

This discussion paper is/has been under review for the journal Atmospheric Chemistry and Physics (ACP). Please refer to the corresponding final paper in ACP if available.

On retrieving refractive index of dust-like particles using shape distributions of ellipsoids

O. Kemppinen^{1,2}, T. Nousiainen¹, S. Merikallio¹, and P. Räisänen¹

Received: 17 April 2015 - Accepted: 31 May 2015 - Published: 19 June 2015

Correspondence to: O. Kemppinen (osku.kemppinen@fmi.fi)

Published by Copernicus Publications on behalf of the European Geosciences Union.

Discussion

Discussion Paper

Paper

Discussion Paper

Discussion Paper

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version



¹Earth Observation, Finnish Meteorological Institute, Helsinki, Finland

²Department of Applied Physics, Aalto University, Espoo, Finland

Ellipsoid-based retrievals are widely used for investigating optical properties of nonellipsoidal atmospheric particles, such as dust. In this work, the applicability of ellipsoids for retrieving the refractive index of dust-like target model particles from scattering data is investigated. This is a pure modeling study, where stereogrammetrically retrieved model dust shapes are used as targets. The primary objective is to study whether the refractive index of these target particles can be inverted from their scattering matrices using ellipsoidal model particles. To achieve this, first scattering matrices for the target model particles with known refractive indices are computed. On one hand, a non-negative least squares fitting is performed, separately for different scattering matrix elements, for a set of 46 differently shaped ellipsoids by using different assumed refractive indices. Then, the fitting error is evaluated to establish whether the ellipsoidal base best matches the target scattering matrix elements when the correct refractive index is assumed. On the other hand, we also test whether the ellipsoids best match the target data with the correct refractive index, if a predefined (uniform) shape distribution for ellipsoids is assumed, instead of optimizing the shape distribution separately for each tested refractive index. The results show that for both of these approaches using the ellipsoids with the true refractive index produces good results, but also that for each element even better results are acquired by using wrong refractive indices. In addition, the best agreement is found for different scattering matrix elements using different refractive indices. The findings imply that the inversion of refractive index of non-ellipsoidal particles may not be reliable using ellipsoids. Furthermore, it is demonstrated that the differences in single-scattering albedo and asymmetry parameter between the best-match ellipsoid ensemble and the target particles may give rise to major differences in simulated aerosol radiative effects.

ACPD

Paper

Discussion Paper

Discussion Paper

Discussion Paper

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ✓ ▶I

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Mineral dust particles are abundant constituents of the Earth's atmoshere (Zender et al., 2003). Through scattering and absorption, these particles interact with electromagnetic radiation propagating in the atmosphere, inducing effects that should be 5 accounted for in radiative balance considerations and in atmospheric remote sensing (e.g. Durant et al., 2009; Haywood et al., 2011).

Dust particles are irregularly shaped and often inhomogeneous, making accurate computations of their single-scattering properties a challenge (Nousiainen et al., 2009; Nousiainen and Kandler, 2015; Zubko et al., 2013). These properties are needed when assessing impacts of the particles on the radiative balance or atmospheric remote sensing measurements. Single-scattering simulations, where the particle irregularity and inhomogeneity can be explicitly accounted for require, in practice, volume-integral methods such as the discrete-dipole approximation (Draine and Flatau, 1994; Penttilä et al., 2007; Yurkin and Hoekstra, 2011). Such methods are, however, computationally demanding and become quite impractical once the particle diameter exceeds the wavelength considerably. Therefore, simpler methods have often been applied to compute dust particles' single-scattering properties. In particular, in applications such as radiative balance assessments or satellite remote sensing, where one needs to consider multiple wavelengths, these simpler but often considerably faster methods are almost

et al. (1997); Dubovik et al. (2006); Bi et al. (2009); Meng et al. (2010) and Merikallio et al. (2013), a suitable set of ellipsoids (or their subset spheroids) can closely mimic scattering by real dust particles. To ease their application, Meng et al. (2010) offer tion of ellipsoid shape, size and refractive index. This database has been used, e.g., to model single-scattering properties of Martian dust analog particles (Merikallio et al., 2013). Regarding the ellipsoids, one fundamental question related to their use is the

Paper

Discussion Paper

Discussion Paper

Discussion

Paper

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** Back Close

Printer-friendly Version

Full Screen / Esc

Interactive Discussion



exclusively used. One such simple model geometry is that of ellipsoids. As shown by e.g. Mishchenko a pre-computed database for the single-scattering properties of ellipsoids as a func-

Paper

Printer-friendly Version

Interactive Discussion



choice of the shape distribution. While a single ellipsoidal shape does not provide good overall fits to real dust particles' single-scattering properties, a suitable set of different ellipsoids may do so. The very same thing applies to spheroids: a sub-set of ellipsoids that consist of only rotationally symmetric ellipsoids. For spheroids, it has been shown (Merikallio et al., 2011; Nousiainen et al., 2011) that the set of spheroidal shapes that optimally mimics the scattering properties of dust particles does not necessarily correlate in any clear way with the physical shapes of the target particles; and that at different wavelengths or for different scattering quantities the sets of spheroids that optimally reproduce scattering by a given dust sample may differ. This implies that the good performance of spheroids in reproducing scattering by real dust is in part artificial, having more to do with different spheroids forming a flexible base for fitting, rather than any close resemblance in scattering by individual dust particles and spheroids (Nousiainen et al., 2011; Lindqvist et al., 2014; Nousiainen and Kandler, 2015). In part it is facilitated by the fact that ensembles of different non-spherical particles often have similar scattering properties (Nousiainen et al., 2012). Since generic ellipsoids are very similar model particles to spheroids, the above considerations are likely to apply also to them.

Since ellipsoids provide an even broader base for fitting than spheroids, they are likely to be able to mimic scattering by a wide variety of different target particles. This great flexibility is, however, potentially also a great risk in remote sensing applications, as it may allow good fits to be obtained with measurements based on wrong parameters. Here, we will investigate this issue with regards to the refractive index. To this end, we will use target data comprising single and ensemble-averaged scattering matrices computed for model particles whose shapes have been derived from real, individual dust particles through stereogrammetry.

In what follows, two types of analyses are carried out for the scattering matrix elements. First, we will seek shape distributions for ellipsoids that mimic the target data as faithfully as possible. Second, for comparison, we will perform forward modelling, and adapt a pre-defined uniform shape distribution of ellipsoids. In both cases, the analy-

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** Back Close Full Screen / Esc

2 Methodology

2.1 Theoretical background

The interaction of incident radiation with a particle can be characterized by the scattering equation. One common formulation is with the Stokes vector $[I,Q,U,V]^T$:

$$\begin{pmatrix} I_{s} \\ Q_{s} \\ U_{s} \\ V_{s} \end{pmatrix} = \frac{C_{\text{sca}}}{d^{2}} \begin{bmatrix} P_{11} & P_{12} & P_{13} & P_{14} \\ P_{21} & P_{22} & P_{23} & P_{24} \\ P_{31} & P_{32} & P_{33} & P_{34} \\ P_{41} & P_{42} & P_{43} & P_{44} \end{bmatrix} \begin{pmatrix} I_{i} \\ Q_{i} \\ U_{i} \\ V_{i} \end{pmatrix},$$
(1)

where subscripts "i" and "s" refer to incident and scattered electromagnetic wave, respectively; Stokes parameter I describes the intensity, Q and U the linear polarization, and V the circular polarization of the wave; $C_{\rm sca}$ is the scattering cross-section, and d the distance from the scatterer. The phase matrix thus contains all information about a scattering event that is carried by the scattered wave.

In general, the scattering matrix has 16 elements. However, when

- 1. the particles are randomly oriented, and
- 2. the particles are mirror symmetric, or particles and their mirror particles are present in equal numbers,

iscussio

Discussion Paper

Discussion Paper

Discussion

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Printer-friendly Version

Full Screen / Esc

Interactive Discussion



the scattering matrix simplifies to only six independent, non-zero elements (Hovenier and van der Mee, 2000). Even when all these conditions are not perfectly true, ensembles of irregular particles, such as dust, seem to closely follow this simplified form of scattering matrix (Nousiainen and Kandler, 2015). Thus, in this study, we consider only the independent scattering matrix elements P_{11} , P_{12} , P_{22} , P_{33} , P_{34} and P_{44} . Apart from P_{11} and P_{12} , the elements can be measured in practice only in laboratory conditions, where the polarization state of the incident light can be varied. See, e.g., Muñoz et al. (2010) for an example of an apparatus for measuring the full scattering matrix. Regardless, for the theoretical validity of the ellipsoid retrieval, all six elements are relevant.

In this work, we consider the phase function formulation of the scattering matrix elements. The scattering matrix is thus normalized such that

$$\int_{T_n} P_{11} d\Omega = 1. \tag{2}$$

The scattering matrix, as all dimensionless single-scattering properties, is subject to the scale invariance rule, stating that these properties depend only on the complex refractive index m and the ratio of particle size and wavelength, typically denoted by the size parameter

$$x = \frac{2\pi r}{\lambda},\tag{3}$$

where r is the characteristic radius of the particle and λ the wavelength of the incident radiation. Here, we will take r to be the radius of a volume-equivalent sphere for all the shapes considered. All considerations are done in the (x, m) space, so λ is in principle not fixed, but the parameter values considered are relevant for mineral dust particles at visible light. In this work we fix the target m, which can be considered to fix the analyses to a single wavelength.

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Printer-friendly Version



In order to evaluate the retrieval results, we need to know the actual refractive indices of our target model particles. It is also desirable that the target particles and their scattering properties are representative of real particles. One option would be to use measured scattering properties, but then the refractive index would be uncertain. We therefore choose to use synthetic data, computed using shapes derived from real dust particles by stereogrammetry. It is important to note that despite being inverted from real atmospheric dust particles, the model particles used here may not be completely realistic due to inherent limitations in the stereogrammetric method (Lindqvist et al., 2014). However, for the purposes of this study it is enough that they are complexshaped and irregular, and could plausibly be close to real particles in overall shape and composition. We consider both individual stereogrammetric particles, as well as an ensemble that combines their scattering matrices. The ensemble is a simple scattering cross-section weighted average of the scattering properties for the individual particles. The particles used are described in detail by Lindqvist et al. (2014), whence we also adapt the names of the particles. We use the particles Cal (calcite), Dol (dolomite) and Agg (aggregate of several minerals, quartz being the most abundant) both individually and for the ensemble. The fourth particle, Sil (silicate, mostly chrysotile), is excluded from the ensemble because it was significantly more prolate than what was covered by the ellipsoid data set we used. However, Sil is considered individually, and discussed in the text wherever its results differ from those of the other particles.

In addition to the original stereogrammetric particles, we discuss results based on their artificially roughened variations. The surfaces of the particles were modified using a Monte Carlo ray collision system that creates several small mounds and craters at the surface, therefore reducing the artificial surface smoothness caused by the stereogrammetric method while keeping the overall particle shapes and volumes nearly intact. The roughening method used is described in more detail by Kemppinen et al. (2015).

ACPD

Paper

Discussion Paper

Discussion Paper

Discussion Paper

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



Discussion Paper

Printer-friendly Version

Interactive Discussion



In principle, the roughened particles may represent the real physical targets of the stereogrammetry study more than the original stereogrammetric shapes, due to the fact that the steregrammetry method can not recreate the fine surface roughness of the physical particles. However, the roughening is based on arbitrarily chosen parameters that have not been related in any way with the (possible) roughness characteristics of the target shapes considered here, or any other dust particles. Therefore, we consider the original unroughened particles as the primary target, and use the roughened versions primarily to study the sensitivity of the results to particles' surface roughness. In particular, if moderate changes in surface roughness significantly alter the results of the refractive index retrieval, it can be said that the retrieval algorithm is too sensitive, or the impact of roughness on scattering dominates that of the refractive index.

For the scattering calculations we used version 1.2 MPI of ADDA (Yurkin and Hoekstra, 2011), which implements the discrete-dipole approximation (DDA) (Purcell and Pennypacker, 1973). DDA allows light scattering simulations by an arbitrarily shaped collection of dipoles, which enables great flexibility in representing irregular shapes. DDA is generally accurate as long as the target dipole resolution is sufficient. In this work, the target shapes for all size parameters were discretized into roughly eight hundred thousand dipoles. The value y = |m|kI, where m is the refractive index, k is the wavenumber and / is the dipole size, is typically used to evaluate the applicability of the DDA method. The largest y value for the particles in this study was less than 0.6, which is below the commonly cited DDA accuracy limit of $y \le 1$ (Zubko et al., 2010). The scattering of each target shape was averaged over 8192 random orientations for all size parameters. Figure 1 shows computer-generated renderings of the DDA representations of the target particles. The images were generated with only 1/8th of the dipole resolution compared to the scattering simulations.

ADDA was run on the Finnish Meteorological Institute Cray XC30 supercomputer Voima, using 64 computer cores per simulation. Additionally, 10 concurrent simulations were run in parallel to reduce the total run time. With this setup, the total amount of CPU time used was approximately 46 thousand hours. The resulting scattering ma-

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** Back Close Full Screen / Esc

The scattering matrices for ellipsoids are taken from the database by Meng et al. (2010), where the optical characteristics are tabulated for size parameters of the largest dimension ranging from 0.025 up to 1000. This gives values larger or equal (for the sphere) to the volume-equivalent size parameter used in this study. The database also provides the corresponding volume-equivalent size parameters, which are used here. The database includes the six independent scattering matrix elements and other optical characteristics, such as the scattering cross section, which we use in integration of the ensemble properties. The range of refractive indices includes, in principle, the real part range from 1.10 up to 2.10 and the imaginary part from 0.0005 to 0.5. In practice, not all real and imaginary part combinations have been computed. Here, we will consider only ellipsoids with real parts of the refractive ranging from 1.4 to 1.6 and imaginary parts from 0.0005 to 0.02, for which all possible combinations are available. In total, 46 different ellipsoids with axis ratios ranging from 1.0 to 3.3 are considered, including a sphere, but excluding some nearly spherical ellipsoids, as was done by Merikallio et al. (2013), to reduce the number of shapes to be considered and to facilitate the fitting.

The particle size distribution for both the ellipsoid and the target data is a lognormal distribution with $\sigma_g = 2.0$ and $r_g = 0.4\,\mu\text{m}$ and a cutoff at size parameter 20. All calculations were done with a size parameter resolution of 0.5 for the sizes 0.5...10, and a size parameter resolution of 1.0 for the sizes 11...20.

2.3 Fitting and error definitions

We investigate how well scattering by ellipsoid ensembles can match scattering matrix elements of target particles. Specifically, the scattering matrix elements of the individual ellipsoids form a basis, and we seek the linear combination of the shapes that minimizes the squared difference to the target data. We want the weights of the indi-

Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

Back Close

Printer-friendly Version

Full Screen / Esc

Interactive Discussion



$$\forall I, p_I \in [0, 1], \tag{4}$$

and

$$5 \quad \sum_{l} p_{l} = 1, \tag{5}$$

where the individual shapes are denoted by ξ_l and the corresponding weights are denoted by p_l .

Due to the requirements in Eqs. (4) and (5), we cannot use a standard least-squares fitting algorithm to minimize the error functions. Instead, we adopt a non-negative least squares algorithm from Kahnert et al. (2002), recently used by Merikallio et al. (2011) and Nousiainen et al. (2011), and described below.

The best-fit ensemble will be

$$P_{ij}^{\text{fit}}(\theta) = \sum_{l} \rho_{l} P_{ij}(\theta; \xi_{l}), \tag{6}$$

where $P_{ij}(\theta;\xi_l)$ are the scattering matrix elements of the shape ξ_l , and $l \in \{0,1,2,...,L-1\}$, where L is the total number of different ellipsoid shapes.

Instead of fitting p_I directly, we initially fit parameters q_I . To determine q_I for P_{11} , the quantity to be minimized is

$$e_{11} = \sum_{\theta=0^{\circ}}^{180^{\circ}} \left[\frac{P_{11}^{\text{ref}}(\theta) - \sum_{l} q_{l}^{2} P_{11}(\theta; \xi_{l})}{P_{11}^{\text{ref}}(\theta)} \right]^{2}, \tag{7}$$

where $P_{11}^{\text{ref}}(\theta)$ is the P_{11} element of the target scatterer. This form is designed to eliminate the strong weighing of forward-scattering angles in the fitting due to the typically 16870

ACPD

Discussion Paper

Paper

Discussion

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

I

Back Close

Printer-friendly Version

Full Screen / Esc



For P_{ij} , $ij \in \{12, 22, 33, 34, 44\}$, we minimize

$$e_{ij} = \sum_{\theta=0^{\circ}}^{180^{\circ}} \left[\frac{P_{ij}^{\text{ref}}(\theta)}{P_{11}^{\text{ref}}(\theta)} - \sum_{l} \frac{q_{l}^{2} P_{ij}(\theta; \xi_{l})}{P_{11}(\theta; \xi_{l})} \right]^{2}, \tag{8}$$

where $P_{ii}^{\text{ref}}(\theta)$ is the corresponding P_{ij} element of the target scatterer. The θ grid is the same as above. The minimization is done with Levenberg-Marquardt method, using an uniform initial shape distribution (Press et al., 1992). Due to the fact that the Levenberg-Marguardt method is not guaranteed to find the global optimum, we performed tests with random initial shape distributions. In total, 100 additional shape distributions were tested for P_{11} . 94 of these tests resulted in the same optimal shape distribution as the uniform one, whereas 6 resulted in a significantly larger fit error. Each of these 6 had a very exotic initial distribution, such as only one shape being present, in which case the algorithm might not be able to converge accurately. We conclude that the uniform initial shape distribution is likely to result in a good and consistent optimum. Theoretically, it is possible that there are better optima than those found by this method, but finding them would likely require some a priori information, which would very probably not be available to an instrument team doing retrieval by fitting.

The final normalization for p_i is done by

$$\rho_l = \frac{q_l^2}{\sum_l q_l^2}. ag{9}$$

This ensures that the weights are positive and properly normalized.

In Sect. 3 we show scattering matrix element errors E_{ij} (briefly, "scattering errors"), which are based on e_{ij} from Eqs. (7) and (8):

$$E_{ij} = \sqrt{e_{ij}},\tag{10}$$

Discussion Paper

Discussion Paper

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page

Abstract Introduction Conclusions References **Tables Figures**

> Close Full Screen / Esc

Back

Printer-friendly Version

Interactive Discussion



In the case of a fixed, uniform shape distribution, instead of using p_I from the least squares solution, we use

$$p_I = \frac{1}{L} \tag{11}$$

in the E_{ij} calculations, to get an equal weight for each shape while satisfying Eqs. (4) and (5). The E_{ij} calculations for the fixed shape distribution are otherwise identical.

3 Results

We investigate the validity of the ellipsoid ensemble assumption by fitting scattering matrix elements of a set of ellipsoids to those of target particles, as described in Sect. 2.3. The fitting is done separately for ellipsoids with 40 different refractive indices, $m_r + im_i$, where $m_r \in \{1.40, 1.45, 1.50, 1.55, 1.60\}$ and $m_i \in \{0.0005, 0.001, 0.002, 0.004, 0.005, 0.008, 0.01, 0.02\}$. The number of ellipsoids that the fitting algorithm employs in the best fit of each element is shown in Table 1. We define an ellipsoid to be employed if its weight is 0.1% or larger in the ensemble. The numbers displayed in Table 1 are means across all refractive indices and all the individual particles in addition to the particle ensemble. The results for original and roughened versions of the target particles are shown separately. First, we see that only a relatively small amount of the 46 different ellipsoids are used at any time. Second, we see that some elements require significantly more ellipsoids for the best fit than others. Third, we see that the roughened particles, with their reduced shape regularity, require a slightly, but systematically, smaller number of ellipsoids for the optimal fit.

Additionally, Table 1 shows the mean scattering error for the elements, also averaged over all the individual particles and the ensemble and across all refractive indices. The

iscussion

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Printer-friendly Version

Full Screen / Esc

Interactive Discussion



Discussion Paper

Discussion Paper

Discussion Paper

Discussion Paper

Back Full Screen / Esc

Printer-friendly Version

Interactive Discussion



particles with the added surface roughness seem to produce worse optimum fits on average, though in some individual cases the error is smaller. Furthermore, different elements produce vastly different scattering errors. It seems that there is a modest anticorrelation between the number of ellipsoids in the optimum fit and the mean error of the fit. For example, P_{11} and P_{44} are the elements with the smallest number of ellipsoids used, and they are the two elements with the largest mean fit errors. Correspondingly, P_{12} and P_{34} are the two elements with the highest number of ellipsoids, and their mean fitting errors are the smallest.

Figures 3 and 4 in Sects. 3.1 and 3.2 show the contour plots of the scattering error of the minimum error ellipsoid shape distributions as a function of the real and imaginary parts of the refractive index. The grids in the plots are linearly interpolated to provide a better overview of the data. In the plots, the true real and imaginary refractive indices are shown with black lines. The intersection of these lines at 1.5 + i0.004 shows the refractive index of the target particle, called the true refractive index ($m_{\rm true}$) below. The refractive index with the minimum error of all the ellipsoid refractive indices is marked with a white circle, and is called the optimum refractive index $(m_{\rm opt})$ in the text. The key question to be investigated is what is the relationship between m_{true} and m_{ont} , specifically whether they are close enough for the retrieval process to be considered valid.

We show the scattering errors only for the ensemble of the original unroughened stereogrammetric particles. The figures for individual particles are not shown, because in most cases the plots for the individual particles match those of the ensemble relatively well. In case there are discrepancies, we will note them in the text. Similarly, the results of the roughened particles are not shown, but are described in the text whenever noteworthy.

The results for individual particles are shown in Tables 2 and 3. The numbers in these tables are the complex refractive index differences $\Delta m = m_{\rm opt} - m_{\rm true}$, and they describe if the optimum refractive index parts are larger or smaller than the true refractive index. Values in bold indicate that $m_{\rm opt}$ is at the edge of the computational domain, meaning

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** Close

It is important to note that the similarities in the m_{opt} values and error contours between different particles are not due to the scattering matrix elements of these particles being very similar. As seen in Fig. 2, there are considerable differences in the scattering matrix elements between the particles.

Fitted shape distribution

First, we take a look at Fig. 3, which shows the results based on fitting the ellipsoid ensemble to the scattering matrix elements of the target scatterer. The good-fit region of P_{11} is located on the small imaginary refractive index side, trending to larger real refractive indices. The optimum refractive index is found at 1.5 + i0.0005. Cal and Agg follow the ensemble result closely, but Dol is slightly different in that the good-fit region reaches even the minimum real refractive indices. Sil behaves differently: only a relatively local subspace of refractive indices produces decent fits. This region is located at the maximum real and imaginary refractive index, where the fit for the other particles is very poor.

The near-optimum band for P_{12}/P_{11} of the ensemble covers most of the refractive index space of m_r greater than 1.5, apart from a local, but prominent, local maximum at the top-right corner, where both the real and imaginary parts of the refractive index have their largest values. Low real refractive indices produce poor fits, in particular if the imaginary part is small as well. All the constituents of the ensemble behave very similarly to the ensemble. The error map for Sil, however, is almost an inverse of the error map of the ensemble. That is, the good-fit refractive indices of the ensemble produce poor fits for Sil, and vice versa.

 P_{22}/P_{11} for the ensemble has the optimum refractive index at 1.5 + i0.0005, but all refractive indices with low-to-medium imaginary part, regardless of the real part, seem to provide good fits. Large imaginary refractive indices, especially if the real part is small, provide poor fits. Cal and Agg are very close to the ensemble, but Dol and Sil

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page

Abstract Conclusions **Tables**

Close

Introduction

References

Figures

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



16874

Discussion Paper

Paper

Discussion Paper

Discussion Paper







differ. For Sil, the imaginary refractive index dependence is similar in that large $m_{\rm i}$ provide poor fits, but the difference is that low real parts provide poor fits as well. For Dol, compared to the ensemble, there is an additional error maximum at high real and low imaginary refractive indices, and only low real refractive indices and low-to-medium imaginary refractive indices provide good fits.

For P_{33}/P_{11} , all real refractive indices below 1.5 provide reasonably good fits for the ensemble, especially if the imaginary part is small as well. Refractive indices with a large real part and a large imaginary part provide very poor fits. This behavior is true for Cal, Dol and Agg, but Sil behaves differently. For Sil, the optimum refractive index is at 1.6 + i0.004, and only refractive indices very near that point provide decent fits. In particular, low real parts, which are good for the other particles and the ensemble, provide very poor fits for Sil.

Compared to the previous elements, the behavior of P_{34}/P_{11} for the ensemble is less straightforward in terms of the refractive indices. There are narrow bands along both axes where the errors are small, but even small changes in the refractive index might have a very large effect on the magnitude of the error. This is in contrast to the elements analyzed above, where the gradients were often relatively mild on both of the refractive index axes. The worst fits are found at low real and low imaginary refractive indices. Dol and Agg follow the behavior of the ensemble relatively well, but Cal and Sil differ. For Cal, the difference is that very small real refractive indices produce decent fits, as do very small imaginary refractive indices, while values around m = 1.45 + i0.002 are still having high errors. For Sil the good-fit region is centered at m = 1.5 + i0.0005, expanding to large imaginary refractive indices, but staying localized at the real axis.

 P_{44}/P_{11} is nearly identical to P_{33}/P_{11} for the ensemble and all individual particles, and is not described separately.

Considering the impact of surface roughness on the retrievals, P_{34}/P_{11} is the only element for which the results deviate markedly from those for the original shapes. Cal and Dol exhibit a major effect, whereas the other particles are not affected noticeably. For both Cal and Dol, the refractive indices that produce the worst fits for the unrough-

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

■ Back Close

Full Screen / Esc

Printer-friendly Version



ened versions produce the best fits for the roughened version. The opposite is also true, especially for Cal: the refractive indices that produce good fits for the unroughened particle produce poor fits for the roughened particle.

3.2 Fixed shape distribution

In addition to allowing the ellipsoid shape distribution to vary while searching for the best-fitting m, we also investigate how the scattering error depends on m when the shape distribution is fixed. For this, we use a uniform distribution that assigns equal weights for all shapes in the distribution, as per Eq. (11). The distribution therefore includes all 46 ellipsoidal shapes. Figure 4 shows the contour plots of E_{ij} for this case.

The minimum scattering matrix element errors are found at the maximum real part and the minimum imaginary part of the refractive index for P_{11} of the particle ensemble. In general, all refractive indices with the imaginary part less than 0.004 have relatively small errors, regardless of the value of the real part. Similarly, all refractive indices with large imaginary parts have large errors. Cal, Dol and Agg are all very similar to the ensemble, while Sil is notably different. In fact, as was the case with the fitted shape distribution, the behavior of the error for Sil is opposite to that of the other particles. That is, Sil errors are small at all refractive indices with $m_{\rm i}=0.02$, and large at all small-to-medium imaginary refractive indices.

For the ensemble P_{12}/P_{11} , refractive indices with real parts larger than 1.45 and imaginary parts smaller than 0.01 produce good fits, with the error increasing only very moderately compared to that with $m_{\rm opt}$. Large imaginary refractive indices produce large errors, while small real refractive indices produce modest errors. Cal and Dol follow the behavior of the ensemble, while Agg and Sil differ from them, but agree with each other. Both Agg and Sil have the minimum error at small real refractive indices and large imaginary refractive indices, which is in stark contrast to the other particles. Moreover, the refractive indices that produce small errors for the ensemble, Cal and Dol, produce large errors for Agg and Sil.

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ← ►I

← ► Back Close

Printer-friendly Version

Full Screen / Esc



Discussion Paper

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



The $m_{\rm ont}$ of P_{22}/P_{11} for the ensemble lies at the maximum of the real axis and the minimum of the imaginary axis of the refractive index range used. The error increases smoothly as the refractive index goes further away from m_{opt} . High imaginary refractive indices produce large errors, whereas at low imaginary refractive indices almost every value of the real refractive index produces at most a modest error. Cal and Agg behave identically to the ensemble, but there are differences in the behaviors of Dol and Sil. Sil has the good-fit region of refractive indices at large real and small-to-medium imaginary refractive indices, like the ensemble, Cal and Dol, but the difference is that the refractive indices with the real part less than 1.5 produce large errors for Sil. Dol, on the other hand, has the optimum at minimum real and minimum imaginary refractive index. Large real and large imaginary parts of the refractive index are associated with large errors.

The P_{33}/P_{11} contour map is very similar to the free shape distribution case for the ensemble, the main difference being that the error gradient is even smoother. Cal, Dol and Agg all resemble the ensemble very closely. Sil, on the other hand, differs from both the other particles as well as the behavior of Sil in the free shape distribution case. The optimum refractive index for Sil is located at the maximum real and maximum imaginary refractive index. Additionally, whereas most of the near-optimum regions for the elements discussed so far have been convex, for Sil in this case the near-optimum region is concave. Effectively, the behavior and the contour map of Sil are yet again inverse to that of the other particles and the ensemble.

For P_{34}/P_{11} , large real refractive indices produce small errors independently of the imaginary part. Conversely, small real refractive indices cause the errors to be large, almost regardless of the imaginary part. Cal, Agg and Sil resemble the ensemble, but Dol is clearly different. For Dol, the optimum refractive index is found at the minimum of the real and at the maximum of the imaginary part of the refractive index. Unlike the other elements, the fitting error for Dol is not independent of the imaginary part of the refractive index, and both small real parts and large imaginary parts produce large errors.

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

 P_{44}/P_{11} resembles P_{33}/P_{11} very closely for the ensemble and all the particles, and is therefore not described separately.

Similarly to what was the case for the fitted shape distribution, P_{34}/P_{11} is the only element that is affected by roughening to a significant degree. Interestingly, the roughened version of Dol resembles the non-roughened versions of the other particles quite closely, and is therefore behaving almost oppositely to its own unroughened version. The behavior for P_{34}/P_{11} of Cal, which was greatly affected by roughening in the case the shape distribution was fitted and not uniform remains unaffected by roughening in the case of an uniform shape distribution.

3.3 Synthesis

From Figs. 3 and 4 and Tables 2 and 3, we see that in most cases $m_{\rm opt}$ deviates significantly from $m_{\rm true}$, the exact location depending on the element used for the retrieval. Furthermore, for several of the elements, $m_{\rm opt}$ varies greatly depending on the particle in question. Specifically, for almost all of the various particles and scattering matrix elements, $m_{\rm opt}$ is not close to $m_{\rm true}$ regardless of whether the ellipsoid shape distribution is a free parameter or a fixed constant. Additionally, most of the $m_{\rm opt}$ are at an extreme of either the real or the imaginary refractive index scales used in this study, which implies that even better fits might have been possible if the refractive index domain tested would have been wider. There are cases where $m_{\rm opt}$ is near the $m_{\rm true}$ value on either or both axes, but those seem to be exceptions. Moreover, the near-optimum regions can be very large, which can make the retrieved refractive index extremely sensitive to small changes in the target particle features, or measurement errors. This is exemplified in the text below.

When performing the analysis for particles with added artificial surface roughness, the results usually change only slightly (not shown). However, sometimes the results change dramatically, particularly for P_{34} . An example of a significant effect of roughening on the scattering error of the fitted shape distribution for P_{34} of Dol is shown in Fig. 5. Although there are similarities in the unroughened and roughened versions of

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

Back Close

Full Screen / Esc
Printer-friendly Version

Interactive Discussion



the error plots, there are also major differences. For example, $m_{\rm opt}$ for the roughened version produces the worst fit of all of the refractive indices for the original version.

Due to the large variability in the optima location for different elements and particles, performing the retrieval using a combination of different elements can yield a wide 5 variety of results, depending on the scaling and weighing of the error functions and individual scattering matrix elements. Most notably, in some cases almost any refractive index could be retrieved, were the weights or error definitions selected accordingly, because the individual m_{opt} cover most of the extremes of the studied refractive index space. This means that any weighing must be done with great care. The flexibility of the combined element retrievals is illustrated in Fig. 6, where we use two different error scaling scenarios for a retrieval using both P_{11} and P_{12} . In the first case, we simply use the sum of the error estimates of individual elements. This resembles the P_{11} case very closely, because P_{11} errors are larger and dominate the combined scattering error. In the second case, we scale the error ranges of each element to unity, and the retrieved refractive index changes significantly. The effect is even more pronounced if there are more than two scattering matrix elements involved, due to greater flexibility in the individual optima locations. Although there is a definite theoretical interest in seeing the results based on all six scattering matrix elements, we chose not to include the six-element analysis in this work, due to ambiguities related to the heavily varying individual optima locations, the limited refractive index range, and the sensitivity of such analysis to scaling

Figure 7, finally, shows the target particle scattering matrix elements P_{11} and P_{12} together with the ellipsoid fits based on $m_{\rm opt}$ and $m_{\rm true}$. We see that the $m_{\rm opt}$ fits are very good for the most part, which is yet another indication that ellipsoids really do form a very flexible base, and are capable of producing good fits to the scattering matrix elements for various irregularly shaped scatterers. However, the $m_{\rm true}$ fits are generally not nearly as good. The greater differences seen at large scattering angles of P_{11} are features of the logarithmic y axis; the absolute magnitudes of these errors are minuscule even though they look prominent in the figures. It should be noted that,

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Full Screen / Esc

Close

Back

Printer-friendly Version



Printer-friendly Version

Interactive Discussion



had our refractive index ranges been more extensive, some of the fits would likely have been even better, and the $m_{\rm opt}$ even further away from $m_{\rm true}$. However, it is evident that the true refractive index produces overall poor fits in many cases, and therefore the goodness of the fit is more of an evidence of the flexibility of the base and not of 5 any inherent physical representativity of the fitted ellipsoid ensembles to the original particle.

Based on these results, it seems that ellipsoids are not reliable in solving the inverse problem of retrieving the refractive index from scattering matrix data of irregular non-ellipsoidal particles, especially when using only individual elements. The retrieval results may be good in some cases for specific combinations of elements, but that appears to depend much on the details of the combination, and any combination that works in one case might not work in another. Ellipsoids do seem to provide good fits with the right parameters, but even better ones with wrong parameters. In fact, the good quality of the fits may actually give a misleading impression of the validity of ellipsoid fitting. However, it needs to be made clear that the ensemble used in this study is a small one, based on just three particles, without any abundance-dependent weighing. Ensembles containing a larger number of different particles, such is the case in the atmosphere, might yield different results.

Implications for radiative transfer

In addition to seeing the retrieval errors of refractive indices, it is interesting to know how the inaccurate retrievals translate into higher-level applications, such as radiative transfer simulations. To investigate this, we calculated the single-scattering albedo (ω) and the asymmetry parameter (g) for the fitted ellipsoid shape distributions of m_{opt} retrieved via each of the individual scattering matrix elements. The results, as well as the true parameter values calculated from the DDA particle ensemble, called REF in the text and figures below, are shown in Fig. 8. We see that apart from the retrieval based on P_{34}/P_{11} , the retrieved parameter values are reasonably well clumped together, especially with regards to the single-scattering albedo. However, this clumping can be

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.



misleading, since the REF values of the parameters are outside of the group on both axes: both the REF single-scattering albedo and the target asymmetry parameter are lower than those retrieved based on any of the scattering matrix elements, except for P_{34}/P_{11} . The retrieval based on P_{34}/P_{11} is a clear outlier, and is farther away from the target case on both axes than any of the others.

We next consider the aerosol radiative effects on the top-of-the atmosphere (TOA) and surface (SFC) net fluxes and atmospheric absorption (ATM), normalized by the downwelling solar flux F_{TOA}^{\downarrow} at TOA:

$$f_{\text{TOA}} = \frac{F_{\text{TOA}}^{\text{net}}(\text{aer}) - F_{\text{TOA}}^{\text{net}}(\text{no aer})}{F_{\text{TOA}}^{\downarrow}}$$

$$10 \quad f_{\text{SFC}} = \frac{F_{\text{SFC}}^{\text{net}}(\text{aer}) - F_{\text{SFC}}^{\text{net}}(\text{no aer})}{F_{\text{TOA}}^{\downarrow}},$$
(12)

$$f_{\rm SFC} = \frac{F_{\rm SFC}^{\rm net}(aer) - F_{\rm SFC}^{\rm net}(no\ aer)}{F_{\rm TOA}^{\downarrow}},\tag{13}$$

$$f_{\mathsf{ATM}} = f_{\mathsf{TOA}} - f_{\mathsf{SFC}} \tag{14}$$

Here F_{net} refers to the net (down – up) radiative flux either in the presence (aer) or absence (no aer) of the aerosol layer.

Two cases are contrasted: the REF case, for which $\omega = 0.9377$ and g = 0.6781, and the retrieval based on P11 (hereafter, the P11-fit), for which $\omega = 0.9881$ and q = 0.7082. Computations were done for the wavelength of $0.55 \,\mu\text{m}$, for mineral aerosol optical depths (AOD) ranging from 0.05 (background conditions) to 3 (a strong dust storm). While the mispresentation of aerosol shape might, in reality, also influence the AOD retrievals, it is assumed here that the AOD is identical for the REF and P_{11} -fit cases, so that the differences between them arise from ω and g only. Following Haapanala et al. (2012), the aerosol was placed in the lowest 3 km of a cloud-free tropical model atmosphere with water vapor reduced by 50 % compared to the standard tropical profile of Anderson et al. (1986). Two values were considered for the surface albedo, $\alpha_s = 0.07$ and $\alpha_s = 0.3$. Optical depths for gaseous absorption and Rayleigh scatter-

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.



Printer-friendly Version

Full Screen / Esc

Close

Back



Figure 9a–c shows f_{TOA} , f_{SFC} and f_{ATM} as a function of AOD, and Fig. 9d–f shows the corresponding fractional differences between the P_{11} -fit and REF cases. The cosine of solar zenith angle is fixed at $\mu_0 = 0.6$, but the main features were similar for other solar elevations as well. The following points can be made:

- 1. Due to the larger ω for the P_{11} -fit case, aerosol absorption is reduced dramatically, so that f_{ATM} is 71–76 % smaller than in the REF case (Fig. 9c and f).
- 2. The larger ω (i.e., reduced absorption) and larger g (i.e., reduced backward scattering) in the P_{11} -fit case both make the aerosol layer more transmissive (Fig. 9b and e). Consequently, $f_{\rm SFC}$ is 26–30 % (31–37 %) smaller than in the REF case for $\alpha_{\rm s}=0.07$ ($\alpha_{\rm s}=0.30$).
- 3. For f_{TOA} , the effects of larger ω and larger g in the P_{11} -fit case are compensatory. However, the former factor dominates, which results in a larger negative f_{TOA} (Fig. 9a and d). For a low surface albedo $\alpha_{\text{s}} = 0.07$, the difference to REF is small for low AOD (e.g., $\approx 5\,\%$ for AOD = 0.1) but it increases to nearly 40 % for AOD = 3. For a high surface albedo $\alpha_{\text{s}} = 0.30$, the differences are larger both in an absolute sense and (especially) in a relative sense, 120–200 %.

15

Overall, this example suggests that errors in refractive index arising from inaccurate shape assumptions in the retrieval scheme may result in very substantial errors in the single-scattering parameters (especially ω) and in the resulting aerosol radiative effects. The detailed results are, of course, sensitive to the actual retrieval algorithm used.

ACPD

Paper

Discussion Paper

Discussion Paper

Discussion Pape

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



In this work we investigated the reliability of the ellipsoid ensemble fitting for retrieving refractive indices of non-ellipsoidal model particles, with shapes retrieved from real dust particles via stereogrammetry. While it is known that ellipsoid ensembles can replicate the scattering of non-ellipsoidal particles closely, it is not known if such ensembles are linked to the microphysical properties of the target particles. That is, if an ellipsoid shape ensemble of a given refractive index fit the scattering data of a particle extremely closely, does it guarantee that the particle has the same refractive index? This is the implicit assumption that is made in various retrieval processes, but the validity has not been investigated thoroughly before.

This question was studied with a two-step process. First we performed fitting of the scattering matrix elements of ellipsoid ensembles of various refractive indices. Second, we investigated the relationships of the scattering errors of the best-fit ensembles and the deviation of the refractive index of this best-fit ensemble from the true refractive index of the target particle, which was known. As target particles we used individual stereogrammetric particles as well as a small ensemble of them. In addition to having the ellipsoid shape distribution as a free parameter, we investigated the scattering matrix element differences between the target particles and a uniform distribution of ellipsoid shapes.

Based on our results, ellipsoid fitting is not a reliable method for retrieving the true refractive index of non-ellipsoidal irregular particles, despite producing good fits to the scattering matrix elements. The retrieval based on error minimization found the true refractive index for only three cases out of 120 shown in Tables 2 and 3. In fact, the scattering error of the ellipsoids with the correct refractive index can be significantly higher than that of a wrong refractive index. This implies fundamental problems in modelling scattering properties of irregular particles by simplified model particles. Depending on which scattering matrix elements are used, the real and the imaginary part may be either smaller or larger compared to the true refractive index, and therefore the retrieved

Paper

Discussion Paper

Discussion Paper

Discussion Paper

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



refractive index can not be used even to restrict the estimate of the true refractive index from any direction. The retrieved refractive index acquired by using several matrix elements at once can be better than those of any individual elements, but that seems to be a case of several wrong solutions averaging to a decent one by pure chance. However, the validity of multi-element fitting can not be investigated reliably at this time due to the limited range of refractive indices in the ellipsoid database that does not cover all of the individual scattering matrix element optima.

When using the modified model particles with added surface roughness, the retrieval results are usually not affected much. Incidentally, the scattering errors increase, suggesting that ellipsoids do a poorer job at mimicking scattering by dust particles with added surface roughness. The retrieval of m works as poorly as for the original target particles. In some cases, though, the effect can be dramatic, such as the $m_{\rm opt}$ moving from one extreme of either of the refractive index axes to the other extreme. This indicates further difficulties in retrieving the refractive index of rough particles using smooth model particles.

Overall, it seems that the refractive index ranges selected were not completely sufficient to find the actual best-fit values, because most retrieved refractive indices were on edge of our complex refractive index space. However, the purpose of this study was not to find the refractive indices with the absolutely best match, but rather to investigate whether the refractive index can be retrieved from the angular dependence of scattering from irregular dust particles using simplified model particles.

The analysis results clearly show that the retrieval of m fails, regardless of whether the ellipsoidal shape distribution is fixed or allowed to vary. Further, the retrieved refractive indices depend on which element or element combinations are used, implying inconsistencies in the performance of ellipsoids. It thus seems that ellipsoids are ill-suited for refractive index retrieval of irregularly shaped non-ellipsoidal particles from light scattering data. Importantly, it was demonstrated that the resulting errors in single-scattering albedo and asymmetry parameter have the potential to produce major errors in computing the aerosol radiative effects.

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ◀ ▶I

Back

Close

Full Screen / Esc

Printer-friendly Version



Discussion Paper

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



When considering the practical implications of our findings, we must emphasize that few actual retrieval methods are based on an approach adapted here. Different instruments employ different types of measurement data, for example, and are thus differently vulnerable to the inconsistent performance of the ellipsoid model. Also, we only 5 considered cases with individual particles or a very small ensemble of three particles. Additionally, our target particles may not scatter light like real dust particles, even though their shapes are directly derived from those of real dust particles. Therefore, this study should not be taken as a proof that dust refractive index retrieval using ellipsoids does not work. Rather, this study should rather be considered a cautionary tale that hopefully encourages retrieval teams to test their algorithm with sufficiently realistic reference data. Yet, we need to emphasize that our retrieval tests were conducted under ideal conditions. We did not have any measurement errors, other external contributions to the "measured" radiation, and we automatically employed the correct size distribution. We note that size and refractive index often have similar effects on scattering, so retrieval of both the size and refractive index may give rise to even larger retrieval errors due to error compensation.

Based on our findings, it would be interesting to carry out similar investigation employing more complex model shapes for the retrieval. Unfortunately, the computational burden of such an investigation would be tremendous. One possible method to facilitate such a study is the shape matrix method by Petrov et al. (2006), which allows relatively fast computations for different refractive indices and sizes, once the shape-dependent shape matrix has been solved.

Acknowledgements. This research has been funded, in part, by the Academy of Finland (grant 255 718) and the Finnish Funding Agency for Technology and Innovation (Tekes; grant 25 3155/31/2009). Maxim Yurkin is acknowledged for making his ADDA code publicly available (https://code.google.com/p/a-dda/). Additionally, we are grateful to Hannakaisa Lindqvist and Zhaokai Meng for providing the stereogrammetric shapes and the ellipsoid database, respectively. Both the ellipsoid and the DDA data are available on request via the lead author (osku.kemppinen@fmi.fi).

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page **Abstract** Introduction Conclusions References **Tables Figures** Back Close

5 Bi, L., Yang, P., Kattawar, G., and Kahn, R.: Single-scattering properties of triaxial ellipsoidal particles for a size parameter range from the Rayleigh to geometric-optics regimes, Appl. Optics, 48, 114-126, 2009, 16863

Draine, B. T. and Flatau, P. J.: Discrete-dipole approximation for scattering calculations, J. Opt. Soc. Am. A, 11, 1491–1499, 1994, 16863

Dubovik, O., Sinyak, A., Lapyonok, T., Holben, B. N., Mishchenko, M., Yang, P., Eck, T. F., Volten, H., Muñoz, O., Veihelmann, B., van der Zande, W. J., Leon, J.-F., Sorokin, M., and Slutsker, I.: Application of spheroid models to account for aerosol particle nonsphericity in remote sensing of desert dust, J. Geophys. Res., 111, D11208, doi:10.1029/2005JD006619, 2006. 16863

Durant, A., Harrison, S., Watson, I., and Balkanski, Y.: Sensitivity of direct radiative forcing by mineral dust to particle characteristics, Prog. Phys. Geog., 33, 80-102, 2009. 16863

Freidenreich, S. M. and Ramaswamy, V.: A new multiple-band solar radiative parameterization for general circulation models, J. Geophys. Res., 104, 31389-31409, doi:10.1029/1999JD900456, 1999. 16882

Haapanala, P., Räisänen, P., Kahnert, M., and Nousiainen, T.: Sensitivity of the shortwave radiative effect of dust on particle shape: comparison of spheres and spheroids, J. Geophys. Res., 117, D08201, doi:10.1029/2011JD017216, 2012. 16881

Haywood, J. M., Johnson, B. T., Osborne, S. R., Mulcahy, J., Brooks, M. E., Harrison, M. A. J., Milton, S. F., and Brindleye, H. E.: Observations and modelling of the solar and terrestrial radiative effects of Saharan dust: a radiative closure case-study over oceans during the GERBILS campaign, Q. J. Rov. Meteor. Soc., 137, 1211-1226, doi:10.1002/gi.770, 2011. 16863

Henyey, L. G. and Greenstein, J. L.: Diffuse radiation in the galaxy, Astrophys. J., 93, 70–83, 1941. 16882

30 Hovenier, J. and van der Mee, C.: Basic relationships for matrices describing scattering by small particles, in: Light Scattering by Nonspherical Particles, edited by: Mishchenko, M. I., Hovenier, J. W., and Travis, L. D., Academic Press, San Diego, chap. 3, 61-85, 2000, 16866

Discussion

Paper

Discussion

Paper

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.

Title Page

Abstract

Conclusions

Tables

Back

Discussion Paper

Discussion Paper



Introduction

References

Figures

Full Screen / Esc

Printer-friendly Version

Interactive Discussion



O. Kemppinen et al.

- - Printer-friendly Version

Full Screen / Esc

- Interactive Discussion
 - © O

- Kahnert, F. M., Stamnes, J. J., and Stamnes, K.: Using simple particle shapes to model the Stokes scattering matrix of ensembles of wavelength-sized particles with complex shapes: possibilities and limitations, J. Quant. Spectrosc. Ra., 74, 167–182, 2002. 16870
- Kemppinen, O., Nousiainen, T., and Lindqvist, H.: The impact of surface roughness on scattering by realistically shaped wavelength-scale dust particles, J. Quant. Spectrosc. Ra., 150, 55–67, doi:10.1016/j.jqsrt.2014.05.024, 2015. 16867
- Lindqvist, H., Jokinen, O., Kandler, K., Scheuvens, D., and Nousiainen, T.: Single scattering by realistic, inhomogeneous mineral dust particles with stereogrammetric shapes, Atmos. Chem. Phys., 14, 143–157, doi:10.5194/acp-14-143-2014, 2014. 16864, 16867
- Meng, Z., Yang, P., Kattawar, G., Bi, L., Liou, K., and Laszlo, I.: Single-scattering properties of tri-axial ellipsoidal mineral dust aerosols: A database for application to radiative transfer calculations, J. Aerosol Sci., 41, 501–512, doi:10.1016/j.jaerosci.2010.02.008, 2010. 16863, 16869
- Merikallio, S., Lindqvist, H., Nousiainen, T., and Kahnert, M.: Modelling light scattering by mineral dust using spheroids: assessment of applicability, Atmos. Chem. Phys., 11, 5347–5363, doi:10.5194/acp-11-5347-2011, 2011. 16864, 16870
- Merikallio, S., Nousiainen, T., Kahnert, M., and Harri, A.-M.: Light scattering by the Martian dust analog, palagonite, modeled with ellipsoids, Opt. Express, 21, 17972–17985, doi:10.1364/OE.21.017972, 2013. 16863, 16869
- Mishchenko, M. I., Travis, L. D., Kahn, R. A., and West, R. A.: Modeling phase functions for dustlike tropospheric aerosols using a shape mixture of randomly oriented polydisperse spheroids, J. Geophys. Res., 102, 16831–16847, 1997. 16863
 - Muñoz, O., Moreno, F., Guirado, D., Ramos, L., López, A., Girela, F., Jerónimo, J., Costillo, L., and Bustamante, I.: Experimental determination of scattering matrices of dust particles at visible wavelengths: The IAA light scattering apparatus, J. Quant. Spectrosc. Ra., 111, 187–196, 2010. 16866
 - Nousiainen, T. and Kandler, K.: Light scattering by atmospheric mineral dust particles, in: Light Scattering Reviews 9, edited by: Kokhanovsky, A. A., Springer Praxis Books, Springer, Berlin, Heidelberg, 3–52, doi:10.1007/978-3-642-37985-7, 2015. 16863, 16864, 16866
- Nousiainen, T., Zubko, E., Niemi, J. V., Kupiainen, K., Lehtinen, M., Muinonen, K., and Videen, G.: Single-scattering modeling of thin, birefringent mineral dust flakes using the discrete-dipole approximation, J. Geophys. Res., 114, D07207, doi:10.1029/2008JD011564, 2009. 16863

- ACPD
 - 15, 16861–16900, 2015
 - Refractive Index Retrieval via Ellipsoids
 - O. Kemppinen et al.
 - Title Page

 Abstract Introduction

 Conclusions References

 Tables Figures

 I

 I

 I

 Back Close

 Full Screen / Esc
 - Printer-friendly Version
 - Interactive Discussion
 - © O

- Nousiainen, T., Kahnert, M., and Lindqvist, H.: Can particle shape information be retrieved from light-scattering observations using spheroidal model particles?, J. Quant. Spectrosc. Ra., 112, 2213–2225, doi:10.1016/j.jqsrt.2011.05.008, 2011. 16864, 16870
- Nousiainen, T., Zubko, E., Lindqvist, H., Kahnert, M., and Tyynelä, J.: Comparison of scattering by different nonspherical, wavelength-scale particles, J. Quant. Spectrosc. Ra., 113, 2391–2405, doi:10.1016/j.jgsrt.2012.03.032, 2012. 16864
- Penttilä, A., Zubko, E., Lumme, K., Muinonen, K., Yurkin, M., Draine, B., Rahola, J., Hoekstra, A., and Shkuratov, Y.: Comparison between discrete dipole implementations and exact techniques, J. Quant. Spectrosc. Ra., 106, 417–436, 2007. 16863
- Petrov, D., Synelnyk, E., Shkuratov, Y., and Videen, G.: The T-matrix technique for calculations of scattering properties of ensembles of randomly oriented particles with different size, J. Quant. Spectrosc. Ra., 102, 85–110, 2006. 16885
 - Press, W. H., Teukolsky, S. A., Vetterling, W. T., and Flannery, B. P.: Numerical Recipes in FORTRAN, 2nd edn., Cambridge University Press, UK, 1992. 16871
- Purcell, E. M. and Pennypacker, C. R.: Scattering and absorption of light by nonspherical dielectric grains, Astrophys. J., 186, 705–714, 1973. 16868
- Stamnes, K., Tsay, S.-C., Wiscombe, W., and Jayaweera, K.: Numerically stable algorithm for discrete-ordinate-method radiative transfer in multiple scattering and emitting layered media, Appl. Optics, 27, 2502–2509, 1988. 16882
- Yurkin, M. A. and Hoekstra, A. G.: The discrete-dipole-approximation code ADDA: capabilities and known limitations, J. Quant. Spectrosc. Ra., 112, 2234–2247, 2011. 16863, 16868
- Zender, C. S., Bian, H., and Newman, D.: The mineral Dust Entrainment And Deposition (DEAD) model: description and 1990s dust climatology, J. Geophys. Res., 108, D14, doi:10.1029/2002JD002775, 2003. 16863
- Zubko, E., Petrov, D., Grynko, Y., Shkuratov, Y., Okamoto, H., Muinonen, K., Nousiainen, T., Kimura, H., Yamamoto, T., and Videen, G.: Validity criteria of the discrete dipole approximation, Appl. Optics, 49, 1267–1279, 2010. 16868
 - Zubko, E., Muinonen, K., Muñoz, O., Nousiainen, T., Shkuratov, Y., Sun, W., and Videen, G.: Light scattering by feldspar particles: comparison of model agglomerate debris particles with laboratory samples, J. Quant. Spectrosc. Ra., 131, 175–187, 2013. 16863

Table 1. Number of ellipsoids employed in the fits, and the scattering errors. The numbers shown are means across all 40 refractive indices and four individual particles plus the three-particle ensemble. An ellipsoid is counted as part of the ensemble if its relative weight is at least 0.1%.

Element	# of ell. in the ensemble, non-roughened ref. particle	# of ell. in the ensemble, roughened ref. particle
P_{11}^{fit}	4.57	4.72
P_{12}^{fit} P_{12}^{fit} P_{22}^{fit} P_{23}^{fit} P_{34}^{fit} P_{44}^{fit}	8.43	8.15
$P_{22}^{\overline{\text{fit}}}$	4.67	3.58
$P_{33}^{\overline{\mathrm{fit}}}$	6.32	5.29
$P_{34}^{\rm fit}$	8.41	8.06
P_{44}^{fit}	3.58	2.87
Element	E_{ij} ,	E_{ij} ,
	non-roughened ref. particle	roughened ref. particle
E ₁₁	1.9498	1.6635
E ₁₁ E ₁₂		
E_{12} E_{22}	1.9498	1.6635
E ₁₂ E ₂₂ E ₃₃	1.9498 0.0029	1.6635 0.0084
E_{12}^{-1}	1.9498 0.0029 0.0783	1.6635 0.0084 0.2250

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.



Printer-friendly Version

Interactive Discussion

Table 2. Complex refractive index errors for the fitted shape distribution.

Original particles						
Particle	P ₁₁	P_{12}/P_{11}	P_{22}/P_{11}	P_{33}/P_{11}	P_{34}/P_{11}	P_{44}/P_{11}
Ensemble	0.00 - i 0.0035	0.05 - i0.0030	0.00 - i 0.0035	-0.05 - i 0.0035	0.05 + i0.0060	-0.10 - <i>i</i> 0.0030
Cal	0.05 - i 0.0035	-0.05 + i0.0060	0.10 - i0.0035	-0.05 - i 0.0035	-0.10 - i0.0035	-0.10 - i0.0030
Dol	0.10 + <i>i</i> 0.0010	0.05 + i0.0010	-0.05 + i0.0010	-0.10 + <i>i</i> 0.0010	0.05 + i0.0060	-0.10 - i0.0030
Agg	0.05 - i 0.0035	0.00 - i0.0030	0.10 - i0.0035	-0.10 - i0.0035	0.05 + i0.0160	-0.10 - /0.0035
Sil	0.10 + i0.0160	0.00 + i 0.0160	0.10 – <i>i</i> 0.0030	0.10 + <i>i</i> 0.0010	0.00 - / 0.0035	0.10 + /0.0160
Roughened particles						
Particle	P ₁₁	P_{12}/P_{11}	P_{22}/P_{11}	P_{33}/P_{11}	P_{34}/P_{11}	P_{44}/P_{11}
Ensemble	0.05 - i0.0020	0.05 + i0.0010	0.10 - /0.0035	-0.10 - /0.0035	0.10 + <i>i</i> 0.0060	-0.10 - /0.0035
Cal	0.05 - i 0.0035	-0.05 + i0.0060	0.10 - i0.0035	-0.10 - /0.0035	0.10 + <i>i</i> 0.0060	-0.10 - /0.0035
Dol	0.10 + <i>i</i> 0.0010	0.10 – <i>i</i> 0.0020	-0.10 - i0.0035	-0.10 + <i>i</i> 0.0010	0.10 + i0.0160	-0.10 - /0.0035
Agg	0.05 - i 0.0035	0.05 + i0.0010	0.10 - i0.0035	-0.10 - /0.0035	0.10 + i0.0160	-0.10 - /0.0035
Sil	-0.10 + i0.0160	-0.10 - <i>i</i> 0.0020	0.10 – i0.0030	0.10 + <i>i</i> 0.0040	0.00 - i0.0035	0.10 + <i>i</i> 0.0060

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Back Close

Full Screen / Esc

Printer-friendly Version



Table 3. Complex refractive index errors for the uniform shape distribution.

Original particles						
Particle	P_{11}	P_{12}/P_{11}	P_{22}/P_{11}	P_{33}/P_{11}	P_{34}/P_{11}	P_{44}/P_{11}
Ensemble	0.10 - /0.0035	0.00 + i0.0040	0.10 - /0.0035	-0.10 - /0.0035	0.10 – <i>i</i> 0.0030	-0.10 - /0.0035
Cal	0.10 - i0.0035	-0.05 + i0.0010	0.10 - i0.0035	-0.05 - i 0.0035	0.10 - i0.0035	-0.10 - /0.0035
Dol	0.10 - i0.0035	0.10 - i0.0035	-0.10 - i0.0035	-0.10 - i0.0035	-0.10 + i0.0160	-0.10 - /0.0035
Agg	0.00 - i0.0020	-0.05 + i 0.0160	0.10 - i0.0035	0.00 + i0.0000	0.10 + i0.0160	-0.10 - /0.0035
Sil	0.10 + i0.0160	-0.10 + /0.0160	0.10 + <i>i</i> 0.0000	0.10 + i0.0160	0.10 + i0.0160	0.10 + i0.0160
Roughened particles						
Particle	P ₁₁	P_{12}/P_{11}	P_{22}/P_{11}	P_{33}/P_{11}	P_{34}/P_{11}	P_{44}/P_{11}
Ensemble	0.10 – <i>i</i> 0.0020	0.05 + i0.0010	0.10 - /0.0035	-0.10 - /0.0035	0.10 + /0.0160	-0.10 - /0.0035
Cal	0.10 – <i>i</i> 0.0020	-0.05 + i0.0010	0.10 - i0.0035	-0.10 - /0.0035	0.10 + i0.0160	-0.10 - /0.0035
Dol	0.10 - i0.0035	0.10 - i0.0035	-0.10 - /0.0035	-0.10 - /0.0035	0.10 + i0.0160	-0.10 - /0.0035
Agg	0.00 + i0.0000	-0.05 + i0.0160	0.10 - i0.0035	-0.05 - i 0.0035	0.10 + i0.0160	-0.10 - i0.0035
Sil	0.10 + i0.0160	-0.10 + /0.0160	0.10 - i0.0035	0.10 + i0.0160	0.10 + i0.0160	0.10 + /0.0160

ACPD

15, 16861-16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page				
Abstract	Introduction			
Conclusions	References			
Tables	Figures			
	►I			

Close

Full Screen / Esc

Back

Printer-friendly Version



Sil

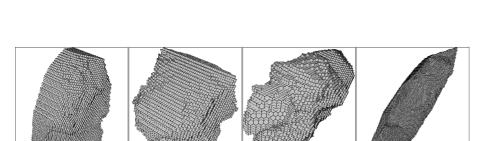


Figure 1. Renders of the DDA representations of the four target particles. The particles are depicted here with a 1/8th of the dipole resolution compared to the calculations.

Dol

Cal

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

I

Back Close

Full Screen / Esc



Printer-friendly Version



15, 16861-16900, 2015

Refractive Index Retrieval via **Ellipsoids**

ACPD

O. Kemppinen et al.







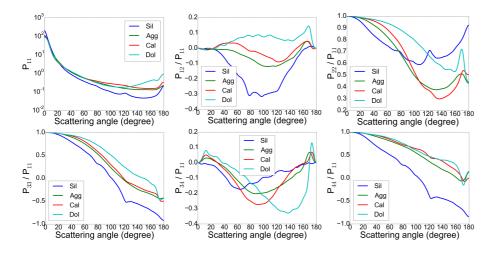


Figure 2. The six independent non-zero scattering matrix elements of the target particles integrated over the size distribution.

0.040

 $2 \cdot 10^{-2}$ 0.016

 4.10^{-3}

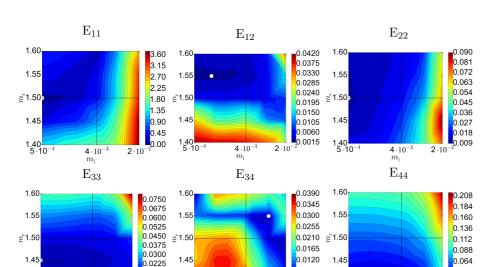


Figure 3. Scattering error E_{ij} for different scattering matrix elements for the particle ensemble of Cal, Dol and Agg, when the ellipsoid shape weights are treated as free parameters to be fitted.

 4.10^{-3}

0.0150 0.0075 2·10⁻²

1.40 5·10⁻⁴

 4.10^{-3}

1.40 5·10⁻⁴ 0.0075

0.0030

 $2 \cdot 10^{-2}$

1.40 5·10⁻⁴

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Printer-friendly Version





15, 16861-16900, 2015

ACPD

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.



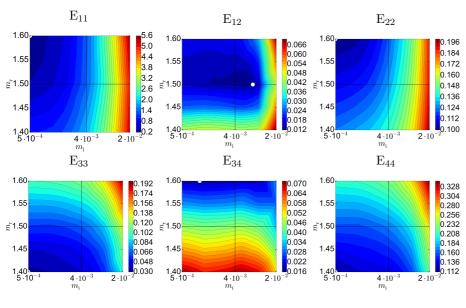


Figure 4. Scattering error E_{ii} for different scattering matrix elements for the particle ensemble of Cal, Dol and Agg, when the ellipsoid shape distribution is fixed to be uniform, with equal weights for each shape.

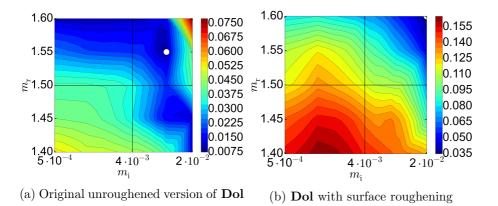


Figure 5. Illustration of the effect of roughening on P_{34} of Dol. The added modest surface roughness in panel **(b)** changes the behavior of the scattering error as function of the refractive index dramatically.

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I ✓ ►I

Back Close

Full Screen / Esc

Printer-friendly Version



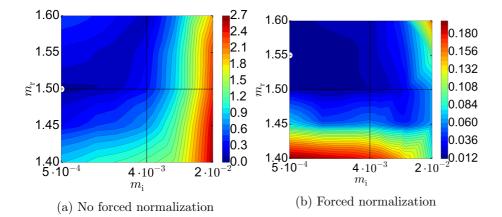


Figure 6. Illustration of two combined P_{11} and P_{12} normalization scenarios for the particle ensembles. Panel **(a)** shows the sum the individual E_{ij} directly such as they are, while panel **(b)** the individual errors are first scaled in such a way that the error range of each element is the same, unity. The behavior of scattering error depends greatly on how the components of the multi-element errors are weighted.

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version



Discussion Paper



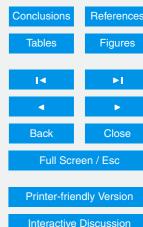
15, 16861-16900, 2015

ACPD

Refractive Index Retrieval via **Ellipsoids**

O. Kemppinen et al.





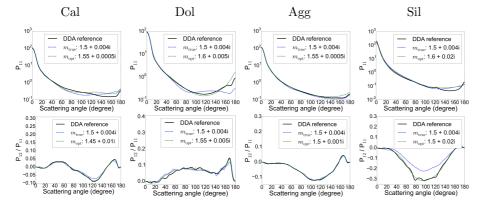


Figure 7. Target scattering matrix elements for P_{11} and P_{12}/P_{11} for the four individual particles as well as the best fits produced by the true refractive index (m_{true}) and the optimum refractive index (m_{opt}) ellipsoid bases.



15, 16861-16900, 2015

Refractive Index Retrieval via **Ellipsoids**

ACPD

O. Kemppinen et al.



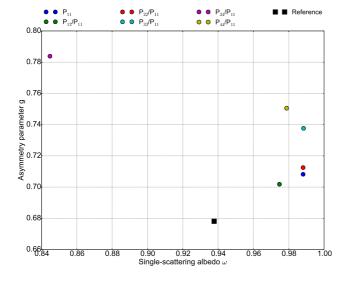


Figure 8. Variability of single-scattering albedo and asymmetry parameter when the retrieval is based on fitting the ellipsoid shape distribution to individual scattering matrix elements of the particle ensemble. The true values of these parameters for the particle ensemble are also shown for reference.

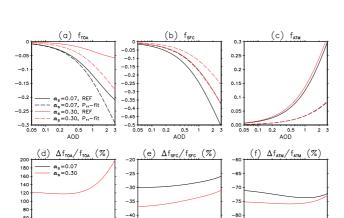


Figure 9. (a–c) Normalized aerosol radiative effects (Eqs. 12–14) for the REF (solid lines) and P_{11} -fit cases (dashed lines), for surface albedos of $\alpha_s = 0.07$ (black) and $\alpha_s = 0.30$ (red). **(d–f)** Corresponding relative differences (in %) between the P_{11} -fit and REF cases.

0.5

0.05 0.1 0.2

0.05 0.1 0.2 0.5 AOD -85

ACPD

15, 16861–16900, 2015

Refractive Index Retrieval via Ellipsoids

O. Kemppinen et al.

Title Page

Abstract Introduction

Conclusions References

Tables Figures

I

I

I

I

Back Close

Full Screen / Esc

Printer-friendly Version

