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*Supplement of*

## **Sensitivities of Amazonian clouds to aerosols and updraft speed**

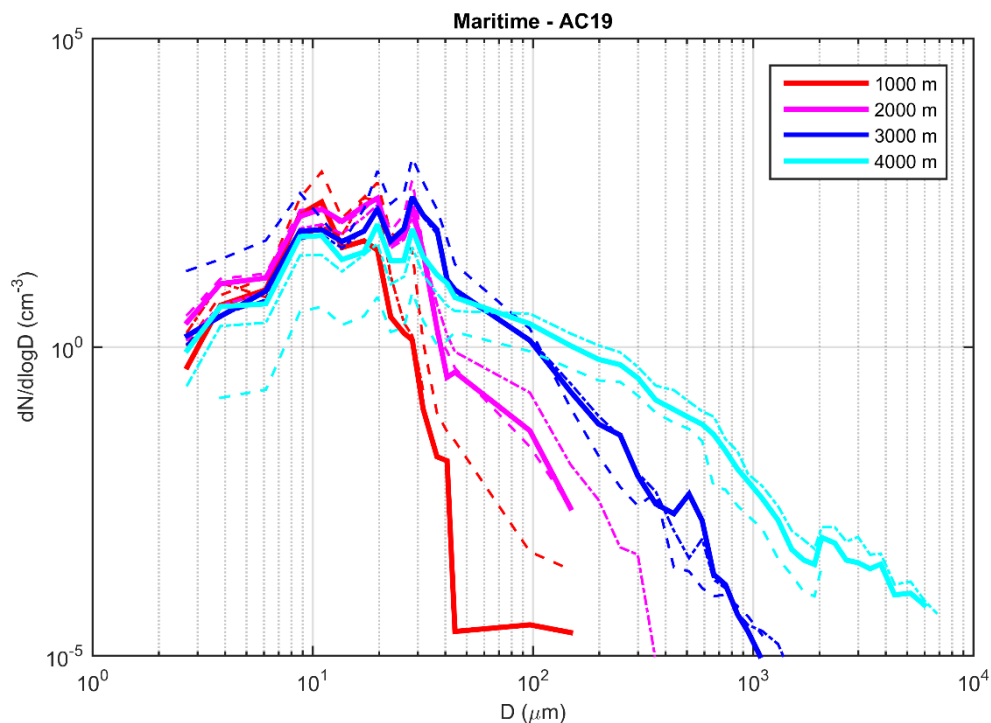
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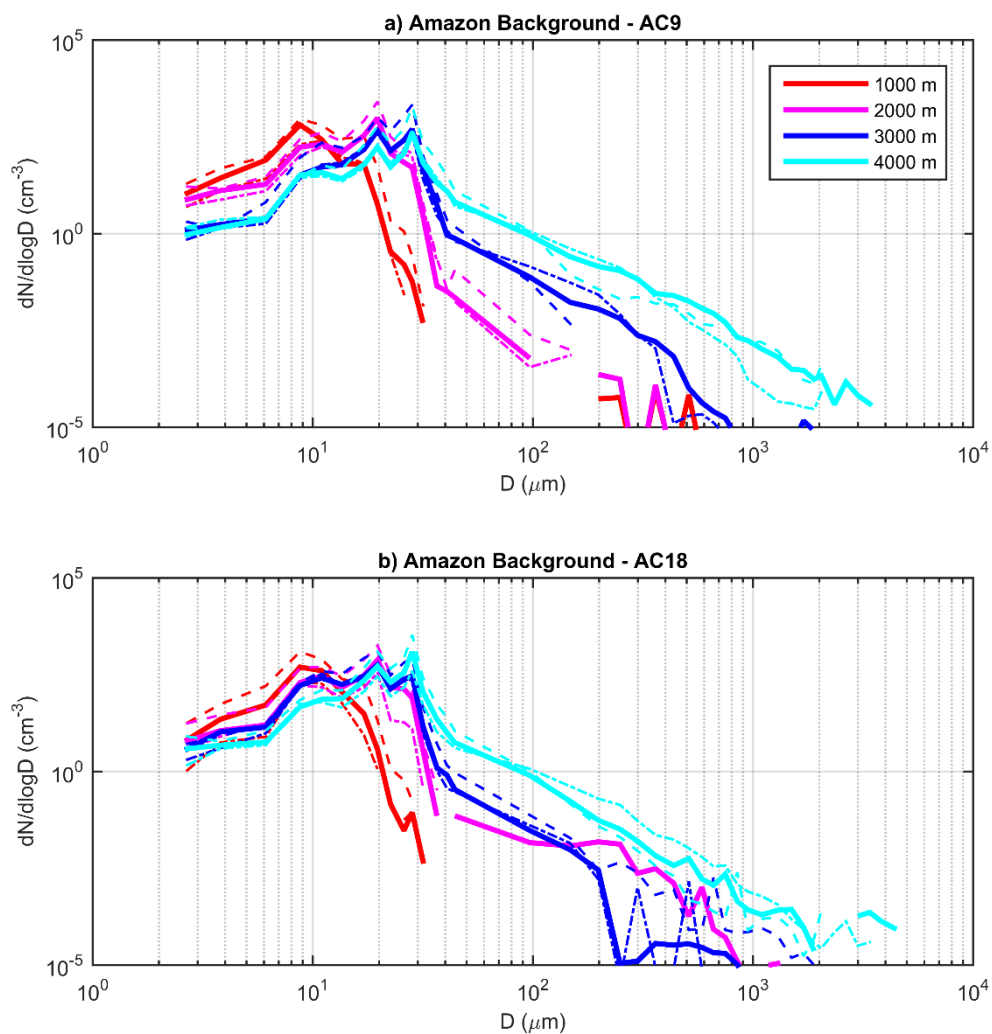
## DSD profiles for each flight

Figures S1-4 show the individual DSD profiles for each flight considered in this study. It clearly shows the cohesiveness of the aerosol effect on the vertical structure of the warm-phase. Altitudes shown are relative to cloud base.

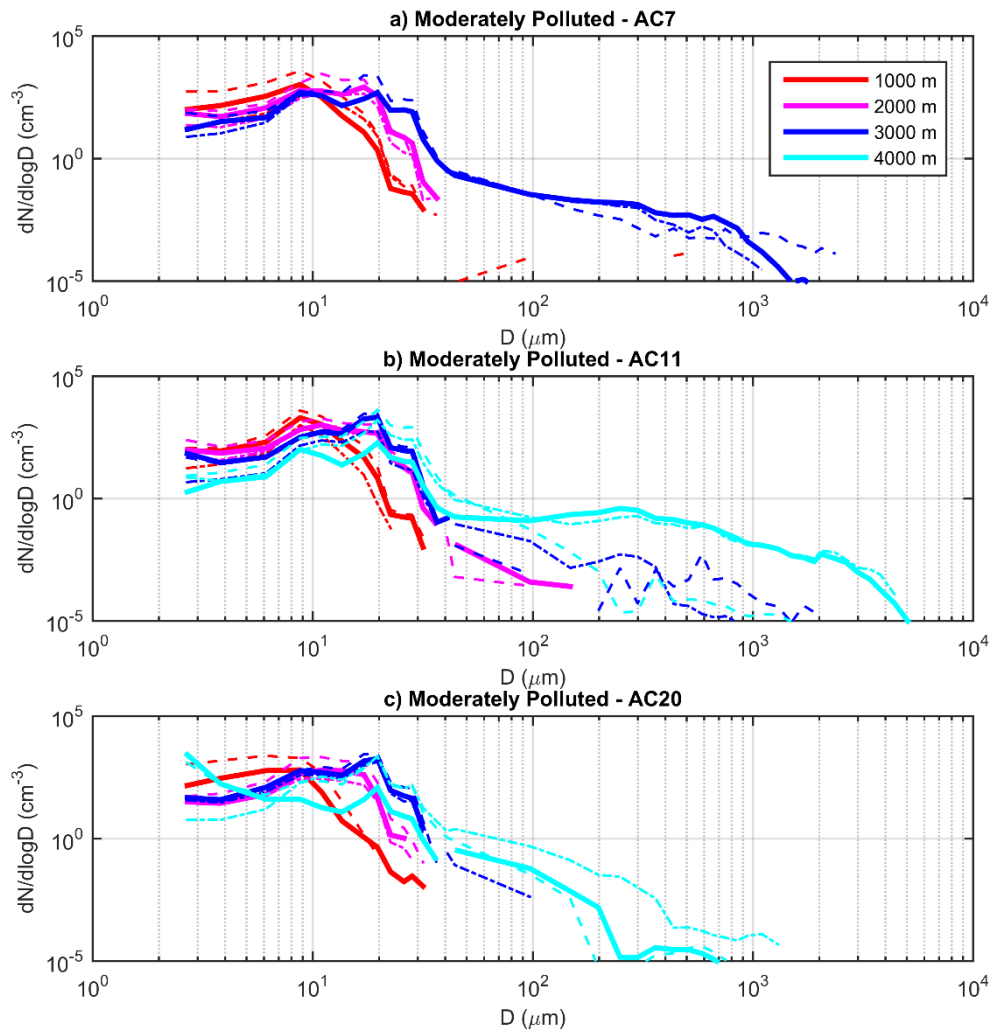


5 **Figure S1.** Droplet size distributions as function of altitude above cloud base, aerosol particle number concentration, and vertical wind speed,  $W$ , for flight AC19. Four 1000-m-thick layers are considered in the vertical, where the legends in the graphs show the respective upper limit of each one. Solid lines represent averaged DSDs for  $-1 \text{ m s}^{-1} \leq W \leq 1 \text{ m s}^{-1}$ , i.e., for relatively neutral vertical movements. Dashed lines represent averaged DSDs for the updraft regions where  $W > 1 \text{ m s}^{-1}$ , and dot-dashed lines represent the downdrafts ( $W < -1 \text{ m s}^{-1}$ ).

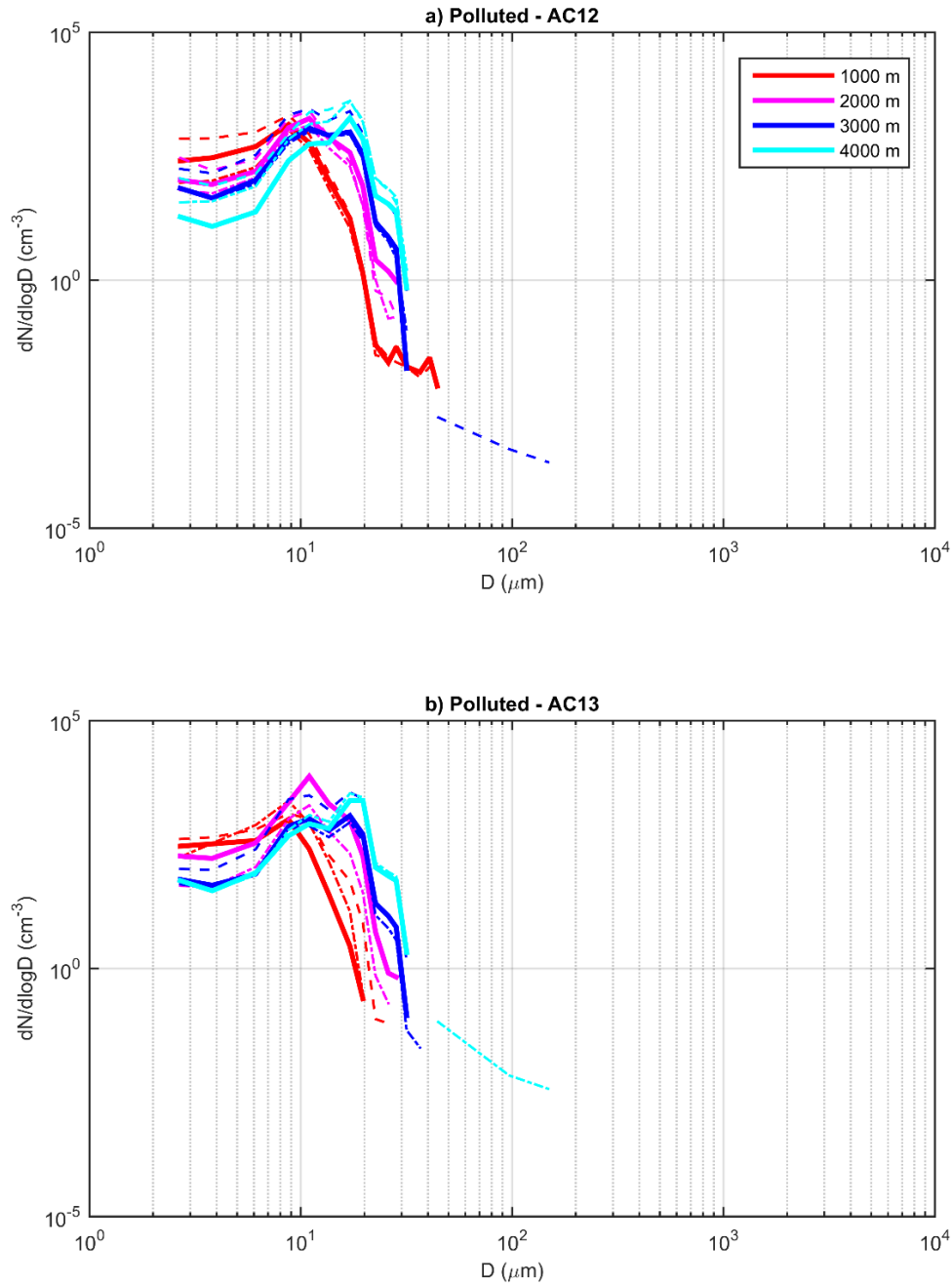
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**Figure S2.** Droplet size distributions as function of altitude above cloud base, aerosol particle number concentration, and vertical wind speed,  $W$ , for flights a) AC9 and b) AC18. Four 1000-m-thick layers are considered in the vertical, where the legends in the graphs show the respective upper limit of each one. Solid lines represent averaged DSDs for  $-1 \text{ m s}^{-1} \leq W \leq 1 \text{ m s}^{-1}$ , i.e., for relatively neutral vertical movements. Dashed lines represent averaged DSDs for the updraft regions where  $W > 1 \text{ m s}^{-1}$ , and dot-dashed lines represent the downdrafts ( $W < -1 \text{ m s}^{-1}$ ).



**Figure S3.** Droplet size distributions as function of altitude above cloud base, aerosol particle number concentration, and vertical wind speed,  $W$ , for flights a) AC7, b) AC11, and c) AC20. Four 1000-m-thick layers are considered in the vertical, where the legends in the graphs show the respective upper limit of each one. Solid lines represent averaged DSDs for  $-1 \text{ m s}^{-1} \leq W \leq 1 \text{ m s}^{-1}$ , i.e., for relatively neutral vertical movements. Dashed lines represent averaged DSDs for the updraft regions where  $W > 1 \text{ m s}^{-1}$ , and dot-dashed lines represent the downdrafts ( $W < -1 \text{ m s}^{-1}$ ).



**Figure S4.** Droplet size distributions as function of altitude above cloud base, aerosol particle number concentration, and vertical wind speed,  $W$ , for flights a) AC12 and b) AC13. Four 1000-m-thick layers are considered in the vertical, where the legends in the graphs show the respective upper limit of each one. Solid lines represent averaged DSDs for  $-1 \text{ m s}^{-1} \leq W \leq 1 \text{ m s}^{-1}$ , i.e., for relatively neutral vertical movements. Dashed lines represent averaged DSDs for the updraft regions where  $W > 1 \text{ m s}^{-1}$ , and dot-dashed lines represent the downdrafts ( $W < -1 \text{ m s}^{-1}$ ).

### Sensitivities for individual intervals

By fixing two dimensions in the 3D matrices and varying the third, we can obtain individual sensitivities in the form of the Equation 1 in the manuscript. As an example, we can fix both  $w$  and  $H$  and obtain the sensitivities of DSD parameters to varying  $N_a$ . By using the natural logarithm scale and applying a linear fit, we obtain the sensitivity as the angular coefficient and the  $R^2$  parameter is a measure of the significance of the relation. By calculating every possible combination, we obtain Tables S1-15 shown below. The amount of 1 Hz data for each sensitivity are shown in Tables S16-18.

$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	-0.11 R <sup>2</sup> = 0.85	-0.27 R <sup>2</sup> = 0.96	-0.25 R <sup>2</sup> = 0.99	-0.23 R <sup>2</sup> = 0.94	-0.38 R <sup>2</sup> = 0.97	-0.47 R <sup>2</sup> = 0.71
<b>1</b>	-0.13 R <sup>2</sup> = 0.84	-0.26 R <sup>2</sup> = 0.93	-0.30 R <sup>2</sup> = 0.99	-0.18 R <sup>2</sup> = 0.86	-0.25 R <sup>2</sup> = 1.00	-0.26 R <sup>2</sup> = 0.96
<b>2</b>	-0.16 R <sup>2</sup> = 0.79	-0.26 R <sup>2</sup> = 0.98	-0.28 R <sup>2</sup> = 0.91	-0.17 R <sup>2</sup> = 0.64	-0.31 R <sup>2</sup> = 0.98	-0.16 R <sup>2</sup> = 0.53
<b>4</b>	-0.18 R <sup>2</sup> = 0.82	-0.28 R <sup>2</sup> = 0.95	-0.25 R <sup>2</sup> = 0.96	-0.25 R <sup>2</sup> = 0.95	-0.31 R <sup>2</sup> = 0.95	-0.28 R <sup>2</sup> = 0.99
<b>8</b>	-	-	-	-	-0.26 R <sup>2</sup> = 0.80	-0.33 R <sup>2</sup> = 0.98

**Table S1.** sensitivities of  $D_{eff}$  to  $N_a$  -  $S_{D_{eff}}(N_a) = \frac{\partial \ln D_{eff}}{\partial \ln N_a} \Big|_{w,H}$ . Intervals upper limits are highlighted in bold letters.

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$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	0.020 R <sup>2</sup> = 0.63	0.049 R <sup>2</sup> = 0.61	0.048 R <sup>2</sup> = 0.90	-0.018 R <sup>2</sup> = 0.034	0.032 R <sup>2</sup> = 0.77	-
<b>1000</b>	0.018 R <sup>2</sup> = 0.17	0.031 R <sup>2</sup> = 0.57	0.0072 R <sup>2</sup> = 0.029	0.046 R <sup>2</sup> = 0.71	0.0032 R <sup>2</sup> = 0.0040	0.0034 R <sup>2</sup> = 0.0010
<b>3000</b>	0.031 R <sup>2</sup> = 0.90	0.044 R <sup>2</sup> = 0.69	-	-0.011 R <sup>2</sup> = 0.055	0.13 R <sup>2</sup> = 0.93	0.18 R <sup>2</sup> = 0.72
<b>4500</b>	-0.085 R <sup>2</sup> = 0.97	0.013 R <sup>2</sup> = 0.57	0.046 R <sup>2</sup> = 0.62	-0.0063 R <sup>2</sup> = 0.23	0.021 R <sup>2</sup> = 0.44	0.024 R <sup>2</sup> = 0.48

**Table S2.** sensitivities of  $D_{eff}$  to  $w$  -  $S_{D_{eff}}(w) = \frac{\partial \ln D_{eff}}{\partial \ln w} \Big|_{N_a,H}$ . Intervals upper limits are highlighted in bold letters.

$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	0.33 R <sup>2</sup> = 0.98	0.27 R <sup>2</sup> = 0.92	0.31 R <sup>2</sup> = 0.85	0.32 R <sup>2</sup> = 0.92	-
<b>1000</b>	0.35 R <sup>2</sup> = 0.98	0.32 R <sup>2</sup> = 0.99	0.30 R <sup>2</sup> = 0.95	0.32 R <sup>2</sup> = 1.00	0.41 R <sup>2</sup> = 0.94
<b>3000</b>	0.14 R <sup>2</sup> = 0.62	0.23 R <sup>2</sup> = 0.90	0.28 R <sup>2</sup> = 0.96	0.26 R <sup>2</sup> = 0.97	0.27 R <sup>2</sup> = 0.96
<b>4500</b>	0.19 R <sup>2</sup> = 0.95	0.24 R <sup>2</sup> = 0.98	0.24 R <sup>2</sup> = 0.99	0.26 R <sup>2</sup> = 0.97	-

**Table S3.** sensitivities of  $D_{eff}$  to  $H$  -  $S_{D_{eff}}(H) = \frac{\partial \ln D_{eff}}{\partial \ln H} \Big|_{N_a, w}$ . Intervals upper limits are highlighted in bold letters.

$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	0.69 R <sup>2</sup> = 0.97	0.75 R <sup>2</sup> = 0.82	1.23 R <sup>2</sup> = 0.89	0.64 R <sup>2</sup> = 0.86	-0.069 R <sup>2</sup> = 0.011	1.24 R <sup>2</sup> = 0.83
<b>1</b>	0.67 R <sup>2</sup> = 0.90	0.79 R <sup>2</sup> = 0.87	0.90 R <sup>2</sup> = 1.00	0.87 R <sup>2</sup> = 0.88	0.70 R <sup>2</sup> = 1.00	1.11 R <sup>2</sup> = 0.95
<b>2</b>	0.72 R <sup>2</sup> = 0.84	0.89 R <sup>2</sup> = 0.98	1.049 R <sup>2</sup> = 0.94	0.87 R <sup>2</sup> = 0.92	0.90 R <sup>2</sup> = 0.92	1.40 R <sup>2</sup> = 0.96
<b>4</b>	0.54 R <sup>2</sup> = 0.62	0.85 R <sup>2</sup> = 0.95	0.79 R <sup>2</sup> = 0.99	0.49 R <sup>2</sup> = 0.37	0.72 R <sup>2</sup> = 0.92	1.22 R <sup>2</sup> = 0.98
<b>8</b>	-	-	-	-	0.94 R <sup>2</sup> = 1.00	0.83 R <sup>2</sup> = 0.98

**Table S4.** sensitivities of  $N_d$  to  $N_a$  -  $S_{N_d}(N_a) = \frac{\partial \ln N_d}{\partial \ln N_a} \Big|_{w, H}$ . Intervals upper limits are highlighted in bold letters.

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$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	0.57 R <sup>2</sup> = 1.00	0.46 R <sup>2</sup> = 0.89	0.86 R <sup>2</sup> = 0.97	-0.12 R <sup>2</sup> = 0.070	0.40 R <sup>2</sup> = 0.76	-
<b>1000</b>	0.45 R <sup>2</sup> = 0.91	0.44 R <sup>2</sup> = 0.99	0.34 R <sup>2</sup> = 0.47	0.32 R <sup>2</sup> = 0.89	0.29 R <sup>2</sup> = 0.91	0.64 R <sup>2</sup> = 0.89
<b>3000</b>	0.61 R <sup>2</sup> = 0.94	0.85 R <sup>2</sup> = 0.96	-	0.37 R <sup>2</sup> = 0.82	0.39 R <sup>2</sup> = 0.95	0.65 R <sup>2</sup> = 0.92
<b>4500</b>	0.24 R <sup>2</sup> = 0.91	0.30 R <sup>2</sup> = 0.89	0.41 R <sup>2</sup> = 0.67	-0.37 R <sup>2</sup> = 0.46	1.034 R <sup>2</sup> = 0.70	0.38 R <sup>2</sup> = 0.90

**Table S5.** sensitivities of  $N_d$  to  $w$  -  $S_{N_d}(w) = \frac{\partial \ln N_d}{\partial \ln w} \Big|_{N_a, H}$ . Intervals upper limits are highlighted in bold letters.

$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	0.20 R <sup>2</sup> = 0.11	-0.29 R <sup>2</sup> = 0.97	-0.084 R <sup>2</sup> = 0.20	-0.094 R <sup>2</sup> = 0.080	-
<b>1000</b>	-0.24 R <sup>2</sup> = 0.36	-0.21 R <sup>2</sup> = 0.24	-0.22 R <sup>2</sup> = 0.21	-0.26 R <sup>2</sup> = 0.54	-0.15 R <sup>2</sup> = 0.64
<b>3000</b>	-0.11 R <sup>2</sup> = 0.97	-0.14 R <sup>2</sup> = 0.26	-0.22 R <sup>2</sup> = 0.94	-0.32 R <sup>2</sup> = 0.89	-0.26 R <sup>2</sup> = 0.85
<b>4500</b>	-0.26 R <sup>2</sup> = 0.094	0.068 R <sup>2</sup> = 0.14	0.075 R <sup>2</sup> = 0.056	0.081 R <sup>2</sup> = 0.022	-

**Table S6.** sensitivities of  $N_d$  to  $H$  -  $S_{N_d}(H) = \frac{\partial \ln N_d}{\partial \ln H} \Big|_{N_a, w}$ . Intervals upper limits are highlighted in bold letters.

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$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	0.30	-0.11	0.48	-0.022	-1.11	0.058
	R <sup>2</sup> = 0.97	R <sup>2</sup> = 0.070	R <sup>2</sup> = 0.66	R <sup>2</sup> = 0.013	R <sup>2</sup> = 0.82	R <sup>2</sup> = 0.0052
<b>1</b>	0.24	-0.030	0.055	0.43	0.024	0.62
	R <sup>2</sup> = 0.40	R <sup>2</sup> = 0.0072	R <sup>2</sup> = 0.42	R <sup>2</sup> = 0.50	R <sup>2</sup> = 0.12	R <sup>2</sup> = 0.90
<b>2</b>	0.22	0.021	0.23	0.41	-0.043	0.60
	R <sup>2</sup> = 0.26	R <sup>2</sup> = 0.019	R <sup>2</sup> = 0.21	R <sup>2</sup> = 0.34	R <sup>2</sup> = 0.097	R <sup>2</sup> = 0.41
<b>4</b>	0.032	-0.025	0.015	-0.42	-0.12	0.20
	R <sup>2</sup> = 0.0033	R <sup>2</sup> = 0.0067	R <sup>2</sup> = 0.054	R <sup>2</sup> = 0.25	R <sup>2</sup> = 0.29	R <sup>2</sup> = 0.98
<b>8</b>	-	-	-	-	0.15	-0.20
					R <sup>2</sup> = 0.17	R <sup>2</sup> = 0.90

**Table S7.** sensitivities of  $LWC$  to  $N_a$  -  $S_{LWC}(N_a) = \frac{\partial \ln LWC}{\partial \ln N_a} \Big|_{w,H}$ . Intervals upper limits are highlighted in bold letters.

$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	0.62	0.60	1.024	0.060	0.34	-
	R <sup>2</sup> = 1.00	R <sup>2</sup> = 0.85	R <sup>2</sup> = 0.98	R <sup>2</sup> = 0.0047	R <sup>2</sup> = 0.91	
<b>1000</b>	0.50	0.42	0.37	0.42	0.31	0.69
	R <sup>2</sup> = 0.87	R <sup>2</sup> = 0.90	R <sup>2</sup> = 0.43	R <sup>2</sup> = 0.88	R <sup>2</sup> = 0.85	R <sup>2</sup> = 0.75
<b>3000</b>	0.70	0.94	-	0.33	0.70	0.89
	R <sup>2</sup> = 0.97	R <sup>2</sup> = 0.94		R <sup>2</sup> = 0.72	R <sup>2</sup> = 0.96	R <sup>2</sup> = 0.87
<b>4500</b>	0.10	0.33	0.53	-0.47	1.00	0.42
	R <sup>2</sup> = 0.44	R <sup>2</sup> = 0.84	R <sup>2</sup> = 0.70	R <sup>2</sup> = 0.64	R <sup>2</sup> = 0.66	R <sup>2</sup> = 0.81

**Table S8.** sensitivities of  $LWC$  to  $w$  -  $S_{LWC}(w) = \frac{\partial \ln LWC}{\partial \ln w} \Big|_{N_a,H}$ . Intervals upper limits are highlighted in bold letters.

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$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	1.14 $R^2 = 0.83$	0.27 $R^2 = 0.45$	0.74 $R^2 = 0.62$	0.80 $R^2 = 0.84$	-
<b>1000</b>	0.73 $R^2 = 0.92$	0.69 $R^2 = 0.90$	0.65 $R^2 = 0.65$	0.71 $R^2 = 0.92$	1.062 $R^2 = 0.79$
<b>3000</b>	0.51 $R^2 = 0.61$	0.58 $R^2 = 0.76$	0.64 $R^2 = 0.95$	0.48 $R^2 = 0.92$	0.52 $R^2 = 0.86$
<b>4500</b>	0.36 $R^2 = 0.16$	0.77 $R^2 = 0.98$	0.70 $R^2 = 0.83$	0.76 $R^2 = 0.62$	-

**Table S9.** sensitivities of  $LWC$  to  $H$  -  $S_{LWC}(H) = \left. \frac{\partial \ln LWC}{\partial \ln H} \right|_{N_a, w}$ . Intervals upper limits are highlighted in bold letters.

$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	-0.25 $R^2 = 0.50$	0.20 $R^2 = 0.50$	0.51 $R^2 = 0.70$	0.43 $R^2 = 0.74$	0.53 $R^2 = 0.87$	0.54 $R^2 = 0.40$
<b>1</b>	-0.33 $R^2 = 0.76$	0.12 $R^2 = 0.17$	0.62 $R^2 = 0.87$	0.37 $R^2 = 0.87$	0.37 $R^2 = 62$	0.74 $R^2 = 0.86$
<b>2</b>	-0.42 $R^2 = 0.93$	0.11 $R^2 = 0.28$	0.40 $R^2 = 0.91$	0.40 $R^2 = 0.66$	0.51 $R^2 = 0.86$	0.069 $R^2 = 0.13$
<b>4</b>	-0.54 $R^2 = 0.97$	-0.15 $R^2 = 0.39$	0.062 $R^2 = 0.20$	0.29 $R^2 = 0.36$	0.56 $R^2 = 0.88$	0.14 $R^2 = 0.18$
<b>8</b>	-	-	-	-	0.52 $R^2 = 0.99$	0.090 $R^2 = 0.93$

**Table S10.** sensitivities of  $\Lambda$  to  $N_a$  -  $S_{\Lambda}(N_a) = \left. \frac{\partial \ln \Lambda}{\partial \ln N_a} \right|_{w, H}$ . Intervals upper limits are highlighted in bold letters.

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$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	0.35 R <sup>2</sup> = 0.98	0.35 R <sup>2</sup> = 0.65	0.41 R <sup>2</sup> = 0.66	0.049 R <sup>2</sup> = 0.14	-0.090 R <sup>2</sup> = 0.98	-
<b>1000</b>	0.061 R <sup>2</sup> = 0.24	0.0043 R <sup>2</sup> = 0.0037	-0.062 R <sup>2</sup> = 0.11	0.19 R <sup>2</sup> = 0.67	-0.11 R <sup>2</sup> = 0.75	0.24 R <sup>2</sup> = 0.82
<b>3000</b>	-0.062 R <sup>2</sup> = 0.31	0.13 R <sup>2</sup> = 0.55	-	0.015 R <sup>2</sup> = 0.045	-0.14 R <sup>2</sup> = 0.83	-0.15 R <sup>2</sup> = 0.42
<b>4500</b>	-0.0064 R <sup>2</sup> = 0.13	-0.11 R <sup>2</sup> = 0.91	-0.097 R <sup>2</sup> = 0.82	-0.18 R <sup>2</sup> = 0.23	0.0068 R <sup>2</sup> = 0.0089	0.049 R <sup>2</sup> = 0.56

**Table S11.** sensitivities of  $\Lambda$  to  $w$  -  $S_{\Lambda}(w) = \left. \frac{\partial \ln \Lambda}{\partial \ln w} \right|_{N_a, H}$ . Intervals upper limits are highlighted in bold letters.

$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	-0.75 R <sup>2</sup> = 0.96	-0.84 R <sup>2</sup> = 0.94	-0.94 R <sup>2</sup> = 0.98	-1.11 R <sup>2</sup> = 0.97	-
<b>1000</b>	-0.61 R <sup>2</sup> = 0.98	-0.63 R <sup>2</sup> = 0.96	-0.47 R <sup>2</sup> = 0.87	-0.54 R <sup>2</sup> = 0.86	-0.25 R <sup>2</sup> = 0.073
<b>3000</b>	-0.10 R <sup>2</sup> = 0.088	-0.17 R <sup>2</sup> = 0.48	-0.25 R <sup>2</sup> = 0.54	-0.21 R <sup>2</sup> = 0.34	-0.26 R <sup>2</sup> = 0.38
<b>4500</b>	-0.17 R <sup>2</sup> = 0.47	-0.15 R <sup>2</sup> = 0.43	-0.15 R <sup>2</sup> = 0.50	-0.14 R <sup>2</sup> = 0.62	-

**Table S12.** sensitivities of  $\Lambda$  to  $H$  -  $S_{\Lambda}(H) = \left. \frac{\partial \ln \Lambda}{\partial \ln H} \right|_{N_a, w}$ . Intervals upper limits are highlighted in bold letters.

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$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	0.17 R <sup>2</sup> = 0.81	0.013 R <sup>2</sup> = 0.014	-0.17 R <sup>2</sup> = 0.45	-0.12 R <sup>2</sup> = 0.66	-0.097 R <sup>2</sup> = 0.56	-0.097 R <sup>2</sup> = 0.36
<b>1</b>	0.21 R <sup>2</sup> = 0.93	0.066 R <sup>2</sup> = 0.21	-0.19 R <sup>2</sup> = 0.75	-0.11 R <sup>2</sup> = 0.80	-0.080 R <sup>2</sup> = 38	-0.24 R <sup>2</sup> = 0.77
<b>2</b>	0.30 R <sup>2</sup> = 0.95	0.027 R <sup>2</sup> = 0.068	-0.12 R <sup>2</sup> = 0.98	-0.14 R <sup>2</sup> = 0.50	-0.14 R <sup>2</sup> = 0.72	0.036 R <sup>2</sup> = 0.090
<b>4</b>	0.44 R <sup>2</sup> = 1.00	0.091 R <sup>2</sup> = 0.24	0.0092 R <sup>2</sup> = 0.018	-0.072 R <sup>2</sup> = 0.12	-0.17 R <sup>2</sup> = 0.70	0.0031 R <sup>2</sup> = 0.0012
<b>8</b>	-	-	-	-	-0.18 R <sup>2</sup> = 0.94	0.16 R <sup>2</sup> = 0.95

**Table S13.** sensitivities of  $\varepsilon$  to  $N_a$  -  $S_\varepsilon(N_a) = \left. \frac{\partial \ln \varepsilon}{\partial \ln N_a} \right|_{w,H}$ . Intervals upper limits are highlighted in bold letters.

$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	-0.29 R <sup>2</sup> = 0.95	-0.11 R <sup>2</sup> = 0.60	-0.19 R <sup>2</sup> = 0.80	0.015 R <sup>2</sup> = 0.057	0.063 R <sup>2</sup> = 1.00	-
<b>1000</b>	-0.080 R <sup>2</sup> = 0.41	-0.016 R <sup>2</sup> = 0.71	0.076 R <sup>2</sup> = 0.34	-0.12 R <sup>2</sup> = 0.78	0.049 R <sup>2</sup> = 0.53	-0.14 R <sup>2</sup> = 0.86
<b>3000</b>	0.037 R <sup>2</sup> = 0.31	-0.17 R <sup>2</sup> = 0.76	-	0.00013 R <sup>2</sup> = 0.000024	0.0024 R <sup>2</sup> = 0.0019	-0.035 R <sup>2</sup> = 0.22
<b>4500</b>	0.027 R <sup>2</sup> = 0.51	0.037 R <sup>2</sup> = 0.61	0.024 R <sup>2</sup> = 0.53	0.018 R <sup>2</sup> = 0.30	-0.025 R <sup>2</sup> = 0.27	-0.023 R <sup>2</sup> = 0.28

**Table S14.** sensitivities of  $\varepsilon$  to  $w$  -  $S_\varepsilon(w) = \left. \frac{\partial \ln \varepsilon}{\partial \ln w} \right|_{N_a,H}$ . Intervals upper limits are highlighted in bold letters.

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$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	0.22 R <sup>2</sup> = 0.85	0.30 R <sup>2</sup> = 0.73	0.36 R <sup>2</sup> = 0.94	0.48 R <sup>2</sup> = 0.99	-
<b>1000</b>	0.15 R <sup>2</sup> = 0.79	0.16 R <sup>2</sup> = 0.82	0.094 R <sup>2</sup> = 0.63	0.16 R <sup>2</sup> = 0.74	-0.16 R <sup>2</sup> = 0.084
<b>3000</b>	0.0066 R <sup>2</sup> = 0.0045	0.0093 R <sup>2</sup> = 0.030	0.017 R <sup>2</sup> = 0.046	0.028 R <sup>2</sup> = 0.032	0.010 R <sup>2</sup> = 0.0024
<b>4500</b>	-0.022 R <sup>2</sup> = 0.062	-0.037 R <sup>2</sup> = 0.20	-0.036 R <sup>2</sup> = 0.17	-0.046 R <sup>2</sup> = 0.29	-

**Table S15.** sensitivities of  $\varepsilon$  to  $H$  -  $S_\varepsilon(H) = \frac{\partial \ln \varepsilon}{\partial \ln H} \Big|_{N_a, w}$ . Intervals upper limits are highlighted in bold letters.

$w$ (m s <sup>-1</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>0.5</b>	289	89	21	32	36	45
<b>1</b>	247	82	20	24	22	45
<b>2</b>	223	87	26	34	28	49
<b>4</b>	111	47	30	37	29	38
<b>8</b>	0	0	0	0	18	27

**Table S16.** number of 1 Hz DSD data for the sensitivities to  $N_a$ .

$N_a$ (cm <sup>-3</sup> ) \ $H$ (m)	<b>200</b>	<b>500</b>	<b>950</b>	<b>1625</b>	<b>2637.5</b>	<b>4156.25</b>
<b>500</b>	259	84	28	27	11	0
<b>1000</b>	234	84	38	40	56	81
<b>3000</b>	265	91	0	61	43	75
<b>4500</b>	125	55	25	16	23	44

5 **Table S17.** number of 1 Hz DSD data for the sensitivities to  $w$ .

$N_a$ (cm <sup>-3</sup> ) \ $w$ (m s <sup>-1</sup> )	<b>0.5</b>	<b>1</b>	<b>2</b>	<b>4</b>	<b>8</b>
<b>500</b>	169	119	90	35	0
<b>1000</b>	137	136	146	94	20
<b>3000</b>	142	100	138	110	51
<b>4500</b>	64	85	73	53	0

**Table S18.** number of 1 Hz DSD data for the sensitivities to  $H$ .