



Supplement of

Characterizing biospheric carbon balance using CO_2 observations from the OCO-2 satellite

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S1 Additional detail on study methodology

S1.1 Details on the CO_2 initial condition and model spin-up

We spin up CO₂ mixing ratios in the PCTM model using outputs from NOAA's CarbonTracker product (Peters et al., 2007). CarbonTracker produces CO₂ fluxes and atmospheric mole fractions that are optimized to match available in situ CO₂ observations. Our goal is to spin up CO₂ mixing ratios within PCTM in a fashion that is both consistent with CarbonTracker and with the PCTM model grid. To this end, we initialize CO₂ simulations on 1 Jan., 2009. We average estimated global CO₂ mole fractions from CarbonTracker by hemisphere and by model vertical level. We then use these averages as the CO₂ initial condition in PCTM for 1 Jan., 2009. Subsequently, we run PCTM forward using CarbonTracker fluxes until 1 Sept., 2014 when the model selection simulations begin. We continue these PCTM simulations past 1 Sept., 2014 using a surface flux of zero. These simulations become the spin-up modeled CO₂, and we subtract these spin-up mole fractions from the OCO-2 retrievals (z in Eq. S2). The resulting vector (z) represents the change in CO₂ mole fractions due to fluxes that occurred after 1 Sept., 2014.

S1.2 Additional detail on the CO_2 flux patterns used in model selection

This section provides additional detail on the terrestrial biosphere models (TBMs) and vegetation indices that are used in the model selection experiments. These TBMs and vegetation indices are used as the input fluxes in the PCTM model. We generate modeled XCO_2 total columns using these PCTM outputs, and the modeled XCO_2 total columns become the predictor variables in the model selection experiments (Eq. S1). Note that the multiple regression will scale the magnitude of the TBMs and vegetation indices in each region and each month to best match the observations (Eq. S2). As a result of this setup, the overall magnitude of each TBM and of each vegetation index does not affect the model selection results. Rather, this study utilizes the spatial and temporal patterns in the TBMs and vegetation indices.

We include four TBMs from the recent MsTMIP project (Huntzinger et al., 2013). The selected TBMs have very different space-time patterns and therefore sample a wide range of plausible flux patterns. These TBMs include the Dynamic Land Ecosystem Model (DLEM; e.g., Tian et al., 2011), the Lund-Potsdam-Jena Model Wald Schnee und Landschaft version (LPJ; e.g., Sitch et al., 2003), the Global Terrestrial Ecosystem Carbon Model (GTEC; e.g., King et al., 1997), and the Simple Biosphere Model with the Carnegie-Ames-Stanford Approach (SIBCASA; e.g., Schaefer et al., 2008). The original MsTMIP model outputs have a spatial resolution of 0.5° latitude by 0.5° longitude and a 3-hourly temporal resolution. We regrid the fluxes to the PCTM model grid (1° latitude by 1.25° longitude) and input the fluxes into PCTM at the original 3-hourly resolution. Note that the gridded, 3-hourly MsTMIP flux estimates are available for years 2004–2010. Few TBMs have readily-available flux estimates for the 2014–2015 time period of this study, including the TBMs in the MsTMIP study. Instead, we use a multi-year average of the MsTMIP fluxes as inputs in the PCTM model. We average these 7 years within each separate grid box and for each separate 3-hourly time period to produce this multi-year average for each MsTMIP flux model.

In addition to these TBMs, we also utilize several vegetation indices (EVI, NDVI, and SIF). Numerous studies indicate that biospheric CO_2 fluxes correlate with these vegetation indices – with EVI (e.g., Sims et al., 2008; Wu et al., 2011), NDVI (e.g., Cihlar et al., 1992; Wylie et al., 2003), and GOME-2 SIF (e.g., Guanter et al., 2014; Yang et al., 2015). These indices are therefore good candidate flux patterns to use within the model selection experiments.

We use EVI and NDVI from the MODIS Aqua product MYD13C1 (Didan, 2015a) and the

MODIS Terra product MOD13C1 (Didan, 2015b). These products are collectively available at 8-day intervals. The individual Aqua and Terra products are each available at 16-day intervals. However, the two products are staggered, so Aqua and Terra can be combined to produce EVI and NDVI estimates every 8 days. These products have a 0.05° latitude by 0.05° longitude, and we regrid them to the PCTM model grid (1° latitude by 1.25° longitude). Both of these products are available for 2014 and 2015, the time period of this study.

We use level 2 SIF retrievals from GOME-2 (Global Ozone Monitoring Experiment-2) (Joiner, 2014). We convert the level 2 retrievals to a gridded SIF product using a block kriging method described by Tadić et al. (2017). This gridded product has a daily temporal resolution and the same spatial resolution as PCTM. We use this product as an input 'flux' into the PCTM model and incorporate the PCTM outputs as candidate variables the regression (Eq. S1).

S1.3 Additional detail on model selection implementation

This sub-section describes the regression and model selection in greater detail. The regression used in this paper will quantitative link OCO-2 XCO_2 observations with atmospheric model outputs:

$$\mathbf{Y} = h(\mathbf{X}) \tag{S1}$$

$$\boldsymbol{z} = \boldsymbol{Y}\boldsymbol{\beta} + \boldsymbol{\epsilon}$$
 (S2)

$$\boldsymbol{\epsilon} \sim \mathcal{N}(\mathbf{0}, \sigma^2 \mathbf{V}) \tag{S3}$$

These equations are an expanded form of the regression equations present in Sect. 2.3. The vector z (dimensions $n \times 1$) represents the XCO₂ observations minus the model initial condition or spin-up (Sect. S1.1). The variable **X** (dimensions $m \times p$) is a matrix of p different flux models, and each column of **X** is a different flux model for a different region and month. The function h() is an atmospheric model that transports the fluxes to the times and locations of the OCO-2 retrievals, and the resulting matrix **Y** has dimensions $n \times p$. Furthermore, the variable ϵ is a $n \times 1$ vector of residuals. These residuals are assumed to follow a multivariate normal distribution with a mean of zero, a variance of σ^2 , and a covariance structure given by **V** (dimensions $n \times n$). The vector of coefficients (β , dimensions $p \times 1$) are estimated as part of the regression.

In this study, we choose a set of variables for \mathbf{X} using model selection based on the Bayesian Information Criterion (BIC) (Schwarz, 1978). We calculate a BIC score for many different candidate models. Each candidate model has a different set of columns (\mathbf{X}) – different combinations of flux models in different geographic regions and in different months.

The best model has the lowest BIC score:

$$BIC = L + p\ln(n^*) \tag{S4}$$

where L is the log likelihood of a particular candidate model (**X**). The log-likelihood has the following form:

$$L = n^* \ln(\sigma^2) + \frac{n^*}{n} RSS$$
(S5)

$$RSS = \frac{1}{\sigma^2} \boldsymbol{z}^T \boldsymbol{z} - \frac{1}{\sigma^2} \boldsymbol{z}^T \mathbf{Y} (\mathbf{Y}^T \mathbf{Y})^{-1} \mathbf{Y}^T \boldsymbol{z}$$
(S6)

where RSS is the residual sum of squares and σ^2 is defined above in Eq. S3.

Both the BIC and log-likelihood equations (Eq. S4 and S5) incorporate n^* , the effective number of independent observations. Jones (2011) discusses this concept in the context of the BIC. Just because the satellite provides n observations does not mean there are n independent pieces of information. Accordingly, n^* ensures that the model selection framework accurately assesses the amount of independent information in the observations. It accounts for the fact that there are often spatial and temporally coherent errors in the satellite observations or in the transport model. If all of the observations were independent (i.e., if **V** were diagonal), then n^* would equal n. However, we de-weight both components of Eq. S4 as the covariances in **V** increase.

We could calculate n^* directly using \mathbf{V}^{-1} (Jones, 2011). In fact, several CO₂ model selection studies incorporate \mathbf{V}^{-1} directly into the equation for RSS (e.g., Mueller et al., 2010; Gourdji et al., 2012; Shiga et al., 2014). We use 5,079,165 observations (*n*) in this study, so \mathbf{V} has 5.08×10^6 rows and columns. As a result, the inverse of \mathbf{V} is computationally intractable. We instead estimate n^* using an approach based on Griffith (2005), an approach that does not require computing \mathbf{V}^{-1} directly:

$$n^* = \frac{n}{1 + \left(\sum_{i=1}^n \sum_{j=1, j \neq i}^n V_{i,j} / n\right)}$$
(S7)

This equation calculates n^* using individual elements of **V** and does not require inverting the full matrix; it is therefore far more computationally tractable. Subsequent paragraphs describe how we estimate the elements of **V**.

The remainder of this section discusses how we characterize the variances (σ^2) and covariance structure (**V**) of the residuals (ϵ) (Eq. S3). An estimate of the variance is required to calculate the residual sum of squares (RSS, Eq. S6), and an estimate of the covariance structure is necessary to calculate the effective number of independent observations (n^* , Eq. S7).

We first describe the method for characterizing the covariance structure (**V**). We estimate the individual elements, $V_{i,j}$, in the vicinity of each observation *i* by fitting a local variogram model on the model-data residuals (ϵ). The covariance structure likely differs in different locations and at different times (i.e., is non-stationary), and several existing studies fit variograms locally to account for this non-stationary structure (e.g., Alkhaled et al., 2008; Hammerling et al., 2012; Tadić et al., 2017). We use a similar approach here. Specifically, we estimate this structure by constructing empirical variograms and fitting spherical variogram models (for an overview of variograms, refer to Kitanidis, 1997). We use a spherical model because it tapers off to zero and is therefore faster to compute with large datasets.

For each i, we create a separate spatial experimental variogram and a temporal experimental variogram. We use all residuals that lie within 3000 kilometers of i and were collected at similar times (within 1 day) to construct the spatial variogram, and we use residuals within 75 days of i and a similar location (within 250 km) to construct the spatial variogram. We choose these spatial and temporal distances because they are larger than transport or retrieval errors that might covary across an entire biome. We then fit spherical models to the spatial and temporal variograms, respectively. In our setup, the elements of $V_{i,j}$ equal the spherical covariance model multiplied by the temporal covariance model:

$$V_{i,j} = \begin{cases} (1 - \frac{3}{2} \frac{d_{i,j}}{\alpha_{d,i}} + \frac{1}{2} \frac{d_{i,j}^3}{\alpha_{d,i}^3})(1 - \frac{3}{2} \frac{t_{i,j}}{\alpha_{t,i}} + \frac{1}{2} \frac{t_{i,j}^3}{\alpha_{t,i}^3}) & \text{if } d \le \alpha_{d,i} \text{ and } t \le \alpha_{t,i} \\ 0 & \text{if } d > \alpha_{d,i} \text{ or } t > \alpha_{t,i} \end{cases}$$
(S8)

where $d_{i,j}$ and $t_{i,j}$ are the distance and time, respectively, between points *i* and *j*. The variables $\alpha_{d,i}$ and $\alpha_{t,i}$ are the decorrelation length and time parameters estimated from the spatial and temporal emperical variograms, respectively. Note that several existing top-down CO₂ studies use a covariance model with multiplied spatial and temporal components (e.g., Mueller et al., 2008; Gourdji et al., 2012), though other recent studies use a more advanced approach (Tadić et al., 2017).

We then use this estimate for $V_{i,j}$ to estimate n^* (Eq. S7). The denominator of Eq. S7 sums over each element *i*. For each element *i* in the summation, we use covariance parameters estimated for that element *i*. Note that Eq. S7 presents a computational challenge. In this setup, i = 1...n where $n = 5.08 \times 10^6$. It would be computationally prohibitive to estimate 5.08×10^6 local variogram models. Instead, we randomly choose 1000 elements of *i* and estimate a variogram model for each of those elements. As a result, the *i* summation term Eq. S7 only sums over 1000 elements. More precisely, Eq. S7 becomes

$$n^* = \frac{n}{1 + \frac{\sum_{1 \le i \le n} \sum_{j=1, j \ne i}^n V_{i,j}}{1000}}$$
(S9)

where i is a set of 1000 randomly chosen numbers between 1 and n.

The model selection equations (i.e., Eq. S6) also require an estimate for σ^2 . We estimate a single value for σ^2 using all *n* residuals:

$$\sigma^2 = \frac{1}{n-1} \sum_{i=1}^n \epsilon_i^2 \tag{S10}$$

This implementation of model selection is iterative. We start by estimating the covariance parameters with all candidate variables included in \mathbf{X} . We use these covariance parameters to estimate n^* and subsequently run model selection. We run model selection with a heuristic branch and bound algorithm described by Yadav et al. (2013). This algorithm dramatically reduces the computing time of the model selection step. We then re-estimate the covariance parameters using the chosen columns of \mathbf{X} . The covariance parameters usually change slightly with the new, updated \mathbf{X} matrix. We alternate between the covariance estimation and model selection until both the covariance parameters and columns selected for \mathbf{X} do not change from one iteration to the next. The estimated covariance parameters and model selection results typically converge on a stable answer within two to three iterations.

S1.4 Additional detail on the simulated, synthetic data errors

This section provides additional information on the simulated atmospheric transport errors and simulated retrieval errors used in the synthetic data experiments (Sect. 2.2 and 2.5).

We use simulated transport errors from an ensemble of meteorology realizations in Miller et al. (2015). That study follows an approach developed by Liu et al. (2011). Both studies simulate global meteorology using the Community Atmosphere Model (CAM) in weather forecasting mode. The studies also include CO_2 as a passive tracer in the model. Miller et al. (2015) and Liu et al. (2011) then run an ensemble of 64 parallel simulations to estimate the effects of atmospheric transport uncertainties on modeled CO_2 . At each time step of the simulations, they assimilate the mean of the 64-member ensemble to match meteorological observations using a local ensemble Kalman filter (LETKF) (e.g., Hunt et al., 2007). Miller et al. (2015) also adjust the ensemble variance to be consistent with the meteorology model-data residuals using an approach known as adaptive covariance inflation (e.g., Miyoshi, 2011). In the present study, we randomly choose one of the ensemble members. We use the difference in modeled CO_2 mixing ratios between the chosen ensemble member and the ensemble mean as our simulated atmospheric transport error (Fig. 1). We then interpolate these estimated transport errors from the CAM model grid (1.9° latitude by 2.5° longitude resolution) to the locations and times of the GOSAT observations.

We use two different approaches to simulate satellite retrieval errors. We employ the first approach in the synthetic data simulations in the main text. We use the second set of errors here in the Supplement (Sect. S2.2) as a robustness or sensitivity check on the synthetic data simulations. In the first approach, we model XCO_2 using PCTM and the SiBCASA model. We then regress the model-data residuals on the retrieval parameters included in the OCO-2 lite data file. These parameters include retrieved surface pressure; the H₂O ratio; temperature at 700 hPa; wind speed; albedo; aerosol optical depth; the log of dust, water, and salt aerosols; the land fraction in the OCO-2 footprint; surface altitude; the satellite operation mode (e.g., nadir mode, target mode, etc.); footprint bias; and the change in CO_2 vertical gradient between the surface and retrieval model level 13.

We use this regression to estimate the portion of the residuals that map on to the retrieval parameters. That result is used as the estimated retrieval error (Fig. 1):

$$\boldsymbol{\epsilon} = \mathbf{1}\beta_{0,r} + \mathbf{X}_{\mathbf{r}}\boldsymbol{\beta}_{\mathbf{r}} + \boldsymbol{\zeta} \tag{S11}$$

where $\boldsymbol{\epsilon}$ are the model-data residuals from Eq. S2, $\beta_{0,r}$ is the intercept term in the regression, $\mathbf{X}_{\mathbf{r}}$ is the matrix of retrieval parameters, $\boldsymbol{\beta}_{r}$ are the estimated coefficients, and $\boldsymbol{\zeta}$ is the portion the residuals ($\boldsymbol{\epsilon}$) not described any other terms in the equation. We use $\mathbf{X}_{\mathbf{r}}\boldsymbol{\beta}_{r}$ as our estimate of the retrieval errors.

This approach is one way to estimate the portion of the residuals that maps onto retrieval parameters. Errors in the model output due to atmospheric transport or due to biospheric fluxes in **X** are unlikely to map onto parameters like aerosol optical depth. Rather, errors that map onto aerosol optical depth may more likely reflect issues in the satellite retrievals. There is always a possibility that residuals caused by inaccurate fluxes could have patterns similar to some of the retrieval parameters. For example, errors in modeled XCO₂ due to inaccurate biospheric flux patterns might correlate weakly or modestly with surface albedo, and errors in modeled XCO₂ due to errors in CO₂ fossil fuel emissions could correlate weakly or modestly with aerosol optical depth.

We generate an alternate set of retrieval errors using a different approach as a consistency check. This approach, described in Sect. 2.2, assigns a non-zero retrieval error if and only if four different flux estimates (input into PCTM) unanimously disagree with the OCO-2 observations. There could be error in the retrievals if all of the biospheric models are in good agreement – if all of the model outputs disagree with the retrievals in the same direction. In that case, either all four flux models are incorrect, there is a consistent transport bias, or there is an error in the satellite retrievals. The four flux models chosen in this study have disparate spatial and temporal patterns, so the first option appears unlikely. The second option (transport errors) could play a role, but transport errors at different vertical model levels often have different signs or magnitudes and can cancel out across the total column (e.g., Miller et al., 2015). Hence, the last option (retrieval errors) may be most likely when all four sets of model outputs consistently disagree with the XCO₂ retrievals. We use this alternative approach for generating retrieval errors solely as a consistency check on our primary synthetic data results.

S2 Sensitivity of the results to methodological choices

S2.1 Real data results that include glint data

We re-run model selection including all retrieval modes in the observation vector (z) – glint, nadir, and target. The results in the main manuscript (Fig. 4), by contrast, exclude glint mode retrievals due to potential biases in these retrievals.

The model selection results that include glint retrievals are shown in Fig. S1, and the results look similar to those without glint retrievals (Fig. 4). Several factors may explain the similarity between these two results. The glint retrievals observe CO_2 mixing ratios in continental outflow but are not likely as sensitive to terrestrial flux patterns as nadir data over land. The model– data residuals over the ocean (i.e., associated with glint mode) are correlated over longer spatial and temporal scales relative to residuals over land. As a result, the glint mode retrievals add a limited amount of new, independent information on terrestrial fluxes in the context of the model selection experiments.

S2.2 Synthetic data results with an alternative set of simulated retrieval errors

Figure S2 displays the results of the synthetic data experiment using an alternate estimate for the retrieval errors, and the results are consistent with those in the main text (Fig. 5). This alternate set of simulated errors displays different characteristics from the errors used in Fig. 5, yet the model selection results are similar. These alternative simulated errors have a larger standard deviation but a smaller mean bias and smaller covariances (Fig. 1). Similarly, n^* is closer to the real data experiments ($n^* = 3700$). The larger standard deviation or variance increases the impact of these errors on the model selection results. However, smaller biases or covariances decrease their effect on the results. These two effects largely offset each other, and we therefore obtain similar results using both sets of simulated retrieval errors.

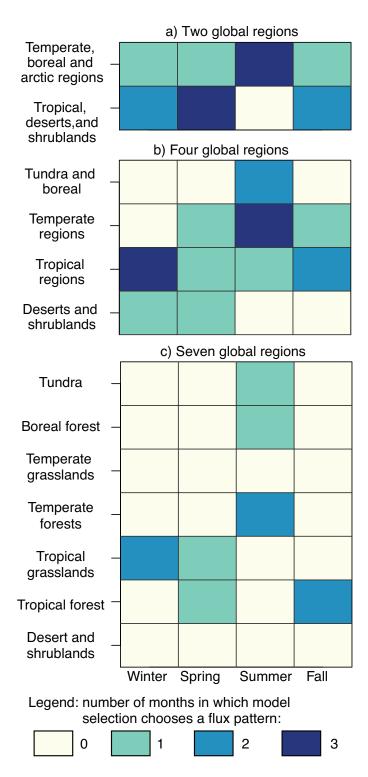


Figure S1: Results of the real data model selection experiment using all good quality OCO-2 retrievals (including glint mode retrievals). These model selection results are similar to those in the main manuscript that exclude glint mode data (Fig. 4).

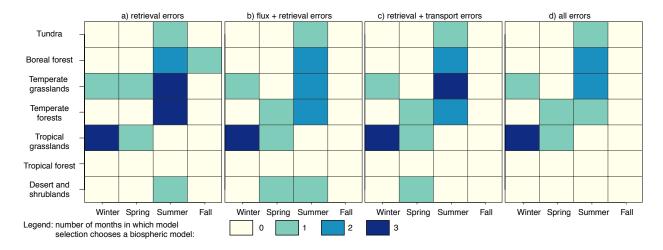


Figure S2: Results of the synthetic data case study using an alternative estimate for the retrieval errors (Sect. 2.2). These results are similar to those in Fig. 5, providing a consistency check on the synthetic data simulations.

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