:=diff(mR30be(t),t) = R30be, mR30be(0) =
startconc;
> D_mR30bf:=diff(mR30bf(t),t) = R30bf, mR30bf(0) =
startconc;
> D_mR30bg:=diff(mR30bg(t),t) = R30bg, mR30bg(0) =
startconc;
> D_mR30bh:=diff(mR30bh(t),t) = R30bh, mR30bh(0) =
startconc;
> D_mR30ca:=diff(mR30ca(t),t) = R30ca, mR30ca(0) =
startconc;
> D_mR30cb:=diff(mR30cb(t),t) = R30cb, mR30cb(0) =

```

```

startconc:
> D_mR30cc:=diff(mR30cc(t),t) = R30cc, mR30cc(0) =
startconc:
> D_mR30cd:=diff(mR30cd(t),t) = R30cd, mR30cd(0) =
startconc:
> D_mR30ce:=diff(mR30ce(t),t) = R30ce, mR30ce(0) =
startconc:
> D_mR30cf:=diff(mR30cf(t),t) = R30cf, mR30cf(0) =
startconc:
> D_mR30cg:=diff(mR30cg(t),t) = R30cg, mR30cg(0) =
startconc:
> D_mR30ch:=diff(mR30ch(t),t) = R30ch, mR30ch(0) =
startconc:
> D_mR31a:=diff(mR31a(t),t) = R31a, mR31a(0) = startconc:
> D_mR32a:=diff(mR32a(t),t) = R32a, mR32a(0) = startconc:
> D_mR32b:=diff(mR32b(t),t) = R32b, mR32b(0) = startconc:
> D_mR32c:=diff(mR32c(t),t) = R32c, mR32c(0) = startconc:
> D_mR32d:=diff(mR32d(t),t) = R32d, mR32d(0) = startconc:
> D_mR32e:=diff(mR32e(t),t) = R32e, mR32e(0) = startconc:
> D_mR32f:=diff(mR32f(t),t) = R32f, mR32f(0) = startconc:
> D_mR33a:=diff(mR33a(t),t) = R33a, mR33a(0) = startconc:
> D_mR33b:=diff(mR33b(t),t) = R33b, mR33b(0) = startconc:
> D_mR33c:=diff(mR33c(t),t) = R33c, mR33c(0) = startconc:
> D_mR33d:=diff(mR33d(t),t) = R33d, mR33d(0) = startconc:
> D_mR34a:=diff(mR34a(t),t) = R34a, mR34a(0) = startconc:

```

The differential equations are gathered into a system of differential equations, Dsys

```

> Dsys:= [D_CH3ONO, D_CH3O, D_NO, D_CH2DONO, D_CH2DO,
D_CH2O, D_HO2, D_DO2, D_CHDO, D_OH, D_NO2, D_OD, D_C6H12,
D_H2O, D_RO2, D_HDO, D_RO, D_O_atom, D_O3, D_CO, D_H2,
D_HD, D_PNA, D_PNAD, D_HOCH2O2, D_DOCH2O2, D_HOCHDO2,
D_DOCHDO2, D_HCOOH, D_HCOOD, D_DCOOH, D_DCOOD, D_CH3ONO2,
D_CH2DONO2, D_D2O, D_H2O2, D_HDO2, D_D2O2, D_HONO, D_DONO,
D_CH2OHOOH, D_CHDOHOH, D_CH2OHOD, D_CHDOHOD, D_CH3OH,
D_CH2OH, D_CH2DOH, D_CHDOH, D_CO2, D_HOCH2OOH, D_DOCH2OOH,
D_HOCHDOOH, D_HOCHDOOD, D_DOCH2OOD, D_HOCH2O, D_DOCH2O,
D_HOCHDO, D_DOCHDO, D_HNO3, D_DNO3, D_mR02a, D_mR02b,
D_mR02c, D_mR03a, D_mR04a, D_mR08a, D_mR08b, D_mR09a,
D_mR09b, D_mR10a, D_mR10b, D_mR11a, D_mR11b, D_mR11c,
D_mR11d, D_mR12a, D_mR12b, D_mR12c, D_mR12d, D_mR15a,
D_mR15b, D_mR15c, D_mR15d, D_mR15e, D_mR15f, D_mR16a,
D_mR16b, D_mR16c, D_mR16d, D_mR16e, D_mR16f, D_mR17a,
D_mR17b, D_mR17c, D_mR18a, D_mR18b, D_mR19a, D_mR19b,
D_mR19c, D_mR20a, D_mR20b, D_mR20c, D_mR20d, D_mR20e,
D_mR20f, D_mR20g, D_mR20h, D_mR20i, D_mR20j, D_mR20k,
D_mR20l, D_mR20m, D_mR20n, D_mR20o, D_mR20p, D_mR21a,
D_mR21b, D_mR21c, D_mR22a, D_mR22b, D_mR24a, D_mR25a,
D_mR25b, D_mR25c, D_mR25d, D_mR25e, D_mR25f, D_mR28a,
```

```
D_mR28b, D_mR29, D_mR30aa, D_mR30ab, D_mR30ac, D_mR30ad,
D_mR30ae, D_mR30af, D_mR30ag, D_mR30ah, D_mR30ba, D_mR30bb,
D_mR30bc, D_mR30bd, D_mR30be, D_mR30bf, D_mR30bg,
D_mR30bh,D_mR30ca, D_mR30cb, D_mR30cc, D_mR30cd, D_mR30ce,
D_mR30cf, D_mR30cg, D_mR30ch, D_mR31a, D_mR32a, D_mR32b,
D_mR32c, D_mR32d, D_mR32e, D_mR32f, D_mR33a, D_mR33b,
D_mR33c, D_mR33d, D_mR34a]:
```

```
>
```

Solution and plotting

```
> with(plots):
Warning, the name changecoords has been redefined
```

Examples

The first step is to define the calculation procedure, p. Maxfun=0 is necessary for long time plots, stiff = true is used for so-called stiff initial value problems (IVP), where different magnitudes will reach steady state at very different time scales.

```
> p:= dsolve(Dsys,numeric,maxfun=0,stiff=true):
```

Next the solution is found at specific times using the procedure p.

Result after 1 second:

```
> p(1);
```


Finally, extract the concentrations of each species/reaction marker at 20 s intervals.

```
> j:=0;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
> j:=1;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
> j:=2;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 0$

$t, C6H12(t), CH2DO(t), CH2DOH(t)$

1, 1, 2262009590175448, 18064009, 44452500972406

21, 21, 2262016615263571, 3961788, 44449563509199

41, 41, 2262020780896112, 2865596, 44446304019080

61, 61, 2262023112351033, 2371058, 44442968899617

81, 81, 2262024696773336, 2073032, 44439627617103

101, 101, 2262025877189123, 1867568, 44436307425925

121, 121, 2262026806068759, 1714345, 44433020573319

141, 141, 2262027564281749, 1594040, 44429772751046
161, 161, 2262028199726625, 1496086, 44426566439695
181, 181, 2262028743020558, 1414148, 44423402433414
201, 201, 2262029214861098, 1344168, 44420280603313
221, 221, 2262029629861137, 1283407, 44417200305521
241, 241, 2262029998689748, 1229941, 44414160610591
261, 261, 2262030329363103, 1182371, 44411160436529
281, 281, 2262030628050157, 1139651, 44408198628286
301, 301, 2262030899583500, 1100982, 44405274006383

$$j := 1$$

CH2DONO(*t*), *CH2DONO2*(*t*), *CH2O*(*t*), *CH2OH*(*t*)
1, 1105095147207160, 61342129088, 17523394457, 0
21, 1101342606662267, 3228128786872, 82118008411, 0
41, 1097322584207876, 6930832037933, 114839338462, 0
61, 1093241162126371, 10756916401221, 140119976958, 0
81, 1089166552336962, 14609046247262, 161468546123, 0
101, 1085125709026225, 18448871268766, 180265148937, 0
121, 1081130526094499, 22258613008691, 197223643711, 0
141, 1077186269579706, 26029483409335, 212771175877, 0
161, 1073294954111217, 29757153276297, 227188024945, 0

181, 1069456892247125, 33439687011047, 240670264065, 0
201, 1065671474873664, 37076499910111, 253361684212, 0
221, 1061937590933342, 40667792139218, 265371624119, 0
241, 1058253863982715, 44214224661531, 276785645297, 0
261, 1054618789407673, 47716726727103, 287672279183, 0
281, 1051030815496811, 51176378279468, 298087483874, 0
301, 1047488391902031, 54594336474535, 308077697576, 0

$$j := 2$$

CH₂OHOD(t), CH₂OHOH(t), CH₃O(t), CH₃OH(t)

1, 3998763, 65055388, 2845, 7113529592
21, 42775903, 2684237338, 632, 7112781136
41, 65850573, 5797980957, 457, 7111948725
61, 85654495, 9058593810, 379, 7111096659
81, 103742708, 12372701531, 331, 7110242881
101, 120716091, 15699498308, 298, 7109394426
121, 136878915, 19017734524, 274, 7108554461
141, 152409684, 22315294387, 255, 7107724461
161, 167423596, 25584919484, 239, 7106905070
181, 182000214, 28822163727, 226, 7106096500
201, 196197367, 32024309649, 215, 7105298722

221, 210058806, 35189750063, 205, 7104511575

241, 223618712, 38317614118, 196, 7103734823

261, 236904512, 41407531496, 189, 7102968191

281, 249938706, 44459477822, 182, 7102211385

301, 262740100, 47473669893, 176, 7101464104

```
> j:=3;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 3$

$CH_3ONO(t)$, $CH_3ONO_2(t)$, $CHDO(t)$, $CHDOH(t)$

1, 176837320546, 9609018, 133321555067, 5

21, 176209545979, 513561651, 638422142342, 6

41, 175551360687, 1104206269, 903586529690, 6

61, 174886230302, 1714863492, 1112667436539, 6

81, 174223726496, 2329833964, 1291902457691, 6

101, 173567638669, 2942927641, 1451620504289, 6

121, 172919599820, 3551270805, 1597178346838, 6

141, 172280290655, 4153439571, 1731792439226, 6

161, 171649926830, 4748729537, 1857581476823, 6

```

181, 171028483249, 5336822851, 1976033559311, 6
201, 170415806951, 5917620059, 2088244373602, 6
221, 169811677602, 6491148786, 2195050376137, 6
241, 169215841357, 7057511427, 2297108646093, 6
261, 168628030291, 7616854050, 2394947442747, 6
281, 168047973715, 8169347380, 2488999660168, 5
301, 167475404780, 8715174908, 2579625789576, 5

> j:=4;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 4$$

CHDOHOD(t), CHDOHOH(t), CO(t), CO2(t)

```

1, 30378371, 220308683, 7836302, 3
21, 328590015, 8159692925, 906136267, 10429
41, 509083701, 17523494844, 2565585504, 61448
61, 665636819, 27409747474, 4743258608, 173375
81, 809824218, 37542534339, 7335536942, 359828
101, 946072563, 47792418733, 10279341775, 630810
121, 1076599974, 58087231418, 13530909284, 994030

```

141, 1202694123, 68382750139, 17057558256, 1455608
161, 1325177572, 78650251939, 20833684206, 2020502
181, 1444612921, 88870368747, 24838534081, 2692790
201, 1561405414, 99029730281, 29054855206, 3475856
221, 1675859129, 109118990192, 33468020454, 4372534
241, 1788209931, 119131596172, 38065432762, 5385206
261, 1898645882, 129062990771, 42836103933, 6515880
281, 2007320444, 138910071364, 47770346746, 7766257
301, 2114361329, 148670812824, 52859543550, 9137772

```
> j:=5;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 5$

$D2O(t), D2O2(t), DCOOD(t), DCOOH(t)$

1, 7188712, 1391759, 30378372, 220308684
21, 75749966, 2585266, 328590015, 8159692934
41, 116027893, 2620481, 509083701, 17523494858
61, 150361874, 2635416, 665636819, 27409747492
81, 181591588, 2644147, 809824219, 37542534361

101, 210827736, 2650030, 946072564, 47792418758
 121, 238638456, 2654321, 1076599975, 58087231446
 141, 265359566, 2657614, 1202694124, 68382750170
 161, 291208827, 2660230, 1325177573, 78650251972
 181, 316336923, 2662361, 1444612922, 88870368782
 201, 340853290, 2664131, 1561405415, 99029730319
 221, 364840447, 2665620, 1675859130, 109118990232
 241, 388362510, 2666889, 1788209932, 119131596214
 261, 411470538, 2667979, 1898645883, 129062990815
 281, 434206027, 2668923, 2007320445, 138910071409
 301, 456603298, 2669743, 2114361330, 148670812871

```

> j:=6;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 6$$

$DNO3(t), DO2(t), DOCH2O(t), DOCH2O2(t)$

1, 118741, 8259303960, 0, 0
 21, 8109578, 394536929, 0, 0
 41, 18603906, 228547997, 0, 0

```

61, 30296502, 167546223, 0, 0
81, 42741086, 135029920, 0, 0
101, 55713484, 114485981, 0, 0
121, 69079464, 100164520, 0, 0
141, 82750383, 89519231, 0, 0
161, 96663879, 81241624, 0, 0
181, 110774085, 74586853, 0, 0
201, 125046138, 69097972, 0, 0
221, 139452842, 64478025, 0, 0
241, 153972552, 60525169, 0, 0
261, 168587741, 57096985, 0, 0
281, 183284025, 54089853, 0, 0
301, 198049456, 51426496, 0, 0

> j:=7;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=7

```

$$DOCH2OOD(t), DOCH2OOH(t), DOCHDO(t), DOCHDO2(t)$$

$$1, 0, 0, 0, 0$$

```

21, 0, 0, 0, 0
41, 0, 0, 0, 0
61, 0, 0, 0, 0
81, 0, 0, 0, 0
101, 0, 0, 0, 0
121, 0, 0, 1, 0
141, 0, 0, 1, 0
161, 0, 0, 1, 0
181, 0, 0, 1, 0
201, 0, 0, 1, 0
221, 0, 0, 1, 0
241, 0, 0, 1, 0
261, 0, 0, 1, 0
281, 0, 0, 1, 0
301, 0, 0, 1, 0

> j:=8;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j:=8

```

DONO(t), H2(t), H2O(t), H2O2(t)

1, 410, 618255, 49238195705, 8433336095

21, 21581, 61929998, 1738128378232, 40148995674

41, 46335, 169263682, 3651166407934, 50752532992

61, 71914, 307393680, 5616469274832, 57656438938

81, 97668, 470526492, 7589258399278, 62750185791

101, 123341, 655253187, 9551946461181, 66750524067

121, 148813, 859239481, 11496539688268, 70015791210

141, 174027, 1080748438, 13419232390188, 72752926301

161, 198952, 1318417231, 15318276578362, 75092820356

181, 223576, 1571136417, 17193011530644, 77123678686

201, 247894, 1837978001, 19043377375497, 78907798822

221, 271909, 2118149475, 20869654378948, 80490808038

241, 295625, 2410962824, 22672315784758, 81907107994

261, 319048, 2715812764, 24451941964083, 83183259997

281, 342184, 3032160905, 26209168727212, 84340182314

301, 365043, 3359523925, 27944655404132, 85394628186

```
> j:=9;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
```

end do;

j := 9

HCOOD(t), HCOOH(t), HD(t), HDO(t)

1, 38375897, 350419460, 2580501, 6841201588

21, 414141820, 13528167604, 262663664, 72569892398

41, 640784846, 29119456763, 724218514, 111555481632

61, 836945809, 45526935099, 1324327021, 144846974371

81, 1017309633, 62287937408, 2038923294, 175110985759

101, 1187504745, 79191415357, 2853740403, 203394829522

121, 1350357805, 96122700475, 3758935313, 230237819347

141, 1507513491, 113013338924, 4747131701, 255961343744

161, 1660024764, 129820090917, 5812503829, 280775680805

181, 1808613349, 146514696213, 6950280342, 304827715422

201, 1953800149, 163078349592, 8156447990, 328225156640

221, 2095976740, 179498490331, 9427561828, 351050007967

241, 2235447354, 195766824421, 10760616976, 373366597142

261, 2372454907, 211878053777, 12152958245, 395226631778

281, 2507197857, 227829027022, 13602214279, 416672524864

301, 2639841529, 243618152625, 15106248175, 437739662965

> j:=10;

lhs(p(1)[4*j+1]), lhs(p(1)[4*j+2]), lhs(p(1)[4*j+3]), lhs(p(1)[4*j+4]);

```
for i from 1 by 20 while i < 302 do  
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs  
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));  
end do;
```

$$j := 10$$

$HDO_2(t)$, $HNO_3(t)$, $HO_2(t)$, $HOCH_2O(t)$

1, 434364352, 378875, 61268355930, 0

21, 1106005515, 112137713, 17446081724, 2

41, 1183436529, 354104985, 13391641204, 3

61, 1224396812, 680363134, 11263399763, 4

81, 1251451605, 1066319214, 9863317828, 5

101, 1271252562, 1496843481, 8842395837, 5

121, 1286637902, 1961832636, 8051792707, 6

141, 1299071993, 2454154299, 7414673615, 7

161, 1309405335, 2968564906, 6886421002, 7

181, 1318173859, 3501087850, 6438950625, 8

201, 1325736068, 4048632121, 6053512523, 8

221, 1332343008, 4608746450, 5717007307, 9

241, 1338176953, 5179454220, 5419955145, 9

261, 1343374190, 5759139081, 5155288987, 9

281, 1348039121, 6346463422, 4917609036, 10

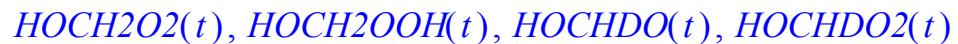
301, 1352253378, 6940308756, 4702710360, 10

```

> j:=11;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 11$$



$$1, 1, 0, 0, 4$$

$$21, 1, 5, 6, 4$$

$$41, 2, 7, 9, 5$$

$$61, 2, 10, 12, 5$$

$$81, 2, 12, 14, 5$$

$$101, 2, 13, 16, 5$$

$$121, 2, 15, 18, 5$$

$$141, 2, 17, 20, 5$$

$$161, 2, 18, 22, 5$$

$$181, 2, 19, 23, 5$$

$$201, 2, 20, 25, 5$$

$$221, 1, 21, 26, 5$$

$$241, 1, 22, 28, 5$$

$$261, 1, 23, 29, 5$$

281, 1, 24, 30, 5

301, 1, 25, 31, 5

```
> j:=12;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 12$

$HOCHDOOD(t)$, $HOCHDOOH(t)$, $HONO(t)$, $NO(t)$

1, 0, 1, 6563, 146061303309

21, 1, 14, 345372, 656913025324

41, 1, 23, 741529, 900321743969

61, 1, 30, 1150898, 1082828297448

81, 1, 36, 1563066, 1234274138265

101, 1, 41, 1973929, 1366281984607

121, 1, 46, 2381585, 1484766258380

141, 1, 51, 2785092, 1593196766818

161, 1, 55, 3183988, 1693802033843

181, 1, 59, 3578065, 1788106966943

201, 1, 62, 3967259, 1877205425797

221, 1, 66, 4351593, 1961911225207

241, 2, 69, 4731135, 2042848045171

261, 2, 72, 5105986, 2120505327682

281, 2, 75, 5476260, 2195274932848

301, 2, 78, 5842082, 2267476172435

```
> j:=13;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 13$

$NO_2(t), O_3(t), OD(t), OH(t)$

1, 4618479215, 6154719, 665957, 4940149

21, 36142619206, 1226105329, 143008, 6324515

41, 53048069857, 3161775409, 113510, 6652333

61, 65105633370, 5015197129, 100063, 6728388

81, 74502162888, 6486454388, 91909, 6715309

101, 82200828600, 7520548623, 86249, 6663425

121, 88720037839, 8176075420, 81994, 6593233

141, 94372585630, 8547549793, 78623, 6514381

161, 99362089171, 8725635992, 75852, 6431831

181, 103828571134, 8781764195, 73509, 6348279

```

201, 107872361746, 8766016594, 71487, 6265238
221, 111567831096, 8710707481, 69712, 6183566
241, 114971402854, 8635363340, 68133, 6103747
261, 118126999979, 8551146816, 66713, 6026044
281, 121069501036, 8464126905, 65424, 5950577
301, 123826894263, 8377442102, 64244, 5877388

> j:=14;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 14$

$$O_atom(t), PNA(t), PNAD(t), RO(t)$$

1, 318, 108391588, 79151079, 446135959

21, 2488, 258838622, 1576658355, 1454869019

41, 3652, 291854729, 2650323062, 1564386575

61, 4482, 301336251, 3593308519, 1596001665

81, 5129, 301992232, 4453248786, 1600433630

101, 5659, 298723452, 5252361837, 1592844633

121, 6107, 293594082, 6003604409, 1579363241

141, 6497, 287591484, 6715485106, 1562885488

161, 6840, 281225693, 7394027814, 1544916880

181, 7148, 274772857, 8043725628, 1526290543

201, 7426, 268385912, 8668060671, 1507487089

221, 7680, 262149866, 9269811737, 1488790186

241, 7915, 256110183, 9851248092, 1470369626

261, 8132, 250289513, 10414257816, 1452325991

281, 8334, 244696828, 10960436229, 1434716031

301, 8524, 239332599, 11491148800, 1417570351

```
> j:=15;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 15$

$RO2(t), mR02a(t), mR02b(t), mR02c(t)$

1, 27886688585, 30411777, 17500971591, 132884877384

21, 19852867407, 147894911, 82402209923, 625679980373

41, 15577717311, 208386004, 115697617642, 878492011348

61, 13214647303, 255644630, 141694676748, 1075887681279

81, 11625793034, 295950093, 163860806132, 1244195101803

101, 10452966243, 331762406, 183552842858, 1393716736765

121, 9537568000, 364348928, 201469348201, 1529756761932

141, 8795832762, 394465194, 218026582111, 1655475839092

161, 8178356496, 422605318, 233496683493, 1772940318966

181, 7653688898, 449113955, 248069423540, 1883591134221

201, 7200651812, 474243215, 261883587760, 1988482083213

221, 6804348676, 498184386, 275044459123, 2088412579540

241, 6453940626, 521086880, 287634259742, 2184006935704

261, 6141310906, 543070187, 299718734985, 2275764356287

281, 5860233811, 564231746, 311351492572, 2364091884706

301, 5605846148, 584652337, 322576968807, 2449326925815

```
> j:=16;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 16$

$mR03a(t), mR04a(t), mR08a(t), mR08b(t)$

1, 49295610535, 48405445071, 618255, 2580501

21, 1740109269932, 1708465864669, 61930020, 262663707

41, 3655468391965, 3588562928288, 169263804, 724218760

61, 5623253942203, 5519819922500, 307394019, 1324327704

81, 7598610915678, 7458263685349, 470527185, 2038924700

101, 9563915344565, 9386634690396, 655254390, 2853742855

121, 11511152813357, 11297095699078, 859241364,
3758939167

141, 13436504894346, 13185921378499, 1080751184,
4747137338

161, 15338215260743, 15051405815789, 1318421030,
5812511654

181, 17215617503191, 16892909561249, 1571141467,
6950290777

201, 19068647755471, 18710382098975, 1837984509,
8156461473

221, 20897583418361, 20504105976200, 2118157652,
9427578813

241, 22702895650333, 22274552429999, 2410972888,
10760637930

261, 24485163291465, 24022297200842, 2715824935,
12152983646

281, 26245021023769, 25747969874234, 3032175409,
13602244615

301, 27983127346866, 27452222618680, 3359540991,
15106283944

```
> j:=17;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
```

end do;

$j := 17$

$mR09a(t), mR09b(t), mR10a(t), mR10b(t)$

1, 206085, 1423185, 572843027, 79151079

21, 20643340, 144863014, 42457074830, 1576658355

41, 56421268, 399417619, 98203104302, 2650323062

61, 102464673, 730386794, 157749809585, 3593308519

81, 156842395, 1124497865, 218176139159, 4453248786

101, 218418130, 1573882423, 278287866290, 5252361837

121, 286413788, 2073111904, 337535241969, 6003604409

141, 360250395, 2618118168, 395657140306, 6715485106

161, 439473677, 3205688245, 452535756486, 7394027814

181, 523713822, 3833190670, 508129073336, 8043725628

201, 612661503, 4498412084, 562436614424, 8668060671

221, 706052551, 5199452557, 615480978973, 9269811737

241, 803657629, 5934654857, 667297423973, 9851248092

261, 905274978, 6702554615, 717927816077, 10414257816

281, 1010725136, 7501843998, 767417040999, 10960436229

301, 1119846997, 8331344476, 815810839119, 11491148800

> j:=18;

lhs(p(1)[4*j+1]), lhs(p(1)[4*j+2]), lhs(p(1)[4*j+3]), lhs(p(1)[4*j+4]);

```
for i from 1 by 20 while i < 302 do  
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs  
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));  
end do;
```

$$j := 18$$

$$mR11a(t), mR11b(t), mR11c(t), mR11d(t)$$

$$1, 57999601, 7997533, 440617809, 60756804$$

$$21, 2117327196, 85551876, 16319398856, 657180571$$

$$41, 4510840566, 131701250, 35047016432, 1018168208$$

$$61, 7011797259, 171309123, 54819535841, 1331274668$$

$$81, 9553969515, 207485574, 75085123920, 1619649671$$

$$101, 12107690602, 241432363, 95584907154, 1892146554$$

$$121, 14657197159, 273758036, 116174547017, 2153201559$$

$$141, 17193324742, 304819595, 136765598968, 2405390034$$

$$161, 19710466901, 334847440, 157300617065, 2650357105$$

$$181, 22205103564, 364000697, 177740865156, 2889227972$$

$$201, 24675012945, 392395024, 198059602667, 3122813124$$

$$221, 27118817486, 420117920, 218238136889, 3351720717$$

$$241, 29535706691, 447237751, 238263363202, 3576422482$$

$$261, 31925260769, 473809372, 258126166702, 3797294544$$

$$281, 34287333974, 499877779, 277820342134, 4014643824$$

$$301, 36621974831, 525480584, 297341839245, 4228725751$$

```

> j:=19;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 19$$

$$mR12a(t), mR12b(t), mR12c(t), mR12d(t)$$

$$1, 0, 0, 0, 0$$

$$21, 0, 0, 0, 0$$

$$41, 0, 0, 0, 0$$

$$61, 0, 0, 0, 0$$

$$81, 0, 0, 0, 0$$

$$101, 0, 0, 0, 0$$

$$121, 0, 0, 0, 0$$

$$141, 0, 0, 0, 0$$

$$161, 0, 0, 1, 0$$

$$181, 0, 0, 1, 0$$

$$201, 0, 0, 1, 0$$

$$221, 0, 0, 1, 0$$

$$241, 0, 0, 1, 0$$

$$261, 0, 0, 1, 0$$

```

281, 0, 0, 1, 0

301, 0, 0, 1, 0

> j:=20;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j := 20

mR15a(t), mR15b(t), mR15c(t), mR15d(t)

1, 178232, 742531535, 46408221, 6398861

21, 6279043, 26161838111, 1635114882, 66546207

41, 13163664, 54849905687, 3428119105, 101130804

61, 20209042, 84210086178, 5263130386, 130191940

81, 27253853, 113569807848, 7098112991, 156300862

101, 34235586, 142668354021, 8916772126, 180471052

121, 41126538, 171390090065, 10711880629, 203225436

141, 47914139, 199682481094, 12480155068, 224876044

161, 54593204, 227523798022, 14220237376, 245627240

181, 61162411, 254908428628, 15931776789, 265621913

201, 67622541, 281839533567, 17614970848, 284964943

221, 73975535, 308325124980, 19270320311, 303736260

```

241, 80223968, 334375865032, 20898491565, 321998631

261, 86370745, 360003791195, 22500236950, 339802565

281, 92418913, 385221556710, 24076347294, 357189542

301, 98371559, 410041968266, 25627623017, 374194209

```
> j:=21;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$$j := 21$$

$mR15e(t), mR15f(t), mR16a(t), mR16b(t)$

1, 102381776, 24575, 381078, 2010870

21, 1064739305, 255552, 57254279, 307030227

41, 1618092858, 388347, 167625996, 906923924

61, 2083071043, 499925, 313361997, 1707164872

81, 2500813793, 600162, 486082388, 2663413588

101, 2887536836, 692950, 680640235, 3748053718

121, 3251606984, 780298, 893485617, 4941797996

141, 3598016704, 863405, 1121998006, 6230247837

161, 3930035835, 943055, 1364152901, 7602165931

181, 4249950607, 1019799, 1618334070, 9048497593

```

201, 4559439093, 1094038, 1883218745, 10561768873
221, 4859780162, 1166079, 2157703099, 12135693521
241, 5151978094, 1236165, 2440851480, 13764903838
261, 5436841044, 1304488, 2731860594, 15444759630
281, 5715032670, 1371209, 3030033363, 17171208154
301, 5987107351, 1436460, 3334759347, 18940678570

> j:=22;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 22$$

$$mR16c(t), mR16d(t), mR16e(t), mR16f(t)$$

$$1, 251359, 34706, 277649, 52617$$

$$21, 38378778, 1275200, 10201597, 1906534$$

$$41, 113365490, 2710107, 21680860, 4019123$$

$$61, 213395609, 4290495, 34323960, 6321862$$

$$81, 332926698, 5989445, 47915563, 8776943$$

$$101, 468506715, 7790316, 62322528, 11361276$$

$$121, 617724749, 9681146, 77449166, 14058417$$

$$141, 778780980, 11652690, 93221518, 16855749$$

161, 950270741, 13697485, 109579883, 19743161
 181, 1131062199, 15809331, 126474644, 22712299
 201, 1320221109, 17982962, 143863693, 25756111
 221, 1516961690, 20213839, 161710716, 28868551
 241, 1720612980, 22498000, 179984003, 32044363
 261, 1930594954, 24831948, 198655581, 35278933
 281, 2146401019, 27212570, 217700564, 38568174
 301, 2367584821, 29637082, 237096655, 41908440

```

> j:=23;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 23$$

$mR17a(t)$, $mR17b(t)$, $mR17c(t)$, $mR18a(t)$
 1, 8433355847, 434365365, 1391763, 19752
 21, 40152271514, 1106113429, 2585540, 3275839
 41, 50760833798, 1183670290, 2621039, 8300805
 61, 57670693654, 1224762510, 2636262, 14254715
 81, 62771041496, 1251952868, 2645283, 20855705
 101, 66778474036, 1271891917, 2651454, 27949970

121, 70051230624, 1287417257, 2656036, 35439414
141, 72796182148, 1299992860, 2659619, 43255847
161, 75144169489, 1310468955, 2662527, 51349133
181, 77183359606, 1319381273, 2664949, 59680920
201, 78976019805, 1327088166, 2667010, 68220983
221, 80567752974, 1333840563, 2668792, 76944936
241, 81992940732, 1339820646, 2670352, 85832739
261, 83278127655, 1345164622, 2671734, 94867658
281, 84444217860, 1349976832, 2672969, 104035546
301, 85507952489, 1354338853, 2674082, 113324303

```
> j:=24;  
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)  
[4*j+4]);  
for i from 1 by 20 while i < 302 do  
  
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs  
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));  
end do;
```

$$j := 24$$

$$mR18b(t), mR19a(t), mR19b(t), mR19c(t)$$

$$1, 1013, 2, 6561, 410$$

$$21, 107914, 82, 345290, 21581$$

$$41, 233761, 177, 741352, 46335$$

$$61, 365698, 275, 1150623, 71914$$

81, 501263, 374, 1562692, 97668
101, 639355, 472, 1973457, 123341
121, 779355, 570, 2381015, 148813
141, 920867, 666, 2784426, 174027
161, 1063620, 762, 3183226, 198952
181, 1207413, 856, 3577208, 223576
201, 1352098, 950, 3966309, 247894
221, 1497556, 1042, 4350551, 271909
241, 1643693, 1133, 4730003, 295625
261, 1790432, 1222, 5104764, 319048
281, 1937711, 1311, 5474949, 342184
301, 2085475, 1399, 5840683, 365043

```
> j:=25;  
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)  
[4*j+4]);  
for i from 1 by 20 while i < 302 do  
  
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs  
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));  
end do;
```

$j := 25$

$mR20a(t), mR20b(t), mR20c(t), mR20d(t)$

1, 13236508, 44824725, 813564, 6180590

21, 643541280, 1954097731, 9971462, 76626865

```

41, 1408095657, 4253301510, 15637367, 120946424
61, 2206071948, 6672775692, 20484279, 159261890
81, 3013125837, 9140310785, 24889287, 194375621
101, 3819220319, 11623886176, 29002089, 227389724
121, 4619432504, 14106534535, 32899907, 258867578
141, 5411143631, 16578380250, 36628728, 289141778
161, 6192917388, 19033355505, 40218610, 318427981
181, 6963977262, 21467620230, 43690546, 346875689
201, 7723936580, 23878719212, 47059944, 374593914
221, 8472648409, 26265097745, 50338557, 401665353
241, 9210117170, 28625806530, 53535636, 428154781
261, 9936444426, 30960314134, 56658651, 454114286
281, 10651794362, 33268383016, 59713758, 479586686
301, 11356371110, 35549984819, 62706127, 504607837

> j:=26;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 26$$

$$mR20e(t), mR20f(t), mR20g(t), mR20h(t)$$

1, 44824725, 151797655, 2755201, 20931102
 21, 1954097731, 5937857681, 30835774, 236901739
 41, 4253301510, 12852161377, 47871699, 370160257
 61, 6672775692, 20188083067, 62566151, 486322563
 81, 9140310785, 27732513992, 76033545, 593676017
 101, 11623886176, 35384438496, 88704657, 695389404
 121, 14106534535, 43086852292, 100797330, 793047260
 141, 16578380250, 50804363863, 112439120, 887566906
 161, 19033355505, 58513651714, 123712179, 979532541
 181, 21467620230, 66198732875, 134673130, 1069342512
 201, 23878719212, 73848365114, 145363053, 1157282902
 221, 26265097745, 81454511679, 155812974, 1243567795
 241, 28625806530, 89011379694, 166047103, 1328362845
 261, 30960314134, 96514791939, 176084841, 1411799857
 281, 33268383016, 103961760053, 185942093, 1493986202
 301, 35549984819, 111350184752, 195632143, 1575011110

```

> j:=27;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do

i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
  
```

$j := 27$

$mR20i(t), mR20j(t), mR20k(t), mR20l(t)$

1, 813564, 2755201, 50017, 379980

21, 9971462, 30835774, 227585, 1741083

41, 15637367, 47871699, 269857, 2071650

61, 20484279, 62566151, 299344, 2304721

81, 24889287, 76033545, 323400, 2496475

101, 29002089, 88704657, 344390, 2664955

121, 32899907, 100797330, 363378, 2818299

141, 36628728, 112439120, 380942, 2960894

161, 40218610, 123712179, 397427, 3095380

181, 43690546, 134673130, 413061, 3223477

201, 47059944, 145363053, 428000, 3346371

221, 50338557, 155812974, 442357, 3464918

241, 53535636, 166047103, 456217, 3579756

261, 56658651, 176084841, 469645, 3691375

281, 59713758, 185942093, 482693, 3800162

301, 62706127, 195632143, 495402, 3906428

```
> j:=28;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
```

```
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));  
end do;
```

$$j := 28$$

$$mR20m(t), mR20n(t), mR20o(t), mR20p(t)$$

$$1, 6180590, 20931102, 379980, 2886699$$

$$21, 76626865, 236901739, 1741083, 13320328$$

$$41, 120946424, 370160257, 2071650, 15905369$$

$$61, 159261890, 486322563, 2304721, 17747644$$

$$81, 194375621, 593676017, 2496475, 19276104$$

$$101, 227389724, 695389404, 2664955, 20628481$$

$$121, 258867578, 793047260, 2818299, 21866837$$

$$141, 289141778, 887566906, 2960894, 23024545$$

$$161, 318427981, 979532541, 3095380, 24121670$$

$$181, 346875689, 1069342512, 3223477, 25171244$$

$$201, 374593914, 1157282902, 3346371, 26182227$$

$$221, 401665353, 1243567795, 3464918, 27161063$$

$$241, 428154781, 1328362845, 3579756, 28112550$$

$$261, 454114286, 1411799857, 3691375, 29040365$$

$$281, 479586686, 1493986202, 3800162, 29947394$$

$$301, 504607837, 1575011110, 3906428, 30835954$$

```

> j:=29;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 29$$

$$mR21a(t), mR21b(t), mR21c(t), mR22a(t)$$

$$1, 21029, 5475532, 87608505, 6254438$$

$$21, 742194, 193252699, 3092043177, 201886279$$

$$41, 1558854, 405903776, 6494460419, 419471177$$

$$61, 2397636, 624324875, 9989198002, 642203340$$

$$81, 3239438, 843542132, 13496674115, 865393414$$

$$101, 4076764, 1061603793, 16985660687, 1087201545$$

$$121, 4906215, 1277624018, 20441984289, 1306799925$$

$$141, 5726176, 1491182103, 23858913653, 1523802775$$

$$161, 6535910, 1702085752, 27233372031, 1738040910$$

$$181, 7335144, 1910263267, 30564212271, 1949458969$$

$$201, 8123858, 2115709531, 33851352493, 2158063960$$

$$221, 8902179, 2318457063, 37095313003, 2363897746$$

$$241, 9670315, 2518559689, 40296955023, 2567021568$$

$$261, 10428519, 2716083023, 43457328363, 2767507066$$

```

281, 11177068, 2911098736, 46577579779, 2965430911
301, 11916247, 3103681027, 49658896430, 3160871516

> j:=30;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=30

mR22b(t), mR24a(t), mR25a(t), mR25b(t)

1, 99688143, 3, 0, 0

21, 3217822299, 10366, 21, 33

41, 6685862086, 61177, 120, 190

61, 10235943649, 172722, 332, 530

81, 13793324382, 358602, 681, 1093

101, 17328679206, 628805, 1184, 1909

121, 20828813846, 991028, 1855, 3002

141, 24287579441, 1451381, 2706, 4393

161, 27702279346, 2014815, 3745, 6100

181, 31072031167, 2685400, 4981, 8136

201, 34396946583, 3466516, 6420, 10516

221, 37677692801, 4360989, 8069, 13250

```

241, 40915245914, 5371197, 9932, 16349

261, 44110747777, 6499147, 12014, 19821

281, 47265420408, 7746532, 14319, 23675

301, 50380513570, 9114787, 16851, 27917

```
> j:=31;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 31$

$mR25c(t), mR25d(t), mR25e(t), mR25f(t)$

1, 0, 0, 0, 0

21, 9, 1, 1, 0

41, 51, 3, 4, 1

61, 142, 6, 8, 2

81, 293, 12, 16, 4

101, 512, 19, 25, 7

121, 805, 29, 38, 10

141, 1177, 40, 53, 14

161, 1635, 54, 71, 19

181, 2181, 70, 93, 25

201, 2818, 88, 117, 31
 221, 3551, 109, 145, 39
 241, 4381, 132, 177, 47
 261, 5312, 157, 211, 57
 281, 6345, 185, 250, 67
 301, 7482, 216, 291, 78

`> j:=32;
 lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
 [4*j+4]);
 for i from 1 by 20 while i < 302 do

 i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
 (p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
 end do;`
 $j := 32$
 $mR28a(t), mR28b(t), mR29(t), mR30aa(t)$
 1, 14593780713, 2017144566, 10116324296, 0
 21, 242849932575, 13536837753, 1499219438320, 4
 41, 333705186178, 15312334732, 3326641532778, 7
 61, 393736806569, 16267013576, 5229511890616, 9
 81, 438333555985, 16902832991, 7151651633480, 11
 101, 473504914458, 17370838382, 9071004566447, 13
 121, 502298804340, 17736142212, 10977298098860, 15
 141, 526490963509, 18032554737, 12865390701854, 16

161, 547211312457, 18279800684, 14732678756417, 17
 181, 565224603094, 18490350465, 16577918417399, 19
 201, 581072747162, 18672567427, 18400633627119, 20
 221, 595153672499, 18832320066, 20200796765784, 21
 241, 607768028676, 18973876425, 21978646656672, 22
 261, 619148340494, 19100432110, 23734580920147, 23
 281, 629477991609, 19214438024, 25469090050713, 24
 301, 638904027740, 19317812383, 27182715859580, 25

```

> j:=33;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 33$$

$mR30ab(t), mR30ac(t), mR30ad(t), mR30ae(t)$

1, 0, 0, 0, 1

21, 0, 0, 0, 13

41, 0, 0, 0, 22

61, 0, 0, 0, 29

81, 0, 0, 0, 35

101, 0, 0, 0, 40

```

121, 0, 0, 0, 45
141, 0, 0, 0, 49
161, 0, 0, 0, 54
181, 0, 0, 0, 57
201, 0, 0, 0, 61
221, 0, 0, 0, 64
241, 0, 0, 0, 68
261, 0, 0, 0, 71
281, 0, 0, 0, 73
301, 0, 0, 0, 76

> j:=34;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=34

mR30af(t), mR30ag(t), mR30ah(t), mR30ba(t)

1, 0, 0, 0, 0
21, 1, 1, 0, 3
41, 1, 1, 0, 4
61, 1, 1, 0, 6

```

```

81, 1, 1, 0, 7
101, 1, 1, 0, 8
121, 1, 1, 0, 9
141, 1, 1, 0, 10
161, 1, 1, 0, 10
181, 1, 1, 0, 11
201, 1, 1, 0, 12
221, 1, 1, 0, 13
241, 1, 1, 0, 13
261, 1, 1, 0, 14
281, 2, 2, 0, 14
301, 2, 2, 0, 15

> j:=35;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=35

```

$$mR30bb(t), mR30bc(t), mR30bd(t), mR30be(t)$$

1, 0, 0, 0, 1

21, 0, 0, 0, 8

```

41, 0, 0, 0, 13
61, 0, 0, 0, 17
81, 0, 0, 0, 21
101, 0, 0, 0, 24
121, 0, 0, 0, 27
141, 0, 0, 0, 30
161, 0, 0, 0, 32
181, 0, 0, 0, 34
201, 0, 0, 0, 37
221, 0, 0, 0, 39
241, 0, 0, 0, 41
261, 0, 0, 0, 42
281, 0, 0, 0, 44
301, 0, 0, 0, 46

> j:=36;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
j :=36

```

$$mR30bf(t), mR30bg(t), mR30bh(t), mR30ca(t)$$

```

1, 0, 0, 0, 0
21, 0, 0, 0, 2
41, 1, 1, 0, 3
61, 1, 1, 0, 4
81, 1, 1, 0, 5
101, 1, 1, 0, 5
121, 1, 1, 0, 6
141, 1, 1, 0, 6
161, 1, 1, 0, 7
181, 1, 1, 0, 7
201, 1, 1, 0, 8
221, 1, 1, 0, 8
241, 1, 1, 0, 9
261, 1, 1, 0, 9
281, 1, 1, 0, 9
301, 1, 1, 0, 10

> j:=37;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$j := 37$

$mR30cb(t), mR30cc(t), mR30cd(t), mR30ce(t)$

1, 0, 0, 0, 0

21, 0, 0, 0, 5

41, 0, 0, 0, 9

61, 0, 0, 0, 11

81, 0, 0, 0, 14

101, 0, 0, 0, 16

121, 0, 0, 0, 18

141, 0, 0, 0, 20

161, 0, 0, 0, 21

181, 0, 0, 0, 23

201, 0, 0, 0, 24

221, 0, 0, 0, 26

241, 0, 0, 0, 27

261, 0, 0, 0, 28

281, 0, 0, 0, 29

301, 0, 0, 0, 30

```
> j:=38;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
```

```
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$$j := 38$$

$$mR30cf(t), mR30cg(t), mR30ch(t), mR31a(t)$$

$$1, 0, 0, 0, 378875$$

$$21, 0, 0, 0, 112137713$$

$$41, 0, 0, 0, 354104985$$

$$61, 0, 0, 0, 680363134$$

$$81, 0, 0, 0, 1066319214$$

$$101, 0, 0, 0, 1496843481$$

$$121, 0, 0, 0, 1961832636$$

$$141, 1, 1, 0, 2454154299$$

$$161, 1, 1, 0, 2968564906$$

$$181, 1, 1, 0, 3501087850$$

$$201, 1, 1, 0, 4048632121$$

$$221, 1, 1, 0, 4608746450$$

$$241, 1, 1, 0, 5179454220$$

$$261, 1, 1, 0, 5759139081$$

$$281, 1, 1, 0, 6346463422$$

$$301, 1, 1, 0, 6940308756$$

```

> j:=39;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;

```

$$j := 39$$

$$mR32a(t), mR32b(t), mR32c(t), mR32d(t)$$

$$1, 5, 1211, 19379, 1$$

$$21, 8893, 2332348, 37317573, 257$$

$$41, 40538, 10612515, 169800236, 857$$

$$61, 97205, 25427282, 406836513, 1750$$

$$81, 178819, 46753880, 748062078, 2909$$

$$101, 284664, 74403874, 1190461986, 4314$$

$$121, 413818, 108136235, 1730179758, 5950$$

$$141, 565312, 147697396, 2363158333, 7804$$

$$161, 738189, 192837281, 3085396496, 9865$$

$$181, 931530, 243315912, 3893054586, 12123$$

$$201, 1144463, 298905937, 4782494997, 14570$$

$$221, 1376168, 359393306, 5750292893, 17197$$

$$241, 1625876, 424577056, 6793232891, 19998$$

$$261, 1892862, 494268715, 7908299440, 22965$$

281, 2176451, 568291531, 9092664489, 26094

301, 2476005, 646479637, 10343674198, 29377

```
> j:=40;
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]),lhs(p(1)
[4*j+4]);
for i from 1 by 20 while i < 302 do
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs
(p(i)[4*j+3])),round(rhs(p(i)[4*j+4]));
end do;
```

$j := 40$

$mR32e(t), mR32f(t), mR33a(t), mR33b(t)$

1, 167, 2676, 129, 8

21, 67364, 1077828, 4262, 70

41, 224376, 3590023, 8825, 104

61, 457834, 7325337, 13487, 132

81, 760634, 12170148, 18175, 158

101, 1127703, 18043256, 22861, 182

121, 1555016, 24880250, 27529, 205

141, 2039206, 32627301, 32173, 227

161, 2577376, 41238011, 36787, 248

181, 3166973, 50671568, 41370, 268

201, 3805722, 60891555, 45919, 289

221, 4491570, 71865127, 50435, 308

241, 5222651, 83562415, 54917, 328

261, 5997255, 95956073, 59364, 347

281, 6813808, 109020930, 63778, 366

301, 7670857, 122733711, 68159, 384

```
> j:=41;  
lhs(p(1)[4*j+1]),lhs(p(1)[4*j+2]),lhs(p(1)[4*j+3]);  
for i from 1 by 20 while i < 302 do  
  
i,round(rhs(p(i)[4*j+1])),round(rhs(p(i)[4*j+2])),round(rhs  
(p(i)[4*j+3]));  
end do;
```

$j := 41$

$mR33c(t)$, $mR33d(t)$, $mR34a(t)$

1, 436, 60, 464451439

21, 12973, 540, 42198236209

41, 26695, 804, 97911249572

61, 40829, 1028, 157448473334

81, 55164, 1232, 217874146927

101, 69600, 1424, 277989142838

121, 84084, 1608, 337241647887

141, 98582, 1785, 395369548822

161, 113073, 1958, 452254530793

181, 127540, 2127, 507854300480

201, 141975, 2293, 562168228512

221, 156368, 2457, 615218829107

241, 170714, 2618, 667041313790

261, 185010, 2776, 717677526564

281, 199251, 2934, 767172344171

301, 213437, 3089, 815571506520

>
>
>
>
>

Comments:

