



Supplement of

Cluster-dynamics-based parameterization for sulfuric acid–dimethylamine nucleation: comparison and selection through box and three-dimensional modeling

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33 **Assessing the reliability of the conventional treatment of gas-cluster-aerosol**
34 **interactions in WRF-Chem/R2D-VBS simulations.**

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36 Olenius and Roldin (2022) provided insights on the potential impact of gas-
37 cluster-aerosol dynamics on NPF simulation using chemical transport models. Among
38 various standard treatments of gas-cluster-aerosol dynamics in chemical transport
39 modeling, they highlighted the assumption of instantaneous steady-state nucleation at
40 every model time step as a potential source of bias. In response to this, we conducted a
41 reliability assessment of steady-state nucleation in our WRF-Chem/R2D-VBS
42 simulations. We evaluated the validity of the steady-state nucleation assumption by
43 considering the system's e-folding time (time for clusters to reach $(1-1/e)$ of their
44 terminal concentration, following Li et al., (2023)). Specifically, we deemed the
45 assumption reasonable if, under certain atmospheric conditions, the system's e-folding
46 time is less than the simulation time step (300 s).

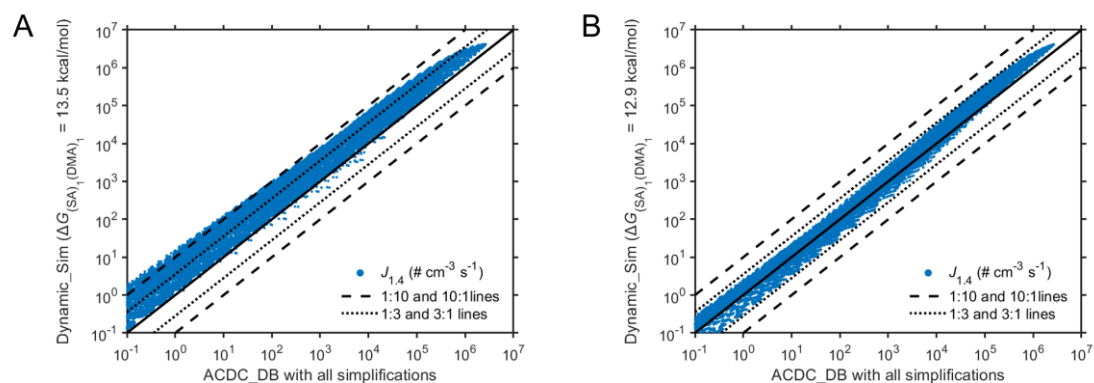
47 As shown in Figure S14, results indicates that the e-folding time does not show a
48 significant correlation with $J_{1.4}$. Under the majority of atmospheric conditions (77.3%),
49 the nucleating system's e-folding time is less than 300 s. Instances where the e-folding
50 time exceeds 300 s are primarily observed in winter clean conditions characterized by
51 low temperature ($T < \sim 270$ K), low condensation sink ($CS < \sim 0.003$ s⁻¹), and low
52 precursor concentrations ($SA < \sim 10^6$ cm⁻³). These findings align with the observations
53 of Olenius and Roldin (2022). It's important to emphasize that this e-folding time
54 represents the duration required for the system to transition from having only precursor
55 molecules to reaching near-equilibrium concentrations of various clusters. In reality,
56 cluster concentrations generally do not start from zero. Therefore, the calculated e-
57 folding time serves as an upper limit estimate. Given the predominance of atmospheric
58 conditions where the e-folding time falls within or below the simulation time step of
59 300 s, consequently, the steady-state treatment is generally deemed reasonable for our
60 WRF-Chem/R2D-VBS simulations.

61 We further investigated another common treatment that may introduce bias:
62 neglecting cluster formation in consuming precursor during nucleation. Our
63 examination focused on assessing the proportion of precursor consumption by cluster
64 formation relative to precursor concentrations. As shown in Figure S15 and S16, we
65 found that this proportion increases with $J_{1.4}$ for both SA and DMA. Under the majority
66 of atmospheric conditions (82.0% for DMA and 57% for SA), proportions are below
67 10%. Proportions exceed 10% are predominantly observed in scenarios also
68 characterized by low temperature ($T < \sim 270$ K) and low condensation sink ($CS <$
69 ~ 0.003 s⁻¹), but with high deference in concentrations between DMA and SA.
70 Specifically, elevated SA concentrations, which lead to significant DMA consumption
71 through cluster formation, and vice versa, contribute to scenarios where precursor
72 consumption by cluster formation exceeds 10%. It's noteworthy that our calculation of
73 precursor consumption by cluster formation starts from zero cluster concentration. Also,
74 in the real atmosphere, cluster concentrations are generally nonzero, leading to another

75 upper limit estimate. Therefore, based on our analysis, it can be inferred that cluster
76 formation may not introduce significant bias into NPF simulations under typical
77 atmospheric conditions.

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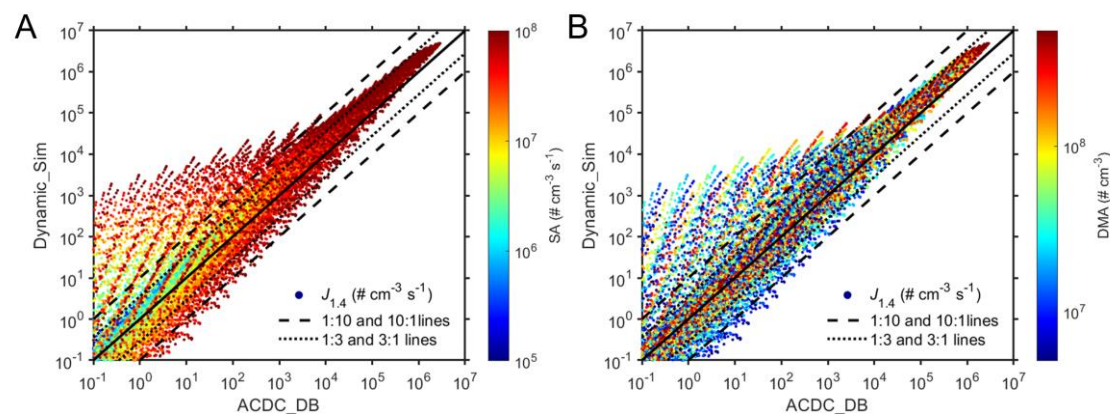
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82 **Figure S1.** Comparison of $J_{1,4}$ predictions between ACDC_DB with all simplifications
 83 and Dynamic_Sim with different ΔG for initial (SA)₁(DMA)₁ cluster. A: $\Delta G = -13.5$
 84 kcal/mol; B: $\Delta G = -12.9$ kcal/mol (Ning et al. 2024). Solid dots represent simulated $J_{1,4}$
 85 values, solid lines indicate a 1:1 line, dotted lines correspond to 1:3 and 3:1 lines, and
 86 dashed lines represent 1:10 and 10:1 lines.

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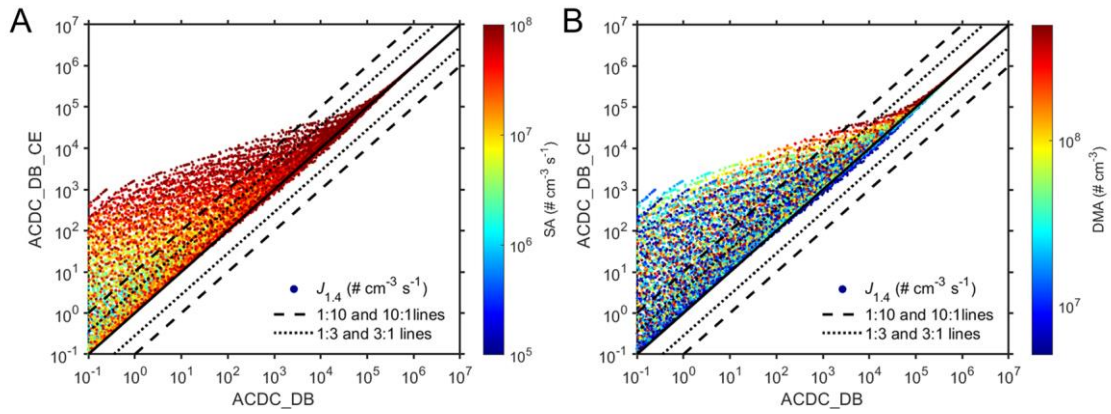
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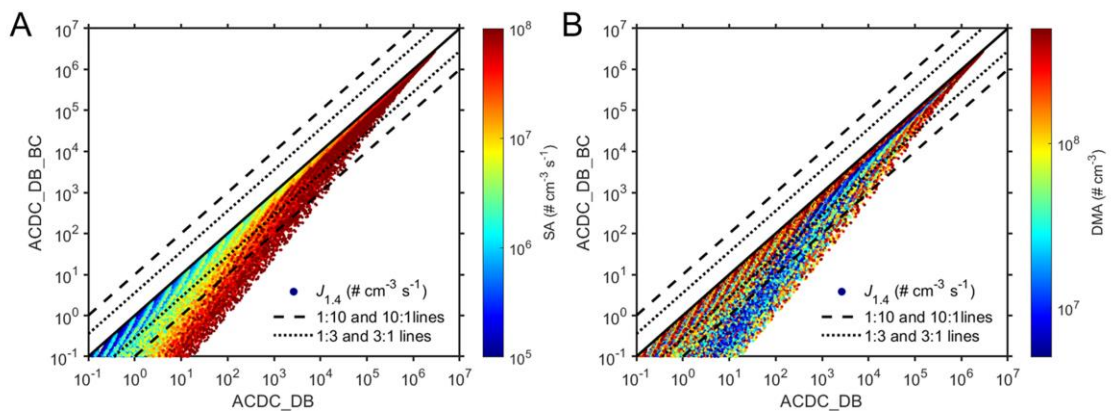
90 **Figure S2.** Comparison of $J_{1,4}$ predictions between ACDC_DB and Dynamic_Sim
 91 correlated with [SA] variation (A) and [DMA] variation (B). Solid dots represent
 92 simulated $J_{1,4}$ values, solid lines indicate a 1:1 line, dotted lines correspond to 1:3 and
 93 3:1 lines, and dashed lines represent 1:10 and 10:1 lines.

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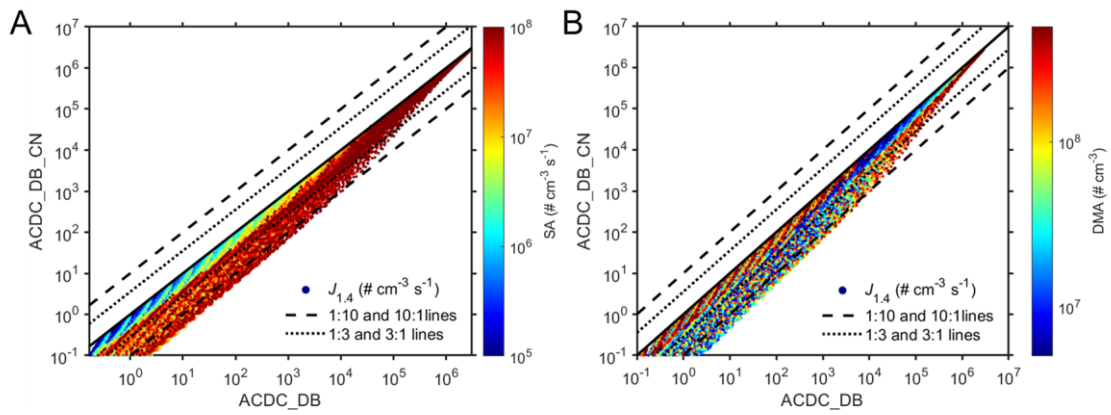
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Figure S3. Same as Figure S2 but for ACDC_DB_CE.



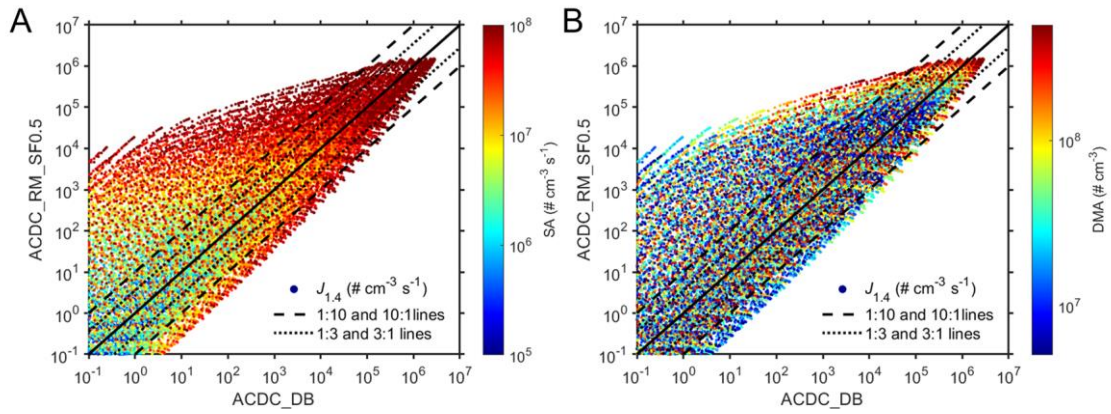
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Figure S4. Same as Figure S2 but for ACDC_DB_BC.



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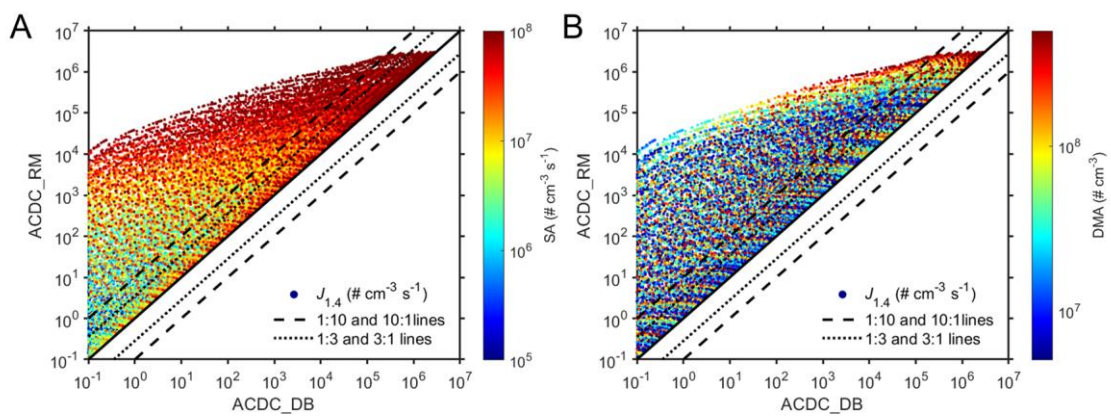
Figure S5. Same as Figure S2 but for ACDC_DB_CN.



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105 **Figure S6.** Same as Figure S2 but for ACDC_RM_SF0.5.

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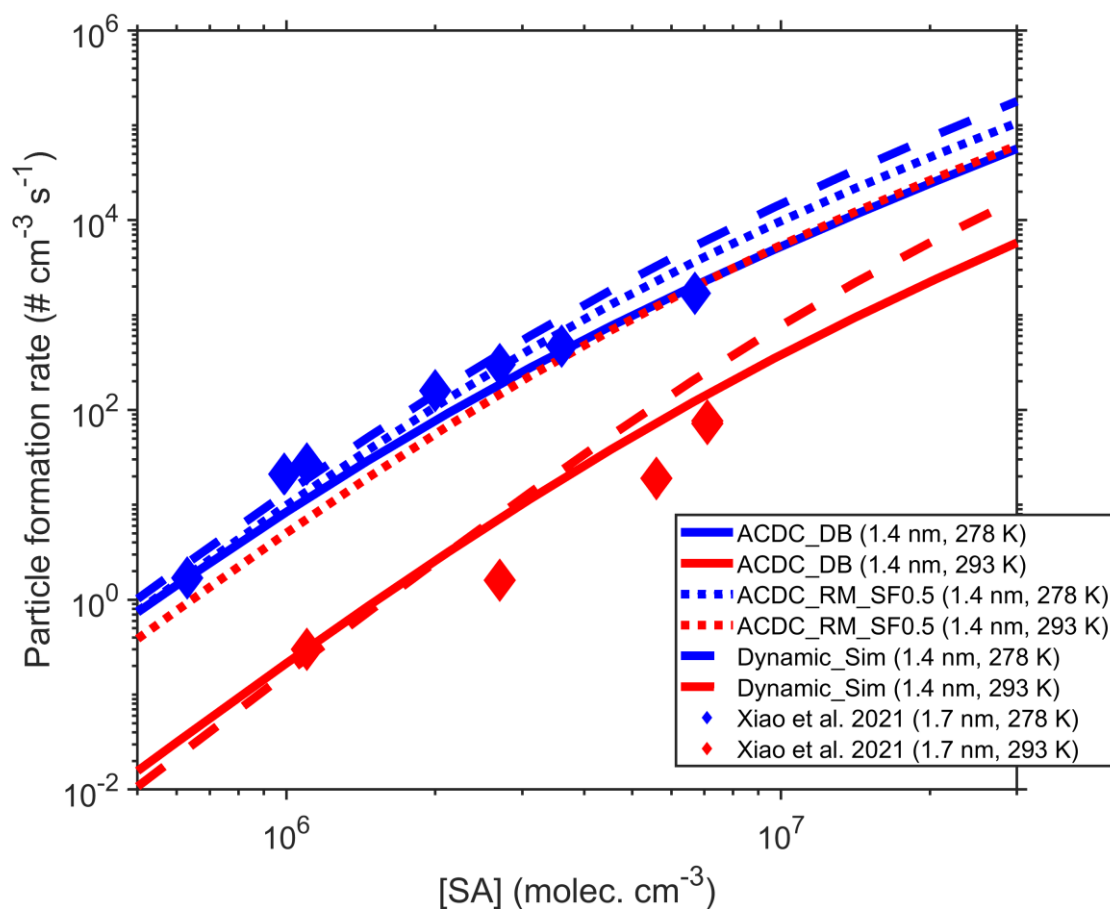
108 **Figure S7.** Same as Figure S2 but for ACDC_RM.

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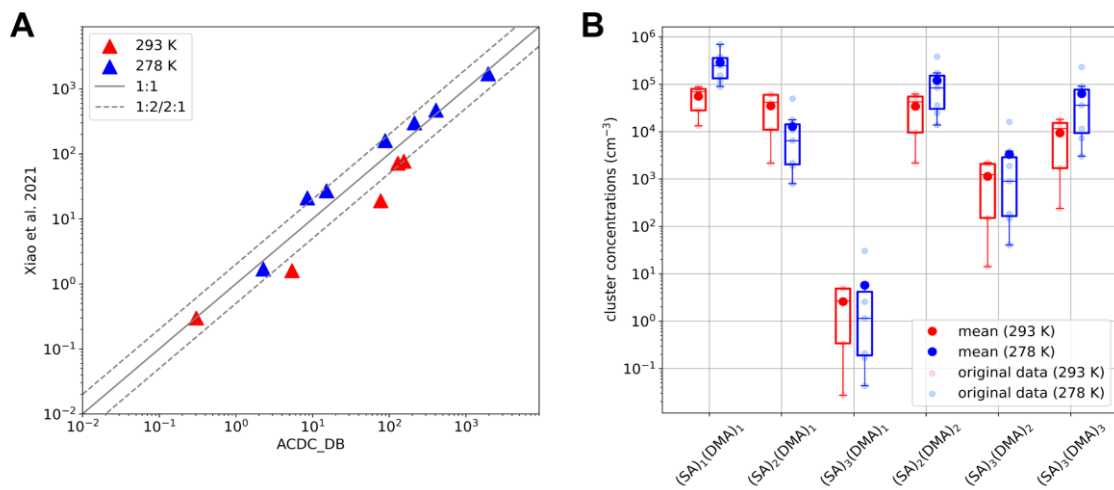
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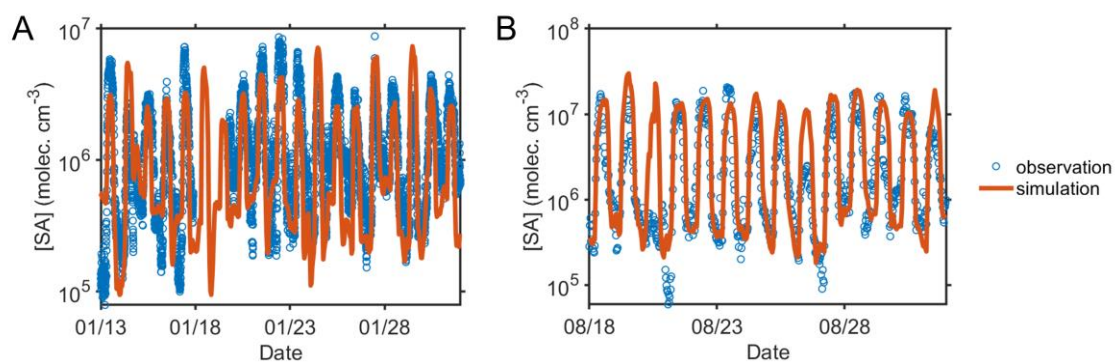
114 **Figure S8.** Comparison of modeled particle formation rates with measurements from
115 CLOUD chamber experiments conducted by Xiao et al. 2021. Blue lines or diamonds
116 represent particle formation rates at 278 K, while red ones represent those at 293 K;
117 solid, dotted, and dashed lines denote the simulated results of ACDC_DB,
118 ACDC_RM_SF0.5, and Dynamic_Sim, respectively. The simulations were conducted
119 following the experimental conditions of Xiao et al. 2021, with specific conditions
120 provided in their Table S1 and Table S2. It is noteworthy that Xiao et al. 2021 reported
121 particle formation rates at 1.7 nm, whereas our simulations are at 1.4 nm. This
122 discrepancy may lead to a slight overestimation of the simulated particle formation rates
123 for simulations compared to the experiments. However, in the experiments, ~1 ppbv
124 NH₃ was involved besides DMA during nucleation, which might enhance nucleation
125 rates somewhat even through DMA is the dominant enhancing agent for SA-driven
126 nucleation. Therefore, the two effects could partly offset each other, allowing for a
127 direct comparison of particle formation rates between simulations and measurements.
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Figure S9. Comparison of measured $J_{1,7}$ from Xiao et al. 2021 and simulated $J_{1,4}$ using ACDC_DB with corresponding DMA concentrations in experiments (A), and the comparison of cluster concentrations at 293 K and 278 K (B).

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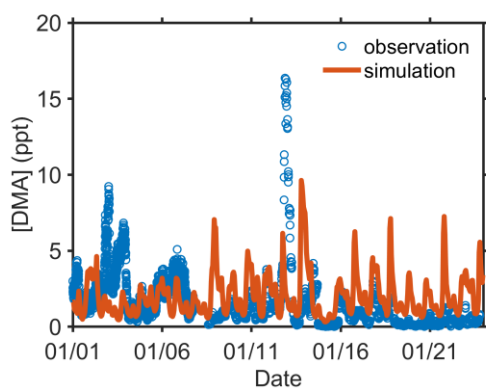


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137 **Figure S10.** Comparison of simulated and observed SA concentrations. A for January
138 and B for August 2019.

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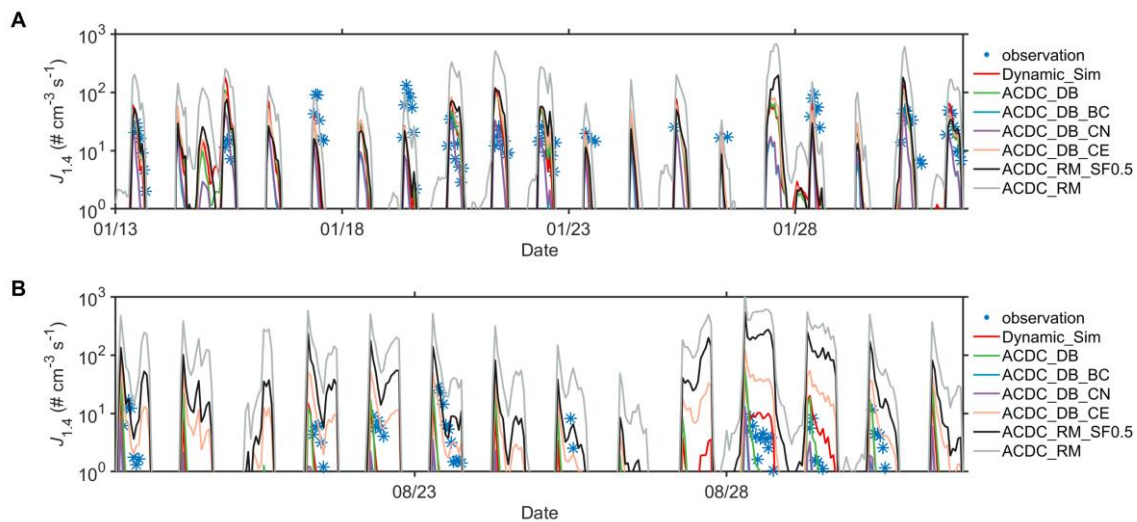
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142 **Figure S11.** Comparison of simulated and observed DMA concentrations in January
143 2019. Only data for winter month (January 2019) is available.

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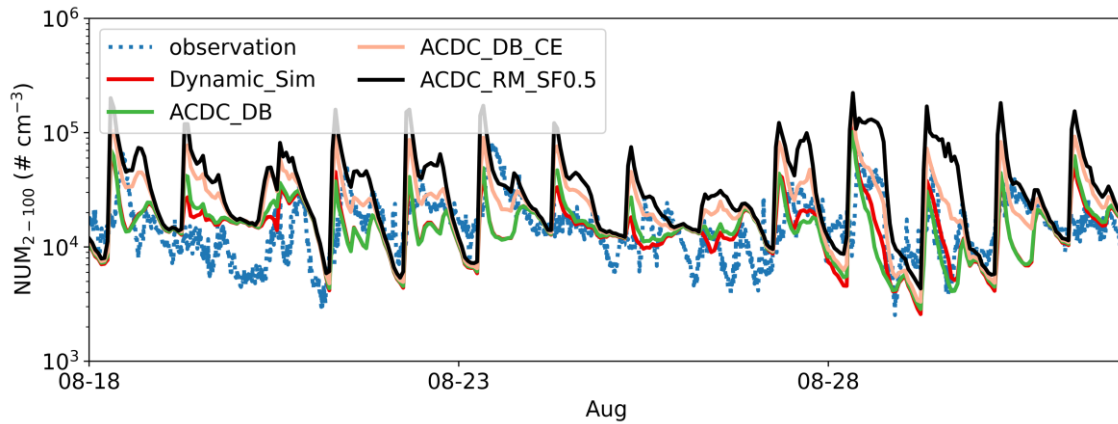
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148 **Figure S12.** Comparison of simulated particle formation rates with those derived from
 149 field measurements during (A) January 13, 2019, to January 31, 2019, and (B) August
 150 18, 2019, to August 31, 2019, in Beijing.

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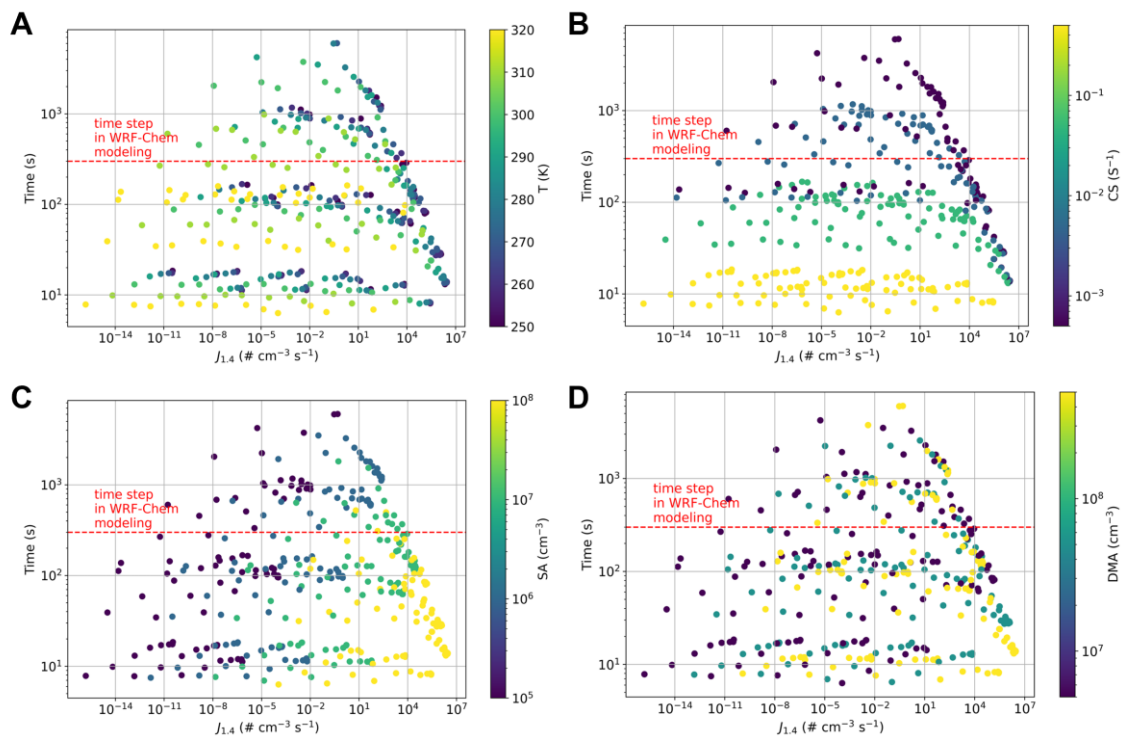
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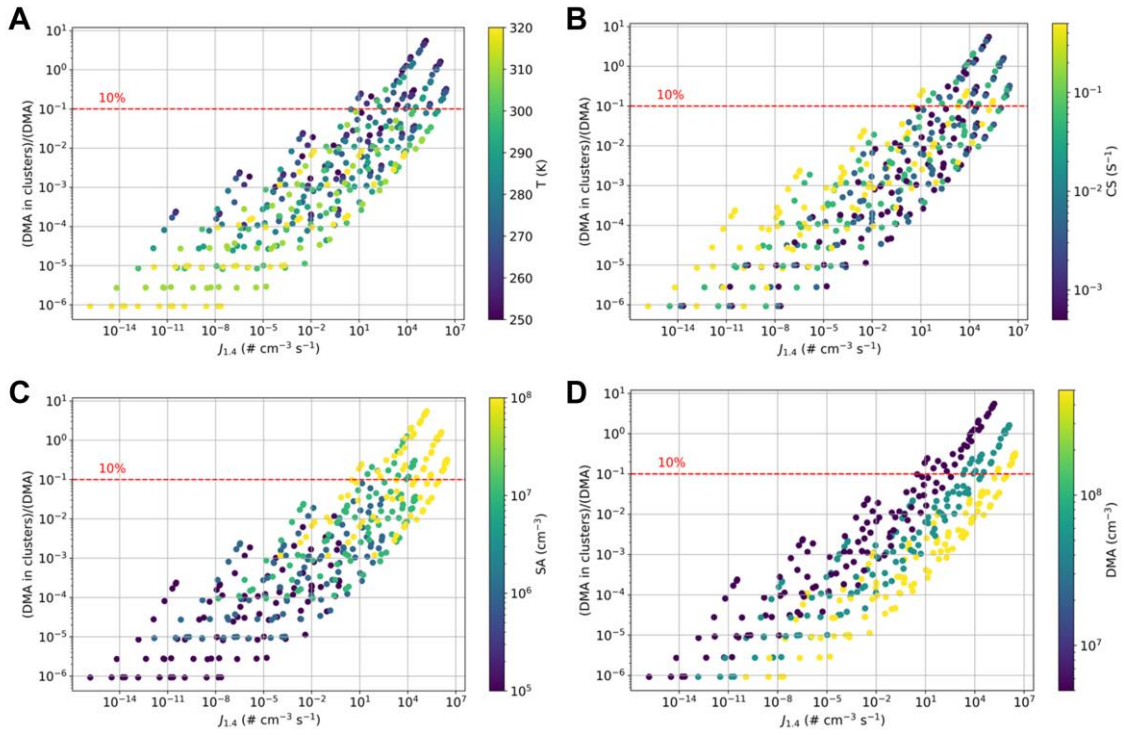
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Figure S13. Comparison of observed and simulated aerosol number concentration within 2-100 nm during August 18, 2019, to August 31, 2019, in Beijing. Simulations are conducted using parameterizations of Dynamic_Sim, ACDC_DB, ACDC_DB_CE, and ACDC_RM_SF0.5.



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Figure S14. The variation of e-folding time with $J_{1.4}$ correlated with temperature (A), CS (B), SA concentration (C), and DMA concentration (D). The data points were calculated using a more sparse sequence of input parameters (T: 250, 260, 270, 280, 290, 300, 310, 320 (K); CS: 5.00×10^{-4} , 5.00×10^{-3} , 5.00×10^{-2} , 5.00×10^{-1} (s^{-1}); SA: 1.00×10^5 , 1.00×10^6 , 1.00×10^7 , 1.00×10^8 (cm^{-3}); DMA: 5.00×10^6 , 5.00×10^7 , 5.00×10^8 (cm^{-3})) compared to those shown in Table S1.

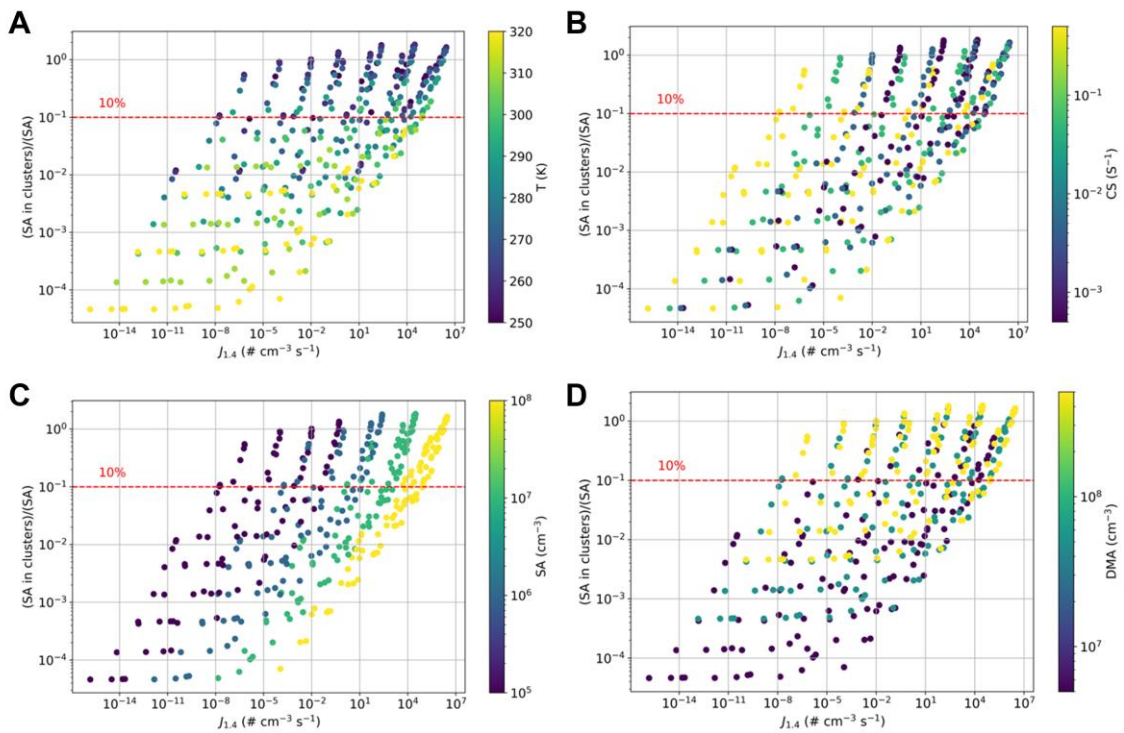


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171 **Figure S15.** The variation of proportion of DMA consumption by cluster formation
 172 relative to precursor concentrations with $J_{1,4}$, correlated with temperature (A), CS (B),
 173 SA concentration (C), and DMA concentration (D). The input variables are consistent
 174 with Figure S14.

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178 **Figure S16.** The variation of proportion of SA consumption by cluster formation
179 relative to precursor concentrations with $J_{1,4}$, correlated with temperature (A), CS (B),
180 SA concentration (C), and DMA concentration (D). The input variables are consistent
181 with Figure S14.
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183 **Table S1.** The ranges, total numbers and values at each point for the input parameters
 184 in deriving look-up tables

	Range	Number of points	Values at each point
T (K)	250 – 320	15	$250 + 5 \times i, i = 0,14$
CS (s^{-1})	$5 \times 10^{-4} - 5 \times 10^{-1}$	16	$5 \times 10^{-4} \times 10^{0.2 \times i}, i = 0,15$
[SA] ($\# \text{ cm}^{-3}$)	$1 \times 10^5 - 1 \times 10^8$	16	$1 \times 10^5 \times 10^{0.2 \times i}, i = 0,15$
[DMA] ($\# \text{ cm}^{-3}$)	$5 \times 10^6 - 5 \times 10^8$	11	$5 \times 10^6 \times 10^{0.2 \times i}, i = 0,10$

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189 **Table S2.** Comparison of simulated and observed concentrations of the nucleating
 190 precursors.

Precursor	Time period	Site	Simulation	Observation	Bias	NMB
SA ($\#/\text{cm}^3$)	2019.01.13- 2019.01.31	Beijing	1.35×10^6	1.47×10^6	1.20×10^5	-10.80%
	2019.08.18- 2019.08.31		5.74×10^6	3.51×10^6	2.23×10^6	14.32%
DMA (pptv)	2019.01.01- 2019.01.31	Beijing	1.96	1.98	-0.02	-10.96%

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