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A semi-analytical method for calculating rates of new sulfate aerosol formation from the gas phase

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Abstract. The formation of new aerosol from the gas phase is commonly represented in atmospheric modeling with parameterizations of the steady state nucleation rate. Present parameterizations are based on classical nucleation theory or on nucleation rates calculated with a numerical aerosol model. These parameterizations reproduce aerosol nucleation rates calculated with a numerical aerosol model only imprecisely. Additional errors can arise when the nucleation rate is used as a surrogate for the production rate of particles of a given size. We discuss these errors and present a method which allows a more precise calculation of steady state sulfate aerosol formation rates. The method is based on the semi-analytical solution of an aerosol system in steady state and on parameterized rate coefficients for H2SO4 uptake and loss by sulfate aerosol particles, calculated from laboratory and theoretical thermodynamic data.

1 Introduction

Aerosol particles play an important role in the Earth's atmosphere and in the climate system: Aerosols scatter and absorb solar radiation (e.g. Haywood and Boucher, 2000), facilitate heterogeneous and multiphase chemistry (Ravishankara, 1997), and change cloud characteristics in many ways (e.g. Lohmann and Feichter, 2005). Aerosol particles can either be directly emitted from surface sources (primary aerosol) or form from the gas phase (secondary aerosol). The processes and compounds involved in secondary aerosol formation and growth, as well as their relative importance, and the spatial and temporal distribution thereof are the subject of ongoing research. The chemical species of interest include inorganic acids, ammonia, and organic molecules (see, e.g. Heintzenberg, 1989; Heintzenberg et al., 2000; Jacobson

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et al., 2000; Kulmala et al., 2004a, and references therein). Among these, sulfuric acid stands out due to its very low vapor pressure, its numerous sources, and its ubiquity. In clean areas, such as over oceans, sulfuric acid appears as the driving force of secondary aerosol formation (Clarke, 1992; Brock et al., 1995), while over continents and in particular in the continental boundary layer, recently formed aerosol particles contain in addition to sulfate substantial amounts of ammonia (Smith et al., 2005) or organic matter (Allan et al., 2006; Cavalli et al., 2006), which may be involved in their formation process (Coffman and Hegg, 1995; Kulmala et al., 2004b). Secondary aerosol formation can significantly increase concentrations of aerosol particles and cloud condensation nuclei, and therefore requires dependable representations in atmospheric models (Kulmala et al., 2004a).

2 Representing secondary aerosol formation in atmospheric models

Detailed representations of secondary aerosol formation, with a molecular size resolution of the involved processes, are numerically expensive and presently used in box (Lehtinen and Kulmala, 2003; Lovejoy et al., 2004) or parcel models (Kazil et al., 2007). In medium- and large scale atmospheric models, numerically less costly parameterizations of the steady state aerosol nucleation rate are used (e.g. Lauer et al., 2005; Ma and von Salzen, 2006). Aerosol nucleation is the process by which supercritical molecular clusters, particles larger than the critical cluster, form from the gas phase. The critical cluster is the smallest particle whose growth due to uptake of gas phase molecules is uninhibited by a thermodynamic barrier.

Different parameterizations of steady state aerosol nucleation rates have been developed: Vehkamäki et al. (2002) and Napari et al. (2002) parameterized nucleation rates calculated using classical nucleation theory, which rests upon the determination of the surface tension of small molecular clusters of a given composition, and on the vapor pressures of the involved molecules above the corresponding bulk solution. Modgil et al. (2005) parameterized nucleation rates that were calculated with a numerical aerosol model that resolves the initial steps of cluster formation molecule by molecule.

These parameterizations reproduce aerosol formation rates calculated with numerical aerosol models only imprecisely, for different reasons: On the one hand, the concepts of surface tension and bulk solution break down in the context of small molecular clusters. On the other hand, nucleation rates are highly non-linear and vary by many orders of magnitude over the atmospherically relevant ranges of ambient conditions. A precise parameterization of the nucleation rate may therefore require a large set of basis functions, with a corresponding number of coefficients, that need to be determined from a sufficiently large nucleation rates table. However, generating a large nucleation rates table with a detailed aerosol model may be numerically prohibitive.

Independently of the intrinsic errors of nucleation rate parameterizations, errors can arise when the nucleation rate is used as a surrogate for the production rate of particles of a given size. We have therefore chosen a different approach for calculating secondary aerosol formation rates. The method is based on the semi-analytical solution of an aerosol system in steady state, and on parameterized rate coefficients for the uptake and loss of gas phase molecules by aerosol particles. The thermodynamic parameters (entropy and enthalpy change) for the uptake and loss of gas phase molecules by small molecular clusters, which are needed for the calculation of dependable particle formation rates, have been determined in the laboratory only for few atmospherically relevant systems: Curtius et al. (2001) and Froyd and Lovejoy (2003a,b) measured the thermodynamic parameters for the formation of charged sulfuric acid and water clusters, while Hanson and Lovejoy (2006) measured the thermodynamic parameters for their neutral counterparts. We therefore focus in the following on the formation of sulfate aerosol from nucleation of neutral and negative sulfuric acid/water particles. The nucleation of positive sulfuric acid/water particles is thought to be less important for aerosol formation at least at temperatures of the lower troposphere (Froyd and Lovejoy, 2003a), and is not considered here.

3 Neutral and negative sulfate aerosol formation

The scheme of neutral and negative H_2SO_4/H_2O aerosol formation from the gas phase is shown in Fig. 1: The ionization rate q is the rate at which the anions A_0^- and the cations A^+ are produced. Here we assume that $A_0^-=NO_3^-$ (HNO₃). The neutral and negative clusters A_i and A_i^- are defined as

$$A_{i} = (H_{2}SO_{4})_{i}(H_{2}O)_{\overline{x}(i)}$$

$$A_{i}^{-} = HSO_{4}^{-}(H_{2}SO_{4})_{i-1}(H_{2}O)_{\overline{y}(i)}, \quad i = 1, ..., n.$$
(1)

 $\overline{x}(i)$ and $\overline{y}(i)$ are the average H₂O contents of the clusters in equilibrium with respect to H₂O uptake and loss. A₁ is, as a matter of course, gas phase sulfuric acid, which we will denote in the following simply with H₂SO₄. The clusters grow and evaporate with the first order rate coefficients

$$\kappa_i = k_{a_i} \cdot [\text{H}_2\text{SO}_4] \quad , \quad \lambda_i = k_{d_i} \quad ,$$

$$\kappa_i^- = k_{a_i}^- \cdot [\text{H}_2\text{SO}_4] \quad , \quad \lambda_i^- = k_{d_i}^- \quad .$$
(2)

 k_{a_i} and k_{d_i} are the H₂SO₄ uptake and evaporation rate coefficients of the A_i, $k_{a_i}^-$ and $k_{d_i}^-$ the H₂SO₄ uptake and evaporation rate coefficients of the A_i⁻, averaged over the equilibrium H₂O distribution of the clusters. The ω_i and ω_i^- in Fig. 1 are the pseudo first order rate coefficients for loss of the A_i and A_i⁻ by coagulation among each other and onto preexisting aerosol. The p_i and p_i^- are production rates of the A_i and A_i⁻ by coagulation of smaller clusters. The α_i are pseudo first order rate coefficients for the recombination of the A_i⁻ and A_i⁻ by coagulation and the recombination of the A_i and A_i⁻ by coagulation and the recombination of the A_i⁻ with the cations A⁺. The rate coefficients and their calculation are explained in more detail in Sect. 4.

We denote the net steady state formation rate of the A_i and A_i^- with i > n from the A_i and A_i^- with $i \le n$ with $\mathcal{J}(n, p, q, r, s, t, [H_2SO_4])$. \mathcal{J} is a function of pressure p, ionization rate q, relative humidity r, H₂SO₄ condensational sink s, temperature t, and of the sulfuric acid gas phase concentration [H₂SO₄]. The pressure dependence of \mathcal{J} is weak if the clusters A_i and A_i^- with $i \le n$ are much smaller than the mean free path of gas phase molecules (typically > 100 nm in atmospheric conditions), when their H₂SO₄ uptake and loss as well as their coagulation take place in the free molecular regime. \mathcal{J} can be broken down into three contributions,

$$\mathcal{J}(n, p, q, r, s, t, [\mathrm{H}_2\mathrm{SO}_4]) = J_{\mathrm{cond}} + J_{\mathrm{evap}} + J_{\mathrm{coag}} \quad , \quad (3)$$

where

$$J_{\text{cond}} = k_{a_n} [\text{H}_2 \text{SO}_4] [\text{A}_n] + k_{a_n}^- [\text{H}_2 \text{SO}_4] [\text{A}_n^-]$$
(4)

represents for the formation of clusters by condensation of sulfuric acid,

$$J_{\text{evap}} = -k_{d_{n+1}}[\mathbf{A}_{n+1}] - k_{d_{n+1}}^{-}[\mathbf{A}_{n+1}^{-}]$$
(5)

the loss of clusters by evaporation of sulfuric acid, and

$$J_{\text{coag}} = \sum_{i=2}^{n} \sum_{j=\max(i,n+1-i)}^{n} k_{c_{i,j}}[A_i][A_j] + \sum_{i=2}^{n} \sum_{j=n+1-i}^{n} k_{c_{i,j}}^{-}[A_i][A_j^{-}]$$
(6)

the formation of clusters due to coagulation. The calculation of the coagulation rate coefficients $k_{c_{i,j}}$ and $k_{c_{i,j}}^-$ is explained in Sect. 4.

The smallest neutral cluster whose sulfuric acid content *c* satisfies

$$k_{a_c} \cdot [\mathrm{H}_2 \mathrm{SO}_4] \ge k_{d_c}$$

$$\land \quad k_{a_i} \cdot [\mathrm{H}_2 \mathrm{SO}_4] > k_{d_i} \quad \forall \ i > c$$
(7)

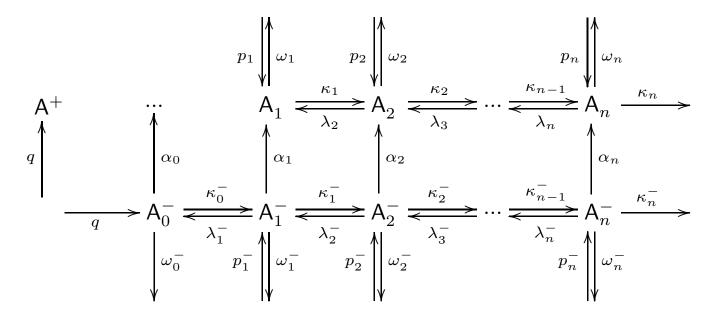


Fig. 1. Reaction scheme of a coupled neutral and negative aerosol system.

is the neutral critical cluster. For $n \gg c$, the particles A_{n+1} and A_{n+1}^- evaporate only very slowly, and $J_{\text{evap}} \approx 0$.

Atmospheric models which account for H_2SO_4/H_2O particles containing more than $n H_2SO_4$ molecules need to be supplied only with the formation rate

$$J(n, p, q, r, s, t, [H_2SO_4]) = J_{\text{cond}} + J_{\text{coag}}$$
(8)

of these particles, since they can either neglect J_{evap} if $n \gg c$, or otherwise calculate it from the concentrations of the particles they account for. We therefore focus in the following on the particle formation rate $J(n, p, q, r, s, t, [H_2SO_4])$, which we will refer to as nucleation rate for n=c.

4 Rate coefficients

The rate coefficients for sulfuric acid uptake by the neutral and negative H₂SO₄/H₂O aerosol particles are calculated with the Fuchs formula for Brownian coagulation (Fuchs, 1964). The effect of particle charge is accounted for as described by Lovejoy et al. (2004). The rate coefficients for sulfuric acid evaporation from the aerosol particles are calculated from the uptake rate coefficients and from the thermodynamic parameters for H₂SO₄ uptake/loss by the particles, described in Sect. 5. The resulting H₂SO₄ uptake and loss rate coefficients are averaged over the equilibrium probability distributions of the particle H₂O content, giving the rate coefficients k_{a_i} , k_{d_i} , $k_{a_i}^-$, and $k_{d_i}^-$. The equilibrium probability distributions of the particle H2O content and the corresponding averages are calculated from the thermodynamic parameters for H₂O uptake/loss by the particles, described in Sect. 5.

The rate coefficients $k_{c_{i,j}}$ for coagulation of the neutral particles among each other, the rate coefficients $k_{c_{i,j}}^-$ for the coagulation of neutral and negative particles, and the rate coefficients $k_{\text{pre},i}$ and $k_{\text{pre},i}^-$ for their coagulation with preexisting aerosol are calculated with the Fuchs formula. The masses and diameters of the particles used in the calculation are determined from their H₂SO₄ and average H₂O contents. The effect of the particle charge is accounted for as described by Lovejoy et al. (2004). Charging of the preexisting aerosol particles is neglected.

The pseudo first order rate coefficients ω_i and ω_i^- (Fig. 1) for loss of the particles by coagulation with each other and with preexisting aerosol are calculated with

$$\omega_{i} = \sum_{j=2}^{n} (1 + \delta_{i,j}) k_{c_{i,j}} [\mathbf{A}_{j}] + \sum_{j=0}^{n} k_{c_{i,j}}^{-} [\mathbf{A}_{j}^{-}] + \frac{k_{\text{pre},i}}{k_{\text{pre},1}} s \quad , \quad i = 1, ..., n \quad ,$$
(9)

and

$$\omega_i^- = \sum_{j=2}^n k_{c_{j,i}}^- [A_j] + \frac{k_{\text{pre},i}}{k_{\text{pre},1}} s \quad , \quad i = 0, ..., n \quad , \tag{10}$$

with the preexisting aerosol H_2SO_4 condensational sink *s*. The summation over the neutral cluster concentrations $[A_j]$ starts with j=2, because coagulation with A_1 is equivalent to uptake of gas phase H_2SO_4 , which is accounted for by the H_2SO_4 uptake rate coefficients.

The production rates p_i of neutral clusters due to coagulation read

$$p_{i} = 0 , \quad i = 1, ..., 3 ,$$

$$p_{i} = \sum_{j=2}^{i-2} \frac{1 + \delta_{j,i-j}}{2} k_{c_{j,i-j}} [A_{j}] [A_{i-j}] , \quad (11)$$

$$i = 4, ..., n .$$

 p_1 equals zero because A₁ is gas phase H₂SO₄. The $p_{i=2,3}$ equal zero, and the summation giving the $p_{i=4,...,n}$ starts with 2 and ends with i-2 because coagulation with A₁ is equivalent to uptake of gas phase H₂SO₄, which is accounted for by the H₂SO₄ uptake rate coefficients.

The production rates p_i^- of negative clusters due to coagulation read

$$p_{1}^{-} = 0 ,$$

$$p_{i}^{-} = \sum_{j=0}^{i-2} k_{c_{i-j,j}}^{-} [A_{i-j}] [A_{j}^{-}] , \quad i = 2, ..., n .$$
(12)

 p_1^- equals zero and the summation giving the $p_{i=2,...,n}^-$ ends with i-2 because coagulation with A₁ is equivalent to uptake of gas phase H₂SO₄, which is accounted for by the H₂SO₄ uptake rate coefficients.

The pseudo first order rate coefficients $\alpha_i = k_{r_i} [A^+]$ describe the recombination of the A_i^- with cations A^+ , where the k_{r_i} are the rate coefficients for recombination of the anions with the cation population. A mass and size independent recombination rate coefficient $k_{r_i} \doteq k_r = 1.6 \times 10^{-6} \text{ cm}^3 \text{ s}^{-1}$ (Bates, 1982) is assumed for all anions/cations in this work.

In atmospheric conditions, the mean free path of gas phase molecules is typically >100 nm. H₂SO₄ uptake and loss as well as the coagulation of particles much smaller than this size take place in the free molecular regime, where the corresponding rate coefficients are essentially independent of pressure. All rate coefficients were therefore calculated at 1013.25 hPa.

5 Thermodynamic parameters for H₂SO₄ and H₂O uptake and loss

The thermodynamic parameters (entropy and enthalpy change) for uptake and loss of H_2SO_4 and H_2O by the small negative clusters are based on the laboratory measurements of Curtius et al. (2001) and of Froyd and Lovejoy (2003b). The thermodynamic parameters for the formation of $(H_2SO_4)_2(H_2O)_{\overline{x}(2)}$ and of $(H_2SO_4)_3(H_2O)_{\overline{x}(3)}$ due to uptake of sulfuric acid from the gas phase are calculated explicitly from fits to the laboratory measurements by Hanson and Lovejoy (2006). These fits read, with RH over water in %,

$$dS(\text{kcal mol}^{-1} \text{ K}^{-1}) = -0.04$$

$$dH(\text{kcal mol}^{-1}) = -18.32 - 4.55 \times 10^{-3} \cdot \text{RH}$$
(13)

for the dimer formation and

$$dS(\text{kcal mol}^{-1} \text{ K}^{-1}) = -0.045$$

$$dH(\text{kcal mol}^{-1}) = -21.41 - 2.63 \times 10^{-2} \cdot \text{RH}$$
 (14)

for the trimer formation.

The thermodynamic parameters for large aerosol particles are based on the the liquid drop model and on H₂SO₄ and H₂O vapor pressures over bulk solutions, calculated with a computer code (S. L. Clegg, personal communication, 2007) that uses data from Giauque et al. (1960) and Clegg et al. (1994). It is assumed that charging of large aerosol has a negligible effect on the uptake and loss of gas phase molecules. The thermodynamic parameters for intermediate size particles are a smooth interpolation of the thermodynamic parameters for the small and large particles. For the negative particles, the interpolation scheme by Froyd (2002) is used. In the case of the neutral particles, exponential correction terms as introduced by Lovejoy et al. (2004) are added to the liquid drop model Gibbs free energies. The correction terms used here are adjusted to match the dimer and trimer data in Eqs. (13) and (14): The term 3 $e^{-(m+n)/5}$ kcal/mol is added to the liquid drop Gibbs free energies for the addition of a sulfuric acid molecule to a $(H_2SO_4)_{m-1}(H_2O)_n$ cluster and for the addition of a water molecule to a $(H_2SO_4)_m(H_2O)_{n-1}$ cluster. The water vapor saturation pressure formulation by Goff (1957) was used in all calculations to transform relative humidity over water to water vapor concentration and vice versa.

6 Parameterization

Calculating H₂SO₄ uptake and loss rate coefficients as described in Sect. 4 is numerically expensive due to the averaging of the rate coefficients over the cluster water content. Using parameterized rate coefficients and average cluster water contents can reduce the computational burden. We parameterize the rate coefficients k_{a_i} , k_{d_i} , $k_{a_i}^-$ and $k_{d_i}^-$ for H₂SO₄ uptake and loss by the neutral and negative clusters and the average cluster H₂O contents $\overline{x}(i)$ and $\overline{y}(i)$ as functions of temperature *t* and relative humidity *r* with a series of Chebyshev polynomials of the first kind $T_u(\overline{t})$ and $T_v(\overline{r})$ up to degrees u' and v', respectively:

$$k(t,r) \approx \tilde{k}_{u',v'}(t,r) = \sum_{u=0}^{u'} \sum_{v=0}^{v'} \alpha_{u,v} T_u(\bar{t}(t)) T_v(\bar{r}(r))$$
(15)

with \overline{t} and \overline{r} defined as

$$\bar{t}(t) = \frac{2t - (t_0 + t_1)}{t_1 - t_0} ,$$

$$\bar{r}(r) = \frac{2r - (r_0 + r_1)}{r_1 - r_0} ,$$
(16)

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on the temperature and relative humidity intervals

$$t \in [t_0, t_1], \ t_0 = 190 \text{ K}, \ t_1 = 300 \text{ K}, r \in [r_0, r_1], \ r_0 = 0.5 \%, \ r_1 = 104 \%.$$
(17)

We determine the coefficients $\alpha_{u,v}$ for $u, v \le 20$ using an orthogonality property of the Chebyshev polynomials:

$$\alpha_{u,v} = \frac{4}{\pi^2 (1 + \delta_{u,0})(1 + \delta_{v,0})} \int_{-1}^1 d\bar{t} \int_{-1}^1 d\bar{r} \ k(\bar{t},\bar{r}) \frac{T_u(\bar{t}) \ T_v(\bar{r})}{\sqrt{1 - (\bar{t})^2} \sqrt{1 - (\bar{r})^2}} \quad .$$
(18)

We then measure the error of the approximation (15) with

$$E_{u',v'} = \max\left|\frac{\tilde{k}_{u',v'}(t,r) - k(t,r)}{k(t,r)}\right|$$
(19)

and determine the cutoff orders $u' \leq 20$ and $v' \leq 20$ which minimize $E_{u',v'}$.

7 Semi-analytical solution for aerosol schemes in steady state

7.1 Neutral aerosol

Here we give a semi-analytical solution for the steady state concentrations of the particles $A_{i=2,...,n}$ in the aerosol scheme in Fig. 2, at a given concentration of the gas phase molecule A_1 . The particles are produced by sources at the rates q_i and lost in sinks with the pseudo first order rate coefficients ρ_i . They grow by condensation of the gas phase molecules A_1 with the pseudo first order rate coefficients κ_i and decay by evaporation of those molecules with the pseudo first order rate coefficients κ_i . Let us start by assuming that the aerosol particles do not interact with each other (no coagulation). With the total pseudo first order rate coefficient for loss of the A_i

$$\sigma_i \doteq \kappa_i + \lambda_i + \rho_i \quad , \quad i = 2, ..., n \tag{20}$$

the system of differential equations for the concentrations $[A_i]$ reads

$$\frac{d[A_i]}{dt} = q_i - \sigma_i[A_i] + \kappa_{i-1}[A_{i-1}] + \lambda_{i+1}[A_{i+1}] ,$$

$$i = 2, ..., n - 1 , \qquad (21)$$

$$\frac{d[A_n]}{dt} = q_n - \sigma_n[A_n] + \kappa_{n-1}[A_{n-1}] .$$

The $[A_i]$ in steady state $(d[A_i]/dt=0)$ can be calculated from this system of equations with

$$[\mathbf{A}_i] = R_{i-1}[\mathbf{A}_{i-1}] + S_{i-1} \quad , \quad i = 2, ..., n \quad .$$
 (22)

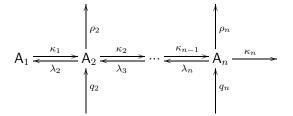


Fig. 2. Reaction scheme of a neutral aerosol system.

The coefficients R_i and S_i read

$$R_{n-1} = \frac{\kappa_{n-1}}{\sigma_n} ,$$

$$R_i = \frac{\kappa_i}{\sigma_{i+1} - \lambda_{i+2}R_{i+1}} , \quad i = n-2, ..., 1 ,$$

$$S_{n-1} = \frac{q_n}{\sigma_n} ,$$
(23)

$$S_{i} = \frac{q_{i+1} + \lambda_{i+2}S_{i+1}}{\sigma_{i+1} - \lambda_{i+2}R_{i+1}} , \quad i = n - 2, ..., 1 .$$

Loss of the particles by self-coagulation can be accounted for by substituting the σ_i according to

$$\sigma_i \to \sigma_i + \sum_{j=2}^n (1 + \delta_{i,j}) k_{c_{i,j}} [A_j] , \quad i = 2, ..., n$$
 (24)

Production of the particles due to self-coagulation can be accounted for by substituting the q_i according to

$$q_{i} \to q_{i} + \sum_{j=2}^{i-2} \frac{1 + \delta_{j,i-j}}{2} k_{c_{j,i-j}} [A_{j}] [A_{i-j}] , \qquad (25)$$
$$i = 4, ..., n .$$

 $k_{c_{i,j}}$ is the rate coefficient for the coagulation of two particles A_i and A_j , which upon coagulation produce a particle A_{i+j} . The $[A_i]$ in steady state can then be obtained by iterating the solution (22) and (23), starting e.g. with $[A_i]=0$ for i=2, ..., n and updating the cluster concentrations after each iteration. The $[A_i]$ after the first iteration will be identical with the $[A_i]$ without coagulation.

7.2 Negative aerosol

A semi-analytical solution for the steady state concentrations of the particles $A_{i=0,...,n}^-$ in the aerosol scheme in Fig. 3 is given here. The particles are produced by sources at the rates q_i^- and lost in sinks with the pseudo first order rate coefficients ρ_i^- . They grow by condensation of the gas phase molecules A_1 with the pseudo first order rate coefficients $\kappa_i^$ and decay by evaporation of those molecules with the pseudo first order rate coefficients λ_i^- . Due to their mutual electrostatic repulsion it is safe to assume that the particles do not

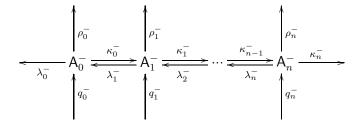


Fig. 3. Reaction scheme of a negative aerosol system.

coagulate. With the total pseudo first order rate coefficient for loss of the A_i^-

$$\sigma_i^- \doteq \kappa_i^- + \lambda_i^- + \rho_i^- \quad , \quad i = 0, ..., n$$
⁽²⁶⁾

the system of differential equations for the concentrations $[A_i^-]$ reads

$$\frac{d[A_0^-]}{dt} = q_0^- - \sigma_0^-[A_0^-] + \lambda_1^-[A_1^-] ,
\frac{d[A_i^-]}{dt} = q_i^- - \sigma_i^-[A_i^-] + \kappa_{i-1}^-[A_{i-1}^-]\lambda_{i+1}^-[A_{i+1}^-] , (27)
i = 1, ..., n - 1 ,
\frac{d[A_n^-]}{dt} = q_n^- - \sigma_n^-[A_n^-] + \kappa_{n-1}^-[A_{n-1}^-] .$$

The $[A_i^-]$ in steady state $(d[A_i^-]/dt=0)$ can be calculated from this system of equations with

$$[A_0^-] = \frac{q_0^- + \lambda_1^- S_0^-}{\sigma_0^- - \lambda_1^- R_0^-} , \qquad (28)$$
$$[A_i^-] = R_{i-1}^- [A_{i-1}^-] + S_{i-1}^- , \quad i = 1, ..., n .$$

The coefficients R_i^- and S_i^- read

$$R_{n-1}^{-} = \frac{\kappa_{n-1}^{-}}{\sigma_{n}^{-}} ,$$

$$R_{i}^{-} = \frac{\kappa_{i}^{-}}{\sigma_{i+1}^{-} - \lambda_{i+2}^{-} R_{i+1}^{-}} , \quad i = n-2, ..., 0 ,$$
(29)

$$S_{n-1}^{-} = \frac{q_n^{-}}{\sigma_n^{-}} ,$$

$$S_i^{-} = \frac{q_{i+1}^{-} + \lambda_{i+2}^{-} S_{i+1}^{-}}{\sigma_{i+1}^{-} - \lambda_{i+2}^{-} R_{i+1}^{-}} , \quad i = n-2, ..., 0 .$$

Loss of the particles by recombination with cations can be accounted for in the system of differential equations (27) by substituting the σ_i^- according to

$$\sigma_i^- \to \sigma_i^- + k_{r_i} \sum_{j=0}^n [A_j^-] \quad , \quad i = 0, ..., n \quad ,$$
 (30)

where $\sum_{j=0}^{n} [A_{j}^{-}]$ is the cation concentration in charge equilibrium, and the $k_{r_{i}}$ the rate coefficients for the recombination of the A_{i}^{-} with the cation population. The $[A_{i}^{-}]$ in steady state can then be obtained by iterating the solution (28) and (29), starting e.g. with $[A_{i}^{-}]=0 \forall i$ and updating the cluster concentrations after each iteration. The $[A_{i}^{-}]$ after the first iteration will be identical with the $[A_{i}^{-}]$ without recombination.

7.3 Coupled neutral and negative aerosol

The semi-analytical approach can be used to solve the coupled neutral/negative aerosol scheme in Fig. 1 in steady state at a fixed gas phase concentration of sulfuric acid $[A_1] = [H_2SO_4]$. The solutions for the neutral and negative aerosol schemes are not iterated independently, but alternatingly: The first iteration of the negative solution is applied to the bottom portion of the scheme, giving the concentrations of the negative clusters $[A_i^-]$. With these the production and loss rates of the neutral clusters A_i are calculated, and the first iteration of the neutral solution applied to the top part of the scheme, giving the concentrations $[A_i]$. These are then used to calculate the production and loss rates of the A_i^- , and the next iteration of the negative solution is applied to the bottom of the scheme. Iterating the procedure until a satisfactory degree of convergence is attained yields the cluster concentrations $[A_i]$ and $[A_i^-]$ in steady state. The neutral and negative cluster concentrations can then be used to calculate *J*(*n*, *p*, *q*, *r*, *s*, *t*, [H₂SO₄]) from Eqs. (4), (6), and (8).

8 Numerical aerosol model

We use a numerical aerosol model to calculate reference particle formation rates. The model integrates the system of differential equations for the concentrations of the neutral and negative aerosol particles $A_{i=2,...,n}$ and $A_{i=0,...,n}^-$ in Fig. 1 for a given set of constant parameters (pressure p, ionization rate q, temperature t, relative humidity r, preexisting aerosol H₂SO₄ condensational sink s, and gas phase sulfuric acid concentration [H₂SO₄]=[A₁]) until the time derivative of the aerosol concentrations falls below a given threshold. The aerosol concentrations and the formation rate $J(n, p, q, r, s, t, [H_2SO_4])$ are then assumed to be good approximations of their steady state values. Alternatively, the model can be run for a given period of time, e.g. 1200 s, a common time step in large scale atmospheric modeling.

9 Comparison of different particle formation rates

In this section we compare steady state particle formation rates $J(n, p, q, r, s, t, [H_2SO_4])$ calculated with different methods and using varied assumptions, given in Table 1. The comparisons are performed for particle formation rates exceeding 10^{-6} cm⁻³ s⁻¹, as smaller formation

Particle formation rate	J_1	J_2	J ₃	J_4	J_5	J ₆	J_7	J_8
Solution	numerical integration	semi- analytical	semi- analytical					
Size of particles formed	super- critical	>2.5 nm	super- critical	>2.5 nm	super- critical	>2.5 nm	super- critical	>2.5 nm
Self-coagulation	on	on	off	off	on	on	on	on
Coagulation with preexisting aerosol	on	on	on	on	on	on	on	on
H ₂ SO ₄ uptake/loss rate coefficients parameterized	no	no	no	no	yes	yes	yes	yes

Table 1. Details of the steady state particle formation rate calculations.

rates can in general be neglected in the context of atmospheric aerosol formation. The particle formation rates are sampled on a grid of parameters covering the intervals [2, 35] cm⁻³ s⁻¹ (ionization rate q), [25, 104]% (relative humidity r), [0, 0.01] s⁻¹ (preexisting aerosol H₂SO₄ condensational sink s), [190, 285] K (temperature t), and $[10^6, 2 \times 10^8]$ cm⁻³ (sulfuric acid gas phase concentration $[H_2SO_4]$), with 7 equidistant grid points on each interval. While this parameter grid covers typical tropospheric conditions, the resulting samples will produce an incomplete picture of the differences between the particle formation rates: The extent and resolution of the grid introduce a sampling uncertainty. Moreover, the deviations between the particle formation rates are not a representative measure of their performance when used in an atmospheric model, as the joint probability distribution of the parameters controlling aerosol formation needs not to be uniform in the atmosphere.

Relative humidities below 25%, sulfuric acid concentrations below 10^6 cm^{-3} , and temperatures above 285 K were excluded from the comparison: The numerical model described in Sect. 8 is unable reach the steady state criterion for unfavorable combinations of these parameters, when the particle formation rates are extremely small ($\ll 10^{-6} \text{ cm}^{-3} \text{ s}^{-1}$), possibly due to numerical errors. The pressure *p* is set to 1013.25 hPa in all calculations, as the considered particles are much smaller than the mean free path of gas phase molecules, and their processes take place in the free molecular regime, with a negligible pressure dependence.

9.1 Nucleation rate as a surrogate for the formation rate of particles of a given size

In large scale atmospheric models treating sulfate aerosol, particle formation rates are usually calculated with nucleation rate parameterizations. The smallest represented particles in these models (e.g. Lauer et al., 2005; Ma and von Salzen, 2006) may be larger (2–10 nm) than the neutral critical cluster, which contains only a few sulfuric acid molecules in conditions favorable for nucleation. The loss of supercritical particles smaller than the smallest represented particles due to coagulation among each other and with larger aerosol is then neglected, leading to an overestimation of particle formation rates. The resulting errors add to the intrinsic errors of aerosol nucleation parameterizations, which may exceed a factor of 2 (Vehkamäki et al., 2002; Modgil et al., 2005).

Figure 4a compares nucleation rates with formation rates of particles exceeding 2.5 nm in diameter, and illustrates the errors which may arise when the aerosol nucleation rate is used in lieu of the formation rate of larger particles: The nucleation rates markedly overestimate the >2.5 nm particle formation rates, in some cases by many orders of magnitude.

A modified approach of calculating the formation rates of particles exceeding a given diameter D is the scaling of the nucleation rates with the factor $(d'/D')^3$, where d' is the diameter of the smallest supercritical particle in given conditions, and D' the diameter of the smallest particle exceeding the diameter D. This is equivalent to the assumption that the particles exceeding the diameter D form solely by coagulation, which entails conservation of the total volume of the particles. In reality, growth by condensation of vapor molecules contributes significantly to the formation of larger particles, and the scaled nucleation rates will tend to underestimate the formation rates of particles exceeding a given diameter. This is illustrated in Fig. 4b, which compares nucleation rates scaled with $(d'/D')^3$ with the formation rates of particles exceeding 2.5 nm in diameter: The majority of the scaled nucleation rates underestimate the >2.5 nm particle formation rates by up to one order of magnitude, while overestimation occurs in some cases by many orders of magnitude.

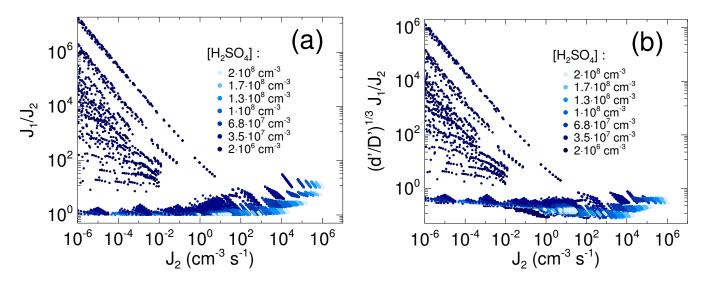


Fig. 4. (a) Comparison of the nucleation rate J_1 with the formation rate J_2 of particles exceeding 2.5 nm in diameter. (b) Comparison of the nucleation rate J_1 , scaled with the factor $(d'/D')^3$, with the formation rate J_2 of particles exceeding 2.5 nm in diameter. d' is the diameter of the smallest supercritical particle in given conditions, D' the diameter of the smallest particle exceeding 2.5 nm. The particle formation rate calculations are described in more detail in Table 1.

In both cases (Figs. 4a and b) the largest differences between the nucleation rate and the > 2.5 nm particle formation rate occur at the lowest H_2SO_4 concentrations and at the lowest temperatures (not shown). This can be explained as follows: At very low temperatures the neutral critical cluster contains very few H_2SO_4 molecules, and even comparably low H_2SO_4 concentrations can sustain non-negligible nucleation rates. However, at low H_2SO_4 concentrations, particles grow slowly, and a given nucleation rate may result in a much smaller formation rate of >2.5 nm particles, owing to loss of particles due to coagulation among each other and with preexisting aerosol.

9.2 Self-coagulation and particle formation

Kerminen and Kulmala (2002) have developed an analytical method to calculate the formation rate of particles of a given size from the formation rate of particles of a smaller size. The method accounts for coagulation with preexisting aerosol, but neglects self-coagulation. Self-coagulation is the coagulation of the forming particles among each other, as opposed to coagulation with preexisting, typically larger aerosol particles. Unlike coagulation with preexisting aerosol, selfcoagulation acts not only as a particle sink, but also contributes to the formation of new particles.

Figure 5a compares the nucleation rate calculated with and without self-coagulation of the nucleating particles. 99% of the nucleation rates calculated without self-coagulation lie within 29% of the nucleation rates calculated with self-coagulation. Figure 5b shows the errors encountered when calculating the formation rate of particles exceeding 2.5 nm in diameter without self-coagulation: Here, 31% of the parti-

cle formation rates calculated without self-coagulation deviate 99% or more from the particle formation rates calculated with self-coagulation. In both cases the largest deviations occur at the low end of the considered temperature range (≤ 206 K for the nucleation and ≤ 238 K for the > 2.5 nm particle formation rate). Hence neglecting self-coagulation is a reasonable approximation in the calculation of the steady state formation rate for small particles or at sufficiently high temperatures.

9.3 Semi-analytical versus numerical particle formation rate calculation

Here we compare the particle formation rates calculated with the semi-analytical method (described in Sect. 7) with particle formation rates calculated with the numerical aerosol model (described in Sect. 8). Both methods employ parameterized H_2SO_4 uptake and loss rate coefficients and average particle H_2O contents (Sect. 6). The rate coefficients for coagulation of the particles among each other and with preexisting aerosol are calculated as described in Sect. 4.

Figure 6a shows the relative deviations of the semianalytical nucleation rates with respect to the numerical nucleation rates. The deviations are minuscule: The maximum error amounts to 0.41%. Figure 6b shows the relative deviation of the semi-analytical formation rates of particles exceeding 2.5 nm in diameter with respect to the corresponding numerical particle formation rates. These deviations are small: The maximum error amounts to 2.0%.

The semi-analytical method is faster than the numerical model when run for a time period of 1200s instead into steady state roughly by a factor of 50 in the case of the

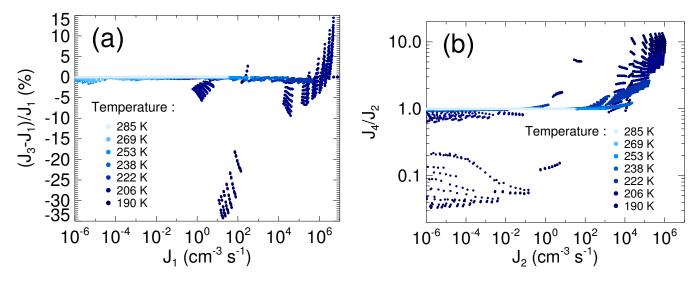


Fig. 5. (a) Comparison of the nucleation rate J_3 , calculated with self-coagulation of the nucleating particles switched off, with the nucleation rate J_1 , calculated with self-coagulation acting both as a particle sink as well as a contribution to the nucleation rate. (b) Comparison of the formation rate J_4 of particles exceeding 2.5 nm in diameter, calculated with self-coagulation switched off, with the formation rate J_2 of particles exceeding 2.5 nm in diameter, calculated with self-coagulation acting both as a particle sink as well as a contribution to the particle formation rate J_2 of particles exceeding 2.5 nm in diameter, calculated with self-coagulation acting both as a particle sink as well as a contribution to the particle formation rate calculations are described in more detail in Table 1.

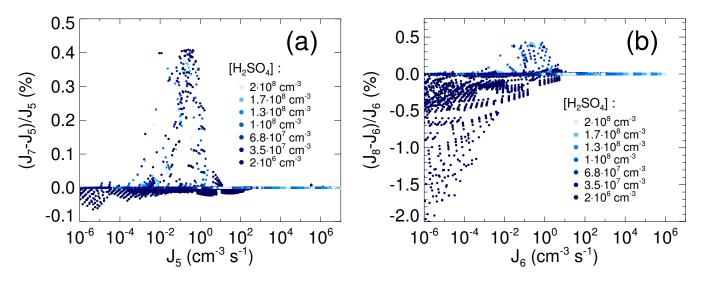


Fig. 6. (a) Comparison of the nucleation rate J_7 , calculated with our semi-analytical method, with the nucleation rate J_5 calculated with a numerical aerosol model. (b) Comparison of the formation rate J_8 of aerosol particles exceeding 2.5 nm in diameter, calculated with our semi-analytical method, with the particle formation rate J_6 of particles exceeding 2.5 nm in diameter, calculated with a numerical aerosol model. Here, both the semi-analytical method and the numerical model use parameterized rate coefficients for the uptake and loss of H_2SO_4 by the aerosol particles, as well as parameterized average particle H_2O contents. The particle formation rate calculations are described in more detail in Table 1.

>2.5 nm particle formation rates. A further acceleration can be achieved when requirements on precision are relaxed, e.g. by reducing the number of iterations in the semi-analytical method. The time for calculating the rate coefficients has been excluded from this comparison. 9.4 Semi-analytical particle formation rates using parameterized rate coefficients versus numerical particle formation rates using calculated rate coefficients

Here we compare particle formation rates calculated with the semi-analytical method of Sect. 7, using parameterized H_2SO_4 uptake and loss rate coefficients and average particle

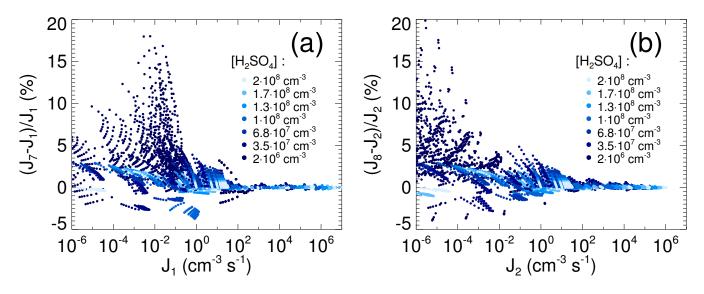


Fig. 7. (a) Comparison of the nucleation rate J_7 , calculated with our semi-analytical method, with the nucleation rate J_1 , calculated with a numerical aerosol model. (b) Comparison of the formation rate J_8 of aerosol particles exceeding 2.5 nm in diameter, calculated with our semi-analytical method, with the particle formation rate J_2 , calculated with a numerical aerosol model. The semi-analytical method uses parameterized rate coefficients for the uptake and loss of H_2SO_4 by the aerosol particles and parameterized average particle H_2O contents, while the numerical model calculates the rate coefficients and average particle H_2O contents from scratch. The particle formation rate calculations are described in more detail in Table 1.

 H_2O contents (Sect. 6), with particle formation rates calculated with the numerical aerosol model described in Sect. 8, which uses H_2SO_4 uptake and loss rate coefficients and and average particle H_2O contents calculated from scratch (Sect. 4). The rate coefficients for coagulation of the particles among each other and with preexisting aerosol are calculated as described in Sect. 4 by both methods.

Figure 7a shows the relative deviation of the semianalytical nucleation rates with respect to the numerical nucleation rates. The maximum error amounts to 18%. Larger deviations are possible (but do not appear on the used parameter grid) when errors in the parameterized rate coefficients lead to an erroneous determination of the neutral critical cluster H_2SO_4 content. Figure 7b shows the relative deviation of the semi-analytical formation rates of particles exceeding 2.5 nm in diameter with respect to the corresponding numerical particle formation rates. Here the maximum error amounts to 20%. In both cases, the deviations are mainly due to errors in the parameterization of the rate coefficients for uptake and loss of H_2SO_4 by the aerosol particles.

Figure 8 shows the cumulative error occurrence (fraction of errors exceeding a given value) of the semi-analytical particle formation rates with respect to the numerical particle formation rates. For both the semi-analytical nucleation rate and the >2.5 nm particle formation rate the cumulative error occurrence falls off quickly, signifying the rare occurrence of large deviations. The cumulative error occurrences are based on particular samples of particle formation rates, and are therefore subject to a sampling uncertainty.

The semi-analytical method using parameterized rate coefficients and average particle water contents is faster than the numerical model using rate coefficients and average particle water contents calculated from scratch when run for a time period of 1200 s by a factor of several hundred in the case of the >2.5 nm particle formation rates. A further acceleration can be achieved when requirements on precision are relaxed, e.g. by reducing the number of iterations in the semianalytical method, or the maximum order of the Chebyshev polynomial expansion used in the rate coefficient parameterization.

10 Summary, discussion, and outlook

Secondary aerosol formation can significantly increase the concentrations of aerosol particles and cloud condensation nuclei in the atmosphere, and therefore requires dependable representations in atmospheric models. However, available representations reproduce aerosol nucleation rates calculated with detailed numerical models only imprecisely. In addition, substantial errors, exceeding an order of magnitude in some cases, can arise when the steady state nucleation rate is used as a surrogate for the steady state formation rate of particles of a given size. To overcome these limitations we have developed a new, semi-analytical method to calculate secondary aerosol formation rates in steady state. The advantages of our method are:

 the use of laboratory thermodynamic parameters for the initial steps of molecular cluster formation from the gas phase,

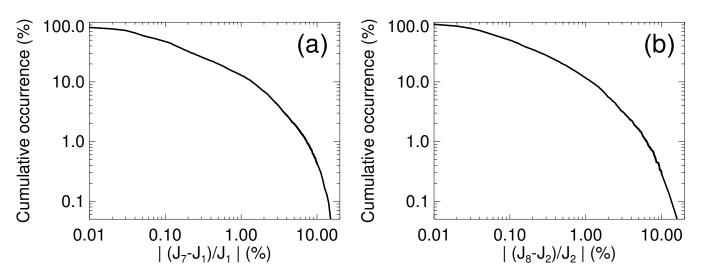


Fig. 8. Cumulative error occurrence (fraction of errors exceeding a given value) of particle formation rates calculated with our semi-analytical method, relative to the particle formation rates calculated with a numerical aerosol model: (a) nucleation rate, (b) formation rate of particles exceeding 2.5 nm in diameter. See Table 1 for details of the particle formation rate calculations.

- its detailed representation of the physical processes leading to new aerosol formation,
- its ability to calculate nucleation rates as well as the formation rates of particles of a given size,
- the good agreement of the resulting particle formation rates with those calculated by a numerical aerosol model.

Disadvantages of our method include

- its higher complexity compared to aerosol formation rate parameterizations, resulting in a higher numerical cost,
- the limited number of aerosol formation mechanisms accounted for: Potentially important mechanisms such as ternary nucleation of ammonia, sulfuric acid, and water, or nucleation involving organic molecules are not included.

How do we proceed from here with respect to representing aerosol formation from the gas phase in atmospheric modeling? Let us muse about possible developments that may advance the field:

First of all, a procedure for assessing and evaluating the various available and future aerosol formation representations needs to be devised. Simply comparing the output of the different representations is not enough: On the one hand, none of the methods can be considered a standard a priori. On the other hand, the flaws in a given representation may not matter when it is used in an atmospheric model: As an example, the joint probability distribution of the parameters controlling aerosol formation needs not to be uniform in the

atmosphere. Then errors of a representation would matter little if they were confined to conditions that occur infrequently, or that contribute little to overall aerosol production. Consequently, assessing and evaluating different implementations should be done using an atmospheric model and comparing its output to observations. In this, it should be noted that large scale models often rely on highly simplified representations of many processes and have a limited spatial resolution. Large scale models may therefore produce good results with a relatively simple but efficient representation of aerosol formation. Smaller scale models, which resolve many processes in detail and on smaller spatial scales may require more sophisticated representations of aerosol formation to produce a good agreement of model results and observations.

The question when steady state representations of aerosol formation are indeed applicable should be addressed: Vigorous nucleation events for example, such as observed in the upper troposphere in connection with tropical convection may not be well captured by steady state methods.

Computer power will continue to grow in the future, and increasingly detailed atmospheric models will become numerically affordable. This situation will require but also enable more complex and detailed representations of secondary aerosol formation. However, before aerosol formation from the gas phase can be represented with a molecular size resolution in large scale atmospheric models, the available methods may have to be further developed. Improvements could be achieved by identifying better sets of basis functions for parameterizing particle formation rates, so that more complex yet precise parameterizations could be constructed with a limited number of terms. In analogy, the method presented in this work would benefit from efficient basis functions for the parameterization of the rate coefficients it uses. It could also be accelerated by finding algorithms that reduce the number of iterations required for convergence towards steady state. Another promising approach for representing aerosol formation rates that has not been widely explored yet is the interpolation of lookup tables.

However, the most severe limitation on modeling secondary aerosol formation in the atmosphere is our lack of understanding of the processes that lead to the formation of stable molecular clusters from the gas phase. Laboratory studies investigating the structure of such clusters and measuring their thermodynamic formation parameters have therefore the greatest potential to advance the field.

11 Conclusions

Secondary aerosol formation can significantly increase concentrations of aerosol particles and cloud condensation nuclei in the atmosphere, and therefore requires dependable representations in atmospheric models. However, the available representations reproduce aerosol nucleation rates calculated with detailed numerical models only imprecisely. In addition, substantial errors, exceeding an order of magnitude in some cases, can arise when the steady state nucleation rate is used as a surrogate for the steady state formation rate of particles of a given size. To overcome these limitations, we have developed a semi-analytical method to calculate steady state formation rates of sulfate aerosol which uses parameterized rate coefficients for sulfuric acid uptake and loss by the aerosol particles. The method reproduces aerosol formation rates calculated with a numerical aerosol model better than other available methods, but is numerically more complex. The method can calculate the steady state formation rates of particles of a given size, and therefore supersedes the use of nucleation rates in lieu of formation rates of larger particles.

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