The density of ambient black carbon retrieved by a new method: implications for cloud condensation nuclei prediction

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Abstract. The effective density of black carbon (BC) is a crucial factor that is relevant to its aging degree and adds uncertainty in evaluating its climate effect. Here, we have developed a new method to retrieve the effective density of internally mixed BC in the atmosphere, combining field observations conducted from 15 November to 14 December 2016 in urban Beijing with the Köhler theory. The uncertainty in the retrieval method was evaluated to be within ±30 %, which was primarily caused by assumptions on both the hygroscopic parameter of organics and the proportional distribution of primary organic aerosols in different hygroscopic modes. Using the method, we find that the ambient internally mixed BC, accounting for 80 % ± 20 % of total BC aerosol particles, was retrieved with a campaign mean density of 1.1 ± 0.6 g cm$^{-3}$ during the observed periods. The retrieved result was comparable with that reported in the literature. By applying a lower (0.14 g cm$^{-3}$) and upper (2.1 g cm$^{-3}$) limit of the retrieved BC density in the cloud condensation nuclei (CCN) number concentration ($N_{CCN}$) estimation, we derived that the neglect of such variations in the BC density would lead to an uncertainty of −28 %–11 % in predicting $N_{CCN}$ at supersaturations of 0.23 % and 0.40 %. We also find that the $N_{CCN}$ was more sensitive to the variations in BC density when it was < 1.0 g cm$^{-3}$. This illustrates the necessity of accounting for the effect of BC density on CCN activity closer to source regions where the BC particles are mostly freshly emitted. The CCN closure was achieved when introducing the retrieved real-time BC density and mixing state. This study provides a unique way of utilizing field measurements to infer ambient BC density and highlights the importance of applying variable BC density values in models when predicting CCN and assessing its relevant climate effect.

1 Introduction

Black carbon (BC) aerosols, as the major absorber of solar radiation, play a vital role in the energy budget and climate of the Earth–atmosphere system by affecting the radiative forcing and cloud properties (Flanner et al., 2007; Ramanathan and Carmichael, 2008). The light-absorbing capability induced by BC is related to its density and morphology (Zhang et al., 2008; Rissler et al., 2014), which can be modified after mixing with other atmospheric aerosol particles (Khalizov et al., 2009; Xue et al., 2009). Changes in its physicochemical properties or the aging process would also regulate its ability to serve as cloud condensation nuclei (CCN) and further affect the CCN number concentrations (F. Zhang et al., 2016, 2017; Ren et al., 2023) and the radiative balance by affecting the cloud processes (Yuan et al., 2008; Wang et al., 2011). Owing to the complex evolution of the mixing state, density, and morphology of BC, the contribution of BC particles to CCN budgets is still not well understood.

BC particles, with diesel vehicles, industrial coal combustion, and residential coal combustion as major sources, are ubiquitous in urban environments (Bond et al., 2013; Dameto et al., 2017; Li et al., 2017; D. Liu et al., 2019). The mixing state of BC describes the distribution of the bare BC...
and coating materials among the aerosol population. Typically, freshly generated BC exists in the form of chain aggregates and is initially uncoated, which is known as externally mixed BC (Ex-BC). When the BC particles were emitted, they generally mixed with other materials by condensation, coagulation, and other processes (Riemer et al., 2004; Zhang et al., 2008; Liu et al., 2013; F. Zhang et al., 2020), forming the internally mixed BC (In-BC) particles consisting of a BC core and other chemical components (Cheng et al., 2006; Y. Zhang et al., 2016). The BC structure would be more compact, with regular shapes (Pagels et al., 2009; Zhang et al., 2008; Wang et al., 2017), and the effective density of internally mixed BC is changed accordingly with the reconstruction (H. Liu et al., 2019). The density and morphology of BC particles are closely related to the sources, mobility size, coating thickness, coating material, and its chemical composition (Pagels et al., 2009; Zhang et al., 2022). A wide range of BC density has been reported in previous studies (Lide, 1992; McMurry et al., 2002; Park et al., 2004; Kiselev et al., 2010). Recent field measurement has indicated that the average BC density is $\sim 1.2$ g cm$^{-3}$ in the ambient atmosphere (Y. Zhang et al., 2016). Field measurements have also indicated that a considerable fraction of externally mixed/uncoated BC exists (Clarke et al., 2004; Cheng et al., 2012), although a higher proportion of internally mixed/aged BC particles were observed in the ambient atmosphere (Schwarz et al., 2008; Massoli et al., 2015; Chen et al., 2020). In climate models, the BC was generally assumed to be completely internally mixed and thus treated to have a void-free spherical structure and a density value of $1.8$ g cm$^{-3}$ (Bond et al., 2013). This may lead to bias in estimating the climate effect driven by BC.

A previous study, based on a case study, has shown that when the aging degree of ambient particles was low, then the BC density ($\sim 1.8$ g cm$^{-3}$) under the spherical assumption would lead to the overestimation of particle hygroscopicity by $40\%$–$50\%$, and the overestimation could be explained by almost $100\%$, using the effective density of fresh BC ($\sim 0.45$ g cm$^{-3}$; Fan et al., 2020). This indicates the importance of using reasonable BC density values in the calculation of particle hygroscopicity. In addition, when estimating the CCN number concentration, a significant bias of $-35\%$---$-20\%$ was found due to the assumption of the particle mixing state (Ren et al., 2018). However, these studies have not yet accounted for such an impact of the BC density and mixing state on the CCN prediction due to a lack of real-time measurement data. Moreover, although the BC accounts for very small mass fractions ($5\%$--$10\%$) in total fine aerosols, according to our previous field observed results, the BC-containing particles could contribute $60\%$--$78\%$ toward the total number concentration in urban Beijing (Chen et al., 2020). This is comparable to the other results using the single-particle soot photometer (SP2) instrument, which measured the number fractions of the coated BC-containing aerosols and showed that they could be as high as about $50\%$--$80\%$ at the field sites in northern China (H. Liu et al., 2019; Zhao et al., 2022). Therefore, the effect of BC density on the uncertainty in CCN prediction should be concerned carefully.

The mixing state and the density of BC particles are usually directly measured by several techniques, such as an integrated system of a volatility tandem differential mobility analyzer and a SP2 instrument (VTDMA-SP2; Y. Zhang et al., 2016) or a differential mobility analyzer with a SP2 (DMA-SP2; Offert et al., 2007; Rissler et al., 2014; Wu et al., 2019) and a differential mobility analyzer coupled with a centrifugal particle mass analyzer and a SP2 (DMA–CPMA–SP2) system (H. Liu et al., 2019; Yu et al., 2020). However, such techniques or measurements are not available in many previously conducted field campaigns. In this study, we develop a novel method for retrieving the mixing state and effective density of ambient BC particles by combining the field-measured hygroscopic growth factor and aerosol chemical composition with the Köhler theory (Petters and Kreidenweis, 2007). The uncertainty in the new retrieval method was evaluated. The retrieved results were also compared and validated with existing observations. In addition, the effect of the BC density and mixing state on the prediction of the CCN number concentrations was further evaluated through a sensitivity and closure test by accounting for the retrieved real-time variations in the BC density and mixing state.

2 Field measurements and methodology

2.1 Field measurements

Measurements in this study were conducted from 15 November to 14 December 2016 at a typical urban site of Beijing (39.97°N, 116.37°E; 49 m above sea level). The site is located at the Institute of Atmospheric Physics, Chinese Academy of Sciences, which is mainly influenced by the surrounding cooking, road traffic, and residential coal burning emissions during the home heating periods (Sun et al., 2016). Detailed information about the sampling site has been presented in previous studies (Sun et al., 2016; Zhang et al., 2019). The number concentration of the condensation nuclei (CN) at each size was measured by a scanning mobility particle sizer, which was equipped with a differential mobility analyzer (DMA; model 3081, TSI) and a condensation particle counter (CPC; model 3772, TSI). Subsequently, the monodispersed particles were introduced into a Droplet Measurement Technologies CCN counter (CCNc; DMT; Lance et al., 2006) to measure the CCN number concentration. A hygroscopic tandem differential mobility analyzer (HTDMA) system was used to measure the hygroscopic growth factor (Gf; Tan et al., 2013). Here, four diameters of 40, 80, 110, 150, and 200 nm were selected in the campaign. Gf is defined as the ratio of the mobility diameter at the given relative humidity (RH) to the dry diameter (Petters and Kreidenweis, 2007). The nonrefractory submicron aerosol chemical
composition was measured by an Aerodyne high-resolution time-of-flight aerosol mass spectrometer (HR-ToF-AMS; Xu et al., 2019), including sulfate, nitrate, ammonium, chloride, and organics. Two factors, including a non-hygroscopic primary organic aerosol (POA) and hygroscopic secondary organic aerosol (SOA), were classified by positive matrix factorization (PMF) with the PMF algorithm (v4.2) method (Paatero and Tapper, 1994) and followed the procedures reported in Ulbrich et al. (2009). The refractory black carbon mass loading was measured by an Aethalometer (model AE33, Magee Scientific). Both the nonrefractory materials and BC mass concentration were measured with diameters < 1.0 µm. A detailed description of the instrument operation and data process have been described in detail elsewhere (Ren et al., 2018; Xu et al., 2019; Zhang et al., 2019; Fan et al., 2020).

2.2 Retrieving the mixing state and density of BC

2.2.1 Retrieving the mixing state of BC

The Gf probability distribution function (Gf-PDF) for a specified diameter can be retrieved, first, based on the TDMAinv algorithm (Gysel et al., 2009). The κ-PDF can be further calculated based on the Gf-PDF (Fan et al., 2020). Size-resolved κ is derived using κ-Köhler theory, based on hygroscopic growth factor (Gf), as follows (Petters and Kreidenweis, 2007):

\[ \kappa_{\text{gf}} = (\text{Gf}^3 - 1) \cdot \left[ \frac{1}{\text{RH}} \exp \left( \frac{4\sigma_{\text{s/a}} M_w}{RT \rho_w D_\text{d} \kappa_{\text{gf}}} \right) - 1 \right]. \]

where Gf is hygroscopic growth factor, RH is the relative humidity in the HTDMA (90 %), \( D_\text{d} \) is the dry diameter, \( \sigma_{\text{s/a}} \) is assumed to be the surface tension of pure water, \( R \) is the universal gas constant, \( T \) is the temperature, and \( M_w \) and \( \rho_w \) are the molecular mass and the density of water, respectively.

The κ-PDF patterns of particles in different sizes always present two modes, namely the nearly hydrophobic (NH) mode, with \( \kappa_{\text{gf}} \leq 0.1 \), and more hygroscopic (MH) mode, with \( \kappa_{\text{gf}} > 0.1 \) (Fig. S1 in the Supplement). First, based on the κ-PDF patterns, the number fraction (NF) of the total nearly hydrophobic group with the boundary of \( [0, 0.1] \) was calculated according to the following equation:

\[ \text{NF} = \int_{0}^{0.1} c(\kappa, D_p) \, d\kappa. \]

where \( c(\kappa, D_p) \) was normalized as \( \int c(\kappa, D_p) \, d\kappa = 1 \), where \( \kappa \) can be replaced by \( \kappa_{\text{gf}} \). \( D_p \) is the selected electrical mobility diameter in the campaign.

The nearly hydrophobic mode consists of both externally mixed POA (Ex-POA or bare POA) and externally mixed BC (Ex-BC). Since the number fraction of the nearly hydrophobic POA would change with the emission and aging processes, in this study, we have applied different values for the number fractions of hydrophobic POA (NH-POA) under clean (91 %), moderately polluted (70 %), and heavily polluted conditions (31 %) by referring to the literature (Liu et al., 2021), as shown in Fig. S2. The number concentration of Ex-BC was then calculated using the total number fraction of the NH mode minus the number of NH-POA.

\[ N_{\text{POA-containing}} = N_{\text{total}} \times \text{NF}_{\text{POA-containing}} \]
\[ N_{\text{bare-POA}} = N_{\text{POA-containing}} \times \text{NF}_{\text{bare-POA}} \]
\[ N_{\text{Ex-BC}} = N_{\text{NH}} - N_{\text{bare-POA}}. \]

where \( N_{\text{POA-containing}} \) and \( \text{NF}_{\text{POA-containing}} \) are the number concentration and fraction of POA-containing particles, \( N_{\text{total}} \) is the total number concentration, \( N_{\text{bare-POA}} \) and \( \text{NF}_{\text{bare-POA}} \) are the number concentration and fraction of bare POA particles, and \( N_{\text{NH}} \) is the number of the nearly hydrophobic group.

The number size distribution of the externally mixed BC \((n_{\text{Ex-BC}}(\log D_p))\) can be calculated based on the particle number size distribution (PNSD) and the number fraction of the hydrophobic mode of BC (\( \text{NF}_{\text{Ex-BC}} \)) as follows:

\[ n_{\text{Ex-BC}}(\log D_p) = \text{NF}_{\text{Ex-BC}} \times n(\log D_p). \]

where \( n(\log D_p) \) is the function of the aerosol number size distribution, and \( D_p \) is the mobility diameter.

By assuming that the particles were spherical (Rader and McMurry, 1986), the mass size distribution of Ex-BC \((M_{\text{Ex-BC}})\) was obtained as follows:

\[ M_{\text{Ex-BC}}(\log D_p) = \frac{\pi}{6} D_p^3 \rho \text{NF}_{\text{Ex-BC}}(\log D_p), \]

where \( D_p \) is the mobility diameter, \( \rho \) is the effective density of Ex-BC, and \( n_{\text{Ex-BC}}(\log D_p) \) is the function of the number size distribution of Ex-BC, respectively. By reviewing and summarizing the existing results, we show that the typical values of density for the freshly emitted or externally mixed BC observed in the winter of urban Beijing or the North China Plain span over 0.14–0.50 g cm\(^{-3}\), with a mean of ∼ 0.40 ± 0.10 g cm\(^{-3}\) (Fig. S3), in the size range of 100 to 300 nm, which is where the mass concentration of externally mixed BC mostly concentrated (Geller et al., 2006; Wu et al., 2019; Liu et al., 2020; Zhao et al., 2022). Therefore, an average \( \rho_{\text{Ex-BC}} \) of 0.4 g cm\(^{-3}\) was used to calculate the mass concentration of externally mixed BC in our study. Uncertainty analyses due to the variations in \( \rho_{\text{Ex-BC}} \) are given in Sect. 2.3.

The mass size distribution of Ex-BC was fitted using the lognormal distribution, as shown in Fig. S4 (Wu et al., 2017; D. Liu et al., 2019; Zhao et al., 2022). Thus, the bulk mass concentration of Ex-BC can be calculated from the integration of the mass size distribution as follows:
where $D_{\text{start}}$ and $D_{\text{end}}$ are the lower and upper size limit, and $M_{\text{Ex-BC}}(\log D_p)$ is the function of the Ex-BC mass size distribution. We then obtained the bulk mass concentration of internally mixed BC ($m_{\text{In-BC}}$) by subtracting $m_{\text{Ex-BC}}$ from the bulk BC mass concentration measured by the AE33 in Eq. (7). It should be noted that the mass concentration of BC obtained from the AE33 based on aerosol light absorption may lead to some uncertainties, as has been further addressed in Sect. 2.3.

### 2.2.2 Retrieving the density of BC

For the retrieval of the density of BC, the principal idea is to use the measured $\kappa_{gf}$ to calculate the density of BC based on the Zdanovskii–Stokes–Robinson (ZSR) mixing rule (Stokes and Robinson, 1966; Zdanovskii, 1948) with the chemical composition measured by AMS (Petters and Kreidenweis, 2007). In the retrieval, several aspects are concerned. First, since the ZSR rule assumes that the aerosol particles are internally mixed, the $\kappa_{gf}$ value of the more MH mode ($\kappa_{gf-MH}$) is thus applied for retrieving the density of the internally mixed BC. Second, since the size distribution of BC number concentration usually has peaks between 100 and 200 nm (D. Liu et al., 2019; Yu et al., 2020; Zhao et al., 2022), the $\kappa_{gf-MH}$ value of the particles in accumulation mode was averaged and applied for the retrieval. Previous studies showed an independence of $\kappa_{gf-MH}$ for the particle size when the $D_p > 100$ nm during the campaign period (Fan et al., 2020). Therefore, the average of $\kappa_{gf-MH}$ in the accumulation mode is reasonable for the determination of the In-BC density. Third, since only one hydrophobic and/or one hygroscopic mode was observed by the HTDMA in most cases during the campaign (Figs. S1 and S5), the chemical components of the more hygroscopic (MH) mode at a given diameter should contain both the hygroscopic non-BC and the coating on BC-containing particles, which would be measured together by the HR-ToF-AMS instrument. Therefore, by subtracting the externally mixed POA in the non-hygroscopic mode (see Sect. 2.3), the concentration and mass fraction of each component measured by HR-ToF-AMS can represent the overall chemical composition of MH modes, and thus, this was applied in the ZSR mixing rule for the retrieval of the density of internally mixed BC in this study. In addition, because of the inversion including measurements from HTDMA and HR-ToF-AMS, a total mass closure of the measured aerosol particles was conducted between the two techniques by comparing the mass concentration of PM$_{1}$, and the results are in good agreement (Fig. S6). The density of the internally mixed BC (In-BC), $\rho_{\text{In-BC}}$ is then derived from the following equations:

\[
\kappa_{gf-MH} = \kappa_{\text{chem}} = \sum_i e_i \kappa_i
\]

\[
\begin{align*}
\rho_{\text{In-BC}} &= \frac{m_{\text{In-BC}}}{v_{\text{total}}} \\
&= \frac{v_{\text{inorg}}}{v_{\text{total}}} \kappa_{\text{inorg}} + \frac{v_{\text{SOA}}}{v_{\text{total}}} \kappa_{\text{SOA}} + \frac{v_{\text{In-POA}}}{v_{\text{total}}} \kappa_{\text{POA}} \\
&\quad + \frac{v_{\text{In-BC}}}{v_{\text{total}}} \kappa_{\text{BC}},
\end{align*}
\]

where $\kappa_{gf-MH}$ is the hygroscopic parameter of the more hygroscopic (MH) mode, $\kappa_{\text{chem}}$ is the hygroscopic parameter of the aerosol particles in the mixed composition and can be calculated based on chemical volume fractions using a simple rule (Stokes and Robinson, 1966; Petters and Kreidenweis, 2007), $\kappa_i$ is the hygroscopic parameter of each pure component, and $e_i$ is the volume fraction of the individual components in the internally mixed particle. $v_{\text{inorg}}, v_{\text{SOA}},$ and $v_{\text{In-POA}}$ are the volumes of the inorganic, SOA, and internally mixed POA species and can be calculated as follows:

\[
\begin{align*}
&v_{\text{In-BC}} = \frac{v_{\text{inorg}} \kappa_{\text{inorg}} + v_{\text{SOA}} \kappa_{\text{SOA}}}{\kappa_{gf-MH}} - v_{\text{inorg}} \\
&\quad - v_{\text{SOA}} - v_{\text{In-POA}} \\
&\quad = \frac{m_{\text{inorg}}}{\rho_{\text{inorg}}} \kappa_{\text{inorg}} + \frac{m_{\text{SOA}}}{\rho_{\text{SOA}}} \kappa_{\text{SOA}} - \frac{m_{\text{inorg}}}{\rho_{\text{inorg}}} - \frac{m_{\text{SOA}}}{\rho_{\text{SOA}}} - m_{\text{In-POA}}.
\end{align*}
\]

Then, the $\rho_{\text{In-BC}}$ can be calculated based on its mass concentration and volume as follows:

\[
\rho_{\text{In-BC}} = \frac{m_{\text{In-BC}}}{\kappa_{gf-MH} v_{\text{total}}},
\]

where $m_{\text{In-BC}}$ is the mass concentration of internally mixed BC, and $m_{\text{inorg}}, m_{\text{SOA}},$ and $m_{\text{In-POA}}$ are the mass concentrations of the inorganic species and SOA, which are measured by the AMS. $m_{\text{In-POA}}$ is the mass concentration of the internally mixed POA and can be calculated through subtracting the mass fraction of the NH-POA from the total mass concentrations of the POA. $\rho_{\text{inorg}}, \rho_{\text{SOA}}$ and $\rho_{\text{POA}}$ are the density of the inorganic species, i.e., SOA and POA, since the AMS measures the concentrations of the organic and inorganic ions, including SO$_4^{2-},$ NO$_3^-, NH_4^+$, and Cl$^-$. Here, inorganic species were derived by applying a simplified ion pairing scheme (Gysel...
negative values for density. This is because a higher fraction of OA usually corresponds to a larger fraction of organic aerosols in non-hygroscopic mode, which is similar to the density of the lubricating oil (Petters and Kreidenweis, 2007) to convert the mass concentrations of the ions to the inorganic salts as follows:

\[ n_{\text{NH}_4\text{NO}_3} = n_{\text{NO}_3^-} \]
\[ n_{\text{NH}_4\text{HSO}_4} = \min(2n_{\text{SO}_4^{2-}} - n_{\text{NH}_4^+} + n_{\text{NO}_3^-}, n_{\text{NH}_4^+} - n_{\text{NO}_3^-}) \]
\[ n_{\text{(NH}_4)_2\text{SO}_4} = \max(n_{\text{NH}_4^+} - n_{\text{NO}_3^-} - n_{\text{SO}_4^{2-}}, 0) \]
\[ n_{\text{H}_2\text{SO}_4} = \max(0, n_{\text{(SO}_4^{2-})} - n_{\text{NH}_4^+} + n_{\text{NO}_3^-}). \]

(11)

where \( n \) represents the number of moles, and the mass concentrations were obtained by the number of moles times the molar mass of each inorganic salt. Because the value of the \( n_{\text{NH}_4\text{HSO}_4} \) was zero in this campaign, three inorganic salts including \( \text{NH}_4\text{HSO}_4 \), \( \text{(NH}_4\text{)}_2\text{SO}_4 \), and \( \text{NH}_4\text{NO}_3 \) were applied in our study. The densities for inorganic salts were taken from previous studies (Gysel et al., 2007; Wu et al., 2016). Here the densities for the three inorganic salts are 1.78, 1.77, and 1.72 g cm\(^{-3}\), respectively. By summarizing the previous studies (Gysel et al., 2007; Dinar et al., 2006), 1.4 g cm\(^{-3}\) was selected as the density of SOA (\( \rho_{\text{SOA}} \)). The density of POA (\( \rho_{\text{POA}} \)) is assumed to be 1.0 g cm\(^{-3}\) for urban environments, which is similar to the density of the lubricating oil (Wu et al., 2016). Since the cooking organic aerosols represent a high contribution to POA in urban environments, we choose the mean density of the rapeseed oil and oleic acid (\( \sim 0.85 \) g cm\(^{-3}\); Reyes-Villegas et al., 2018) to evaluate the result, as shown in Sect. 2.3. The values of \( \kappa \) for inorganic components are 0.56 for \( \text{NH}_4\text{HSO}_4 \); 0.48 for \( \text{(NH}_4\text{)}_2\text{SO}_4 \); and 0.58 for \( \text{NH}_4\text{NO}_3 \) along with the best-fit values for the three inorganic salts (Petters and Kreidenweis, 2007; Gunthe et al., 2009). The \( \kappa_{\text{SOA}} \) is assumed to be 0.15, according to the field studies in urban areas (Chang et al., 2010; Kawana et al., 2016).

Note that the method fails to retrieve the BC density when organic aerosol (OA) accounts for a large fraction (> 60%). This is because a higher fraction of OA usually corresponds to lower total volume of all the species (Fig. S7), yielding negative values for \( v_{\text{Ex-BC}} \) introduced in Eq. (9). As a result, 61% of the data observed during the campaign were valid for calculating the BC density.

Similarly, the bulk density of BC (\( \rho_{\text{bulk-BC}} \)) is calculated with the same method as for the calculation of the \( \rho_{\text{In-BC}} \). When calculating the \( \rho_{\text{bulk-BC}} \), the bulk \( \kappa_{\text{glob}} \) value measured by HTDMA is applied, assuming that all the aerosol particles are internally mixed.

2.3 Uncertainties and limitations

For the retrieval, the assumptions on the values of \( \kappa_{\text{SOA}}, \rho_{\text{POA}}, \rho_{\text{SOA}}, \text{ and } \rho_{\text{Ex-BC}}, \) as well as the fraction of primary organic aerosols in non-hygroscopic mode, would add uncertainty to the inferred values of ambient internally mixed BC density. For example, the freshly emitted POA particles might be consistently coated with secondary particles during the aging process, resulting in changes in the \( \rho_{\text{NF-POA}} \). However, a real-time variation in the \( \rho_{\text{NF-POA}} \) is not yet available due to the lack of such measurement data.

Applying only rough fractions of hydrophobic POA for three different atmospheric conditions could still cause uncertainties. Also, the densities of POA and SOA may differ due to their precursors, emission sources, and the formation mechanisms in ambient atmosphere (Alfarra et al., 2006; Reyes-Villegas et al., 2018). The density of Ex-BC is generally characterized by the morphology and size (Wu et al., 2019). In addition, the value of \( \kappa_{\text{SOA}} \) spans largely due to the variations in the emissions of gas precursors and formation processes under different atmospheric conditions (Zhang et al., 2015; J. Liu et al., 2021). Therefore, we examined the sensitivities of In-BC density to the variations in these factors, as exhibited in Figs. 1 and 2.

The figures show that the In-BC density gradually decreases with the increment of the \( \rho_{\text{NF-POA}} \), implying that the high fraction of bare POA particles corresponds to the early aging stage of aerosol particles. With the increase in \( \kappa_{\text{SOA}} \), the In-BC density was generally reduced but with small fluctuations (Figs. 1a and 2b). This suggests a complex impact of the assumptions of \( \kappa_{\text{SOA}} \) on the retrieved BC density. In addition, the In-BC density decreased slightly as \( \rho_{\text{Ex-BC}} \) increased (Fig. 2e), suggesting that applying a larger \( \rho_{\text{Ex-BC}} \) would derive smaller values for In-BC density. The In-BC density was insensitive to the changes in the density of POA and SOA, showing an almost negligible effect on the retrieved results (Fig. 2c and d).

The uncertainty analysis shows that, by comparing the results based on the mean fraction of the \( \rho_{\text{NF-POA}} \) with a typical atmospheric observed range of 50%–90% for the \( \rho_{\text{NF-POA}} \) (L. Liu et al., 2021), the assumption on \( \rho_{\text{NF-POA}} \) can lead to relative deviations (uncertainty) of −17%–+27% for the retrieved BC density (Fig. 3a).

In addition, unlike inorganics (e.g., \( \text{NH}_4\text{HSO}_4, \text{(NH}_4\text{)}_2\text{SO}_4, \text{and } \text{NH}_4\text{NO}_3 \)), for which the hygroscopicity of organic species varies largely due to the complexity in organic aerosol constituents. Therefore, the assumption of the values of \( \kappa_{\text{SOA}} \) will add to the uncertainty in the calculation of BC density. Previous studies have suggested that the organics have a wide range of \( \kappa \) values ranging from 0.05 to 0.3 (Jimenez et al., 2009; Mei et al., 2013). Thus, a sensitivity test has also been done to examine the effect due to changes in \( \kappa_{\text{SOA}} \) on calculating the density of BC (Fig. 1a). The result shows that the assumption of \( \kappa_{\text{SOA}} \) values can cause an average relative deviation of −10%–+3% when calculating the density of In-BC (Fig. 3b).

However, the sensitivity test shows that the impact of both the \( \rho_{\text{POA}} \) and \( \rho_{\text{SOA}} \) variations on the BC density estimation was very small or even negligible (Fig. 1b and c). By varying the \( \rho_{\text{POA}} \) from 0.85 to 1.5 g cm\(^{-3}\) and the \( \rho_{\text{SOA}} \) from 0.9 to 1.65 g cm\(^{-3}\), according to the literature (Noureddini et al., 1992; Alfarra et al., 2006; Reyes-Villegas et al., 2018;
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Figure 1. Sensitivities of In-BC density to the variations in the number fraction of the nearly hydrophobic (NH) POA and hygroscopic parameter of OA ($k_{SOA}$) (a), POA density (b), SOA density (c), and the externally mixed BC density (d).

Figure 2. Sensitivity of the In-BC density to variations in the number fraction of nearly hydrophobic (NH) POA (a), the hygroscopic parameter of SOA (b), the POA density (c), the SOA density (d), the externally mixed BC density (e), and the harmonic mean of multiple factors (f).

Kostenidou et al., 2007), the retrieval uncertainties in the BC density were both within ±5% (Fig. 3c and d). For $\rho_{Ex-BC}$, it exhibited that the evolution of the $\rho_{Ex-BC}$ could lead to an average deviation of −16%−+9% in calculating the In-BC density (Fig. 3e) when increasing the values of $\rho_{Ex-BC}$ from 0.1 to 1.0 g cm$^{-3}$, which represents a typical range in the ambient atmosphere (Wu et al., 2019; Liu et al., 2020). A combined uncertainty ($\delta$), which was calculated by Eq. (12), was $-26\%$–$+29\%$, as shown in Fig. 3f.

$$\delta = \sqrt{\sum_{i=1}^{n} \delta_i^2}$$

(12)
3 Results and discussion

3.1 A comparison and validation of retrieved mixing state and density of BC

Figure 4a shows the retrieved time series of the mixing state of ambient BC during the campaign. Large temporal variations in the mass fraction of internally and externally mixed BC are present during the observed period at the sites. The temporal changes should be related to the atmospheric aging process or diurnal variations in emissions (D. Liu et al., 2019; Fan et al., 2020). Statistically, the average mass fractions of externally and internally mixed BC were 20% ± 18% and 80% ± 20%, respectively, showing that most of the BC particles were aged and internally mixed with other components. Previous studies at urban sites have shown the co-existence of the externally mixed BC in the ambient atmosphere (Schwarz et al., 2008; Cheng et al., 2012; Chen et al., 2020) due to continuous combustion processes (e.g., vehicle exhaust and residential sector; Wang et al., 2017; D. Liu et al., 2019). Our results are basically comparable with those previously reported, which are directly measured or indirectly retrieved. For example, Chen et al. (2020) found that the mass fraction of internally mixed BC particles was nearly ∼80%–90% in summer in Beijing, based on VTDMA measurements. Liu et al. (2020), using a tandem system with an aerodynamic aerosol classifier and SP2, reported that the mass fraction of internal BC-containing particles would increase with increasing size and reach ∼70% in Beijing. Overall, the mass fraction obtained in our study was comparable with that reported in urban Beijing. Previous studies also showed the significant diversity of the BC mixing state among emission conditions and coating processes (Shiraiwa et al., 2008; Pan et al., 2017; Y. Zhang et al., 2020). Accordingly, the densities of the bulk and internally mixed BC present apparent fluctuations (as shown in Fig. 4b), which is significantly affected by the variations in BC emission sources and BC aging processes. The density of the In-BC during daytime was generally higher than that at night (Fig. 4c). The elevated BC density during daytime was likely due to the strong photochemical processes promoting the aging of BC particles, which resulted in a conversion from an uncompactd structure to the compact and regular spherical shape of BC (Qiao et al., 2018; H. Liu et al., 2019). The increase in BC density at around 20:00 LT (local time) might indicate that the BC particles would be rapidly coated with secondary inorganic aerosol (SIA) particles and continuously aged in the polluted period due to the
heterogeneous reactions of SIA in urban regions (Y. Zhang et al., 2016; Peng et al., 2016, 2017). Actually, following the haze evolution, the fraction of the nearly hydrophobic group reduced rapidly (Fig. S9). Consequently, the average density of In-BC showed an obvious increase from the clean conditions to the polluted periods (Fig. S5). A slight decrease was observed in the bulk BC density during traffic hours. This is likely associated with the continuous emissions (e.g., vehicle exhaust) that lead to uncoated or uncompacted BC particles in this period. The diurnal cycle in In-BC density was consistent with the coating thickness measured by a tandem CPMA-SP2-DMA-SP2 (Liu et al., 2020), demonstrating that the new method can derive the density of ambient BC particles reasonably. On average, the campaign average values of the bulk and internally mixed BC densities were 0.7 ± 0.5 and 1.1 ± 0.6 g cm\(^{-3}\), respectively, which were much less than 1.8 g cm\(^{-3}\), implying that the BC particles are not void-free spheres in the urban atmosphere. The results of In-BC density were comparable with those observed at other sites in North China Plain (NCP; as shown in Fig. 4d), illustrating that the BC effective density retrieved by this method was within the range of density from field measurements.

Based on both field measurements (e.g., Lide, 1992; Y. Zhang et al., 2016; Wu et al., 2019; H. Liu et al., 2019) and laboratory studies (e.g., McMurry et al., 2002; Park et al., 2003, 2004; Olfert et al., 2007; Kiselev et al., 2010; Gysel et al., 2011, 2012), the BC density from diverse combustion sources or representing different aging degrees has been obtained and ranges widely from 0.14 to 2.1 g cm\(^{-3}\), as summarized and shown in Fig. 5. The mean probability distribution function (PDF) of the density of bulk and In-BC retrieved by this study is also presented in Fig. 5. It shows that the retrieved density of bulk BC exhibited a dominant mode, with a peak value at 0.7 g cm\(^{-3}\), which was situated between the typical density range of those externally mixed and internally mixed BC measured previously. For the In-BC, the PDF had a peak value at 1.1 g cm\(^{-3}\) but ranged widely from \(\sim 0.5\) to 2.5 g cm\(^{-3}\), which indicated various morphologies and different aging degrees and compositions of ambient BC particles due to the complex impact of multiple local sources and aging processes during the observed period in urban Beijing. Overall, the retrieved values for In-BC density fall within the range of the typical internally mixed BC values reported in the literature, verifying the reliability of our inversion results.
A previous study showed that the use of an inaccurate density value of BC particles would result in large biases in estimating $\kappa$ of ambient aerosol particles with the ZSR mixing rule (Fan et al., 2020) and would further lead to uncertainties in the prediction of $N_{CCN}$ and relevant climate effects. Considering the large variation range of BC density during the campaign, which is closely associated with BC morphology or the degree of BC aging, we further examine the sensitivity of critical supersaturation ($S_c$), critical diameter ($D_{cut}$), and predicted $N_{CCN}$ to variations in BC density (Fig. 6). Here, we use the critical diameter and particle number size distribution to calculate $N_{CCN}$. The method to derive the critical diameter is based on the Köhler theory and ZSR rule. Three CCN closure studies were assumed to evaluate the effect of BC density and mixing state on the prediction of the CCN number concentrations. Closure studies provide a useful way to investigate the importance of aerosol properties for CCN concentration prediction. If the closure study is achieved, then it means that the bias between the predicted and measured CCN concentrations is within $\pm 15\%$ (Chang et al., 2007).

Detailed calculation methods are presented in the Supplement (see the Methods section) or in Ren et al. (2018). The results show that, by varying the value of the density that represents the range of BC density in the atmosphere from 0.14 to 2.1 g cm$^{-3}$, the $D_{cut}$ is apparently reduced at a given supersaturation ($S$; Fig. 6a), or similarly, the $S_c$ is decreased rapidly for a given particle size (Fig. 6b). The results show that the changes in the $D_{cut}$ and $S_c$ were more sensitive when the BC density was below 1.0 g cm$^{-3}$. The effects on the $D_{cut}$ and $S_c$ both gradually weakened with the increase in BC density. This shows that it is critical to apply a more accurate BC density for the aerosol particles with a low aging degree for predicting CCN and its climate effect. Accordingly, the ratios of predicted-to-measured $N_{CCN}$ ranged from 0.72 to 1.11 by varying the BC density from 0.14 to 2.1 g cm$^{-3}$ at the typical $S$ of 0.23 % and 0.40 % (Fig. 6c and d), showing an estimation uncertainty of $-28\%$–$11\%$ in the $N_{CCN}$ prediction.

The diurnal variations in the ratio of predicted-to-measured $N_{CCN}$ at $S = 0.40\%$ and 0.23 % are shown to examine the response of the BC density on $N_{CCN}$ prediction at different time periods (Fig. 6e and f). By applying the lower limit of the density value of 0.14 g cm$^{-3}$, the prediction was much worse than when using the density of 2.1 g cm$^{-3}$ at night (00:00–06:00 LT), which is when the latter was much closer to the real density of ambient BC (Fig. 4c). The prediction was improved substantially by applying the value of 2.1 g cm$^{-3}$, and an obvious overestimation by up to $\sim 40\%$ was shown. The results further illustrate that it is critical to account for the real-time mixing state and density of BC particles in $N_{CCN}$ prediction, particularly in regions with heavy traffic and residential coal emissions.

It should be noted that the assumption of the surface tension of water would overestimate the critical diameter and underpredict CCN number concentration, while the surface tension depression might be more obvious for small-sized particles (< 60 nm), as the fraction of organics is higher at small particle sizes (Meng et al., 2014; Cai et al., 2018). Here, in this study, we calculated the critical diameters at supersaturations of 0.40 % and 0.23 %. Typical values in cloud, corresponding to larger sizes (> 70 and 90 nm) of aerosols. Therefore, the uncertainties from the application of the surface tension of pure water should be negligible (< 10 %).

### 3.3 $N_{CCN}$ prediction based on the real-time variations in BC density and mixing state

Figure 7 exhibits the comparisons between predicted and measured $N_{CCN}$ at $S$ of 0.23 % and 0.40 % by accounting for the retrieved real-time variations in the BC density and mixing state. It shows that the $N_{CCN}$ can be well predicted,
Figure 6. Sensitivity of critical supersaturation ($S_c$) (a) and diameter ($D_{cut}$) (b) to the variations in BC density. Predicted $N_{CCN}$ as a function of measured $N_{CCN}$ by varying the density from 0.14 to 2.1 g cm$^{-3}$ at $S = 0.40\%$ (c) and $S = 0.23\%$ (d). The solid black line is the 1 : 1 line. Diurnal variations in the ratio of the predicted-to-measured $N_{CCN}$ at $S = 0.40\%$ (e) and $S = 0.23\%$ (f) are shown.

with a slope of 1.01 and 1.02 at $S = 0.23\%$ and 0.40\%, respectively (Fig. 7a and b), and only presents a slight deviation. The slight deviation is primarily due to the fixed value of the density for the externally mixed BC caused by the retrieval method, especially during noontime and evening rush periods (Fig. 7c and d).

The diurnal variations in the ratio of predicted-to-measured $N_{CCN}$ show that the $N_{CCN}$ can be underestimated by up to 15\% at $S = 0.40\%$ during noontime, while being slightly overrated during the evening traffic hours and nighttime, possibly due to the underestimation of the number fraction of Ex-BC. Overall, the dependence of the CCN prediction on $S$ is due to the size dependence of $\kappa$ and the mixing state (Zhang et al., 2017; Liu et al., 2020; Ren et al., 2018). A better closure at $S = 0.23\%$ is because the bulk $\kappa$ of the particles is closer to that at the critical diameter of 100–150 nm. Similarly, the effect on the CCN prediction induced by the bulk mixing state would be more critical for smaller particles, corresponding to the critical diameter at high $S$.

Overall, when considering the effective density of BC relevant to its mixing state, the CCN closure is achieved. Previous studies have shown that the freshly emitted BC particles may convert from fractal-like aggregates to a compact structure, and their density would increase with the aging process (H. Liu et al., 2019; F. Zhang et al., 2020, 2022), but the actual density of In-BC may be lower than 1.8 g cm$^{-3}$ in the ambient atmosphere, according to this study. Therefore, the currently applied value represents a density of the void-free structure of BC particles and may cause an overestimation in CCN prediction. In addition, although the BC accounts for small mass fractions in ambient fine aerosols, according to the measurements simultaneously conducted at the site, the BC-containing particles could contribute 60\%–78\% to the total number concentration in urban Beijing (Chen et al., 2020). Our results further highlight that the effect of BC density on the uncertainty in CCN prediction should be concerned carefully.
4 Conclusions

The mixing state and effective density of BC changed through the heterogeneous chemistry process and thus would cause uncertainty in evaluating its CCN activity. In this study, we develop a new method to retrieve the mixing state and effective density of ambient BC using field measurements and the Köhler theory. The uncertainty in the new retrieval method was evaluated within ±30%, which was primarily caused by assuming the value of $\kappa_{SOA}$ and the fraction of primary organic aerosols in the non-hygroscopic mode. The retrieved results show that most of the BC particles were aged and internally mixed with other components, with the mean mass fraction of 80% ± 20%. Averagely, the retrieved densities of the bulk and internally mixed BC were 0.7 ± 0.5 and 1.1 ± 0.6 g cm$^{-3}$, respectively, but ranged widely from ~ 0.1 to 2.5 g cm$^{-3}$, indicating various morphologies and different aging degrees and compositions of ambient BC particles, due to the complex impact of multiple local sources and aging processes during the observed period. The retrieved result was basically comparable with previous observations in the North China Plain.

A further examination shows that the uncertainties in the $N_{CCN}$ prediction were -28%–11% at the typical $S$ of 0.23% and 0.40%, by varying the BC density from 0.14 to 2.1 g cm$^{-3}$ that represented the range of ambient BC particles. Moreover, the prediction was found to be more sensitive to the variations in the BC density when it was < 1.0 g cm$^{-3}$, suggesting a great significance of accounting for the effect of BC density on the aerosol particles with a low aging degree when evaluating the climate effect. The CCN closure was achieved when introducing the retrieved real-time BC density relevant to its mixing state. This work provides a unique way of utilizing field observations to infer ambient BC density and highlights that the current assumption of a void-free structure of BC particles in models would cause large uncertainties in CCN prediction and in the relevant climate effect evaluation.

The method used to derive the ambient BC density has limitations, since the assumptions of the values of $\kappa_{SOA}$, $\rho_{POA}$, $\rho_{SOA}$, and $\rho_{Ex-BC}$, as well as the fraction of primary organic aerosols in non-hygroscopic mode, would add uncertainty to the inferred values of ambient internally mixed BC density. It is thus necessary to examine observational data to verify this methodology in future studies. However, the method and results of this study could provide an avenue for a more comprehensive understanding of the variations in the BC density in Beijing. Additionally, it has the potential to reveal the uncertainties in the usage of a void-free structure of the BC density when assessing the climate effects.
Data availability. All data needed to evaluate the conclusions in the paper are presented in the paper and/or the Supplement. All data used in the study are also available from the corresponding author upon request (zhangfang2021@hit.edu.cn).

Supplement. The supplement related to this article is available online at: https://doi.org/10.5194/acp-23-4327-2023-supplement.

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Competing interests. The contact author has declared that none of the authors has any competing interests.

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