



# Supplement of

# Inverse modeling of $SO_2$ and $NO_x$ emissions over China using multisensor satellite data – Part 2: Downscaling techniques for air quality analysis and forecasts

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## Box height



Figure S1. The box height of the lowest layer of GEOS-Chem in October 2013.



Figure S2. It is similar to Fig. 4, but GC adjoint v35m rather than GCv12.0.0 is used.

## CGS and MIX-DDC for SO<sub>2</sub>

#### GCS, MIX-DDC and NL-DC for NO<sub>2</sub>



Figure S3. It is similar to Fig. 5, but GC adjoint v35m rather than GCv12.0.0 is used.

#### NMSE of surface SO<sub>2</sub> and NO<sub>2</sub>



Figure S4. Normalized mean squared error (NMSE) of surface  $SO_2$  (a) and  $NO_2$  (b). All surface  $SO_2$  and  $NO_2$  simulations come from MIX-DDC and NL-DC, respectively. Black dots are posterior simulations from Joint-F-POS. The blue line is prior simulation results with  $SO_2$  NMSE from MIX-DDC-PRI and  $NO_2$  NMSE from NL-DC-PRI, respectively. The orange line is simulation results with  $SO_2$  NMSE from MIX-DDC-POS and  $NO_2$  NMSE from NL-DC-POS, respectively. The green line is similar to orange line, but posterior  $SO_2$  emission from separate assimilation and prior  $NO_x$  emission are used. The red line is similar to orange line, but posterior  $NO_x$  emission from separate assimilation and prior  $SO_2$  emission are used. In the figure (a), the blue line is covered by the red line, and the orange line is covered by the green line.

### O<sub>3</sub> forecasts



Figure S5. (a) is similar to Fig. 14c, but in the posterior forecasts, the prior MIX  $NO_x$  emission inventory and the posterior MIX-DE SO<sub>2</sub> emission inventory is used. (b) is similar to Fig. 14c, but in the posterior forecasts, the prior MIX SO<sub>2</sub> emission inventory and the posterior MIX-DE NO<sub>x</sub> emission inventory is used.

Figure S5 shows that the improvement of  $O_3$  forecasts is caused by using optimized posterior NO<sub>x</sub> emission inventory; the change SO<sub>2</sub> emission inventory has negligible impact.