Oligomer formation from the gas-phase reactions of Criegee intermediates with hydroperoxide esters: mechanism and kinetics

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Abstract. Hydroperoxide esters, formed in the reactions of carbonyl oxides (also called Criegee intermediates, CIs) with formic acid, play a crucial role in the formation of secondary organic aerosol (SOA) in the atmosphere. However, the transformation mechanism of hydroperoxide esters in the presence of stabilized Criegee intermediates (SCIs) is not well understood. Herein, the oligomerization reaction mechanisms and kinetics of distinct SCI (CH₂OO, syn-CH₃CHOO, anti-CH₃CHOO, and (CH₃)₂COO) reactions, with their respective hydroperoxide esters and with hydroperoxymethyl formate (HPMF), are investigated in the gas phase using quantum chemical and kinetics modeling methods. The calculations show that the addition reactions of SCIs with hydroperoxide esters proceed through successive insertion of SCIs into hydroperoxide ester to form oligomers that involve SCIs as the repeated chain unit. The saturated vapor pressure and saturated concentration of the formed oligomers decrease monotonically as the number of SCIs is increased. The exothermicity of oligomerization reactions decreases significantly when the number of methyl substituents increases, and the exothermicity of anti-methyl substituted carbonyl oxides is obviously higher than that of syn-methyl substituted carbonyl oxides. The −OOH insertion reaction is energetically more feasible than the −CH insertion pathway in the SCI oligomerization reactions, and the barrier heights increase with increasing the number of SCIs added to the oligomer, except for syn-CH₃CHOO. For the reactions of distinct SCIs with HPMF, the barrier of the −OOH insertion pathway shows a dramatic decrease when a methyl substituent occurs at the anti-position, while it reveals a significant increase when a methyl group is introduced at the syn-position and dimethyl substituent. Compared with the rate coefficients of the CH₂OO + HPMF reaction, the rate coefficients increase by about 1 order of magnitude when a methyl substituent occurs at the anti-position, whereas the rate coefficients decrease by 1–2 orders of magnitude when a methyl group is introduced at the syn-position. These new findings advance our current understanding of the influence of Criegee chemistry on the formation and growth processes and the chemical compositions of SOA.
1 Introduction

Alkenes are an important class of volatile organic compounds (VOCs) that are emitted into the atmosphere from large quantities of biogenic and anthropogenic sources (Lester and Klippenstein, 2018). The reaction with ozone is one of the dominant degradation pathways for alkenes in the atmosphere (Johnson and Marston, 2008; Atkinson and Arey, 2003). Ozonolysis of alkene proceeds through the electrophilic 1,3-cycloaddition of ozone to a C=C bond of alkenes to form a primary ozonide (POZ), and then it rapidly decomposes into a carbonyl compound and a carbonyl oxide (also called Criegee intermediates, CIs; Criegee, 1975; Osborn and Taatjes, 2015; Giorio et al., 2017). Part of the initially energized CIs (∼37%–50%) may promptly dissociate to OH radicals, which are thought to be an important non-photolytic source of OH radicals in the atmosphere (Novelli et al., 2014; Liu et al., 2014). The remaining CIs (∼63%–50%) are collisionally stabilized prior to the thermal unimolecular decay (Lester and Klippenstein, 2018; Novelli et al., 2014; Anglada and Solé, 2016). The stabilized Criegee intermediates (SCIs) can proceed with bimolecular reactions with various trace species such as H₂O, NO₂, SO₂, and HCOOH to generate secondary organic aerosol (SOA), thus profoundly influencing the air quality, global climate, and human health (Osborn and Taatjes, 2015; Khan et al., 2018; Lin and Chao, 2017; Liu et al., 2019; Chhantyal-Pun et al., 2018; Gong and Chen, 2021; Taatjes, 2017).

Formic acid (HCOOH), one of the most abundant carboxylic acids, has a significant influence on rainwater acidity in remote areas, where pH reduces by 0.25–0.5 in the presence of HCOOH (Stavrakou et al., 2012; Wang et al., 2020; Chaliyakunnel et al., 2016). It also plays an important role in the formation of cloud condensation nuclei (CCN), indirectly influencing radiative forcing and climate change (Yu, 2000). The primary sources of HCOOH include biomass burning, human activities, tropical and boreal forests, as well as the secondary sources involving the photochemical oxidation of non-methane hydrocarbons, such as ketene enols, vinyl alcohol, isoprene, and terpenoids (Stavrakou et al., 2012; Wang et al., 2020; Chaliyakunnel et al., 2016; So et al., 2014; Paulot et al., 2011). According to satellite measurements, the production of HCOOH is up to 100–120 Tg yr⁻¹, and the value is expected to increase due to the acceleration of industrialization and urbanization (Stavrakou et al., 2012). Recent kinetic measurements have revealed that the reaction with HCOOH is a more important loss process for SCI than is presently assumed, especially in terrestrial equatorial areas and in high SCI concentration areas (Welz et al., 2014; Chung et al., 2019). The formed hydroperoxide esters have been identified as the low-volatility and high-oxygenated compounds, contributing to the formation and growth of SOA (Welz et al., 2014; Vansco et al., 2021; Sakamoto et al., 2017; Riva et al., 2017).

Welz et al. (2014) directly determined the rate coefficients for the reactions of CH₂OO and CH₂CHOO with formic and acetic acid by employing multiplexed photoionization mass spectrometry and cavity-enhanced broadband ultraviolet absorption spectroscopy. They found that the measured rate coefficients are in the excess of 1.0 × 10⁻¹⁰ cm³ molec⁻¹ s⁻¹, which are several orders of magnitude greater than those derived from previous experimental studies (Johnson et al., 2001; Tobias and Ziemann, 2001). Sipilä et al. (2014) conducted a competitive reaction kinetics experiment to investigate the reactions of acetone oxide ((CH₃)₂O₀) with SO₂, HCOOH, and CH₃COOH, and they concluded that the rate coefficients of the (CH₃)₂O₀ + HCOOH/CH₂OOH reactions are faster than that of the (CH₃)₂O₀ + SO₂ system by about 3 times (Sipilä et al., 2014). These high rate coefficients could make the reaction with carboxylic acids a substantial dominant chemical sink for carbonyl oxides in the atmosphere (Welz et al., 2014; Taatjes et al., 2019; Chhantyal-Pun et al., 2017). Quantum chemical calculations show that the reaction of CH₂OO with HCOOH proceeds through a facile transfer of the hydrogen atom from the acidic OH group to the terminal oxygen of CH₂OO to form hydroperoxymethyl formate (HPMF; Long et al., 2009; Vereecken, 2017; Porterfield et al., 2019). Chen et al. (2018) concluded the same by investigating the reactions of various carbonyl oxides with HCOOH and finding that the barrierless 1,4 insertion reaction is the most favorable pathway, and that the primary products are hydroperoxide esters. Caravan et al. (2020) employed high-level ab initio CCSD(T)-F12 methods to study the reaction of methyl vinyl ketone oxide (MVK oxide) with HCOOH, and they found that the barrierless net insertion of MVK oxide into HCOOH, leading to the formation of a functionalized hydroperoxide, is dominant over fragmentation to produce an alkoxy radical and OH radicals. Moreover, oligomerization reactions with hydroperoxides and peroxy radicals are identified as being one of the dominant loss processes for carbonyl oxides under atmospheric conditions (Sakamoto et al., 2013; Sadezky et al., 2008; Zhao et al., 2015; Chen et al., 2017, 2019). All the above milestone investigations provide important information for understanding the chemistry of Criegee intermediates in the presence of carboxylic acids. However, to the best of our knowledge, there are few studies on the oligomerization reactions of SCIs with hydroperoxide esters, which are important with regard to organic new particle and cloud condensation nuclei formations. Moreover, the relationship between the reactivity of SCIs and the nature of substituents remains uncertain in the SCIs oligomerization reactions.

In the present study, we mainly focus on the oligomerization reaction mechanisms and kinetics of four carbonyl oxides reactions with their respective hydroperoxide esters and with HPMF by employing quantum chemical calculations and kinetics modeling methods. For the initiation reactions of carbonyl oxides with formic acid, four kinds of pathways, including 1,4-OH insertion, 1,2-OH insertion, C-H insertion,
and C=O cycloaddition, are considered. For the oligomerization reactions of the successive insertion of carbonyl oxides into hydroperoxide esters, two types of reactions involving −O=O and −CH= inserts are taken into account. The selected carbonyl oxides, including CH₂OO, syn- and anti-CH₂CHOO, and (CH₃)₂CHOO, are anticipated upon the ozonolysis of ethylene, propylene, and 2,3-dimethyl-2-butene, whereas the hydroperoxide esters are assumed to arise from the bimolecular reactions of carbonyl oxides with formic acid in the atmosphere.

2 Computational details

2.1 Electronic structure and energy calculations

The geometries of all stationary points, including reactants (Rs), intermediates (IMs), transition states (TSs), and products (Ps), are optimized at the M06-2X/6-311+G(2df,2p) level of theory, since the M06-2X functional has a reliable performance for predicting thermochemistry, kinetics, and hydrogen bonding interactions (Zhao and Truhlar, 2008). Harmonic vibrational frequencies are performed at the same level to verify the nature of transition state (NIMAG = 1) and minimum (NIMAG = 0), and to provide zero-point vibrational energy (ZPVE) and Gibbs free energy corrections (G_corr), which are scaled by a factor of 0.98 (Alecu et al., 2010). Intrinsic reaction coordinate (IRC) calculations are carried out to verify that each transition state is connected to the desired reactant and product (Fukui, 1981). The single point energy (SPE) calculations are performed at the M06-2X/ma-TZVP level of theory based on the M06-2X/6-311+G(2df,2p) optimized geometries. Moreover, the basis set superposition error (BSSE) is performed by using the counterpoise method proposed by Boys and Bernardi (1970) to evaluate the stability of the pre-reactive complex (RC). Herein, the Gibbs free energy (G) is defined as the sum of the SPE and Gibbs correction (G = E + G_corr). Electronic energy (ΔE^e) and Gibbs free energy (ΔG^e) barriers are defined as the difference in energy between a TS and a RC (ΔE^e = E_Ts − E_Rc and ΔG^e = G_Ts − G_Rc). Reaction Gibbs free energy (ΔG^f) is defined as the difference in energy between a P and a R (ΔG = G_P − G_R).

To further assess the reliability of the selected M06-2X/ma-TZVP method for SPE calculations, the single point energies of all stationary points involved in the initiation reactions of distinct SCIs with HCOOH are recalculated at the high-accuracy CCSD(T)/6-311+G(2df,2p) and QCISD(T)/6-311+G(2df,2p) levels of theory. The calculated results are summarized in Table S1 in the Supplement. This table shows that the ΔE^e and ΔG^e obtained using the QCISD(T) method are in excellent agreement with those obtained using the CCSD(T) approach. It is therefore the reason why the energies obtained using the CCSD(T) method are used as the benchmark for comparison. The mean absolute deviations (MADs) of ΔE^e and ΔG^e between the CCSD(T) and M06-2X methods are 0.43 and 0.41 kcal mol⁻¹, respectively; the largest deviations of ΔE^e and ΔG^e are 1.0 and 1.1 kcal mol⁻¹, respectively. These results reveal that the energies obtained using the M06-2X method are close to those obtained using the CCSD(T) approach. Therefore, the M06-2X/ma-TZVP method is suitable for investigating the SCI oligomerization reactions. In the following discussion, the energies are applied in terms of Gibbs free energy to describe the reaction mechanism, unless otherwise stated. All electronic structure calculations are carried out by using the Gaussian09 program (Frisch et al., 2009). The Multiwfn program and Visual Molecular Dynamics (VMD) are utilized to analyze and visualize the molecular orbitals of the relevant species (Lu and Chen, 2012; Humphrey et al., 1996).

2.2 Kinetics calculations

The rate coefficients for the barrierless 1,4 O-H insertion reactions are computed by employing the variable–reaction–coordinate variational transition state theory (VRC-VTST; Bao and Truhlar, 2017), in which the potential energies are calculated by direct dynamics using the M06-2X/6-311+G(2df,2p) method. Rate coefficients for the SCIs + HCOOH reactions are calculated using the E, J-resolved microcanonical variational theory (E, J-μVT) using a single-faceted dividing surface. In the VRC-VTST calculations, the reaction coordinate s is defined by pivot points, which are used to orient the reactants 1 and 2. s is defined as the minimal value of r_ij, where r_ij is the distance between pivot points i and j, i is a pivot point on reactant 1, and j is a pivot point on reactant 2. Two of the pivot points are located at a distance ±d from the center of mass (COM) of SCIs, and the other two pivot points are located at a distance ±d from the COM of HCOOH, with a fixed length of 0.05, 0.10, 0.15, 0.2, and 0.25 Å. Then, for a given choice of pivot points, the variationally lowest rate coefficients are minimized with respect to s at each of the temperatures. We observed that d = 0.05 produces the best variation results, and only its value is reported in the present study.

The rate coefficients for the bimolecular reactions with the tight transition states are calculated by using the canonical transition state theory (CTST) along with one-dimensional asymmetric Eckart tunneling correction (Truhlar et al., 1996; Eckart, 1930). As shown in Fig. 1, the entrance pathway Entry 2 of the R₁R₂COO reaction with HCOOH consists of two steps, where (i) an intermediate IMent2 is formed via a barrierless process, and (ii) then it rearranges to the product Pent2 through a tight transition state TSent2. The whole reaction process can be described as Reaction (R1), as follows:

\[
R_1R_2COO + HCOOH \overset{k_1}{\longrightarrow} IMent2 \overset{k_2}{\rightarrow} Pent_2, \quad (R1)
\]

assuming that the rapid equilibrium is established between the IMent2 and reactants. According to the steady-state ap-
proximation (SSA), the total rate coefficient is approximately expressed as Eq. (1) (Zhang et al., 2012):
\[
k_{\text{tot}} = \frac{k_1}{k_{-1} + k_2} \approx \frac{k_1}{k_{-1}}k_2 = K_{eq} k_2.
\]
(1)

The equilibrium constant \(K_{eq}\) is written as Eq. (2):
\[
K_{eq} = \sigma \frac{Q_{IM}(T)}{Q_{R_1}(T)Q_{R_2}(T)} \exp \left(\frac{G_R - G_{IM}}{RT}\right),
\]
(2)

where \(\sigma\) refers to reaction symmetry number, \(Q_{IM}(T)\), \(Q_{R_1}(T)\), and \(Q_{R_2}(T)\) denote the partition functions of intermediate, reactants \(R_1\) and \(R_2\) are equal to the multiplication of translational, rotational, vibrational, and electronic partition functions \((Q = Q_{rot}Q_{vib}Q_{trans}Q_{elec})\) (Mendes et al., 2014). \(T\) is the temperature in Kelvin, \(R\) is the ideal gas constant, and \(G_R\) and \(G_{IM}\) are the total Gibbs free energies of reactant and intermediate, respectively. The rate coefficient calculations are performed with the Polyrate 2017-C and KiSThelP 2019 programs (Canneaux et al., 2013; Zheng et al., 2018).

3 Results and discussion

3.1 Initiation reactions of distinct SCIs with HCOOH

The reaction with HCOOH is one of the dominant loss processes for SCIs and is expected to trigger the formation of SOA in the atmosphere (Chhantyal-Pun et al., 2018; Cabezas and Endo, 2020; Zhao et al., 2018; Zhou et al., 2019). The potential energy surface (PES) of distinct SCI (CH₂OO, syn- and anti-CH₃CHOO, and (CH₃)_2COO) reactions with HCOOH is drawn in Fig. 1. The geometries of all stationary points are displayed in Fig. S1 in the Supplement. The relative free energy of each stationary point and free energy barrier (\(\Delta G^f\)) of each elementary reaction are summarized in Table 1. As shown in Fig. 1, the bimolecular reaction of distinct SCIs with HCOOH proceeds via four possible pathways, namely (1) 1,4 O-H insertion (Entry 1), (2) 1,2 O-H insertion (Entry 2), (3) C-H insertion (Entry 3), and (4) C=O cycloaddition (Entry 4). For Entry 1, the addition reaction of CH₂O with HCOOH proceeds through the 1,4 O-H insertion of CH₂OO into HCOOH to form a hydroperoxide ester H(C(O)O-CH₂OO-H with an exoergicity of 37.6 kcal mol⁻¹. The formation of H(C(O)O-CH₂OO-H is obtained through a concerted process of O₂-H₂ bond breaking in the HCOOH and O₂-H₂ and C₂-O₁ bonds forming. Despite an attempt by various methods, the corresponding transition state is still not located through the efforts of optimization. To further validate the barrierless process of 1,4 O-H insertion reaction, a relaxed scan over the O-H and C-O bonds is performed at the M06-2X/6-311+G(2df,2p) level of theory. The scans start from the optimized structure of the adduct products, and the O-H and C-O bond lengths are then increased in steps of 0.10 Å, while other geometric parameters are fully optimized. The zero of energy is set to be the energy of the adduct products. The electronic potential energy profiles along the O-H and C-O dissociation coordinate are presented in Fig. S2. As seen in Fig. S2a, the electronic potential energy of the minimum potential energy path (MEP) decreases monotonically when the bond length of the O-H and C-O bonds decreases, suggesting that the 1,4 O-H insertion reaction of CH₂OO with HCOOH is indeed barrierless. A similar conclusion is also obtained from the electronic potential energy profiles for the anti-CH₃CHOO + HCOOH, sym-CH₃CHOO + HCOOH, and (CH₃)₂COO + HCOOH (Fig. S2b–d) reactions that 1,4 O-H insertion reactions are barrierless. This conclusion is further supported by the analogous reaction systems that the 1,4 O-H insertion reactions of carbonyl oxides with carboxylic acids are a barrierless process, including the concerted hydrogen atom transfer and new C-O bond formation (Chhantyal-Pun et al., 2017; Long et al., 2009; Vereecken, 2017; Cabezas and Endo, 2019; Lin et al., 2019).

The exothermicities of 1,4 O-H insertion reactions of distinct SCIs with HCOOH are assessed by the reaction enthalpies (\(\Delta_r H_{298}^o\)), which are defined as the difference between the enthalpies of formation of the products and reactants (\(\Delta_r H_{298}^o = \sum \Delta f H_{298}^o - \sum \Delta f H_{298}^o\)) of the products and reactants. To the best of our knowledge, there are no literature values available on the enthalpies of formation of carbonyl oxides and hydroperoxide esters, except the simplest carbonyl oxide CH₂OO. Therefore, the isodesmic reaction method is adopted to obtain the enthalpies of formation, and the results are listed in Table S2. An isodesmic reaction is a hypothetical reaction in which the type of chemical bonds in the reactants is similar to those of chemical bonds in the products. The following isodesmic reaction is constructed because the experimental values of H₂, CH₄, and H₂O are available (\(\Delta f H_{298}^o(H_2) = 0.00 \text{ kcal mol}^{-1}\), \(\Delta f H_{298}^o(CH_4) = -17.82 \text{ kcal mol}^{-1}\), and \(\Delta f H_{298}^o(H_2O) = -57.79 \text{ kcal mol}^{-1}\)).

\[
\text{SCIs} + nH_2 \rightarrow CH_4 + nH_2O.
\]

As seen in Table S2, the enthalpy of formation of CH₂OO is calculated to be 23.23 kcal mol⁻¹, which is in good agreement with the available literature values (Chen et al., 2016; Karton et al., 2013). This result implies that the theoretical method utilized herein is reasonable for the prediction of the thermochemical parameters. The enthalpies of formation of carbonyl oxides and hydroperoxide esters significantly decrease when increasing the number of methyl groups. Notably, the decreased values in the enthalpies of formation of carbonyl oxides are greater than those of hydroperoxide esters under the condition of the same number of methyl groups. For example, the enthalpy of formation of anti-CH₃CHOO decreases by 12.95 kcal mol⁻¹ compared to the enthalpy of formation of CH₂OO (23.23 kcal mol⁻¹),
and the enthalpy of formation of Pent1b decreases by 12.12 kcal mol$^{-1}$ compared to the enthalpy of formation of Pent1a (−112.08 kcal mol$^{-1}$). The reaction enthalpies of the reactions of distinct SCIs with HCOOH have decreases of the order of −44.69 (CH$_2$OO + HCOOH → Pent1a) < −43.86 (anti-CH$_3$CHOO + HCOOH → Pent1b) < −38.13 (syn-CH$_3$CHO + HCOOH → Pent1c) < −37.12 kcal mol$^{-1}$ (CH$_3$)$_2$COO + HCOOH → Pent1d), indicating that the reaction enthalpies are highly dependent on the number and location of methyl groups. The trend in reaction enthalpies is consistent with the trend in the enthalpies of formation of carbonyl oxides.

For Entry 2, each addition reaction starts with the formation of a pre-reactive hydrogen bonded complex, IMent2, in the entrance channel. Then it immediately converts into product Pent2 through the 1,2 O-H insertion transition state. The formation of Pent2 is obtained via a concerted process of O$_2$-H$_2$ bond rupture in the HCOOH and O$_4$-H$_2$ and C$_2$-O$_2$ bonds forming. The reaction barrier $\Delta G^\neq$ has increases of the order of 10.0 (CH$_2$OO) < 13.0 (anti-CH$_3$CHOO) < 14.6 (syn-CH$_3$CHO) ≈ 14.4 ((CH$_3$)$_2$COO) kcal mol$^{-1}$, suggesting that the parent CH$_2$OO + HCOOH reaction is favored kinetically. Compared with the barrier of the parent system, the barrier increases by 3.0 kcal mol$^{-1}$ when a methyl substitution occurs at the R$_1$ position, and the barrier increases by ~5 kcal mol$^{-1}$ when a methyl group is introduced at the R$_2$ position and dimethyl substituent. The aforementioned result implies that the methyl-substituted CH$_2$OO hinders the 1,2 O-H insertion of carbonyl oxides into formic acid. Notably, the exothermicity decreases significantly as the number of the methyl group is increased. The products Pent1 and Pent2 formed from Entries 1 and 2 are two conformations that differ in the orientation of the −C(O)H moiety over the −OOH group. The calculated result shows that Pent1 is more stable than Pent2 in energy due to the existence of intramolecular hydrogen bond between the hydrogen atom of −OOH group and carbonyl oxygen atom.

For Entry 3, the addition reaction begins with the formation of a pre-reactive complex, IMent3, in the entrance channel, and then it surmounts a barrier to reaction. However, the barriers of C-H insertion reactions are significantly high (21.8–27.6 kcal mol$^{-1}$), such that they are of less importance in the atmosphere. The high reaction barriers might be attributed to the large bond dissociation energy (BDE) of C-H bond in the formic acid. For Entry 4, the addition reaction proceeds through a cyclization process of a C$_2$-O$_1$ and O$_4$-C$_1$ bond forming to produce a five-membered ring compound Pent4. The barrier of the C=O cycloaddition reaction in the CH$_2$OO + HCOOH reaction is 5.8 kcal mol$^{-1}$, which is lower than that of the corresponding channels in Entry 2 and Entry 3 by 4.2 and 16.0 kcal mol$^{-1}$, respectively. The result reveals that the C=O cycloaddition reaction is feasible kinetically. A similar conclusion is also obtained from the reactions of HCOOH with syn- and anti-CH$_3$CHOO and (CH$_3$)$_2$COO in that the C=O cycloaddition reactions are favored over 1,2 O-H and C-H insertion reactions.

The rate coefficients of each elementary pathway included in the initiation reactions of distinct SCIs with HCOOH are tabulated in Tables S3–S6. The total rate coefficient is equal to the sum of the rate coefficient of each elementary pathway. As shown in Table S3, the total rate coefficients $k_{tot-CH$_3$CHO}$ of CH$_2$OO reaction with HCOOH are in excess of 1.0 × 10$^{-10}$ cm$^3$ molec.$^{-1}$ s$^{-1}$, and they exhibit a slightly negative temperature dependence in the temperature range of 273–400 K. At room temperature, $k_{tot-CH$_3$CHO}$ is estimated to be 1.29 × 10$^{-10}$ cm$^3$ molec.$^{-1}$ s$^{-1}$, which is in good agreement with the experimental values reported by Welz et al. (2014; [1.1±0.1] × 10$^{-10}$), Chung et al. (2019; [1.4±0.3] × 10$^{-10}$), and Peltola et al. (2020; [1.0±0.3] × 10$^{-10}$). $k_{TS_{ent1}}$ is approximately equal to $k_{tot-CH$_3$CHO}$ in the whole temperature range, and it decreases in the range from 1.34 × 10$^{-10}$ (273 K) to 1.05 × 10$^{-10}$ (400 K) cm$^3$ molec.$^{-1}$ s$^{-1}$ with increasing temperature. $k_{TS_{ent1}}$ is several orders of magnitude greater than $k_{TS_{ent2}}$, $k_{TS_{ent3}}$, and $k_{TS_{ent4}}$ over the temperature range from 273 to 400 K. The result again shows that the barrierless 1,4 O-H insertion reaction is predominant. It should be noted that, although the barrier of Entry 2 is 4.2 kcal mol$^{-1}$ higher than that of Entry 4, $k_{TS_{ent2}}$ is merely about 1–2 fold smaller than $k_{TS_{ent4}}$. The reason is ascribed to the fact that the C=O cycloaddition reaction is entropically unfavorable (Vereecken, 2017).

Equivalent to the case of the reaction of CH$_2$OO with HCOOH, the total rate coefficient $k_{tot-anti}$ of the anti-CH$_3$CHOO reaction with HCOOH also decreases slightly with the temperature increase (Table S4). This table in the Supplement shows that Entry 1 is kinetically favored over Entries 2, 3, and 4, and Entry 2 is competitive with Entry 4 in the temperature range of 273–400 K. A similar conclusion is also obtained from the results of the rate coefficients for the reactions of syn-CH$_3$CHOO and (CH$_3$)$_2$COO with HCOOH in that Entry 1 is the dominant pathway (Tables S5–S6). It is worth mentioning that the competition of Entry 2 is significantly greater than that of Entry 4 in the syn-CH$_3$CHOO + HCOOH and (CH$_3$)$_2$COO + HCOOH systems. Based on the above discussions, it can be concluded that the relative importance of different pathways is highly dependent on the number and location of methyl substituents in the carbonyl oxides. Notably, the rate coefficient of each elementary pathway included in the anti-CH$_3$CHOO + HCOOH reaction is several orders of magnitude greater than that of the corresponding channel involved in the other SCIs + HCOOH systems. It is because anti-CH$_3$CHOO is substantially more reactive toward HCOOH than other SCIs. A similar phenomenon has also observed from the reactivity of anti-CH$_3$CHOO toward water and SO$_2$ (Taatjes et al., 2013; Long et al., 2016; Huang et al., 2015; Cabezas and Endo, 2018). At ambient temperature, the total rate coefficients of HCOOH reactions with anti-CH$_3$CHOO, syn-CH$_3$CHOO, and (CH$_3$)$_2$COO are estimated to be 5.22, 14533
Table 1. Relative free energies of stationary points and free energy barriers \((\Delta G^\circ)\) at 298 K (in kcal mol\(^{-1}\)) for the various SCI \((R_1R_2\text{COO, } R_1, \text{ and } R_2 = \text{H, CH}_3)\) reactions with HCOOH calculated at the M06-2X/ma-TZVP/M06-2X/6-311+G(2df,2p) level of theory.

<table>
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<th>Entry</th>
<th>(R_1)</th>
<th>(R_2)</th>
<th>Iment</th>
<th>TSent</th>
<th>Pent</th>
<th>(\Delta G^\circ)</th>
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2.18, and 3.97 \(\times 10^{-10}\) cm\(^3\) molec\(^{-1}\) s\(^{-1}\), respectively, which are consistent with the prior experimental measurements of 5±3, 2.5±0.3, and 4.5±0.9 \(\times 10^{-10}\) cm\(^3\) molec\(^{-1}\) s\(^{-1}\) (Welz et al., 2014; Sipilä et al., 2014).

In summary, the barrierless 1,4 O-H insertion reaction is the dominant pathway in the initiation reactions of distinct SCIs with HCOOH. This conclusion is consistent with the recent experimental results derived from the reactions of formic acid with methacrolein oxide (MACR-OO) and methyl vinyl ketone oxide (MVK-OO) that the 1,4 addition mechanism is energetically favorable (Vansco et al., 2021; Caravan et al., 2020). Therefore, in the present study, the adduct products Pent1 forming the barrierless 1,4 O-H insertion of carbonyl oxides into HCOOH are selected as the model compounds to investigate the oligomerization reaction mechanisms of carbonyl oxides reactions with hydroperoxide esters.

3.2 The reactions of distinct SCIs with their respective hydroperoxide esters

The formed hydroperoxide ester has two possible unimolecular decay pathways. The first is the direct O-O bond rupture, resulting in the formation of oxymethyleneformate and OH radicals (Vereeeken, 2017). The second is the –OH fragment binding to adjacent hydrogen atom, leading to the formation of anhydride and H\(_2\)O (Aplincourt and Ruiz-López, 2000; Neeb et al., 1998). However, the barriers of these two unimolecular reactions are extremely high, such that they are of less importance in the atmosphere. The formed hydroperoxide ester possess –OOG and –OC(O)H groups, and both of them can serve as the reactive moieties to react with carbonyl oxides, giving rise to the formation of oligomers. In the present study, we mainly consider two types of pathways, i.e., (a) –OOG insertion and (b) –CH insertion, while the C=O cycloaddition reaction is not taken into account because it is entropically unfavorable (Vereeeken, 2017; Lin et al., 2019). The aforementioned reactions are discussed in detail in the following subsections.

3.2.1 The reactions of 2CH\(_2\)OO with Pent1a

The simplest carbonyl oxide, CH\(_2\)OO, originates from the reaction of all terminal alkenes with ozone (ozonolysis) in the atmosphere (Lin and Chao, 2017). The reaction with HCOOH is expected to be one of the dominant loss processes for CH\(_2\)OO, and the main product is Pent1a (also called HPMF; Welz et al., 2014; Cabezas and Endo, 2019). A schematic PES for the addition reaction 2CH\(_2\)OO + Pent1a is shown in Fig. 2, and the optimized geometries of all stationary points are displayed in Fig. S3. As seen in Fig. 2, the successive insertion of CH\(_2\)OO into Pent1a eventually leads to the formation of oligomers P2a and P2b composed of CH\(_2\)OO as the repeat unit. These oligomerization reactions are strongly exothermic and spontaneous (> 83 kcal mol\(^{-1}\)), implying that they are feasible thermodynamically.

The addition reaction 2CH\(_2\)OO + Pent1a initially proceeds through two possible pathways, namely (1) –OOG insertion reaction R1a and (2) –CH insertion reaction R1b. For the –OOG insertion reaction R1a, the pre-reactive intermediate IM1a with a seven-membered ring structure is formed in the entrance channel, which is stabilized by the hydrogen bond interactions between the H\(_4\) atom of Pent1a and the O\(_6\) atom of CH\(_2\)OO (\(D_{\text{O}_6\text{H}_4} = 1.706 \text{ Å}\)) and between the H\(_6\) atom of CH\(_2\)OO and the O\(_3\) atom of Pent1a (\(D_{\text{O}_3\text{H}_6} = 2.115 \text{ Å}\)). Then IM1a converts into P1a (\(C_3\text{H}_6\text{O}_6, \text{HC(O)O-(CH}_2\text{OO)}_2\text{-H}\)) via a concerted process of the O\(_4\)-H\(_4\) bond breaking in the Pent1a and O\(_4\)-C\(_3\) and H\(_4\)-O\(_6\) bonds forming with a barrier of 8.1 kcal mol\(^{-1}\). For the –CH insertion reaction R1b, the pre-reactive intermediate IM1b with a seven-membered ring structure is formed in the entrance channel, which is stabilized by the van der Waals (vdW) interactions between the O\(_3\) atom of Pent1a and the C\(_3\) atom of CH\(_2\)OO (\(D_{\text{O}_3\text{C}_3} = 2.602 \text{ Å}\)) and between the O\(_6\) atom of CH\(_2\)OO and the C\(_1\) atom of Pent1a (\(D_{\text{O}_6\text{C}_1} = 2.608 \text{ Å}\)). Due to the absence of the hydrogen bond in IM1b, the energy of IM1b is lower than that of IM1a by 3.0 kcal mol\(^{-1}\). IM1b transforms into P1b (\(C_3\text{H}_6\text{O}_6, \text{HO}_2\text{CH}_2\text{O(C(O)CH}_2\text{OOH)}\)) via a concerted process of a C\(_1\)-H\(_1\) bond breaking in the Pent1a and C\(_1\)-C\(_3\) and H\(_1\)-O\(_6\) bonds forming with a barrier of 21.5 kcal mol\(^{-1}\). By comparing the barriers of reactions R1a and R1b, it can be concluded that the –OOG insertion reaction is favored over the –CH insertion reaction. The high reaction barrier of reaction R1b is attributed to the

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Figure 1. Schematic PES for the possible entrance pathways of the initiation reactions of HCOOH with various SCIs (black, pink, blue, and red lines represent the 1,4 O-H insertion, 1,2 O-H insertion, C-H insertion, and C=O cycloaddition reactions, respectively).

large bond dissociation energy (BDE) of the C-H bond in the Pent1a. To gain further insight into the reaction mechanism of reaction R1a, the natural bond orbital (NBO) analysis of the donor–acceptor orbitals involved in the TS1a is performed using the M06-2X wave function. The possible donor–acceptor interactions are estimated by using the second-order perturbation theory. As illustrated in Fig. S4, the strong interactions are identified as the interaction of the lone pair orbital of O atom and the antibonding orbital of O-H bond and the interaction of the lone pair orbital of O atom and the antibonding orbital of C=O bond.

Similarly, the addition reaction CH2OO + P1a proceeds through the formation of the pre-reactive intermediates IM2a and IM2b in the entrance channel, which are stabilized by a hydrogen bond between the terminal oxygen atom of CH2OO and the reacting hydrogen atom of P1a and a van der Waals (vdW) interaction between the central carbon atom of CH2OO and the carbonyl oxygen atom of P1a. The relative energies of IM2a and IM2b, with respect to the separate reactants P1a and CH2OO, are −1.2 and 3.2 kcal mol⁻¹, respectively, below the energies of the initial reactants 2CH2OO, and Pent1a are 41.6 and 37.2 kcal mol⁻¹, respectively. Then they immediately transform into the respective products P2a and P2b through the −OOH and −CH insertion transition states TS2a and TS2b, with the barriers of 10.1 and 21.6 kcal mol⁻¹. This result again shows that the −OOH insertion reaction is favored kinetically. It deserves mentioning that the barrier of −OOH insertion reaction increases as the number of CH2OO is increased. From the viewpoint of the geometrical parameters of TS2a and TS2b, the breaking O-H and C-H bonds are elongated by 14.8 % and 20.6 %, respectively, with respect to the equilibrium structures of IM2a and IM2b, while the forming C-O and C-C bond lengths are 2.013 and 2.264 Å, respectively. The result reveals that TS2a and TS2b are structurally reactant-like, which are consistent with the Hammond’s (1955) hypothesis that the earlier transition states are generally exothermic.

3.2.2 The reactions of anti-CH3CHO with Pent1b

The methyl-substituted CH2OO has two conformers, syn- and anti-CH3CHO, that distinguish by the orientation of methyl group relative to the terminal oxygen (Taatjes et al., 2013). syn-CH3CHO is more stable than anti-CH3CHO in energy due to the existence of intramolecular hydrogen bond (Long et al., 2016). The activation enthalpy of the interconversion between syn-CH3CHO and anti-CH3CHO is up to 38.5 kcal mol⁻¹, implying that they can be treated as independent species in the atmosphere (Long et al., 2016; Yin and Takahashi, 2017). A schematic PES for the addition reaction 2anti-CH3CHO + Pent1b is presented in Fig. 3, and the optimized geometries of all stationary points are shown in Fig. S5. As shown in Fig. 3, the addition reaction 2anti-CH3CHO + Pent1b proceeds through successive insertion of anti-CH3CHO into Pent1b, leading to the formation of oligomers P4a and P4b that contain anti-CH3CHO as chain unit. The first anti-CH3CHO addition reaction begins with the formation of IM3a and IM3b in the entrance channel, which lie at −2.2 and 2.4 kcal mol⁻¹, respectively,
with respect to the separate reactants. Then the IM3a and IM3b transform into P3a and P3b via $-\text{OOH}$ and $-\text{CH}$ insertion transition states TS3a and TS3b, with the barriers of 5.6 and 20.3 kcal mol$^{-1}$, respectively. This result shows that the $-\text{OOH}$ insertion reaction is more favorable than the $-\text{CH}$ insertion pathway. Compared with the barriers of R1a and R1b in the $2\text{CH}_2\text{OO} + \text{Pent}1a$ reaction, the barriers of R3a and R3b decrease by 2.5 and 1.2 kcal mol$^{-1}$ when a methyl group is introduced at the anti-position. The result reveals that the reactivity of anti-$\text{CH}_3\text{CHOO}$ is substantially higher than that of CH$_2$OO. This conclusion is further supported by the findings of other studies, which have reported that anti-$\text{CH}_3\text{CHOO}$ is more reactive toward H$_2$O, SO$_2$, and H$_2$O$_2$ than CH$_2$OO (Chen et al., 2017; Taatjes et al., 2013; Huang et al., 2015). Similarly, the secondary anti-$\text{CH}_3\text{CHOO}$ addition reaction starts with the formation of IM4a and IM4b in the entrance channel with the 0.1 and 3.7 kcal mol$^{-1}$ stability, followed by conversion to the final products P4a and P4b through the $-\text{OOH}$ and $-\text{CH}$ insertion reactions R4a and R4b. The transition states TS4a and TS4b lie at 7.0 and 21.0 kcal mol$^{-1}$, respectively, above the energies of the respective intermediates of IM4a and IM4b. This result again shows that the $-\text{OOH}$ insertion reaction is the most favorable channel, and the barrier increases as the number of anti-$\text{CH}_3\text{CHOO}$ is increased.

### 3.2.3 The reactions of syn-$\text{CH}_3\text{CHOO}$ with Pent1c

Equivalent to the 2anti-$\text{CH}_3\text{CHOO} + \text{Pent}1b$ reaction, the addition reaction 2syn-$\text{CH}_3\text{CHOO} + \text{Pent}1c$ has similar transformation pathways and is thus briefly discussed in the present study. From Fig. 4, it can be seen that the addition reaction 2syn-$\text{CH}_3\text{CHOO} + \text{Pent}1c$ undergoes change via the successive insertion of syn-$\text{CH}_3\text{CHOO}$ into Pent1c to form P6a and P6b that involves syn-$\text{CH}_3\text{CHOO}$ as the repeating unit. The most favorable pathway is that the breakage of the O4-H6 bond in the $-\text{OOH}$ group of Pent1c occurs simultaneously with the insertion of the first syn-$\text{CH}_3\text{CHOO}$ into Pent1c to form P5a, followed by the insertion of the secondary syn-$\text{CH}_3\text{CHOO}$ into P5a to produce P6a. The barriers of these two $-\text{OOH}$ insertion reactions R5a and R6a are 13.8 and 11.8 kcal mol$^{-1}$, respectively, which are higher than those of R3a and R4a in the 2anti-$\text{CH}_3\text{CHOO} + \text{Pent}1b$ system by 8.2 and 4.8 kcal mol$^{-1}$, respectively. The result reveals that the reactivity of syn-$\text{CH}_3\text{CHOO}$ is substantially lower than that of anti-$\text{CH}_3\text{CHOO}$. Notably, the barrier of the favorable $-\text{OOH}$ insertion pathway decreases with increasing the number of syn-$\text{CH}_3\text{CHOO}$ in the 2syn-$\text{CH}_3\text{CHOO} + \text{Pent}1c$ reaction, which is contrary to the case of the $2\text{CH}_2\text{OO} + \text{Pent}1a$ and 2anti-$\text{CH}_3\text{CHOO} + \text{Pent}1b$ reactions.
Figure 3. PES ($\Delta G$ and $\Delta E$) for the $2\text{anti-CH}_3\text{CHOO} + \text{Pent1b}$ reaction at the M06-2X/ma-TZVP//M06-2X/6-311+G(2df,2p) level of theory.

Figure 4. PES ($\Delta G$ and $\Delta E$, in italics) for the $2\text{syn-CH}_3\text{CHOO} + \text{Pent1c}$ reaction at the M06-2X/ma-TZVP//M06-2X/6-311+G(2df,2p) level of theory.
3.2.4 The reactions of 2(CH\textsubscript{3})\textsubscript{2}COO with Pent1d

The dimethyl-substituted Criegee intermediate, (CH\textsubscript{3})\textsubscript{2}COO, is generated from the ozonolysis of 2.3-dimethyl-2-butene in the atmosphere (Lester and Klippenstein, 2018; Drozd et al., 2017; Long et al., 2018). The bimolecular reaction of (CH\textsubscript{3})\textsubscript{2}COO with water is not fast enough \((k < 1.5 \times 10^{-16} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1})\), while the reaction of (CH\textsubscript{3})\textsubscript{2}COO with HCOOH has a near-gas-kinetic-limit rate \((k = 5.4 \times 10^{-10} \text{ cm}^3 \text{ molec}^{-1} \text{ s}^{-1})\) (Huang et al., 2015). The result implies that a fraction of (CH\textsubscript{3})\textsubscript{2}COO may survive under high humidity environments and react with HCOOH, leading to the formation of hydroperoxide ester Pent1d. A schematic PES for the addition reaction 2 (CH\textsubscript{3})\textsubscript{2}COO + Pent1d is plotted in Fig. 5, and the optimized geometries of all stationary points are shown in Fig. S7.

As seen in Fig. 5, the addition reaction 2 (CH\textsubscript{3})\textsubscript{2}COO + Pent1d starts with the formation of complexes IM\textsubscript{7}a and IM\textsubscript{7}b, which lie at 1.9 and 2.4 kcal mol\textsuperscript{-1}, respectively, above the energies of the separate reactants. Then they subsequently transform into products P7a and P7b through the \(-\text{OOH}\) and \(-\text{CH}\) insertion transition states TS\textsubscript{7}a and TS\textsubscript{7}b, with barriers of 12.2 and 26.4 kcal mol\textsuperscript{-1}. This result again shows that the \(-\text{OOH}\) insertion reaction is favored over the \(-\text{CH}\) insertion pathway. A similar conclusion is also obtained from the secondary (CH\textsubscript{3})\textsubscript{2}COO addition reaction that the \(-\text{OOH}\) insertion reaction is the dominant pathway. It is of interest to compare the barriers of \(-\text{OOH}\) insertion reactions in the (CH\textsubscript{3})\textsubscript{2}COO + Pent1d system with those of the analogous reactions in other SCIs + Pent1 reactions. It can be found that the barriers have decreases of the order of \textit{syn}-CH\textsubscript{3}CHOO \(>\) (CH\textsubscript{3})\textsubscript{2}COO \(>\) CH\textsubscript{2}OO \(>\) anti-CH\textsubscript{3}CHOO in the first-step SCI addition reaction, while they become (CH\textsubscript{3})\textsubscript{2}COO \(>\) \textit{syn}-CH\textsubscript{3}CHOO \(>\) CH\textsubscript{2}OO \(>\) anti-CH\textsubscript{3}CHOO in the second-step SCI addition pathway. The result shows that the reactivity of SCIs is significantly affected by the number and location of methyl substituents.

A similar conclusion is also obtained from the thermodynamic parameters that the exothermicity of \(-\text{OOH}\) insertion reactions significantly decreases with increasing the number of methyl substituents, and the exothermicity of \textit{anti}-methyl substituted carbonyl oxide is obviously higher than that of \textit{syn}-methyl substituted carbonyl oxide.

3.3 The reactions of distinct SCIs with Pent1a and implications in atmospheric chemistry

To further elucidate the effect of the number and location of methyl substituents on the reactivity of carbonyl oxides toward hydroperoxide esters, Pent1a (also called HPMF) is selected as the model compound since it is the simplest hydroperoxide ester formed from the barrierless reaction of the 1,4 O-H insertion of CH\textsubscript{2}OO into HCOOH. As mentioned above, \(-\text{OOH}\) insertion reaction in the oligomerization reactions is the most favorable pathway. Therefore, this type of reaction is merely considered in the reactions of distinct SCIs with Pent1a. The corresponding PES and the optimized geometries of all stationary points are displayed in Figs. 6 and S8, respectively. As seen in Fig. 6, each pathway starts with the formation of a pre-reactive intermediate, and then it overcomes a modest barrier to reaction. The barrier of the reaction of CH\textsubscript{2}OO with Pent1a is calculated to be 8.1 kcal mol\textsuperscript{-1}, which is higher than that of the \textit{anti}-CH\textsubscript{3}CHOO + Pent1a reaction by 2.5 kcal mol\textsuperscript{-1}. The reason for the low barrier can be explained by the natural population analysis (NPA) atomic charges, as presented in Fig. S9. As seen in Fig. S9, the charges of the central carbon atom C\textsubscript{1} and the terminal oxygen atom O\textsubscript{1} of CH\textsubscript{2}OO are 0.186 e and -0.459 e, respectively, indicating that CH\textsubscript{2}OO is indeed a zwitterion. The C\textsubscript{1} atom charge becomes more negative (-0.497 e), when a methyl substituent occurs at the \textit{anti}-position. This result suggests that the \textit{anti}-methyl substituent enhances the characteristic of the carbonyl oxide zwitterion and reduces the reaction barriers. Compared with the barrier of the CH\textsubscript{2}OO + Pent1a reaction, the barriers increase by about 3.0 kcal mol\textsuperscript{-1} when a methyl group is introduced at the \textit{syn}-position and dimethyl substituent. Although \textit{syn}-methyl and dimethyl substituent promote the raise of carbonyl oxides zwitterion, the steric hindrance effect and intramolecular hydrogen bond are obviously dominant for \textit{syn}-CH\textsubscript{3}CHOO and (CH\textsubscript{3})\textsubscript{2}COO, which is not thus conducive to the nucleophilic attack of hydroperoxide esters. It is worth noting that the exothermicity of distinct SCIs reactions with Pent1a obviously decreases as the number of methyl group is increased, and the exothermicity of \textit{anti}-methyl substituent is higher than that of \textit{syn}-methyl substituent.

The rate coefficients of distinct SCIs reactions with Pent1a are calculated in the temperature range of 273–400 K, as summarized in Table S7. This table shows that the rate coefficients \(k_{\text{R1a}}\) of the CH\textsubscript{2}OO + Pent1a reaction (R1a) decrease in the range of \(5.0 \times 10^{-11}\) (273 K) to \(5.0 \times 10^{-12}\) cm\textsuperscript{3} molec\textsuperscript{-1} s\textsuperscript{-1} (400 K) with increasing temperature. A similar phenomenon is also observed from the rate coefficients of Pent1a reactions with \textit{anti}-CH\textsubscript{3}CHOO (R9), \textit{syn}-CH\textsubscript{3}CHOO (R10), and (CH\textsubscript{3})\textsubscript{2}COO (R11) in that they exhibit a slightly negative temperature dependence. \(k_{\text{R9}}\) is several orders of magnitude greater than \(k_{\text{R1a}}, k_{\text{R10}}\) and \(k_{\text{R11}}\) in the whole temperature range, suggesting that the bimolecular reaction \textit{anti}-CH\textsubscript{3}CHOO + Pent1a (R9) is favored kinetically. Compared with the rate coefficients of R1a, the rate coefficients increase by about 1 order of magnitude when a methyl substituent occurs at the \textit{anti}-position, whereas the rate coefficients decrease by 1 to 2 orders of magnitude when a methyl group is introduced at the \textit{syn}-position. It should be noted that, although the barrier of R10 is nearly identical to that of R11, \(k_{\text{R10}}\) is 1 to 2 orders of magnitude lower than \(k_{\text{R11}}\) in the entire temperature range. This is probably because the rate coefficients are mediated by pre-reactive intermediates so that IM11 is more stable than IM10 in energy.
It is of interest to assess whether the reactions of distinct SCIs with HPMF can compete well with the losses to reactions with trace species (e.g., \( \text{H}_2\text{O}, \text{HCOOH}, \) and \( \text{SO}_2 \)) because it is well known that the reactions with trace species are expected to be the dominant chemical sinks for SCIs in the atmosphere (Taatjes et al., 2013; Long et al., 2016). The reported concentrations of coreactant, the rate coefficients \( k \), and the effective pseudo-first-order rate constants \( k_{\text{eff}} = k([\text{coreactant}]) \) for the reactions of distinct SCIs with \( \text{H}_2\text{O}, \text{HCOOH}, \text{SO}_2, \) and HPMF are summarized in Table 2. As seen in Table 2, the rate coefficient of a particular SCI reaction with trace species is strongly dependent on its structure. The methyl group substitution may alter the rate coefficient by several to tens of times. The atmospheric concentrations of \( \text{H}_2\text{O}, \text{HCOOH}, \) and \( \text{SO}_2 \) in tropical forest environments are measured to be \( 3.9-6.1 \times 10^{17} \), \( 5.0-10 \times 10^{10} \) and \( 1.7-9.0 \times 10^{10} \) molec. cm\(^{-3} \), respectively (Vereecken et al., 2012). For the reactions of \( \text{CH}_2\text{OO} \) with \( \text{H}_2\text{O}, \text{HCOOH}, \) and \( \text{SO}_2 \), the experimental rate coefficients are determined to be \( < 1.5 \times 10^{-15}, [1.1 \pm 0.1] \times 10^{-10} \) and \( [3.9 \pm 0.7] \times 10^{-11} \) cm\(^3\) molec.\(^{-1}\) s\(^{-1} \), respectively (Welz et al., 2012, 2014; Chao et al., 2015), which translate into \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{H}_2\text{O}), k_{\text{eff}}(\text{CH}_2\text{OO}+\text{HCOOH}), \) and \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{SO}_2) \) of \( 5.9-9.2 \times 10^{2}, 5.5-11, \) and \( 0.7-3.5 \) s\(^{-1} \), respectively. The result reveals that the reaction of \( \text{CH}_2\text{OO} \) with \( \text{H}_2\text{O} \) is the most important bimolecular reaction. \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{HCOOH}) \) is greater, by a factor of 3–8, than \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{SO}_2) \), indicating that the \( \text{CH}_2\text{OO} \) reaction with HCOOH is favored over reaction with \( \text{SO}_2 \). A similar conclusion is also obtained from the results of \( k_{\text{eff}} \) for the reactions of \( \text{anti-CH}_2\text{CHOH}, \text{syn-CH}_2\text{CHOH}, \text{CH}_3\text{CHOH}, \) and \( \text{(CH}_3)_2\text{COO} \) with \( \text{H}_2\text{O}, \text{HCOOH}, \) and \( \text{SO}_2 \) in that SCI reactions with \( \text{H}_2\text{O} \) are faster than with HCOOH, which, in turn, are faster than with \( \text{SO}_2 \).

According to the results shown in the Table 2, the room temperature rate coefficient for the reaction of \( \text{CH}_2\text{OO} \) with HPMF is calculated to be \( 2.7 \times 10^{-11} \) cm\(^3\) molec.\(^{-1}\) s\(^{-1} \). However, to the best of our knowledge, the atmospheric concentration of HPMF has not been reported up to now. We assume that the concentration of HPMF is approximately equal to the atmospheric concentration of SCIs, since the SCIs are the deficient reactant in the bimolecular reaction of SCIs with HCOOH. Previous model measurement studies have estimated the surface-level SCI concentrations to be in the range of \( 1.0 \times 10^4 \) to \( 1.0 \times 10^5 \) molec. cm\(^{-3} \) (Khan et al., 2018; Novelli et al., 2017). \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{HPMF}) \) is calculated to be \( 2.7-27 \times 10^{-7} \) s\(^{-1} \), which is several orders of magnitude lower than \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{H}_2\text{O}), k_{\text{eff}}(\text{CH}_2\text{OO}+\text{HCOOH}), \) and \( k_{\text{eff}}(\text{CH}_2\text{OO}+\text{SO}_2) \). A similar conclusion is also obtained from the reactions of \( \text{anti-CH}_2\text{CHOH}, \text{syn-CH}_2\text{CHOH}, \) and \( \text{(CH}_3)_2\text{COO} \) with HPMF.

To further evaluate the relative importance of the complex SCI reactions with the coreactant, the bimolecular reactions of methyl vinyl ketone oxide (MVK-OO) with \( \text{H}_2\text{O}, \text{HCOOH}, \) and HPMF are taken into account. MVK-OO, formed with 21\% to 23\% yield from the ozonolysis of isoprene, is a four-carbon, asymmetric, resonance-stabilized Criegee intermediate (Barber et al., 2018). MVK-OO has four conformers, \( \text{syn-trans}, \text{syn-cis}, \text{anti-trans}, \) and \( \text{anti-cis} \), as shown in Fig. S10. Herein, \( \text{syn-} \) and \( \text{anti-} \) refer to the orientation of the \( \text{–CH}_3 \) group relative to the termi-
nal oxygen of MVK-OO, whereas cis- and trans- refer to the orientation of the C₈=O₈ bond relative to the C₁=O₂ bond. According to the results shown in the Fig. S10, the lowest-energy conformer is syn-trans-MVK-OO, which is lower than syn-cis-, anti-trans-, and anti-cis-MVK-OO by 1.42, 2.43, and 2.69 kcal mol⁻¹, respectively. Therefore, the lowest-energy conformer syn-trans-MVK-OO is selected as the model compound to study its bimolecular reactions. As shown in Table 2, the rate coefficient of the H₂O reaction with syn-trans-MVK-OO is lower than with other SCIs by 2 to 3 orders of magnitude. The reason is likely to be that the presence of methyl and vinyl groups hinders the occurrence of bimolecular reaction with water vapor. Consequently, a fraction of syn-trans-MVK-OO may survive in the presence of water vapor and react with other species. kₐeff(MVK-OO+H₂O) is nearly identical to kₐeff(MVK-OO+HCOOH), which is greater than kₐeff(MVK-OO+SO₂), which, in turn, is greater than kₐeff(MVK-OO+HPMF) when the concentration of HPMF is equal to the atmospheric concentration of SCIs. Based on the above discussions, it can be concluded that the reactions of SCIs with HPMF are of minor importance in the atmosphere. These reactions may play a certain role in the formation and growth of organic new particle in some regions where low concentration of water vapor and high concentration of hydroperoxide esters occur.

3.4 Vapor pressure and volatility of the adduct products

The saturated vapor pressure (P₀) of the adduct products formed from the successive reactions of SCIs with HCOOH is estimated by using the EVAPORATION (Estimation of VApour Pressure of ORganics, Accounting for Temperature, Intramolecular, and Non-additivity effects) method proposed by Compernolle et al. (2011), and the room temperature results are summarized in Table S8. This table shows that the P₀ of the adduct products decreases significantly as the number of SCIs is increased. Notably, the P₀ of the adduct products decreases when the size of SCIs increases. For example, the P₀ of the adduct product HC(O)O(CH₂OO)₃H in the nCH₂OO + HCOOH reaction is estimated to be 3.41 × 10⁻⁵ atm, which is greater than those of the corresponding adduct products in the nanti-CH₃CHOO + HCOOH (4.73 × 10⁻⁶ atm), nsyn-CH₃CHOO + HCOOH (4.73 × 10⁻⁶ atm), and n(CH₃)₂COO + HCOOH (1.03 × 10⁻⁶ atm) reactions by 7.21, 7.21, and 33.11 times, respectively.

A classify scheme of various organic compounds is based on their volatility, as presented by Donahue et al. (2012). The volatility of organic compounds is described by their effective saturation concentrations. The saturated concentrations (c₀) of the adduct products formed from the successive reactions of SCIs with HCOOH are listed in Table S8. As shown in Table S8, the c₀ of the adduct products decreases significantly as the number of SCIs is increased. It deserves mentioning that the c₀ of the adduct products decreases with the increasing the size of the SCIs. For the nCH₂OO + HCOOH reaction, the c₀ of the adduct products is estimated to be 1.03 × 10⁰ (n = 1), 5.42 × 10⁰ (n = 2), 2.53 × 10⁵ (n = 3), 1.11 × 10⁴ (n = 4), and 4.67 × 10² (n = 5) µg m⁻³, respectively. According to the volatility basis set (VBS) of organic compounds (Donahue et al., 2012), the adduct products belong to volatile organic compounds (VOCs; c₀ > 3 × 10⁶ µg m⁻³) when the number of SCIs is less than or equal to two, while they belong to intermediate volatility organic compounds (IVOCs; 300 < c₀ < 3 × 10⁶ µg m⁻³) when the number of SCIs is greater than or equal to three. Similarly, the adduct products in the nanti-CH₃CHOO + HCOOH, nsyn-CH₃CHOO + HCOOH, and n(CH₃)₂COO + HCOOH reactions belong to IVOCs when the number of SCIs ranges from 2 to 4, whereas they belong to semivolatile organic compounds (SVOCs; 0.3 < c₀ < 300 µg m⁻³) when the number of SCIs is equal to 5. Based on the above discussion, it can be concluded that the volatility of the adduct products is significantly affected by the number and size of SCIs in the successive reaction of SCIs with HCOOH. The formed adduct products may participate in the formation and growth processes of organic new particle in the atmosphere.

4 Conclusions

The oligomerization reaction mechanism and kinetics of Criegee intermediate reactions with their respective hydroperoxide esters and HPMF are investigated using quantum chemical calculations and kinetics modeling methods. The main conclusion is summarized as follows.

a. For the initiation reactions of distinct SCIs with HCOOH, the barrierless 1,4 O-H insertion reaction, leading to the formation of hydroperoxide esters, is the most favorable pathway. The exothermicity of distinct SCIs reactions with HCOOH decreases when the number of methyl groups increases, and the exothermicity of the anti-CH₃CHOO + HCOOH reaction is higher than that of the syn-CH₃CHOO + HCOOH system.

b. The addition reactions of SCIs with hydroperoxide esters proceed through successive insertion of SCIs into hydroperoxide ester to form oligomers that involve SCIs as the repeating unit. These oligomerization reactions are strongly exothermic and spontaneous. The exothermicity of oligomerization reactions significantly decreases when the number of methyl substituents increases, and the exothermicity of anti-methyl substituted carbonyl oxides is higher than that of syn-methyl substituted carbonyl oxides.

c. The −OOH insertion reaction is favored over the −CH insertion pathway in the SCIs oligomerization reactions, and the barrier heights increase with increasing the number of SCIs added to the oligomer, except for syn-CH₃CHOO. The barrier of −OOH insertion pathway shows a dramatic decrease when a methyl substituent
Figure 6. PES (∆G and ∆E) for the distinct SCI + Pent1a reactions at the M06-2X/ma-TZVP//M06-2X/6-311+G(2df,2p) level of theory.

Table 2. The reported concentrations of the coreactant, the rate coefficients $k$, and the effective pseudo-first-order rate constants ($k_{eff} = k[\text{coreactant}]$) for distinct SCI reactions with HPMF, H$_2$O, HCOOH, and SO$_2$ in tropical forest environments.

<table>
<thead>
<tr>
<th>SCIs</th>
<th>Coreactant</th>
<th>[Coreactant] (molec. cm$^{-3}$)</th>
<th>$k$ (cm$^3$ molec.$^{-1}$ s$^{-1}$)</th>
<th>$k_{eff}$ (s$^{-1}$)</th>
<th>Reference</th>
</tr>
</thead>
<tbody>
<tr>
<td>CH$_2$OO</td>
<td>H$_2$O</td>
<td>3.9–6.1 × 10$^{17}$</td>
<td>&lt; 1.5 × 10$^{-15}$</td>
<td>5.9–9.2 × 10$^2$</td>
<td>Chao et al. (2015)</td>
</tr>
<tr>
<td></td>
<td>HCOOH</td>
<td>5.0–10.0 × 10$^{10}$</td>
<td>[1.1 ± 0.1] × 10$^{-10}$</td>
<td>5.5–11</td>
<td>Welz et al. (2014)</td>
</tr>
<tr>
<td></td>
<td>SO$_2$</td>
<td>1.7–9.0 × 10$^{10}$</td>
<td>[3.9 ± 0.7] × 10$^{-11}$</td>
<td>0.7–3.5</td>
<td>Welz et al. (2012)</td>
</tr>
<tr>
<td></td>
<td>HPMF</td>
<td>–</td>
<td>2.7 × 10$^{-11}$</td>
<td>–</td>
<td>This work</td>
</tr>
<tr>
<td>anti-CH$_3$COO</td>
<td>H$_2$O</td>
<td>3.9–6.1 × 10$^{17}$</td>
<td>[1.0 ± 0.4] × 10$^{-14}$</td>
<td>3.9–6.1 × 10$^3$</td>
<td>Taatjes et al. (2013)</td>
</tr>
<tr>
<td></td>
<td>HCOOH</td>
<td>5.0–10.0 × 10$^{10}$</td>
<td>[5 ± 3] × 10$^{-10}$</td>
<td>25.0–50.0</td>
<td>Welz et al. (2014)</td>
</tr>
<tr>
<td></td>
<td>SO$_2$</td>
<td>1.7–9.0 × 10$^{10}$</td>
<td>[6.7 ± 1.0] × 10$^{-11}$</td>
<td>1.1–6.0</td>
<td>Taatjes et al. (2013)</td>
</tr>
<tr>
<td></td>
<td>HPMF</td>
<td>–</td>
<td>3.3 × 10$^{-10}$</td>
<td>–</td>
<td>This work</td>
</tr>
<tr>
<td>syn-CH$_3$COO</td>
<td>H$_2$O</td>
<td>3.9–6.1 × 10$^{17}$</td>
<td>&lt; 4.0 × 10$^{-15}$</td>
<td>1.6–2.4 × 10$^3$</td>
<td>Taatjes et al. (2013)</td>
</tr>
<tr>
<td></td>
<td>HCOOH</td>
<td>5.0–10.0 × 10$^{10}$</td>
<td>[2.5 ± 0.3] × 10$^{-10}$</td>
<td>12.5–25.0</td>
<td>Welz et al. (2014)</td>
</tr>
<tr>
<td></td>
<td>SO$_2$</td>
<td>1.7–9.0 × 10$^{10}$</td>
<td>[2.4 ± 0.3] × 10$^{-11}$</td>
<td>0.4–2.2</td>
<td>Taatjes et al. (2013)</td>
</tr>
<tr>
<td></td>
<td>HPMF</td>
<td>–</td>
<td>1.7 × 10$^{-13}$</td>
<td>–</td>
<td>This work</td>
</tr>
<tr>
<td>(CH$_3$)$_2$COO</td>
<td>H$_2$O</td>
<td>3.9–6.1 × 10$^{17}$</td>
<td>&lt; 4.0 × 10$^{-16}$</td>
<td>58.5–91.5</td>
<td>Huang et al. (2015)</td>
</tr>
<tr>
<td></td>
<td>HCOOH</td>
<td>5.0–10.0 × 10$^{10}$</td>
<td>4.5 × 10$^{-10}$</td>
<td>22.5–45.0</td>
<td>Sipilä et al. (2014)</td>
</tr>
<tr>
<td></td>
<td>SO$_2$</td>
<td>1.7–9.0 × 10$^{10}$</td>
<td>1.3 × 10$^{-10}$</td>
<td>2.2–11.7</td>
<td>Huang et al. (2015)</td>
</tr>
<tr>
<td></td>
<td>HPMF</td>
<td>–</td>
<td>2.2 × 10$^{-11}$</td>
<td>–</td>
<td>This work</td>
</tr>
<tr>
<td>syn-trans-MVK-OO</td>
<td>H$_2$O</td>
<td>3.9–6.1 × 10$^{17}$</td>
<td>&lt; 4.0 × 10$^{-17}$</td>
<td>15.6–24.4</td>
<td>Caravan et al. (2020)</td>
</tr>
<tr>
<td></td>
<td>HCOOH</td>
<td>5.0–10.0 × 10$^{10}$</td>
<td>[3.0 ± 0.1] × 10$^{-10}$</td>
<td>15.0–30.0</td>
<td>Caravan et al. (2020)</td>
</tr>
<tr>
<td></td>
<td>SO$_2$</td>
<td>1.7–9.0 × 10$^{10}$</td>
<td>[4.2 ± 0.6] × 10$^{-11}$</td>
<td>0.7–3.8</td>
<td>Caravan et al. (2020)</td>
</tr>
<tr>
<td></td>
<td>HPMF</td>
<td>–</td>
<td>3.0 × 10$^{-11}$</td>
<td>–</td>
<td>This work</td>
</tr>
</tbody>
</table>
occurs at the anti-position, while it reveals a significant increase when a methyl group is introduced at the syn-position and dimethyl substituent.

d. Compared with the barrier of CH$_2$OO reaction with HPMF (8.1 kcal mol$^{-1}$), the barrier decreases by 2.5 kcal mol$^{-1}$ when a methyl substituent occurs at the anti-position, while the barrier increases by about 3.0 kcal mol$^{-1}$ when a methyl group is introduced at the syn-position and dimethyl substituent. The rate coefficients increase by about 1 order of magnitude when a methyl substituent occurs at the anti-position, whereas the rate coefficients decrease by 1 to 2 orders of magnitude when a methyl group is introduced at the syn-position compared to the rate coefficients of the CH$_2$OO + HPMF reaction.

e. In tropical forest environments, the effective pseudo-first-order rate constants for the reactions of distinct SCIs with HPMF ($k_{\text{eff}(\text{SCIs+HPMF})}$) are several orders of magnitude lower than those for the reactions of distinct SCIs with H$_2$O ($k_{\text{eff}(\text{SCIs+H}_2\text{O})}$), HCOOH, ($k_{\text{eff}(\text{SCIs+HCOOH})}$) and SO$_2$ ($k_{\text{eff}(\text{SCIs+SO}_2})$). $k_{\text{eff}(\text{SCIs+H}_2\text{O})}$ is greater than $k_{\text{eff}(\text{SCIs+HCOOH})}$, which, in turn, is greater than $k_{\text{eff}(\text{SCIs+SO}_2})$.

f. The saturated vapor pressure and saturated concentration of the adduct products formed from the successive reactions of SCIs with HCOOH decrease significantly as the number of SCIs is increased. The adduct products in the nCH$_2$OO + HCOOH reactions belong to IVOCs when the number of SCIs is greater than or equal to 3. The adduct products in the nanti-CH$_3$CHOO + HCOOH, n$_{\text{syn}}$-CH$_3$CHOO + HCOOH, and n(CH$_3$)$_2$COO + HCOOH reactions belong to IVOCs when the number of SCIs ranges from 2 to 4, whereas they belong to SVOCs when the number of SCIs is equal to 5.

Data availability. The data are accessible by contacting the corresponding author (huangyu@ieecas.cn).

Supplement. The following information is provided in the Supplement:

- Electronic potential energy along the O-H and C-O distance calculated by the M06-2X/6-311+G(2df,2p) method for the barrierless 1,4 insertion reactions.
- Natural bond orbital (NBO) analysis of the donor–acceptor orbitals involved in the TS1a.
- NPA charges of different atoms in the distinct SCIs.
- Optimized geometries of all the stationary points.

The supplement related to this article is available online at: https://doi.org/10.5194/acp-22-14529-2022-supplement.

Author contributions. LC designed the study. LC and YH wrote the paper. LC performed theoretical calculation. YX, ZJ, and WW analyzed the data. All authors reviewed and commented on the paper.

Competing interests. The contact author has declared that none of the authors has any competing interests.

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