



*Supplement of*

## **Global methane emission estimates from a dual-isotope inversion: new constraints from $\delta\text{D-CH}_4$**

**Bibhasvata Dasgupta et al.**

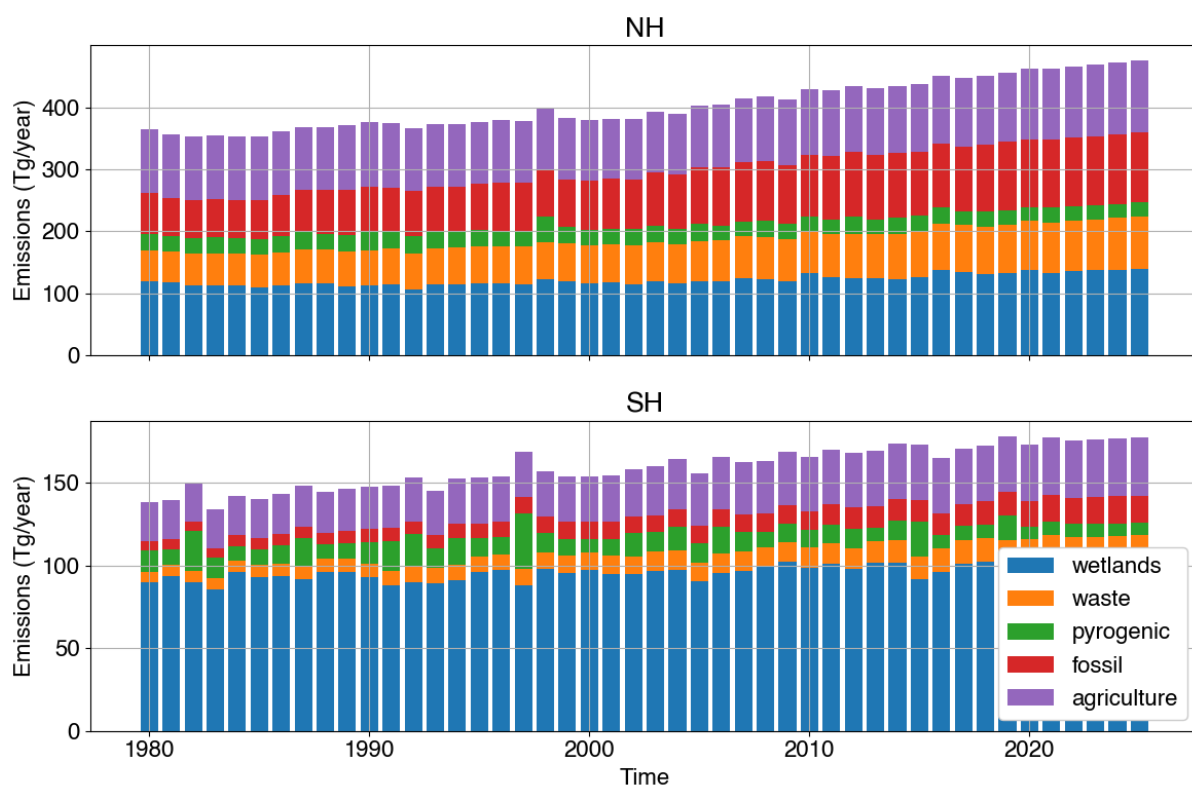
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## S1. Prior Emissions

The a priori methane (CH<sub>4</sub>) emissions for the inversion model were derived from six data inventories and grouped into five main source categories: wetlands, agriculture, pyrogenic (biomass burning), fossil fuel use, and waste management (Fig. S1; Table S1). Wetland emissions are estimated using the Lund–Potsdam–Jena – Wald, Schnee, Landschaft v2.0 (LPJ-wsl; Zhang et al., 2017) model, which incorporates precipitation variability via the Trends in Precipitation and its Predictability (TIPP) framework. This category includes emissions from swamps and freshwater systems, as well as other natural microbial sources (e.g., oceans and wild animals), which contribute on average 20% and 17% of natural emissions in the Northern and Southern Hemispheres, respectively (Sitch et al., 2003; Hodson et al., 2011). Agricultural emissions are derived from EDGAR v7.0 (Crippa et al., 2022), primarily from enteric fermentation (69% and 89% in the Northern/Southern Hemispheres, respectively) and agricultural soils, including rice cultivation. Pyrogenic emissions are informed by EDGAR, the Atmospheric Chemistry and Climate Model Intercomparison Project (ACCMIP/MACCity; Voulgarakis et al., 2013), and the Global Fire Assimilation System (GFAS) for wildfire observations. Natural fires account for 44% to 81% of pyrogenic emissions in the Northern/Southern Hemispheres, with the remainder attributed to anthropogenic burning of waste, transportation fuels, industrial processes, and energy use in buildings. Fossil fuel emissions are categorised according to EDGAR and are primarily driven by fugitive releases during extraction (96% and 85% in the Northern/Southern Hemispheres, respectively), with the remaining contributions coming from refining, power generation, and the chemical industries. Waste emissions include wastewater treatment (44%/56%), landfills (40%/36%), and manure management (16%/8%).

A Python script compiles CH<sub>4</sub> emissions from different sources into a hemispheric time-series dataset for use in a two-box atmospheric model. Emissions are grouped based on established sector definitions (e.g., EDGAR anthropogenic sectors, GFAS and ACCMIP/MACCity for biomass burning, LPJ-wsl for wetlands, and TIPP for additional natural emissions such as oceans, termites, and wild animals). Gridded emission fields are summed over all longitudes and separated into Northern and Southern Hemisphere totals (0–90°N and 0°–90°S). These are then averaged into annual values and expressed in teragrams of CH<sub>4</sub> per year (Tg yr<sup>-1</sup>). Anthropogenic emissions are taken from EDGAR v7.0. Biomass burning emissions are based on ACCMIP/MACCity for 1980–2002 and GFAS satellite-based estimates for 2003 onward. Wetland emissions are from the LPJ-wsl model, while the remaining natural microbial emissions are based on TIPP outputs. Each source type is first compiled at the subsector level and then aggregated into the five major categories. These category totals are finally summed to produce overall methane emissions for each hemisphere. The resulting dataset is also used to produce stacked bar figures comparing source contributions over time (Fig. S1).



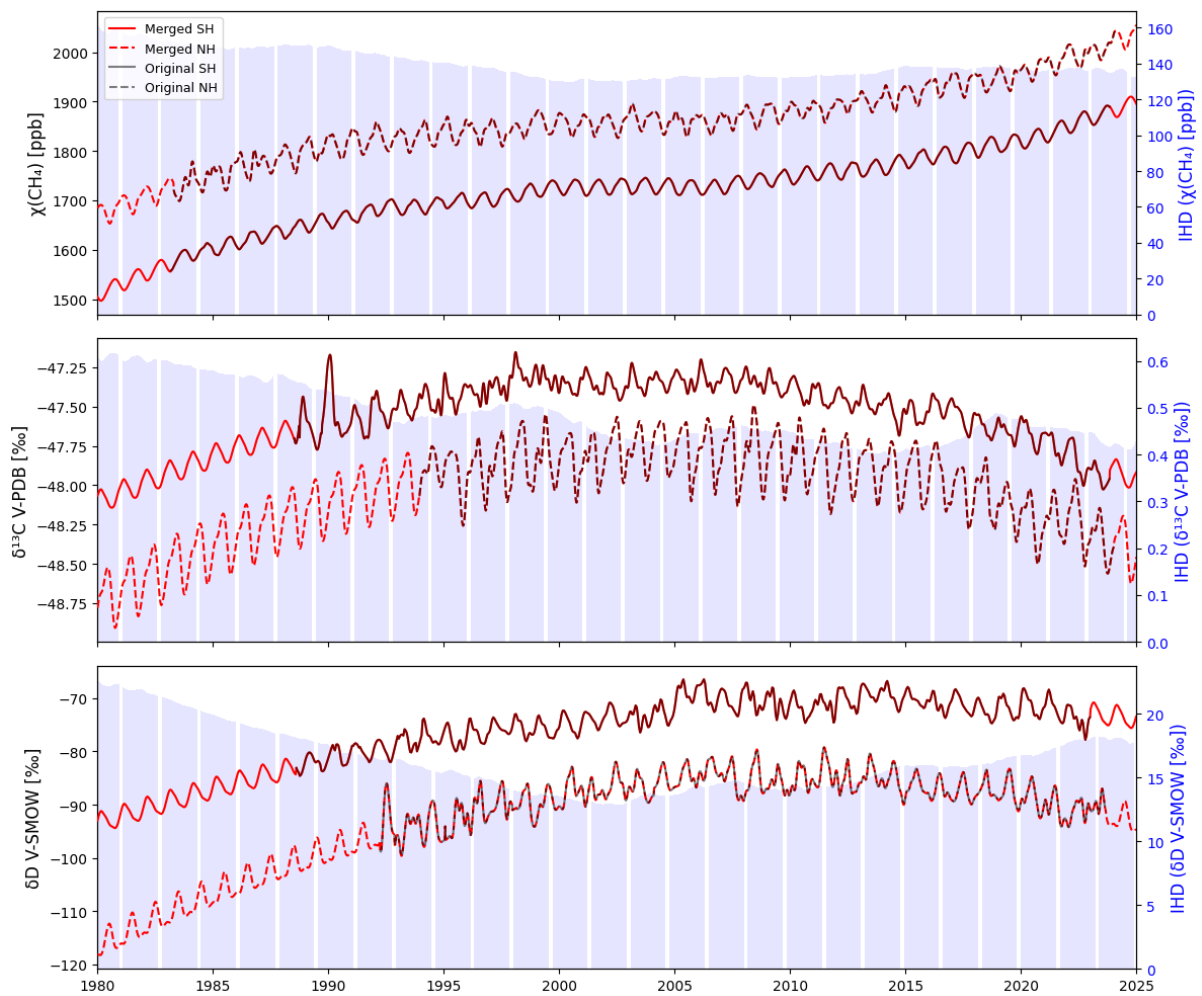
**Figure S1:** Yearly a priori CH<sub>4</sub> emission estimates for Agriculture, Pyrogenic, Fossil, Waste and Wetlands, compiled from different inventories (see text), integrated by hemisphere.

**Table S1:** a priori emissions sources for the CH<sub>4</sub> inversion model. All categories verified from European Commission, Joint Research Centre (EC-JRC)/Netherlands Environmental Assessment Agency (PBL), 2021

Source Category	Data Inventory/Model	Details
Natural Wetlands	LPJ-wsl (Lund–Potsdam–Jena – Wald, Schnee, Landschaft v2.0)	Predicts emissions using precipitation trends via the TIPP (Trends in Precipitation and its Predictability) framework.
Agriculture	EDGAR v7.0 (Emissions Database for Global Atmospheric Research)	Includes subcategories like Agricultural Soils and Enteric Fermentation.
Pyrogenic (Biomass Burning)	EDGAR, ACCMIP/MACCity, GFAS	- EDGAR: Agricultural, Waste, Pyrogenic, Fossil Fuel use
		- ACCMIP/MACCity: Historical biomass burning
		- GFAS: Daily wildfire emissions via satellite data (since 2003)
Fossil Fuel Use	EDGAR	Includes Fuel exploration, Oil refineries, Chemical processes, and Power industry.
Waste Management	EDGAR	Covers emissions from mining, landfills, and wastewater treatment.

## S2. Harmonised long-term atmospheric timeseries

The CH<sub>4</sub> mole fraction and isotope composition data were compiled from eight laboratories, using atmospheric measurements from high northern and southern latitudes following Dasgupta et al. (2025b). These regions were chosen because their well-mixed air masses allow for effective interlaboratory comparison of co-located samples. The dataset is harmonised with respect to the MPI-BGC scale and merged into two sets of three hemispheric time series for  $\chi(\text{CH}_4)$ ,  $\delta^{13}\text{C-CH}_4$ , and  $\delta\text{D-CH}_4$ , which overlap between 1994 and 2022. This original dataset is shown in Fig. S2. To extend our original time series back to 1980 and forward to 2025, we used extrapolated data from longer measurement periods, constrained with 2 criteria (1) Firn core  $\chi(\text{CH}_4)$ ,  $\delta^{13}\text{C-CH}_4$ , and  $\delta\text{D-CH}_4$  data from Antarctica and Greenland converted to atmospheric values, as reported in Sapart et al. (2013); and (2) a relatively constant interhemispheric difference for each tracer, consistent with that of the original data. The NOAA Curve Fitting Methods and Seasonal Decomposition model (Thoning et al., 1989), widely utilised in previous studies (Miller and Tans, 2003; Ballantyne et al., 2010; Dowd et al., 2023; Woolley Maisch et al., 2023), was applied for this extrapolation. This fit function captures the annual oscillation, depicted by harmonic cycles, and the long-term growth, represented by a polynomial function, using general linear least-squares regression (Press et al., 1988). The harmonic and polynomial functions thus obtained were applied to the extrapolated time series. While the analysis period covered co-overlapping original data from 1994 to 2022, the extended periods (1980-1993 and 2023-2025) were used for the model's spin-up and spin-down periods.



**Figure S2:** Merged time series of harmonised data in black, with extrapolation periods in red for each tracer and hemisphere. For additional information about offset correction, data merging and uncertainties, please refer to

Dasgupta et al. (2025a).

### S3. Analysis and Spin-up / Spin-down Periods

In atmospheric inversion models, observational constraints critically influence the posterior emission estimates, requiring careful treatment of spin-up and spin-down phases. The spin-up period ensures that inversion results are independent of initial conditions. During this phase, the model is initialised with constant emissions and observation errors, following the approach of Thanwerdas et al. (2022), who used a 30-year spin-up with meteorological data from 2012. As the initial condition effects on isotopic composition diminish, the posterior fluxes become more consistent with the prior values. In the spin-down phase, the measurement constraints reduce, causing the posterior emissions to converge toward the priors. The equilibration timescales for  $\delta^{13}\text{C-CH}_4$  and  $\delta\text{D-CH}_4$  are longer than those for  $\chi(\text{CH}_4)$  (Tans, 1997), making isotopic signatures particularly sensitive to initial conditions and observational fluctuations. Houweling et al. (2017) pointed out that if the initial burdens of  $\chi(\text{CH}_4)$ ,  $\delta^{13}\text{C-CH}_4$ , and  $\delta\text{D-CH}_4$  are well known, the inversion can recover in a relatively short spin-up period. Thanwerdas et al. (2022) further showed that isotope signatures diverge from their priors during spin-up, stabilising only after 2–3 years. We take both arguments into account by using a long spin-up but also optimising the initial conditions by constraining our extrapolated time series to firm core measurements, ensuring that results accurately represent posterior fluxes rather than artefacts of initial biases, if any.

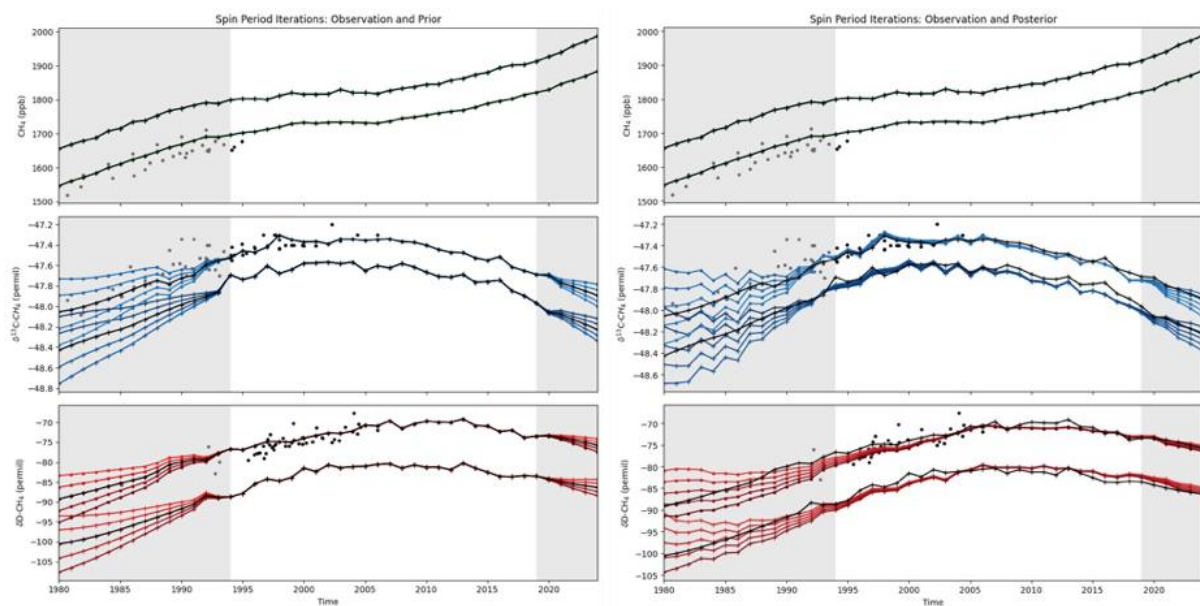
To test the model's sensitivity to the spin-up and spin-down periods, the extrapolated dataset (Fig. S3) was systematically perturbed during these periods. Perturbations were introduced by incrementally offsetting values backwards from 1994 (end of spin-up) and forward from 2023 (start of spin-down) by  $\pm 0.01\text{‰}$  per year and  $\pm 0.02\text{‰}$  per year for  $\delta^{13}\text{C-CH}_4$ , and by  $\pm 0.2\text{‰}$  per year and  $\pm 0.4\text{‰}$  per year for  $\delta\text{D-CH}_4$ . These offsets correspond to 10% and 20% of the observation error ( $0.1\text{‰}$  for  $\delta^{13}\text{C-CH}_4$  and  $2\text{‰}$  for  $\delta\text{D-CH}_4$ ). The inverted tracer results for the respective prior iterations during the spin periods are shown in the right panel of Fig. S3. The spin period iterations weren't tested on  $\chi(\text{CH}_4)$ , because the measurements are better constrained and the equilibration period is negligible compared to the isotopologues.

#### S3.1 Spin-up and Spin-down results

Figure S3 shows the prior and observational tracers alongside their posterior model results, based on five different starting and ending points for the tracers, as designed during the spin-up and spin-down periods. Excluding the spin-up (first 13 years) and spin-down (last 3 years) periods from the original time series is essential to ensure the reliability and robustness of the model's results. Sensitivity tests were performed by varying tracer observational values during these periods, offset by 10% and 20% of the observed baseline, on either side, to

assess the stability of the analysis period (1994–2022) and eliminate potential biases from initial and final conditions (Fig. S3). Posterior model estimates of emissions and their corresponding atmospheric tracers (coloured lines) showed variability during the spin-up but stabilised within the first year of the analysis period, confirming that the results within the main analysis period are independent of initial condition artefacts. Towards the end of the analysis period, the spin-down phase demonstrated a gradual divergence from prior values over time, as expected.

The equilibration times for  $\text{CH}_4$ ,  $\delta^{13}\text{C}\text{-CH}_4$ , and  $\delta\text{D}\text{-CH}_4$  differ, with  $\delta\text{D}\text{-CH}_4$  requiring the longest equilibration period, reflecting its sensitivity to isotopic changes. Nevertheless, the allotted spin-up and spin-down durations were sufficient for all three tracers to equilibrate, ultimately converging to a common posterior trajectory from five diverse starting and ending points. This underscores the sufficiency of the spin-up/spin-down periods in providing consistent and reliable results. It ensures that the conclusions drawn from the main analysis period are robust, reflecting the true dynamics of the  $\text{CH}_4$  cycle rather than artefacts of observational errors, prior emissions, or initial and final artefacts in the timeseries.



**Figure S3:** Impact of initial and final conditions during the spin-up and spin-down periods (shaded background) on the main analysis period (unshaded) for inverted tracers:  $\chi(\text{CH}_4)$ ,  $\delta^{13}\text{C}\text{-CH}_4$ , and  $\delta\text{D}\text{-CH}_4$ . The left panel shows the prior scenarios (original-extrapolated in black and perturbed in various colours) used to test different spin-up and spin-down periods. The right panel displays the posterior results (from the original prior and five perturbed scenarios, in black and various colours) for the three tracers. The prior-perturbed scenarios start and end at different values for each hemisphere during the spin-up and spin-down periods. The posterior

results from perturbed scenarios converge or diverge toward the central posterior values during the main analysis period, demonstrating the model's robustness to diverse spin scenarios and the stability of results within the analysis timeframe. Black circles represent the observed tracer values measured at SH firm air (Sapart et al., 2013). The spin-up and spin-down periods are shaded, and the analysis period is unshaded.

## S4. Source Isotopic Signatures

The isotopic signatures of  $\delta^{13}\text{C}$  and  $\delta\text{D}$  in  $\text{CH}_4$  are specific to the type of emissions and latitude. The values assigned for each emission category are obtained from recent publications (Table S2). Most values are averages from the global isotope database (Sherwood et al., 2017; Menoud et al., 2022) and weighted by emission rates used as prior information in the model. For fossil fuels and biomass burning,  $\delta^{13}\text{C}$  values are from Schwietzke et al. (2016), while the  $\delta^{13}\text{C}\text{-CH}_4$  value for enteric fermentation is from Chang et al. (2019). The isotopic signature of  $\text{CH}_4$  from wetlands and freshwater is known to be latitude-dependent (Brownlow et al., 2017; Ganesan et al., 2018; Douglas et al., 2021), and we use averaged hemispheric  $\delta^{13}\text{C}\text{-CH}_4$  and  $\delta\text{D}\text{-CH}_4$  values computed from a global model by Stell et al. (2021), based on up-to-date observations from sites at various latitudes. Further details on the calculations for each category are provided in Table S2.

Table S2: Assigned  $\delta^{13}\text{C}$  and  $\delta\text{D}$  Values for  $\text{CH}_4$  Sources

Source Category	Region	Sub-category	$\delta^{13}\text{C}$ (‰)	$\delta\text{D}$ (‰)	Weight (from emission rates a-priori)
Fossil Fuels	NH	Oil & natural gas exploitation		-182.9	0.69
		Coal exploitation		-209.8	0.31
		Total	-44 <sup>1</sup>	-191.2	1
	SH	Oil & natural gas exploitation		-182.9	0.66
		Coal exploitation		-209.8	0.34
		Total	-44 <sup>1</sup>	-192	1
Agriculture	NH	Ruminants	-64.93 <sup>2</sup>	-310.4	0.69
		Rice paddies	-59.9	-323.3	0.31
		Total	-63.4	-314.4	1
	SH	Ruminants	-64.93 <sup>2</sup>	-310.4	0.89
		Rice paddies	-59.9	-323.3	0.11
		Total	-64.4	-311.8	1
Wetlands	NH	Wetlands	-64.9 <sup>3</sup>	-338 <sup>3</sup>	0.8
		Termites	-65.2	-343	0.11
		Oceans	NS	NS	0.09
		Total	-64.9	-338.6	1
	SH	Wetlands	-57.4 <sup>3</sup>	-297 <sup>3</sup>	0.83
		Termites	-65.2	-343	0.11
		Oceans	NS	NS	0.06
		Total	-58.3	-302.4	1
		NH/SH	Total	-54.5	-292.2
Waste Pyrogenic	NH	Biomass burning	-22.2 <sup>1</sup>	-225.6	0.53
		Fossil fuel burning	-22.7	-136	0.48
		Total	-22.4	-183	1.01
	SH	Biomass burning	-22.2 <sup>1</sup>	-225.6	0.86
		Fossil fuel burning	-22.7	-136	0.14
		Total	-22.3	-213.1	1
Footnotes:					

<sup>1</sup>Schwietzke et al., 2016 – Nature

<sup>2</sup>Chang et al., 2019 – Nature Communications

<sup>3</sup>Stell et al., 2021 – Phil. Trans. R. Soc. A

NS = No Significant Values

## S5. Intra and Inter-Hemispheric Gradients

Atmospheric CH<sub>4</sub> mixing ratios and isotopic compositions are known to vary with latitude (Brownlow et al., 2017; Ganesan et al., 2018; Douglas et al., 2021). As a result, time series reconstructed from high-latitude sites do not represent hemispheric averages. Latitudinal gradients must be accounted for to obtain representative time series for each hemispheric average. We calculated the difference between the hemispheric average and high-latitude values using data from NOAA measurement stations at various latitudes (White et al., 2018). Figure S4 shows the data used to calculate the gradient. Each hemisphere was divided into two latitudinal zones, from 0 to 30° and 30 to 90°, and a high-latitude zone, from 60 to 90°. The average of the two latitudinal zones represents the hemispheric average, from which we calculated differences relative to the high-latitude zone stations and applied the resulting offsets to the time series as a constant offset. The time series from high latitudes is adjusted for these offsets, with corrections of +0.107‰ for the NH and -0.015‰ for the SH in  $\delta^{13}\text{C}$ , and +4.32‰ and -2.08‰ for  $\delta\text{D}$  in the NH and SH, respectively.

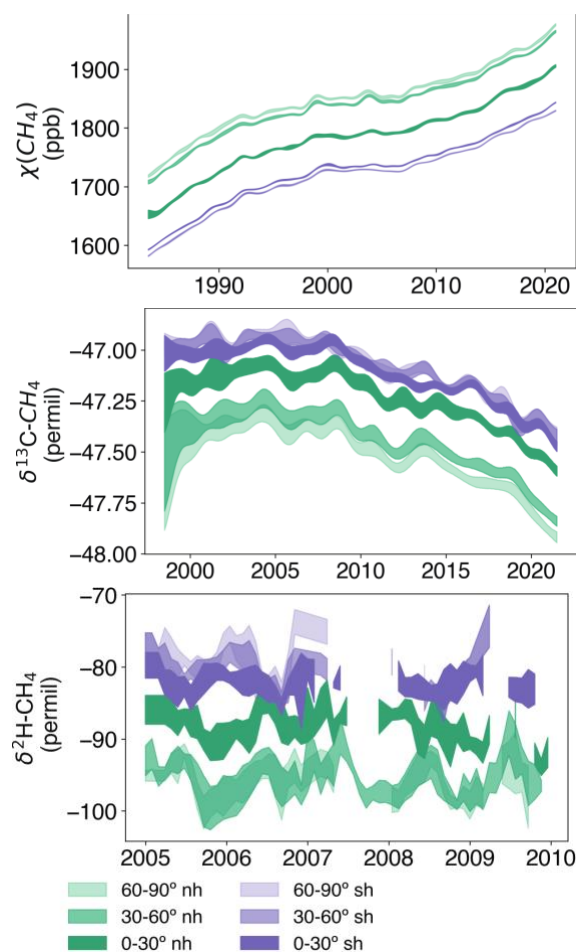


Figure S4: Latitude dependence of  $\chi(\text{CH}_4)$ ,  $\delta^{13}\text{C}$ , and  $\delta^2\text{H}-\text{CH}_4$  based on observations from the NOAA Global Greenhouse Gas Reference Network (White et al., 2018). 'nh'=northern hemisphere; 'sh'=southern hemisphere.

The inter-hemispheric transport of CH<sub>4</sub> plays a crucial role in determining its global distribution. A key factor in this process is the inter-hemispheric CH<sub>4</sub> concentration gradient. The tau term (parametrised in the two-box model as ‘ $\tau$ ’) represents the interhemispheric exchange time, i.e., how quickly methane mixes between the NH and SH. It directly affects the transport of CH<sub>4</sub> and its isotopologues between hemispheres, influencing the posterior concentration gradients and isotopic signatures. The exchange time between the hemispheres is set to  $\tau = 0.75$  yr, which is shorter than the commonly assumed value of 1 year, but has been found to produce realistic fields of the transport tracer for our two-box model setup. The shorter exchange time in our two-box framework likely compensates for structural simplifications in the model, including the lack of vertical stratification and explicit stratospheric representation, which affect interhemispheric transport dynamics differently than in three-dimensional models (see Fig. S5 for sensitivity analysis). The model updates CH<sub>4</sub> concentrations in each hemisphere at each time step using this  $\tau$ -controlled exchange rate. A lower  $\tau$  value means faster interhemispheric mixing, so methane differences between the NH and SH are reduced more quickly by atmospheric transport. As a result, the model cannot sustain large concentration gradients between hemispheres. To fit the observed hemispheric differences in CH<sub>4</sub>, the inversion compensates by making the emissions in the NH and SH more different (further apart) in the posterior. This larger emission contrast is necessary to maintain the observed gradient when mixing is rapid, as any difference in emissions is quickly evened out by the fast exchange. In contrast, with a higher  $\tau$  (slower mixing), the model can maintain a given concentration difference with a smaller emission contrast, since the hemispheres remain more isolated. To assess the model's sensitivity to this parameter, we perform a sensitivity test by varying ‘ $\tau$ ’ in steps (e.g., from 0.65 to 0.95 years; Fig. S5), running the full inversion for each value, and comparing the resulting posterior emissions and sinks. The choice of  $\tau = 0.75$  years appears ideal because it yields posterior estimates of emission and sinks that are physically reasonable and consistent with prior knowledge, without requiring extreme hemispheric contrasts. At this value, the model achieves a balance: it is fast enough to realistically mix atmospheric CH<sub>4</sub> between hemispheres, but not so fast as to force the inversion to create unrealistic emission differences. This value is also supported by literature (Naus et al., 2019) and atmospheric tracer studies (SF<sub>6</sub>), making it a robust and justifiable choice for the two-box model.

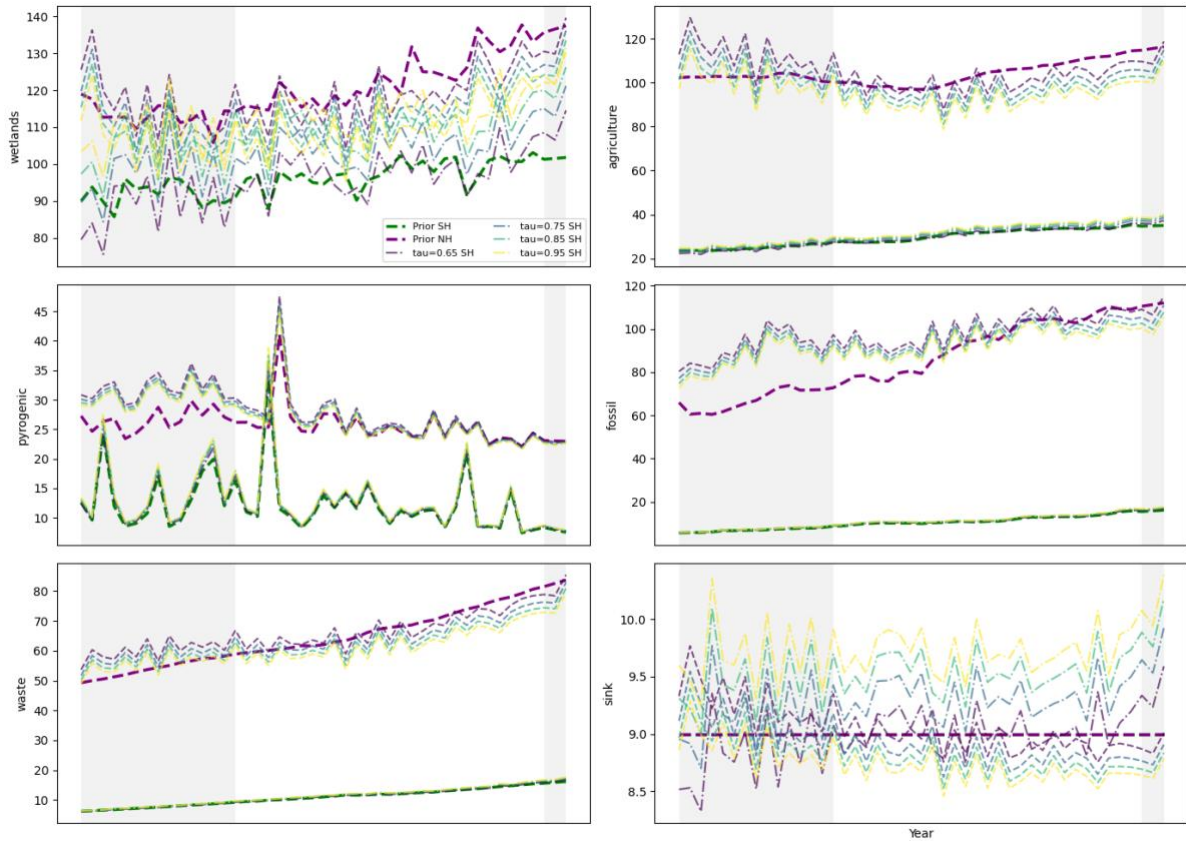


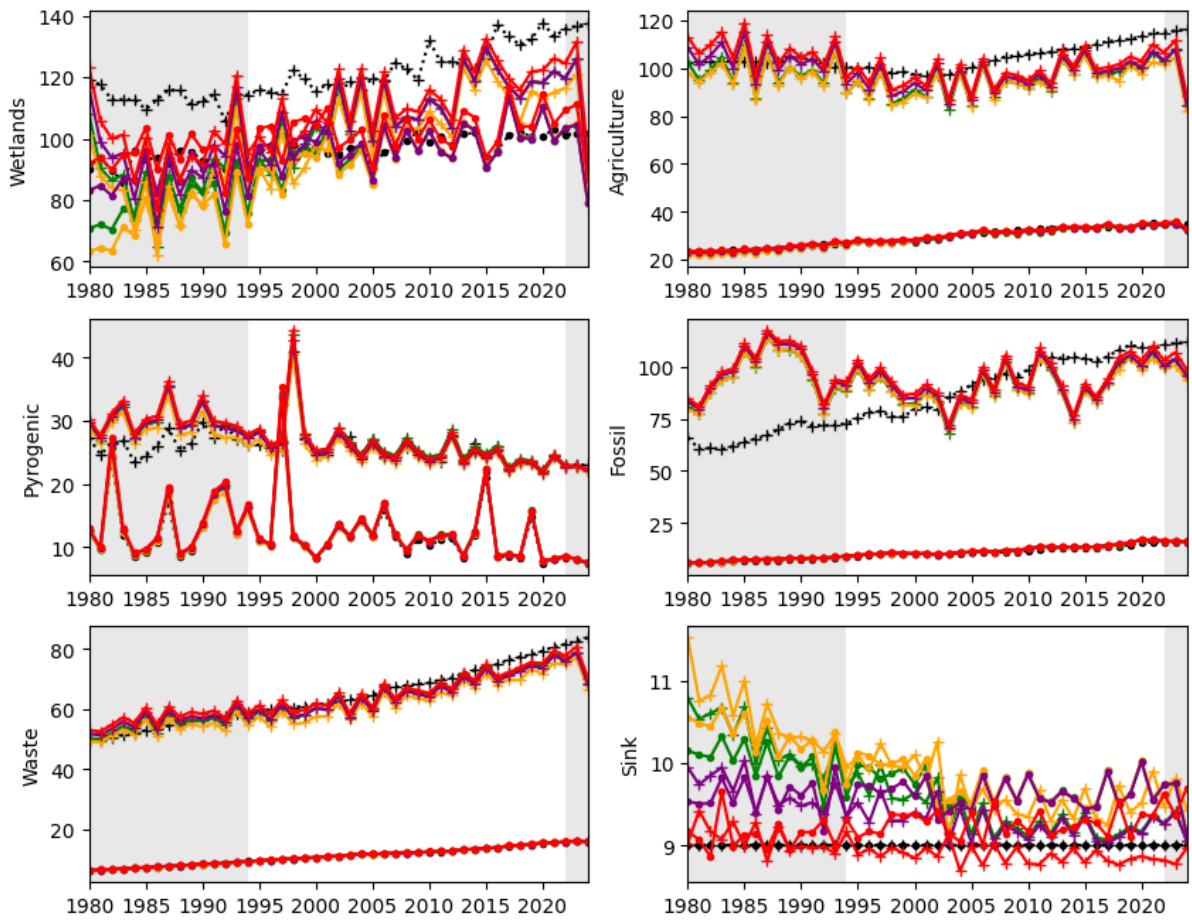
Figure: S5: Sensitivity tests with varying ‘ $\tau$ ’ values to optimise the interhemispheric exchange time of CH<sub>4</sub>, with NH lines dashed and SH lines dash-dotted. The spin-up and spin-down periods are shaded, and the analysis period is unshaded.

## S6. Lifetime

CH<sub>4</sub> is primarily removed from the atmosphere through reactions with OH, Cl, (O<sup>1</sup>D), and soil microbes, with an average atmospheric lifetime of approximately 9 years; however, its exact value remains unknown and is subject to uncertainties. This is determined as the sum of the reciprocals of the three major sinks—troposphere, stratosphere, and soil—corresponding to lifetimes of 9.97, 181, and 188 years (Stevenson et al., 2020), with relative removal contributions of ~90:5:5, respectively. Variability in simulated OH distributions among global atmospheric chemistry models arises from differences in chemical mechanisms and meteorological conditions, which are influenced by large-scale teleconnections such as the El Niño-Southern Oscillation (ENSO). In the model, the total CH<sub>4</sub> lifetime is fixed at  $9.0 \pm 0.9$  years, with individual sink lifetimes optimised based on their inverted removal percentages. These values align with those reported by Prather et al. (2012) ( $9.1 \pm 0.9$  years, mean  $\pm 1$  standard deviation), as used by the Intergovernmental Panel on Climate Change (IPCC; Myhre et al., 2013). Lifetimes may have decreased since the increase in OH (Anderson et al., 2021).

In the two-box model, the handling of CH<sub>4</sub> lifetimes has a significant influence on inversion results and model complexity. Initially, we applied a constant prior lifetime of 9 years, which resulted in scenarios where the posterior lifetimes were adjusted to account for variability in both sinks and sources. Alternatively, the model can be initialised with a dynamic prior lifetime, such as the CAMS TM5 inverted lifetime. This method adds complexity by allowing the prior lifetime to vary over time, reflecting changes in atmospheric conditions and chemical processes. The TM5 model calculates methane's lifetime by simulating its chemical loss through reactions with hydroxyl radicals (OH), O(<sup>1</sup>D), and chlorine (Cl), using monthly time series of concentration fields and fitting an exponential decay function to observed surface concentrations (Innes et al., 2019). To further explore the impact of varying prior lifetimes, perturbations were applied to the original CAMS TM5 dataset in incremental steps. These adjustments increased the lifetime values by 1%, 3%, and 5% relative to the original dataset. Starting with baseline lifetimes of 9.5, 10.5, and 11.5 years in 1980, the perturbed lifetimes reflect year-to-year changes in atmospheric conditions, progressively increasing the deviation from the reference case.

Figure S6 shows the two-box inverted results for different lifetimes input. For priors, the constant value is 9 years, while the variable lifetimes are versions of the TM5 CAMS inverted lifetime values. For posteriors, as depicted in the lower-right panel of Fig. S6, there is a general trend of lowering lifetime from all scenarios. In both cases, regardless of whether the prior lifetime is constant or variable, the inverted lifetime drops to under 10 years before the analysis period and eventually converges to  $9.25 \pm 0.2$  years. The effect of variable prior lifetimes, based on a combined sink of the troposphere, stratosphere, and soil, does not yield significantly different posterior results for both tracers and emissions compared to the constant prior lifetime.



**Figure S6:** Prior (black) and posterior (coloured) emissions and sink lifetime values, with NH in '+' markers and SH in 'o' markers, modelled by the two-box inversion from both constant (DPT Optimised) and variable (TM5 perturbed) prior lifetimes and a consolidated sink on the analysis period (not shaded).

## S7. Two-Box Bayesian Inversion: uncertainty and limitations

The two-box model simplifies atmospheric CH<sub>4</sub> dynamics by dividing the atmosphere into the NH and SH boxes, assuming slow mixing between them and well-mixed CH<sub>4</sub> concentrations in each box. CH<sub>4</sub> concentrations in each box are governed by the balance of sources and sinks, with an estimated residence time of about 9 years. In each box, the CH<sub>4</sub> mole fraction,  $\delta^{13}\text{C-CH}_4$ , and  $\delta\text{D-CH}_4$  isotopic signatures result from the combined effects of emission sources, chemistry, and transport processes. Briefly, the two-box model uses prior estimates and sink kinetic isotope effects in a forward model to generate fluxes, compares these with observations, and iteratively adjusts the state vector through a cost function to achieve the best agreement between the model output and the observed data.

The following differential equation describes the inversion model

$$dX_{i,h}(t)/dt = E_{i,h}(t) - \sum_k [L_{k,h} / KIE_{i,k}] \cdot X_{i,h}(t) + [X_{i,opp}(t) - X_{i,h}(t)] / \tau_e$$

where:

- $E_{i,h}(t)$  = emissions of tracer  $i$  in hemisphere  $h$  ( $\text{Tg yr}^{-1}$ ),
- $L_{k,h}$  = sink reaction rate for process  $k$  (troposphere, stratosphere, soil) in  $h$ ,
- $KIE_{i,k}$  = kinetic isotope effect for tracer  $i$  and sink  $k$  ( $\pm 10\%$  uncertainty),
- $X_{i,opp}$  is the mole fraction in the opposite hemisphere,
- $\tau_e \approx 0.75$  yr is the inter-hemispheric exchange time.

The inversion minimises the following cost function

$$J(x) = (x - x_{prior})^T \cdot S_a^{-1} \cdot (x - x_{prior}) + (y - F(x))^T \cdot S_y^{-1} \cdot (y - F(x))$$

where:

- $x$  = vector of sectoral CH<sub>4</sub> and isotopologue mole fraction fluxes;  $x_{prior}$  = prior flux estimate ( $\pm 30\%$ ),
- $S_a$  = prior flux error covariance;  $S_y$  = data error covariance
- $y$  = observed CH<sub>4</sub> mole fractions;  $F(x)$  = forward-modelled mole fractions

### Step 1: CH<sub>4</sub>-only linear update

We prescribe a prior flux vector  $x_a$  (sectoral emissions, with an aggregate sink/lifetime parameterisation

as appropriate) with covariance  $S_a$  representing  $\pm 30\%$  uncertainty in the inventory. Observation errors for hemispheric  $\text{CH}_4$  mole fractions are represented by a diagonal covariance  $S_y = \text{diag}(\sigma_{\text{CH}_4}^2)$  with  $\sigma_{\text{CH}_4} = 1$  ppb; these  $\sigma$  values encode total model–data mismatch (not instrument precision alone). The two-box forward model maps  $x$  to observations  $F(x)$ ; its Jacobian  $K = \partial F / \partial x$  is computed analytically from the model. Under linear–Gaussian assumptions, the posterior mean and covariance are:  $x_{\text{post}} = x_a + S_{\text{post}} K^T S_y^{-1} [y - F(x_a)]$ ,  $S_{\text{post}} = (K^T S_y^{-1} K + S_a^{-1})^{-1}$ . This step yields a self-consistent  $\text{CH}_4$  mass balance that (i) initialises the subsequent isotopologue analysis and (ii) provides the reference needed to express isotopologue measurements in per-mil units.

### Step 2: Joint isotopologue Gauss–Newton update.

We take  $S_{\text{post}}$  from Step 1 as the new prior covariance for emissions and assimilate  $\delta^{13}\text{C}\text{-CH}_4$  ( $\sigma_{\delta^{13}\text{C}} = 0.01$  ppb), and  $\delta\text{D}\text{-CH}_4$  ( $\sigma_{\delta\text{D}} = 0.001$  ppb) observations. Observation errors are specified as  $1\text{-}\sigma$  uncertainties in the absolute isotopologue concentrations. These uncertainties enter the block in a block-diagonal  $S_y$ , alongside uncertainties in sink KIEs ( $\pm 10\%$ ). At iteration  $k$ , with state  $x_k$ , Jacobian  $K_k$ , and model output  $F(x_k)$ , we minimise the quadratic cost function via the Gauss–Newton step:

$$x_{k+1} = x_a + (K_k^T S_y^{-1} K_k + S_a^{-1})^{-1} K_k^T S_y^{-1} [y - F(x_k) + K_k(x_k - x_a)]$$

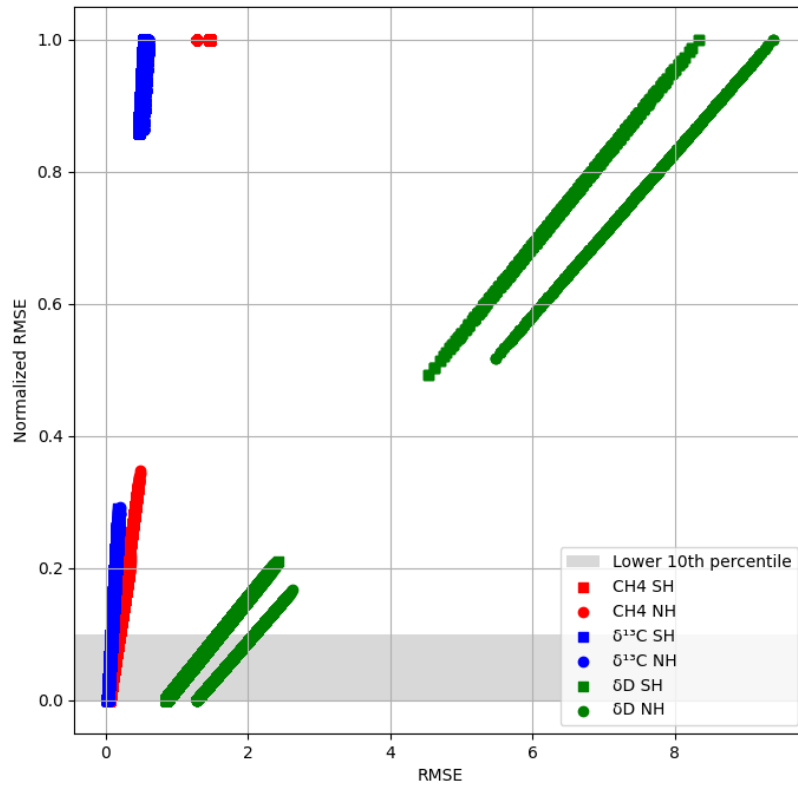
This joint update refines both emission rates and tracer-specific parameters (including adjustable KIEs), yielding an updated posterior covariance that is invariably tighter than the original  $S_a$  and reflects the incremental information gained from the isotopologue data. Throughout,  $\sigma$  denotes combined model–data mismatch (not measurement precision alone), and the state vector  $x$  includes all emission sectors, as well as the adjustable KIE parameters in Step 2, so that each source of uncertainty is treated distinctly and transparently.

## S8. Sensitivity Testing and Optimisation of the Two-Box Model

To systematically explore the parameter space of prior choices, we employ a Discrete Parameter Tuning technique that iteratively tests different combinations of prior parameter values (Table S2), based on previously reported literature values. This involves varying the source  $\delta^{13}\text{C-CH}_4$  and  $\delta\text{D-CH}_4$  values of the five emission categories by  $\pm 0.2\%$  and  $\pm 4\%$ , respectively, around the literature values. Additionally, the sink  $^{13}\text{C}$  and D KIEs are varied by  $\pm 0.0002$  and  $\pm 0.002$ , respectively, along with the error percentages associated with the priors (only Tropospheric KIEs are varied in the tests, as the other 2 sinks remove very small amounts of  $\text{CH}_4$ ). The model adjusts emissions based on these combinations to generate posterior outputs that best fit the observed tracer distributions. The six posterior tracers ( $\chi(\text{CH}_4)_{(\text{NH}, \text{SH})}$ ,  $\delta^{13}\text{C-CH}_4_{(\text{NH}, \text{SH})}$ , and  $\delta\text{D-CH}_4_{(\text{NH}, \text{SH})}$ ) are then compared to their respective observational counterparts, and the root-mean-square error (RMSE) is calculated. By systematically testing all possible combinations of input parameter values described in Table S2, approximately 13.1 million simulations are generated, each associated with six RMSE values for the six outputs. To ensure equal weighing across tracers and hemispheres, the RMSE for each tracer and hemisphere is normalised to a range of 0-1. The mean normalised RMSE (unitless fractional numeral) is then computed for each simulation. Only simulations with a mean normalised RMSE below 0.1 are retained, representing combinations of prior parameter values that produce the best fit to the observational data. These optimised parameter ranges, identified through the lowest RMSE, enable a more accurate closure of the  $\text{CH}_4$  budget within the simplified two-box model framework (Fig. S8). The results and discussion in the following sections are limited to this optimised range of input parameters.

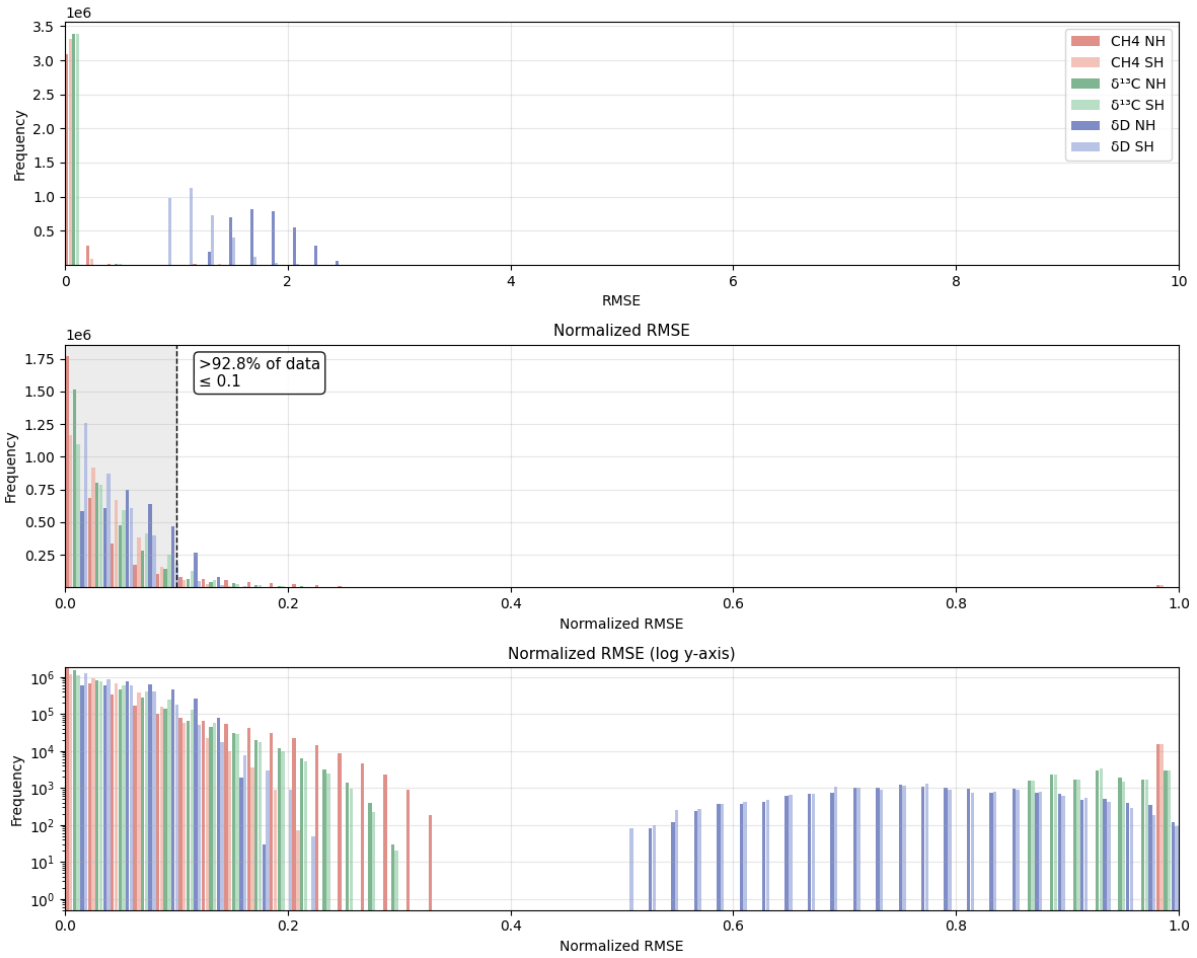
**Table S3:** Summary of all Parameters and Their Ranges Used in Our Simulations. For source signatures and KIEs the range is twice the measurement errors on either side of the values from Table S2. For errors its approximately 25% or less on either side of the baseline values.

Parameter	Mean [min., max.]	Definition
Wetland NH	$\delta^{13}\text{C-CH}_4$ : -64.9 [-65.1, -64.7]	$\delta^{13}\text{C-CH}_4$ for wetland sources in NH (‰)
	$\delta\text{D-CH}_4$ : -339 [-343, -335]	$\delta\text{D-CH}_4$ for wetland sources in NH (‰)
Wetland SH	$\delta^{13}\text{C-CH}_4$ : -58.3 [-58.5, -58.1]	$\delta^{13}\text{C-CH}_4$ for wetland sources in SH (‰)
	$\delta\text{D-CH}_4$ : -302 [-306, -298]	$\delta\text{D-CH}_4$ for wetland sources in SH (‰)
Agriculture	$\delta^{13}\text{C-CH}_4$ : -64.4 [-64.6, -64.2]	$\delta^{13}\text{C-CH}_4$ for agricultural sources (‰)
	$\delta\text{D-CH}_4$ : -311 [-315, -307]	$\delta\text{D-CH}_4$ for agricultural sources (‰)
Pyrogenic	$\delta^{13}\text{C-CH}_4$ : -22.3 [-22.5, -22.1]	$\delta^{13}\text{C-CH}_4$ for pyrogenic sources (‰)
	$\delta\text{D-CH}_4$ : -213 [-217, -209]	$\delta\text{D-CH}_4$ for pyrogenic sources (‰)
Fossil fuels	$\delta^{13}\text{C-CH}_4$ : -44 [-44.2, -43.8]	$\delta^{13}\text{C-CH}_4$ for fossil fuel sources (‰)
	$\delta\text{D-CH}_4$ : -192 [-196, -188]	$\delta\text{D-CH}_4$ for fossil fuel sources (‰)
Waste	$\delta^{13}\text{C-CH}_4$ : -54.5 [-54.7, -54.3]	$\delta^{13}\text{C-CH}_4$ for waste sources (‰)
	$\delta\text{D-CH}_4$ : -292 [-296, -288]	$\delta\text{D-CH}_4$ for waste sources (‰)
Troposphere	KIE <sup>13</sup> C: 1.0066 [1.0052, 1.0075]	Sink-weighted total KIE <sup>13</sup> C in the troposphere
	KIE D: 1.317 [1.305, 1.327]	Sink-weighted total KIE D in the troposphere
Stratosphere	KIE <sup>13</sup> C: 1.01436 [not varied]	KIE <sup>13</sup> C in the stratosphere
	KIE D: 1.133 [not varied]	KIE D in the stratosphere
Soil	KIE <sup>13</sup> C: 1.0201 [not varied]	KIE <sup>13</sup> C in the soil
	KIE D: 1.0825 [not varied]	KIE D in the soil
Emission errors ( $\epsilon$ )	Prior values $\pm$ 30% [10-50%]	Emission errors per source category
Interhem. Mixing ( $\tau$ )	Prior values 0.75 [0.65-0.95]	Interhemispheric exchange time of methane between NH and SH
Observational errors:	1, 0.1, 0.001	Observational errors based on natural abundance of species
$\sigma_{\chi(\text{CH}_4)}$	1 ppb, 0.001 ppb, 0.0001 ppb	Optimal for $\delta^{13}\text{C-CH}_4$
$\sigma_{\delta^{13}\text{C-CH}_4}$	1 ppb, 0.001 ppb, 0.00005 ppb	Balanced observational errors
$\sigma_{\delta\text{D-CH}_4}$	1 ppb, 0.005 ppb, 0.0001 ppb	Optimal for $\delta\text{D-CH}_4$

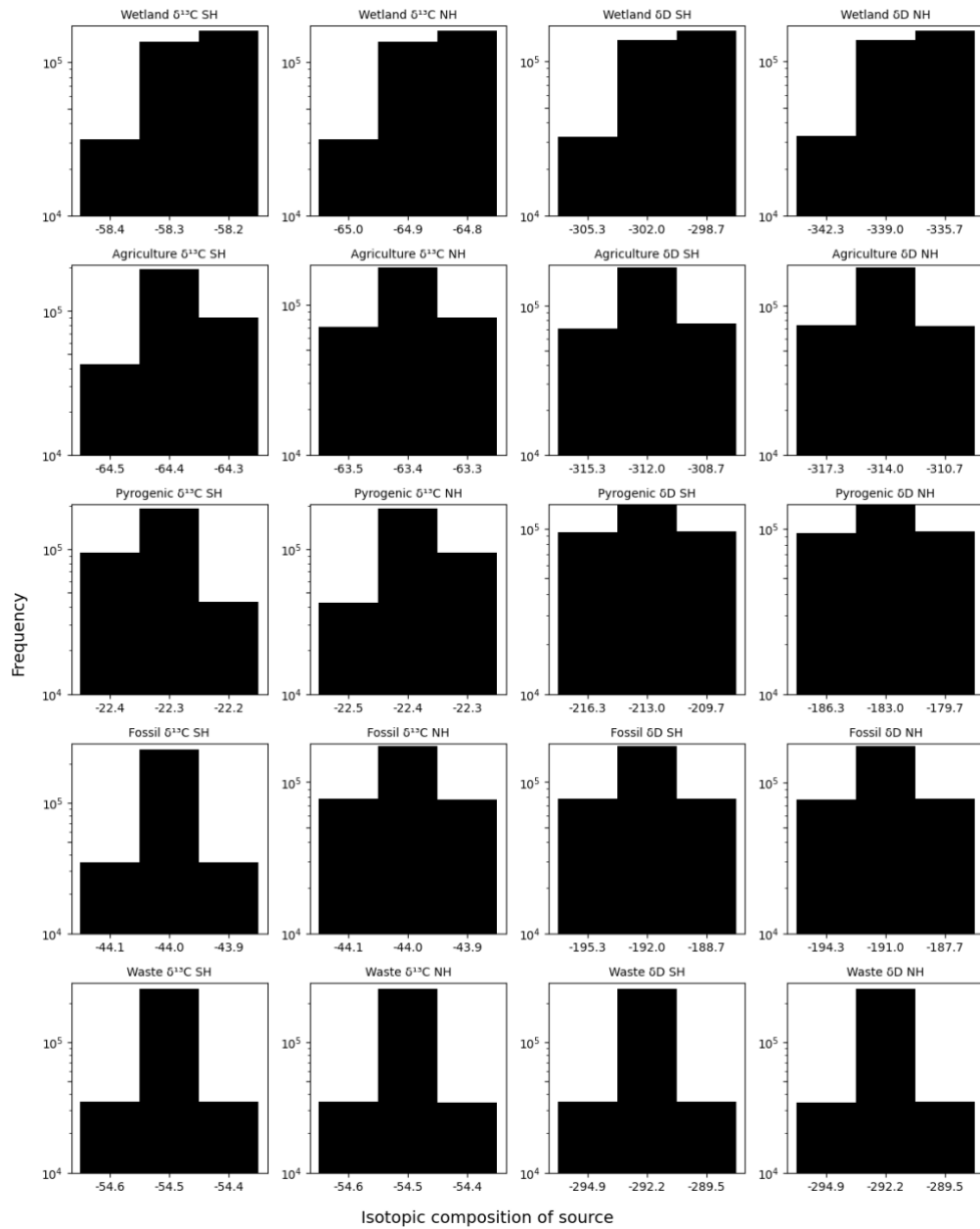


**Figure S7a:** Scatter plot showing the relationship between the raw RMSE and the normalised RMSE across approximately 13.1 million simulations. Each point represents a specific combination of prior parameter values, with normalisation applied to the RMSE of each tracer and hemisphere to ensure comparability. Only simulations with a mean normalised RMSE below 0.1 are highlighted in grey, indicating the optimised parameter combinations that best align the posterior tracers with the observational data.

### Model Evaluation



**Figure S7b:** Frequency histogram plot showing the distribution of raw RMSE (top), normalised RMSE (middle), and normalised RMSE in log scale (bottom) across  $\sim 13.1$  million simulations. Each colour represents a specific RMSE calculated by comparing observation-posterior results per tracer/hemisphere combination. Only simulations with a mean normalised RMSE below 0.1 are highlighted in grey (middle panel), indicating the optimised parameter combinations that best align the posterior tracers with the observational data.

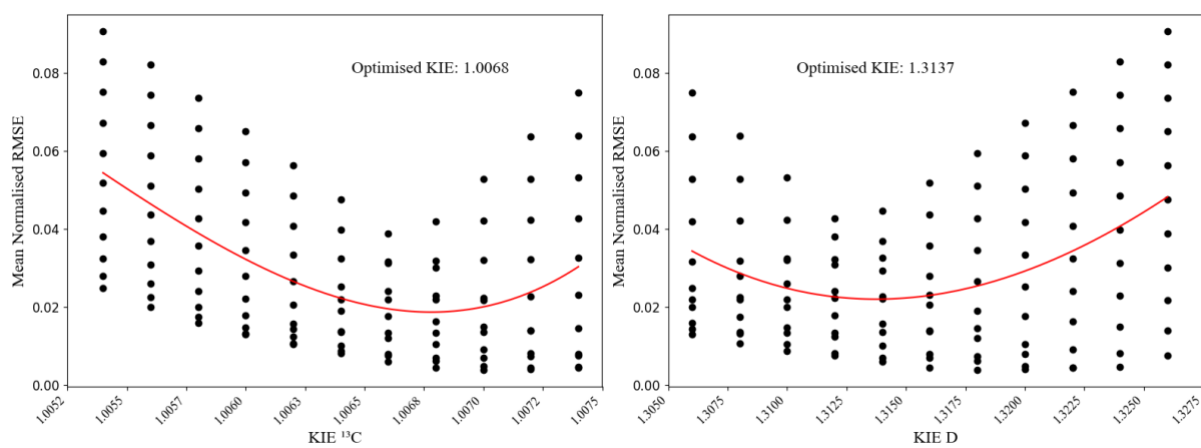


**Figure S8:** Variability in isotopic composition of  $\text{CH}_4$  sources for each hemisphere, showing  $\delta^{13}\text{C}$  and  $\delta\text{D}$  values (‰) by source category in the two-box model. The x-axis represents the range of source isotopic compositions tested during model iterations, and the y-axis indicates the count of occurrences for each value within the  $<0.1$  RMSE subset of results. Optimised values shown as the peak in each subplot, derived from this approach, are the most occurring model parameters within the sub-0.1 RMSE subset.

## S9. Isotopic Fractionation Due to Sink

CH<sub>4</sub> is removed from the atmosphere mainly by three photochemical reactions with OH, O(<sup>1</sup>D), and Cl. Approximately 90% of atmospheric CH<sub>4</sub> removal occurs in the troposphere (Oh et al., 2025). The largest part is thereby the reaction with OH (>90% of the tropospheric sink), while the rest is attributed to the reaction with Cl in the marine boundary layer (MBL; Kirschke et al., 2013). About 8% of CH<sub>4</sub> is depleted in the stratosphere through reactions with OH, O(<sup>1</sup>D), and Cl, as well as via photolysis and soil uptake (IPCC, 2013).

Three types of atmospheric CH<sub>4</sub> sink processes were considered: a weighted tropospheric chemical sink (reaction with OH and Cl), a weighted stratospheric sink (reaction with OH, O(<sup>1</sup>D), and Cl in the stratosphere), and a soil sink. These sink reactions influence the isotopic composition of the remaining CH<sub>4</sub>, with fractionation constants summarised in Table 2. When discrepancies arose among studies, we opted for values supported by inverse modelling results; for instance, for tropospheric OH fractionation on δ<sup>13</sup>C-CH<sub>4</sub>, Lan et al. (2021) found that a fractionation value of -5.4 ‰ based on Cantrell et al. (1990) best matched observations, in contrast to -3.9 ‰ from Saueressig et al. (2001). Similarly, for Cl, Saueressig et al. (1995) reported a value of 1.0676. Combining both of these values in their relative form, we get a net tropospheric KIE of 1.0066. Tropospheric removal of δD-CH<sub>4</sub> due to Cl and OH is temperature-dependent, with a global rate-weighted average temperature of 4.0 ± 0.1 °C derived from the ECHAM/MESSy Atmospheric Chemistry model (2009-2017) (Gromov, 2022). The fractionation constants for sink reactions involving OH, O(<sup>1</sup>D), and Cl were determined from sample observations (Röckmann et al., 2011). However, since our model doesn't consider each stratospheric sink separately, the effective stratospheric sink is parameterised as a first-order sink in the hemispheric boxes, with a pseudo-KIE that mimics stratospheric removal processes (see Rockmann et al., 2011; also explained below). This parameterisation allows the model to account for the influence of stratospheric sinks on tropospheric CH<sub>4</sub> without explicitly modelling the stratosphere as a separate entity (Table 2). For tropospheric KIE, the DPT analysis was iterated over specified ranges of fractionation values (e.g., 1.005–1.0076 for <sup>13</sup>C, with a step size of 0.0002) and calculated the RMSE for all combinations, identifying the lowest RMSE values as the best candidates (Fig. S9).



**Figure S9:** Range of KIE signatures for  $\delta^{13}\text{C}\text{-CH}_4$  and  $\delta\text{D}\text{-CH}_4$  derived from DPT tests with RMSE <0.1, measured in the model output (between atmospheric observations and posterior results)

## Pseudo-KIE Calculation Process

### 1. Stratospheric Fractionation Factor (epsilon)

Using the formula:

$$\epsilon_s = 1/\text{KIEs} - 1$$

- For  $^{13}\text{C}$ :

$$\epsilon_s^{13\text{C}} = 1/1.0147 - 1 = 0.9855 - 1 = -0.0145$$

- For  $^2\text{H}$ :

$$\epsilon_s^{2\text{H}} = 1/1.137 - 1 = 0.8793 - 1 = -0.1207$$

These align with the previously calculated values.

### 2. Effective Fractionation Factor (epsilon effective)

Using the formula for effective fractionation:

$$\epsilon_{\text{eff}} = \ln(\delta_{\text{eff}}/\delta_0) / \ln(f_{\text{trop\_sink}})$$

with:

$$f_{\text{trop\_sink}} = (\text{total sources} - \text{sink}) / \text{total sources}$$

- Given:

Total sources = 703 Tg/year,

Stratospheric sink = 31 Tg/year,

$$f_{\text{trop\_sink}} = (703 - 31) / 703 = 0.956$$

- For  $^{13}\text{C}$ :

Using KIEs=1.0147,

$$\epsilon_s^{13\text{C}} = \ln(1.0147) / \ln(0.956) = 0.0146 / -0.0452 = -0.323$$

- For  $^2\text{H}$ :

Using KIEs=1.137,

$$\epsilon_s^{2\text{H}} = \ln(1.137) / \ln(0.956) = 0.1286 / -0.0452 = -2.847$$

### 3. Adjusting the KIE Values

The adjusted KIE incorporates the effective fractionation ( $\epsilon_{\text{eff}}$ ) to modify the observed fractionation.

For  $\text{KIE}_{\text{adjusted}}$ , we add  $\epsilon_{\text{eff}}$  to the original KIEs.

- For  $^{13}\text{C}$ :

$$\text{KIE}_{\text{adjusted}}^{13\text{C}} = 1.0147 - 0.000323 = 1.0144$$

- For  $^2\text{H}$ :

$$\text{KIE}_{\text{adjusted}}^{2\text{H}} = 1.137 - 0.002847 = 1.133$$

#### Final Adjusted KIE Values

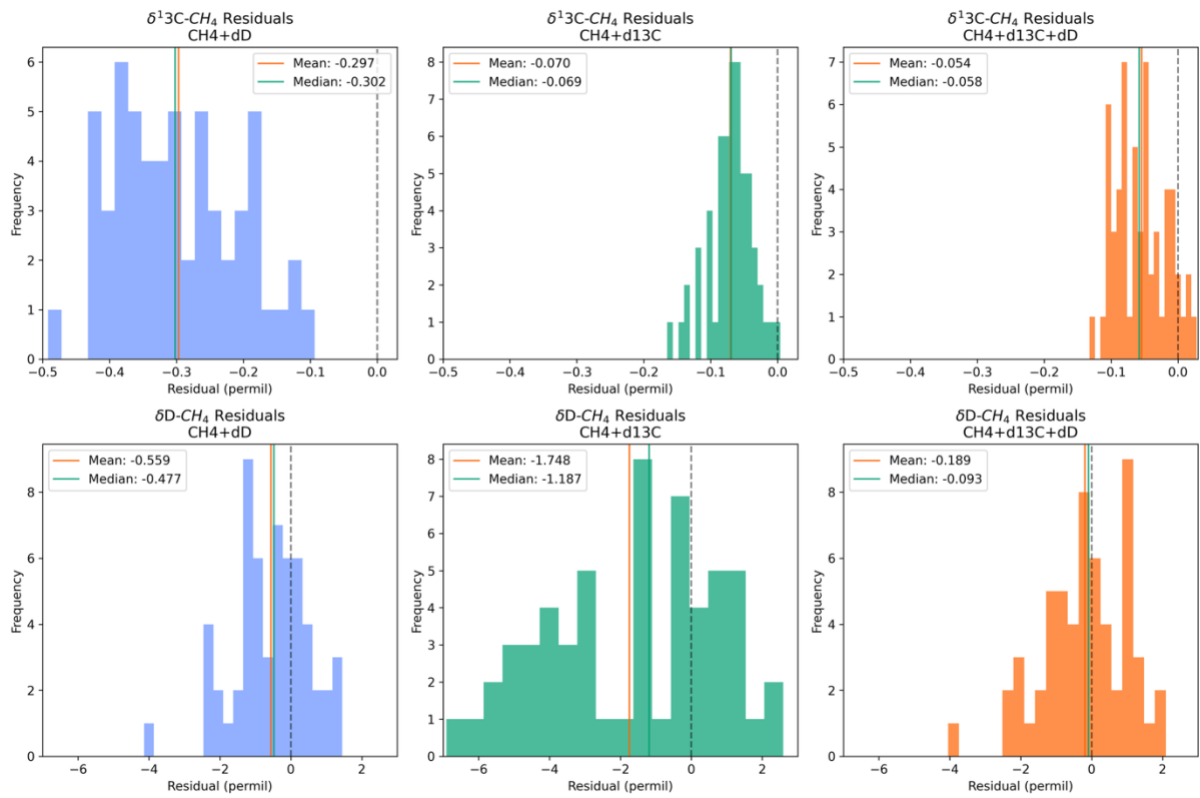
- $\text{KIE}^{13\text{C}} = 1.0144$
- $\text{KIE}^{2\text{H}} = 1.133$

## S10. Isotopic Constraints on the Inversion

Three inversion setups were tested: dual-isotope ( $\text{CH}_4 + \delta^{13}\text{C}$ - $\text{CH}_4 + \delta\text{D}$ ), carbon-only ( $\text{CH}_4 + \delta^{13}\text{C}$ ), and hydrogen-only ( $\text{CH}_4 + \delta\text{D}$ ). All inversions utilise the same two-box framework, DPT-optimised source signatures, sink KIEs, and prior uncertainties. To evaluate each inversion's performance, we calculate residuals, defined as the difference between the modelled and observed isotopic values. Lower residuals indicate that the inversion better reproduces the measured data.

The optimised source signatures from our DPT framework (Table 1), particularly the +3–4‰ enrichment in wetland  $\delta\text{D}$  relative to literature values, suggest that field-based isotopic characterisation may underrepresent emissions from enriched tropical wetland environments. While our residual analysis (Fig. S10) shows that dual-isotope inversions achieve superior fits for both tracers (mean  $\delta^{13}\text{C}$  residual  $-0.05\text{‰}$ ;  $\delta\text{D}$  residual  $-0.18\text{‰}$ ), systematic biases remain in specific periods, highlighting the need for expanded high-frequency isotopic observations, particularly in tropical and mid-latitude regions where source characterisation uncertainties are largest.

A small systematic negative bias in the SH posterior  $\delta^{13}\text{C}$  (Figure 2b) is apparent across the analysis period (mean residual  $\sim -0.05$  to  $-0.07 \text{‰}$ ; Fig. S10), most likely reflecting residual uncertainty in SH biogenic source signatures and the latitudinal gradient correction (SI Section 5). The DPT optimisation partially reduces this bias by shifting SH wetland  $\delta^{13}\text{C}$  toward slightly heavier values (Table 1). A modest underestimation of NH  $\delta\text{D}$ - $\text{CH}_4$  in the early record is similarly attributed to source-signal uncertainty and to the two-box structural limitations discussed in Section 4.6.



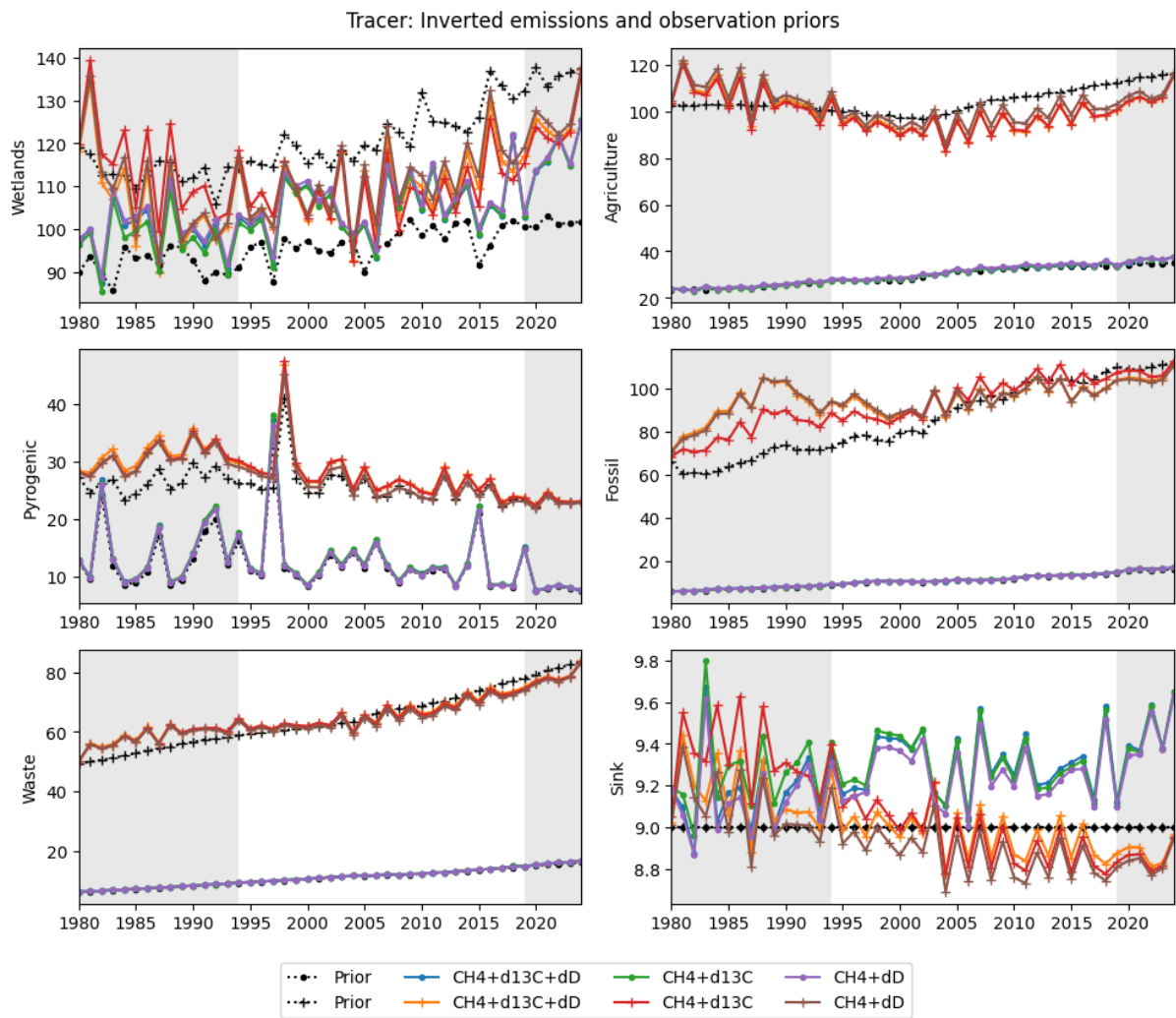
**Figure S10:** Histogram of residuals (modelled minus observed) for the 3 inversion setups (rows) calculated for the 2 isotopic tracers (columns).

**S11. Prior and posterior Flux Statistics (1994–2022). Growth is defined as the difference between the 1993-95 and 2021-23 averages.**

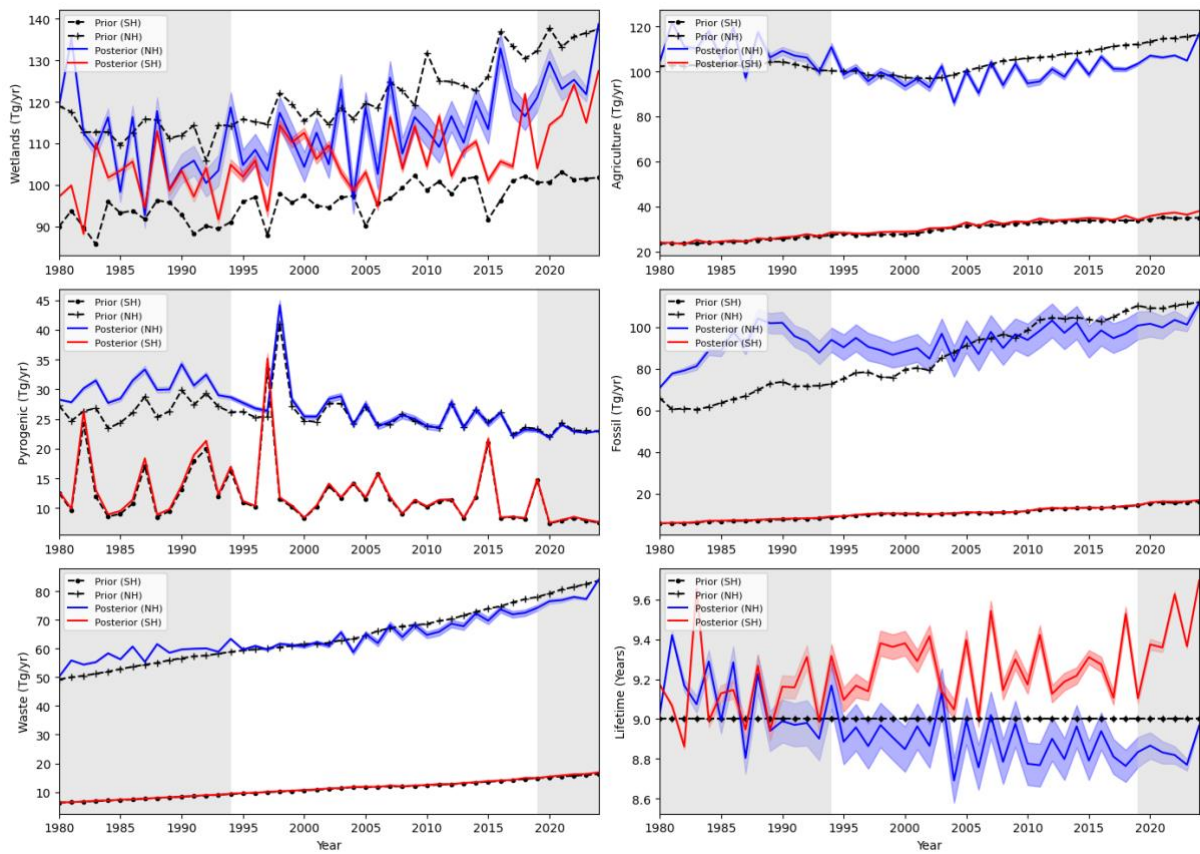
**Table S4:** Prior and posterior Flux Statistics (1994–2022). Growth is defined as the difference between the 1993-95 and 2021-23 averages.

<i>Iteration</i>	<b>Source</b>	<b>SH Mean ± SD (Tg)</b>	<b>SH Growth (Tg)</b>	<b>NH Mean ± SD (Tg)</b>	<b>NH Growth (Tg)</b>	<b>Global Mean ± SD (Tg)</b>	<b>Global Growth (Tg)</b>
<i>Prior</i>	wetlands	97.5 ± 3.9	9.8	123.5 ± 7.5	20.3	221.1 ± 10.1	30.1
<i>Prior</i>	agriculture	31.3 ± 2.7	7.6	104.5 ± 5.9	14.7	135.7 ± 8.4	22.3
<i>Prior</i>	pyrogenic	12.0 ± 5.1	-5.0	25.5 ± 3.4	-3.0	37.5 ± 6.3	-8.0
<i>Prior</i>	fossil	11.8 ± 2.0	7.1	93.6 ± 12.8	36.9	105.4 ± 14.7	44
<i>Prior</i>	waste	12.2 ± 1.9	6.4	68.3 ± 7.1	22.7	80.5 ± 9.0	29.1
<i>Dual isotope</i>	wetlands	106.5 ± 7.4	19.2	111.3 ± 8.7	16.1	217.8 ± 13.9	35.3
<i>Dual isotope</i>	agriculture	31.8 ± 2.9	9	96.4 ± 5.9	5.8	128.1 ± 7.5	14.8
<i>Dual isotope</i>	pyrogenic	12.6 ± 5.8	-5.6	27.1 ± 4.5	-6.0	39.7 ± 7.6	-11.6
<i>Dual isotope</i>	fossil	12.0 ± 2.0	7.4	96.3 ± 6.2	13.3	108.4 ± 7.9	20.7
<i>Dual isotope</i>	waste	12.4 ± 1.9	6.7	67.7 ± 5.7	16.7	80.1 ± 7.5	23.4
<i>Dual isotope</i>	sink	9.3 ± 0.1	0.3	9.0 ± 0.1	-0.2	9.1 ± 0.1	-0.1
<i>Carbon only</i>	wetlands	106.5 ± 7.5	20.5	110.3 ± 8.1	12.1	216.8 ± 13.3	32.6
<i>Carbon only</i>	agriculture	31.8 ± 3.0	9.4	96.2 ± 5.9	7.5	128.0 ± 7.8	16.9
<i>Carbon only</i>	pyrogenic	12.6 ± 5.9	-5.8	27.1 ± 4.6	-6.4	39.7 ± 7.9	-12.1
<i>Carbon only</i>	fossil	12.1 ± 2.1	7.4	98.0 ± 9.0	21.3	110.1 ± 10.7	28.7
<i>Carbon only</i>	waste	12.4 ± 1.9	6.7	67.5 ± 5.5	16.1	79.9 ± 7.3	22.8
<i>Carbon only</i>	sink	9.3 ± 0.1	0.2	9.0 ± 0.2	-0.4	9.1 ± 0.1	-0.2
<i>Hydrogen only</i>	wetlands	107.5 ± 7.1	18.9	113.1 ± 8.9	16.9	220.7 ± 13.7	35.8
<i>Hydrogen only</i>	agriculture	32.2 ± 3.0	9.1	99.3 ± 5.7	5.8	131.5 ± 7.6	14.8
<i>Hydrogen only</i>	pyrogenic	12.3 ± 5.6	-5.5	26.1 ± 4.3	-5.9	38.4 ± 7.4	-11.3
<i>Hydrogen only</i>	fossil	12.0 ± 2.0	7.4	96.6 ± 5.8	11.9	108.6 ± 7.4	19.2
<i>Hydrogen only</i>	waste	12.4 ± 1.9	6.7	66.7 ± 5.5	16.4	79.1 ± 7.3	23.1
<i>Hydrogen only</i>	sink	9.3 ± 0.1	0.3	8.9 ± 0.1	-0.2	9.1 ± 0.1	-0.1
<i>Error-scaled</i>	wetlands	101.1 ± 4.5	13.1	119.4 ± 7.1	18.5	220.4 ± 10.3	31.5
<i>Error-scaled</i>	agriculture	32.4 ± 2.9	9.3	96.8 ± 6.3	5.4	129.3 ± 7.8	14.7
<i>Error-scaled</i>	pyrogenic	12.5 ± 5.7	-5.5	26.4 ± 4.5	-5.9	38.9 ± 7.5	-11.4
<i>Error-scaled</i>	fossil	12.2 ± 2.1	7.6	98.7 ± 6.8	13.5	110.9 ± 8.4	21.1
<i>Error-scaled</i>	waste	12.5 ± 1.9	6.9	65.2 ± 5.6	15.5	77.7 ± 7.3	22.4
<i>Error-scaled</i>	sink	9.5 ± 0.2	0.5	8.8 ± 0.2	-0.2	9.1 ± 0.1	0.0
<i>DPT-ensemble</i>	wetlands	107.8 ± 7.4	19.1	114.7 ± 8.7	14.4	222.6 ± 13.8	33.5
<i>DPT-ensemble</i>	agriculture	32.3 ± 2.9	8.9	99.8 ± 5.6	3	132.0 ± 7.2	12
<i>DPT-ensemble</i>	pyrogenic	12.2 ± 5.4	-5.3	26.0 ± 4.1	-5.2	38.2 ± 7.0	-10.5
<i>DPT-ensemble</i>	fossil	12.0 ± 2.0	7.4	94.5 ± 5.6	10.8	106.5 ± 7.2	18.2
<i>DPT-ensemble</i>	waste	12.4 ± 1.9	6.7	66.8 ± 5.8	16.8	79.1 ± 7.6	23.5
<i>DPT-ensemble</i>	sink	9.3 ± 0.2	0.3	8.9 ± 0.1	-0.2	9.1 ± 0.1	-0.1

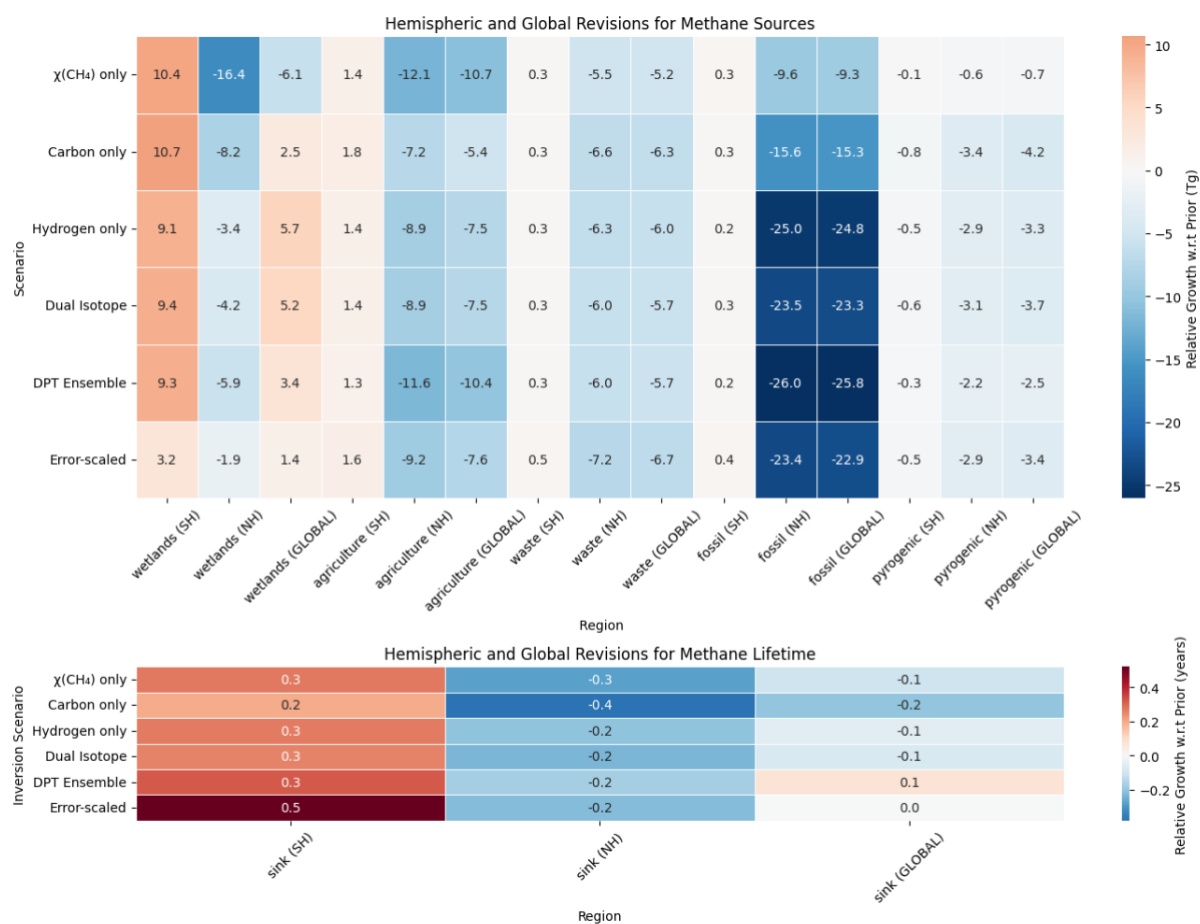
**S12. Hemispheric plots for figures 3 and 4; CH<sub>4</sub>-only inversion results in figure 5**



**Figure S11:** (Hemispheric): Prior (black) and posterior (coloured) emissions and sink lifetime values, with NH in '+' markers and SH in 'o' markers, modelled by the two-box inversion computed for 3 inversion scenarios: (i) CH<sub>4</sub> + δ<sup>13</sup>C + δD, (ii) CH<sub>4</sub> + δ<sup>13</sup>C, and (iii) CH<sub>4</sub> + δD. The spin-up and spin-down periods are shaded, and the analysis period is unshaded.



**Figure S12:** Prior (black; with NH in '+' markers and SH in 'o' markers) and posterior (NH – blue, SH – red) emission rates and lifetime computed from the optimised values derived from sensitivity tests (<0.1 RMSE). These values are calculated from the ensemble mean of the DPT-optimised model output, which is obtained by comparing the posterior tracers ( $\text{CH}_4$ ,  $\delta^{13}\text{C}\text{-CH}_4$ , and  $\delta\text{D}\text{-CH}_4$ ) with atmospheric observational data. The optimised emission rates and lifetime represent the model's best estimates of  $\text{CH}_4$  sources and sinks, refined to minimise the difference between simulated and observed tracer values. The spin-up and spin-down periods are shaded, and the analysis period is unshaded.



**Figure S13:** Top panel: Hemispheric and global revisions w.r.t the priors ( $\text{Posterior}_{\text{growth}} - \text{Prior}_{\text{growth}}$ ) of the growth in emissions by sector (wetlands, agriculture, waste, fossil, pyrogenic) in teragrams (Tg). Growth is defined as the difference between the 1993-95 and 2021-23 averages. Bottom panel: hemispheric and global revisions for  $\text{CH}_4$  lifetime (in years). Apart from not being able to reproduce the atmospheric measurements of  $\delta^{13}\text{C}-\text{CH}_4$  and  $\delta\text{D}-\text{CH}_4$ , the  $\chi(\text{CH}_4)$ -only inversion also shows the maximum disagreement with the Priors compared to all other inversion scenarios in both sources and lifetime, suggesting that  $\chi(\text{CH}_4)$ -only inversion inadequately budgets the global  $\text{CH}_4$  burden.

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