

## Box 1

### Coupled AerChemMIP experiments (3 UKESM1 ensemble members)

$X$  = radiative flux  
and cloud properties

All historical emissions  
(AerChemMIP-all-emissions)

$\Delta X_{\text{all}}$

minus

All historical emissions with  
PI aerosol emissions  
(AerChemMIP-GHG-only-proxy)

$\Delta X_{\text{GHG}}$

produces

Aerosol-only historical emissions  
proxy  
(AerChemMIP-aerosol-only-proxy)

$\Delta X_{\text{aer}} = \Delta X_{\text{all}} - \Delta X_{\text{GHG}}$

### Aerosol forcing & associated feedback

## Box 3

### Feedback calculations

#### Feedback due to GHGs

$\Delta X_{\text{feedback GHG}} = \Delta X_{\text{GHG}}$   
(all of the response is assumed  
to be due to feedbacks)

#### Feedback due to aerosols

$\Delta X_{\text{feedback aer}} = \Delta X_{\text{aer}} - \Delta X_{\text{aer}}^{\text{eff}}$   
(Equation 2, see also Equation 3 for an  
alternative method).

### Total feedback

$\Delta X_{\text{feedback tot}}$   
 $= \Delta X_{\text{feedback GHG}} + \Delta X_{\text{feedback aer}}$

## Box 2

### Nudged UKESM1 atmosphere-only

Pre-industrial and present day  
(2009) emission  
*Grosvenor and Carslaw (2020)*

Aerosol ERFs  
 $\Delta F_{\text{ari}}^{\text{eff}}$  nudged,  $\Delta F_{\text{aci}}^{\text{eff}}$  nudged

Aerosol-cloud adjustments  
 $\Delta f_{\text{c aci}}^{\text{eff}}$  nudged  
 $\Delta L_{\text{aci}}^{\text{eff}}$  nudged  $\Delta N_{\text{d aci}}^{\text{eff}}$  nudged  
(ARI values are zero)

Scaling using  $\Delta N_{\text{d aer}}$   
and  $\Delta N_{\text{d aci}}^{\text{eff}}$

Coupled model aerosol ERFs  
 $\Delta F_{\text{ari}}^{\text{eff}}$  coupled,  $\Delta F_{\text{aci}}^{\text{eff}}$  coupled

Coupled model aerosol-cloud adjustments  
 $\Delta f_{\text{c aci}}^{\text{eff}}$  coupled,  $\Delta L_{\text{aci}}^{\text{eff}}$  coupled

Coupled model total aerosol ERF and adjustments  
 $\Delta X_{\text{aer}}^{\text{eff}}$  coupled =  $\Delta X_{\text{ari}}^{\text{eff}}$  coupled +  $\Delta X_{\text{aci}}^{\text{eff}}$  coupled

### Aerosol forcing only