



Supplement of

A new process-based and scale-aware desert dust emission scheme for global climate models – Part I: Description and evaluation against inverse modeling emissions

Danny M. Leung et al.

Correspondence to: Danny M. Leung (dannymleung@ucla.edu)

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30 **Section S1. Converting the volumetric soil moisture to the gravimetric soil moisture.**

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32 The conversion from volumetric to gravimetric soil moisture is documented in many papers, such
33 as in Oleson et al. (2013). We followed Kok et al. (2014b) and adopted a globally constant soil
34 particle density of $\rho_p = 2650 \text{ kg m}^{-3}$. Then we used the MERRA-2 global soil porosity (poros,
35 φ , Fig. S1b) to yield the bulk density of soil ρ_b :

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$$\rho_b = \rho_p(1 - \varphi) \tag{S1}$$

37 Then, using the water density of $\rho_w = 1000 \text{ kg m}^{-3}$, we converted the MERRA-2 volumetric soil
38 moisture (SFMC, θ , $\text{m}^3 \text{ water} / \text{m}^3 \text{ soil}$, Fig. S1a) to gravimetric moisture w (kg water / kg soil,
39 Fig. S1c):

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$$w = \frac{\rho_w}{\rho_b} \theta \tag{S2}$$

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50 **Section S2. A discussion on other approaches of combining rock and vegetation drag**
51 **partition effects**

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53 To our knowledge only a few approaches explicitly proposed to represent both rock and
54 vegetation roughness in one drag partition scheme, but they all have different limitations. The first
55 approach was proposed by Darменова et al. (2009) and subsequently modified by Foroutan et al.
56 (2017): They assumed rock λ for different land types (e.g., Table 2 in Darменова et al., 2009),
57 and combined rock λ with vegetation λ (from Eq. 9b) using Darменова’s double drag partition
58 equation (see Eq. 5 in Foroutan et al., 2017). The second approach was also proposed by
59 Darменова et al. (2009): They provided measured rock z_{0a} and vegetation z_{0a} for different land
60 types (Table 1 in Darменова et al., 2009), determined the dominant land type (bare or vegetated)
61 for each grid, and then applied M&B95 to calculate drag partitioning. The third approach was
62 proposed by Klose et al. (2021): They provided a relation between vegetation λ , h , and z_{0a} , plus
63 a relation between vegetation height h and LAI, and thus derived the vegetation roughness length
64 z_{0a} as a function of LAI. They then used Prigent et al. (2012) satellite measurements of z_{0a} (time-
65 invariant, static, mostly representing rocks), and took the larger z_{0a} between Prigent’s static z_{0a}
66 and their dynamic vegetation z_{0a} . They finally used M&B95 to calculate drag partitioning with
67 z_{0a} . All three approaches tried to represent both rock and vegetation roughness using either z_{0a} or
68 λ , which was problematic because rocks are better measured in z_{0a} by satellites and plants are
69 better parameterized in λ . For example, globally gridded rock λ was not available and thus the first
70 and second approaches needed to assign λ for rocks as a function of land type, which can be
71 inaccurate and highly uncertain because λ also depends on other factors apart from the land type.
72 On the other hand, the second and the third approaches assumed one dominant land type and used
73 one single (either rock or vegetation) z_{0a} to represent the whole grid, but ignored the fact that a
74 grid can be partly covered by plants and partly by rocks, which was only accounted for by the first
75 approach (the double drag partition equation is a function of rock λ , plant λ , and f_v). Note that the
76 second and the third approaches had to choose either rock or plant z_{0a} because adding up the rock
77 z_{0a} and plant z_{0a} is not allowed (z_0 is not additive, whereas λ is additive). The same problem
78 would not occur if there were global scale observations of rock roughness measured in density λ ,
79 which could either be directly applied to the double drag partition equation in Darменова et al.
80 (2009) or be added upon plant λ and then converted to z_{0a} in Klose et al. (2021). All in all, due to
81 insufficient and inadequate observations, all the aforementioned approaches struggle to accurately
82 represent the combined effect of vegetation and rocks on the drag partition and dust emission. In
83 Sect. 3.2, we will propose a novel approach that incorporates both roughness of rocks and plants
84 and equally respects the z_{0a} and λ from both schools of drag partition parameterizations,
85 quantifying the drag partitions of rocks and plants into one hybrid drag partition factor F_{eff} .

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90 **Section S3. Description of the Comola et al. (2019) intermittency scheme coupled with Kok**
 91 **et al. (2014b) dust emission equation**

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93 In the C19 scheme, the dust emission flux F_d is calculated using the impact threshold (u_{*it})
 94 instead of either the fluid (u_{*ft}) or a combined threshold (u_{*t}). Following the reasoning in Comola
 95 et al. (2019b), we update K14 (Eq. 7) with u_{*it} instead of u_{*t} as the threshold (see Sect. 2 for the
 96 description of K14 and dust emission thresholds):

$$97 \quad F_d = C_{tune} C_d f_{bare} f_{clay} \frac{\rho_a (u_{*s}^2 - u_{*it}^2)}{u_{*it}} \left(\frac{u_{*s}}{u_{*it}} \right)^{\frac{C\alpha(u_{*st} - u_{*st0})}{u_{*st0}}} \quad \text{for } u_{*s} > u_{*it} \quad (S3a)$$

98 where $u_{*st} = u_{*ft} \sqrt{\rho_a / \rho_{a0}}$ is the same standardized fluid threshold as in the default K14 scheme.
 99 Because $u_{*it} < u_{*ft}$, this modified equation accounts for more small dust fluxes that occur due to
 100 turbulent winds intermittently driving transport even when $u_* < u_{*ft}$. These fluxes are important
 101 over marginal source regions for which emissions are otherwise missed by employing u_{*ft} as the
 102 threshold (Comola et al., 2019b).

103 Next, we account for the intermittency effect on dust emissions by following C19 in
 104 introducing the intermittency factor η , which denotes the fraction of time that saltation is active in
 105 a model time step (e.g., ~ 30 mins). η corrects the horizontal sand saltation flux, but since dust
 106 emission flux scales with saltation flux (Shao et al., 1993), η is also the fraction of time that dust
 107 emission is active in a model timestep. We thus account for the effect of intermittency by
 108 multiplying the dust emission flux by η (Comola et al., 2019):

$$109 \quad F_{d,\eta} = \eta F_d \quad (S3b)$$

110 where $\eta \in [0,1]$.

111 C19 determines η using the average wind speed, wind fluctuations, and the saltation (and
 112 thus dust emission) thresholds. C19 parameterizes η using information at the typical saltation
 113 height of $z_{sal} = 0.1$ m, so we need to first define u_{ft} , u_{it} , and u_s to be u_{*ft} , u_{*it} , and u_{*s} translated
 114 to the height of z_{sal} using the log law of the wall:

$$115 \quad u_X(z_{sal}) = \frac{u_{*X}}{k} \ln \left(\frac{z_{sal}}{z_{0a}} \right) \quad (S4a)$$

116 where subscript X could be ft , it or s , $u(z_{sal})$ is the wind speed at saltation height z_{sal} , z_{0a} is the
 117 aeolian roughness length taken here as 10^{-4} m for simplicity (see Martin and Kok, 2018), and $k =$
 118 0.386 is the von Kármán constant in the atmospheric boundary layer (Andreas et al., 2006). To
 119 parameterize the effect of turbulent wind fluctuations on saltation intermittency, we further define
 120 \tilde{u} to be the instantaneous wind speed at z_{sal} , which is described by a normal distribution with a
 121 mean equal to the model time step mean u and a standard deviation $\sigma_{\tilde{u}_s}$ (Chu et al., 1996), and u_s
 122 and $\sigma_{\tilde{u}_s}$ are defined for a time interval of > 10 min. Comola et al. (2019b) then showed that the $\sigma_{\tilde{u}}$
 123 parameterization using the Monin-Obukhov similarity theory (MOST) worked well for in-situ
 124 measurements of horizontal saltation fluxes. $\sigma_{\tilde{u}}$ is height invariant and can be parameterized using
 125 MOST as (Panofsky et al., 1977):

$$126 \quad \sigma_{\tilde{u}_s} = u_{*s} \left(12 - 0.5 \frac{z_i}{L} \right)^{1/3} \quad \text{for } 12 - 0.5 \frac{z_i}{L} \geq 0 \quad (S4b)$$

127 where L is the Monin-Obukhov length and z_i is the planetary boundary layer (PBL) height. In
 128 boundary-layer meteorology, turbulence is generated by mechanical shear and buoyancy (Stull,
 129 1988). The shear-driven turbulence in a flow scales with u_{*s} , while the buoyancy-driven
 130 turbulence scales with z_i/L . According to Eq. (S4b), high-frequency wind fluctuations ($\sigma_{\tilde{u}_s}$)
 131 increase with shear ($u_{*s} > 0$) and buoyancy ($L < 0$). For larger wind fluctuations $\sigma_{\tilde{u}_s}$, it is easier

132 for \tilde{u}_s to sweep across u_{it} and shut off dust emission, leading to $\eta < 1$. As a result, the emission
 133 flux predicted by our scheme will be smaller than the other existing parameterizations for $u_s >$
 134 u_{ft} . If $u_s \gg u_{ft}$, \tilde{u}_s will be less likely to sweep across u_{it} and η will approach 1. Furthermore,
 135 when $u_{it} < u_s < u_{ft}$, η will be much smaller than one and closer to zero, leading to a small
 136 emission flux when other parameterizations predict a zero emission flux. When $u_s < u_{it}$, η could
 137 also be greater than zero when $\sigma_{\tilde{u}_s}$ is large enough so that the instantaneous \tilde{u}_s crosses through u_{it} ,
 138 but the DPM employed would not generate any emission anyway according to Eq. S3a.

139 With saltation-height variables defined, the total fraction of time η when saltation is active
 140 in a model timestep is then formulated as:

$$141 \quad \eta = 1 - P_{ft} + \alpha(P_{ft} - P_{it}) \quad (\text{S5})$$

142 where $P_{it} = P(\tilde{u}_s < u_{it})$ is the cumulative probability that the instantaneous wind \tilde{u} does not
 143 exceed the impact threshold u_{it} , and $P_{ft} = P(\tilde{u}_s < u_{ft})$ is the cumulative probability that \tilde{u}_s does
 144 not exceed the fluid threshold u_{ft} . The fluid threshold crossing fraction α is defined as the fluid
 145 threshold crossing rate C_{ft} , which is the number of times \tilde{u}_s sweeps across u_{ft} per second, divided
 146 by the total crossing rate $C_{ft} + C_{it}$, which is the number of times \tilde{u}_s sweeps across u_{ft} and u_{it} per
 147 second: $\alpha = \frac{C_{ft}}{C_{ft} + C_{it}}$. α approaches 1 when instantaneous wind \tilde{u}_s mostly crosses u_{ft} , and
 148 approaches 0 when \tilde{u} mostly crosses u_{it} . C19 showed that α is a function of u_s , $\sigma_{\tilde{u}}$, u_{it} , and u_{ft} :

$$149 \quad \alpha \approx \left[\exp\left(\frac{u_{ft}^2 - u_{it}^2 - 2u_s(u_{ft} - u_{it})}{2\sigma_{\tilde{u}_s}^2}\right) + 1 \right]^{-1} \quad (\text{S6a})$$

150 such that $\alpha \rightarrow 1$ in the limit of $u_s \gg u_{ft}$, and $\alpha \rightarrow 0$ for $u_s \rightarrow 0$ and $\sigma_{\tilde{u}_s} \rightarrow 0$. As for P_{ft} and P_{it} ,
 151 assuming a Gaussian distribution for \tilde{u} , i.e., $\tilde{u}_s \sim \mathcal{N}(u_s, \sigma_{\tilde{u}_s}^2)$, P_{ft} and P_{it} can be expressed using
 152 the error functions $\text{erf}(x)$ as:

$$153 \quad P_{ft} = \frac{1}{2} \left[1 + \text{erf}\left(\frac{u_{ft} - u_s}{\sqrt{2}\sigma_{\tilde{u}_s}}\right) \right] \quad (\text{S6b})$$

$$154 \quad P_{it} = \frac{1}{2} \left[1 + \text{erf}\left(\frac{u_{it} - u_s}{\sqrt{2}\sigma_{\tilde{u}_s}}\right) \right] \quad (\text{S6c})$$

155 Within a model timestep, dust emission is continuous for the fraction of time $1 - P_{ft}$ when
 156 $\tilde{u}_s > u_{ft}$, and for the fraction of time $P_{ft} - P_{it}$ dust emission is in the hysteresis regime ($u_{it} <$
 157 $\tilde{u}_s < u_{ft}$) where dust emission can only be active for a fraction of time α when \tilde{u}_s crossed u_{ft}
 158 more recently than u_{it} in the hysteresis regime. Using Eqs. S3–S6, we computed η from Eq. S3b,
 159 yielding the dust emission flux $F_{d,\eta}$ that accounts for the effects of intermittency.

160 We note that the C19 scheme is designed for GCMs and RCMs in RANS mode (not in LES
 161 mode), regardless of the time step used.

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164 **Section S4. Calculating the Obukhov length L from MERRA-2 meteorological fields**

165

166 MERRA-2 does not include the Obukhov length L , but outputs several variables that allows us to
167 compute L , using (Bonan, 2015; Lee and Buban, 2020):

168
$$L = -\rho_a c_p T u_*^3 / k g H, \tag{S7}$$

169 where ρ_a is air density (kg m^{-3}), c_p is the specific heat capacity of air under constant pressure (J
170 $\text{kg}^{-1} \text{K}^{-1}$), T is air temperature (in this study we chose T_{10} , which is air temperature at the height of
171 10 m), u_* is friction velocity (m s^{-1}), k is the von Kármán constant, g is gravitational acceleration
172 (m s^{-2}), and H is the sensible heat flux (W m^{-2}). MERRA-2 provides sensible heat flux (SHLAND)
173 and T_{10} (T10M), allowing us to directly compute L .

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177 **Section S5. Comparing our simulated dust emission threshold against observationally**
178 **derived Pu et al. (2020) threshold**

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180 Here we make a comparison between our simulations of dust emission thresholds and the
181 observationally based threshold estimate from Pu et al. (2020). They compared the wind speed
182 distributions from reanalyses against observationally derived DAOD distributions to obtain a
183 threshold wind speed $u_{t,Pu}$ for each gridbox (Fig. S13 below) that corresponds to a threshold
184 DAOD value (i.e., 0.5 over arid regions and 0.05 over semiarid regions), above which is defined
185 as a dust emission event.

186 In this paper, we argue that dust emission equations should employ the impact threshold
187 u_{*it} . Given that $u_{t,Pu}$ was obtained by matching DAOD distributions against the distributions of
188 wind speed u , $u_{t,Pu}$ is more relevant to the impact threshold u_{it} than the fluid threshold u_{ft} (i.e.,
189 the moisture effect is less relevant). Furthermore, Pu et al. (2020) used wind speed u at 10 m
190 instead of the soil surface wind speed $u_s (= uF_{eff})$ in the analysis, and thus $u_{t,Pu}$ captured a larger
191 threshold wind speed that included the impact threshold u_{it} as well as the drag partition effect F_{eff}
192 that inhibits saltation. To make a fair comparison, we compare here $u_{t,Pu}$ against our u_{*it} divided
193 by the drag partition factor, u_{*it}/F_{eff} , which is larger than u_{*it} . We used the log law of the wall
194 (Eq. S4a) to change u_{*it} from a velocity scale to a velocity of u_{it} at the level of $z = 10$ m, yielding
195 u_{it}/F_{eff} instead.

196 In Fig. S13, the top two panels show the Pu et al. (2020) annual mean threshold $u_{t,Pu}$ (Fig.
197 S13a) and the u_{it}/F_{eff} from our scheme (Fig. S13b). Both maps share similar spatial variability
198 and magnitudes over certain regions such as Africa and Australia. The bottom panels show the
199 bias (Fig. S13c) and ratio (Fig. S13d) of the thresholds, showing that the larger discrepancies occur
200 over East and Central Asia. For instance, over the Kyzylkum, $u_{t,Pu}$ is 4–7 m s⁻¹ higher than our
201 threshold. In general, Fig. S13c shows that, over most emission source regions, $u_{t,Pu}$ and our
202 threshold are relatively close to each other and differ by ~1–2 m s⁻¹. This comparison shows that
203 both methods derived dust emission thresholds of similar magnitudes and moderate spatial
204 consistency.

205 We note two small caveats to this comparison. First, $u_{t,Pu}$ was derived by using a DAOD
206 threshold as a proxy for defining an emission event, such that the inferred threshold depends on
207 the extent to which non-local dust is advected from upwind regions instead of emitted locally. This
208 transport effect might cause a lower $u_{t,Pu}$ in downwind regions, such as over the Sahel, as seen in
209 Fig. S13a. Therefore, the global spatial pattern of $u_{t,Pu}$ partially reflects the DAOD spatial
210 variability. Second, our u_{it}/F_{eff} (Fig.13b) is an annual mean, including those high-LAI seasons
211 when there are no dust emissions. Therefore, removing seasons with high LAI and low emissions
212 would likely yield a smaller mean u_{it}/F_{eff} over semiarid regions, which might better represent
213 the annual threshold wind speed (beyond which dust emission occurs).

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219 **Section S6. A detailed discussion of the caveats and limitations of the new dust emission**
220 **scheme**

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222 **6.1. Soil median diameter representation**

223 For our derived parameterization for the dry soil median diameter \bar{D}_p , we obtained a
224 relationship between \bar{D}_p and silt+clay fraction for non-arid regions ($LAI > 1$), and a constant of
225 $\bar{D}_{p0} = 127 \pm 47 \mu\text{m}$ for arid regions ($LAI < 1$). In theory, \bar{D}_p should be a function of soil properties
226 (Hillel, 1980) and therefore implicitly of space and time, but we obtained a simple relationship for
227 \bar{D}_p over arid regions because 1) different studies provided measurements of different soil
228 properties such that data are limited and insufficient for a more detailed statistical analysis, 2) the
229 uncertainties of the measured soil PSDs are moderately large, and 3) most \bar{D}_p measurements over
230 arid regions found \bar{D}_p within 40–250 μm (Fig. 1c), which limited the dry fluid threshold u_{*ft0} to
231 vary within the relatively small range of $\sim 0.204\text{--}0.268 \text{ m s}^{-1}$ (from Eq. 2 assuming $\rho_a =$
232 1.225 kg m^{-3}). This range is about ten times smaller than the global range of the wet fluid
233 threshold u_{*ft} ($\sim 1 \text{ m s}^{-1}$). Thus, using a single $\bar{D}_{p0} \sim 127 \mu\text{m}$ across all arid regions appears to be
234 a reasonable approach given the current data availability.

235 A number of previous studies have also compiled their global \bar{D}_p maps for calculating the
236 dust emission threshold (Laurent et al., 2008; Tegen et al., 2002; Menut et al., 2013). These studies
237 used global soil texture data (with known fractions f_a of soil components including sand, silt, and
238 clay) to determine gridded soil types using the soil texture triangle diagram (e.g.,
239 FAO/IIASA/ISRIC/ISS-CAS/JRC, 2012; Chatenet et al., 1996; Shirazi and Boersma, 1984), and
240 calculated gridded \bar{D}_p maps by combining the soil component fractions f_a with the estimated
241 aggregated particle size \bar{D}_a of the soil components by a weighted mean $\bar{D}_p = \sum_a f_a \bar{D}_a$ (Menut et
242 al., 2013). Since these \bar{D}_a values are based on measurements from Chatenet et al. (1996), these
243 studies also took into account the aggregated sizes of the individual soil components. However,
244 owing to insufficient data worldwide, these maps have not been verified against the measurements
245 of the in-situ soil PSD. On the other hand, our results based on observations suggest that the spatial
246 variability of \bar{D}_p over deserts are relatively small compared to \bar{D}_p over nonarid regions, and does
247 not significantly correlate with soil texture and soil properties (see Eq. 14). Our results thus
248 surprisingly suggest that the \bar{D}_p parameterization can reasonably be much simplified into a global
249 constant over arid regions. This approach is consistent with another current approach of employing
250 a globally constant soil particle diameter (e.g., Zender et al., 2003a; Mahowald et al., 2006) and
251 significantly different from another approach of employing a \bar{D}_p map (e.g., see Fig. S10 for the
252 input \bar{D}_p map for the CHIMERE CTM; Mailler et al., 2017; Menut, 2018; Menut et al., 2021).
253 Furthermore, the \bar{D}_p measurements showed a positive relationship with the silt+clay fraction
254 $f_{\text{silt+clay}}$ over the non-arid regions, which we attributed to the increasing cohesion between soil
255 particles with the increasing silt+clay content. This is different from the negative $\bar{D}_p - f_{\text{silt+clay}}$
256 relationship assumed by most past studies (Tegen et al., 2002; Laurent et al., 2008; Menut et al.,
257 2013) as they assumed that \bar{D}_p increased with sand content ($f_{\text{sand}} = 1 - f_{\text{silt+clay}}$). We argue that
258 our $\bar{D}_p - f_{\text{silt+clay}}$ relationships are based on observations and should thus represent an
259 improvement over the past assumed \bar{D}_p -texture relationships. We anticipate that as more
260 measurements emerge in the future, more statistical or machine learning modeling approaches can

261 more robustly decipher the intricate relationships between the aggregated \bar{D}_p and the soil
262 properties in order to further improve the representation of the global \bar{D}_p map.

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265 **6.2. Hybrid drag partition scheme**

266 For our drag partition scheme, we combined the drag partition for rocks ($f_{eff,r}$) from the
267 Marticorena and Bergametti (1995) scheme with the drag partition for vegetation ($f_{eff,v}$) from the
268 Okin (2008) scheme using a weighted mean approach employing the land cover fractions of rocks
269 and vegetation, which is a novel approach. Nonetheless, our scheme still contains several major
270 limitations. First and foremost, we calculate the rock $f_{eff,r}$ using the Prigent et al. (2005) aeolian
271 roughness length data derived from the ERS microwave sensor, but we could not completely
272 separate rock roughness from vegetation roughness in the dataset. Marticorena et al. (2006) argued
273 that ERS sensor measurements has relative small local incident angles such that the contribution
274 from vegetation roughness is relatively small compared to the contribution from rock roughness.
275 We also removed as much vegetation influence as possible on z_{0a} by taking the minimum z_{0a} out
276 of the 12 available monthly data for all grids, but it is still possible that a small fraction of
277 vegetation roughness remains. Thus, our approach of combining the time-invariant Pr05 z_{0a} (and
278 $f_{eff,r}$) with the time-varying $f_{eff,v}$ will probably result in a small degree of double-counting of
279 vegetation roughness in our drag partition scheme. We also note that the Pr05 data used the
280 microwave backscatter coefficient as a proxy for inferring z_{0a} , but it does not perfectly correlate
281 with the z_{0a} measured by the ground sites, and so there will be some corresponding errors in the
282 Pr05 z_{0a} used in our drag partition scheme.

283 Second, the land cover fraction areas used are obtained from the ESA CCI dataset in our
284 drag partition scheme, which are annual mean and thus not season-dependent. The land cover of
285 vegetation A_v in Eq. 21b should also be a function of time mainly because of the seasonally
286 changing vegetation cover. However, most current land cover datasets provide annual data but not
287 seasonal data, and thus A_r and A_v in Eq. 21b are only spatially varying within the year 2006.
288 Furthermore, most land cover datasets only provide near-term land cover data (the farthest data
289 goes back to the year 850; e.g., Klein Goldewijk et al., 2017). ESA CCI has a temporal coverage
290 of 1992–2019, and so the dataset will represent relatively well for present-day scenarios but
291 become less representative of paleoclimatological scenarios, for which the vegetation distributions
292 differ from that in the present day, such as during the Green Sahara > 6000 years ago (Kutzbach
293 et al., 1996; Bonan, 2015).

294 A third limitation of our new drag partition scheme is that the Okin (2008) drag partition
295 scheme requires the vegetation cover fraction f_v as a proxy for vegetation density. In this study,
296 we proposed $LAI \sim f_v = 1 - f_{bare}$ as discussed in Eq. 18b. Since LSMs do not have accurate
297 simulations of f_v , there are only preliminary equations for calculating the bare and vegetated
298 fractions proposed by previous papers (e.g., Mahowald et al., 2006; see discussions in Eq. 11 and
299 Eq. 18b). However, Eq. 11 (and thus $f_v \sim LAI$) only applies to regions with low LAI because
300 leaves are mostly not overlapped; over regions with higher LAI, leaves start to overlap and $LAI >$
301 f_v . Thus, this assumption could overestimate f_v and thus $f_{eff,v}$, thereby underestimating dust
302 emissions over vegetated regions (e.g., underestimations over western U.S. deserts in Fig. 7e).
303 Thus, LSMs need a more accurate parameterization of f_v to get a more accurate vegetation drag
304 partition effect regardless of whether the Okin (2008) or the Raupach et al. (1993) scheme is used.
305 Alternatively, LSMs could also read in observed f_v from available satellite-derived products such

306 as MODIS or AVHRR f_v , as done by Wu et al. (2016) for instance. We used the observed/modeled
307 LAI instead of observed f_v , because LSMs actively simulate LAI, allowing the scheme to be used
308 in past and future climates when vegetation cover observations are not available.

309 A fourth important limitation is that O08 does not fundamentally distinguish the drag
310 partitioning between different plant functional types (PFTs). O08 assumes that all short plants are
311 hemispheric in shape and produce the same $f_{eff,v}$ if they have the same f_v or LAI. In reality, short
312 plants such as shrubs, herbaceous plants, and crops have vastly different shapes; some are far from
313 hemispheric and can hardly be approximated by a simple geometry or shape. Nonetheless, this
314 limitation is not unique to O08 but shared by other drag partition schemes such as Raupach et al.
315 (1993), as their $f_{eff,v}$ equations are also functions of f_v only and not functions of PFTs. More
316 research is thus warranted in the future to better quantify the plant shapes and $f_{eff,v}$ of different
317 PFTs.

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320 **6.3. Dust emission intermittency scheme**

321 There are two important caveats about the Comola et al. (2019b) intermittency scheme.
322 The first caveat is that it has exponential dependences on u_{*s} , $\sigma_{\tilde{u}_s}$, u_{*it} , and u_{*ft} (see Sect. S3) and
323 is thus very sensitive and vulnerable to the accuracy of the GCM simulations of the four variables.
324 For instance, if the thresholds are overestimated by the threshold schemes, not only will emissions
325 be underestimated but η from C19 will also be close to zero and further worsen the low bias of the
326 dust emissions. Therefore, a prerequisite of employing the C19 scheme is that the wind u_{*s} and
327 the thresholds should be adequately simulated and have reasonable ranges of variability throughout
328 the year. If simulated well, η will have reasonable day-to-day and seasonal fluctuations. Otherwise,
329 η can constantly fall on one or zero and become unindicative of the boundary-layer dynamics
330 temporal variability, and the resulting η time series will further impact and worsen the temporal
331 variability of the $F_{d,\eta}$ time series.

332 There is a second caveat about a technical flaw in C19. When $u_{*s} < u_{*it}$ in a time step,
333 while Comola's theory allows turbulence to generate instantaneous winds \tilde{u}_s that exceed the
334 impact and fluid thresholds and generate some emissions (even when the averaged $u_{*s} < u_{*it}$
335 across the model timestep), the setup in Eq. S3 by nature could not allow emissions when $u_{*s} <$
336 u_{*it} . C19 allows $\eta > 0$ (per Eq. S5) when $u_{*s} < u_{*it}$. However, the way C19 was parameterized
337 was such that C19 still depends on conventional dust emission equations such as Kok et al. (2014b)
338 or Zender et al. (2003a), which by nature prohibit emissions when the mean $u_{*s} < u_{*it}$ within a
339 model time step (Eq. S3). This means that the C19 theory and the C19 dust emission
340 parameterization contain an internal logical inconsistency, and the C19 scheme per se still does
341 not generate emissions $F_{d,\eta}$ (Eq. S3b) for $u_{*s} < u_{*it}$ ($\eta > 0$ per Eq. S5, but $F_{d,\eta} = \eta F_d = 0$ since
342 $F_d = 0$ per Eq. S3). But, because the turbulent emissions in the $u_{*s} < u_{*it}$ regime is small, the
343 C19 formulation is still a good approximation for turbulent emissions, performing much better
344 than the conventional timestep-constant models as demonstrated in Comola et al. (2019b).

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348 **6.4 Reducing the grid scale-dependence of dust emission simulations**

349 We produced the correction maps to scale the spatial variability of the low-resolution dust
350 emission simulations, matching the spatial variability of the high-resolution emissions (Fig. 9) to

351 reduce the scale-dependence of dust emission simulations. As such, it is an alternative to the
352 computationally expensive but more fundamental solution of simulating dust emissions in the
353 highest model resolution possible and then regrid to coarser resolution. Employing the scaling map
354 \tilde{K}_c is different from the fundamental solution in the sense that the maps in Fig. 9 are time-
355 independent and derived by matching the annual total high-resolution emissions (Sect. 4.2). As
356 seen in Fig. S10, the scaling map exhibits a moderate degree of seasonality, but employing an
357 annual scaling map like Fig. 9 will already address a large part of the scale-dependence problem.
358 We suggest GCMs and CTMs, which focus on present-day simulations, perform multiyear
359 simulations in both high and native grid resolutions to obtain monthly climatological maps of
360 scaling factors for present-day dust emission simulations. Afterwards, ESMs only need to read in
361 the climatological monthly scaling maps to rescale the native grid dust emissions every month
362 before passing the dust emissions to the atmospheric model component. If desired, instead of
363 generating climatological maps, models can even choose to obtain transient (e.g., monthly) \tilde{K}_c
364 maps as a time series for the past decades of the historical period (e.g., 1980–2020) so that the
365 scaling maps contain a much better temporal variability in terms of seasonality, interannual and
366 decadal variability, of the historical dust emissions than compared with the climatological scaling
367 maps.

368 Our proposed approach is an alternative to a more common approach, which is to employ
369 a Weibull distribution to the GCM winds (Cakmur et al., 2004; Grini et al., 2005; Cowie et al.,
370 2015; Zhang et al., 2016; Menut, 2018; Tai et al., 2021). In the Weibull approach, in each time
371 step the model assumes a Weibull PDF for each grid that is characterized by the modeled mean
372 wind speed and a shape parameter k representing the subgrid wind variability. k could be a global
373 constant (e.g., $k = 4$ in Menut, 2018), a parameterized function of the model mean wind speed (e.g.,
374 Grini et al., 2005), or a globally gridded map obtained by comparing coarse winds against high-
375 resolution winds (Ridley et al., 2013; Tai et al., 2021). A distinction between our approach and the
376 Weibull approach is that while previous studies derived the shape parameter by comparing high-
377 and low-resolution winds (e.g., Tai et al., 2021), we directly make use of the high- and low-
378 resolution input fields to calculate dust emissions (Figs. 8c and d) and then compare between the
379 high- and low-resolution emissions. Therefore, the correction map \tilde{K}_c (Fig. 9) captures subgrid
380 wind variability due to subgrid spatial characteristics just like k in the Weibull approach, and thus
381 we anticipate some intrinsic spatial correlations between the \tilde{K}_c and k maps.

382 However, there are three distinctions and advantages of our approach over the Weibull
383 approach. The first and the most important one is that our approach accounts for not only the
384 subgrid variability of wind but all other fields (u_{*s} , w , LAI, etc). \tilde{K}_c is obtained via comparing
385 emissions across resolutions and thus its magnitude is a result of the subgrid variability of all input
386 fields, whereas in Tai et al. (2021) the k is obtained via comparing winds across resolutions and
387 thus only captures subgrid wind variability. The second advantage is that our approach makes no
388 assumption about the distributions of the subgrid variability of forcings. The Weibull approach is
389 a parametric statistical method, which means the dust models need to assume the subgrid winds
390 follow a Weibull distribution, but the subgrid spatial wind variability can deviate substantially
391 from a Weibull distribution due to several reasons, such as complex terrain (Jiménez et al., 2011).
392 Our method is non-parametric and thus more robust in capturing subgrid variability of multiple
393 input fields at once. The third advantage is that our approach saves computational cost because it
394 only needs to (1) find the \tilde{K}_c map and (2) directly apply \tilde{K}_c to correct the coarse emissions.
395 Meanwhile, past studies needed to (1) find the k map, (2) iteratively calculate emissions by
396 looping across the Weibull PDF (3) sum across the PDF to yield the total emission, and (4) update

397 the Weibull PDF for each grid and time step. Repeating step (2) for all times and grids is
398 computationally very expensive.

399 There is yet another alternative approach to account for subgrid variability of winds and
400 other parameters. Some CTM studies (e.g., Meng et al., 2021) proposed to simulate dust emissions
401 at the highest resolution possible and then store the results as a gridded emission inventory. Meng
402 et al. (2021) proposed that CTMs do not need to simulate dust emissions and instead only need to
403 regrid the stored gridded dust emissions to the desired grid resolutions. An advantage of their
404 approach is clearly that their regridded dust emissions will have the correct spatial and temporal
405 correlations with their high-resolution dust emission inventory, which means there will be no grid
406 scale-dependence problem in their approach. Their approach also saves time and computational
407 resources because they do not simulate but just read in and regrid dust emissions. This approach
408 is particularly favorable for the CTM simulations for air quality forecasts and hindcasts in which
409 models need to ensure the near-term input meteorological fields are very accurate to generate an
410 accurate dust emission inventory, such as the air quality forecasts conducted by the Environmental
411 Protection Agency (EPA) using CMAQ (Appel et al., 2013, 2017), or other CTM studies such as
412 GEOS-Chem (Zhang et al., 2013; Meng et al., 2021). However, for GCMs/ESMs that care about
413 long-term simulations and aerosol–climate interactions, there is a need to actively simulate dust
414 emissions and allow a full coupling between meteorology and dust, which could not be achieved
415 by feeding the models with an inventory. In that case, our scaling method is likely more desirable
416 for GCMs and ESMs to reduce the scale-dependence problem.

417 Also, we note that although our approach alleviated the grid-scale dependence of dust
418 emissions, the grid-scale dependence problem also appears in other component of dust cycle
419 simulations, such as in dust transport. The grid-scale dependence can be due to not just the
420 averaging problem but also other problems, such as numerical diffusion which worsens with
421 increasing grid size in an Eulerian GCM (Rastigejev et al., 2010; Eastham and Jacob, 2017; Zhuang
422 et al., 2018). It has to be solved in the atmospheric model component such as by some adaptive
423 mesh refinement approaches (e.g., Semakin and Rastigejev, 2016) or machine learning methods
424 (e.g., Zhuang et al., 2021).

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426 Table S1. Past studies employed in this paper that collected dry soil aggregate size distributions
 427 over different countries.

Study	Number of samples we used	Location of the sites	Aridity ^a
Ciric et al. (2012)	5	Pannonian Basin, Serbia	nonarid
Li et al. (2014)	4	Tarim Basin	arid
Wagner et al. (1992)	2	Kansas	arid
Chandler et al. (2004)	3	Columbia Plateau	arid
Mei et al. (2004)	4	Northern China	arid
Swet and Katra (2016)	2	Negev, Israel	arid
Mirzamostafa et al. (1998)	2	Kansas	nonarid
Liu et al. (1998)	3	Inner Mongolian Plateau & Tengger Desert, China	arid
Kalhor et al. (2017)	6	Loess Plateau	nonarid
Su et al. (2007)	4	Hexi Corridor	arid
Udom and Ogunwole (2015)	4	Port Harcourt, Nigeria	nonarid
Malobane et al. (2019)	2	University of Fort Hare	nonarid
Klose et al. (2017)	5	New Mexico	arid
Shao et al. (2011)	1	Victoria, Australia	arid

428 ^aThe aridity of the sampling site was classified by this study based on whether the annual mean MERRA-2 LAI (see Fig. 3a in
 429 the main text) is smaller or larger than 1.

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Table S2. The global total redistributions in the normalized emissions from each modification.

	Using $\bar{D}_p = 127 \mu\text{m}^a$	Including F_{eff}^b	Including the intermittency ^c	Our scheme compared with K14 ^d
Arid	216 Tg yr ⁻¹	3257 Tg yr ⁻¹	3075 Tg yr ⁻¹	3663 Tg yr ⁻¹
Nonarid	34 Tg yr ⁻¹	354 Tg yr ⁻¹	87 Tg yr ⁻¹	395 Tg yr ⁻¹
Globe	250 Tg yr ⁻¹	3611 Tg yr ⁻¹	3163 Tg yr ⁻¹	4058 Tg yr ⁻¹

436 ^aNormalized Expt. II minus normalized Expt. I (Fig. S7a).
 437 ^bNormalized Expt. III minus normalized Expt. II (Fig. S7b).
 438 ^cNormalized Expt. V minus normalized Expt. III (Fig. S7e).
 439 ^dNormalized Expt. V minus normalized Expt. I (Fig. S7f).

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Table S3. The global total emissions all simulations schemes and their contributions from arid and nonarid regions.

	Original emissions	Normalized emissions	% of emissions from arid regions	% of emissions of nonarid regions
K14	29254 Tg yr ⁻¹	5000 Tg yr ⁻¹	92.1 %	7.9 %
Our scheme	11494 Tg yr ⁻¹	5000 Tg yr ⁻¹	97.8 %	2.2 %
MERRA-2	1561 Tg yr ⁻¹	5000 Tg yr ⁻¹	97.3 %	2.7 %
Z03-Z	424 Tg yr ⁻¹	5000 Tg yr ⁻¹	100 %	0 %
Z03-G	442 Tg yr ⁻¹	5000 Tg yr ⁻¹	100 %	0 %

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Table S4. Regional contributions of dust emissions to the global total emission for different schemes. ^{a, b}

	DustCOM M & B16 ^c	K14	Our scheme	Z03-Z	Z03-G	MERRA-2
NW Africa	18 %	10.4 %	14.4 %	7.5 %	23.2 %	20.1 %
NE Africa	16 %	17.5 %	14.5 %	13.3 %	17.9 %	17.1 %
Sahel	13 %	17.4 %	15.9 %	20.8 %	16.5 %	21.5 %
Middle East / C Asia	29 %	29.4 %	30.6 %	32.5 %	31.3 %	29.2 %
E Asia	13 %	4.1 %	11.9 %	14.3 %	4.0 %	6.5 %
N America	3 %	1.8 %	1.1 %	0.1 %	0.02 %	0.5 %
Australia	3 %	10.8 %	6.4 %	9.7 %	6.8 %	2.6 %
S America	4 %	2.3 %	2.2 %	0.5 %	0.07 %	1.7 %
S Africa	2 %	6.3 %	3.0 %	1.4 %	0.3 %	0.7 %
high-lat (w/ Patagonia)	5 % (from B16)	2.8 %	6.3 %	0.2 %	0.2 %	1.7 %

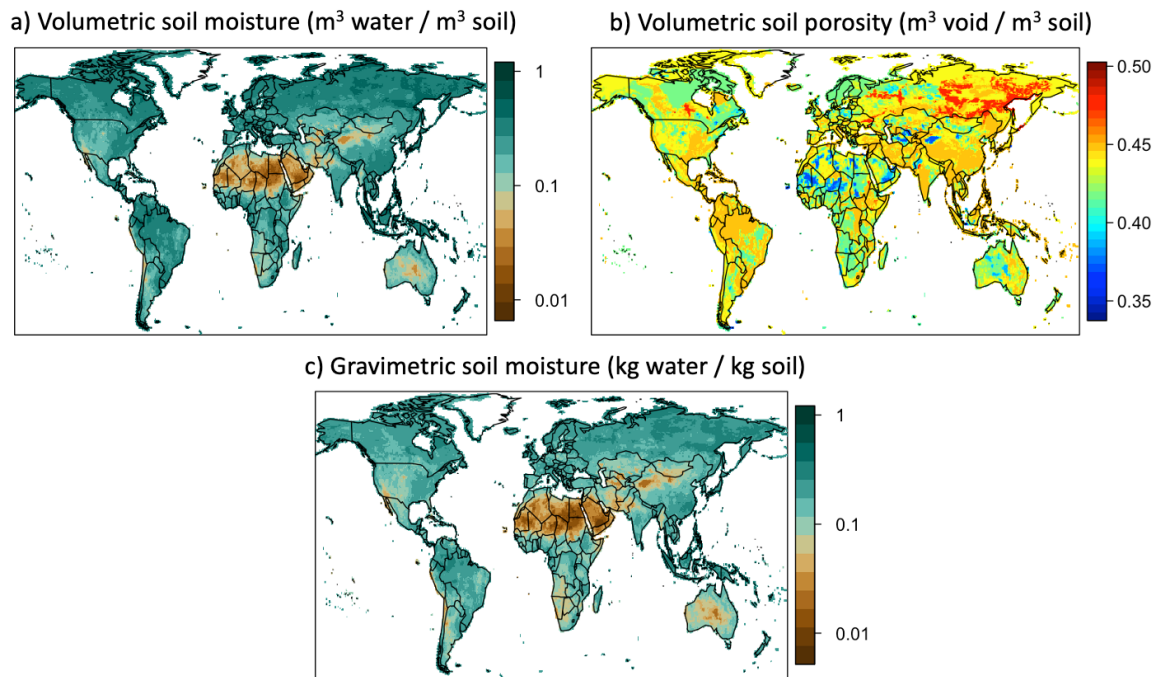
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^aAll percentages from MERRA-2 and our simulations are rounded to 1 decimal place, except for smaller values where we rounded to 2 decimal places.

^bBullard et al. (2016) obtained 5 % including Patagonia emissions, which overlaps with the S. America domain defined in Kok et al. (2021a, b). We present the percentage here assuming the nine K21 source regions sum up to be 100 %, since K21 (DustCOMM) predicted zero emissions outside of the domains (including B16 will yield 105 %). We arrange the other columns the same way such that the percentages from the nine K21 regions sum up to 100 % also.

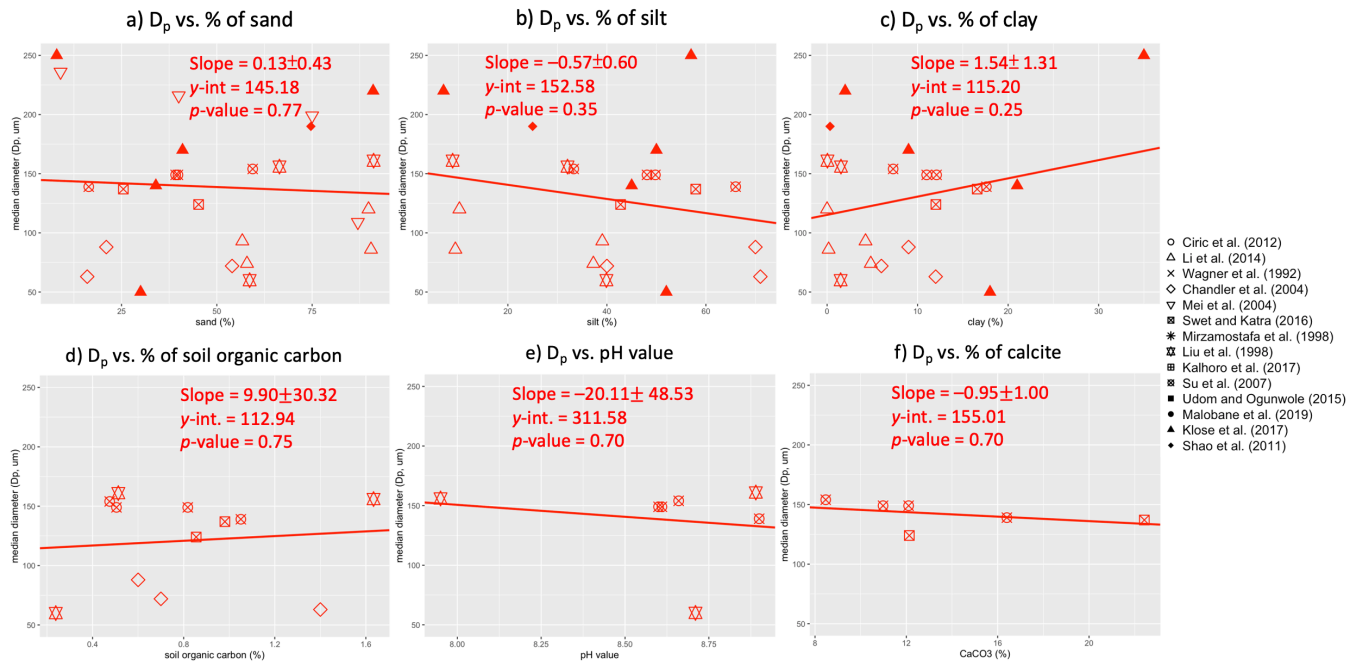
^cValues are directly obtained from Table 2 of Kok et al. (2021b), which were rounded up to integers, except for high-latitude emissions that are obtained from Bullard et al. (2016).

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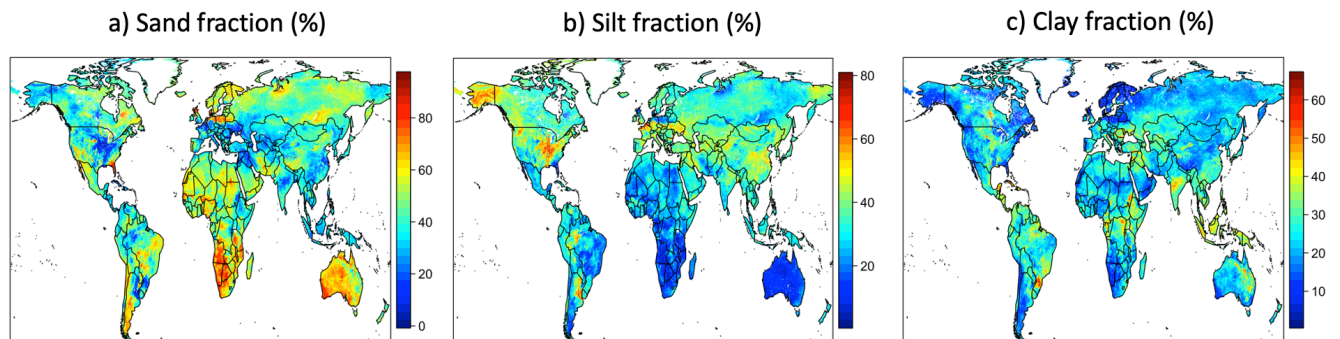
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Figure S1. MERRA-2 soil moisture for the year 2006 used in this study. (a) Volumetric soil moisture ($\text{m}^3 \text{ m}^{-3}$), (b) soil porosity, and (c) gravimetric soil moisture (kg kg^{-1}).



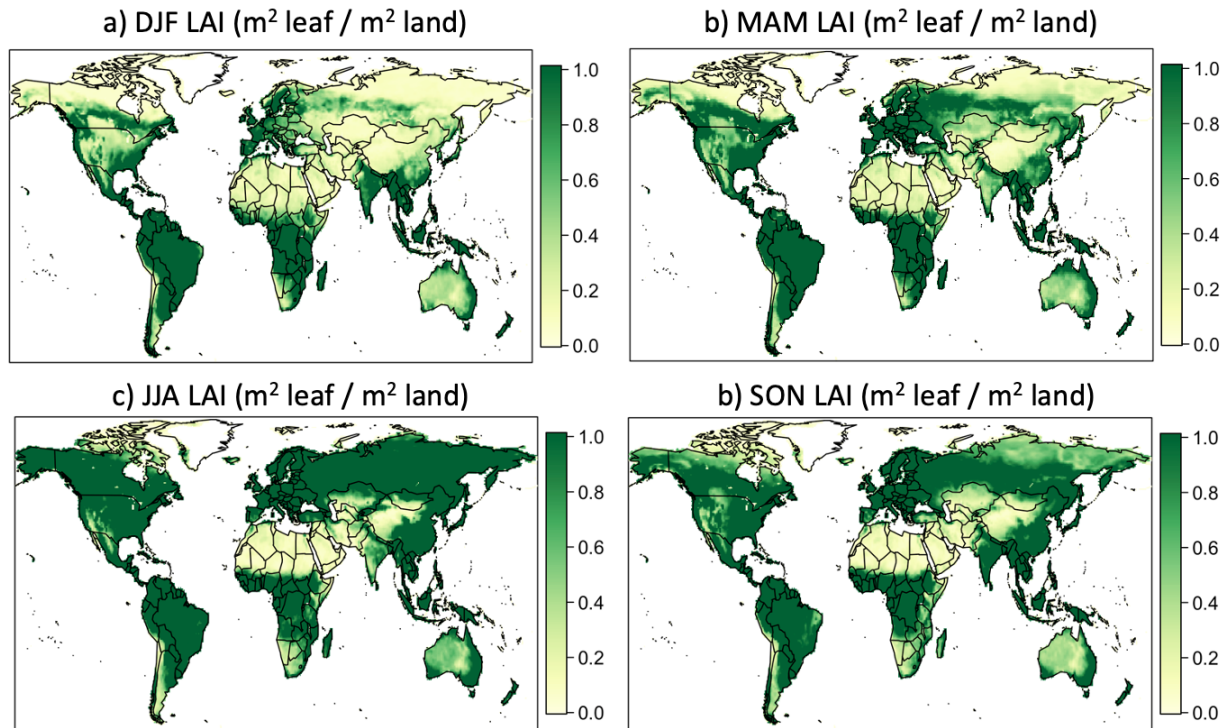
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Figure S2. The relationships between soil median diameter \bar{D}_p and soil texture and other soil properties documented in multiple past studies for arid regions. We relate D_p to content of (a) sand, (b) silt, (c) clay in %, as well as to (d) soil organic carbon (SOC) content in %, (e) pH value, and (f) % of calcite (CaCO_3). The symbols show the name of each individual study and lines denote linear regressions for which statistics are included for each panel. Studies may not have documented certain texture or properties, so some plots have fewer data points (especially for soil properties).



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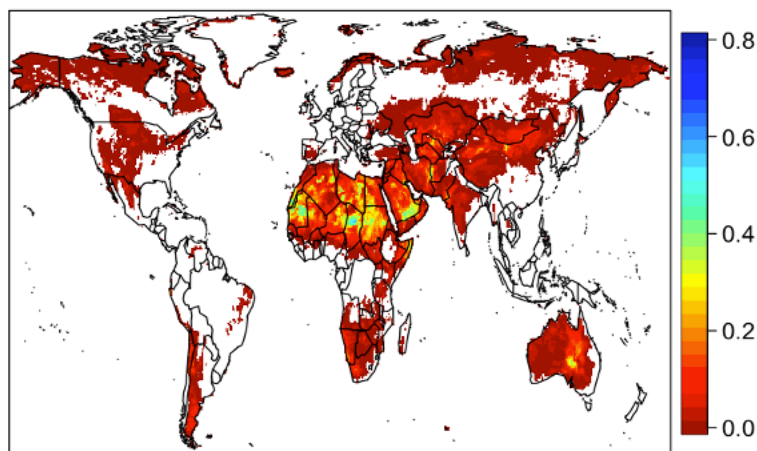
Figure S3. The SoilGrids global $0.1^\circ \times 0.1^\circ$ maps of (a) sand, (b) silt, and (c) clay in % (Hengl et al., 2017).



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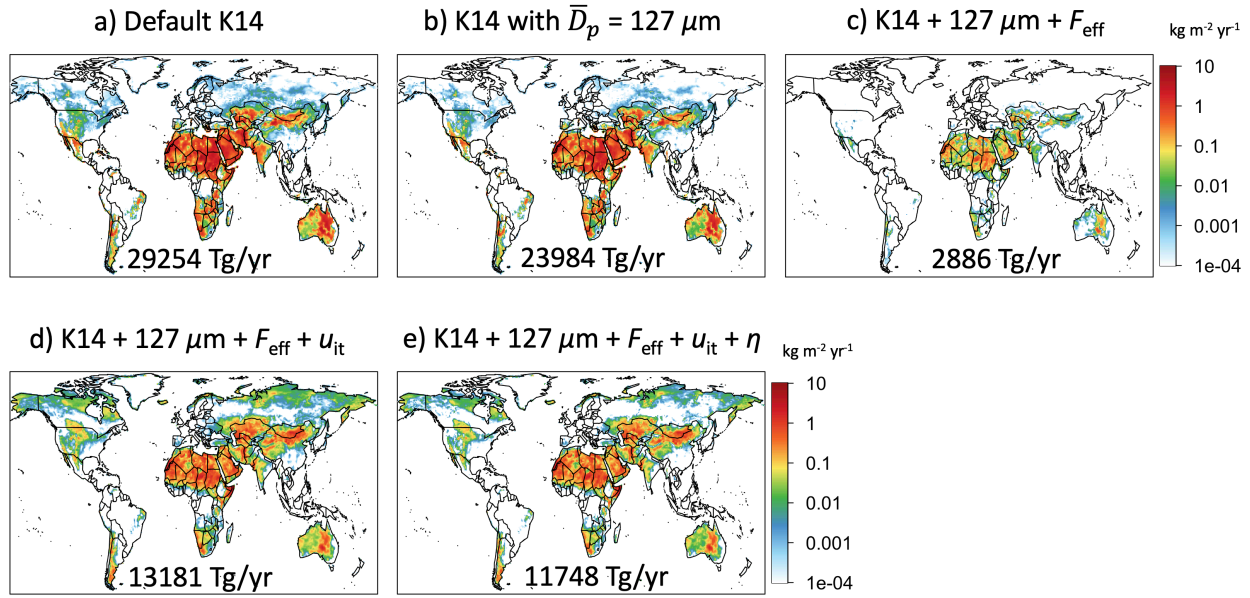
Figure S4. Global distributions of MERRA-2 seasonal mean LAI for the year 2006. Four seasonal mean LAI maps are plotted, including the (a) December–January–February, (b) March–April–May, (c) June–July–August, and (d) September–October–November. The color bar saturates at 1, so regions in dark green color have LAI > 1 and are defined as non-arid area in this study.

Annual mean η



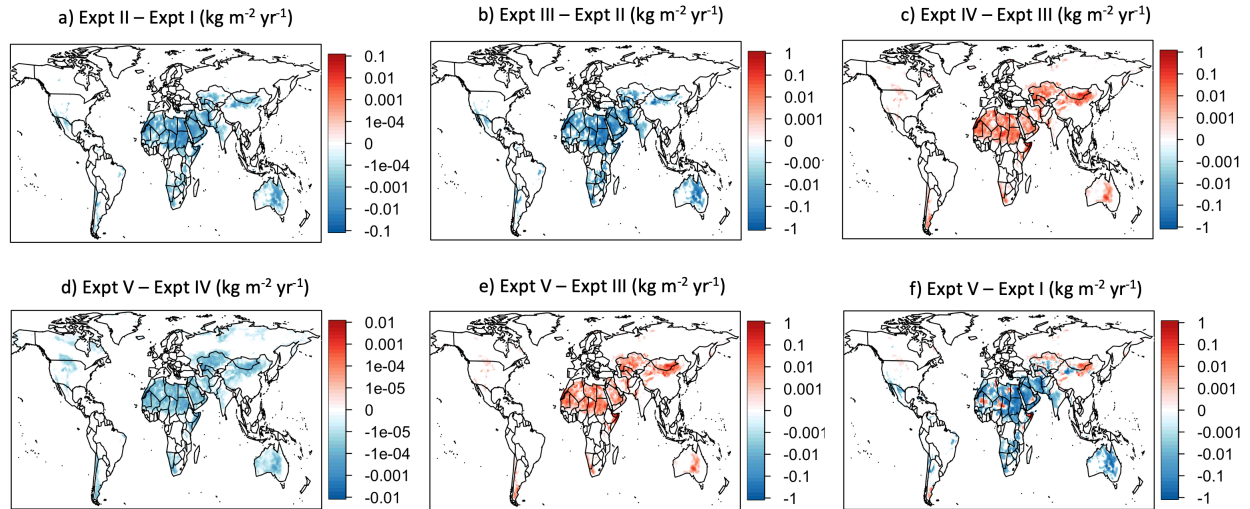
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Figure S5. The annual mean intermittency factor η , which denotes the fraction of time within a time step that emission is active, averaged over the whole year 2006.



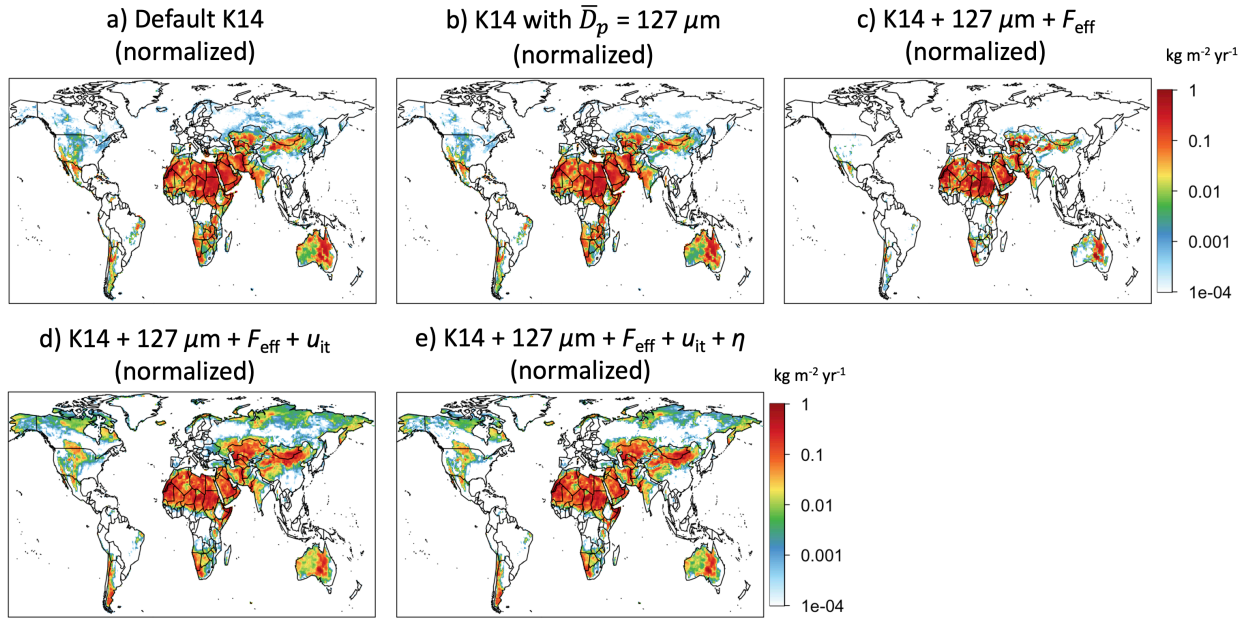
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 507 Figure S6. Spatial patterns of the unnormalized dust emission flux for each modification of the
 508 default dust emission scheme. The plots include results for the (a) default K14 scheme (expt. I),
 509 (b) K14 with changed soil particle diameter only (expt. II), (c) K14 with the new soil particle
 510 diameter and drag partition effect (expt. III), (d) K14 with the new soil particle diameter, drag
 511 partition effect, and impact threshold (expt. IV), and (e) K14 with all modifications, i.e., our new
 512 scheme (expt. V). The bottom of each panel notes the unnormalized global total emission in Tg yr⁻¹.
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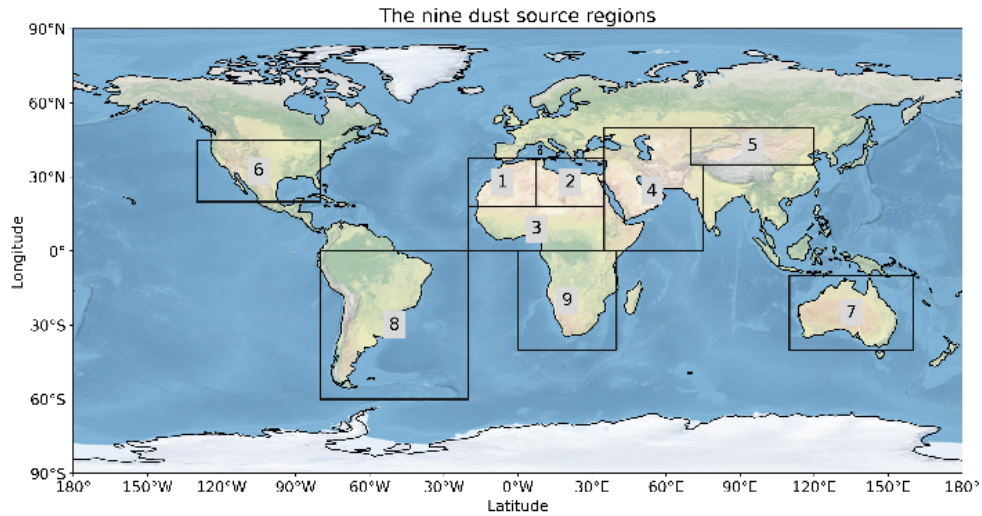
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 521 Figure S7. The effects of the proposed improvements to the parameterization of dust emissions on
 522 the default (Kok et al., 2014a, b) dust emission scheme. Maps of unnormalized emission
 523 differences with individual improvements added on top of the default K14 scheme. The individual
 524 improvements are respectively (a) changing the soil median diameter to $127 \mu\text{m}$ (expt. II), (b)
 525 including the drag partition effect (expt. III), (c) employing the impact threshold, (d) applying the
 526 intermittency factor, and (e) including the Comola et al. (2019b) intermittency scheme, a
 527 combination of (c, d). (f) Maps of unnormalized emission differences between our new scheme
 528 and the K14 scheme. The color bars of the maps of differences are drawn to \log_{10} scale.

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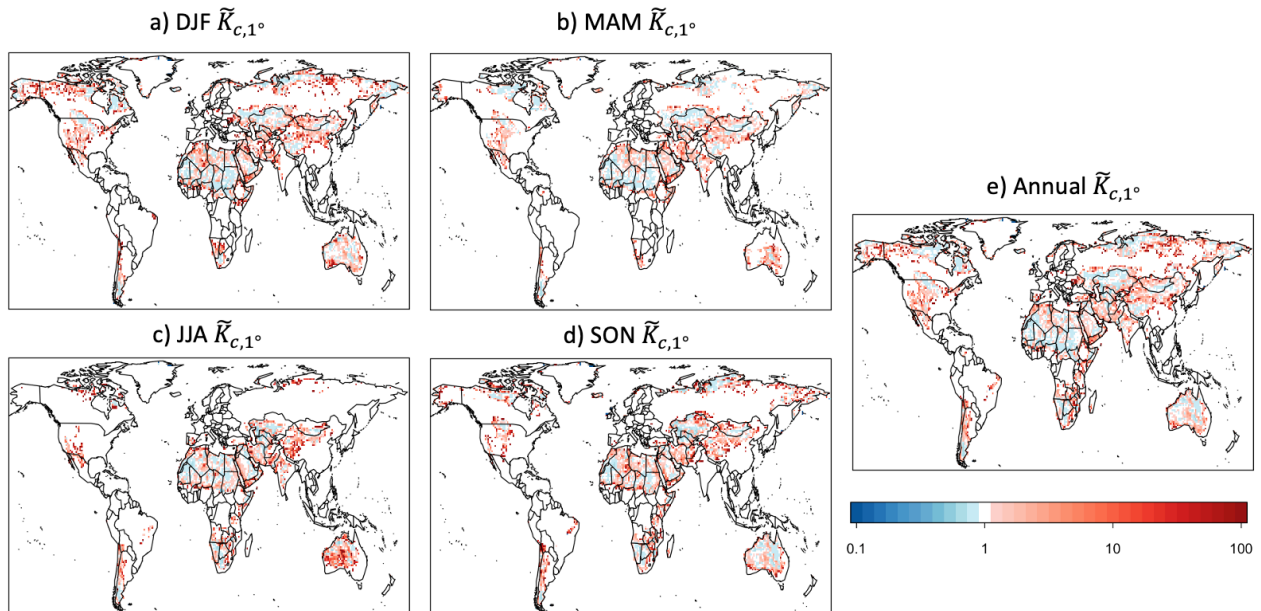
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 538 Figure S8. Spatial patterns of the normalized dust emission flux for each modification of the default
 539 dust emission scheme (same as Figure S6 but normalized). The plots include results for the (a)
 540 default K14 scheme (expt. I), (b) K14 with changed soil particle diameter only (expt. II), (c) K14
 541 with the new soil particle diameter and drag partition effect (expt. III), (d) K14 with the new soil
 542 particle diameter, drag partition effect, and impact threshold (expt. IV), and (e) K14 with all
 543 modifications, i.e., our new scheme (expt. V). All plots are normalized to have a global total
 544 emission of 5000 Tg yr^{-1} .

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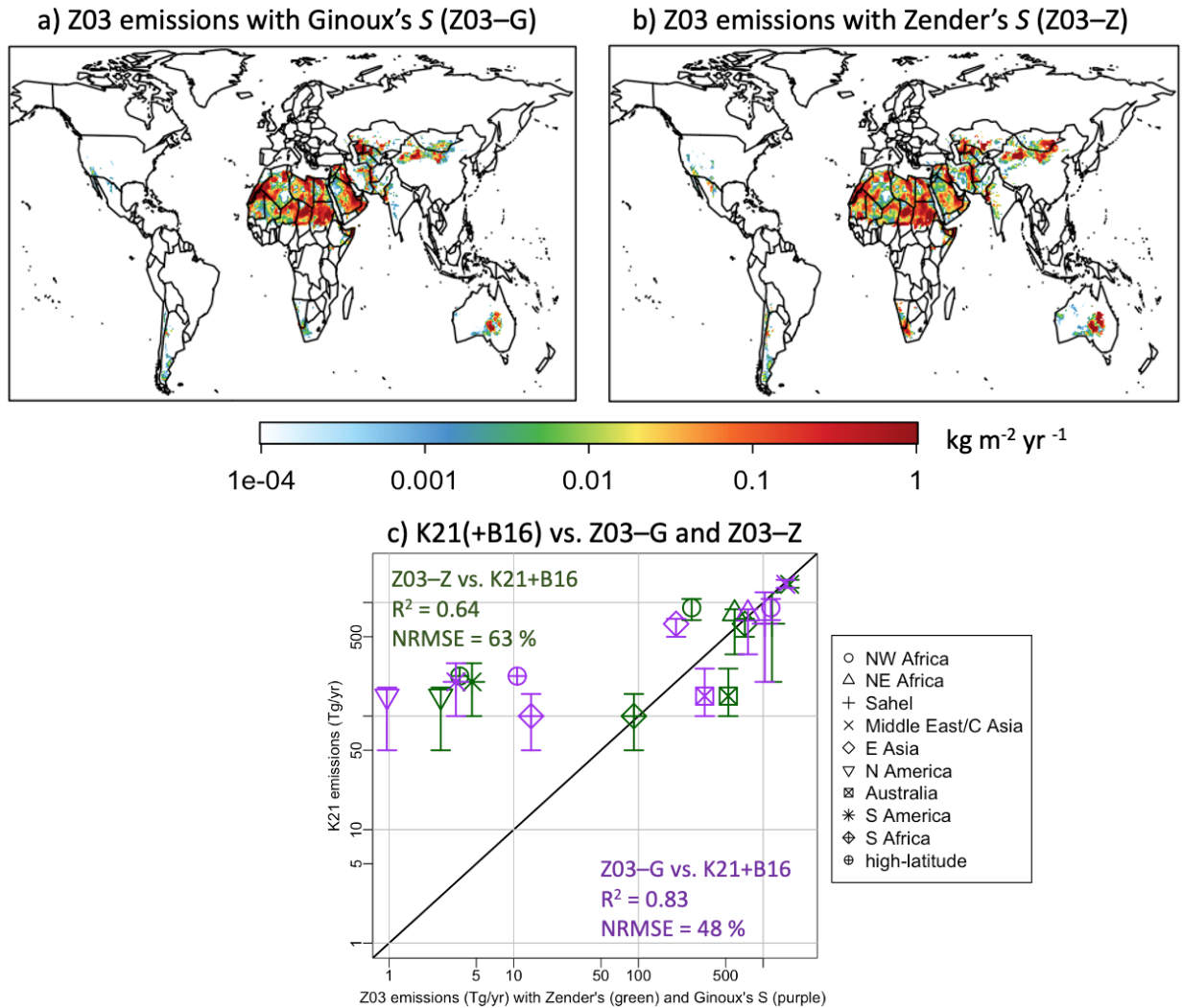


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 552 Figure S9. Coordinates of the nine main dust source regions in Kok et al. (2021a) adapted in this
 553 study. The coordinates of the nine source regions are: (1) western North Africa (20°W – 7.5°E;
 554 18°N – 37.5°N), (2) eastern North Africa (7.5°E – 35°E; 18°N – 37.5°N), (3) the Sahel (20°W –
 555 35°E; 0°N – 18°N), (4) Middle East / Central Asia (30°E – 70°E for 0°N – 35°N, and 30 – 75°E
 556 for 35 – 50°N), (5) East Asia (70°E – 120°E; 35°N – 50°N), (6) North America (130°W – 80°W;
 557 20°N – 45°N), (7) Australia (110°E – 160°E; 10°S – 40°S), (8) South America (80°W – 20°W;
 558 0°S – 60°S), and (9) Southern Africa (0°E – 40°E; 0°S – 40°S). The graph is adopted from (Kok
 559 et al., 2021a).

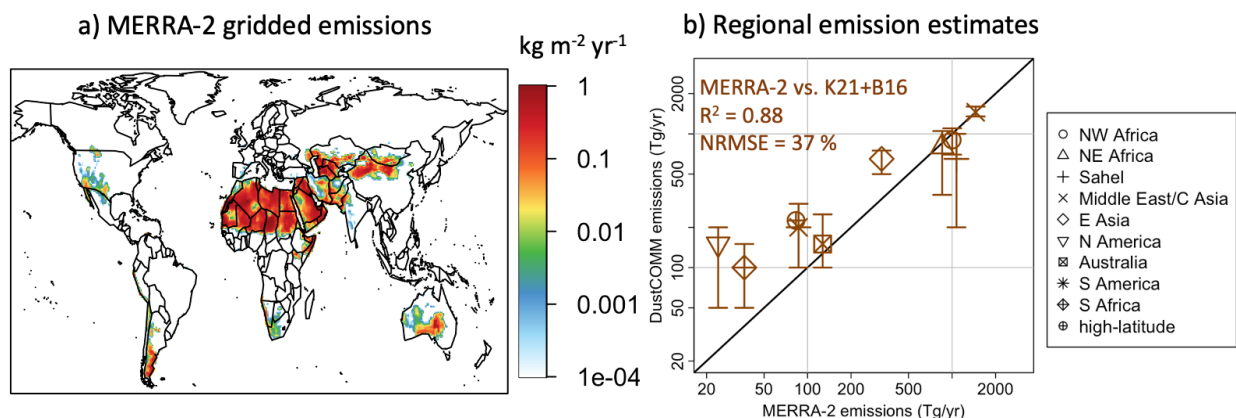
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 565 Figure S10. Seasonal variability in the correction map \tilde{K}_c at a resolution of $0.9^\circ \times 1.25^\circ$, for (a)
 566 December–January–February, (b) March–April–May, (c) June–July–August, (d) September–
 567 October–November, and (e) the whole year.
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572 Figure S11. (Kok et al., 2021a, b) DustCOMM emissions versus the dust emission simulations
573 using the (Zender et al., 2003a) scheme with different source functions S . (a) Globally gridded
574 Zender et al. (2003a) emissions ($\text{kg m}^{-2} \text{ yr}^{-1}$) with source function S from Ginoux et al. (2001)
575 (Z03-G). (b) Globally gridded Zender et al. (2003a) emissions ($\text{kg m}^{-2} \text{ yr}^{-1}$) with source function
576 S from (Zender et al., 2003b) (Z03-Z). Both (a) and (b) panels are normalized to 5000 Tg yr^{-1}
577 annual global total emissions. (c) Kok et al. (2021a, b) DustCOMM regional emissions (obtained
578 from the fifth column of Table 1 in K21b scaled to a global total of 5000 Tg yr^{-1}) versus the regional
579 emissions computed by the Z03-G scheme and the Z03-Z scheme. The regional emissions are
580 obtained following the nine source regions in Fig. 10a, with one extra point being the “high-latitude”
581 emissions obtained from the Bullard et al. (2016) estimation. The error bars show one standard
582 error, except that the B16 high-latitude emission does not contain any error estimate. The black
583 line shows the 1:1 line.



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 590 Figure S12. Kok et al. (2021a, b) DustCOMM emissions versus the dust emission simulated by
 591 MERRA-2 (Gelaro et al., 2017). (a) Globally gridded MERRA-2 emissions (kg m⁻² yr⁻¹) using
 592 GOCART (Ginoux et al., 2001). Emissions in (a) are normalized to 5000 Tg yr⁻¹ annual global
 593 total emissions. (c) Kok et al. (2021a, b) DustCOMM regional emissions (obtained from the fifth
 594 column of Table 1 in K21b scaled to a global total of 5000 Tg yr⁻¹) versus the regional emissions
 595 simulated by MERRA-2. The regional emissions are obtained following the nine source regions
 596 in Fig. 10a, with one extra point being the “high-latitude” emissions obtained from the Bullard et
 597 al. (2016) estimation. The error bars show one standard error, except that the B16 high-latitude
 598 emission does not contain any error estimate. The black line shows the 1:1 line.

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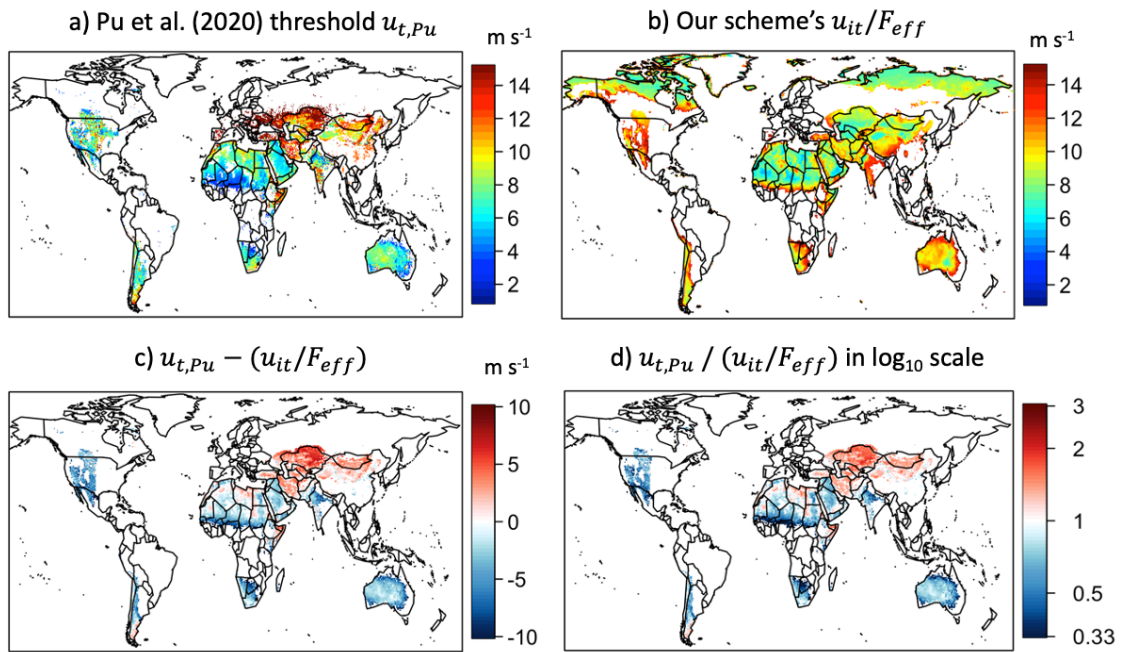
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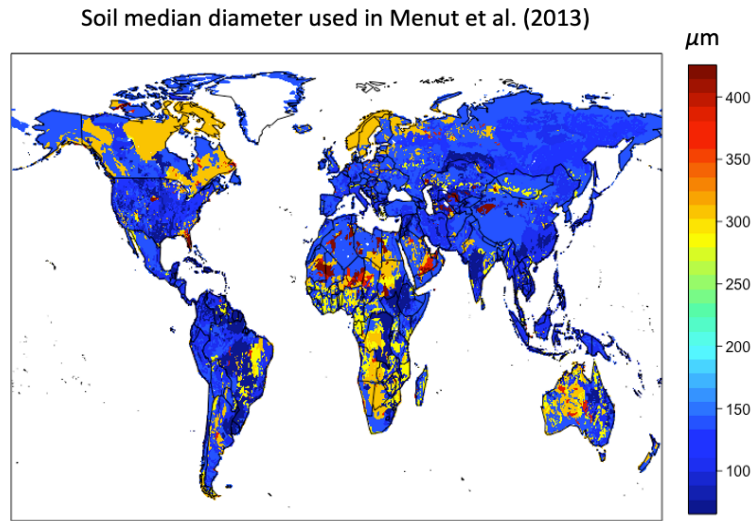
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 617 Figure S13. Comparison between the dust emission threshold simulated in this study and the
 618 observationally derived dust emission threshold from Pu et al. (2020). (a) Pu et al. (2020) threshold
 619 wind speed at 10 m height ($u_{t,Pu}$, m s⁻¹). (b) The simulated impact threshold friction velocity u_{*it}
 620 modified by the simulated hybrid drag partition effect, u_{it}/F_{eff} (m s⁻¹), from this study. The
 621 impact threshold was translated from a u_{*it} to u_{it} at 10 m height using the log law of the wall. (c)
 622 The differences between $u_{t,Pu}$ and u_{it}/F_{eff} . (d) The ratio between the two thresholds, with color
 623 bar drawn to log₁₀ scale.

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633 Figure S14. Soil median diameter \bar{D}_p used in Menut et al. (2013) as an input of the CHIMERE
634 chemical transport model, for the dust emission threshold and drag partition effect calculations.

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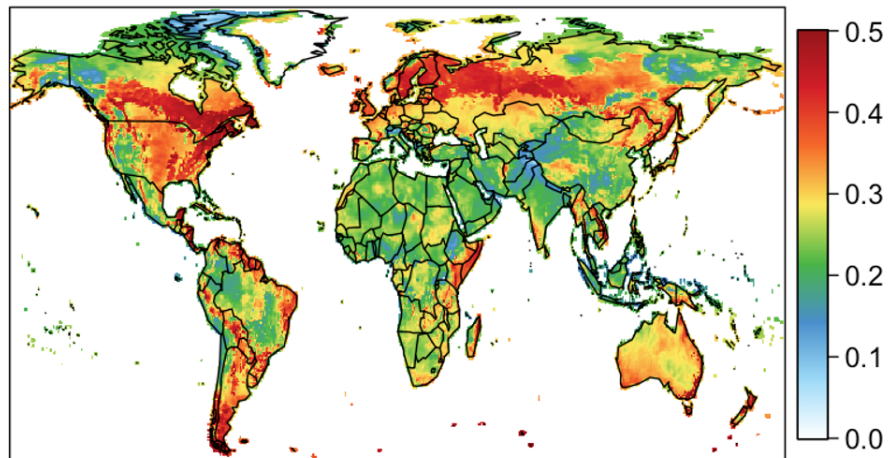
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2006 annual mean MERRA-2 friction velocity (m/s)



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642 Figure S15. Global distributions of MERRA-2 friction velocity u_* for the year 2006.

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