

## Addendum to

# “Validation of remotely sensed profiles of atmospheric state variables: strategies and terminology” published in Atmos. Chem. Phys., 6, 4311–4320, 2006

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In Eq. (33) of the original paper, of which the terminology is used here and to which all following equation and section numbers refer, a  $\chi^2$  test is suggested to test the significance of a bias  $\mathbf{b}$ , i.e. the mean difference of  $K$  co-incident profiles. This approach assumes a perfectly known covariance matrix  $\check{\mathbf{S}}_{\text{bias}}$ , i.e. a large size of the sample this covariance matrix is estimated from. However, it turns out that in real applications the sample size  $K$  often is too small to justify this approach. In such cases the  $T^2$  statistics (Hotelling, 1951) is the method of choice for profile validation. The quantity to be tested is

$$T^2 = \check{\mathbf{b}}_{\text{diff}}^T \check{\mathbf{S}}_{\text{bias}}^{-1} \check{\mathbf{b}}_{\text{diff}} = \chi_{\text{bias}}^2 \quad (1)$$

but the probability function applicable to this test is the Hotelling's  $T^2$  distribution instead of the  $\chi^2$  distribution. For univariate applications as discussed in Sect. 7, the Student's  $t$ -test (Gosset, 1908) is the natural choice for assessment of the significance of a scalar bias in the case of small sample sizes.

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## References

- Gosset, W. S. (pen name: Student): The probable error of a mean, in: *Biometrika* 6 (1908), pp. 1–25, reprinted on pp. 11–34 in: “Student's” *Collected Papers*, edited by: Pearson, E. S. and Wishart, J., Cambridge University Press for the Biometrika Trustees, 1942.
- Hotelling, H.: A generalized T-Test and measure of multivariate dispersion, in: *Proc. Second Berkley Symposium of Mathematical Statistics and Probability*, edited by: Newman, J., Berkeley, University of California Press, pp. 23–42, 1951.