



# Supplement of

# Estimating cloud condensation nuclei number concentrations using aerosol optical properties: role of particle number size distribution and parameterization

Yicheng Shen et al.

Correspondence to: Aki Virkkula (aki.virkkula@fmi.fi) and Aijun Ding (dingaj@nju.edu.cn)

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## 1 Supplement

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3 The Supplement contains the following sections:

- 4
- 5 S1. Amount of data used for the analyses, fractions of accepted data and criteria for data removal
- 6 S2. Application of Reduced Major Axis (RMA) regression
- 7 S3. Derivation of Equation (8)
- 8 S4. Derivation of Equation (9)
- 9 S5. Analysis of the uncertainty related to the number of samples
- 10 S6. N<sub>CCN</sub>(AOP) calculated by using the site-specific median SAE
- 11
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- 13

1 2 3	<b>S1. Amount of data used for the analyses, fractions of accepted data and criteria for data removal</b> Suspicious data within the whole dataset were removed according to the following criteria:
4 5	1) For the size distribution data, all the data with unexplainable spikes were removed manually;
6	There were 7587 available hourly-averaged-PNSD in MAO with 104 bins of each. A total of 5234 spikes were
7	removed. This accounts for ~0.7% of the total number of bins. 423 out of 7587 (~5.6%) distributions had at least 1
8	bin(s) removed. A distribution with few missing bins are still usable if treated properly. Only 55 (~0.7%)
9	distributions had more than 10 spikes removed.
10	
11	Besides for MAO, other data sets rarely suffered from such spikes. 32 out of 11502 (~0.3%) distributions were
12	removed for ASI. For SORPES and SMEAR2, less than 1% of distributions were removed. We didn't remove
13	anything from PNSD of PVC and PNSD is not available in PGH.
14	
15	2) for CCN measurements, insufficient water supply may cause underestimation of CCN, especially at lower
16	supersaturation ratios (DMT, 2009). N <sub>CCN</sub> reading at lower SS% has a sudden drop a few hours before the similar
17	sudden drop for higher SS% under such conditions, so data from such periods were removed;
18	
19	Besides from the QC flag within MAO dataset, additional 55, 112,120 and 123 data points were removed at
20	SS=0.25%,0.4%, 0.6% and 0.8% respectively, which accounts for ~0.7%-1.6% of total available data. For SORPES
21	and SMEAR2 ~1% of total available data were removed. For ASI, PVC and PGH, no further treatment was applied
22	besides the original QC flag.
23	
24	3) if any obvious inconsistencies between the AOPs and PNSD or between the N <sub>CCN</sub> and PNSD were found on
25	closure study, all the data in the same hour were removed.
20 27	
21 20	S1 successive nours of data from PVC were removed before analysis, which account for $\sim$ 3% of the data we used in
20 20	this study. 84 sparse data points were removed from the ASI data set, which account for ~0.7% of total available
29 30	data. For SORPES and SMEAR2 less than 1% of data were removed.
31	In total additional quality control removes $\sim 2\%$ $\sim 3\%$ $\sim 1\%$ and 0% of the total available data in MAO PVC ASI
32	and PGH respectively. The exact number for SORPES and SMEAR2 is not applicable since those 3 criteria are
33	within the original data process procedures. However, a rough estimation of fractional data removed by such criteria
34	are 0.5%~2%.
35	
36	The total number of available hourly-averaged data, accepted data and removed data and the fractions of these are

37 presented in Table S1.

## Table S1. Number of data and fractions of removed data from all stations

									-		
			AOPs		CCN			Size distribution			
	Period		from	Addtional	finalized	from	Addtional		from	Addtional	finalized
	(hours)		Dataset	QC	data	Dataset	QC	finalized data	Dataset	QC	data
SMEAD2	8784	N_total			8626			6973-6994			8461
SIMEAR2		Percentage			98.2%			79.3-79.6%			96.3%
CODDEC	8760	N_total			5266			4825~4906			5440
SORFES		Percentage			60.1%			55.1~56%			62.1%
ACT	12144	N_total	11851	84	11767	9894-10343		9894-10343	10931	32	10899
ASI		Percentage	97.6%	0.7%	96.9%	81.5-85.2%		81.5-85.2%	90.0%	0.3%	89.7%
DVC	1800	N_total	1637		1637	1495		1495	1730	0	1730
FVC		Percentage	90.9%		90.9%	83.1%		83.1%	96.1%	0.0%	96.1%
MAO	8160	N_total	7532		7532	7574-7653	55-123	7507-7541	7587	56	7541
MAO		Percentage	92.3%		92.3%	92.8~93.8%	0.7-1.5%	92-92.4%	93.0%	0.7%	92.4%
PGH	3498	N_total	3453		3453	3380-3420		3380-3420			
		Percentage	98.7%		98.7%	96.6-97.8%		96.6-97.8%			

#### S2. Application of Reduced Major Axis (RMA) regression

The Matlab code of Trujillo-Ortiz and Hernandez-Walls (2010) was applied to calculate the reduced major axis (RMA) regressions of  $R_{CCN/\sigma}$  vs. BSF to get the slope and offset (a and b, respectively) of  $R_{CCN/\sigma} = a BSF + b$  at the supersaturations (SS) of the CCN counters at the six 

stations. The results are shown in Table S2. The values of Table S2 were plotted as a function

of SS in Fig. S1 where also the fittings to the data are shown.

Table T2. Slopes (a) and offsets (b) of  $R_{CCN/\sigma} = a BSF + b$  obtained with RMA. The unit of the coefficients is  $[N_{CCN}]/[\sigma_{sp}] = cm^{-3}/Mm^{-1}$ .

			- cen s	-4-	
Station	SS(%)	а	(а <sub>LOW</sub> - анідн)	b	(b <sub>LOW</sub> - b <sub>HIGH</sub> )
SMEAR II	0.1	175	(170 - 181)	-15.0	(-15.814.3)
	0.2	511	( 502 - 521)	-49.8	(-51.248.5)
	0.5	1031	( 1011 - 1050)	-110.1	(-112.9107.3)
	1	1492	( 1459 - 1525)	-164.4	(-169.1159.7)
SORPES	0.1	121	( 117 - 125)	-9.1	(-9.58.7)
	0.2	333	( 326 - 341)	-25.8	(-26.625.0)
	0.4	657	( 643 - 671)	-53.0	( -54.651.5)
	0.8	926	( 905 - 946)	-76.6	( -78.974.4)
PGH	0.12	-53	( -54.651)	5.1	(5.0 - 5.2)
	0.22	161	( 156 - 167)	-6.9	( -7.36.5)
	0.48	712	( 689 - 734)	-37.6	( -39.236.0)
	0.78	849	( 823 - 876)	-44.1	(-46.042.3)
PVC	0.15	517	( 500 - 534)	-42.4	(-44.540.3)
	0.25	989	( 956 - 1023)	-85.8	(-89.981.7)
	0.4	1465	( 1416 - 1514)	-130.7	( -136.7124.7)
	1	2452	( 2369 - 2536)	-223.5	( -233.7213.3)
MAO	0.25	472	( 462 - 481)	-46.7	(-48.145.4)
	0.4	833	( 817 - 849)	-83.4	(-85.681.1)
	0.6	1188	( 1163 - 1213)	-122.1	( -125.6118.7)
	1.1	2128	( 2065 - 2190)	-226.5	(-234.9218.2)
ASI	0.1	150	( 147 - 153)	-15.9	( -16.315.4)
	0.2	319	( 312 - 325)	-34.0	(-34.933.1)
	0.4	372	( 365 - 380)	-39.8	( -40.938.7)
	0.8	406	( 397 - 414)	-42.4	(-43.641.1)



Figure S1. The RMA-derived coefficients a and b of each station (Table S2) as a function of supersaturation. Two types of functions, a logarithmic and a power fuction were fitted to the coefficient a, to coefficient b only a logarithmic function. The squared correlation coefficients  $R^2$  are shown only for the power function fittings, for the logarithmic fittings they were all > 0.99. The unit of the coefficients is  $[N_{CCN}]/[\sigma_{sp}] = cm^{-3}/Mm^{-1}$ .

7

8



Figure S2. Relationship between the coefficients  $a_0$ ,  $a_1$ ,  $b_0$  and  $b_1$  shown in Fig. S1 that were obtained from the fitting of  $a = a_1 \ln(SS) + a_0$  and  $b = b_1 \ln(SS) + b_0$  with the data in Table S2. a)  $a_0$  vs.  $a_1$ , b)  $b_0$  vs.  $b_1$ , c)  $b_1$  vs.  $a_1$ , d)  $b_0$  vs.  $a_0$ . The unit of the coefficients is  $[N_{CCN}]/[\sigma_{sp}] = cm^{-3}/Mm^{-1}$ .

1 When using RMA-derived slopes and offsets of  $R_{CCN/\sigma} = a BSF + b$  the relationship between

2 the factor  $a_1$  and SAE became  $a_1 \approx 391 \cdot \text{SAE}_{10}$  (Fig. S3).

3





Figure S3: Relationship between RMA-derived *a*<sub>1</sub> and SAE<sub>10,median</sub>.



8

This was further used to estimate CCN number concentration in the formula

$$N_{CCN}(RMA) \approx \left( \ln \left( \frac{SS}{0.12 \pm 0.02} \right) a_1(BSF - BSF_{\min}) + R_{\min} \right) \sigma_{sp}$$
(S1)

9 The derivation of Eq. (S1) is presented in supplement S4. N<sub>CCN</sub>(RMA) is in general in 10 agreement with the N<sub>CCN</sub>(AOP<sub>2</sub>) and N<sub>CCN</sub>(meas). However for SS~0.1% the performance of 11 RMA method is poor. At SS~0.1%, R<sup>2</sup> between N<sub>CCN</sub>(RMA) and N<sub>CCN</sub>(meas) is much lower than between N<sub>CCN</sub>(AOP<sub>2</sub>) and N<sub>CCN</sub>(meas) which indicates using RMA gives very uncertain 12 13 results ast lowest SS. Nevertheless, for SS>0.15%, OLS-derived N<sub>CCN</sub>(AOP<sub>2</sub>) and RMA-14 derived N<sub>CCN</sub>(RMA) agree well. Figure S4 shows the scatter plots for N<sub>CCN</sub>(RMA) vs. N<sub>CCN</sub>(meas) and R<sup>2</sup> and bias. The R<sup>2</sup> are between 0.5~0.85 and bias are within 0.5~2 when 15 16 SS>0.15% for  $N_{CCN}(AOP_2)$ .

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Figure S4. Statistics of  $N_{\rm CCN}(\rm RMA)$  from parameterization in Eq. (ES1).  $N_{\rm CCN}(\rm RMA)$  vs.  $N_{\rm CCN}(\rm meas)$  at different sites at different supersaturations, bias =  $N_{\rm CCN}(\rm RMA)/N_{\rm CCN}$  (meas) at different sites and supersaturations, and  $R^2$  of the linear regression of  $N_{\rm CCN}(\rm RMA)$  vs.  $N_{\rm CCN}$ (meas) at different sites and supersaturations. same as Figure 8, but for N<sub>CCN</sub>(RMA).

#### 1 The choice between OLS and RMA

- 2 Many studies use the reduced major axis (RMA) method instead of ordinary least squares (OLS)
- 3 method to define a line of best fit for a bivariate relationship when variable represented on the
- 4 X-axis contains measurement error. Smith (2009) point out that the major difference RMA and
- 5 OLS is not in the difference in the assumption made about the distribution of error, but in their
- 6 symmetry/asymmetry property. The reduced major axis regression is to describe the symmetric
- 7 relationship between two variables and not for predictive use of the variable x with respect to
- 8 y or y with respect to x (Smith, 2009). For predictive use OLS is preferred.
- 9
- 10

#### 11 **References**

Smith, R. J.: Use and Misuse of the Reduced Major Axis for Line-Fitting, Am. J. Phys.
Anthropol., 140, 476–486, doi:10.1002/ajpa.21090, 2009

- 14
- 15 Trujillo-Ortiz, A. and Hernandez-Walls, R.: gmregress: Geometric Mean Regression (Reduced
- 16 Major Axis Regression), a MATLAB file available at:
- 17 http://www.mathworks.com/matlabcentral/fileexchange/27918-gmregress, 2010.
- 18
- 19

#### 1 S3. Derivation of Equation (8)

#### 2 a) Using slopes and offsets from ordinary linear regressions

$$\begin{split} &N_{\mathcal{CCN}}(AOP) = \left(a_{ss}BSF + b_{ss}\right)\sigma_{sp} = \left(\left(a_{1}\ln(SS) + a_{0}\right)BSF + b_{1}\ln(SS) + b_{0}\right)\sigma_{sp} \\ &R_{\mathcal{CCN}/\sigma} = \frac{N_{\mathcal{CCN}}(AOP)}{\sigma_{sp}} = a_{ss}BSF + b_{ss} = \left(a_{1}\ln(SS) + a_{0}\right)BSF + b_{1}\ln(SS) + b_{0} \\ &\text{Linear regressions of the coefficients in Table 2 yield} \\ &a_{0} \approx (2.38 \pm 0.06)a_{1}, b_{0} \approx (2.33 \pm 0.03)b_{1}, b_{1} \approx -(0.096 \pm 0.013)a_{1} + (6.0 \pm 5.9) \\ \Rightarrow \\ &a_{1}\ln(SS) + a_{0} \approx a_{1}\ln(SS) + (2.38 \pm 0.06)a_{1} \approx a_{1}(\ln(SS) + (2.38 \pm 0.06)) \\ &b_{1}\ln(SS) + b_{0} \approx b_{1}\ln(SS) + (2.33 \pm 0.03)b_{1} = b_{1}(\ln(SS) + (2.33 \pm 0.03)) \\ \approx (-(0.096 \pm 0.013)a_{1} + (6.0 \pm 5.9))(\ln(SS) + (2.33 \pm 0.04)) \\ \Rightarrow \\ &R_{\mathcal{CCN/\sigma}} = \left(a_{1}\ln(SS) + a_{0}\right)BSF + b_{1}\ln(SS) + b_{0} \\ &\approx a_{1}(\ln(SS) + (2.38 \pm 0.06))BSF + (-(0.096 \pm 0.013)a_{1} + (6.0 \pm 5.9))(\ln(SS) + (2.33 \pm 0.03)) \\ &Approximation, since (2.33 \pm 0.03) \approx (2.38 \pm 0.06) \\ \Rightarrow \\ &R_{\mathcal{CCN/\sigma}} \approx a_{1}(\ln(SS) + (2.38 \pm 0.06))BSF - (0.096 \pm 0.013)a_{1}(\ln(SS) + (2.38 \pm 0.07)) + (6.0 \pm 5.09)(\ln(SS) + (2.38 \pm 0.06)) \\ \Rightarrow \\ &R_{\mathcal{CCN/\sigma}} \approx a_{1}(\ln(SS) + (2.38 \pm 0.06))BSF - (0.096 \pm 0.013)a_{1}(\ln(SS) + (2.38 \pm 0.07)) + (6.0 \pm 5.09)(\ln(SS) + (2.38 \pm 0.06)) \\ \approx (\ln(SS) + (2.38 \pm 0.06))(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)(\ln(SS) + (2.38 \pm 0.06)) \\ \approx (\ln(SS) + (2.38 \pm 0.06))(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)(\ln(SS) + (2.38 \pm 0.06)) \\ \approx (\ln(SS) + (2.38 \pm 0.06))(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx (\ln(SS) - \ln(0.093 \pm 0.006))(a_{1}(BSF - (0.097 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(a_{1}(BSF - (0.096 \pm 0.013)) + (6.0 \pm 5.9)) \\ \approx$$

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#### 5 b) Using slopes and offsets from reduced major axis regressions

$$N_{CCN}(RMA) = (a_{SS}BSF + b_{ss})\sigma_{sp} = ((a_1 \ln(SS) + a_0)BSF + b_1 \ln(SS) + b_0)\sigma_{sp}$$

$$R_{CCN/\sigma} = \frac{N_{CCN}(RMA)}{\sigma_{sp}} = a_{SS}BSF + b_{ss} = (a_1 \ln(SS) + a_0)BSF + b_1 \ln(SS) + b_0$$
RMA regressions  $\Rightarrow a_0 \approx (2.11 \pm 0.16)a_1, b_0 \approx (2.02 \pm 0.16)b_1, b_1 \approx -(0.108 \pm 0.016)a_1 + (7.7 \pm 11.0)$ 

The same steps as above in (a)  $\Rightarrow$   $R_{CCN/\sigma} \approx (\ln(SS) + (2.11 \pm 0.16))(a_1(BSF - (0.108 \pm 0.016)) + (7.7 \pm 11.0))$   $\approx (\ln(SS) - \ln(0.12 \pm 0.02))(a_1(BSF - (0.108 \pm 0.016)) + (7.7 \pm 11.0))$  $\approx \ln\left(\frac{SS}{0.12 \pm 0.02}\right)(a_1(BSF - (0.11 \pm 0.02)) + (8 \pm 11))$ 

## 1 S4. Derivation of Equation (9)

2 If the original slopes and offsets were calculated using ordinary linear regressions

$$N_{CCN}(AOP) \approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right) (a_1(BSF - BSF_{min}) + C)\sigma_{sp},$$

where C is an unknown constant.

$$\begin{aligned} \text{If } BSF &= BSF_{\min} \\ \Rightarrow a_1(BSF - BSF_{\min}) &= 0 \\ \Rightarrow N_{CCN}(AOP, BSF_{\min}) &\approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right) C \cdot \sigma_{sp} \\ \Leftrightarrow C &\approx \frac{1}{\ln\left(\frac{SS}{0.093 \pm 0.006}\right)} \frac{N_{CCN}(AOP, BSF_{\min})}{\sigma_{sp}} \approx \frac{1}{\ln\left(\frac{SS}{0.093 \pm 0.006}\right)} R_{\min} \\ \Rightarrow \\ N_{CCN}(AOP) &\approx \ln\left(\frac{SS}{0.093 \pm 0.006}\right) \left(a_1(BSF - BSF_{\min}) + \frac{1}{\ln\left(\frac{SS}{0.093 \pm 0.006}\right)} R_{\min}\right) \sigma_{sp} \\ &\approx \left(\ln\left(\frac{SS}{0.093 \pm 0.006}\right) a_1(BSF - BSF_{\min}) + R_{\min}\right) \sigma_{sp} \end{aligned}$$

4 If the original slopes and offsets were calculated using reduced major axis regressions

5 
$$N_{CCN}(RMA) \approx \left( \ln \left( \frac{SS}{0.12 \pm 0.02} \right) a_1(BSF - BSF_{\min}) + R_{\min} \right) \sigma_{sp}$$

6

- **1** S5. Analysis of the uncertainty related to the number of samples
- 2 The following procedure was used for testing how different values would be change if the number
- 3 of samples decrease.
- For each site 2%,3%,5%,10%,20%,30%,50% and 100% of samples were taken from the whole
  period.
- 6 2. The slope and offset a, b, BSF<sub>min</sub> (calculated as the 1<sup>st</sup> percentile of the BSF data) and
   7 SAE<sub>10</sub>,median were calculated from the randomly chose subsets.
- 8 3. The a, b,  $BSF_{min}$  and  $SAE_{10}$ , median should be slightly different if the sub-set is different.
- 9 Therefore the random sampling was repeated 100 times resulting in 100 different results
- 10 4. The averages and standard deviations of the 100 results were calculated and plotted below for11 all the sites. The average are the reds circles and the stds the error bars in the plots.
- 12

#### 13 **Results of the analysis**

14 The averages of a,b, BSF<sub>min</sub> and SAE<sub>10</sub>,median don't have clear dependence on the number of

- 15 samples. However, the uncertainty is very large at low number of samples and decreases with
- 16 increasing number of samples. The uncertainties depend on parameter and site. The plots suggest
- 17 that if the number of samples is larger than 1000 the uncertainty is low enough. For example, the
- 18 std of  $BSF_{min}$  is ~0.0005-0.005 and the std of  $SAE_{10}$ , median is ~0.01-0.02. For a and b, std is ~10%
- 19 of the a average value.



Figure S5. A monte-carlo test on the dependence of the parameters a, b, SAE<sub>10,median</sub> and BSF<sub>min</sub> on
 the number of hourly-averaged samples. The average are the reds circles and the stds the error bars.

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#### 1 S6. N<sub>CCN</sub>(AOP) calculated by using the site-specific median SAE

- 2
- 3 The general combined parameterization was presented in the main test as Eq.10:
- 4

$$N_{CCN}(AOP_2) \approx \left(a_1 \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(BSF - BSF_{\min}) + R_{\min}\right)\sigma_{sp}$$
$$\approx \left((286 \pm 46)SAE \cdot \ln\left(\frac{SS}{0.093 \pm 0.006}\right)(BSF - BSF_{\min}) + (5.2 \pm 3.3)\right)\sigma_{sp}$$

5 In the main text, we used SAE of hourly-averaged  $\sigma_{sp}$  to estimate  $N_{CCN}(AOP_2)$ . Here we give 6 another alternative for using this formula by using the site-specific median SAE values (Table 7 4 in the main text). The N<sub>CCN</sub>(AOP) calculated by using the site-specific median SAE is compared 8 with N<sub>CCN</sub>(meas) in Figure S6. When compared with N<sub>CCN</sub>(AOP) calculated by using the hourly-9 varying SAE (Fig. 8 in the main text), it is obvious that the two approaches are competitive with 10 each other. A comparison of the biases and correlation coefficients is presented in Table S3 below. 11 For some combinations of SS and sites, the site-specific median SAE gives a smaller R<sup>2</sup> and a higher 12 bias than the hourly SAE especially for ASI. 13 14 However, site-specific median SAE is very probably always positive, while the hourly SAE is

15 sometimes negative which may yield negative N<sub>CCN</sub>(AOP). For the 6 sites of this study, the fraction

16 of negative SAE of all hourly data varied between 0-6%. To estimate N<sub>CCN</sub> for a site with a large

17 fraction of negative SAE, we recommend to use site-specific median SAE.





Figure S6. Same as Figure 8 in the main text, but N<sub>CCN</sub>(AOP) calculated by using the site-specific
median SAE. For details see the caption of Fig. 8 in the main text

- 1 Table S3. Performance of the general combined parametrization using SAE of hourly-averaged
- 2 scattering coefficients and site-specific median SAE at the supersaturations of the CCN
- 3 counters of each station.

	Fraction of			N <sub>CCN</sub> (AOP) calculated using					
	hourly		hourly-va	arying SAE	median SAE				
Station	SAE < 0	SS	$R^2$	bias	R <sup>2</sup>	bias			
Π		0.10%	0.675	0.72	0.657	0.72			
AR	0.00/	0.20%	0.832	1.09	0.850	1.07			
ME	0.0%	0.50%	0.719	1.26	0.754	1.24			
SI		1.00%	0.504	1.20	0.554	1.18			
$\mathbf{s}$		0.10%	0.595	1.61	0.587	1.62			
PE	0.00/	0.20%	0.773	1.36	0.751	1.43			
OR	0.0%	0.40%	0.650	1.22	0.699	1.30			
S		0.80%	0.636	1.27	0.687	1.34			
		0.25%	0.840	1.24	0.816	1.07			
AO	6 00/	0.40%	0.834	0.97	0.832	0.82			
M	0.0%	0.60%	0.725	0.91	0.742	0.76			
		1.10%	0.583	0.71	0.622	0.67			
		0.12%	0.852	4.53	0.821	4.71			
Ηt	1 104	0.22%	0.871	2.13	0.832	2.35			
Ы	4.4%	0.48%	0.784	1.13	0.779	1.30			
		0.78%	0.703	1.07	0.723	1.25			
		0.10%	0.872	1.92	0.828	1.72			
SI	0.04%	0.20%	0.923	1.41	0.844	1.21			
A		0.40%	0.900	1.61	0.836	1.35			
		0.80%	0.857	1.90	0.818	1.57			
		0.15%	0.880	0.71	0.835	0.69			
)C	0.3%	0.25%	0.780	0.70	0.747	0.69			
Ы		0.40%	0.687	0.71	0.655	0.69			
		1.00%	0.519	0.71	0.499	0.70			

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6 The biases of N<sub>CCN</sub>(AOP<sub>2</sub>) presented in Table S3 were calculated from the ratio 7  $N_{CCN}(AOP_2)/N_{CCN}(meas)$ . Since  $N_{CCN}(AOP_2) \approx (a_1 \ln(SS/0.093)(BSF - BSF_{min}) + R_{min})\sigma_{sp}$  it is 8 obvious that biases of a1 affect the bias of N<sub>CCN</sub>(AOP2). If we consider the a1 values in the main text 9 Table 4 as the accurate station-specific values then the fitted line  $a_1 = 286 \cdot SAE$  overestimates or 10 underestimates a<sub>1</sub> by +37%, +30%, -20%, -32%, -20% and +251% for SMEAR II, SORPES, 11 PGH, PVC, MAO and ASI, respectively. These values were calculated from 100%(286 SAE -12  $a_1$ / $a_1$ . The biases of  $a_1$  calculated from 286 SAE/ $a_1$  are therefore 1.373, 1.295,0.796, 0.675, 13 0.792, 3.509 for the respective stations. The average biases of N<sub>CCN</sub>(AOP<sub>2</sub>) at all supersaturations 14 of each station presented in Table TS3 are compared with the biases of  $a_1$  in Figure S7. For each 15 station two values are shown: the average bias of N<sub>CCN</sub>(AOP<sub>2</sub>) calculated by using the median SAE 16 of each station and the average bias of N<sub>CCN</sub>(AOP<sub>2</sub>) calculated by using the hourly-varying SAE. 17 For PGH the average bias of N<sub>CCN</sub>(AOP<sub>2</sub>) at all supersaturations and at SS>0.3% are shown because 18 the biases at the lowest supersaturations are anomalously high. The plot shows that for most stations 19 the bias of  $N_{CCN}(AOP_2)$  can be explained by the bias of  $a_1$ : when  $a_1$  is underestimated so is 20 N<sub>CCN</sub>(AOP<sub>2</sub>) and when a<sub>1</sub> is overestimated so is N<sub>CCN</sub>(AOP<sub>2</sub>). PGH is the only exception to this, 21 especially at the lowest two supersaturations (SS = 0.12% and 0.22%) and we cannot explain why. 22 For ASI the bias of  $N_{CCN}(AOP_2)$  is clearly smaller than the bias of  $a_1$ . This would happen when in 23 the formula  $N_{CCN}(AOP_2) \approx (a_1 \cdot \ln(SS/0.093)(BSF - BSF_{min}) + R_{min})\sigma_{sp}$  both SAE and BSF are very 24 small and especially when BSF is close to BSF<sub>min</sub>. Both of these would take place when aerosol is 25 dominated by large aerosols. This is true especially for ASI, a site dominated by marine aerosols.



3 Figure S7. Biases of  $N_{CCN}(AOP_2)$  vs the bias of  $a_1$  calculated from  $a_1 = 286$ ·SAE. The biases of

N<sub>CCN</sub>(AOP<sub>2</sub>) are the averages of biases at all supersaturations presented in Table S3. For each station
 two values are shown: the average bias of N<sub>CCN</sub>(AOP<sub>2</sub>) calculated by using the median SAE of each

6 station (open circles) and the hourly-varying SAE (filled circles). For PGH the average bias of

- $N_{CCN}(AOP_2)$  at all supersaturations and at SS> 0.3.